

8-Point Algorithm + RANSAC

Arezou Fatemi, Kangxue Yin, Ali Mahdavi Amiri

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1 NORMALIZED 8-POINT ALGORITHM (10 POINTS)

Implement the function “FM_by_normalized_8_point” in “FM.py”. You need to compute the Fundamental Matrix using the 8-point algorithm. To verify your implementation, you can compare your result with the following opencv function:

```
F, _ = cv2.findFundamentalMat(pts1, pts2, cv2.FM_8POINT)
```

Here's the general idea for normalizing the input points:

1. Find the centroid of the points (find the mean x and mean y value)
2. Compute the mean distance of all the points from this centroid
3. Construct a 3 by 3 matrix that would translate the points so that the mean distance would be $\sqrt{2}$

(Let's say (x,y) is the centroid and m is the mean distance from centroid. This would be the matrix:

$$\begin{bmatrix} \sqrt{2}/m & 0 & -x(\sqrt{2}/m) \\ 0 & \sqrt{2}/m & -y(\sqrt{2}/m) \\ 0 & 0 & 1 \end{bmatrix}$$

Now you can use this matrix to normalize (and later de-normalize) the points.

You can find more information about this in the [wikipedia page](#).

- normalize the input points	+ 2 pts
- construct the coefficient matrix of the linear system correctly	+ 2 pts

- solve the linear least square problem correctly	+ 2 pts
- get correct results	+ 2 pts
- comments that explain in details how your code works	+ 2 pts

2 RANSAC (10 POINTS)

Implement the function “FM_by_RANSAC” in “FM.py”. You need to compute the Fundamental Matrix using RANSAC. Here is the pseudo code:

```

n ← 0
for i = 1:M do
  choose 8 pairs of matching points randomly
   $F_i \leftarrow$  fundamental matrix obtained by normalized 8-point algorithm
  Compute the number of inliers,  $n_i$ , with respect to  $F_i$ 
  If  $n_i > n$ :
    n =  $n_i$ 
    F =  $F_i$ 
  end
end
end

```

To verify your implementation, you can compare your result with the following opencv function:

$F, \text{mask} = \text{cv2.findFundamentalMat}(\text{pts1}, \text{pts2}, \text{cv2.FM_RANSAC})$

- compute number of inliers correctly	+ 3 pts
- get correct results	+ 5 pts
- comments that explain in details how your code works	+ 2 pts

