

Started on	Monday, 13 September 2021, 8:01 AM
State	Finished
Completed on	Monday, 13 September 2021, 10:01 AM
Time taken	2 hours
Grade	Not yet graded

Question **1**
Correct
Mark 1.00 out of 1.00

Question 1. (1 point) Consider the languages $L_1 = \{\}$ and $L_2 = \{\epsilon\}$. Which of the following is equivalent to $\{\}$?

Select one:

☒ a. L_1L_2

☐ b. $L_1L_2^* \cup L_1^*$

☐ c. $L_1^*L_2$

☐ d. $L_1^*L_2^* \cup L_1$

Your answer is correct.

The correct answer is: L_1L_2

Question **2**
Not answered
Marked out of 1.00

Question 2. (1 point) What is the minimum number of states required to construct a DFA to recognize $L = \{0^{5n} | n > 0\}$?

Select one:

☐ a. 5

☐ b. 4

☐ c. 7

☐ d. 6

Your answer is incorrect.

The correct answer is: 5

Question 3

Correct

Mark 2.00 out of 2.00

Question 3. (2 points) Which of the following regular expression are equivalent?

$$R_1 : a^*(ab^*a^* + b^*) + b^*(ba^*b^* + a^*)$$

$$R_2 : (a^* + b^*)(a^* + b^*)(b^* + a^*)$$

$$R_3 : a^*b^*a^* + b^*a^*b^*$$

$$R_4 : a^*b^* + bb^*a^* + aa^*b^*a^*$$

Select one:

- ☐ a. Only R_3 and R_4
- ☐ b. Only R_2, R_3 and R_4
- ☒ c. Only R_1, R_2 and R_3 ✓
- ☐ d. Only R_1 and R_3

Your answer is correct.

Only R_1, R_2 and R_3

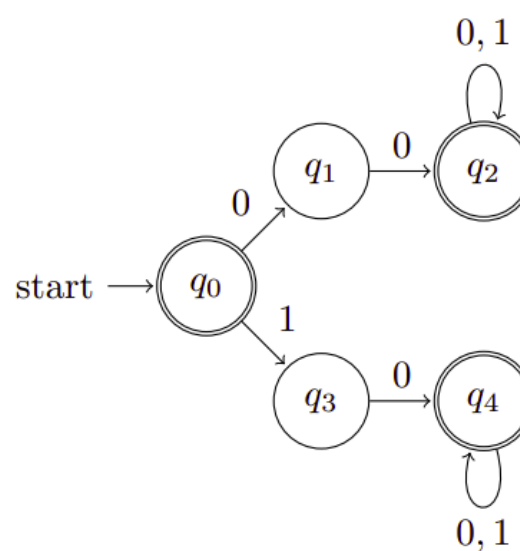
The correct answer is:

Question 4

Correct

Mark 2.00 out of 2.00

Question 4. (2 points) What is the regular expression corresponding to the following NFA?



Select one:

- ☐ a. $(\epsilon + 00 + 10)(0 + 1)^*$
- ☐ b. $(\epsilon + (0 + 1)0)(0 + 1)^*$
- ☒ c. $\epsilon + (0 + 1)0(0 + 1)^*$ ✓
- ☐ d. $(\epsilon + 0 + 1)0(0 + 1)^*$

Your answer is correct.

