# Bocconi University, Microeconometrics (cd. 20295) Professor: Thomas Le Barbanchon and T.A.: Erick Baumgartner Problem Set 1: Experiments and Randomization Inference

Due: Tuesday March 18<sup>th</sup> by 11:59pm. Submit by email to erick.baumgartner@unibocconi.it.

# Problem Set 1

We will replicate and re-analyze the discussion initiated by LaLonde (1986) about how regressions with controls (i.e., non-experimental methods) do at replicating experimental results.

In a second stage of this problem set, we will revisit LaLonde (1986) to go through recent econometric advancements on statistical inference of randomized experiments. In particular, we will draw on Athey and Imbens (2017) to implement a randomization-based inference routine over LaLonde (1986)'s experimental data.

# Exercise 1

## **Short Summary of Discussion**

LaLonde (1986) presented a highly influential comparison between experimental and non-experimental methods. He studied the results of the National Supported Work (NSW) demonstration project - a subsidized work experience program that operated for 4 years at 15 locations throughout the US.

Between the rounds of 1975-1977, the treatment was randomized in 10 locations. The program served four target groups: (i) female long term aid recipients, (ii) ex-drug addicts, (iii) ex-offenders and (iv) young school dropouts. It provided trainees with work in a sheltered training environment and then helped them find a regular job. Eligibility criteria for participants included: being currently unemployed, with no more than 3 months of work in the last 6 months.

For the non-experimental results, instead of using the randomized control group, LaLonde (1986) contrasted outcomes from the NSW randomized treated group with those for control groups drawn from two national surveys (PSID and CPS). Since he found extremely different results, he concluded that observational methods are unreliable.

## Data

We will use two datasets (posted on Blackboard):

(i) jtrain2 is a restricted sample from the experimental data used by LaLonde (1986). The original dataset from LaLonde (1986) consisted of two randomly allocated groups: 297

treated and 425 controls. In the restricted dataset that is available we only have a subset of those, 185 treated males who received treatment during 1976-1977 and 260 controls. Thus, it is natural to expect some imbalances.

(ii) jtrain3 includes the 185 treated from the NSW data that were part of the experiment, and a group of 2,490 men (under 55 who are not retired) drawn from the PSID who were not part of the experiment, and are used as a non-experimental control group.

#### Variables

All variables have self-explanatory labels in the dta versions of the dataset (to confirm it, type describe in Stata): (1) the outcome of interest re78 are real earnings during 1978, measured in 1982's US\$1000 (take this into account when you interpret the results)<sup>1</sup>; (2) the treatment variable train is an indicator variable equal to 1 when the individual participates in the NSW training group.

#### Instructions

No need to produce a pdf file with your answers. Save all plots and tables requested (e.g., as pset\_1\_question\_1\_a.xlsx) and a do-file summarizing all of your work in a zipped folder identifying your group and the problem set (e.g., as pset\_X\_group\_Y.zip) to erick.baumgartner @unibocconi.it. In the sub-questions where you are asked to write, please add your answer as a comment in your do file.

**Hint:** If you're using Stata, type \* to add a comment in your do-file (e.g., \* this is a comment line \*). If you're using R, type # (e.g., # this is a comment line).

Hint: You can choose your preferred way of preparing tables: (1) one option if using Stata is to use the command outsheet to construct the tables of summary statistics and the command outreg2 to construct the regression tables (you can use them to export results of summary statistics and regressions to an excel file); (2) another option is to save results using the command eststo and then export these directly to a .tex (latex) file using the command esttab. If using R, one option for exporting results is the stargazer package. Read carefully through the help vignettes for each command you choose and try different options, so to have well-formatted tables.

**Hint:** Have in mind that some commands have different default procedures in Stata and R. Since we are not asking you to specify some of these procedures, it is normal that sometimes the results are not exactly the same between the two languages.

<sup>&</sup>lt;sup>1</sup>Note that all other earnings-related variables within both datasets are also measured in 1982's US\$1000.

# Questions

# 1. Use the file jtrain2.

(a) Construct a table checking for balance across treatment and control for the following covariates: age educ black hisp nodegree re74 re75.

Name it TABLE\_1.

Present for each variable: mean for treated, mean for controls, standard deviations for treated, standard deviations for control, difference in means between treatment and control, appropriate standard errors for difference in means.

Comment on how many variables are balanced or not. Is it what you expected?

