

# Midterm question 3

May 4, 2018

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In [1]: from sympy import*
        %matplotlib inline
        import matplotlib.pyplot as plt
        from __future__ import division
        x, y, z, t = symbols('x y z t')
        k, m, n = symbols('k m n', integer = True)
        f, g, h = symbols('f g h', cls = Function)
        import math

In [2]: def f(x):
        return math.e**(-x)*x**(5.1)

In [3]: def compositeSimpson(startPoint, endPoint, numIntervals):
        a = startPoint
        b = endPoint
        n = numIntervals
        h = (b - a) / n
        leftRight = f(a) + f(b)
        oddSum = 0
        evenSum = 0
        for i in range(1, n):
            x = a + i*h
            if i % 2 == 1:
                oddSum = oddSum + f(x)
            else:
                evenSum = evenSum + f(x)
        areaEstimate = h * (leftRight + 2*evenSum + 4*oddSum) / 3
        return areaEstimate

In [6]: def midterm(initial):
        areaEstimate = 0
        while abs(areaEstimate - 6.1) > 0.00001:
            areaEstimate = compositeSimpson(0, initial, 50)
            initial = initial + 0.000001
        return initial

In [7]: midterm(2.57)
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Out[7]: 2.576475000000905
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In [8]: abs(6.1 - compositeSimpson(0, 2.576475, 100))
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Out[8]: 1.0357748525535726e-07
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