$\epsilon + (0 + 1)0(0 + 1)^*$

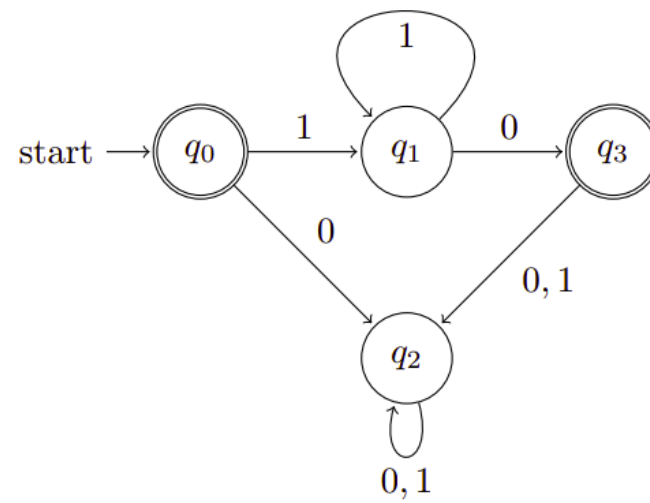
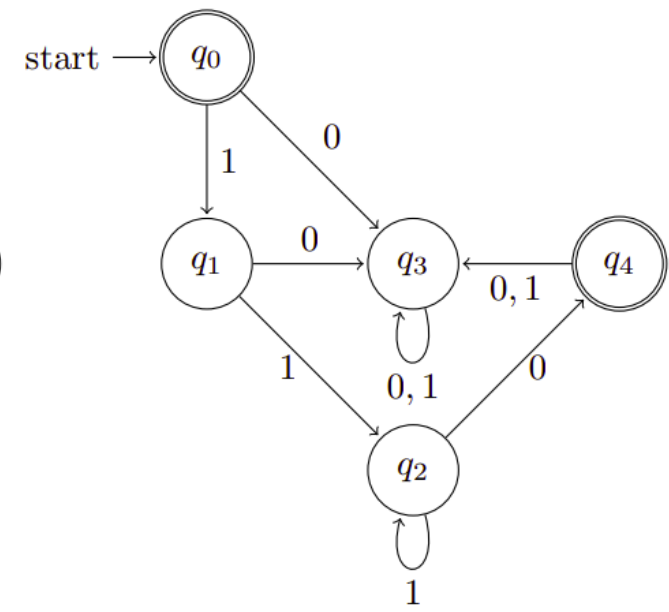
The correct answer is:

Question 5

Correct

Mark 5.00 out of 5.00

Question 5. (5 points) Consider the following two DFAs A_1 and A_2

DFA A_1 DFA A_2

Which one of the following is true?

Select one:

- ☐ a. $L(A_1) \subsetneq L(A_2)$
- ☒ b. $L(A_2) \subsetneq L(A_1)$ ✓
- ☐ c. $L(A_1) = L(A_2)$
- ☐ d. None of the above

Your answer is correct.

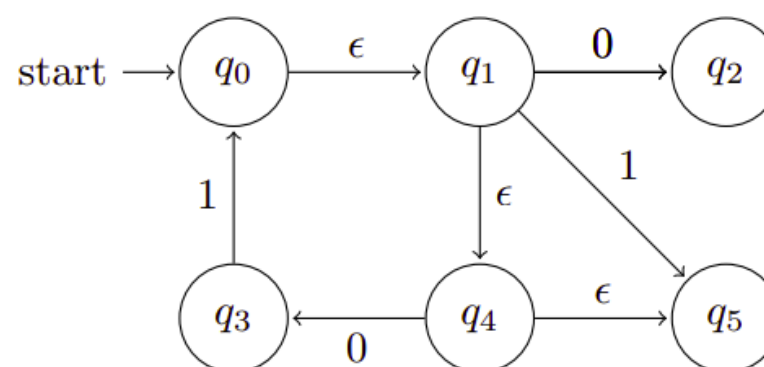
The correct answer is: $L(A_2) \subsetneq L(A_1)$

Question 6

Partially correct

Mark 0.67 out of 1.00

Question 6. (1 point) Consider the following NFA.



Which states belong to the ϵ -closure of the state q_1 in the above NFA?

Select one or more:

- ☐ a. q_0
- ☒ b. q_4 ✓
- ☒ c. q_5 ✓
- ☐ d. q_1

Your answer is partially correct.

You have correctly selected 2.

The correct answers are: q_1 , q_4 , q_5

Question 7

Correct

Mark 1.00 out of 1.00

Question 7. (1 point) Context-free languages are closed under which of the following operations?

Select one or more:

- ☒ a. Union ✓
- ☐ b. Set difference
- ☒ c. Concatenation ✓
- ☐ d. Complementation

Your answer is correct.

The correct answers are: Concatenation , Union

Question 8

Partially correct

Mark 0.67 out of 1.00

Question 8. (1 point) Which of the following production rules are not allowed in a grammar in Chomsky Normal Form (S is the start symbol)?

