```
!pip install umap-learn
     Collecting uman-learn
       Downloading umap-learn-0.5.5.tar.gz (90 kB)
                                                  - 90.9/90.9 kB 1.3 MB/s eta 0:00:00
       Preparing metadata (setup.py) ... done
     Requirement already satisfied: numpy>=1.17 in /usr/local/lib/python3.10/dist-packages (from umap-learn) (1.23.5)
     Requirement already satisfied: scipy>=1.3.1 in /usr/local/lib/python3.10/dist-packages (from umap-learn) (1.11.3)
     Requirement already satisfied: scikit-learn>=0.22 in /usr/local/lib/python3.10/dist-packages (from umap-learn) (1.2.2)
     Requirement already satisfied: numba>=0.51.2 in /usr/local/lib/python3.10/dist-packages (from umap-learn) (0.58.1)
     Collecting pynndescent>=0.5 (from umap-learn)
       Downloading pynndescent-0.5.11-py3-none-any.whl (55 kB)
                                                   55.8/55.8 kB 6.7 MB/s eta 0:00:00
     Requirement already satisfied: tqdm in /usr/local/lib/python3.10/dist-packages (from umap-learn) (4.66.1)
     Requirement already satisfied: llvmlite<0.42,>=0.41.0dev0 in /usr/local/lib/python3.10/dist-packages (from numba>=0.51.2->umap-learn) (@
     Requirement already satisfied: joblib>=0.11 in /usr/local/lib/python3.10/dist-packages (from pynndescent>=0.5->umap-learn) (1.3.2)
     Requirement already satisfied: threadpoolctl>=2.0.0 in /usr/local/lib/python3.10/dist-packages (from scikit-learn>=0.22->umap-learn) (3.
     Building wheels for collected packages: umap-learn
       Building wheel for umap-learn (setup.py) ... done
       Created wheel for umap-learn: filename=umap learn-0.5.5-py3-none-any.whl size=86831 sha256=22a2408bbb51dfeb32e14b4d4dc13a66c88b757bbf8
       Stored in directory: /root/.cache/pip/wheels/3a/70/07/428d2b58660a1a3b431db59b806a10da736612ebbc66c1bcc5
     Successfully built umap-learn
     Installing collected packages: pynndescent, umap-learn
     Successfully installed pynndescent-0.5.11 umap-learn-0.5.5
import pandas as pd
import numpy as np
import seaborn as sns
import matplotlib.pyplot as plt
from sklearn.decomposition import PCA
from sklearn.preprocessing import StandardScaler
import umap
from sklearn.manifold import TSNE
from sklearn.linear_model import LinearRegression
import sklearn.metrics as metrics
from sklearn.model_selection import train_test_split
from \ sklearn.model\_selection \ import \ cross\_val\_score
from sklearn.model_selection import GridSearchCV
from sklearn.tree import DecisionTreeRegressor
from sklearn.ensemble import RandomForestRegressor
boston_housing=pd.read_csv("BostonHousing.csv",header=0)
boston_housing.head()
           crim
                   zn indus chas
                                                        dis rad tax ptratio
                                                                                     b 1stat
                                     nox
                                            rm age
      0 0.00632 18.0
                        2.31
                                0 0.538 6.575 65.2 4.0900
                                                               1 296
                                                                           15.3 396.90
                                                                                         4.98
      1 0.02731
                                0 0.469 6.421 78.9 4.9671
                                                               2 242
                                                                           17.8 396.90
                                                                                         9.14
                  0.0
                        7.07
      2 0.02729
                  0.0
                        7.07
                                         7.185
                                                     4.9671
                                                               2 242
                                                                           17.8 392.83
                                                                                         4.03
                                0 0.469
                                                61.1
        0.03237
                                                               3 222
                  0.0
                        2.18
                                0 0.458 6.998 45.8 6.0622
                                                                           18.7 394.63
                                                                                         2.94
         0 06006
                  Λ Λ
                                   0 150
                                          7 1/17
                                                E4 2 6 0622
                                                                                306 00
boston_housing.dtypes
     crim
                float64
                float64
                float64
     indus
     chas
                  int64
                float64
     nox
                float64
     rm
                float64
     age
                float64
```

```
rad int64
tax int64
ptratio float64
b float64
lstat float64
medv float64
dtype: object
```

```
boston_housing.isnull().sum()
```

```
crim
           0
zn
           0
indus
           0
chas
           0
nox
           0
           5
           0
age
           0
dis
           0
rad
           0
           0
ptratio
           0
b
lstat
           0
medv
           0
dtype: int64
```

```
boston_housing['rm'].index[boston_housing['rm'].apply(np.isnan)]
```

