

Will it Rain Tomorrow in Australia?

2023-07-15

Import R Libraries

```
library(corrplot)
```

```
## corrplot 0.92 loaded
```

```
library(ggplot2)
```

```
library(caret)
```

```
## Loading required package: lattice
```

```
library(magrittr)
```

```
library(gridExtra)
```

```
library(scales)
```

```
library(DMwR2)
```

```
## Registered S3 method overwritten by 'quantmod':
```

```
##   method             from
```

```
##   as.zoo.data.frame zoo
```

```
library(UBL)
```

```
## Loading required package: MBA
```

```
## Loading required package: gstat
```

```
## The legacy packages mapproj, rgdal, and rgeos, underpinning this package
```

```
## will retire shortly. Please refer to R-spatial evolution reports on
```

```
## https://r-spatial.org/r/2023/05/15/evolution4.html for details.
```

```
## This package is now running under evolution status 0
```

```
## Loading required package: automap
```

```
## Loading required package: sp
```

```
## Loading required package: randomForest
```

```
## randomForest 4.7-1.1
```

```
## Type rfNews() to see new features/changes/bug fixes.
```

```
##
```

```
## Attaching package: 'randomForest'
```

```
## The following object is masked from 'package:gridExtra':
```

```
##
```

```
##   combine
```

```
## The following object is masked from 'package:ggplot2':
```

```
##
```

```
##   margin
```

```

library(caret)
library(MASS)
library(ipred)
library(rsample)
library(mlr)

## Loading required package: ParamHelpers

## Warning message: 'mlr' is in 'maintenance-only' mode since July 2019.
## Future development will only happen in 'mlr3'
## (<https://mlr3.ml-org.com>). Due to the focus on 'mlr3' there might be
## uncaught bugs meanwhile in {mlr} - please consider switching.

##
## Attaching package: 'mlr'

## The following object is masked from 'package:caret':
##
##      train

library(knitr)
library(glmnet)

## Loading required package: Matrix

## Loaded glmnet 4.1-7

library(outliers)

##
## Attaching package: 'outliers'

## The following object is masked from 'package:randomForest':
##
##      outlier

library(class)

```

Download the Rain Dataset

We downloaded the Rain Australia dataset as a CSV from the following link: <https://www.kaggle.com/datasets/jsphyg/weather-dataset-rattle-package/code?datasetId=6012&searchQuery=visual>. The dataset is originally composed of 23 columns and 145,460 examples. The aim of the data is to use available information about today's weather, i.e. Temperature, Humidity, Pressure, to predict whether it will rain tomorrow. Therefore, we originally start with 22 features and 1 target variable, RainTomorrow with binary classification (Yes=1, No=0).

```

file_path <- "/Users/Sofia/Desktop/Rain_Australia/weatherAUS.csv"
rain <- read.csv(file_path)
head(rain)

```

```

##      Date Location MinTemp MaxTemp Rainfall Evaporation Sunshine WindGustDir
## 1 2008-12-01  Albury   13.4   22.9     0.6           NA         NA          W
## 2 2008-12-02  Albury    7.4   25.1     0.0           NA         NA         WNW
## 3 2008-12-03  Albury   12.9   25.7     0.0           NA         NA         WSW
## 4 2008-12-04  Albury    9.2   28.0     0.0           NA         NA          NE
## 5 2008-12-05  Albury   17.5   32.3     1.0           NA         NA          W
## 6 2008-12-06  Albury   14.6   29.7     0.2           NA         NA         WNW

```

```
##      WindGustSpeed WindDir9am WindDir3pm WindSpeed9am WindSpeed3pm Humidity9am
## 1           44         W      WNW           20           24           71
## 2           44        NNW      WSW           4           22           44
## 3           46         W      WSW          19           26           38
## 4           24         SE       E          11           9           45
## 5           41        ENE      NW           7           20           82
## 6           56         W       W          19           24           55
##      Humidity3pm Pressure9am Pressure3pm Cloud9am Cloud3pm Temp9am Temp3pm
## 1           22      1007.7      1007.1         8        NA      16.9      21.8
## 2           25      1010.6      1007.8        NA        NA      17.2      24.3
## 3           30      1007.6      1008.7        NA         2      21.0      23.2
## 4           16      1017.6      1012.8        NA        NA      18.1      26.5
## 5           33      1010.8      1006.0         7         8      17.8      29.7
## 6           23      1009.2      1005.4        NA        NA      20.6      28.9
##      RainToday RainTomorrow
## 1           No           No
## 2           No           No
## 3           No           No
## 4           No           No
## 5           No           No
## 6           No           No
```

```
summary(rain)
```

```
##      Date           Location           MinTemp           MaxTemp
## Length:145460      Length:145460      Min.   :-8.50      Min.   :-4.80
## Class :character    Class :character    1st Qu.: 7.60      1st Qu.:17.90
## Mode  :character    Mode  :character    Median :12.00      Median :22.60
##                                     Mean  :12.19      Mean  :23.22
##                                     3rd Qu.:16.90      3rd Qu.:28.20
##                                     Max.   :33.90      Max.   :48.10
##                                     NA's   :1485      NA's   :1261
##      Rainfall           Evaporation           Sunshine           WindGustDir
## Min.   : 0.000      Min.   : 0.00      Min.   : 0.00      Length:145460
## 1st Qu.: 0.000      1st Qu.: 2.60      1st Qu.: 4.80      Class :character
## Median : 0.000      Median : 4.80      Median : 8.40      Mode  :character
## Mean   : 2.361      Mean   : 5.47      Mean   : 7.61
## 3rd Qu.: 0.800      3rd Qu.: 7.40      3rd Qu.:10.60
## Max.   :371.000      Max.   :145.00      Max.   :14.50
## NA's   :3261        NA's   :62790      NA's   :69835
##      WindGustSpeed      WindDir9am      WindDir3pm      WindSpeed9am
## Min.   : 6.00      Length:145460      Length:145460      Min.   : 0.00
## 1st Qu.: 31.00      Class :character    Class :character    1st Qu.: 7.00
## Median : 39.00      Mode  :character    Mode  :character    Median : 13.00
## Mean   : 40.03
## 3rd Qu.: 48.00
## Max.   :135.00
## NA's   :10263
##                                     Mean   : 14.04
##                                     3rd Qu.: 19.00
##                                     Max.   :130.00
##                                     NA's   :1767
##      WindSpeed3pm      Humidity9am      Humidity3pm      Pressure9am
## Min.   : 0.00      Min.   : 0.00      Min.   : 0.00      Min.   : 980.5
## 1st Qu.:13.00      1st Qu.: 57.00      1st Qu.: 37.00      1st Qu.:1012.9
## Median :19.00      Median : 70.00      Median : 52.00      Median :1017.6
## Mean   :18.66      Mean   : 68.88      Mean   : 51.54      Mean   :1017.6
## 3rd Qu.:24.00      3rd Qu.: 83.00      3rd Qu.: 66.00      3rd Qu.:1022.4
## Max.   :87.00      Max.   :100.00      Max.   :100.00      Max.   :1041.0
```



```
head(rain)
```

```
##      MinTemp MaxTemp Rainfall Evaporation Sunshine WindGustSpeed WindSpeed9am
## 6050    17.9    35.2      0      12.0      12.3          48             6
## 6051    18.4    28.9      0      14.8      13.0          37            19
## 6053    19.4    37.6      0      10.8      10.6          46            30
## 6054    21.9    38.4      0      11.4      12.2          31             6
## 6055    24.2    41.0      0      11.2       8.4          35            17
## 6056    27.1    36.1      0      13.0       0.0          43             7
##      WindSpeed3pm Humidity9am Humidity3pm Pressure9am Pressure3pm Cloud9am
## 6050             20          20          13      1006.3      1004.4         2
## 6051             19          30           8      1012.9      1012.1         1
## 6053             15          42          22      1012.3      1009.2         1
## 6054              6          37          22      1012.7      1009.1         1
## 6055             13          19          15      1010.7      1007.4         1
## 6056             20          26          19      1007.7      1007.4         8
##      Cloud3pm Temp9am Temp3pm RainToday RainTomorrow
## 6050         5    26.6    33.4          0           0
## 6051         1    20.3    27.0          0           0
## 6053         6    28.7    34.9          0           0
## 6054         5    29.1    35.6          0           0
## 6055         6    33.6    37.6          0           0
## 6056         8    30.7    34.3          0           0
```

```
rain <- as.data.frame(lapply(rain, as.numeric))
summary(rain)
```

```
##      MinTemp      MaxTemp      Rainfall      Evaporation
## Min.      :-6.70    Min.      : 4.10    Min.      : 0.00    Min.      : 0.000
## 1st Qu.: 8.60    1st Qu.:18.70    1st Qu.: 0.00    1st Qu.: 2.800
## Median :13.20    Median :23.90    Median : 0.00    Median : 5.000
## Mean   :13.46    Mean   :24.22    Mean   : 2.13    Mean   : 5.503
## 3rd Qu.:18.40    3rd Qu.:29.70    3rd Qu.: 0.60    3rd Qu.: 7.400
## Max.    :31.40    Max.    :48.10    Max.    :206.20    Max.    :81.200
##      Sunshine      WindGustSpeed      WindSpeed9am      WindSpeed3pm
## Min.      : 0.000    Min.      : 9.00    Min.      : 2.00    Min.      : 2.00
## 1st Qu.: 5.000    1st Qu.: 31.00    1st Qu.: 9.00    1st Qu.:13.00
## Median : 8.600    Median : 39.00    Median :15.00    Median :19.00
## Mean   : 7.736    Mean   : 40.88    Mean   :15.67    Mean   :19.79
## 3rd Qu.:10.700    3rd Qu.: 48.00    3rd Qu.:20.00    3rd Qu.:26.00
## Max.    :14.500    Max.    :124.00    Max.    :67.00    Max.    :76.00
##      Humidity9am      Humidity3pm      Pressure9am      Pressure3pm
## Min.      : 0.00    Min.      : 0.0    Min.      : 980.5    Min.      : 977.1
## 1st Qu.: 55.00    1st Qu.: 35.0    1st Qu.:1012.7    1st Qu.:1010.1
## Median : 67.00    Median : 50.0    Median :1017.2    Median :1014.7
## Mean   : 65.87    Mean   : 49.6    Mean   :1017.2    Mean   :1014.8
## 3rd Qu.: 79.00    3rd Qu.: 63.0    3rd Qu.:1021.8    3rd Qu.:1019.4
## Max.    :100.00    Max.    :100.0    Max.    :1040.4    Max.    :1038.9
##      Cloud9am      Cloud3pm      Temp9am      Temp3pm
## Min.      :0.000    Min.      :0.000    Min.      : -0.7    Min.      : 3.70
## 1st Qu.:1.000    1st Qu.:2.000    1st Qu.:13.1    1st Qu.:17.40
## Median :5.000    Median :5.000    Median :17.8    Median :22.40
## Mean   :4.242    Mean   :4.327    Mean   :18.2    Mean   :22.71
## 3rd Qu.:7.000    3rd Qu.:7.000    3rd Qu.:23.3    3rd Qu.:27.90
```

```
## Max. :8.000 Max. :9.000 Max. :39.4 Max. :46.10
## RainToday RainTomorrow
## Min. :0.0000 Min. :0.0000
## 1st Qu.:0.0000 1st Qu.:0.0000
## Median :0.0000 Median :0.0000
## Mean :0.2209 Mean :0.2203
## 3rd Qu.:0.0000 3rd Qu.:0.0000
## Max. :1.0000 Max. :1.0000
```

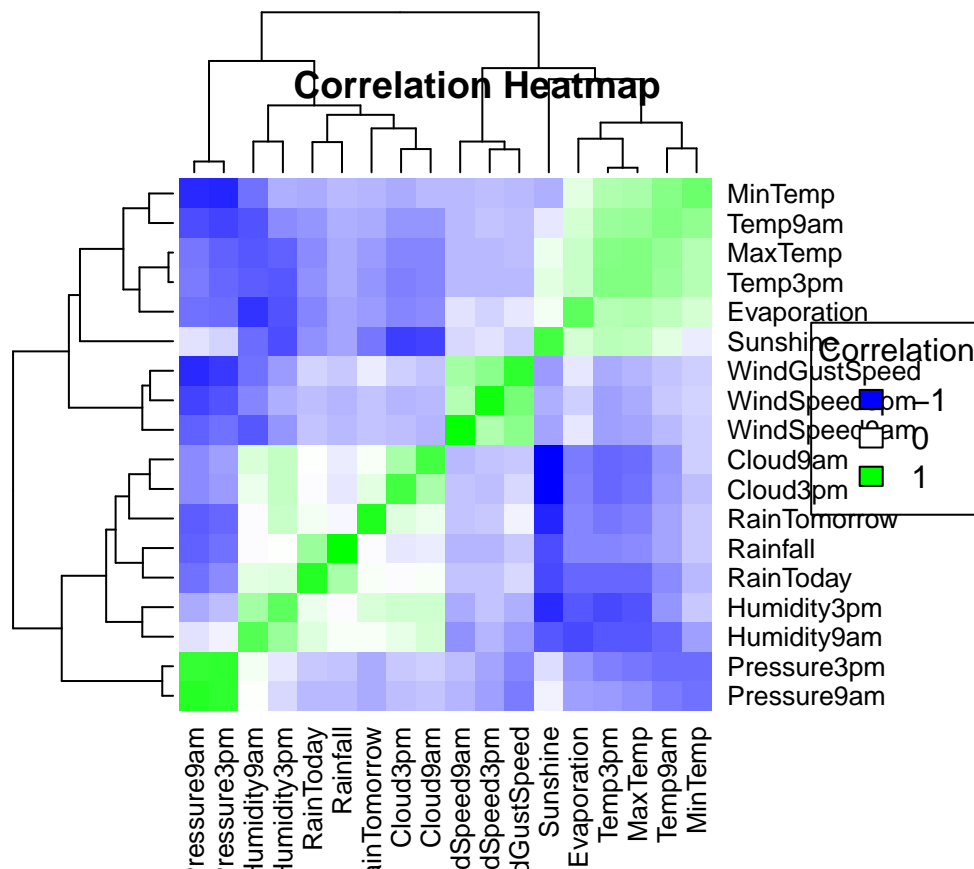
Correlation

```
# Build a Correlation Matrix
cor_matrix <- cor(rain)

# Create a heatmap from the correlation matrix with blue, white, and green color scheme
heatmap(cor_matrix, col = colorRampPalette(c("blue", "white", "green"))(100))

# Add a color legend to corr_matrix
legend_colors <- c("blue", "white", "green")
legend("right", legend = c(-1, 0, 1), fill = legend_colors, title = "Correlation")

# Add a main title
title(main = "Correlation Heatmap")
```

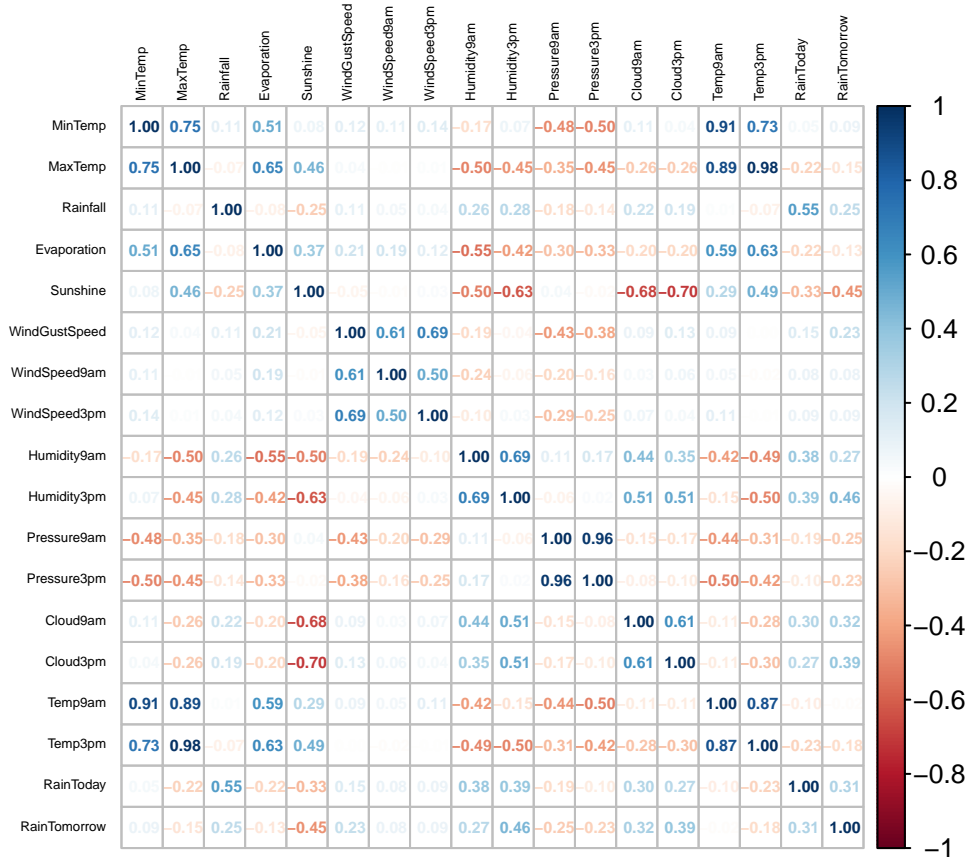


```
#Plot correlation matrix with numerical values
corrplot <- corrplot(cor(rain[, -19]),
```

```

method = "number",
diag = TRUE,
tl.cex = 0.4,
number.cex = 0.5,
tl.col = "black")

