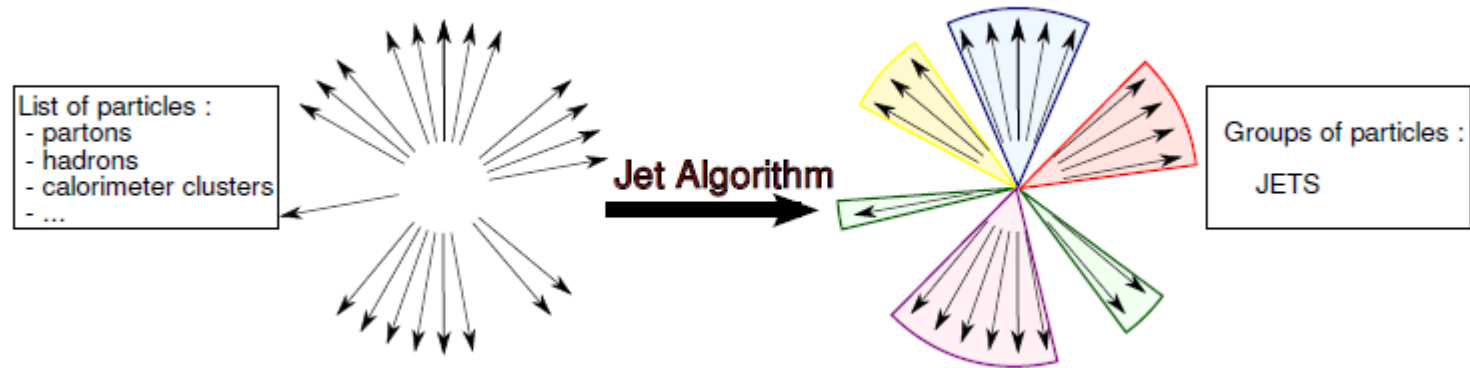
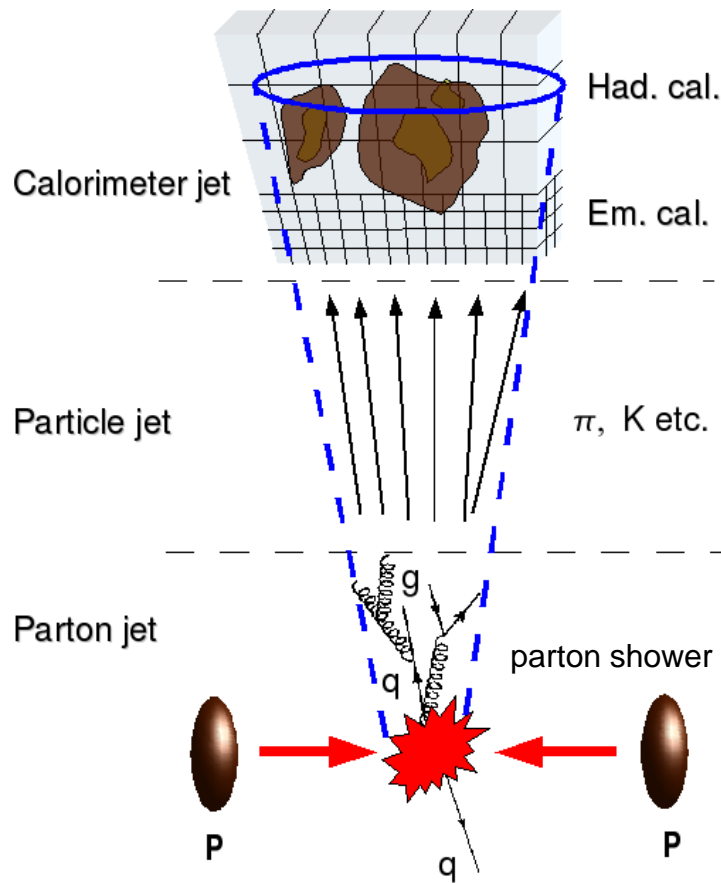


Jet algorithms

Pavel Weber



Evolution of the partonic system



Definition of the jet

- Different, depends on the **algorithm**
- Observation level

Calorimeter jet

- Reconstructed jet after applying jet algorithms
- Uncertainties: Detector properties (non linear response, dead regions noise etc), pile-up

Particle jet

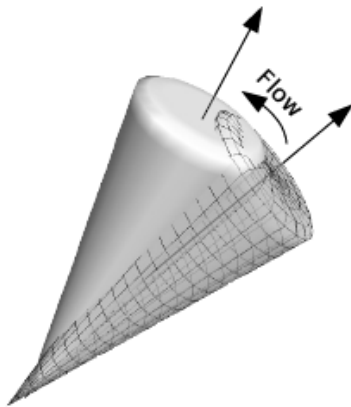
- Particle jets are reconstructed applying jet algorithm to stable particles
- Physics: UE, out-of-cone, pile-up

Parton jet

- Energy of initial parton



ATLAS Cone algorithm

Cone with seed



Cone size: $R \leq \sqrt{\Delta\eta^2 + \Delta\phi^2}$

Reconstruction procedure:

- Find a cone based on seed
- Calculate the centroid (recombination) 
- Redraw cone around the new centre
- Recalculate centroid
- Find stable cone
- Apply split-merge algorithm to separate  jets, depending on energy fraction in overlapping region



Recombination scheme:

E-Scheme or 4-vector recombination

$$p^J = (E^J, p^J) = \sum_{i \in J} (E^i, p_x^i, p_y^i, p_z^i)$$

$$p_T^J = \sqrt{(p_x^J)^2 + (p_y^J)^2}$$

$$y^J = \frac{1}{2} \ln \frac{E^J + p_z^J}{E^J - p_z^J}, \varphi = \tan^{-1} \frac{p_y^J}{p_x^J}$$

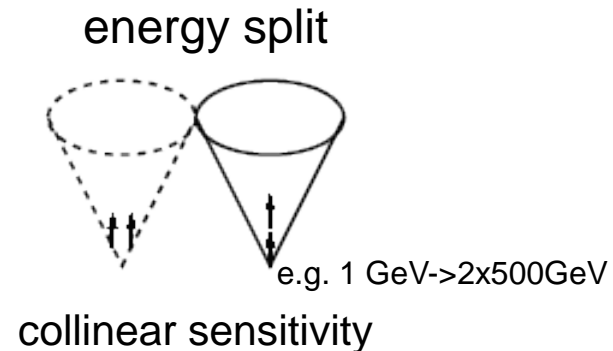
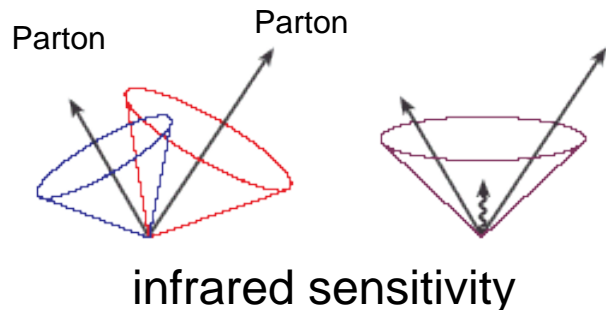
 F = 50-75%

