## Resit Exam Software Specification and Testing, January 11, 2016

There are 4 theory questions (T) and 4 lab questions (L).

If you are only taking the resit for theory, you can skip the lab questions, and if you are only taking the resit for lab, you can skip the theory questions.

(T)

A property p on a domain D is a function  $D \to \{\top, \bot\}$ , where  $\top$  and  $\bot$  are the two truth values. A property p on D is stronger than a property q on D if it holds for all  $x \in D$  that p(x) implies q(x). A property p on D is weaker than a property q on D if q is stronger than p. (You have seen these notions during the workshop sessions.)

Which of the following pairs of properties on the integers is stronger?

- 1.  $\lambda x \mapsto x < 3$  and  $\lambda x \mapsto x > x$ .
- 2.  $\lambda x \mapsto x + y = 0$  and  $\lambda x \mapsto x + y \ge 0$ .
- 3.  $\lambda x \mapsto x \ge 0$  and  $\lambda x \mapsto x \le 0$ .
- 4.  $\lambda x \mapsto x^2 > 0$  and  $\lambda x \mapsto x \neq 0$ .
- 5.  $\lambda x \mapsto x y > 0$  and  $\lambda x \mapsto x > y$ .
- (T) Give all symmetric relations on the set  $\{0,1\}$ . Express these relations as sets of pairs, and draw pictures of them.
- (T) Let the relation R on the set  $A = \{0, 1, 2\}$  be given by

$$R = \{(0,1), (1,2)\}.$$

- 1. Determine  $R^{-1}$
- 2. Determine  $R \cup R^{-1}$
- 3. Determine  $R^* \cup (R^{-1})^*$
- 4. Determine  $(R \cup R^{-1})^*$
- (T) Prove with induction:

$$1 + 2 + 2^2 + \dots + 2^n = 2^{n+1} - 1.$$

This is the end of the Theory part.

This is the beginning of the Lab part.

module ResitExam where

import Data.List

import System.Random

import Test.QuickCheck

(L) Let the following function be given:

```
g :: [Int] -> (Int,Int) -> [Int]
g xs (i,j) = take (j-i) (drop i xs)
```

Thus, g xs i j gives the subsequence of xs starting with xs!!i and ending at xs!!(j-1). Here is a check (recall that the first item of a list has index 0).

```
*ResitExam> g [-2,3,-4,11,13,-1] (0,2) [-2,3]

*ResitExam> g [-2,3,-4,11,13,-1] (0,0) []

*ResitExam> g [-2,3,-4,11,13,-1] (2,5) [-4,11,13]
```

Use this to write a function maxval for finding the value of a subsequence with a maximal sum.

This should give:

```
*Main> maxval [-2,3,-4,11,13,-1] 24
```

Test your solution with at least two QuickCheck properties.

(L) Continued from the previous.

The subsequence of [-2, 3, -4, 11, 13, -1] consisting of just [11, 13] has a maximal sum, and this sum is 24.

Write a function

```
maxseq :: [Int] -> [Int]
```

for finding a subsequence of a list of integers with maximal sum.

Your program should give:

```
*ResitExam> maxseq [-2,3,-4,11,13,-1] [11,13]
```

But, of course, a single test case is not enough. Your task is to test your function with QuickCheck.

(L) We have a set of cards with values (positive natural numbers). Example: suppose you have five cards, numbered 1, 2, 3, 4, 5.

The task is to spit this set into two piles X and  $\overline{X}$  (the remaining cards of the set), with the *sum* of the values of the cards in X equal to the *product* of the values of the cards in  $\overline{X}$ .

In the example: if there are just five cards, numbered 1, 2, 3, 4, 5, then there is only one solution, namely [3, 5], for 3 + 5 = 8 and the complement of [3, 5] satisfies 1 \* 2 \* 4 = 8.

Write a program for the general case, and give all solutions for the card set [1, 2, 3, 4, 5, 6, 7, 8, 9, 10]. The type of the solutions function should be:

```
solutions :: [Int] -> [[Int]]
```

For the example case [1, 2, 3, 4, 5] we should get:

```
solutions [1,2,3,4,5] = [[3,5]]
```

for, as we have seen, for this case [3,5] is the only solution.

Give code for solutions. Next, test your code for correctness.

(L) Your programmer Red Curry has written the following function for generating lists of floating point numbers.

He claims that these numbers are random in the half open interval [0..1). Your task is to test whether this claim is correct, by counting the numbers in the quartiles

```
[0..0.25), [0.25..0.5), [0.5..0.75), [0.75..1)
```

and checking whether the proportions between these are as expected.

E.g., if you generate 10000 numbers, then roughly 2500 of them should be in each quartile.

Implement this test, and report on the test results.