Int64Index([10, 35, 63, 96, 135], dtype='int64')

boston\_housing.describe()

	crim	zn	indus	chas	nox	rm	age
count	506.000000	506.000000	506.000000	506.000000	506.000000	501.000000	506.000000
mean	3.613524	11.363636	11.136779	0.069170	0.554695	6.284341	68.574901
std	8.601545	23.322453	6.860353	0.253994	0.115878	0.705587	28.148861
min	0.006320	0.000000	0.460000	0.000000	0.385000	3.561000	2.900000
25%	0.082045	0.000000	5.190000	0.000000	0.449000	5.884000	45.025000
50%	0.256510	0.000000	9.690000	0.000000	0.538000	6.208000	77.500000
75%	3.677083	12.500000	18.100000	0.000000	0.624000	6.625000	94.075000
mav •	<u> </u>	100 000000	27 7/10000	1 000000	Λ 971ΛΛΛ	8 48UUUU	100 000000

At this point we have so far seen the structure of the overall data. We see that the 'rm' column has 5 null/NaN values which will need to be addressed. The types seem to have been inferred correctly as we see no object type columns meaning all columns contain values of same type

```
boston_housing.median()
```

```
crim
             0.25651
             0.00000
indus
             9.69000
chas
             0.00000
nox
             0.53800
             6.20800
rm
            77.50000
age
             3.20745
dis
             5.00000
rad
tax
           330.00000
            19.05000
ptratio
           391.44000
            11.36000
lstat
medv
            21.20000
dtype: float64
```

The mean and median of 'rm' are very similar so it could be a good try to replace the 5 missing values with either mean or median.

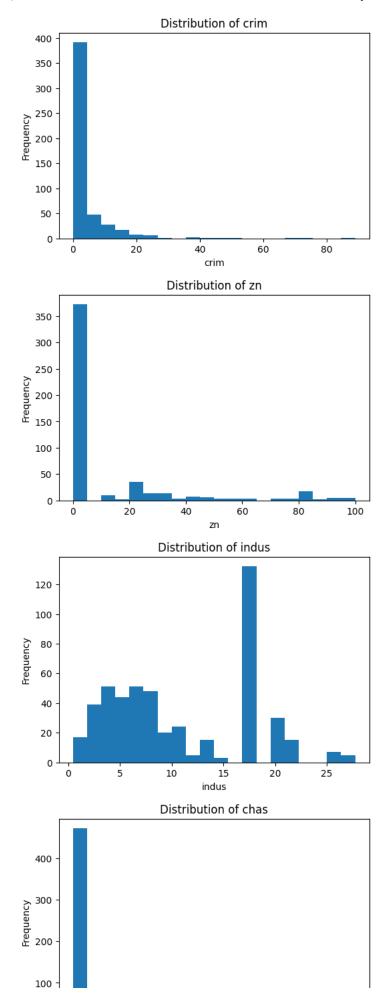
```
boston_housing['rm'].fillna(boston_housing['rm'].median(), inplace=True)
```

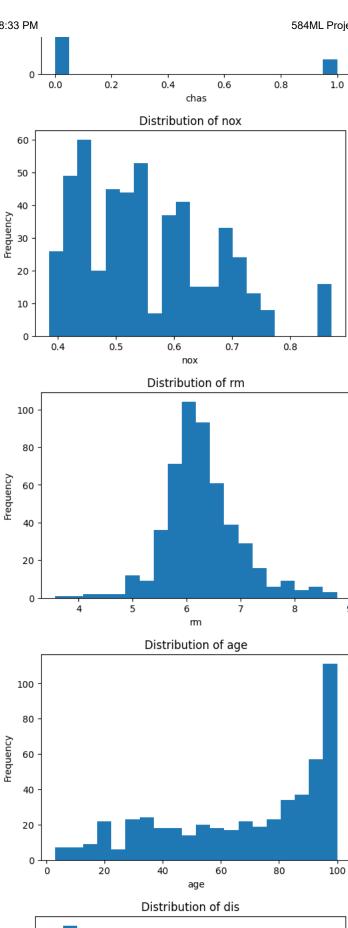
```
boston_housing.isnull().sum()
     crim
                 0
     zn
     indus
                 0
     chas
                 0
     nox
     rm
                 0
     age
     dis
                 0
     rad
                 0
                 0
     ptratio
                 0
     1stat
                 a
     medv
                 0
     dtype: int64
```