- Energy in overlap > F -> merge
- else split

Theoretical and experimental requirements for jet algorithm

- Experimental:
 - Detector technology independence
 - “Easy” to calibrate
 - High reconstruction efficiency
 - Efficient use of computing resources
- Theoretical:
 - Infrared safety
 - Collinear safety
 - Easy to compare with theory

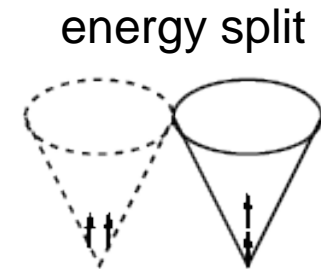
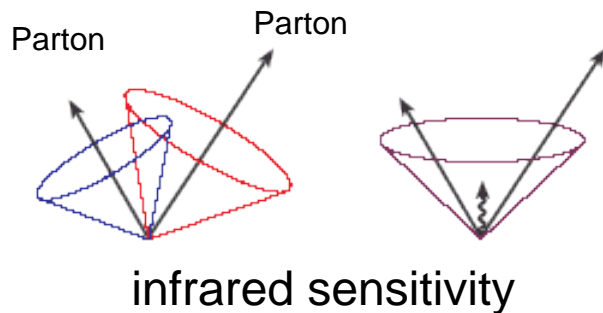
Canonical examples



- Seedless Algorithm resolve the infrared sensitivity, but rather slow
 - Seedless Infrared-Safe Cone – SIScone implemented in ATLAS

Cone Algorithm problems

Canonical examples



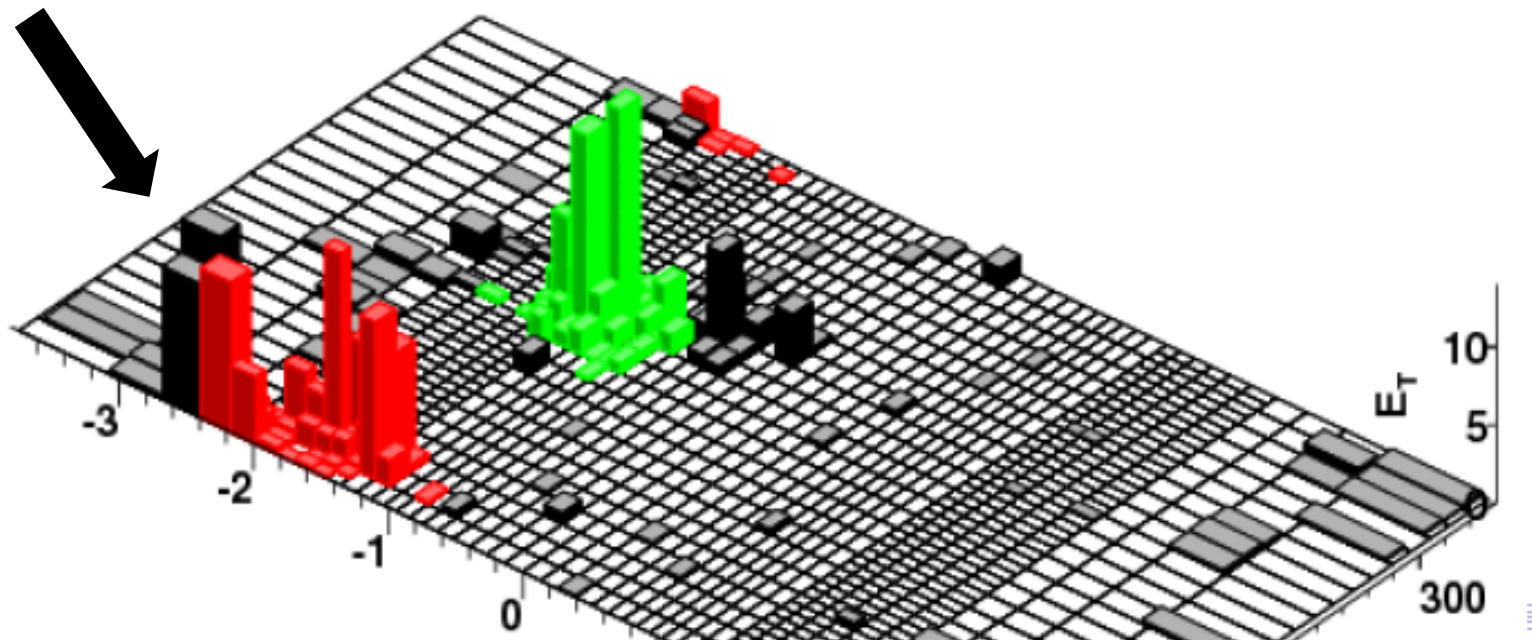
- Seedless Algorithm resolve the infrared sensitivity, but rather slow
 - Seedless Infrared-Safe Cone – SIScone implemented in ATLAS

Dark Tower



Cone Algorithm problems

- Dark towers found in ATLAS when using the Cone algorithm
- These are energetic clusters which are outside any jet in event