Select one or more:

☒ a. $A \rightarrow aB$ ✓

☒ b. $A \rightarrow BCD$ ✓

☐ c. $A \rightarrow AB$
☒ d. $S \rightarrow SA$ ✗

Your answer is partially correct.

You have correctly selected 2.

The correct answers are: $A \rightarrow BCD$, $A \rightarrow AB$, $A \rightarrow aB$

Question 9

Correct

Mark 2.00 out of 2.00

Question 9. (2 points) A CFG G is given below with S as the start symbol.

$$\begin{aligned} S &\rightarrow aS \mid A \\ A &\rightarrow aAb \mid bAa \mid \epsilon \end{aligned}$$

Which of the following strings is generated by the grammar?

Select one or more:

☐ a. abababb

☒ b. aababab ✓

☒ c. aabbaab ✓

☐ d. aabbaba

Your answer is correct.

The correct answers are: aababab, aabbaab

Question **10**

Incorrect

Mark 0.00 out of 2.00

Question 10. (2 points) Consider the language

$$L = \{w \in \{0,1\}^* \mid w \text{ begins with } 11 \text{ and has an even number of } 1\text{'s}\}.$$

How many states will the minimal DFA for L have?

Select one:

- ☒ a. 4 ✖
- ☐ b. 6
- ☐ c. 5
- ☐ d. 3

Your answer is incorrect.

The correct answer is: 5

Question **11**

Correct

Mark 1.00 out of 1.00

Question 11. (1 point) Identify the language generated by the following grammar -

$$\begin{aligned} S &\longrightarrow AB \\ A &\longrightarrow aAb \mid \epsilon \\ B &\longrightarrow bB \mid b \end{aligned}$$

Select one:

- ☐ a. $\{a^m b^n \mid n \geq m, m > 0\}$
- ☒ b. $\{a^m b^n \mid n > m, m \geq 0\}$ ✔
- ☐ c. $\{a^m b^n \mid n > m, m > 0\}$
- ☐ d. $\{a^m b^n \mid n \geq m, m \geq 0\}$

Your answer is correct.

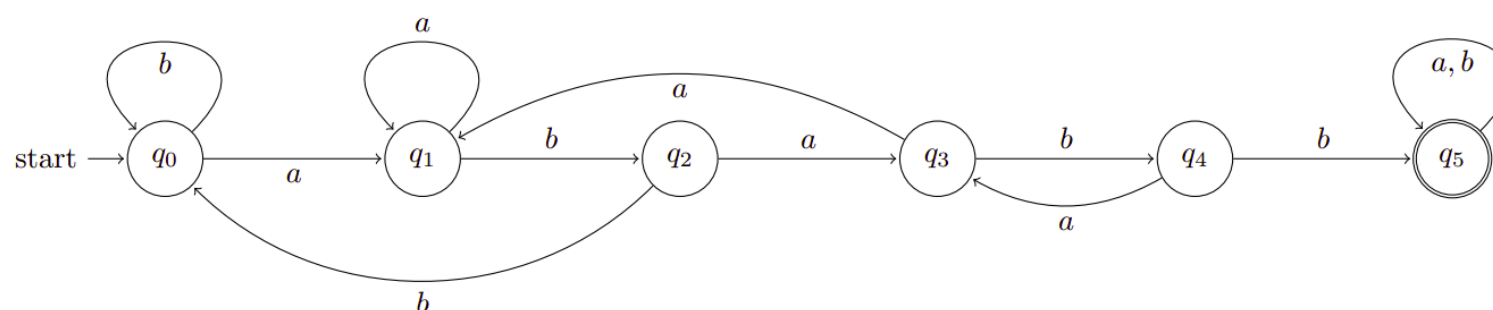
The correct answer is: $\{a^m b^n \mid n > m, m \geq 0\}$

Question 12

Correct

Mark 2.00 out of 2.00

Question 12. (2 points) What is the language accepted by the following DFA?



Select one:

- ☒ a. The set of string containing *ababb* as substring ✓
- ☐ b. The set of strings ending with *ababb*
- ☐ c. The set of strings beginning with *ababb*
- ☐ d. The set of strings with *bababb* as substring

Your answer is correct.