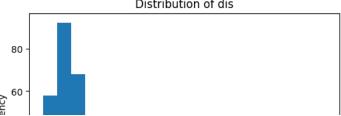
### ▼ EDA

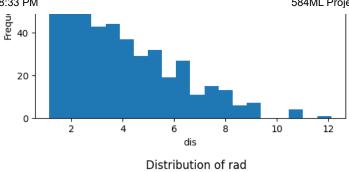
### Analyze any type of relationship within or between features

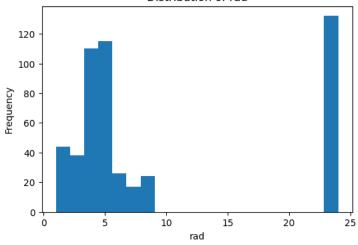
```
target_variable = boston_housing.iloc[:, -1]
features = boston_housing.iloc[:, :-1]
target_variable.head()
     0
          24.0
          21.6
     1
          34.7
     3
          33.4
     Name: medv, dtype: float64
features.head()
            crim
                   zn indus chas
                                     nox
                                             rm age
                                                         dis rad tax ptratio
                                                                                      b 1stat
      0.00632
                 18.0
                        2.31
                                 0 \quad 0.538 \quad 6.575 \quad 65.2
                                                     4.0900
                                                                1 296
                                                                            15.3 396.90
                                                                                          4.98
      1 0.02731
                  0.0
                        7.07
                                 0 0.469 6.421 78.9
                                                     4.9671
                                                                2 242
                                                                           17.8 396.90
                                                                                          9.14
      2 0.02729
                  0.0
                        7.07
                                 0 0.469
                                          7.185
                                                61.1 4.9671
                                                                2 242
                                                                            17.8 392.83
                                                                                          4.03
      3 0.03237
                  0.0
                        2.18
                                 0 0.458 6.998 45.8 6.0622
                                                                3 222
                                                                            18.7 394.63
                                                                                          2.94
         n neans
                   \cap
                                   በ /5ዩ
                                          7 1/17
                                                 5/1 2 6 0622
                                                                            12 7
                                                                                 306 QU
                                                                                          5 22
# Plotting the distribution of each feature in separate graphs
for column in features.columns:
    plt.figure(figsize=(6, 4)) # Adjust the figure size if needed
    plt.hist(features[column], bins=20) # You can also use sns.distplot for more detailed plots
    plt.title(f"Distribution of {column}")
    plt.xlabel(column)
    plt.ylabel("Frequency")
    plt.show()
```

