0.80581147

0.38348503

0.6652413

0.64155897

0.24070017

0.35429554

0.70827991

0.32318987

0.8708774

0.22902348

2.27515993

-0.15308204

1.41590601

0.79686399

-0.45275524

2.03862963

1.16148089

2.68814558

0.7010376

0.04881045

$$h_{\alpha}(x) = Q_{\alpha} + Q_{\alpha}x$$

$$J(Q_0,Q_1) = \frac{1}{2n} \sum_{i=1}^{m} (ha(X_{1i}) - y_i)^2$$

m = len(x)

m = 10

$$J(00,01) = \frac{1}{27N} \left(0.0 + 0.80581101 - 2.27515 \right)^{2} + \left(0.0 + 0.3834850, + 0.15308 \right)^{2}$$
(convex function)
$$+ \left(0.0 + 0.665240, -1.43590 \right)^{2} + \left(0.0 + 0.6415590, -0.79686 \right)^{2}$$

$$+ \left(0.0 + 0.240700, + 0.45275 \right)^{2} + \left(0.0 + 0.354290, -2.03863 \right)^{2}$$

$$+ \left(0.0 + 0.708280, -1.16148 \right)^{2} + \left(0.0 + 0.323790, -2.68814 \right)^{2}$$

$$+ \left(0.0 + 0.870870, -0.701103 \right)^{2} + \left(0.0 + 0.229020, -0.048810 \right)^{2}$$

$$\frac{\partial J}{\partial \theta_0} = \frac{1}{m} \sum_{i=1}^{m} -\left(h_0\left(x_{2i}\right) - y_i\right) \qquad \theta_0 = 0, -\alpha \frac{\partial J}{\partial \theta_0}.$$

1 = 1 - x; (ho(x1i) - yi)

0, = 0, - ~ 0 1/000

$$-\left(\alpha_{0} + 0.66524\alpha_{1} - 1.43590\right) - \left(\alpha_{0} + 0.641559\alpha_{1} - 0.79686\right)$$

$$-\left(\alpha_{1} + 0.24070\alpha_{1} + 0.45275\right) - \left(\alpha_{0} + 0.35429\alpha_{1} - 2.03863\right)$$

$$-\left(\alpha_{1} + 0.70828\alpha_{1} - 1.16148\right) - \left(\alpha_{1} + 0.32279\alpha_{1} - 2.68814\right)$$

$$-\left(\alpha_{1} + 0.87087\alpha_{1} - 0.701103\right) - \left(\alpha_{0} + 0.22902\alpha_{1} - 0.048810\right)$$

$$-\left(0.805611\left(\alpha_{0} + \alpha_{1}\left(0.805811\right) - 2.27715\right)\right) - \left(0.38348\left(\alpha_{0} + 0.38348\alpha_{1} + 0.15308\right)\right)$$

$$-\left(0.66524\left(\alpha_{0} + 0.66524\alpha_{1} - 1.42790\right)\right) - \left(0.641559\left(\alpha_{0} + 0.641559\alpha_{1} - 0.79682\right)\right)$$

$$-\left(0.66524\left(\alpha_{0} + 0.66524\alpha_{1} - 1.42790\right)\right) - \left(0.541559\left(\alpha_{0} + 0.641559\alpha_{1} - 0.79682\right)\right)$$

$$-\left(0.70828\left(\alpha_{1} + 0.70828\alpha_{1} - 1.16148\right)\right) - \left(0.32779\left(\alpha_{0} + 0.32779\alpha_{1} - 2.68814\right)\right)$$

$$-\left(0.87081\left(\alpha_{0} + 0.87087\alpha_{1} - 0.701103\right)\right) - \left(0.22902\left(\alpha_{0} + \alpha_{1} + 2.2902\alpha_{1} - \alpha.048810\right)\right)$$

35(5) = = = (0.805811) - 2.27515) - (0.40.383480, +0.15308)

#	tetha 0	tetho 2	J
1	0	0	1.066335
2	0.737818	0.431844	0.491165
3	0.801275	0.495645	0.484387
4	0.796986	0.521724	0.483450

```
· First iteration
 initially,
      00 =0
      Q1 = 0.
     m = len(x)
     m = 10.
     J(0,0) = 1.066335.
       \frac{\partial J}{\partial Q} = \frac{1}{m} \sum_{i=1}^{m} - \left( h_{o}(x_{1i}) - y_{i} \right)
        at (0,0),
        \frac{\partial 5}{\partial 8} = -1.054026
        \frac{\partial J}{\partial a_i} = \frac{1}{m} \sum_{i=1}^{m} - \chi_i \left( h_0(\chi_{2i}) - y_i \right)
        at (0,0),
         \frac{\partial J}{\partial \alpha_i} = -0.616920.
     new Q_0 = Q_0 - \alpha * \frac{\partial T}{\partial Q_0}
         0.0 = 0.7 * -1.054026.
             0. = 0.737818
    new Q_1 = Q_1 - \alpha * \frac{\partial J}{\partial Q_1}
              0, = 0 - 0.7 * -0.616920.
              Q_1 = 0.431844.
```

J (0.737818, 0.431844) = 0.491165.

```
second iteration
```

at which the cost is 0.491165.

$$\frac{\partial J}{\partial \theta_0} = -0.090652$$

$$\frac{\partial J}{\partial Q_1} = -0.091144$$

new
$$0_0 = 0_0 - x + \frac{\partial J}{\partial 0_0}$$

$$\Delta_0 = 0.737818 - 0.7 * (-0.0906252)$$

new
$$0_1 = 0_1 - x * \frac{\partial J}{\partial a_1}$$

$$Q_1 = 0.431844 - 0.7 \times (-0.091144)$$

Third iteration

initially,

at which the cost is 0.484387.

$$\frac{\partial J}{\partial \theta_0} = 0.061279.$$

$$\frac{\partial J}{\partial Q} = -0.037256.$$

new
$$\theta_0 = \theta_0 - \alpha * \frac{\partial J}{\partial \theta_0}$$

New
$$Q_1 = Q_1 - \alpha \frac{\partial T}{\partial Q_1}$$

 $Q_1 = 0.495647 - 0.7*(-0.037256)$
 $Q_1 = 0.521724$