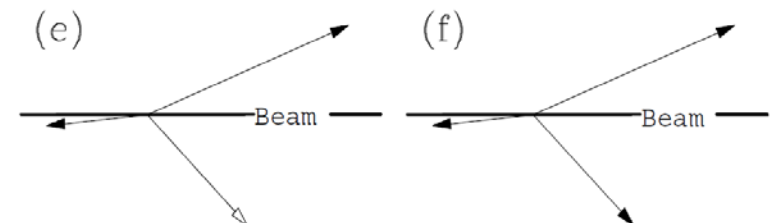
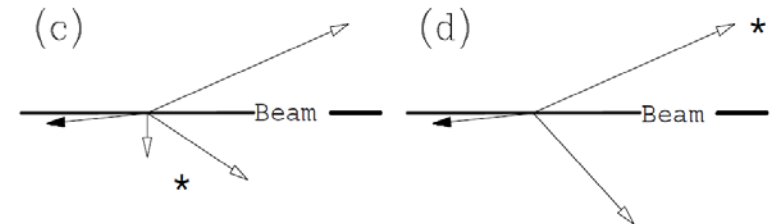
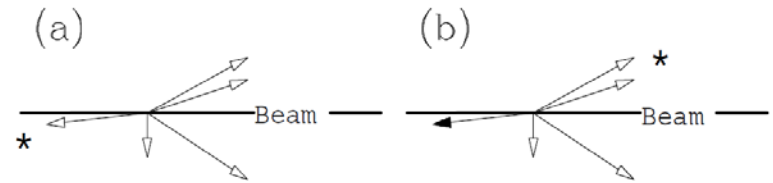
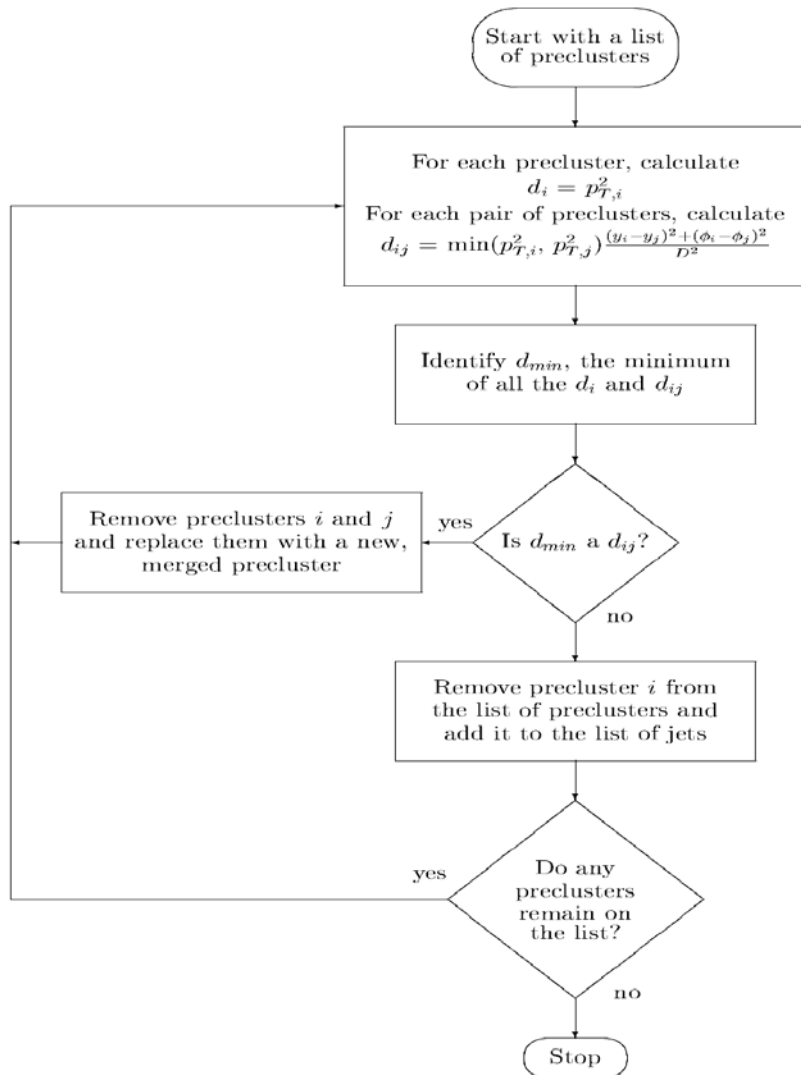
K_T Algorithm



successive recombination of pairs of clusters in an iterative procedure in order of increasing relative P_T

- No seed needed
- Infrared and collinear safe
- No overlapping problem, no spit/merge
- Complex boundaries
- Pile-up problems

K_T Algorithm



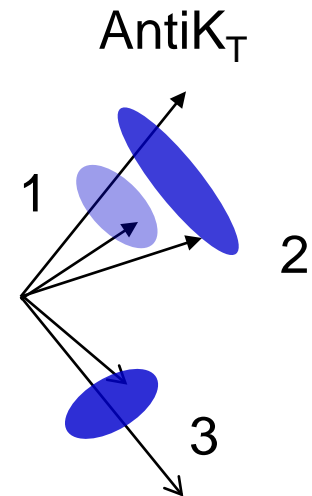
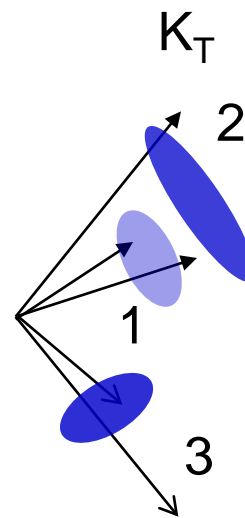
*
Empty arrows – preclusters
Filled arrows – final jets