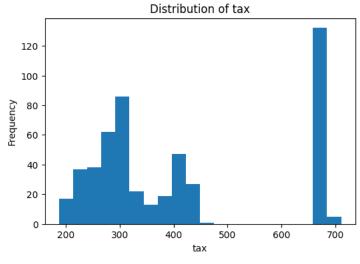


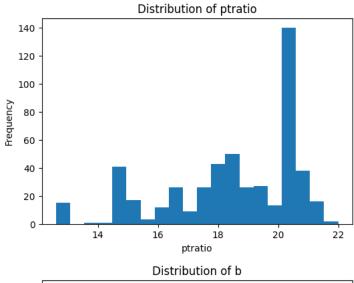




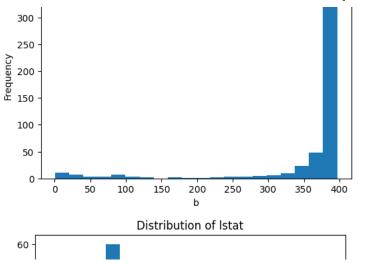






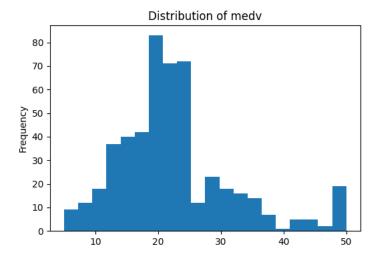


350



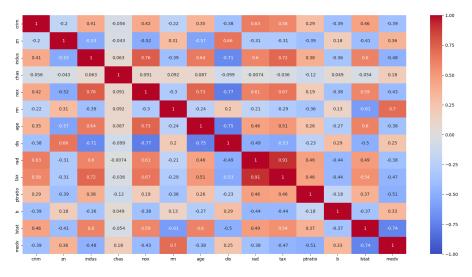
the columns crim, zn, and b have highly skewed data. Chas is apparent now as a 'categorical' column

```
plt.figure(figsize=(6, 4)) # Adjust the figure size if needed plt.hist(target_variable, bins=20) # You can also use sns.distplot for more detailed plots plt.title("Distribution of medv") plt.ylabel("Frequency") plt.show()
```



## correlation analysis

```
plt.figure(figsize=(20, 10))
sns.heatmap(boston_housing.corr(),annot=True,cmap="coolwarm",center=0,vmin=-1,vmax=1);
```



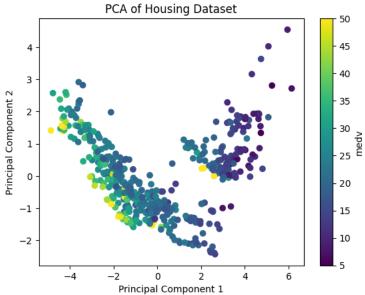
'chas' doesnt seem to be correlated to anything (could possibly drop) however 'tax' and 'rad' seem to have very high correlation.

### Dimensionality Visual Analysis

two concerns 'chas' is categorical will try with and without

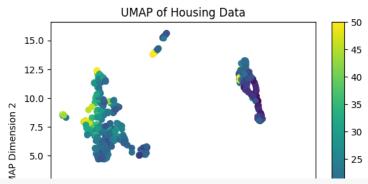
```
features_withoutchas = features.drop('chas', axis=1)
x = StandardScaler().fit_transform(features_withoutchas)
x=pd.DataFrame(x)
x=pd.concat([x,features["chas"]],axis=1)
x=np.array(x)
pca = PCA(.95)
principalComponents = pca.fit_transform(x)
pca.explained_variance_ratio_
     array([0.5077823 , 0.11137644, 0.09813515, 0.06923388, 0.05511658,
            0.04456185, 0.03279204, 0.02296884, 0.01818564])
plt.scatter(principalComponents[:, 0], principalComponents[:, 1], c=boston_housing['medv'], cmap='viridis')
plt.colorbar(label='medv')
plt.xlabel('Principal Component 1')
plt.ylabel('Principal Component 2')
plt.title('PCA of Housing Dataset')
plt.show()
```





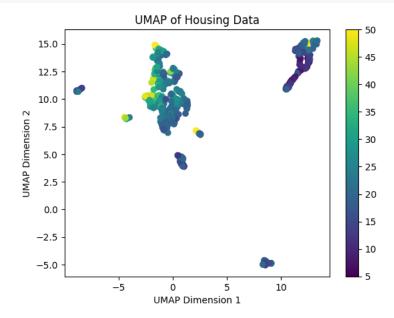
```
umap_model = umap.UMAP(n_components=2)
housing_umap = umap_model.fit_transform(x)

# Scatter plot after UMAP
plt.scatter(housing_umap[:, 0], housing_umap[:, 1], c=boston_housing["medv"], cmap="viridis")
plt.xlabel("UMAP Dimension 1")
plt.ylabel("UMAP Dimension 2")
plt.title("UMAP of Housing Data")
plt.colorbar()
plt.show()
```