The correct answer is: The set of string containing *ababb* as substring

Question 13

Incorrect

Mark 0.00 out of 2.00

Question 13. (2 points) Consider the following two grammars: G_1 :

$$S \longrightarrow SbS \mid a$$

G_2 :

$$S \longrightarrow aB \mid ab$$

$$A \longrightarrow AB \mid a$$

$$B \longrightarrow ABb \mid b$$

Which of the following option is correct?

Select one:

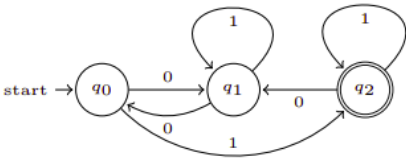
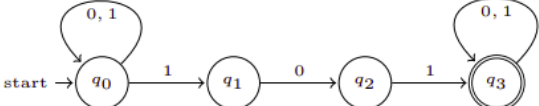
- ☐ a. Only G_1 is ambiguous.
- ☐ b. Neither G_1 nor G_2 are ambiguous.
- ☒ c. Only G_2 is ambiguous. ✗
- ☐ d. Both G_1 and G_2 are ambiguous.

Your answer is incorrect.

The correct answer is: Both G_1 and G_2 are ambiguous.

Question **14**
Correct
Mark 5.00 out of 5.00

Question 14. (5 points) Match the NFAs , DFAs and REs in column A with their appropriate languages in column B.

Column A	Column B
<div></div> <div>(1)</div> <div>(2) $00^*1(0+1)^*$</div> <div>(3) $0^*(\epsilon+10^*(\epsilon+10^*))$</div> <div></div> <div>(4)</div>	<div>(a) $\{w \in \{0,1\}^* \mid w \text{ ends with 1 and has even no. of 0's}\}$</div> <div>(b) $\{w \in \{0,1\}^* \mid w \text{ has 101 as a substring}\}$</div> <div>(c) $\{w \in \{0,1\}^* \mid w \text{ has at most two 1's}\}$</div> <div>(d) $\{w \in \{0,1\}^* \mid w \text{ begins with 0 and has at least one 1}\}$</div>

Choose the correct matching from following choices.

- Select one:
- ☒ a. 1-a, 2-d, 3-c, 4-b ✓
 - ☐ b. 1-d, 2-c, 3-a, 4-b
 - ☐ c. 1-b, 2-d, 3-a, 4-c
 - ☐ d. 1-b, 2-c, 3-a, 4-d

Your answer is correct.

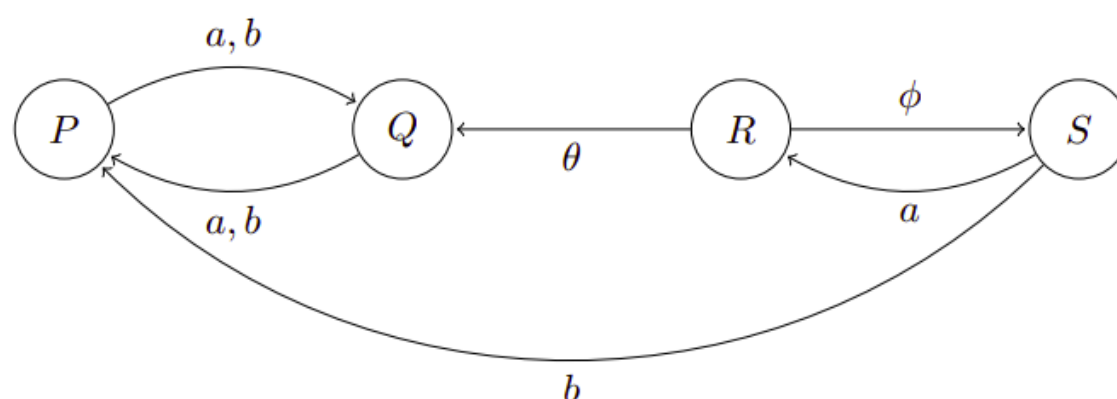
The correct answer is: 1-a, 2-d, 3-c, 4-b

