

# **An Introduction to Database Systems**

## **Chapter 6. Relations**

## 6.2 Tuples

- Given a collection of types  $T_i$  ( $i=1,2,\dots,n$ ), not necessary all distinct, a tuple value on those types –  $t$  – is a set of ordered triples of the form  $\langle A_i, T_i, v_i \rangle$ , where  $A_i$  is an attribute name,  $T_i$  is a type name, and  $v_i$  is a value of type  $t_i$ , and :
- ♦ The value  $n$  is the degree or arity of  $t$ .
  - ♦ The ordered triple  $\langle a_i, T_i, v_i \rangle$  is a component of  $t$ .
  - ♦ The ordered pair  $\langle a_i, T_i \rangle$  is an attribute of  $t$ , and it is uniquely identified by the attribute name  $A_i$ . The value of  $v_i$  is the attribute value for attribute  $A_i$  of  $t$ .
  - ♦ The complete set of attributes is the heading of  $t$ .
  - ♦ The tuple type of  $t$  is determined by the heading of  $t$ , and the heading and that tuple type both have the same attributes and the same degree as  $t$  does.

## 6.2 Tuples

□ The tuple type name is precisely :

- ♦ `TUPLE { A1 T1, A2 T2, ... , An Tn }`
- ♦ heading

MAJOR_P#: P#	MINOR_P#: P#	QTY: QTY
P2	P4	7

♦ Type

- `Tuple { MAJOR_P# P#, MINOR_P# P#, QTY QTY }`

## 6.2 Tuples

### □ Properties of Tuples

- ♦ Every tuple contains exactly one value(of the appropriate type) for each of its attributes
- ♦ There is no left-to-right ordering to the components of a tuple. (a set of components)
- ♦ Every subset of a tuple is a tuple (and every subset of a heading is a heading).

### □ The TUPLE Type Generator

- ♦ `TUPLE { <ATTRIBUTE COMMA LIST> }`
- ♦ `VAR ADDR TUPLE { STREET CHAR,  
CITY CHAR,  
STATE CHAR,  
ZIP CHAR } ;`

## 6.2 Tuples

- ♦ **EX) tuple selector;**

- `TUPLE { STREET '1600 Pennsylvania Ave.' , CITY 'Washington' , STATE 'DC' , ZIP '20500' }`

- **Operators on Tuples**

- ♦ **Tuple equality:** Tuples t1 and t2 are equal if and only if they have the same attributes A1, A2, ..., An and, for all I (i=1,2,, ..., n), the value v1 of Ai in t1 is equal to the value v2 of Ai in t2.

- ♦ **Tuple projection**

- `ADDR { CITY, ZIP } => TUPLE { CITY 'Washington', ZIP '20500' }`

- ♦ **Extract**

- `ZIP FRM ADDR => '20500'`

- ♦ **Tuple type inference – determine the type of the result**

- `ADDR { CITY, ZIP } => TUPLE { CITY CHAR, ZIP CHAR }`

## 6.2 Tuples

- ♦ **WRAP and UNWRAP**

- `TUPLE { NAME NAME, ADDR TUPLE { STREET CHAR, CITY CHAR, STATE CHAR, ZIP CHAR } } ----- TYPE TT1`
- `TUPLE { NAME NAME, STREET CHAR, CITY CHAR, STATE CHAR, ZIP CHAR } } ----- TYPE TT2`
- Let NADDR1 and NADDR2 be tuple var of types TT1 and TT2
- `NADDR1 := NADDR2 WRAP { STREET, CITY, STATE, ZIP } AS ADDR ;` (The result of the expression is of type TT1)
- `NADDR1 UNWRAP ADDR (--- TYPE TT2)`