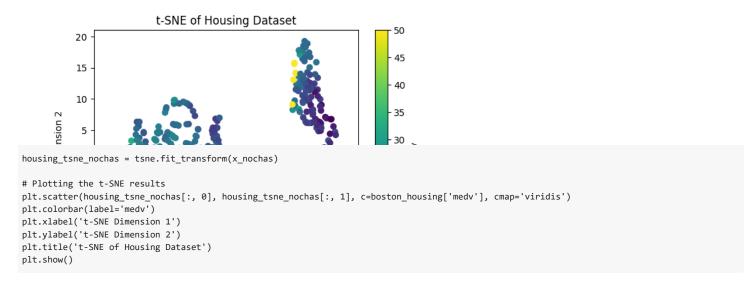
```
housing_umap_nochas = umap_model.fit_transform(x_nochas)

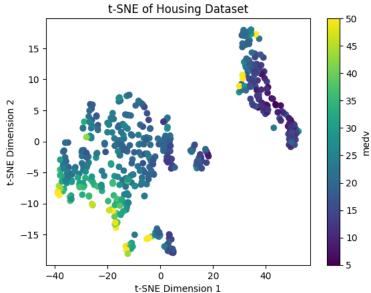
# Scatter plot after UMAP
plt.scatter(housing_umap_nochas[:, 0], housing_umap_nochas[:, 1], c=boston_housing["medv"], cmap="viridis")
plt.xlabel("UMAP Dimension 1")
plt.ylabel("UMAP Dimension 2")
plt.title("UMAP of Housing Data")
plt.colorbar()
plt.show()
```



```
# Applying t-SNE
tsne = TSNE(n_components=2,random_state=42)
housing_tsne = tsne.fit_transform(x)

# Plotting the t-SNE results
plt.scatter(housing_tsne[:, 0], housing_tsne[:, 1], c=boston_housing['medv'], cmap='viridis')
plt.colorbar(label='medv')
plt.xlabel('t-SNE Dimension 1')
plt.ylabel('t-SNE Dimension 2')
plt.title('t-SNE of Housing Dataset')
plt.show()
```





Tried each dimensionality reduction technique (including and excluding 'chas' feature) as a visualization tool and noticed that the first dimension (on x-axis) separates lower median value houses and higher median value houses quite well. Overall, it is still hard to interpret as is the case with dimensionality reduction techniques. Moving on, dataset will \*NO LONGER USE \* 'chas' because of the overall low variance (info value) and 'rad' (high correlation with tax).

## Cross-Validation Strategy

Our group has concluded that the best cross-validation strategy would be to use some permutation of kfold cv. This is the case because our dataset is small, and we have decided to drop some features. kfold will allow us to avoid underfitting while mainting a balance of variance. Since our dataset is not a classification dataset, it was hard to justify stratified cv as a good strategy and instead we went for a simpler kfold.

# Model Building and Experimentation

### Start with simple linear model

```
features=features.drop(['chas','rad'],axis=1)
```

```
linear_model_base=LinearRegression().fit(X_train,y_train)
train_pred=linear_model_base.predict(X_train)
mse = metrics.mean_squared_error(y_train, train_pred)
rmse = np.sqrt(mse) #mse**(0.5)
r2 = metrics.r2_score(y_train,train_pred)
print("Train MSE:", mse)
print("Train RMSE:", rmse)
print("Train R-Squared:", r2)
     Train MSE: 22.925500186282807
     Train RMSE: 4.788058080922036
     Train R-Squared: 0.736104501783255
## Test Metrics
y_hat=linear_model_base.predict(X_test)
mse = metrics.mean_squared_error(y_test, y_hat)
rmse = np.sqrt(mse) #mse**(0.5)
r2 = metrics.r2_score(y_test,y_hat)
print("Test MSE:", mse)
print("Test RMSE:", rmse)
print("Test R-Squared:", r2)
     Test MSE: 27.304132213791554
     Test RMSE: 5.22533560776641
     Test R-Squared: 0.6276732082115685
Linear model is not the best at house price predicting
linear\_scores = cross\_val\_score(linear\_model\_base, X\_train, y\_train, scoring="neg\_mean\_squared\_error", cv=10)
print(-linear_scores)
     [14.77055266 18.42757285 29.37484809 44.33827652 25.33293528 30.08698198
      20.01305631 18.81680525 12.64071601 37.98959581]
As shown above the cv scores are very inconsistent alluding to the idea that our data is inherently bad
## first train simple regressor tree
DTregressor = DecisionTreeRegressor(random_state=42).fit(X_train,y_train)
DTregressor.score(X_train,y_train) #R^2 of train test
     1.0
DTregressor.score(X_test,y_test) #R^2 of test set
     0.8354849663551922
print("MSE DT test: ", metrics.mean_squared_error(y_test,(DTregressor.predict(X_test))))
     MSE DT test: 12.06450980392157
DTregressor.get_depth()
     19
DTregressor.get_n_leaves()
     382
Decision Tree results in much better r^2
```

```
clf = GridSearchCV(DecisionTreeRegressor(random_state=42), {
    'max_depth': np.arange(1,20),
    'splitter': ['best','random'],
    'max_leaf_nodes': np.arange(2,400)
}, cv=10, return_train_score=False)
clf.fit(X_train, y_train)
DTgridcvresults=pd.DataFrame(clf.cv_results_)
DTgridcvresults
```