(b) Regress re78 on train.

Save the estimate and the standard error of the coefficient on train as scalars. Interpret the coefficient.

- (c) Construct a table by sequentially adding the output of the following regressions to each column:
  - (1) re78 on train;
  - (2) re78 on train age educ black hisp;
  - (3) re78 on train age educ black hisp re74 re75;

Add rows to the table with the number of controls and treated in each regression.

Name it TABLE\_2.

Are your results sensitive to the introduction of covariates?

(d) dfbeta is a statistic that measures how much the regression coefficient of a certain variable changes in standard deviations if the i-th observation is deleted.

If using Stata, type help dfbeta and discover how to estimate this statistic after a regression. The command in R is also dfbeta and can also be checked using help(dfbeta).

Generate a variable named influence\_train storing the dfbetas of train of the last regression you did in point (c).

Redo the last regression you did in point (c) but removing the observations with the 3, 5, and 10 lowest and largest values in influence\_train.

Are your results sensitive to influential observations?

#### 2. Use the jtrain3.

(a) Do a table with the same structure of TABLE\_1 of item (a) in question 1 for the following covariates: age educ black hisp re74 re75 (note that nodegree is not present in the current dataset.)

Add the corresponding columns to TABLE 1.

(b) Generate a variable named treated that randomly allocates half of observations to a (fake) treatment group and the other half to a (fake) control group.

Fix a seed of 5 digits using the command set seed.

**Hint:** Try to do it yourself, but use the following code if you cannot.

```
* generate empty variable to fill with 0s and 1s *
gen treated=.
* fix a seed to make realization of your random variables unique *
set seed 88888

* generate random numbers and order them *
gen random=uniform()
sort random

* create a rank from 1 to N based on the random_order *
egen random_order=rank(random)

* assign the first N/2 obs to treatment and the rest to control *
qui sum random
gen N =r(N)
replace treated=0 if random_order<=(N/2)
replace treated=1 if random_order>(N/2) & random_order<=N</pre>
```

Listing 1: Randomly Assigning Treatment in Stata

```
# Set seed for reproducibility
set.seed(88888)

# Generate a random variable
data_jtrain3$random <- runif(nrow(data_jtrain3))

# Rank observations based on the random variable
data_jtrain3$random_order <- rank(data_jtrain3$random, ties.method = "first")

# Get the total number of observations (N)
N <- nrow(data_jtrain3)

# Assign treatment: First N/2 get 0 (control), rest get 1 (treated)
data_jtrain3$treated <- ifelse(data_jtrain3$random_order <= (N / 2), 0, 1)

# Display first few rows
head(data_jtrain3)</pre>
```

Listing 2: Randomly Assigning Treatment in R

(c) If using Stata, type ssc install randtreat. Then, read randtreat help file. If using R, check the command treatment\_assign from the package RCT.

Redo point (b) using the command randtreat.

Name treated\_2 your new (fake) treatment variable.

Check whether the correlation between treated\_2 and treated is statistically significant or not. (Hint: use pwcorr X Y, sig)

(d) Do a table with the same structure of TABLE\_1 of item (a) in question 1., but using treated instead of train.

Use the same list of covariates of item (a) of this question.

Add the corresponding columns to TABLE\_1.

What you find corresponds to your expectations?

- (e) Sequentially add the output of the following regressions to TABLE\_2:
  - (1) re78 on treated;
  - (2) re78 on treated age educ black hisp;
  - (3) re78 on treated age educ black hisp re74 re75.

Add lines in the table with the number of controls and treated in each regression.

Comment on what you find. Is it what you expected?

- (f) Sequentially add the output of the following regressions to TABLE\_2:
  - (1) re78 on train;
  - (2) re78 on train age educ black hisp;
  - (3) re78 on train age educ black hisp re74 re75.

Add lines in the table with the number of controls and treated in each regression.

Compare the results with the first three columns of TABLE\_2.

Comment on what you find. Is it what you expected? Are your results sensitive to the introduction of covariates?

- 3. So far we have selected the covariates to be added to the regression ourselves. We will now use regularization methods to perform this selection in a data-driven approach. You may use the lassopack package in Stata or the hdm package in R to perform your analysis. To answer the questions below, read Belloni et al. (2014) to understand the "double selection" procedure and check the help files of the commands above in the language you chose.
  - (a) Revisit your analysis of the data set jtrain2 in exercise 1 as a post-Lasso OLS estimation. To do this, in the first step you should perform a Lasso regression of re78 on age educ black hisp re74 re75. Then, in a second step, run an

 $<sup>^{2}</sup>$ You may use the rlasso command (both in R and Stata) to perform this analysis, but may also choose other procedures if you prefer.