AntiK_T Algorithm

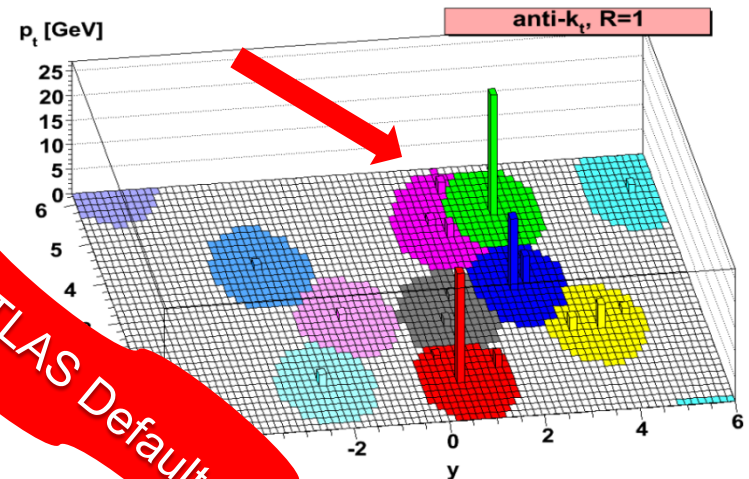
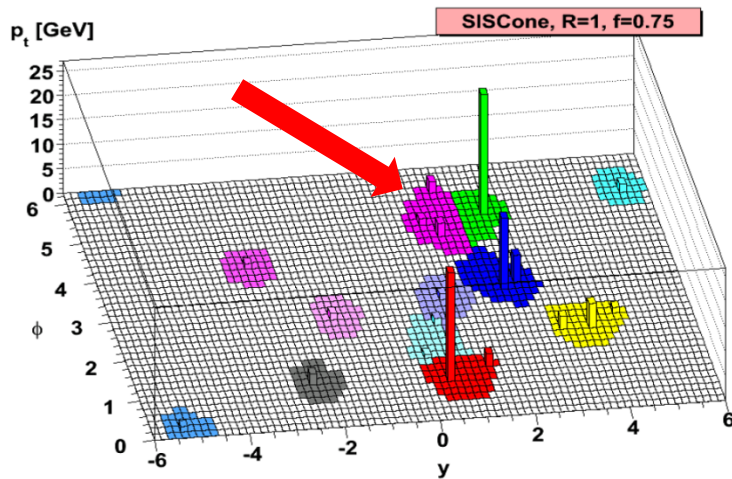
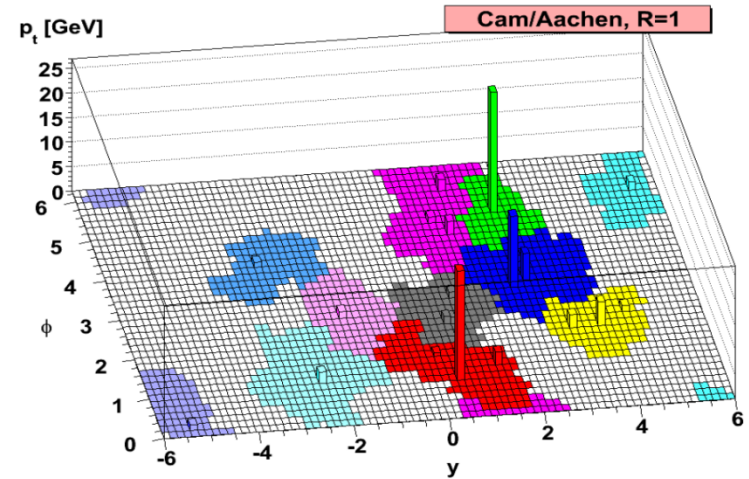
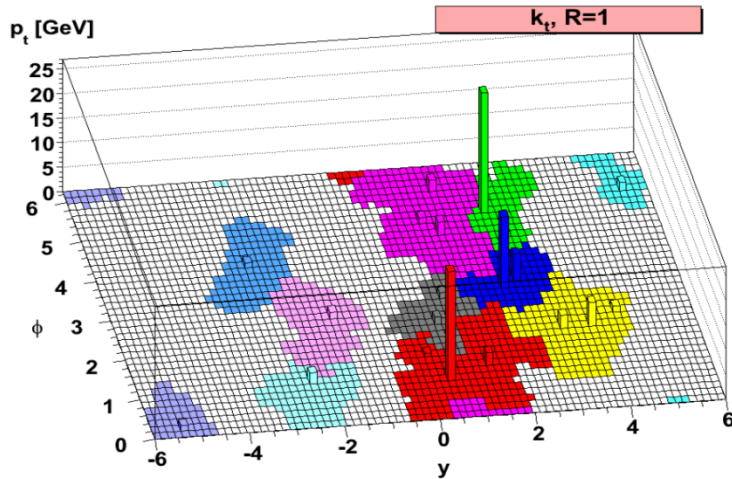
- Similar to the K_T, but:
 - Recombination starts from hardest objects
 - Soft particles tend to cluster with hard ones long before they cluster among themselves
 - Regular boundary shape
 - Shape of the jet is unaffected by soft radiation

$$d_{ij} = \min\left(\frac{1}{p_{Ti}}, \frac{1}{p_{Tj}}\right) \frac{\Delta_{ij}^2}{D^2}$$

$$d_i = \frac{1}{p_{Ti}}$$



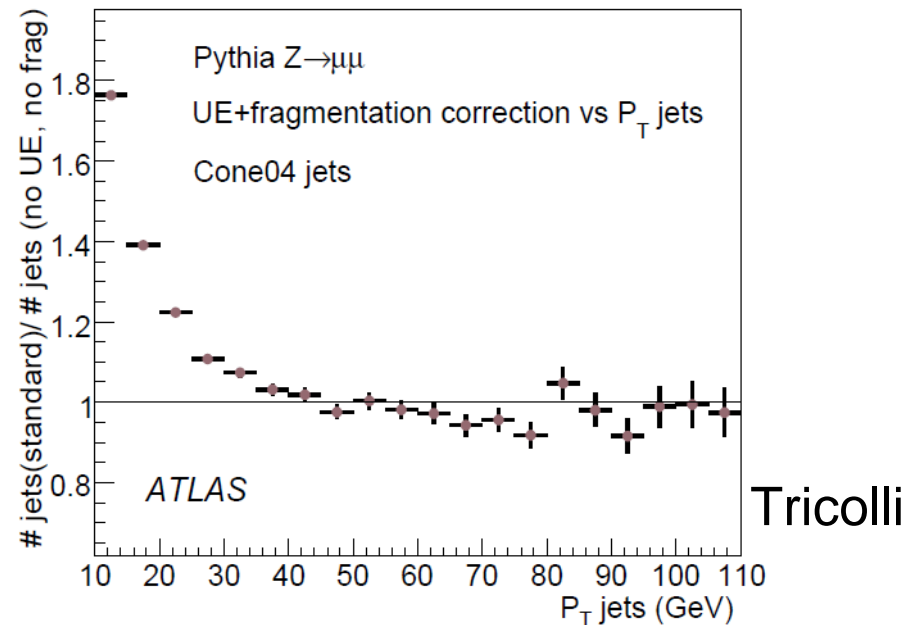
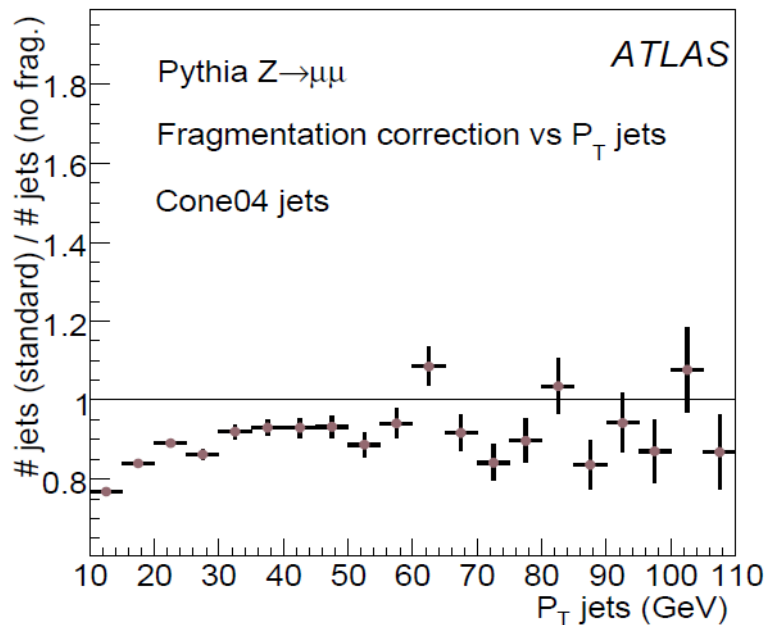
Algorithm Boundaries