- ♦ **Tuple Types vs. Possible Representations**

## 6.3 Relation Types(1/8)

- relation variable
  - ♦ variable in the usual programming language sense
- relation value
  - ♦ value of such a variable at any given time
- definition of relation ( a relation value )
  - ♦ Given a collection of  $n$  types  $T_i$  ( $i=1, 2, \dots, n$ ), not necessarily all distinct,  $r$  is a relation on those types if it consists of two parts, a *heading* and a *body*, where :
    - a. The heading is a set of  $n$  attributes of the form  $A_i:T_i$ , where  $A_i$  ( which must all be distinct ) are the *attribute names* of  $r$  and the  $T_i$  are the corresponding *type names* ( $i=1, 2, \dots, n$ ) ;
    - b. The body is a set of  $m$  tuples  $t$ , where  $t$  in turn is a set of components of the form  $A_i:v_i$  in which  $v_i$  is a value of type  $T_i$  - the *attribute value* for attribute  $A_i$  of tuple  $t$  ( $i=1, 2, \dots, n$ ) ;
  - ♦ The values  $m$  and  $n$  are called the cardinality and the degree, respectively, of relation  $r$ .

## 6.3 Relation Types(2/8)

- ♦ in fig 5.1,
  - four underlying types : S#, NAME, STATUS, CITY
  - table have two parts :
    - ✦ row of column headings , set of data rows

- ♦ Set of ordered pairs

(S#, SNAME, STATUS, CITY)



{ S# : S#,  
SNAME : NAME,  
STATUS : STATUS,  
CITY : CITY }

(S1, Smith, 20, London)



{ S# : S# ('S1'),  
SNAME : NAME ('Smith'),  
STATUS : 20,  
CITY : 'London' }



## 6.3 Relation Types(3/8)

- Relation type name
  - ♦  $\text{RELATION} \{ A_1 T_1, A_2 T_2, \dots, A_n T_n \}$
- "Nondistinct types"

*PART-STRUCTURE (MAJOR\_P#, MINOR\_P#, QTY)*

MAJOR_P#: P#	MINOR_P#: P#	QTY: QTY
P1	P2	5
P1	P3	3
P2	P3	2
P2	P4	7
P3	P5	4
P4	P6	8

## 6.4 Relation Values

- The table in Fig. 5.1 can indeed be regarded as a picture of a relation – provided we can agree on how to read such a picture ( rules of interpretation )
- Rules of interpretation
  - ♦ There are some underlying types
  - ♦ Each column corresponds to exactly one of those types
  - ♦ Each row represents a tuple
  - ♦ Each attribute value is a value of the relevant type

*If we can agree on all of these “rules of interpretation” then we can agree that a “table” is a reasonable picture of a relation*

- A Relation is what the definition says it is, namely a abstract kind of object, and a table is a concrete picture of such an abstract object. They are not quite the same. Tabular representation suggests some things that are not true.



*Properties of relations*

## 6.4 Relation Values

### □ Properties of Relations

#### 1. There are no duplicate tuples

- the body of relations is mathematical set of tuples

- SQL permit tables to contain duplicate rows

*(relation and table are not the same thing)*

- corollary

✦ *There is always a primary key*

*( Since tuples are unique, at least, the combination of all attributes of the relations has the uniqueness property)*

#### 2. Tuples are unordered(top to bottom)

- mathematical set property

- reverse sequence of relation : the same relation

- no such things "the fifth tuple", "the 97th tuple", "the next tuple"

- no concept of *positional addressing* and "nextness"

- The rows of a table do have a top-to-bottom ordering, whereas the tuples of a relation do not. *(a relation and a table are not the same thing)*

## 6.4 Relation Values

### □ Properties of relations (cont.)

#### 3. Attributes are unordered(left to right)

- heading of a relation is also defined as a set of attributes
- no such things "the first attribute",...
- no concept of "*nextness*"
  - ✦ attributes are always referenced by name never by position
- The columns of a table obviously do have a left-to-right ordering, but the attributes of a relation do not

#### 4. Each value contains exactly one value for each attribute

- A tuple is a set of  $n$  components or ordered pairs of the form  $A_i:v_i$  (  $i=1, 2, \dots, n$  ) ( by definition )
- A relation that satisfies this property is said to be normalized (first normal form ( 1NF ) )

