

Assignment-4

Here **divide and conquer** is used to generate a segment Tree which stores the pair of minimum and maximum.

In the function make it is made by first traveling to the leaf node by **dividing** the array into sub-parts until the size is 1 and then generate it by **conquering** as it comes back using its min and max of its left and right child. The query function returns the minimum and maximum in the range l to r in $O(\log N)$ time.

To find the indices i and j we iterate through the array and fix each i in each iteration and **binary_search** to find j. in each step of binary search we are calculating the minimum and maximum in the range i to mid using the **query** function in $O(\log N)$ time. Thus, the overall time complexity is-

$O(N)$ [for iteration] * $O(\log N)$ [for binary_search] * $O(\log N)$ [for query function using **conquer** on segment tree]

Recurrence Relation:-

For segtree make() function:-

$$T(n) = 2 * T(n/2) + 1$$

Time Complexity – $O(N)$

For query() function:-

$$T(n) = T(n/2) + 1$$

Time Complexity – $O(\log N)$

For binary_search():-

$$T(n) = T(n/2) + 1$$

Time Complexity – $O(\log N)$

Overall Time Complexity – $O(N \log_2 N)$

Space Complexity – $O(N)$