```



Density Plots

```
## Find features with highest correlation with target variable (RainTomorrow)
```

```

correlations <- cor_matrix['RainTomorrow',]
highly_correlated_columns <- correlations[abs(correlations) > 0.3 & correlations != 1]
column_names <- names(highly_correlated_columns)
print(column_names)

```

```
## [1] "Sunshine" "Humidity3pm" "Cloud9am" "Cloud3pm" "RainToday"
```

```
rain_subset <- rain[,c(column_names)]
```

```
# We are trying to visualize relationship between Target Variable, RainTomorrow with the features havin
```

```
# Calculate the count of each feature
```

```

count_rain_today <- sum(rain$RainToday == 1)
count_no_rain_today <- sum(rain$RainToday == 0)
count_rain_tomorrow <- sum(rain$RainTomorrow == 1)
count_no_rain_tomorrow <- sum(rain$RainTomorrow == 0)

```

```

# Create a data frame with the counts
count_df <- data.frame(
  Feature = c("RainToday", "RainTomorrow", "RainToday", "RainTomorrow"),
  Value = c("1", "1", "0", "0"),
  Count = c(count_rain_today, count_rain_tomorrow, count_no_rain_today, count_no_rain_tomorrow)
)

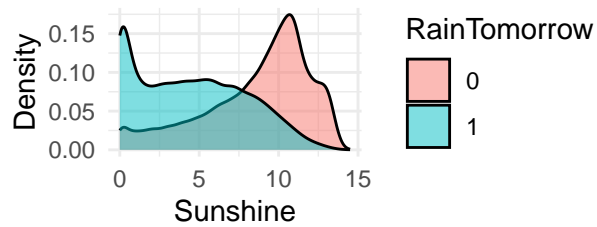
plot_list <- list()

for (col in column_names) {
  if (col == "RainToday") {
    # Plot the barplot
    bar_plot <- ggplot(count_df, aes(x = Value, y = Count, fill = Feature)) +
      geom_bar(stat = "identity", position = "dodge") +
      labs(x = "Feature", y = "Count", fill = "") +
      scale_fill_manual(values = c("red", "blue"), labels = c("RainToday", "RainTomorrow")) +
      theme_minimal()
    plot_list <- append(plot_list, list(bar_plot))
  }
  else {
    density_plot <- rain%>% ggplot(aes(x = .data[[col]] , fill = factor(RainTomorrow))) +
      geom_density(alpha = 0.5) +
      labs(x = col, y = "Density", fill = "RainTomorrow") +
      ggtitle(paste("Density Plot of ", col, "by Raintomorrow")) +
      theme_minimal() +
      theme(plot.title = element_text(hjust = 0.5, size = 10))
    plot_list <- append(plot_list, list(density_plot))
  }
}

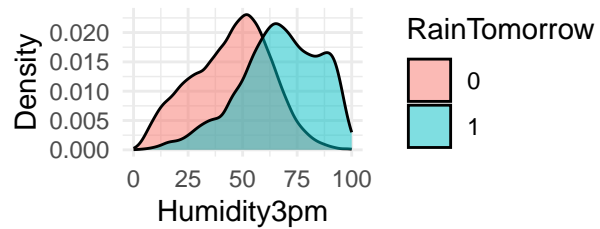
# Visualize density and bar plots
grid.arrange(grobs = plot_list, nrow = 3, ncol = 2)

```

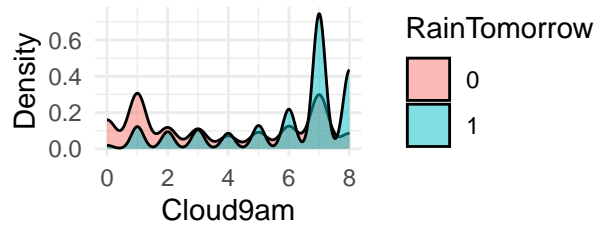

density Plot of Sunshine by Raintomorrow



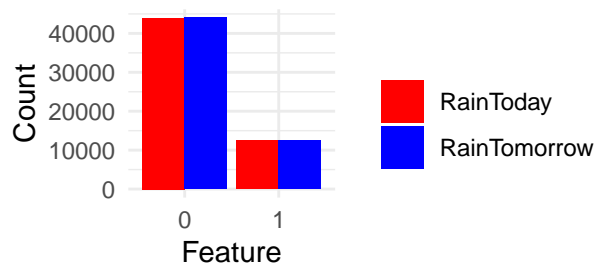
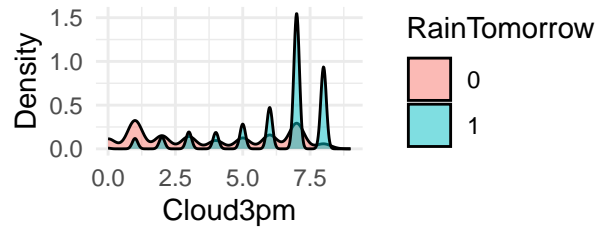
Density Plot of Humidity3pm by Raintomorrow



ensity Plot of Cloud9am by Raintomorrow



Density Plot of Cloud3pm by Raintomorrow



Sunshine: fraction of total days having higher sunshine record more 0 RainTomorrow, lower sunshine, m
Humidity3pm: overlap more but still higher humidity associated with 1 RainTomorrow and vice versa
#Cloud9am/Cloud3pm: oscillates a bit across x-axis with higher discrepancies between RainTomorrow value.
#RainToday: Since RainToday is a binary variable, the density plots are concentrated around 0 and 1. Wh

Feature Scaling

```
# Check distribution of RainTomorrow values to see how balanced the data is
# 0: 43993; 1: 12427
table(rain$RainTomorrow)
```

```
##
##      0      1
## 43993 12427
```

```
# Handling balancing of data below in train/test split
```

```
# Feature Scaling: Scale feature values using min/max scaling
min_max_norm <- function(x) {(x - min(x)) / (max(x) - min(x))}
```

```
rain_n <- as.data.frame(lapply(rain[,1:16], min_max_norm))
```

```
#Add back in Binary Features: RainToday and target variable, RainTomorrow
rain_n$RainToday <- rain$RainToday
rain_n$RainTomorrow <- rain$RainTomorrow
```

```
##First Logistic Regression Model: without balancing or feature selection
```

```

#Test/Train Split

#Set Seed for Reproducibility
set.seed(123)

# Set Training Set Size to 75% of Total Dataset
train0 <- sample(1:nrow(rain_n), nrow(rain_n) * 0.75)

# Calculate the test indices
test0 <- setdiff(1:nrow(rain_n), train0)

# Split the target variable into train and test sets
rain_n_train0 <- rain_n[train0,]
rain_n_test0 <- rain_n[test0 ,]

# Run GLM Logistic Regression Model using Training Set
glm_model0 <- glm(data = rain_n_train0,
  rain_n_train0$RainTomorrow ~ .,
  family = binomial)

# R squared and Variance Inflation Factor (VIF)

# R squared: Coefficient of Determination, gives the proportion of deviance explained by the model
# VIF: If the VIF value for a predictor variable is greater than 1, it indicates the presence of multicollinearity

model_summary0 <- summary(glm_model0)
summary(glm_model0)

##
## Call:
## glm(formula = rain_n_train0$RainTomorrow ~ ., family = binomial,
##      data = rain_n_train0)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -3.0778  -0.5047  -0.2791  -0.1248   3.1273
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)  -3.27671    0.21755 -15.062 < 2e-16 ***
## MinTemp      -1.75799    0.32913  -5.341 9.23e-08 ***
## MaxTemp       0.90140    0.60726   1.484 0.13771
## Rainfall      2.00857    0.50309   3.992 6.54e-05 ***
## Evaporation  -0.68500    0.55112  -1.243 0.21390
## Sunshine     -2.12269    0.10235 -20.739 < 2e-16 ***
## WindGustSpeed  7.07457    0.21145  33.458 < 2e-16 ***
## WindSpeed9am  -0.77965    0.15902  -4.903 9.44e-07 ***
## WindSpeed3pm  -2.14228    0.18900 -11.335 < 2e-16 ***
## Humidity9am    0.25419    0.18214   1.396 0.16285
## Humidity3pm    5.62834    0.19259  29.225 < 2e-16 ***
## Pressure9am    8.41492    0.56060  15.011 < 2e-16 ***
## Pressure3pm  -12.37656    0.58288 -21.233 < 2e-16 ***
## Cloud9am      -0.10464    0.06917  -1.513 0.13036
## Cloud3pm       0.99910    0.08537  11.703 < 2e-16 ***

```

```

## Temp9am          1.58034    0.50982    3.100    0.00194 **
## Temp3pm          -0.28768    0.65560   -0.439    0.66080
## RainToday        0.47364    0.04201   11.273 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 44559  on 42314  degrees of freedom
## Residual deviance: 28080  on 42297  degrees of freedom
## AIC: 28116
##
## Number of Fisher Scoring iterations: 6

r2_0 <- 1 - (model_summary0$deviance/model_summary0$null.deviance) # 0.3698141
vif0 <- 1/(1-r2_0) # 1.586833

#Predict test using glm model
glm_predict0 <- predict(glm_model0, rain_n_test0, type = "response")

#Convert predictions into 0,1 based on different thresholds

threshold4 <- 0.4
threshold5 <- 0.5
threshold6 <- 0.6

glm_predict_4_0<- ifelse(glm_predict0 > threshold4, 1, 0)
glm_predict_5_0<- ifelse(glm_predict0 > threshold5, 1, 0)
glm_predict_6_0<- ifelse(glm_predict0 > threshold6, 1, 0)

# Function to create a confusion matrix with F1 score, error and accuracy rate
# A confusion matrix is a table that is often used to evaluate the performance of a classification model

create_confusion_matrix <- function(confusion_matrix, threshold, error, accuracy) {
  # Extract the confusion matrix table
  cm_table <- as.data.frame(confusion_matrix$table)

  #Extract F1 score
  f1_score <- confusion_matrix$byClass["F1"]

  # Plot the confusion matrix using ggplot2
  ggplot(data = cm_table, aes(x = Reference, y = Prediction, fill = Freq)) +
    geom_tile(color = "white") +
    geom_text(aes(label = Freq), color = "black", size = 8) +
    scale_fill_gradient(low = "white", high = "steelblue") +
    labs(title = paste("Confusion Matrix for Threshold = ", threshold, "with F1-Score:", round(f1_score, 2)))
    theme_minimal() +
    theme(axis.text = element_text(size = 8),
          plot.title = element_text(size = 8, face = "bold"))
}

# Confusion matrix with threshold = 0.4
error4_0 <- mean(glm_predict_4_0!=rain_n_test0$RainTomorrow)

```

```

accuracy4_0 <- mean(glm_predict_4_0==rain_n_test0$RainTomorrow)
cm4_0 <- confusionMatrix(data = factor(glm_predict_4_0), reference = factor(rain_n_test0$RainTomorrow),

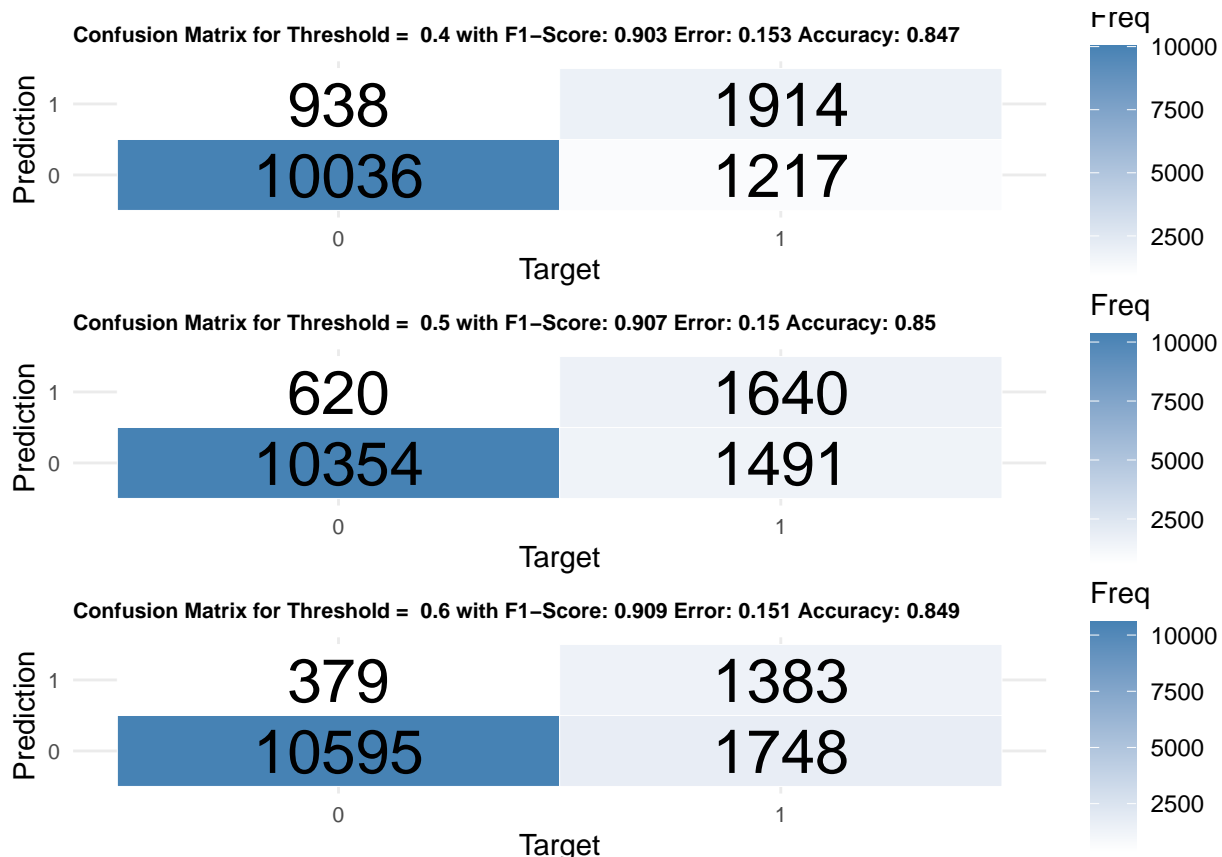
# Confusion matrix with threshold = 0.5
error5_0 <- mean(glm_predict_5_0!=rain_n_test0$RainTomorrow)
accuracy5_0 <- mean(glm_predict_5_0==rain_n_test0$RainTomorrow)
cm5_0 <- confusionMatrix(data = factor(glm_predict_5_0), reference = factor(rain_n_test0$RainTomorrow),

# Confusion matrix with threshold = 0.6
error6_0 <- mean(glm_predict_6_0!=rain_n_test0$RainTomorrow)
accuracy6_0 <- mean(glm_predict_6_0==rain_n_test0$RainTomorrow)
cm6_0 <- confusionMatrix(data = factor(glm_predict_6_0), reference = factor(rain_n_test0$RainTomorrow),

a0 <- create_confusion_matrix(cm4_0, 0.4, error4_0, accuracy4_0)
b0 <- create_confusion_matrix(cm5_0, 0.5, error5_0, accuracy5_0)
c0 <- create_confusion_matrix(cm6_0, 0.6, error6_0, accuracy6_0)

# Threshold of 0.05 is the best among thresholds in terms of accuracy, sensitivity, and specificity
cm_all0 = list(a0, b0, c0)
plot_width <- c(4, 4, 4)
grid.arrange(grobs = cm_all0, nrow = 3, width = plot_width)