ATLAS Default

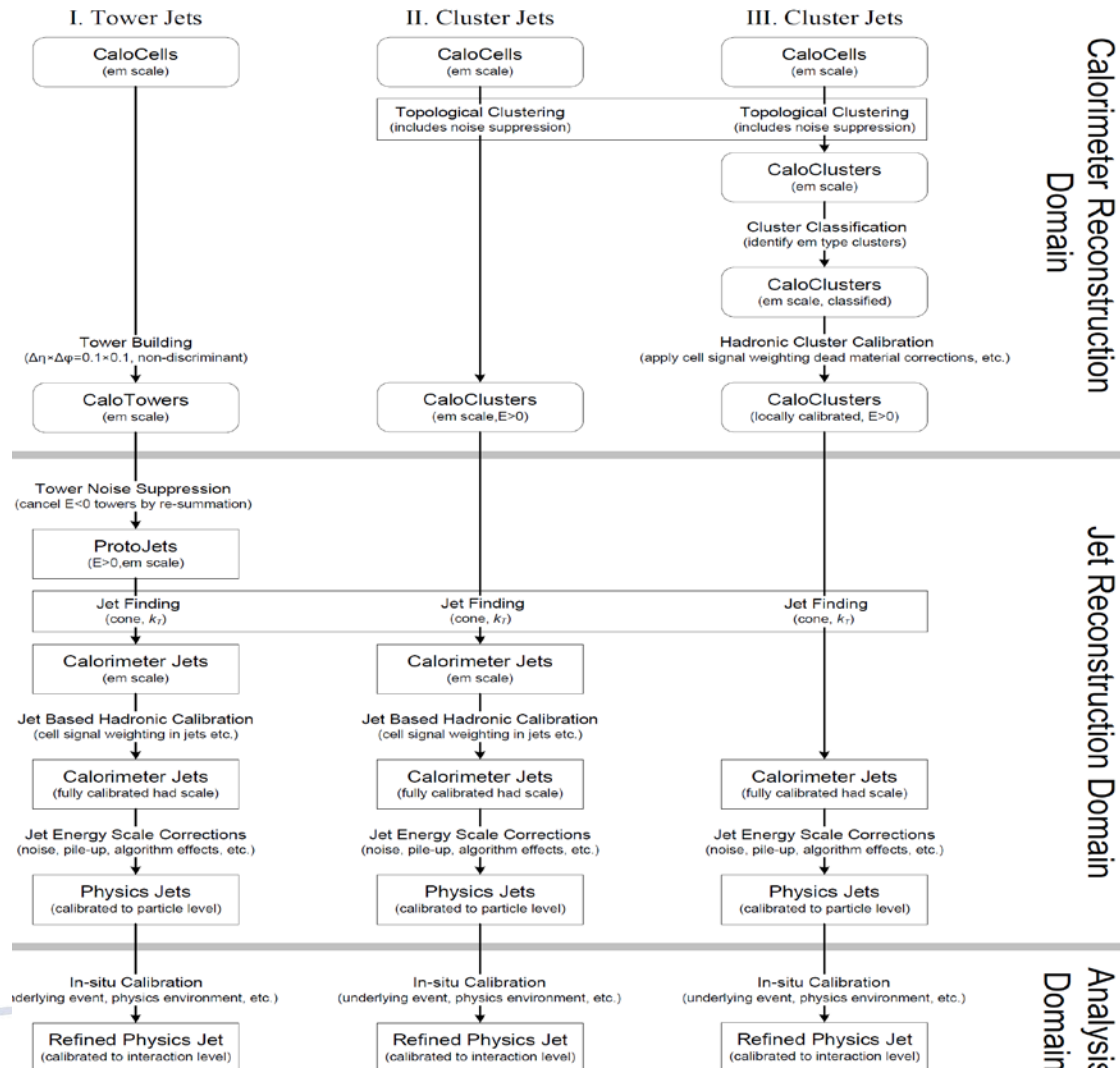
Underlying Event, Fragmentation...

- Underlying Event is known not very well
- Predictions for LHC differ by 30% depending on generator
- Always competitive effects of fragmentation, UE, ISR/FSR



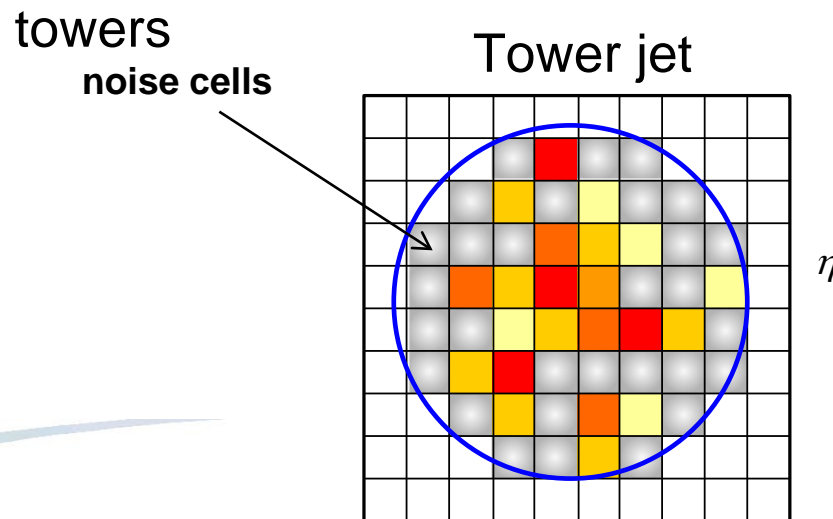
Fragmentation reduces the amount of energy in cone, while UE adds it

Calorimeter Jets Reconstruction



Tower jets

- Tower jets:
 - Input: Calorimeter signal towers – fixed geometry
 - Relatively easy to calibrate
 - Too many non-signal cells included in jet
 - Problematic to use with K_T algorithm
 - Noise tool – cancellation noise neighbor-by-neighbor basis
 - Negative energy towers are cancelled by close-by positive



Cluster Jets

- Topocluster jets:
 - Input: “3-d energy blobs”
 - noise suppression
 - Natural approach, but complication in multistep calibration procedure: e/h, dead material, out-of-cluster corrections etc.

Primary seeds

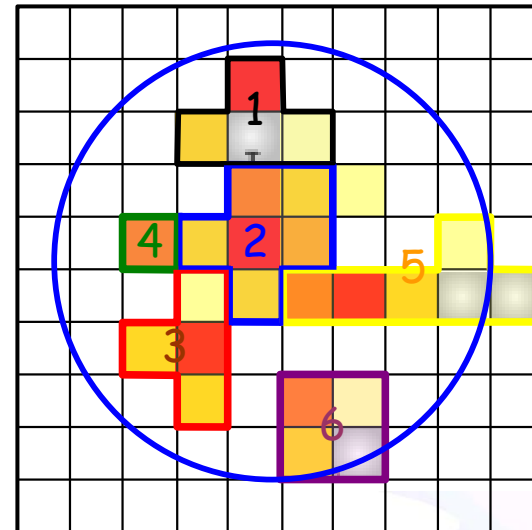
$$\left| \frac{E_{cell}}{\sigma_{cell}^{noise}} \right| > 4$$