OLS regression of re78 on train and all the variables selected in the first step. Discuss your results. What are the issues of performing inference based on such a regression?

- (b) Now perform the "double selection" procedure as described by Belloni et al. (2014). We will perform this for two sets of variables in the exercises below. For each of these cases, you should first perform the "double selection" procedure directly using pdslasso in *Stata* or rlassoEffect in *R* and then check each step of this selection by running rlasso either in *Stata* or *R*.
  - (1) In a first step, perform the "double selection" on the original variable list age educ black hisp re74 re75. Comment on your results.
  - (2) Now increase the potential selected features by creating dummies for each of the age and educ levels (you're also free to add other variables, such as interactions between controls)<sup>3</sup>. Discuss your results and the improvements provided by the "double selection" procedure with respect to the one performed in exercise 3 (a). What can you say about the balance of the characteristics of the treatment and control group based on the selected variables?

## 4. Use the jtrain2 data set.

Read Athey and Imbens (2017) (focus on those sections where the authors discuss how to perform inference in completely randomized experiments; in particular, section 4).

- (a) Under which conditions, allowing for heterogeneous treatment effects, is Neyman's inference unbiased?
- (b) Describe Fisher's inference and replicate section 4.1 of Athey and Imbens (2017) in Stata. Do you arrive at their same p-value? If not, why? **Hint:** Note that you can draw motivation from third-parties for your own answer; for this case, we suggest that you read Heß (2017).
- (c) Read again the randomization plan in LaLonde (1986). On which grounds Athey and Imbens (2017)'s illustration of Fisherian inference on LaLonde (1986)'s paper could be criticized?
- (d) The article Channeling Fisher: Randomization Tests and the Statistical Insignificance of Seemingly Significant Experimental Results (Young, 2019) presents the results of an exercise to test the null hypothesis of no treatment effects in a series of experimental papers recently published in AEA journals, showing that many of the coefficients reported in those papers are no longer significant in a randomization test. A critique of this paper has been published by professors Uri Johnson,

<sup>&</sup>lt;sup>3</sup>If you're interested in reading more about some of the usual procedures of "double selection", you may read David McKenzie's blog post.

Leif Nelson and Joe Simmons in their blog, Data Colada. Read their post here and answer the questions below.

- (1) Briefly explain the difference between the procedure used as the default in Stata for the calculation of standard errors (HC1) and the one proposed by the Data Colada post (HC3).
- (2) Using the dataset jtrain2, rerun the analysis you have performed in exercise 1, now calculating the standard errors based on HC3 (this is done in Stata using the option vce() in your regression command).
- (3) Perform a third version of your analysis, now based on bootstrapping (use the bootstrap command in Stata or the boot command from the boot package in R). Briefly describe how the standard errors are calculated in this approach.
- (4) Do any of your conclusions regarding the effect of the training program change based on the analysis performed in this exercise? Based on the discussion provided in the Data Colada post, can you think of a reason for why your results using HC3 should or shouldn't change for this exercise?<sup>4</sup>

<sup>&</sup>lt;sup>4</sup>If you'd like to read further regarding the discussion on robust standard errors, a recent Stata Blog post also covers some simulations and comparisons related to the Data Colada discussion.

# References

- Athey, S. and Imbens, G. W. (2017). The Econometrics of Randomized Experiments. In *Handbook of Economic Field Experiments*, volume 1, pages 73–140. Elsevier.
- Belloni, A., Chernozhukov, V., and Hansen, C. (2014). High-dimensional methods and inference on structural and treatment effects. *Journal of Economic Perspectives*, 28(2):29–50.
- Heß, S. (2017). Randomization Inference with Stata: A Guide and Software. *The Stata Journal*, 17(3):630–651.
- LaLonde, R. J. (1986). Evaluating the Econometric Evaluations of Training Programs with Experimental Data. *American Economic Review*, 76(4):604–620.
- Young, A. (2019). Channeling fisher: Randomization tests and the statistical insignificance of seemingly significant experimental results. *The quarterly journal of economics*, 134(2):557–598.