```



Balancing ### The data extracted wasn't balanced, in which 0 was the majority class with over 40,000 and 1 had only about 12,000 samples. To account for this imbalance, we performed a method of downsampling, whereby we reduced the number of samples in the majority class (0) to the same number of samples of the minority class (1). This methodology may reduce the pool of data we have available, but it removes the bias in our model predictions toward one dominating class.

```

#Downsamples majority class(0)
#Added yname to specify the target variable in downSample function, ow it assumes first col is target
rain_balanced <- downSample(x = rain_n[, -which(names(rain_n) == "RainTomorrow")],
                             y = factor(rain_n$RainTomorrow),
                             yname = "RainTomorrow")
table(rain_balanced$RainTomorrow)

##
##      0      1
## 12427 12427

head(rain_balanced)

##      MinTemp    MaxTemp    Rainfall Evaporation    Sunshine WindGustSpeed
## 1 0.6692913 0.4409091 0.007759457 0.06896552 0.1172414 0.2608696
## 2 0.8661417 0.6772727 0.000000000 0.08374384 0.7034483 0.2260870
## 3 0.4094488 0.5204545 0.000000000 0.06403941 0.5931034 0.2434783
## 4 0.7086614 0.6750000 0.000000000 0.09852217 0.6275862 0.3565217
## 5 0.5301837 0.6795455 0.000000000 0.11822660 0.6275862 0.2782609
## 6 0.6141732 0.4886364 0.000000000 0.08128079 0.7103448 0.2782609
##      WindSpeed9am WindSpeed3pm Humidity9am Humidity3pm Pressure9am Pressure3pm
## 1 0.2307692 0.2432432 0.64 0.71 0.6494157 0.6521036
## 2 0.2000000 0.3513514 0.72 0.59 0.5358932 0.5129450
## 3 0.1076923 0.2702703 0.72 0.45 0.6961603 0.6618123
## 4 0.3076923 0.2297297 0.60 0.45 0.4741235 0.4854369
## 5 0.1076923 0.1486486 0.32 0.18 0.5225376 0.5339806
## 6 0.2615385 0.2297297 0.76 0.45 0.5409015 0.5679612
##      Cloud9am Cloud3pm Temp9am Temp3pm RainToday RainTomorrow
## 1 0.875 0.7777778 0.5810474 0.4363208 1 0
## 2 0.250 0.2222222 0.7605985 0.6816038 0 0
## 3 0.625 0.3333333 0.4738155 0.5188679 0 0
## 4 0.625 0.6666667 0.6832918 0.6698113 0 0
## 5 0.750 0.5555556 0.5960100 0.6297170 0 0
## 6 1.000 0.1111111 0.4588529 0.4740566 0 0

#Check if there are any NAs
sum(is.na(rain_balanced$RainTomorrow))

## [1] 0

```

Logistic Regression before Feature Selection

```

#Test/Train Split
set.seed(123)

train_balanced <- sample(1:nrow(rain_balanced), nrow(rain_balanced) * 0.75)

# Calculate the test indices
test_balanced <- setdiff(1:nrow(rain_balanced), train_balanced)

# Split the target variable into train and test sets
rain_balanced_train <- rain_balanced[train_balanced,]
rain_balanced_test <- rain_balanced[test_balanced,]
glm_model_balanced <- glm(data = rain_balanced_train,
                           rain_balanced_train$RainTomorrow ~ .,

```

```

    family = binomial)

#R squared and Variance Inflation Factor (VIF)
#If the VIF value for a predictor variable is greater than 1, it indicates the presence of multicollinearity
model_summary_balanced <- summary(glm_model_balanced)
summary(glm_model_balanced)

##
## Call:
## glm(formula = rain_balanced_train$RainTomorrow ~ ., family = binomial,
##      data = rain_balanced_train)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -3.5064  -0.6447   0.0516   0.6418   2.8163
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)  -1.78587    0.28387  -6.291 3.15e-10 ***
## MinTemp      -1.45819    0.41703  -3.497 0.000471 ***
## MaxTemp       1.04710    0.84911   1.233 0.217513
## Rainfall      1.47028    0.77973   1.886 0.059346 .
## Evaporation   -1.42725    0.70721  -2.018 0.043577 *
## Sunshine      -2.57528    0.13469 -19.119 < 2e-16 ***
## WindGustSpeed  6.91036    0.29248  23.627 < 2e-16 ***
## WindSpeed9am  -0.64221    0.21128  -3.040 0.002369 **
## WindSpeed3pm  -1.72241    0.25163  -6.845 7.65e-12 ***
## Humidity9am    0.19478    0.23371   0.833 0.404623
## Humidity3pm    5.68413    0.25584  22.217 < 2e-16 ***
## Pressure9am    8.31613    0.75726  10.982 < 2e-16 ***
## Pressure3pm   -12.46658    0.79195 -15.742 < 2e-16 ***
## Cloud9am      -0.27995    0.08624  -3.246 0.001169 **
## Cloud3pm       1.07058    0.10368  10.325 < 2e-16 ***
## Temp9am        0.49761    0.65435   0.760 0.446979
## Temp3pm        0.73571    0.89965   0.818 0.413484
## RainToday      0.46663    0.05825   8.011 1.14e-15 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 25840  on 18639  degrees of freedom
## Residual deviance: 15893  on 18622  degrees of freedom
## AIC: 15929
##
## Number of Fisher Scoring iterations: 5

r2_balanced <- 1 - (model_summary_balanced$deviance/model_summary_balanced$null.deviance) # 0.3849359
vif_balanced <- 1/(1-r2_balanced) # 1.625847

#Predict test with model
glm_predict_balanced <- predict(glm_model_balanced, rain_balanced_test, type = "response")

#Convert predictions into 0,1 based on different thresholds

```

```

glm_predict_4_balanced<- ifelse(glm_predict_balanced > threshold4, 1, 0)
glm_predict_5_balanced<- ifelse(glm_predict_balanced > threshold5, 1, 0)
glm_predict_6_balanced<- ifelse(glm_predict_balanced > threshold6, 1, 0)

# Confusion matrix with threshold = 0.4
table(rain_balanced_test$RainTomorrow, glm_predict_4_balanced)

##      glm_predict_4_balanced
##           0           1
##  0 2335    798
##  1   446   2635

error4_balanced <- mean(glm_predict_4_balanced!=rain_balanced_test$RainTomorrow)
accuracy4_balanced <- mean(glm_predict_4_balanced==rain_balanced_test$RainTomorrow)
cm4_balanced <- confusionMatrix(data = factor(glm_predict_4_balanced), reference = factor(rain_balanced_test$RainTomorrow))

# Confusion matrix with threshold = 0.5
table(rain_balanced_test$RainTomorrow, glm_predict_5_balanced)

##      glm_predict_5_balanced
##           0           1
##  0 2528    605
##  1   649   2432

error5_balanced <- mean(glm_predict_5_balanced!=rain_balanced_test$RainTomorrow)
accuracy5_balanced <- mean(glm_predict_5_balanced==rain_balanced_test$RainTomorrow)
cm5_balanced <- confusionMatrix(data = factor(glm_predict_5_balanced), reference = factor(rain_balanced_test$RainTomorrow))

# Confusion matrix with threshold = 0.6
table(rain_balanced_test$RainTomorrow, glm_predict_6_balanced)

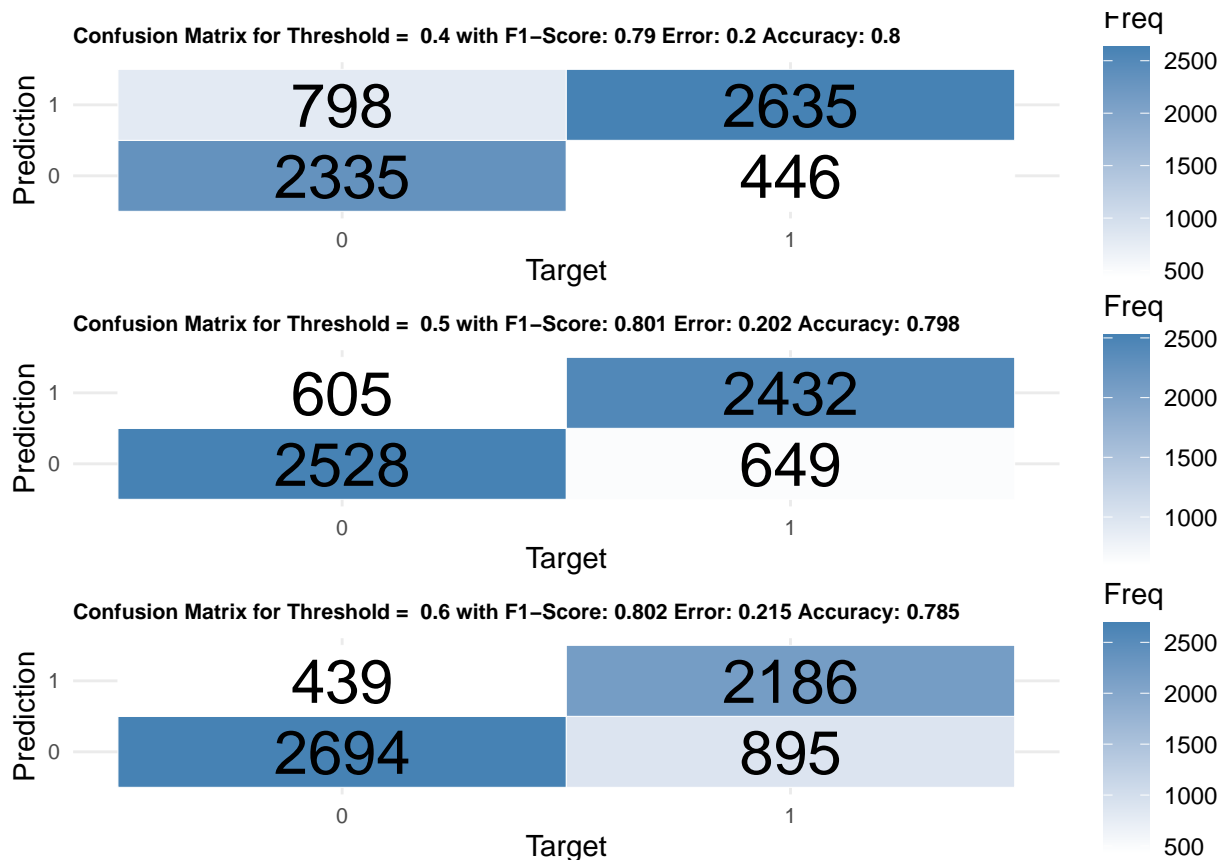
##      glm_predict_6_balanced
##           0           1
##  0 2694    439
##  1   895   2186

error6_balanced <- mean(glm_predict_6_balanced!=rain_balanced_test$RainTomorrow)
accuracy6_balanced <- mean(glm_predict_6_balanced==rain_balanced_test$RainTomorrow)
cm6_balanced <- confusionMatrix(data = factor(glm_predict_6_balanced), reference = factor(rain_balanced_test$RainTomorrow))

a_balanced <- create_confusion_matrix(cm4_balanced, 0.4, error4_balanced, accuracy4_balanced)
b_balanced <- create_confusion_matrix(cm5_balanced, 0.5, error5_balanced, accuracy5_balanced)
c_balanced <- create_confusion_matrix(cm6_balanced, 0.6, error6_balanced, accuracy6_balanced)

# Threshold of 0.5 is the best among thresholds in terms of accuracy, sensitivity, and specificity
cm_all_balanced = list(a_balanced, b_balanced, c_balanced)
plot_width <- c(4, 4, 4)
grid.arrange(grobs = cm_all_balanced, nrow = 3, width = plot_width)

```



Feature Selection (Backward Selection using BIC)

Perform logistic regression with backward stepwise selection

```
logit_model <- glm(rain_balanced$RainTomorrow ~ ., data = rain_balanced, family = binomial)
```

Perform forward stepwise selection using AIC with log(n)

```
logit_model <- stepAIC(logit_model, direction = "backward", k = log(nrow(rain_balanced)), trace = FALSE)
```

Print the summary of the logistic regression model

```
summary(logit_model)
```

##

Call:

```
## glm(formula = rain_balanced$RainTomorrow ~ MinTemp + MaxTemp +
##      Rainfall + Sunshine + WindGustSpeed + WindSpeed9am + WindSpeed3pm +
##      Humidity3pm + Pressure9am + Pressure3pm + Cloud9am + Cloud3pm +
##      RainToday, family = binomial, data = rain_balanced)
```

##

Deviance Residuals:

```
##      Min      1Q   Median      3Q      Max
## -3.5377 -0.6440 -0.0412  0.6411  2.8180
```

##

Coefficients:

```
##      Estimate Std. Error z value Pr(>|z|)
## (Intercept)  -1.63412    0.22495  -7.264 3.74e-13 ***
## MinTemp      -1.01052    0.24797  -4.075 4.60e-05 ***
## MaxTemp       1.39711    0.30809   4.535 5.77e-06 ***
## Rainfall      2.29815    0.69305   3.316 0.000913 ***
```



```
## Sunshine      -2.36985    0.11567 -20.488 < 2e-16 ***
## WindGustSpeed  7.04107    0.24971  28.197 < 2e-16 ***
## WindSpeed9am  -0.81429    0.17622  -4.621 3.82e-06 ***
## WindSpeed3pm  -1.98642    0.21483  -9.246 < 2e-16 ***
## Humidity3pm    5.76180    0.15339  37.562 < 2e-16 ***
## Pressure9am    8.78896    0.61661  14.254 < 2e-16 ***
## Pressure3pm   -13.07527    0.64902 -20.146 < 2e-16 ***
## Cloud9am      -0.25366    0.07282  -3.483 0.000495 ***
## Cloud3pm       1.11010    0.08919  12.447 < 2e-16 ***
## RainToday      0.47366    0.04919   9.629 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
## Null deviance: 34455 on 24853 degrees of freedom
## Residual deviance: 21168 on 24840 degrees of freedom
## AIC: 21196
##
## Number of Fisher Scoring iterations: 5
# Subset the dataframe with the chosen features based on stepwise selection
rain_subset <- rain_balanced[, c("MinTemp", "Sunshine", "WindGustSpeed", "WindSpeed9am", "WindSpeed3pm")

#Train/Test Split
set.seed(123)

train <- sample(1:nrow(rain_subset), nrow(rain_subset) * 0.75)

# Calculate the test indices
test <- setdiff(1:nrow(rain_subset), train)

# Split the target variable into train and test sets
rain_subset_train <- rain_subset[train,]
rain_subset_test <- rain_subset[test,]

head(rain_subset_train)

##      MinTemp  Sunshine WindGustSpeed WindSpeed9am WindSpeed3pm Humidity3pm
## 18847 0.4934383 0.3931034    0.3565217    0.10769231    0.2297297      0.71
## 18895 0.8188976 0.1931034    0.4869565    0.16923077    0.2432432      0.86
## 2986  0.6220472 0.2413793    0.4086957    0.33846154    0.4189189      0.18
## 1842  0.7034121 0.7793103    0.3391304    0.06153846    0.3513514      0.40
## 3371  0.4619423 0.4689655    0.1652174    0.16923077    0.2297297      0.27
## 11638 0.5170604 0.1448276    0.2086957    0.07692308    0.2702703      0.73
##      Pressure9am Pressure3pm Cloud9am  Cloud3pm  Temp3pm RainToday
## 18847  0.5392321  0.5841424    0.125 0.3333333 0.3537736      1
## 18895  0.4190317  0.4271845    0.875 0.8888889 0.5306604      1
## 2986   0.5592654  0.5695793    0.875 0.5555556 0.4811321      0
## 1842   0.5091820  0.4870550    0.250 0.3333333 0.6910377      0
## 3371   0.5876461  0.5776699    0.875 0.6666667 0.5070755      0
## 11638  0.6711185  0.7103560    0.625 0.8888889 0.3278302      1
##      RainTomorrow
## 18847           1
```

```
## 18895      1
## 2986       0
## 1842       0
## 3371       0
## 11638      0
```

```
head(rain_subset_test)
```

```
##      MinTemp  Sunshine WindGustSpeed WindSpeed9am WindSpeed3pm Humidity3pm
## 1  0.6692913 0.1172414    0.2608696    0.2307692    0.24324324      0.71
## 6  0.6141732 0.7103448    0.2782609    0.2615385    0.22972973      0.45
## 8  0.5433071 0.6827586    0.4173913    0.3384615    0.32432432      0.39
## 12 0.1863517 0.6413793    0.1304348    0.1076923    0.17567568      0.57
## 24 0.4881890 0.2000000    0.2086957    0.2307692    0.14864865      0.86
## 29 0.3569554 0.8758621    0.1913043    0.1692308    0.09459459      0.24
##      Pressure9am Pressure3pm Cloud9am  Cloud3pm   Temp3pm RainToday RainTomorrow
## 1    0.6494157    0.6521036    0.875 0.7777778 0.4363208          1          0
## 6    0.5409015    0.5679612    1.000 0.1111111 0.4740566          0          0
## 8    0.6093489    0.6682848    0.875 0.6666667 0.3844340          0          0
## 12   0.6627713    0.6423948    0.750 0.1111111 0.2948113          1          0
## 24   0.6544240    0.6100324    0.875 0.8888889 0.2735849          0          0
## 29   0.7412354    0.7103560    0.125 0.1111111 0.4599057          0          0
```