Secondary seeds

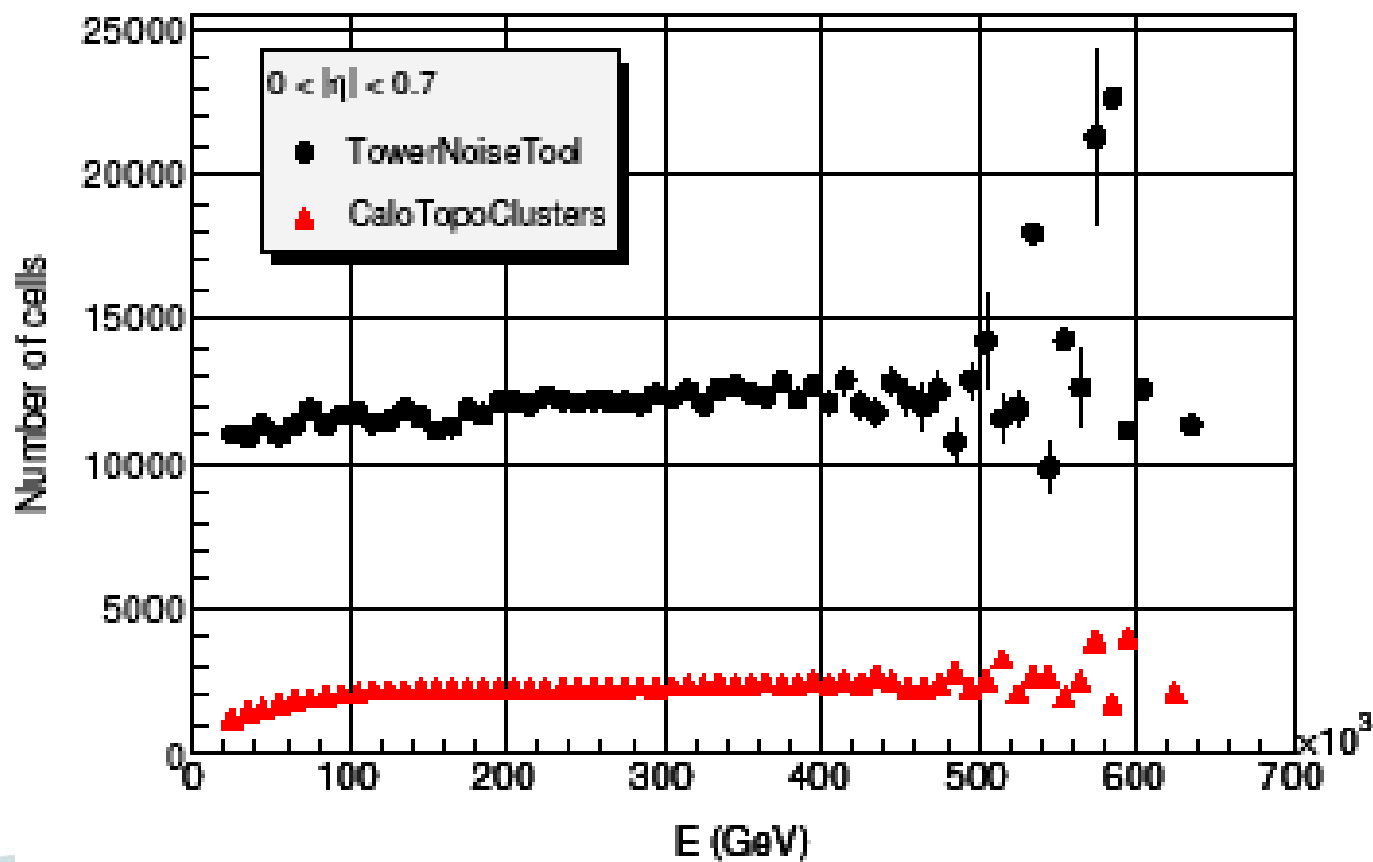
$$\left| \frac{E_{cell}}{\sigma_{cell}^{noise}} \right| > 2$$

