Assignment 6

1.
$$P(HBP) = \sum_{Sm} \sum_{ME} P(HBP, Sm, ME)$$

 $P(HBP) = \sum_{Sm} \sum_{ME} P(HBP | Sm, Me) * P(Sm) * P(ME)$
 $P(HBP) = 0.6*0.2*0.5 + 0.72*0.2*0.5 + 0.33*0.8*0.5 + 0.51*0.8*0.5$
 $P(HBP) = 0.47$

2. $P(HD) = \sum_{Ath} \sum_{HBP} \sum_{FH} P(HD, Ath, HBP, FH)$ $P(HD) = \sum_{Ath} \sum_{HBP} \sum_{FH} P(HD|Ath, HBP, FH) * P(Ath) * P(HBP) * P(FH)$ Here's a table for each component and then summed at the bottom

Ath	НВР	FH	P(HD)	P(Ath)	P(HBP)	P(FH)	P(HD,Ath,HBP,FH)
У	У	У	0.92	0.53	0.47	0.15	0.03
У	У	n	0.91	0.53	0.47	0.85	0.19
У	n	У	0.81	0.53	0.53	0.15	0.03
У	n	n	0.77	0.53	0.53	0.85	0.19
n	У	У	0.75	0.47	0.47	0.15	0.02
n	У	n	0.69	0.47	0.47	0.85	0.13
n	n	У	0.38	0.47	0.53	0.15	0.01
n	n	n	0.23	0.47	0.53	0.85	0.05
Total							0.66

$$P(HD) = 0.66$$

3. P(HD | Rapid) =
$$\frac{P(Rapid | HD) * P(HD)}{P(Rapid)}$$

$$P(HD \mid Rapid) = \frac{P(Rapid \mid HD) * P(HD)}{\sum_{HD} P(HD, Rapid)}$$

P(HD | Rapid) =
$$\frac{0.99 * 0.66}{0.99*0.66+0.35*0.3}$$

4. P(HBP | HD, FH) =
$$\frac{P(HD,FH,HBP)}{P(HD,FH)}$$

First I need to figure out the P(HD, FH) which is shown by the following table:

Ath	НВР	FH	P(HD)	P(Ath)	P(HBP)	P(FH)	P(HD,Ath,HBP,FH)
У	У	У	0.92	0.53	0.46	0.15	0.03
У	n	У	0.81	0.53	0.54	0.15	0.03
n	У	У	0.75	0.47	0.46	0.15	0.02
n	n	у	0.38	0.47	0.54	0.15	0.01
						Total	0.11

Now, I can use this data to find the P(HD,FH, HBP) with the following data points:

Ath	НВР	FH	P(HD)	P(Ath)	P(HBP)	P(FH)	P(HD,Ath,HBP,FH)
у	У	У	0.92	0.53	0.46	0.15	0.03
n	У	У	0.75	0.47	0.46	0.15	0.02
Total							0.06

Now I just put everything into the equation to solve:

P(HBP | HD, FH) =
$$\frac{0.06}{0.11}$$

$$P(HBP \mid HD, FH) = 0.55$$

5.
$$P(Sm \mid HD) = \frac{P(HD|Sm)*P(Sm)}{P(HD)}$$

$$P(Sm \mid HD) = \frac{P(HD,HBP)*P(HBP)*P(HBP,Sm)*P(Sm)}{P(HD)}$$

Now, I can find the probability of Heart Disease given High Blood Pressure by adding the different probabilities

Ath	НВР	FH	P(HD)	P(Ath)	P(HBP)	P(FH)	P(HD,Ath,HBP,FH)
У	У	У	0.92	0.53	1	0.15	0.07
У	У	n	0.91	0.53	1	0.85	0.41
n	У	У	0.75	0.47	1	0.15	0.05
n	У	n	0.69	0.47	1	0.85	0.28
Total							0.81

The P(HBP,Sm) =
$$\sum_{Sm} P(HBP,Sm,ME)$$

P(HBP,Sm) = 0.6*0.5*1 +0.72*0.5*1
P(HBP,Sm) =0.66

Now, I just substitute everything into the equation and solve.

P(Sm | HD) =
$$\frac{P(HD,HBP)*P(HBP)*P(HBP,Sm)*P(Sm)}{P(HD)}$$
P(Sm | HD) =
$$\frac{0.81*0.47*0.66*0.2}{0.65}$$
P(Sm | HD) = 0.07

6. The probability in question 5 would increase because now you know that the person has high blood pressure which can be caused by smoking. Because of this, you don't need to multiply by P(HBP) in the above equation. As such, the numerator is larger increasing the probability to 0.16.

7.
$$P(Me | Ang) = \frac{P(Ang,HD)*P(HD)*P(HD,HBP)*P(HBP)*P(HBP,ME)*P(ME)}{P(Ang)}$$
 First we solve for P(HBP,ME) which is: The P(HBP,ME) = $\sum_{ME} P(HBP,Sm,ME)$ P(HBP,ME) = 0.6*1*0.2 + 0.33*1*0.8 P(HBP,ME) = 0.38

We can calculate the P(Ang) as well:

$$P(Ang) = \sum_{HD} P(Ang, HD)$$

 $P(Ang) = 0.85*0.66+0.4*0.34$
 $P(Ang) = 0.70$

As we've solved for the other probabilities above, we can just substitute everything into the equation in order to solve:

$$P(Me|Ang) = \frac{0.85*0.66*0.81*0.47*0.38*0.5}{0.7}$$

$$P(Me|Ang) = 0.058$$