Selected Model

```
# Model Definition
```

```
glm_model <- glm(data = rain_subset_train,
  rain_subset_train$RainTomorrow ~ .,
  family = binomial)
```

```
#R squared and Variance Inflation Factor (VIF)
```

```
#If the VIF value for a predictor variable is greater than 1, it indicates the presence of multicollinearity
```

```
model_summary <- summary(glm_model)
summary(glm_model)
```

```
##
## Call:
## glm(formula = rain_subset_train$RainTomorrow ~ ., family = binomial,
##      data = rain_subset_train)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -3.5021  -0.6462   0.0540   0.6430   2.8063
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)  -1.73364    0.26519  -6.537 6.26e-11 ***
## MinTemp      -1.38220    0.30132  -4.587 4.49e-06 ***
## Sunshine     -2.57348    0.13375 -19.242 < 2e-16 ***
## WindGustSpeed  6.89157    0.28504  24.177 < 2e-16 ***
## WindSpeed9am  -0.74847    0.20273  -3.692 0.000222 ***
## WindSpeed3pm  -1.67831    0.24595  -6.824 8.87e-12 ***
## Humidity3pm    5.97653    0.19279  31.000 < 2e-16 ***
## Pressure9am    8.34452    0.73462  11.359 < 2e-16 ***
## Pressure3pm  -12.54847    0.77299 -16.234 < 2e-16 ***
```

```

## Cloud9am      -0.28562    0.08367   -3.414 0.000641 ***
## Cloud3pm      1.08002    0.10194   10.595 < 2e-16 ***
## Temp3pm       1.97120    0.37774    5.218 1.80e-07 ***
## RainToday     0.54230    0.04751   11.414 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
## Null deviance: 25840  on 18639  degrees of freedom
## Residual deviance: 15903  on 18627  degrees of freedom
## AIC: 15929
##
## Number of Fisher Scoring iterations: 5

r2 <- 1 - (model_summary$deviance/model_summary$null.deviance) # 0.3845522
vif <- 1/(1-r2) # 1.624833

#Predict test with model
glm_predict <- predict(glm_model, rain_subset_test, type = "response")

#Convert predictions into 0,1 based on different thresholds

glm_predict_4<- ifelse(glm_predict > threshold4, 1, 0)
glm_predict_5<- ifelse(glm_predict > threshold5, 1, 0)
glm_predict_6<- ifelse(glm_predict > threshold6, 1, 0)

# Confusion matrix with threshold = 0.4
table(rain_subset_test$RainTomorrow, glm_predict_4)

##      glm_predict_4
##      0      1
## 0 2338   795
## 1   444 2637

error4 <- mean(glm_predict_4!=rain_subset_test$RainTomorrow)
accuracy4 <- mean(glm_predict_4==rain_subset_test$RainTomorrow)
cm4 <- confusionMatrix(data = factor(glm_predict_4), reference = factor(rain_subset_test$RainTomorrow),

# Confusion matrix with threshold = 0.5
table(rain_subset_test$RainTomorrow, glm_predict_5)

##      glm_predict_5
##      0      1
## 0 2529   604
## 1   653 2428

error5 <- mean(glm_predict_5!=rain_subset_test$RainTomorrow)
accuracy5 <- mean(glm_predict_5==rain_subset_test$RainTomorrow)
cm5 <- confusionMatrix(data = factor(glm_predict_5), reference = factor(rain_subset_test$RainTomorrow),

# Confusion matrix with threshold = 0.6
table(rain_subset_test$RainTomorrow, glm_predict_6)

##      glm_predict_6
##      0      1

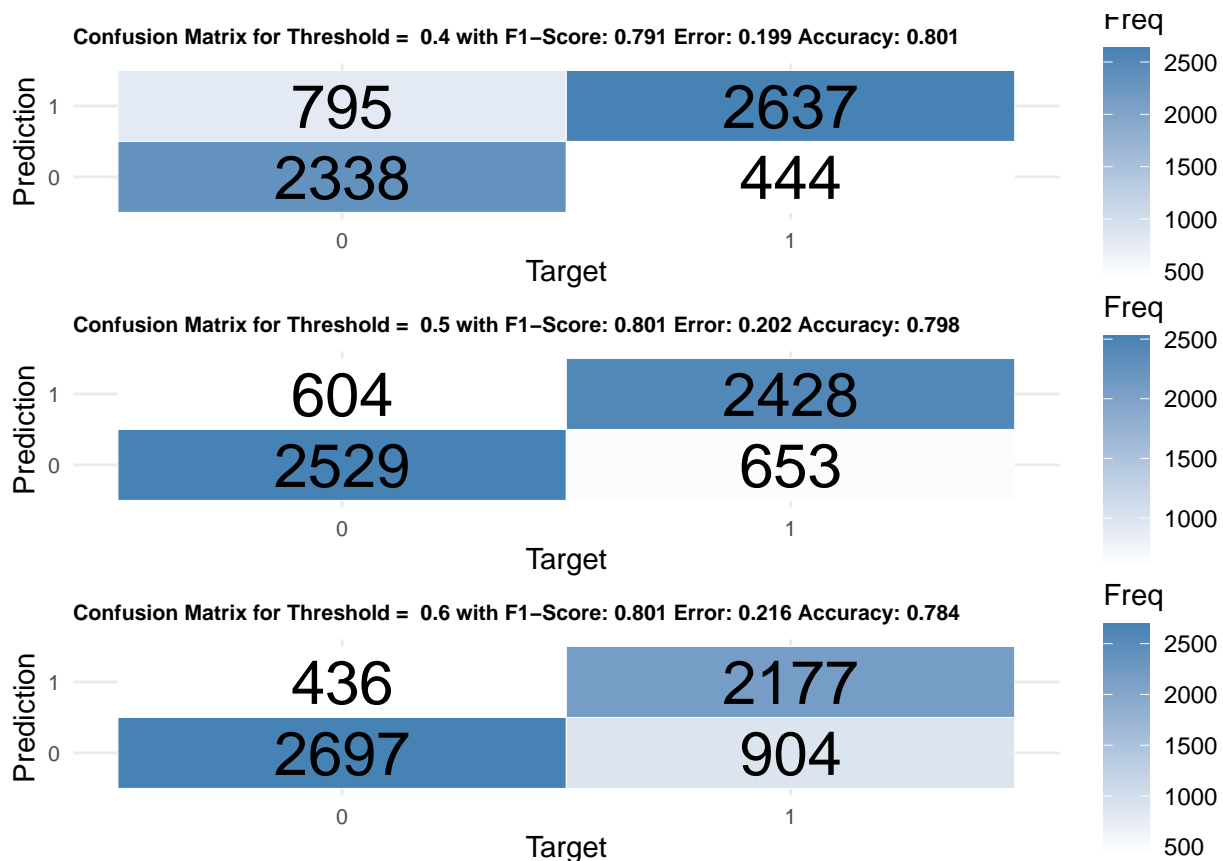
```

```
## 0 2697 436
## 1 904 2177

error6 <- mean(glm_predict_6!=rain_subset_test$RainTomorrow)
accuracy6 <- mean(glm_predict_6==rain_subset_test$RainTomorrow)
cm6 <- confusionMatrix(data = factor(glm_predict_6), reference = factor(rain_subset_test$RainTomorrow))

a <- create_confusion_matrix(cm4, 0.4, error4, accuracy4)
b <- create_confusion_matrix(cm5, 0.5, error5, accuracy5)
c <- create_confusion_matrix(cm6, 0.6, error6, accuracy6)

cm_all = list(a, b, c)
plot_width <- c(4, 4, 4)
grid.arrange(grobs = cm_all, nrow = 3, width = plot_width)
```



Comparison of 3 Models

Summary Statistics: F1-Score, Error, Accuracy

```
models <- c("Simple GLM", "GLM with Balancing", "GLM with Balancing and Feature Selection")
model_suffix <- c( "_0", "_balanced", "" )

thresholds <- c(4, 5, 6)
threshold_values <- c(0.4, 0.5, 0.6)

metrics <- data.frame(Model = character(), Threshold = numeric(), F1_Score = numeric(), Error = numeric(),
                        j <- 1)
```

```

for (model in models) {
  model_suff <- model_suffix[j]
  j <- j + 1
  for (i in 1:length(thresholds)) {
    threshold <- thresholds[i]
    threshold_value <- threshold_values[i]

    # Calculate the F1 score for each combination of model and threshold
    cm_name <- paste0("cm", threshold, model_suff)
    cm <- get(cm_name)
    f1_score <- cm$byClass["F1"]

    error_name <- paste0("error", threshold, model_suff)
    error <- get(error_name)

    accuracy_name <- paste0("accuracy", threshold, model_suff)
    accuracy <- get(accuracy_name)

    # Add the F1 score to the data frame
    metrics <- rbind(metrics, data.frame(Model = model, Threshold = threshold_value, F1_Score = f1_score,
                                          Error = error, Accuracy = accuracy))
  }
}

```

metrics

```

##           Model Threshold  F1_Score    Error
## 1           Simple GLM      0.4 0.9030458 0.1527827
## 2           Simple GLM      0.5 0.9074894 0.1496632
## 3           Simple GLM      0.6 0.9087790 0.1507976
## 4      GLM with Balancing      0.4 0.7896517 0.2001931
## 5      GLM with Balancing      0.5 0.8012678 0.2018024
## 6      GLM with Balancing      0.6 0.8015472 0.2146765
## 7 GLM with Balancing and Feature Selection      0.4 0.7905325 0.1993885
## 8 GLM with Balancing and Feature Selection      0.5 0.8009501 0.2022852
## 9 GLM with Balancing and Feature Selection      0.6 0.8010098 0.2156421
##      Accuracy
## 1 0.8472173
## 2 0.8503368
## 3 0.8492024
## 4 0.7998069
## 5 0.7981976
## 6 0.7853235
## 7 0.8006115
## 8 0.7977148
## 9 0.7843579

```

##Predictions

```

#for different features: mintemp an temp3pm
a00 <- ggplot(data = rain_n_test0 , aes(x = MinTemp,
y = Temp3pm,

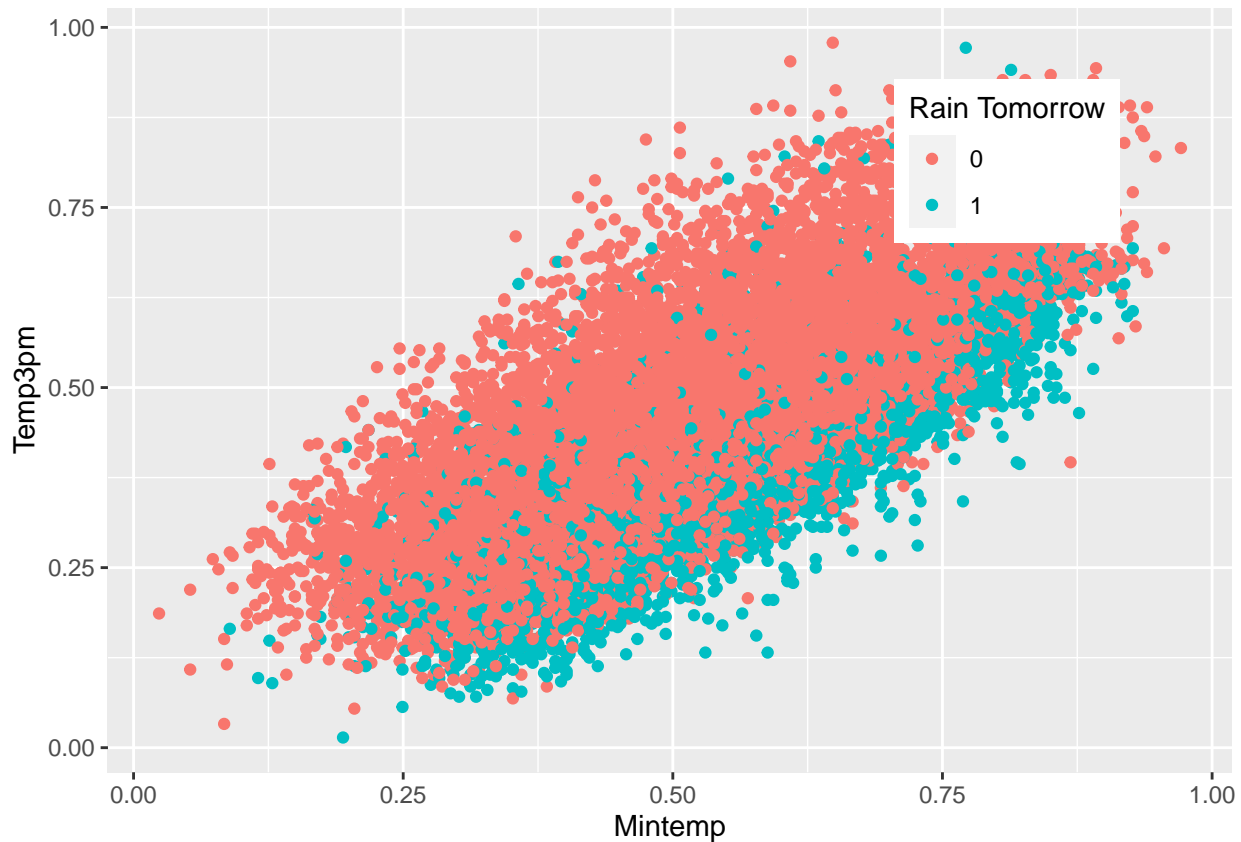
```

```

color= as.factor(RainTomorrow) )) +
geom_point()+
labs(x = "Mintemp",
y = "Temp3pm",
color = "Rain Tomorrow") +
theme(legend.position = c(0.8, 0.8))

print(a00)

```



#since the 2 features are highly correlated, we cannot see a clear separation of the classes in the scatter plot

```

# original classification
a0 <- ggplot(data = rain_n_test0 , aes(x = Sunshine,
y = Temp3pm,
color= as.factor(RainTomorrow) )) +
geom_point()+
labs(x = "Sunshine",
y = "Temp3pm",
color = "Rain Tomorrow") +
theme(legend.position = c(0.8, 0.8))

# Simple GLM: Threshold of 0.5
a2 <- ggplot(data = rain_n_test0 , aes(x = Sunshine,
y = Temp3pm,
color= as.factor(glm_predict_5_0) )) +
geom_point()+