Basic threshold

$$\left| \frac{E_{cell}}{\sigma_{cell}^{noise}} \right| > 0$$



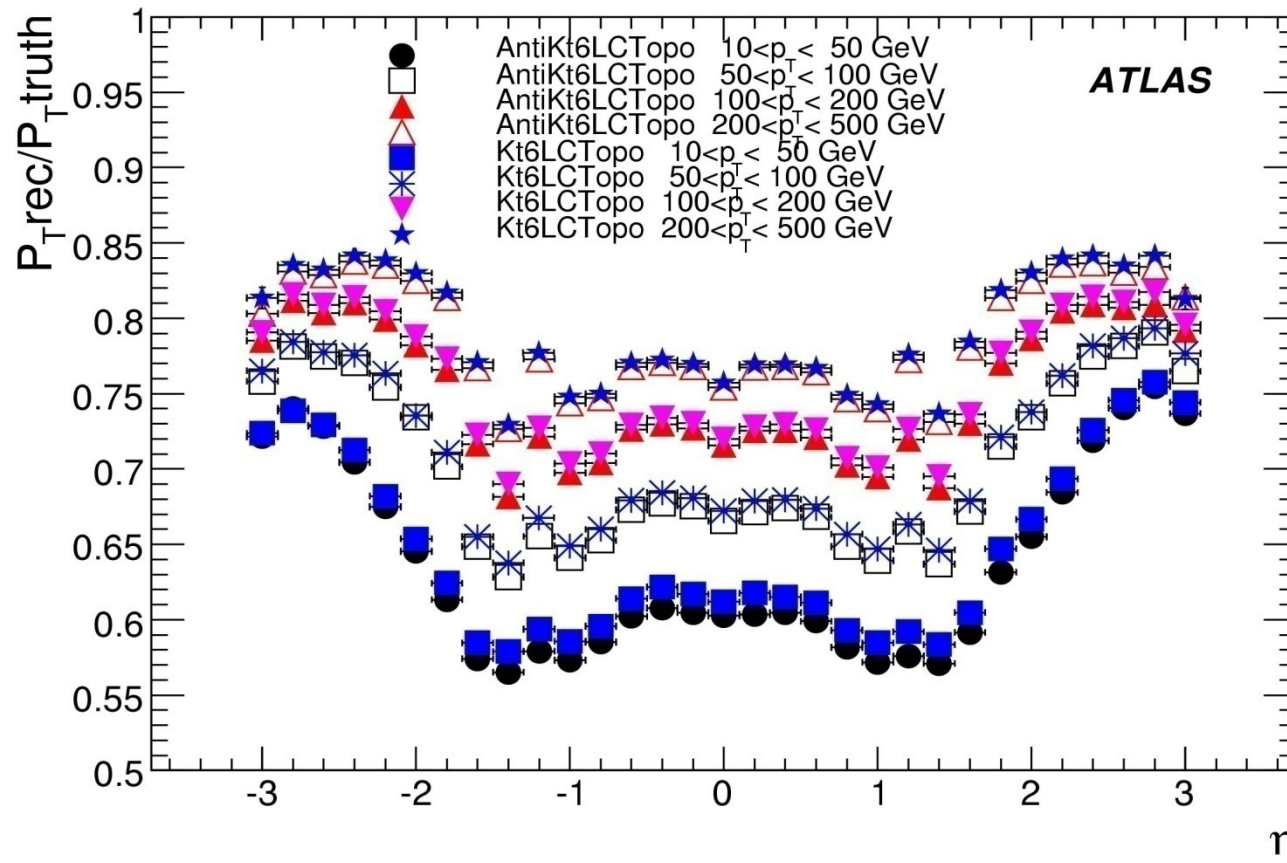
Cluster Jets



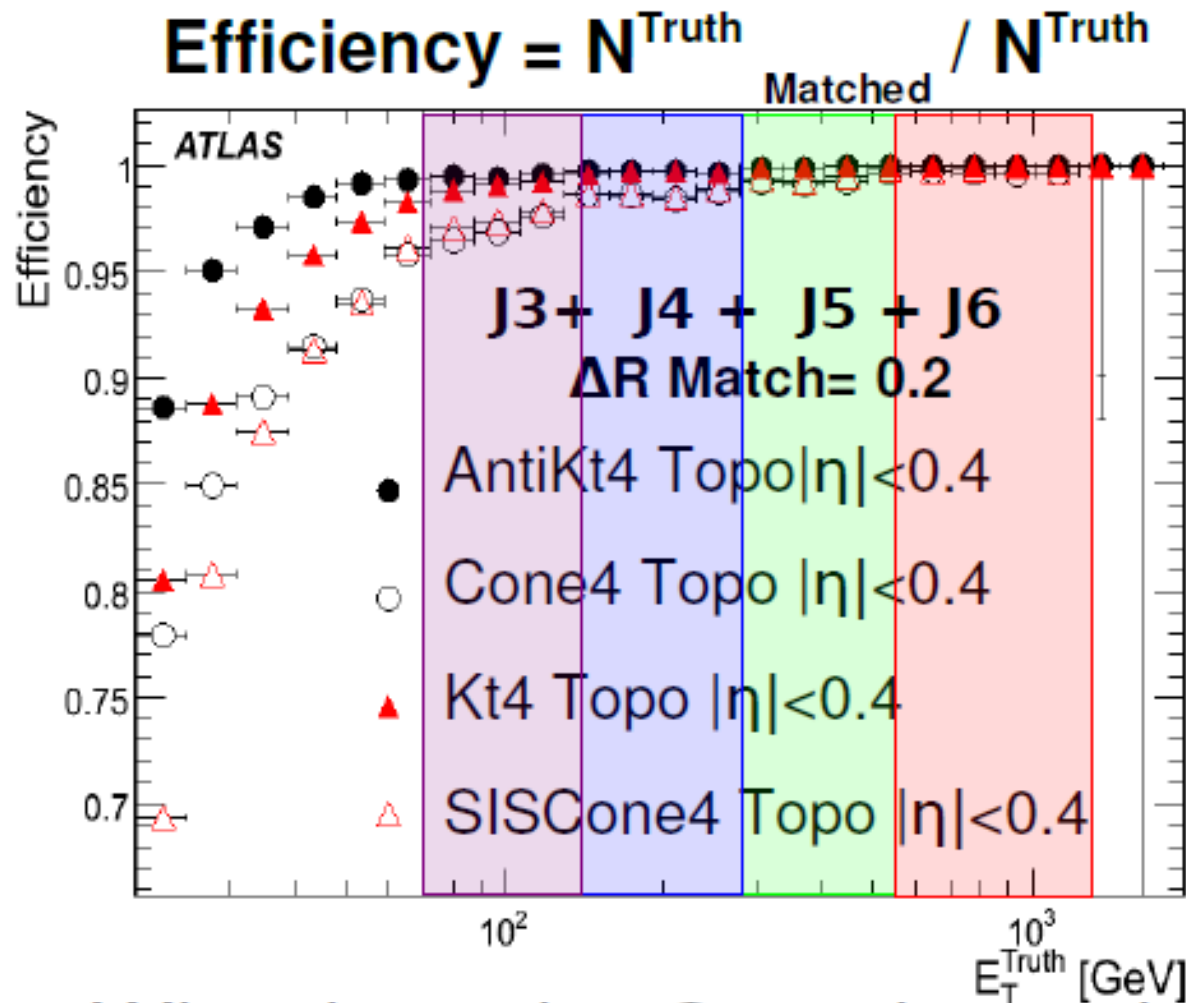
Jet Algorithm Performance

- In MC studies jet at particle level is a reference jet for main quantities:
 - Signal linearity
 - Signal uniformity
 - Energy resolution
 - Reconsturction efficiency
 - Reconsturction purity