	mean_fit_time	std_fit_time	mean_score_time	std_score_time	param_max_depth	pa
0	0.002946	0.000519	0.001757	0.000341	1	
1	0.002534	0.000319	0.001687	0.000381	1	
2	0.003098	0.000671	0.001698	0.000187	1	
3	0.002428	0.000147	0.001600	0.000099	1	
4	0.002626	0.000120	0.001567	0.000080	1	
15119	0.003694	0.000245	0.001813	0.000127	19	
15120	0.005900	0.000662	0.002114	0.000238	19	
15121	0.003580	0.000240	0.001819	0.000237	19	
15122	0.006115	0.000437	0.002322	0.000196	19	
15123	0.003555	0.000117	0.001748	0.000048	19	
15124 r	ows × 21 columns					

```
print(clf.best_estimator_,clf.best_score_,)
```

```
bestDTpred=clf.predict(X_test)

print("Grid CV R^2 DT Test: ", metrics.r2_score(y_test,bestDTpred))
print("Grid CV MSE DT Test: ", metrics.mean_squared_error(y_test,bestDTpred))

Grid CV R^2 DT Test: 0.7841876323568392
Grid CV MSE DT Test: 15.82633737205945
```

The grid search interestingly gave worse metric results but also created a simpler model. 7 depth, with 30 max leafs is much simpler than a tree with depth of 19 with 382 leaves

	Features	Importance
0	crim	0.014846
1	zn	0.009501
2	indus	0.019941
3	nox	0.029444
4	rm	0.390391
5	age	0.022805
6	dis	0.014797
7	tax	0.035315
8	ptratio	0.008942
9	b	0.018057
10	Istat	0.435961

The feature importances show that rm and Istat are above and beyound more important than any other feature.

### ▼ Model Improvement Proposals

#### ▼ Feature Selection

Remove worst feature indicated from above model and retrain (with cv) on the same Decision Tree Regressor

```
features_nopratio=features.drop(["ptratio"],axis=1)
X_trainfs, X_testfs, y_trainfs, y_testfs = train_test_split(features_nopratio, target_variable, test_size=0.2, random_state=42)
fsDT=DecisionTreeRegressor(random_state=42).fit(X_trainfs,y_trainfs)
fsDT_pred=fsDT.predict(X_testfs)
print("Feature Selected DT Test R^2: ", metrics.r2_score(y_testfs,fsDT_pred))
print("Feature Selected DT Test MSE: ", metrics.mean\_squared\_error(y\_testfs,fsDT\_pred))
     Feature Selected DT Test R^2: 0.8726371448806778
     Feature Selected DT Test MSE: 9.34
fsDT.get_depth()
     19
fsDT.get_n_leaves()
     380
fsDT.get_params()
     {'ccp_alpha': 0.0,
      'criterion': 'squared_error',
      'max_depth': None,
      'max_features': None,
      'max_leaf_nodes': None,
      'min_impurity_decrease': 0.0,
      'min_samples_leaf': 1,
      'min_samples_split': 2,
      'min_weight_fraction_leaf': 0.0,
      'random_state': 42,
      'splitter': 'best'}
```

```
clf_featureselected = GridSearchCV(DecisionTreeRegressor(random_state=42), {
    'max_depth': np.arange(1,20),
    'splitter': ['best','random'],
    'max_leaf_nodes': np.arange(2,400)
}, cv=10, return_train_score=False)
clf_featureselected.fit(X_trainfs, y_trainfs)
fsDTgridcvresults=pd.DataFrame(clf_featureselected.cv_results_)
fsDTgridcvresults
```

	mean_fit_time	std_fit_time	mean_score_time	std_score_time	param_max_depth	pa
0	0.003584	0.001091	0.002035	0.000516	1	
1	0.002554	0.000134	0.001586	0.000076	1	
2	0.002948	0.000340	0.001672	0.000163	1	
3	0.002820	0.000333	0.001720	0.000153	1	
4	0.003249	0.000285	0.001895	0.000210	1	
15119	0.005266	0.000116	0.002676	0.000136	19	
15120	0.008056	0.000257	0.003427	0.001193	19	
15121	0.005317	0.000123	0.002811	0.000264	19	
15122	0.008609	0.001572	0.003587	0.001114	19	
15123	0.005770	0.000717	0.002854	0.000202	19	
15124 r	ows × 21 columns					

We see that grid search cv leads again to a worse model, but this time the metrics are much worse, so the smaller model may not make sense in this case and better to just use default parameters on the DecisionTreeRegressor with the dropped feature.