```

```

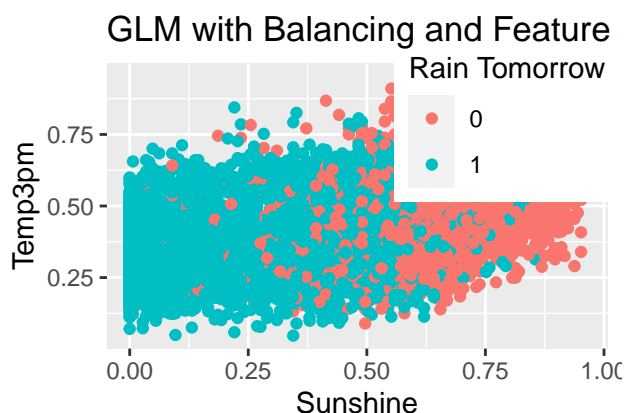
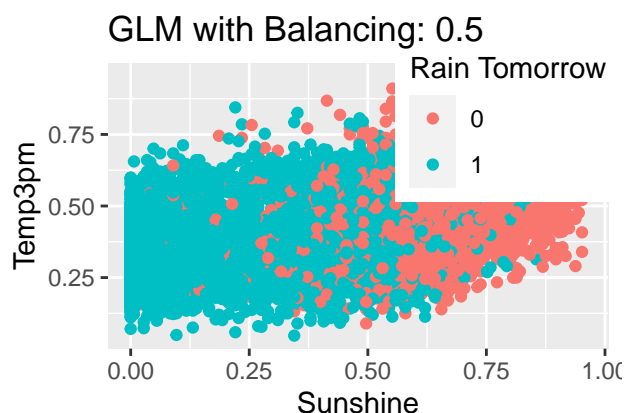
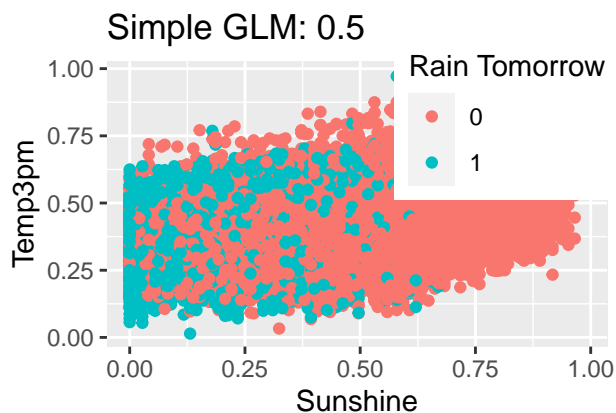
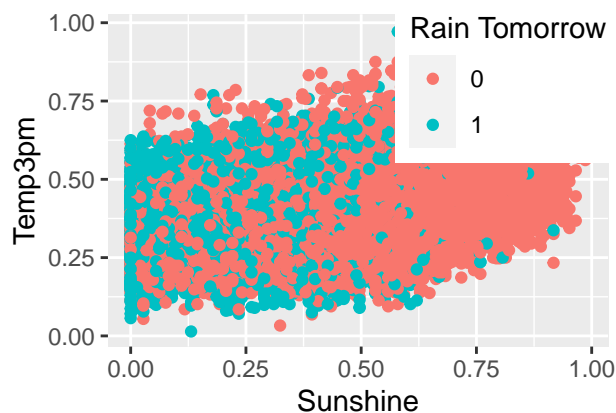
labs(x = "Sunshine",
y = "Temp3pm",
color = "Rain Tomorrow",
title = "Simple GLM: 0.5") +
theme(legend.position = c(0.8, 0.8))

# GLM with Balancing: Threshold of 0.5
b2 <- ggplot(data = rain_balanced_test , aes(x = Sunshine,
y = Temp3pm,
color= as.factor(glm_predict_5_balanced) )) +
geom_point()+
labs(x = "Sunshine",
y = "Temp3pm",
color = "Rain Tomorrow",
title = "GLM with Balancing: 0.5") +
theme(legend.position = c(0.8, 0.8))

# GLM with Balancing and Feature Selection
c2 <- ggplot(data = rain_balanced_test , aes(x = Sunshine,
y = Temp3pm,
color= as.factor(glm_predict_5) )) +
geom_point()+
labs(x = "Sunshine",
y = "Temp3pm",
color = "Rain Tomorrow",
title = "GLM with Balancing and Feature Selection: 0.5") +
theme(legend.position = c(0.8, 0.8))

grid.arrange(a0, a2, b2, c2, nrow = 2)

```



```
X_train_subset <- model.matrix(RainTomorrow~., data=rain_subset_train)
X_test_subset <- model.matrix(RainTomorrow~., data=rain_subset_test)
X_train_subset <- X_train_subset[,-1]
X_test_subset <- X_test_subset[,-1]
```

```
# Target vector
y_train_subset <- rain_subset_train$RainTomorrow
y_test_subset <- rain_subset_test$RainTomorrow
```

LASSO and Ridge Regression

```
set.seed(123)
#we're implementing lasso/ridge with balanced data with no selection ie. rain_balanced_train

X <- model.matrix(RainTomorrow~., data=rain_balanced)
X <- X[,-1]

X_train <- model.matrix(RainTomorrow~., data=rain_balanced_train)
X_test <- model.matrix(RainTomorrow~., data=rain_balanced_test)
X_train <- X_train[,-1]
X_test <- X_test[,-1]

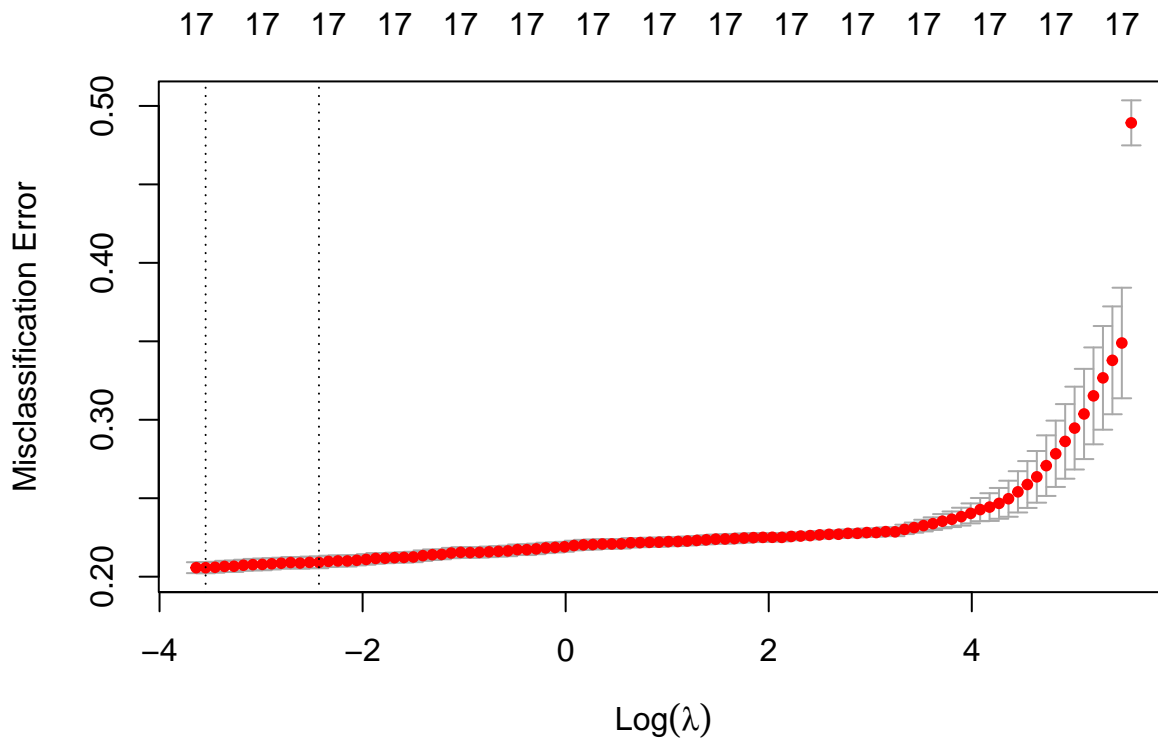
# Target vector
y <- rain_balanced$RainTomorrow
y_train <- rain_balanced_train$RainTomorrow
y_test <- rain_balanced_test$RainTomorrow
```



```
# alpha=0 for ridge, alpha=1 (default) for lasso
```

```
# Ridge Regression (L2)
```

```
ridge_cv <- cv.glmnet(X_train, y_train, alpha=0, family = "binomial", type.measure = "class")
plot(ridge_cv)
```



```
# to select best lambda
```

```
lambda_opt_ridge <- ridge_cv$lambda.min
lambda_opt_ridge
```

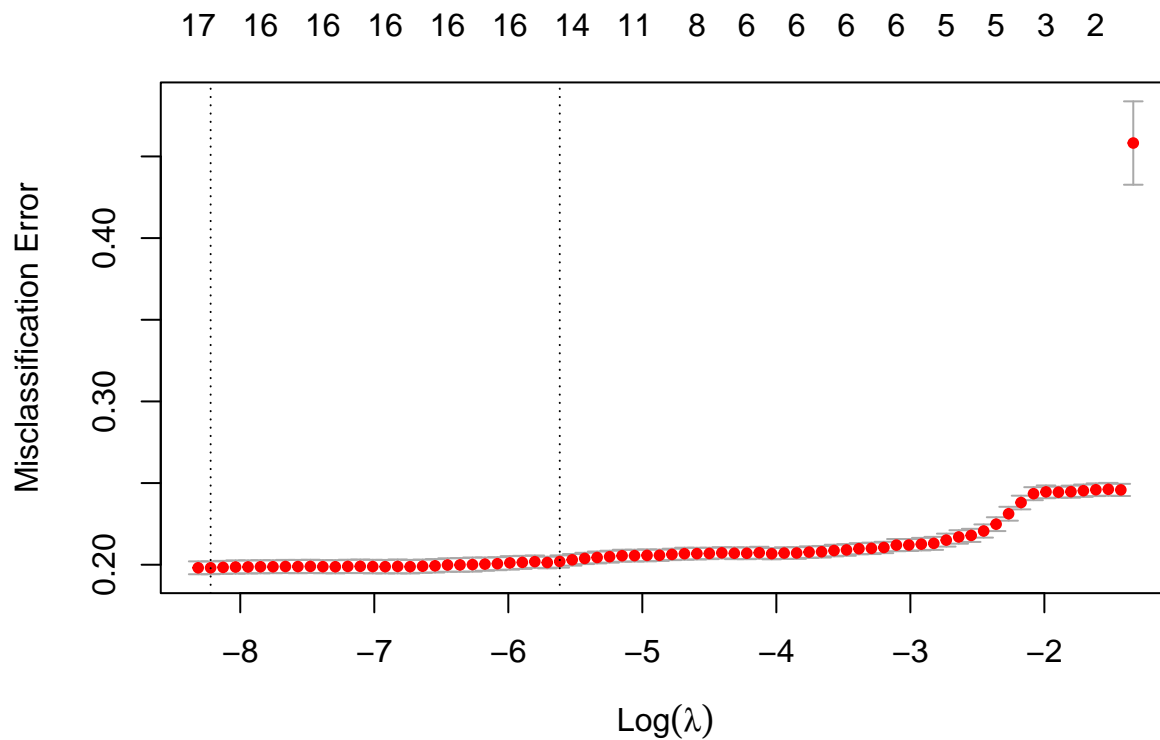
```
## [1] 0.0288348
```

```
pred_ridge <- predict(ridge_cv, X_test, type = "class", s = lambda_opt_ridge)
table(y_test, pred_ridge)
```

```
##      pred_ridge
## y_test    0    1
##      0 2469  664
##      1  633 2448
```

```
#Lasso Regression (L1)
```

```
lasso_cv <- cv.glmnet(X_train, y_train, alpha=1, family = "binomial", type.measure = "class")
plot(lasso_cv)
```



```
lambda_opt_lasso <- lasso_cv$lambda.min
lambda_opt_lasso
```

```
## [1] 0.0002689143
```

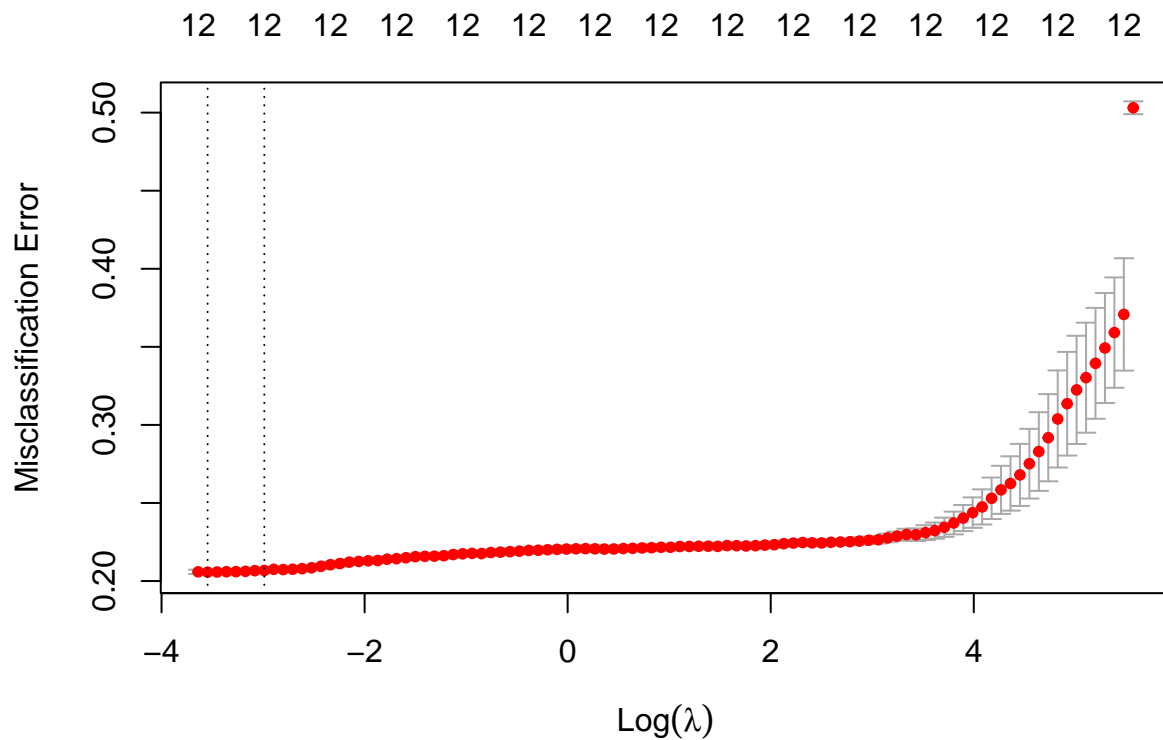
```
pred_lasso<- predict(lasso_cv, X_test, type = "class", s = lambda_opt_lasso)
table(y_test, pred_lasso)
```

```
##      pred_lasso
## y_test    0    1
##      0 2529  604
##      1  652 2429
```

#Implement Ridge and LASSO after feature selection

Ridge Regression (L2)

```
ridge_cv_subset <- cv.glmnet(X_train_subset, y_train_subset, alpha=0, family = "binomial", type.measure
plot(ridge_cv_subset)
```



```
# to select best lambda
```

```
lambda_opt_ridge_subset <- ridge_cv_subset$lambda.min
```

```
lambda_opt_ridge_subset
```

```
## [1] 0.0288348
```

```
pred_ridge_subset<- predict(ridge_cv_subset, X_test_subset, type = "class", s = lambda_opt_ridge_subset)
```

```
table(y_test_subset, pred_ridge_subset)
```

```
##           pred_ridge_subset
```

```
## y_test_subset    0     1
```