Signal Uniformity at em scale



Reconstruction Efficiency

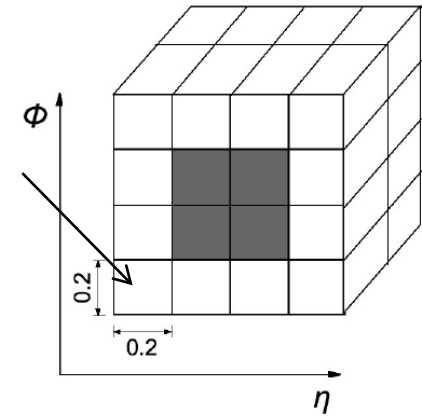


Francavilla

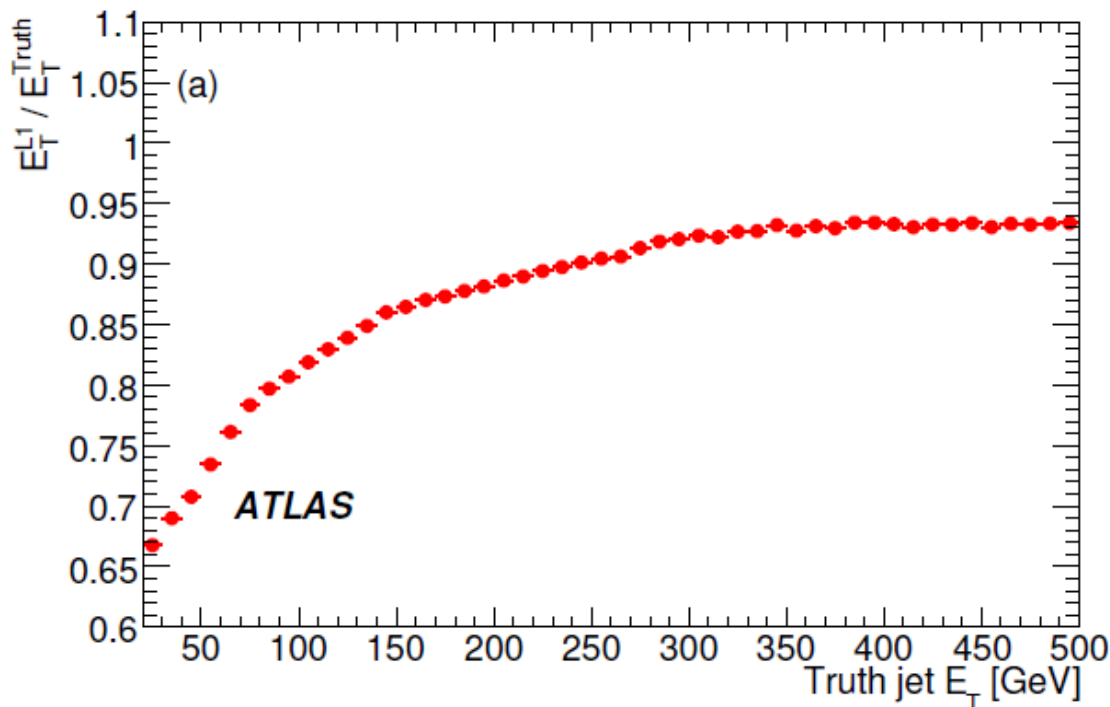
L1 Trigger Jet Performance (linearity)

- Sliding window jet algorithm with different size: 2x2, 3x3, 4x4
- Jet elements as a input for L1 Jet Algorithm

Jet element



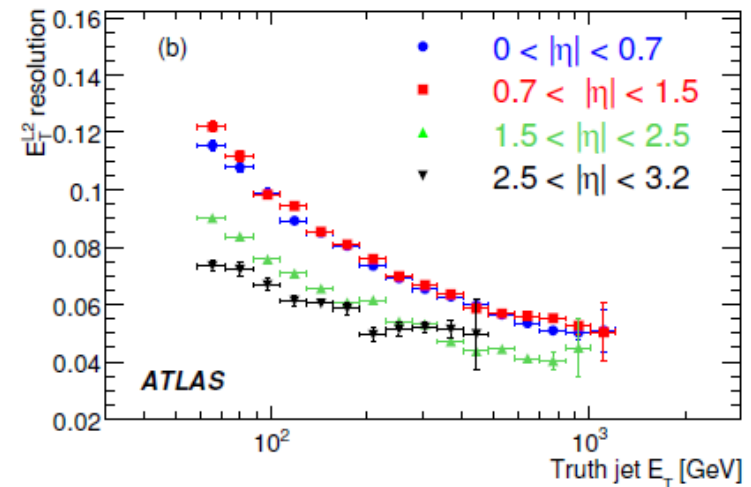
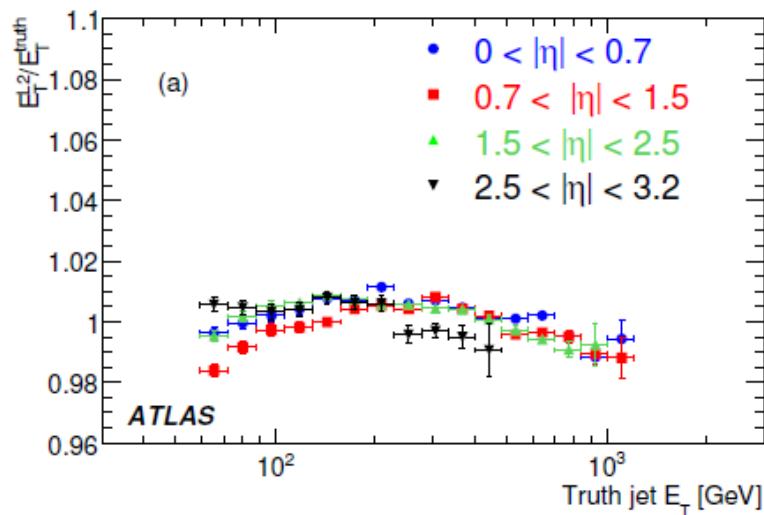
L1 jet algorithm



The L1 jet transverse energy scale as function of truth jet transverse energy

L2 Jet Performance

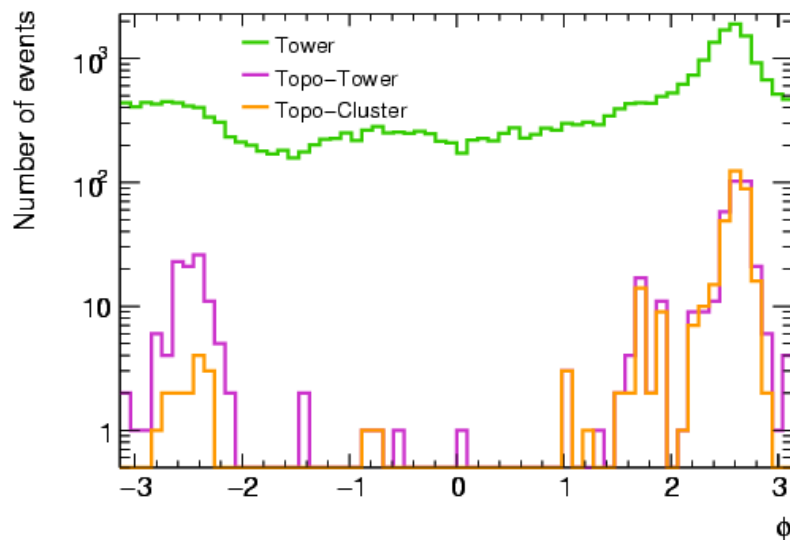
- L2 Jet algorithm is simple iterative cone based on L1 RoI
- Maximum 3 iterations
- Cone $R=0.4$, window size in η ϕ 1.4×1.4
- Simple hadronic calibration based on layers



➤ Jet energy scale and resolution for the L2 jets as a function of the truth jet E_T and pseudorapidity

Algorithm behaviour with random trigger data

- In data taken with random trigger: no jets are expected ...
- Noise can create fake jets in random trigger events
 - Coherent noise in PS $2 < \phi < \pi$
 - Noise in Lar: uniform in ϕ



		Fraction of evts with at least 1 jet (%) ($et > 7\text{GeV}$)		
R	Algo	Towers	Topo towers	Topo clusters
0.4	Cone	0.01	0.01	0.04
	SISCone	0.19	0.04	0.05
	Kt	0.08	0.03	0.04
	AntiKt	0.15	0.04	0.04
0.7	Cone	0.03	0.01	0.06
	SISCone	4.11	0.07	0.06
	Kt	3.02	0.07	0.06
	AntiKt	4.14	0.07	0.05

Nicola Macovec

Acknowledgments

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Backup