### Increased Model Complexity

Grid CV MSE DT Test: 28.62892644236298

The next proposal is to use a more complex model, specifically an ensemble method of RandomForestRegressor. Use the same dataset as used in the first DTRegressor model and apply same cv approach.

```
rf=RandomForestRegressor(random_state=42).fit(X_test,y_test)
print("train set RF R^2: ", rf.score(X_train,y_train))
print("test set RF R^2: ", rf.score(X_test,y_test))

    train set RF R^2: 0.8146972847430404
    test set RF R^2: 0.9693605585307042

rfpred=rf.predict(X_test)
print("test set RF MSE: ", metrics.mean_squared_error(rfpred,y_test))

    test set RF MSE: 2.2469061568627438
```

Right off the bat, the R^2 scores look great for default random forest regressor, and an exceptionally low MSE

```
rf.get_params()
     {'bootstrap': True,
      'ccp_alpha': 0.0,
      'criterion': 'squared_error',
      'max_depth': None,
      'max_features': 1.0,
      'max_leaf_nodes': None,
      'max_samples': None,
      'min_impurity_decrease': 0.0,
      'min_samples_leaf': 1,
      'min_samples_split': 2,
      'min_weight_fraction_leaf': 0.0,
      'n_estimators': 100,
      'n_jobs': None,
      'oob_score': False,
      'random_state': 42,
      'verbose': 0,
      'warm_start': False}
clf_rf = GridSearchCV(RandomForestRegressor(random_state=42), {
    'max_depth': np.arange(1,20),
    'n_estimators': np.arange(50,150),
}, cv=10, return_train_score=False)
clf_rf.fit(X_train, y_train)
RFgridcvresults=pd.DataFrame(clf_rf.cv_results_)
RFgridcvresults
```

,				,		,		
	mean_fit_time	std_fit_time me	an_score_time s	td_score_time para	m_max_depth param_n_e	estimators	params	split0_test_score
						{	max_depth':	
0	0.079775	0.007883	0.003804	0.000236	1	50 <sub>'n</sub>	1, _estimators': 50}	0.625816
						{	max_depth':	
1	0.077003	0.002804	0.004029	0.000781	1	51 <sub>'n</sub>	1, _estimators': 51}	0.627426
						{	max_depth':	
2	0.080201	0.004814	0.004173	0.000858	1	52 <sub>'n</sub>	1, _estimators': 52}	0.628685
						{	max_depth':	
3	0.080021	0.002920	0.003809	0.000107	1	53 <sub>'n</sub>	1, estimators':	0.629867
int(clf_	rf.best_estimato	r_,clf_rf.best_sc	core_,)					
Rando	mForestRegressor	(max_depth=13, n_	_estimators=146,	random_state=42) 0	.8236368259793689			
-	0.002017	0.007200	0.000022	0.000101	ı	'n	estimators':	U.UUUUT I
stRFpred:	clf_rf.predict(	X_test)						
		: ", metrics.r2_s		tRFpred)) y_test,bestRFpred))				
		0.87588133470614 9.10209128680857						
							max denth!	
f all exper	riments, the best	model performand	ce was the default	t Random Forest Reg	gressor with a R^2 of .96	i9 and MSE of		
							146}	
						•	max_depth': 19,	
1897	0.484681	0.021206	0.008456	0.001287	19	147 <sub>'n</sub>	_estimators': 147}	0.831395
						{	max_depth': 19,	
1898	0.659911	0.131709	0.011787	0.003024	19	148 'n <sub>.</sub>	_estimators': 148}	0.831926
						{	max_depth':	
1899	0.480904	0.016309	0.008330	0.000449	19	149 <sub>'n</sub>	19, _estimators':	0.831563