

# ST: Lab Assignment 4

Elias El Khaldi Ahanach, Dylan Bartels, Wojciech Czabanski, Quinten Heijn

October 1, 2017

## Assignment 1

**Time required: 4 hours**

1. "The Comprehension Principle. A set is a collection into a whole of definite, distinct objects of our intuition or of our thought." What is meant by definite, distinct objects of our intuition?
2. flexibility of the abstraction notation:  $x \in A \mid P(x)$
3. "In most cases you will have that  $a \neq a$ ". Why not all cases? What is a counter example?
4. In example 4.6, why does  $F$  not belong to  $F$  in the example?
5. Why does 'halts' take 2 arguments: 'funny' and 'funny'? What are the types of arguments in this reasoning?
6. How to show that a set containing an empty set ( $\emptyset$ ) and a set containing a set, containing an empty set ( $\emptyset$ ) are different?
7. How to determine how many elements a power set has of a set with  $n$  elements?
8. Would it be possible to prove that if every number in the domain of input for the program, after transforming using the following formula:  $n_1 = 3n_0 + 1$ , converges, at some point to a power of 2 then the program can halt?

## Assignment 2

**Time required: 4 hours 30 min**

*See code for implementation*

## Assignment 3

**Time required: 3 hours**

Testable properties setIntersection:

- Commutativity =  $A \text{ (Intersect) } B = B \text{ (Intersect) } A$  (p.130)

setUnion:

- Commutativity =  $A \text{ (union) } B = B \text{ (union) } A$  (p.130)
- Contains itself =  $A \text{ (union) } B$  should contain every element from  $A$  (p.130)

setDifference:

- Difference =  $A - B$  (p.127)

## Assignment 4

**Time required: 3 hours**

1. How to show that there are only 13 transitive relations on 0, 1?

## Assignment 5

**Time required: 55 min**

*See code for implementation*

## Assignment 6

**Time required: 30 minutes**

*See code for implementation*

## Assignment 7

**Time required: 90 minutes**

If you interpret a set of relations as a graph,  $n$  is the number of individual nodes in that graph. In the code, we implemented a function that lists all the nodes, and a function that calculates the number of nodes. The number of nodes will be of interest when defining properties for the `trClos` and `symClos` functions.

**For the Symmetric Closure function (`symClos`) we defined the following properties:**

- Length constraint: The length of a `symClos` of  $x$  can at max be double the length of  $x$ , and at least the length of  $x$
- After applying `symClos` once to  $x$ , it should always remain the same no matter how many more times you apply it
- All relations in  $x$  should be in (`symClos`  $x$ )
- No new nodes should be included

**For the Transitive Closure function (`traClos`) we defined the following properties:**

- Length constraint: The length of `trClos`  $x$  should be at least as big as length  $x$  and at most  $n$  squared ( $n$  = number of nodes)
- After applying `trClos` once to  $x$ , it should always remain the same no matter how many more times you apply it
- All relations in  $x$  should be in (`trClos`  $x$ )
- No new nodes should be included

For both properties, we implemented a `quickCheck` test method. The way the test and the properties were implemented can be seen in the code. Example outputs are given below:

```
*Assignment7> quickCheck testTra
+++ OK, passed 100 tests.
*Assignment7> quickCheck testSym
+++ OK, passed 100 tests.
```

## Assignment 8

**Time required: 15 minutes**

After some time brain storming we were able to come up with a counter example:

take  $x = [(1,2)]$

then:  $trClos (symClos x) = [(1,1), (1,2), (2,1), (2,2)]$

but:  $symClos (trClos x) = [(1,2), (2,1)]$

## Bonus Assignment 9

**Time required: 90 minutes**

Properties to test both implementations are:

- $read (show statement) == statement$
- $show (read textStatement) == textStatement$

## Extra Bonus Assignment 10

**Time required: 40**

*See code for implementation*