# 6.4 Relation Values

- Relation-Valued Attributes
  - ♦ The values that make up a type can be of any kind at all.  
We can have a type whose values are relations

S#	SNAME	STATUS	CITY	PQ										
S1	Smith	20	London	<table><tr><th>P#</th><th>QTY</th></tr><tr><td>P1</td><td>300</td></tr><tr><td>P2</td><td>200</td></tr><tr><td>...</td><td>...</td></tr><tr><td>P6</td><td>100</td></tr></table>	P#	QTY	P1	300	P2	200	...	...	P6	100
P#	QTY													
P1	300													
P2	200													
...	...													
P6	100													
S2	Jones	10	Paris	<table><tr><th>P#</th><th>QTY</th></tr><tr><td>P1</td><td>300</td></tr><tr><td>P2</td><td>400</td></tr></table>	P#	QTY	P1	300	P2	400				
P#	QTY													
P1	300													
P2	400													
...	...	...	.....	.....										
S5	Adams	30	Athens	<table><tr><th>P#</th><th>QTY</th></tr><tr><td></td><td></td></tr></table>	P#	QTY								
P#	QTY													

## 6.4 Relation Values

### □ Relation and Their Interpretation

- ♦ (a) The heading of any given relation can be regarded as a predicate, and (b) the tuples of that relation can be regarded as true propositions, obtained from the predicate by substituting values of the appropriate type for the parameters of that predicate.
- ♦ Closed World Assumption :
  - If a valid tuple does not appear in the body of the relation, then we can assume the corresponding proposition is false.

## 6.5 Relation Variables(1/6)

### □ Base Relvar Definition

- ♦ syntax :

```
VAR      <relvar name>      BASE      <relation type>
                                             <candidate key definition list>
                                             [ <foreign key definition list> ] ;
```

<relation type> :

```
RELATION { <attribute commalist> }
```

<attribute> :

```
<attribute name> <type name>
```

## 6.5 Relation Variables(2/6)

□ Example for the suppliers and parts database

VAR	S	BASE	RELATION
	{ S#	S#,	
	SNAME	NAME,	
	STATUS	INTEGER,	
	CITY	CHAR }	
	PRIMARY KEY { S# };		
VAR	P	BASE	RELATION
	{ P#	P#,	
	PNAME	NAME,	
	COLOR	COLOR,	
	WEIGHT	WEIGHT,	
	CITY	CHAR }	
	PRIMARY KEY { P# };		

VAR	SP	BASE	RELATION
	{ S#	S#,	
	P#	P#,	
	QTY	QTY }	
	PRIMARY KEY { S#, P# }		
	FOREIGN KEY { S# } REFERENCES S		
	FOREIGN KEY { P# } REFERENCES P;		



## 6.5 Relation Variables(3/6)

□ **Explanation :**

1. types of these 3 base relvars

**RELATION is a type generator**

2. All possible relation values are of the same relation type
3. All interpretation
4. Cataloging
5. Candidate key definition
6. Foreign key definition

□ **DROP VAR < relvar name >**

## 5.4 Relation Variables(4/6)

### □ Updating Relvar

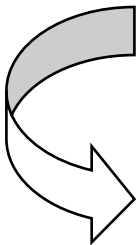
<relvar name> := <relational expression> ;

Tutorial D syntax

VAR R BASE RELATION


{ S# S#, SNAME NAME, STATUS INTEER, CITY CHAR } ... ;

- R := S ;
- R := S WHERE CITY = 'London' ;
- R := S MINUS ( S WHERE CITY = 'Paris' ) ;
- S := S WHERE CITY = 'London' ;
- S := S MINUS ( S WHERE CITY = 'Paris' ) ;