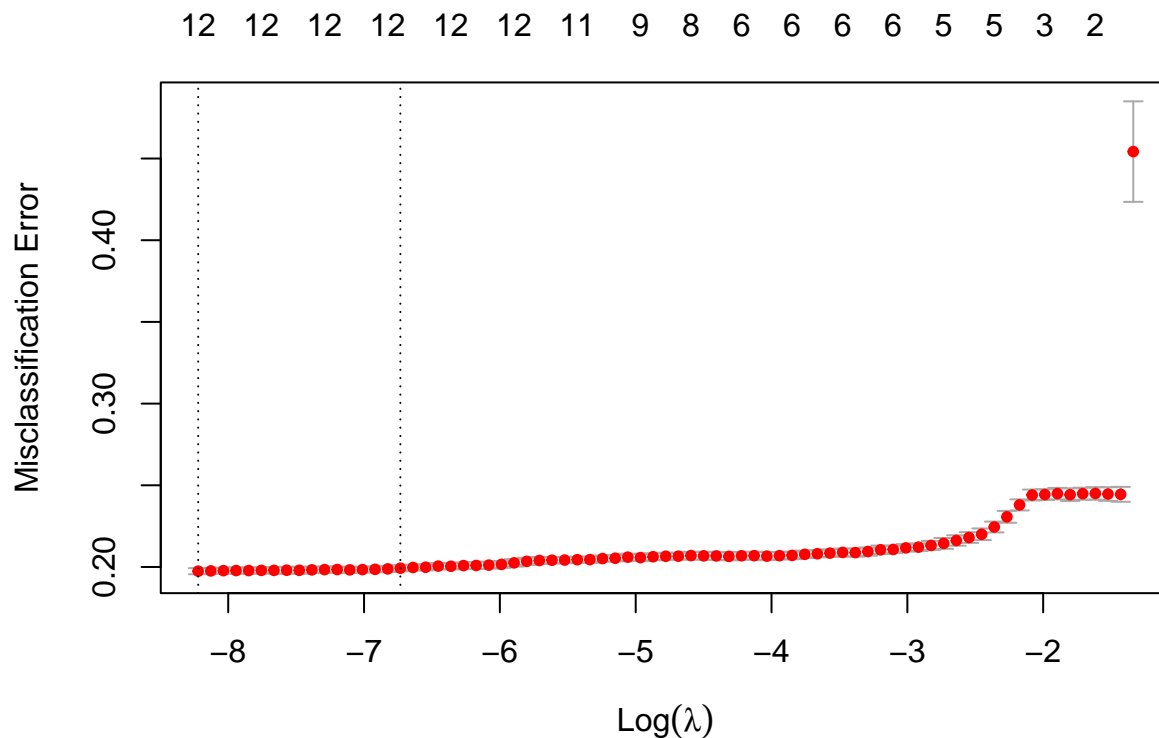
```
##           0 2480  653
```

```
##           1  637 2444
```

```
#Lasso Regression (L1)
```

```
lasso_cv_subset <- cv.glmnet(X_train_subset, y_train_subset, alpha=1, family = "binomial", type.measure
```

```
plot(lasso_cv_subset)
```



```
lambda_opt_lasso_subset <- lasso_cv_subset$lambda.min
lambda_opt_lasso_subset
```

```
## [1] 0.0002689143
```

```
pred_lasso_subset<- predict(lasso_cv_subset, X_test_subset, type = "class", s = lambda_opt_lasso_subset)
table(y_test_subset, pred_lasso_subset)
```

```
##           pred_lasso_subset
## y_test_subset    0     1
##           0 2530   603
##           1   651 2430
```

```
##Remove outliers from data
```

```
#looking for outliers in our data after balancing and feature selection
```

```
g1<- ggplot(data = rain_subset_train, aes(y = MinTemp,fill = 2)) +
geom_boxplot(outlier.colour = "red", outlier.shape = 16,
outlier.size = 2)+
theme(legend.position="none") +
ylab("Min Temperature")
#print(g1)
chisq.out.test(rain_subset_train$MinTemp) #p-value = 0.00151, remove 376
```

```
##
## chi-squared test for outlier
##
## data: rain_subset_train$MinTemp
## X-squared = 10.066, p-value = 0.00151
## alternative hypothesis: lowest value 0 is an outlier
```

```

which(rain_subset_train$MinTemp == 0)

## [1] 376

g2<- ggplot(data = rain_subset_train, aes(y = Sunshine,fill = 2)) +
geom_boxplot(outlier.colour = "red", outlier.shape = 16,
outlier.size = 2)+
theme(legend.position="none") +
ylab("Sunshine")
#print(g2)
chisq.out.test(rain_subset_train$Sunshine) #p-value = 0.04431, index 6965

##
## chi-squared test for outlier
##
## data: rain_subset_train$Sunshine
## X-squared = 4.0448, p-value = 0.04431
## alternative hypothesis: highest value 1 is an outlier
which(rain_subset_train$Sunshine == 1)

## [1] 6965

g3<- ggplot(data = rain_subset_train, aes(y = WindGustSpeed,fill = 2)) +
geom_boxplot(outlier.colour = "red", outlier.shape = 16,
outlier.size = 2)+
theme(legend.position="none") +
ylab("WindGustSpeed")
#print(g3)
chisq.out.test(rain_subset_train$WindGustSpeed) #p-value = 3.071e-07, no values

##
## chi-squared test for outlier
##
## data: rain_subset_train$WindGustSpeed
## X-squared = 26.204, p-value = 3.071e-07
## alternative hypothesis: highest value 0.939130434782609 is an outlier
which(rain_subset_train$WindGustSpeed == 0.939130434782609)

## integer(0)

g4<- ggplot(data = rain_subset_train, aes(y = WindSpeed9am,fill = 2)) +
geom_boxplot(outlier.colour = "red", outlier.shape = 16,
outlier.size = 2)+
theme(legend.position="none") +
ylab("WindSpeed9am")
#print(g4)
chisq.out.test(rain_subset_train$WindSpeed9am) #p-value = 1.43e-08 , no values

##
## chi-squared test for outlier
##
## data: rain_subset_train$WindSpeed9am
## X-squared = 32.146, p-value = 1.43e-08
## alternative hypothesis: highest value 0.969230769230769 is an outlier

```

```
which(rain_subset_train$WindSpeed9am == 0.969230769230769)
```

```
## integer(0)
```

```
g5<- ggplot(data = rain_subset_train, aes(y = WindSpeed3pm, fill = 2)) +  
geom_boxplot(outlier.colour = "red", outlier.shape = 16,  
outlier.size = 2)+  
theme(legend.position="none") +  
ylab("WindSpeed3pm")  
#print(g5)  
chisq.out.test(rain_subset_train$WindSpeed3pm) #p-value = 4.733e-07 , no values
```

```
##
```

```
## chi-squared test for outlier
```

```
##
```

```
## data: rain_subset_train$WindSpeed3pm
```

```
## X-squared = 25.37, p-value = 4.733e-07
```

```
## alternative hypothesis: highest value 0.851351351351351 is an outlier
```

```
which(rain_subset_train$WindSpeed3pm == 0.851351351351351)
```

```
## integer(0)
```

```
g6<- ggplot(data = rain_subset_train, aes(y = Humidity3pm, fill = 2)) +  
geom_boxplot(outlier.colour = "red", outlier.shape = 16,  
outlier.size = 2)+  
theme(legend.position="none") +  
ylab("Humidity3pm")  
#print(g6)  
chisq.out.test(rain_subset_train$Humidity3pm) #p-value = 0.009785, indices:3782 10189 10959 15362 16105
```

```
##
```

```
## chi-squared test for outlier
```

```
##
```

```
## data: rain_subset_train$Humidity3pm
```

```
## X-squared = 6.6737, p-value = 0.009785
```

```
## alternative hypothesis: lowest value 0.01 is an outlier
```

```
which(rain_subset_train$Humidity3pm == 0.01)
```

```
## [1] 3782 10189 10959 15362 16105 18240
```

```
g7<- ggplot(data = rain_subset_train, aes(y = Pressure9am, fill = 2)) +  
geom_boxplot(outlier.colour = "red", outlier.shape = 16,  
outlier.size = 2)+  
theme(legend.position="none") +  
ylab("Pressure9am")  
#print(g7)  
chisq.out.test(rain_subset_train$Pressure9am) # p-value = 2.435e-06, index= 1935
```

```
##
```

```
## chi-squared test for outlier
```

```
##
```

```
## data: rain_subset_train$Pressure9am
```

```
## X-squared = 22.217, p-value = 2.435e-06
```

```
## alternative hypothesis: lowest value 0.0283806343906518 is an outlier
```

```
which(rain_subset_train$Pressure9am ==0.0283806343906518)
```

```
## [1] 1935
```

```
g8<- ggplot(data = rain_subset_train, aes(y = Pressure3pm,fill = 2)) +  
geom_boxplot(outlier.colour = "red", outlier.shape = 16,  
outlier.size = 2)+  
theme(legend.position="none") +  
ylab("Pressure3pm")  
#print(g8)  
chisq.out.test(rain_subset_train$Pressure3pm) # p-value = 2.756e-07, index=15369
```

```
##  
## chi-squared test for outlier  
##  
## data: rain_subset_train$Pressure3pm  
## X-squared = 26.413, p-value = 2.756e-07  
## alternative hypothesis: lowest value 0 is an outlier
```

```
which(rain_subset_train$Pressure3pm ==0)
```

```
## [1] 15369
```

```
g9<- ggplot(data = rain_subset_train, aes(y = Cloud9am,fill = 2)) +  
geom_boxplot(outlier.colour = "red", outlier.shape = 16,  
outlier.size = 2)+  
theme(legend.position="none") +  
ylab("Cloud9am")  
#print(g9)  
chisq.out.test(rain_subset_train$Cloud9am)
```

```
##  
## chi-squared test for outlier  
##  
## data: rain_subset_train$Cloud9am  
## X-squared = 3.2178, p-value = 0.07284  
## alternative hypothesis: lowest value 0 is an outlier
```

```
which(rain_subset_train$Cloud9am ==0) # we got a p-value of 0.07 so we cannot refute the null hypothesis.
```

```
##      [1]      22      60     108     154     160     183     197     201     212     227     238     292  
##     [13]     319     333     359     366     391     406     411     412     425     439     440     450  
##     [25]     498     501     503     514     524     530     534     550     555     569     577     618  
##     [37]     654     685     687     704     707     708     721     725     736     747     748     753  
##     [49]     769     771     774     787     805     842     866     890     900     919     922     937  
##     [61]     953     979     997    1022    1056    1057    1060    1066    1110    1117    1125    1131  
##     [73]    1151    1184    1216    1221    1231    1233    1242    1260    1261    1264    1283    1298  
##     [85]    1309    1327    1337    1360    1406    1407    1422    1435    1444    1458    1477    1497  
##     [97]    1533    1535    1554    1556    1577    1608    1617    1636    1653    1654    1667    1700  
##    [109]    1708    1716    1737    1781    1816    1870    1880    1883    1900    1918    1923    1972  
##    [121]    1991    2001    2004    2009    2022    2033    2044    2085    2086    2112    2117    2166  
##    [133]    2225    2252    2273    2278    2292    2293    2296    2299    2314    2321    2334    2340  
##    [145]    2343    2346    2382    2394    2403    2416    2425    2429    2442    2470    2476    2495  
##    [157]    2498    2520    2528    2536    2552    2573    2587    2611    2636    2638    2644    2659  
##    [169]    2661    2691    2697    2716    2723    2729    2738    2773    2792    2794    2798    2815  
##    [181]    2825    2827    2869    2871    2878    2911    2922    2938    3020    3022    3030    3033  
##    [193]    3040    3051    3080    3096    3127    3129    3143    3148    3155    3183    3204    3221
```

