## Visualization

## May 16, 2018

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In [1]: from __future__ import division
        from numpy import *
        from sympy import *
        import matplotlib.pyplot as plt
        %matplotlib notebook
        from mpl_toolkits import mplot3d
        x, y, z, t = symbols('x y z t')
        k, m, n = symbols('k m n', integer=True)
        f, g, h = symbols('f g h', cls=Function)
In [3]: def f(x, y):
             return x + y
        def c(x):
            return 0
        def d(x):
            return 1
In [4]: def Simpson_Double(a, b, m, n):
                h = (b - a)/n
                J1, J2, J3 = 0, 0, 0
                for i in range(0, n + 1):
                             x = a + i*h
                             HX = (d(x) - c(x))/m
                             k1 = f(x, c(x)) + f(x, d(x))
                             k2 = 0
                             k3 = 0
                             for j in range (1, m):
                                   y = c(x) + j*HX
                                    Q = f(x, y)
                                    if j\%2 == 0:
                                       k2 = k2 + Q
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else:
                                       k3 = k3 + Q
                             L = (k1 + 2*k2 + 4*k3)*HX/3
                             if i == 0 or i == n:
                                      J1 = J1 + L
                             elif i\%2 == 0:
                                      J2 = J2 + L
                             else:
                                J3 = J3 + L
                J = h*(J1 + 2*J2 + 4*J3)/3
                return J
In [5]: xlist = []
        ylist = []
        zlist = []
        real_z = []
        error = []
        total_error = 0
In [6]: for i in arange(0, 1, 0.05):
                for k in arange(0, 1, 0.05):
                    #redefine the y-functions.
                     def c(x):
                        return 0
                     def d(x):
                        return k
                     z = Simpson_Double(0, i, 30, 30)
                     r_z = (i**2)*(k/2) + (k**2)*(i/2)
                     zlist = zlist + [z]
                     xlist = xlist + [i]
                     ylist = ylist + [k]
                     real_z = real_z + [r_z]
                     error = error + [abs(z - r_z)]
                     total\_error = total\_error + abs(z - r_z)
                    \# print('xlist = %3f, ylist = %3f, actual = %.17f, approximate = %.17f'%(i
```

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print(total_error)
ax = plt.axes(projection='3d')
ax.set_xlabel('X')
ax.set_ylabel('Y')
ax.set_zlabel('Z')
ax.scatter3D(xlist, ylist, zlist, cmap='Greens');
plt.draw()
```

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