## 5.4 Relation Variables(5/6)

▪ INSERT INTO S

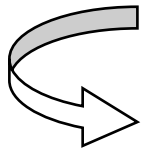


```
RELATION { TUPLE { S# S# ( 'S6' ),  
                    SNAME NAME ( 'Smith' ),  
                    STATUS 50,  
                    CITY 'Rome' } };
```

S := S UNION

```
RELATION { TUPLE { S# S# ( 'S6' ),  
                    SNAME NAME ( 'Smith' ),  
                    STATUS 50,  
                    CITY 'Rome' } };
```

## 5.4 Relation Variables(6/6)



▪ DELETE S WHERE CITY = 'Paris' ;

S := S MINUS ( S WHERE CITY = 'Paris' ) ;

▪ UPDATE S WHERE CITY = 'Paris'

STATUS := 2 \* STATUS,

CITY := 'Rome' ;

The assignment equivalent see reference [3.3].

▪ syntax of INSERT, DELETE and UPDATE :

▪ INSERT INTO <relvar name> <relational expression> ;

▪ DELETE <relvar name> [ WHERE <boolean expression> ] ;

▪ UPDATE <relvar name> [ WHERE <boolean expression> ]

<attribute update commalist> ;

## 6.6 SQL Facilities

- Rows
- SQL does not support tuples; it supports rows, which have a left-to-right ordering to their components.
  - ♦ ROW ( P# ( 'P2' ), P# ( 'P4' ), QTY ( 7 ) )
  - ♦ ROW type constructor (its counterpart to TUPLE type generator)
- Table Types
  - ♦ SQL does not support relations; it supports tables.
- Table Values and variables

## 6.6 SQL Facilities

### □ Table Values and Variables

- 1) SQL tables are allowed to include duplicate rows ( not necessarily a primary key )
- 2) SQL tables are considered to have a left-to-right column ordering

### □ Base Table :

CREATE TABLE <base table name>

( <base table element commalist> );

- ♦ <base table element> is either a <column definition> or a <constraint>
- ♦ <column definition>
  - <column name> <type name> [ <default spec> ]
- ♦ <default spec> defines the default value or default
- ♦ NULL : default default
- ♦ Fig. 4.1

## 6.6 SQL Facilities

### □ DROP TABLE

**DROP TABLE <base table name> <option> ;**

- ♦ **option : RESTRICT or CASCADE**
- 1) **If RESTRICT is specified and the base table is referenced in an view definition or integrity constraint, the DROP will fail.**
- 2) **If CASCADE is specified, the DROP will succeed ( dropping the table and deleting all of its rows ), and any referencing view definitions and integrity constraints will be dropped also.**

## 6.6 SQL Facilities

### □ ALTER TABLE statement :

- ♦ A new column can be added;
- ♦ A new default can be defined for an existing column;
- ♦ An existing column default can be deleted;
- ♦ An existing column can be deleted;
- ♦ A new integrity constraint can be specified;
- ♦ An existing integrity constraint can be deleted

ex) ALTER TABLE S ADD COLUMN DISTINCT INTEGER DEFALUT -1 ;



## 6.6 SQL Facilities

### □ Structured Types

- ♦ CREATE TYPE POINT AS ( X FLOAT, Y FLOAT ) NOT FINAL ;
- ♦ CREATE TABLE NADDR

```
( NAME ... ,  
  ADDR ... ,  
  LOCATION POINT ...,  
  ... )
```

```
SELECT  NT.LOCATION.X, NT.LOCATION.Y  
FROM    NADDR AS NT  
WHERE   NAME = ... ;
```

```
UPDATE  NADDR AS NT  
SET     NT.LOCATION.X = 5.0  
WHERE   NAME = ... ;
```

## 6.6 SQL Facilities

```
CREATE TYPE POINT1 AS ( X FLOAT, Y FLOAT ) NOT FINAL ;  
CREATE TYPE POINT2 AS ( X FLOAT, Y FLOAT ) NOT FINAL ;  
DECLARE V1 POINT1 ;  
DECLARE V2 POINT2 ;
```

variables V1 and V2 are of different types.