##	[205]	3224	3238	3247	3286	3309	3355	3359	3376	3377	3390	3454	3456
##	[217]	3470	3495	3564	3602	3603	3612	3626	3653	3655	3673	3687	3688
##	[229]	3691	3698	3723	3727	3765	3782	3811	3816	3838	3850	3861	3862
##	[241]	3873	3888	3913	3940	3959	3964	3977	3985	3990	4007	4016	4019
##	[253]	4026	4034	4044	4048	4058	4123	4194	4225	4230	4286	4305	4312
##	[265]	4342	4345	4352	4368	4371	4396	4402	4426	4477	4486	4492	4499
##	[277]	4576	4577	4586	4596	4607	4630	4674	4679	4689	4693	4716	4724
##	[289]	4742	4744	4789	4802	4840	4858	4859	4870	4873	4892	4893	4897
##	[301]	4902	4919	4921	4923	4926	4932	4933	4938	4943	4972	4983	5003
##	[313]	5018	5055	5057	5082	5096	5101	5119	5120	5138	5139	5146	5168
##	[325]	5192	5199	5231	5262	5263	5265	5267	5292	5324	5331	5333	5346
##	[337]	5397	5413	5494	5496	5538	5556	5606	5617	5626	5636	5650	5664
##	[349]	5665	5686	5690	5692	5693	5701	5705	5721	5739	5769	5784	5808
##	[361]	5812	5824	5841	5848	5849	5852	5860	5866	5901	5904	5914	5916
##	[373]	5925	5940	5946	5966	5982	6024	6031	6034	6041	6060	6068	6086
##	[385]	6118	6160	6163	6171	6186	6208	6227	6239	6250	6253	6264	6269
##	[397]	6273	6300	6301	6333	6334	6370	6374	6387	6421	6424	6434	6439
##	[409]	6479	6524	6544	6546	6575	6580	6600	6603	6663	6667	6705	6707
##	[421]	6722	6723	6754	6796	6858	6894	6899	6903	6926	6954	6965	6975
##	[433]	7040	7042	7082	7086	7099	7111	7141	7180	7199	7202	7221	7223
##	[445]	7224	7251	7258	7259	7299	7313	7323	7351	7354	7371	7376	7406
##	[457]	7407	7438	7446	7451	7489	7500	7503	7505	7510	7558	7574	7577
##	[469]	7585	7589	7594	7596	7606	7611	7614	7615	7632	7640	7648	7652
##	[481]	7661	7685	7701	7707	7714	7739	7752	7757	7761	7763	7774	7787
##	[493]	7802	7803	7829	7864	7900	7914	7920	7926	7954	7961	7962	7969
##	[505]	7978	7991	7993	8004	8011	8039	8044	8047	8048	8066	8082	8113
##	[517]	8119	8144	8148	8149	8164	8167	8174	8179	8187	8198	8211	8234
##	[529]	8244	8258	8261	8264	8274	8291	8313	8333	8336	8340	8352	8359
##	[541]	8365	8379	8536	8578	8583	8592	8601	8618	8654	8680	8699	8706
##	[553]	8737	8742	8757	8773	8776	8812	8832	8850	8855	8866	8870	8882
##	[565]	8928	8992	9009	9023	9024	9031	9052	9084	9085	9111	9178	9187
##	[577]	9190	9209	9213	9221	9228	9248	9260	9292	9293	9297	9313	9332
##	[589]	9343	9365	9381	9421	9433	9446	9459	9462	9476	9482	9493	9500
##	[601]	9528	9576	9582	9611	9618	9628	9653	9680	9708	9712	9717	9723
##	[613]	9731	9732	9735	9742	9744	9795	9852	9854	9858	9861	9879	9911
##	[625]	9928	9942	9972	9974	10037	10046	10055	10057	10060	10067	10082	10088
##	[637]	10118	10128	10162	10174	10179	10203	10208	10212	10213	10218	10226	10238
##	[649]	10247	10293	10312	10333	10351	10352	10360	10377	10393	10413	10420	10467
##	[661]	10500	10521	10532	10551	10555	10556	10572	10578	10582	10586	10592	10626
##	[673]	10641	10650	10656	10683	10698	10702	10718	10726	10737	10749	10785	10793
##	[685]	10796	10830	10831	10837	10853	10889	10904	10951	10955	10956	10958	11021
##	[697]	11024	11045	11048	11115	11120	11121	11123	11142	11156	11174	11182	11235
##	[709]	11251	11322	11333	11337	11345	11354	11369	11411	11417	11423	11444	11474
##	[721]	11475	11492	11506	11584	11599	11638	11648	11671	11678	11679	11684	11685
##	[733]	11703	11706	11712	11725	11730	11757	11759	11770	11774	11776	11777	11783
##	[745]	11796	11808	11821	11844	11886	11900	11938	11992	11997	12007	12008	12024
##	[757]	12027	12039	12067	12069	12081	12083	12123	12133	12147	12178	12182	12235
##	[769]	12240	12259	12270	12314	12343	12351	12375	12377	12378	12381	12407	12426
##	[781]	12430	12464	12469	12483	12514	12524	12534	12542	12561	12594	12617	12625
##	[793]	12649	12680	12722	12736	12739	12744	12758	12760	12767	12772	12774	12775
##	[805]	12784	12818	12829	12862	12881	12962	12989	13003	13027	13034	13051	13066
##	[817]	13076	13081	13099	13103	13116	13122	13134	13150	13160	13169	13170	13196
##	[829]	13209	13211	13227	13228	13250	13256	13272	13349	13373	13380	13383	13385
##	[841]	13386	13411	13413	13417	13432	13435	13437	13439	13452	13484	13491	13535


```
## [853] 13563 13571 13584 13596 13608 13613 13638 13647 13668 13671 13752 13761
## [865] 13774 13801 13810 13816 13848 13867 13870 13875 13879 13894 13901 13933
## [877] 13936 13944 13962 13963 13966 13988 13989 13991 13993 14024 14026 14033
## [889] 14046 14059 14099 14104 14150 14164 14167 14175 14180 14194 14212 14215
## [901] 14217 14219 14231 14272 14279 14282 14293 14296 14339 14343 14359 14372
## [913] 14374 14411 14417 14440 14449 14456 14457 14466 14478 14482 14487 14493
## [925] 14523 14539 14561 14581 14583 14592 14710 14735 14747 14756 14776 14784
## [937] 14801 14809 14814 14816 14840 14875 14878 14889 14896 14898 14899 14903
## [949] 14916 14938 14995 15001 15049 15095 15097 15102 15166 15174 15186 15191
## [961] 15216 15233 15271 15275 15281 15328 15337 15418 15426 15427 15432 15437
## [973] 15448 15451 15460 15463 15464 15500 15527 15530 15607 15618 15628 15659
## [985] 15663 15692 15709 15715 15737 15742 15788 15791 15795 15801 15802 15843
## [997] 15846 15848 15849 15850 15857 15859 15883 15900 15923 15931 15964 15969
## [1009] 15994 16058 16060 16064 16073 16092 16095 16111 16133 16138 16181 16193
## [1021] 16196 16202 16205 16220 16229 16255 16271 16280 16282 16304 16309 16310
## [1033] 16319 16408 16437 16479 16494 16560 16576 16577 16588 16605 16625 16639
## [1045] 16663 16685 16718 16735 16773 16782 16799 16803 16821 16826 16837 16858
## [1057] 16870 16885 16892 16895 16901 16902 16924 16944 16949 16951 16977 16988
## [1069] 17015 17016 17025 17029 17052 17082 17084 17115 17141 17155 17164 17171
## [1081] 17190 17208 17213 17224 17251 17260 17283 17287 17290 17293 17335 17345
## [1093] 17360 17368 17401 17417 17435 17439 17471 17475 17505 17507 17508 17517
## [1105] 17518 17551 17572 17587 17590 17598 17609 17617 17634 17636 17661 17662
## [1117] 17666 17667 17677 17690 17701 17727 17775 17776 17785 17798 17801 17809
## [1129] 17824 17862 17879 17899 17945 17959 17965 17971 17992 18010 18038 18067
## [1141] 18083 18084 18090 18105 18112 18119 18159 18160 18221 18240 18245 18274
## [1153] 18288 18311 18312 18329 18359 18368 18392 18394 18449 18451 18469 18488
## [1165] 18499 18571 18589 18622 18631 18632
```

```
g10<- ggplot(data = rain_subset_train, aes(y = Cloud3pm, fill = 2)) +
geom_boxplot(outlier.colour = "red", outlier.shape = 16,
outlier.size = 2)+
theme(legend.position="none") +
ylab("Cloud3pm")
#print(g10)
chisq.out.test(rain_subset_train$Cloud3pm) #p-value = 0.04988
```

```
##
## chi-squared test for outlier
##
## data: rain_subset_train$Cloud3pm
## X-squared = 3.8456, p-value = 0.04988
## alternative hypothesis: lowest value 0 is an outlier
```

```
which(rain_subset_train$Cloud3pm ==0)
```

```
## [1] 108 154 160 201 227 238 292 304 313 319 391 411
## [13] 412 450 503 528 530 550 555 569 575 584 644 654
## [25] 657 687 704 708 712 721 748 753 774 805 919 979
## [37] 995 997 1022 1057 1066 1091 1095 1184 1191 1221 1264 1266
## [49] 1283 1290 1298 1444 1445 1458 1497 1504 1533 1535 1617 1636
## [61] 1643 1653 1667 1708 1716 1737 1781 1797 1865 1869 1883 1917
## [73] 1918 1974 2001 2085 2112 2171 2224 2225 2252 2296 2321 2333
## [85] 2343 2346 2394 2401 2416 2428 2453 2464 2475 2476 2498 2520
## [97] 2536 2552 2587 2625 2661 2691 2697 2729 2738 2773 2780 2794
## [109] 2811 2869 2871 2875 2878 3020 3022 3030 3033 3096 3127 3143
```

```
## [121] 3204 3245 3247 3252 3345 3355 3384 3386 3390 3424 3454 3590
## [133] 3602 3603 3637 3660 3673 3687 3688 3698 3718 3723 3727 3782
## [145] 3811 3816 3850 3854 3862 3888 3892 3942 3985 3986 4007 4021
## [157] 4026 4034 4046 4058 4123 4136 4155 4184 4198 4226 4283 4308
## [169] 4323 4371 4426 4442 4458 4477 4486 4492 4499 4510 4524 4538
## [181] 4577 4591 4633 4667 4674 4689 4716 4744 4748 4763 4766 4772
## [193] 4776 4859 4868 4873 4892 4897 4923 4932 4933 4970 4972 4986
## [205] 5003 5010 5055 5057 5082 5120 5146 5197 5213 5262 5263 5267
## [217] 5346 5367 5397 5398 5407 5412 5413 5424 5428 5496 5538 5595
## [229] 5606 5693 5723 5769 5783 5786 5824 5866 5870 5901 5925 5978
## [241] 5982 6031 6034 6041 6068 6086 6154 6171 6186 6206 6239 6253
## [253] 6319 6332 6334 6362 6374 6421 6424 6434 6439 6490 6544 6559
## [265] 6575 6600 6663 6722 6731 6754 6831 6894 6899 6954 6965 6975
## [277] 6988 7042 7082 7091 7141 7202 7227 7251 7299 7313 7323 7351
## [289] 7362 7371 7378 7406 7407 7433 7465 7489 7500 7512 7580 7594
## [301] 7606 7611 7614 7615 7637 7652 7661 7680 7685 7701 7706 7707
## [313] 7757 7763 7774 7793 7801 7829 7864 7954 7961 7969 7978 8011
## [325] 8038 8044 8047 8063 8069 8082 8120 8144 8164 8174 8192 8194
## [337] 8222 8229 8234 8264 8274 8340 8365 8379 8395 8575 8578 8652
## [349] 8654 8711 8735 8866 8870 8872 8874 8882 8916 8928 8975 9023
## [361] 9024 9084 9111 9154 9187 9190 9209 9213 9221 9228 9260 9293
## [373] 9297 9381 9412 9416 9421 9433 9500 9528 9535 9536 9582 9658
## [385] 9708 9712 9742 9762 9852 9861 9885 9903 9911 9928 9942 9974
## [397] 9987 10018 10025 10028 10055 10088 10118 10154 10174 10203 10212 10226
## [409] 10247 10293 10294 10351 10360 10387 10393 10459 10481 10500 10521 10532
## [421] 10556 10572 10578 10586 10590 10592 10595 10641 10702 10726 10737 10785
## [433] 10796 10863 10904 10951 10953 10958 10979 11021 11045 11048 11063 11066
## [445] 11123 11128 11142 11174 11185 11235 11251 11311 11353 11354 11360 11369
## [457] 11428 11433 11438 11475 11488 11506 11584 11648 11678 11679 11685 11706
## [469] 11712 11757 11774 11776 11783 11796 11827 11887 11893 11900 11905 11997
## [481] 12008 12081 12123 12135 12147 12240 12270 12339 12343 12351 12381 12407
## [493] 12456 12483 12514 12529 12534 12542 12617 12627 12633 12649 12683 12716
## [505] 12751 12752 12758 12760 12772 12774 12775 12862 12884 12989 13003 13027
## [517] 13092 13099 13111 13179 13196 13209 13262 13286 13301 13316 13349 13351
## [529] 13376 13386 13410 13417 13452 13473 13515 13535 13558 13567 13571 13584
## [541] 13613 13662 13668 13687 13752 13761 13774 13793 13801 13810 13815 13870
## [553] 13944 13972 13984 13989 14062 14096 14136 14150 14175 14194 14212 14277
## [565] 14296 14417 14456 14459 14466 14482 14540 14583 14592 14608 14747 14756
## [577] 14775 14781 14784 14790 14801 14814 14875 14889 14899 14903 14916 14966
## [589] 14978 14989 14995 15035 15037 15049 15095 15097 15102 15172 15174 15218
## [601] 15271 15275 15328 15337 15418 15432 15437 15448 15473 15479 15486 15522
## [613] 15537 15538 15556 15607 15691 15709 15715 15742 15745 15780 15846 15848
## [625] 15850 15890 15891 15965 15994 16052 16060 16091 16124 16133 16432 16576
## [637] 16577 16588 16605 16639 16659 16663 16754 16756 16773 16799 16803 16837
## [649] 16855 16870 16879 16885 16892 16895 16924 16949 16988 17001 17052 17115
## [661] 17150 17171 17213 17224 17251 17256 17259 17287 17293 17310 17320 17335
## [673] 17345 17368 17383 17401 17402 17417 17564 17572 17587 17590 17617 17618
## [685] 17634 17641 17661 17662 17718 17727 17809 17862 17899 18046 18052 18067
## [697] 18083 18090 18159 18221 18232 18240 18311 18329 18359 18361 18368 18392
## [709] 18394 18420 18469 18488 18589 18591 18622 18626 18632
```

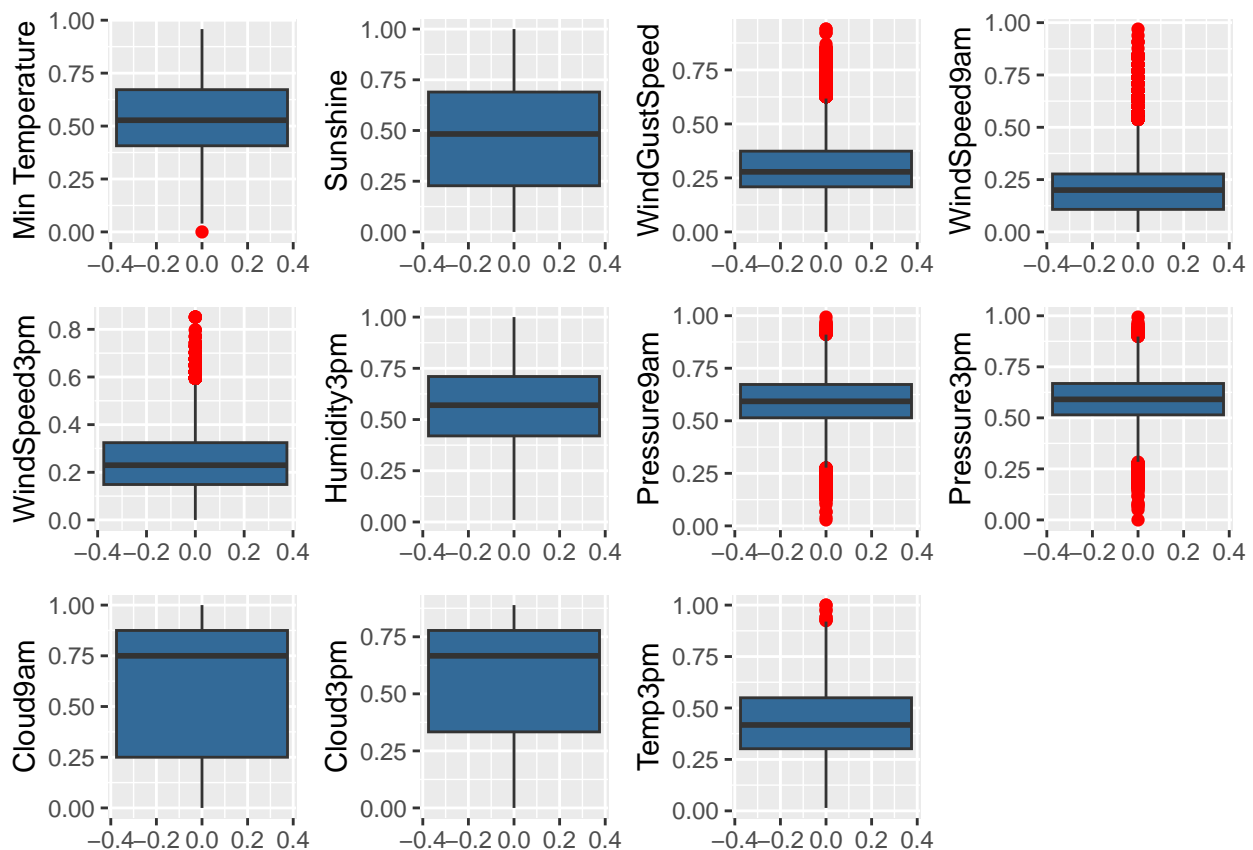
```
g11<- ggplot(data = rain_subset_train, aes(y = Temp3pm, fill = 2)) +
geom_boxplot(outlier.colour = "red", outlier.shape = 16,
outlier.size = 2)+
```

```
theme(legend.position="none") +
ylab("Temp3pm")
#print(g11)
chisq.out.test(rain_subset_train$Temp3pm)#p-value = 0.0003997, indices= 4596, 10679
```

```
##
## chi-squared test for outlier
##
## data: rain_subset_train$Temp3pm
## X-squared = 12.534, p-value = 0.0003997
## alternative hypothesis: highest value 1 is an outlier
which(rain_subset_train$Temp3pm ==1)
```

```
## [1] 4596 10679
```

```
grid.arrange(g1, g2, g3,g4,g5,g6,g7,g8,g9,g10,g11, nrow = 3)
```



```
#remove outliers for p_values less than 0.05
rain_subset_train_NoOutliers <- rain_subset_train[-c(4596,10679,15369,1935,3782,10189,10959,15362,16105
```

```
##LDA
```

```
# Model definition starting from the previous glm_bal model:
```

```
lda<- lda(data = rain_subset_train_NoOutliers,RainTomorrow ~.,family = "binomial")
lda
```

```
## Call:
```

```
## lda(RainTomorrow ~ ., data = rain_subset_train_NoOutliers, family = "binomial")
```

```
##
## Prior probabilities of groups:
##      0      1
## 0.4986052 0.5013948
##
## Group means:
##      MinTemp  Sunshine WindGustSpeed WindSpeed9am WindSpeed3pm Humidity3pm
## 0 0.5198474 0.5981404      0.2639337      0.2044065      0.2354919      0.4472972
## 1 0.5566944 0.3136079      0.3289740      0.2318952      0.2608863      0.6693281
##      Pressure9am Pressure3pm  Cloud9am  Cloud3pm   Temp3pm RainToday
## 0      0.6284978      0.6232747 0.4703169 0.4187170 0.4626215 0.1561222
## 1      0.5583618      0.5622434 0.7413733 0.6944504 0.3922791 0.4574149
##
## Coefficients of linear discriminants:
##                      LD1
## MinTemp      -0.8224766
## Sunshine      -1.7816536
## WindGustSpeed  3.7461372
## WindSpeed9am  -0.4589668
## WindSpeed3pm  -0.7932450
## Humidity3pm    3.3868009
## Pressure9am    3.5262631
## Pressure3pm   -5.8402214
## Cloud9am       -0.1977520
## Cloud3pm        0.7803935
## Temp3pm        1.3252533
## RainToday      0.3534121

pred_lda<- predict(lda, rain_subset_test, type = "response")

post_lda<- pred_lda$posterior

pred_lda_04<- as.factor(ifelse(post_lda[,2] > threshold4, 1, 0))
pred_lda_05<- as.factor(ifelse(post_lda[,2] > threshold5, 1, 0))
pred_lda_06<- as.factor(ifelse(post_lda[,2] > threshold6, 1, 0))

# Confusion matrix with threshold = 0.4
error_lda4 <- mean(pred_lda_04!=rain_subset_test$RainTomorrow)
accuracy_lda4 <- mean(pred_lda_04==rain_subset_test$RainTomorrow)
lda_CM04 <- confusionMatrix(data = factor(pred_lda_04), reference = factor(rain_subset_test$RainTomorrow))

# Confusion matrix with threshold = 0.5
error_lda5 <- mean(pred_lda_05!=rain_subset_test$RainTomorrow)
accuracy_lda5 <- mean(pred_lda_05==rain_subset_test$RainTomorrow)
lda_CM05 <- confusionMatrix(data = factor(pred_lda_05), reference = factor(rain_subset_test$RainTomorrow))

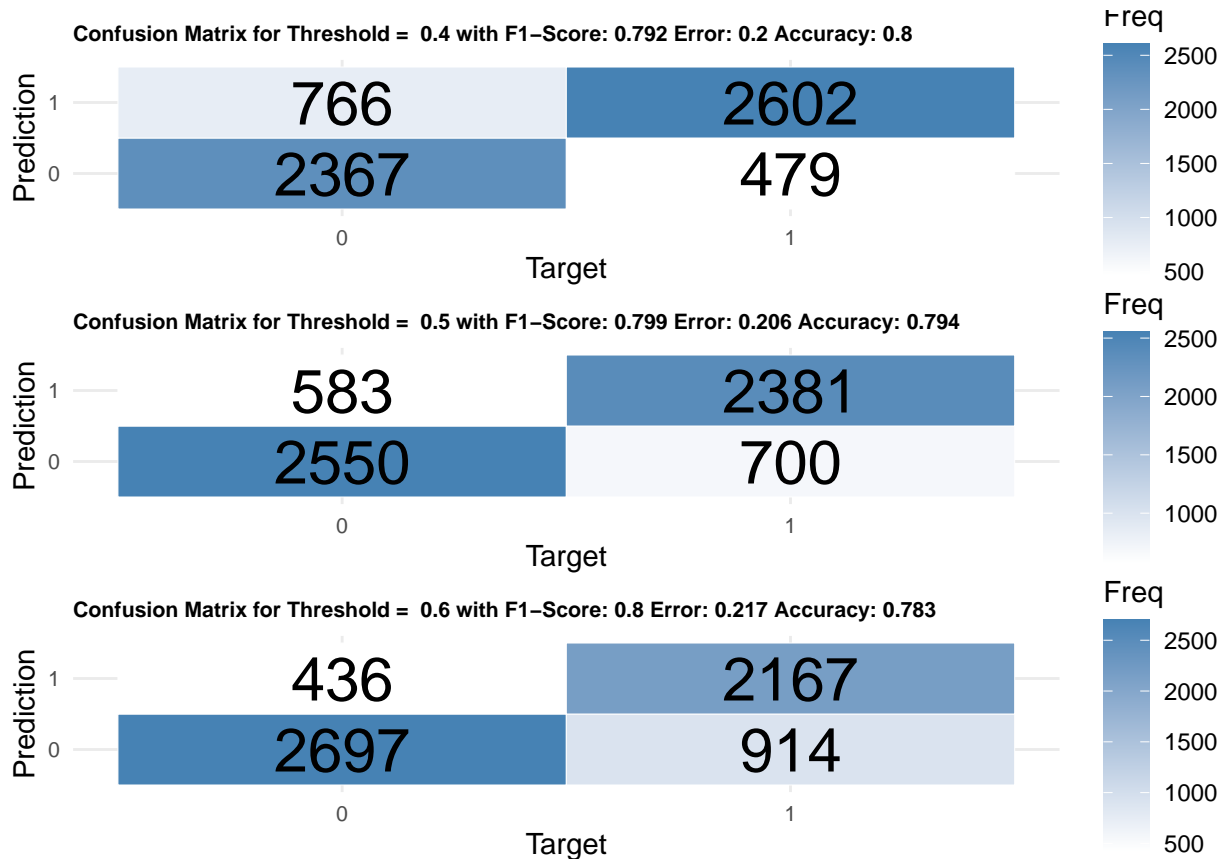
# Confusion matrix with threshold = 0.6
error_lda6 <- mean(pred_lda_06!=rain_subset_test$RainTomorrow)
accuracy_lda6 <- mean(pred_lda_06==rain_subset_test$RainTomorrow)
lda_CM06 <- confusionMatrix(data = factor(pred_lda_06), reference = factor(rain_subset_test$RainTomorrow))
```

```

A <- create_confusion_matrix(lda_CM04, 0.4, error_lda4, accuracy_lda4)
B <- create_confusion_matrix(lda_CM05, 0.5, error_lda5, accuracy_lda5)
C <- create_confusion_matrix(lda_CM06, 0.6, error_lda6, accuracy_lda6)

# Threshold of 0.6 is the best among thresholds in terms of accuracy, sensitivity, and specificity
CM_all_lda = list(A,B,C)
plot_width <- c(4, 4, 4)
grid.arrange(grobs = CM_all_lda, nrow = 3, width = plot_width)

```

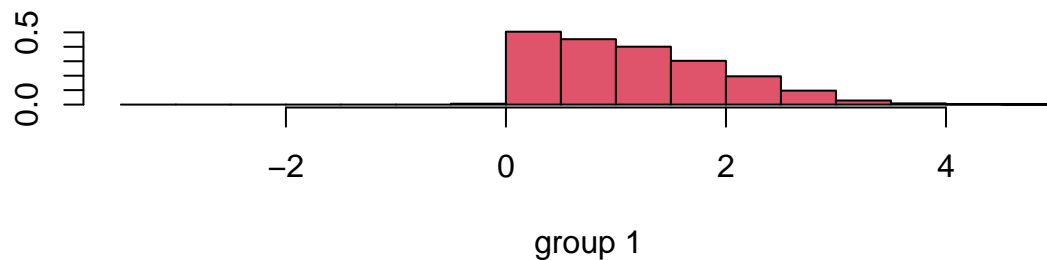
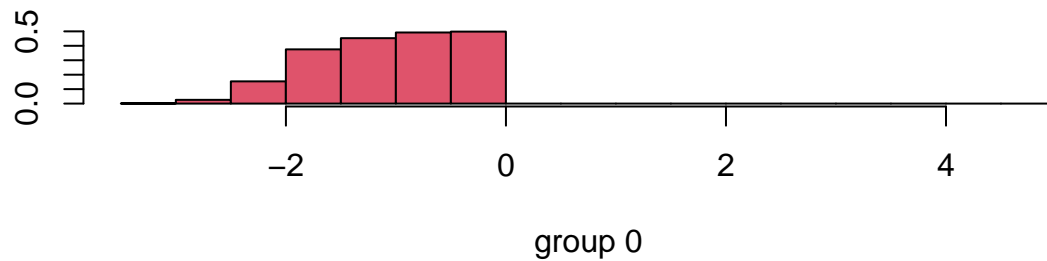


```

# We use now the information given by:
# - x: linear combination of the variables that better describe the examples
# - class: assigned class

ldahist(pred_lda$x[,1], g = pred_lda$class, col = 2)

```



```
qda<- qda(data = rain_subset_train_NoOutliers,RainTomorrow ~.,family = "binomial")
qda
```

```
## Call:
## qda(RainTomorrow ~ ., data = rain_subset_train_NoOutliers, family = "binomial")
##
## Prior probabilities of groups:
##      0      1
## 0.4986052 0.5013948
##
## Group means:
##      MinTemp  Sunshine WindGustSpeed WindSpeed9am WindSpeed3pm Humidity3pm
## 0 0.5198474 0.5981404      0.2639337      0.2044065      0.2354919      0.4472972
## 1 0.5566944 0.3136079      0.3289740      0.2318952      0.2608863      0.6693281
##      Pressure9am Pressure3pm Cloud9am Cloud3pm Temp3pm RainToday
## 0 0.6284978      0.6232747 0.4703169 0.4187170 0.4626215 0.1561222
## 1 0.5583618      0.5622434 0.7413733 0.6944504 0.3922791 0.4574149
```

```
pred_qda<- predict(qda, rain_subset_test, type = "response")
```

```
post_qda<- pred_qda$posterior
```

```
pred_qda_04<- as.factor(ifelse(post_qda[,2] > threshold4, 1, 0))
```

```
pred_qda_05<- as.factor(ifelse(post_qda[,2] > threshold5, 1, 0))
```

```
pred_qda_06<- as.factor(ifelse(post_qda[,2] > threshold6, 1, 0))
```

```
# Confusion matrix with threshold = 0.4
```

```
error_qda4 <- mean(pred_qda_04!=rain_subset_test$RainTomorrow)
```

```
accuracy_qda4 <- mean(pred_qda_04==rain_subset_test$RainTomorrow)
```

```
qda_CM04 <- confusionMatrix(data = factor(pred_qda_04), reference = factor(rain_subset_test$RainTomorrow))
```

```

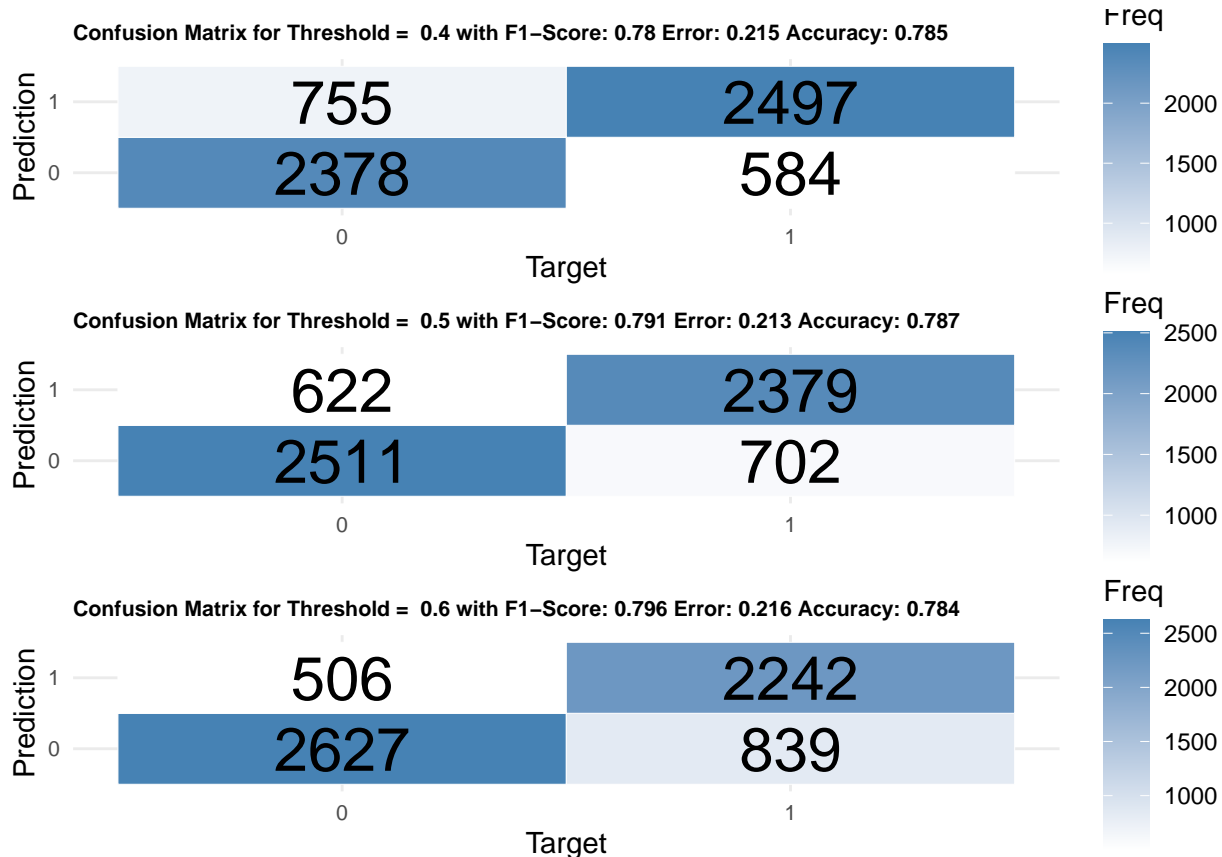
# Confusion matrix with threshold = 0.5
error_qda5 <- mean(pred_qda_05!=rain_subset_test$RainTomorrow)
accuracy_qda5 <- mean(pred_qda_05==rain_subset_test$RainTomorrow)
qda_CM05 <- confusionMatrix(data = factor(pred_qda_05), reference = factor(rain_subset_test$RainTomorrow))

# Confusion matrix with threshold = 0.6
error_qda6 <- mean(pred_qda_06!=rain_subset_test$RainTomorrow)
accuracy_qda6 <- mean(pred_qda_06==rain_subset_test$RainTomorrow)
qda_CM06 <- confusionMatrix(data = factor(pred_qda_06), reference = factor(rain_subset_test$RainTomorrow))

A <- create_confusion_matrix(qda_CM04, 0.4, error_qda4, accuracy_qda4)
B <- create_confusion_matrix(qda_CM05, 0.5, error_qda5, accuracy_qda5)
C <- create_confusion_matrix(qda_CM06, 0.6, error_qda6, accuracy_qda6)

# Threshold of 0.05 is the best among thresholds in terms of accuracy, sensitivity, and specificity
CM_all_qda = list(A,B,C)
plot_width <- c(4, 4, 4)
grid.arrange(grobs = CM_all_qda, nrow = 3, width = plot_width)

```



```

set.seed(2531)

# We look now for the best value of the parameter
kmax <- 100
knn_test_error <- numeric(kmax)

# For each possible value of k we consider the obtained accuracy of the model

```

```

for(k in 1:kmax)
{
  knn_pred <- as.factor(knn(X_train_subset,X_test_subset,cl = y_train_subset, k = k))

  cm <- confusionMatrix(data = knn_pred, reference = y_test_subset)

  knn_test_error[k] <- 1 - cm$overall[1]
}

# We took the minimum value of the error
k_min <- which.min(knn_test_error)
k_min

```

```
## [1] 29
```

```

# We compute now the prediction with the value of k that gives us the minimum error
knn<- knn(X_train_subset, X_test_subset,cl = y_train_subset, k = k_min)

```

```
knn_pred_min <- knn
```

```

# Confusion matrix for KNN on the test set
tab<- table(y_test_subset, knn)
tab

```

```

##           knn
## y_test_subset  0   1
##              0 2476 657
##              1  632 2449

```

```

accuracy <-function(x){sum(diag(x)/(sum(rowSums(x)))) * 100}
accuracy(tab)

```

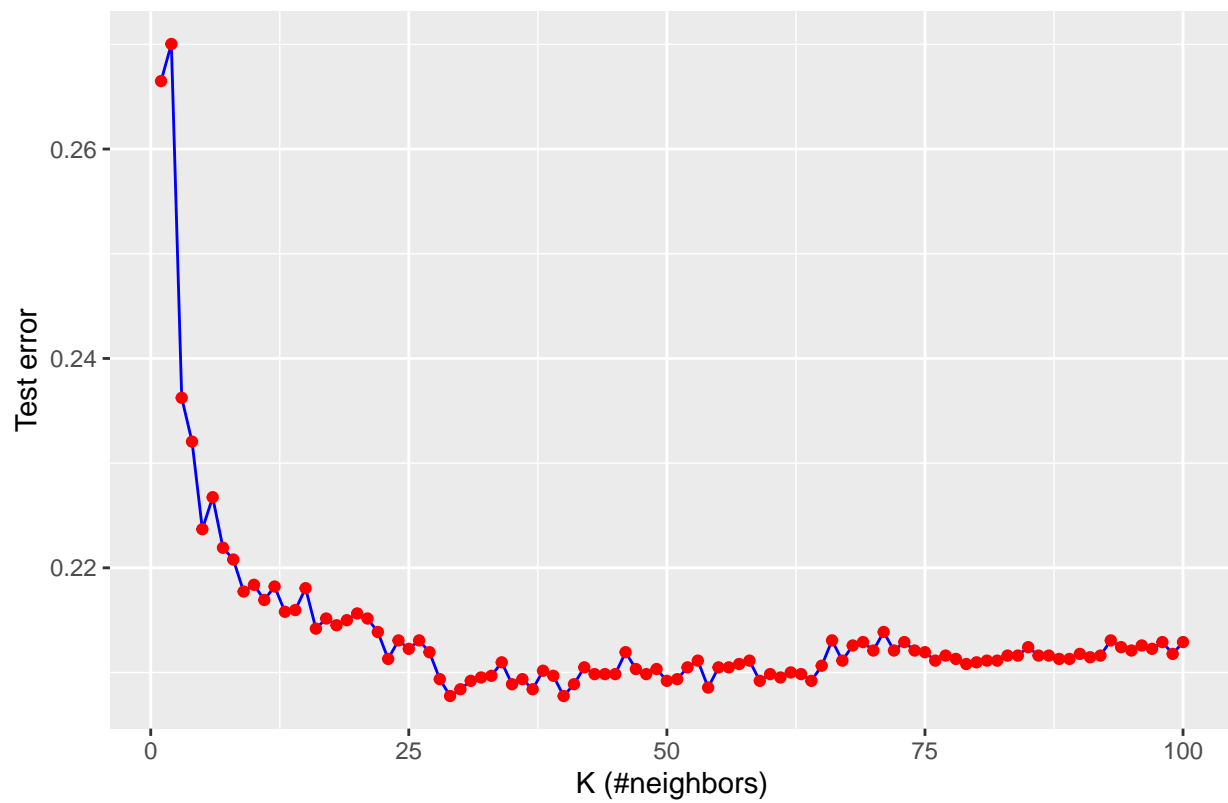
```
## [1] 79.25652
```

```

ggplot(data.frame(knn_test_error),
  aes(x = 1:kmax, y = knn_test_error)) +
  geom_line(colour="blue") +
  geom_point(colour="red") +
  xlab("K (#neighbors)") +
  ylab("Test error") +
  ggtitle(paste0("Best value of K = ", k_min,
    " (minimal error = ",
    format((knn_test_error[k_min])*100, digits = 4),
    "%)"))

```


Best value of $K = 29$ (minimal error = 20.78%)



#TODO: Analysis, Clean Visualizations and Code

Analysis