Question 15

Correct

Mark 5.00 out of 5.00

Question 15. (5 points) Consider the following finite state machine A



Choose the correct modifications so that A becomes a DFA and

$$L(A) = \{w \in \{a, b\}^* \mid w \text{ has odd length with at least one } b\}.$$

Select one:

- ☐ a.
Replace θ by ' b ' and ϕ by ' a ' and make P starting state and S accept state
- ☐ b.
Replace θ by ' a ' and ϕ by ' b ' and make Q starting state and P accept state
- ☒ c.
Replace θ by ' b ' and ϕ by ' a ' and make S starting state and P accept state ✓
- ☐ d.
Replace θ by ' a ' and ϕ by ' b ' and make P starting state and Q accept state

Your answer is correct.

The correct answer is:

Replace θ by ' b ' and ϕ by ' a ' and make S starting state and P accept state

Question 16

Correct

Mark 1.00 out of 1.00

Question 16. (1 point) If $L = \{a, ab\}$, which of the following are in L^* ?

Select one or more:

- ☐ a. bababaaba
- ☒ b. abababaab ✓
- ☒ c. aabaaab ✓
- ☐ d. abababbab

Your answer is correct.

The correct answers are: aabaaab , abababaab

Question **17**

Partially correct

Mark 1.00 out of 2.00

Question 17. (2 points) Consider the following grammar.

$$\begin{aligned} S &\rightarrow AB \\ A &\rightarrow a \mid BaB \\ B &\rightarrow bbA \end{aligned}$$

Which of the following statements is/are true?

Select one or more:

- ☐ a. The grammar is in Chomsky Normal Form.
- ☐ b. The length of every string produced by this grammar is even.
- ☒ c. No string produced by this grammar has three consecutive *as*. ✓
- ☐ d. The string *abbaab* is generated by this grammar.

Your answer is partially correct.

You have correctly selected 1.

The correct answers are:

The length of every string produced by this grammar is even. ,

No string produced by this grammar has three consecutive *as*.Question **18**

Correct

Mark 2.00 out of 2.00

Question 18. (2 points) Let R be a regular language and L be a context-free language. Which of the following is necessarily true?

Select one or more:

- ☐ a. $L \cap R$ is regular
- ☐ b. If $L \cup R$ is regular then L is regular
- ☒ c. $L \cup R$ is context-free ✓
- ☒ d. \overline{R} is regular ✓

Your answer is correct.

The correct answers are: \overline{R} is regular , $L \cup R$ is context-free

Question 19

Partially correct

Mark 1.33 out of 2.00

Question 19. (2 points) Which of the following languages are regular?

Select one or more:

- ☐ a. $\{w \in \{a, b, c\}^* \mid w \text{ has no } c \text{ to the left of an } a\}$
- ☒ b. $\{w \in \{0, 1\}^* \mid w \text{ has an even number of 0's}\}$ ✓
- ☒ c. $\{w \in \{a, b, c\}^* \mid w \text{ has 10 } c\text{'s after every } a\}$ ✓
- ☐ d. $\{w \in \{0, 1\}^* \mid w \text{ has equal number of 0's and 1's}\}$

Your answer is partially correct.

You have correctly selected 2.

The correct answers are: $\{w \in \{0, 1\}^* \mid w \text{ has an even number of 0's}\}$,
 $\{w \in \{a, b, c\}^* \mid w \text{ has no } c \text{ to the left of an } a\}$,
 $\{w \in \{a, b, c\}^* \mid w \text{ has 10 } c\text{'s after every } a\}$

Question 20

Correct

Mark 5.00 out of 5.00

Question 20. (5 points) Let L be a language over Σ . Define

$$L' = \{w \in \Sigma^* \mid wx \in L \text{ for some } x \in \Sigma^* \text{ and } |w| = |x|\}.$$

Which one of the following statements are correct?

Select one or more:

- ☒ a. If L is regular then L' is regular ✓
- ☒ b. There exists a non-regular language L such that L' is regular ✓
- ☐ c. If L is regular then L' is non-regular
- ☐ d. There exists a regular language L such that L' is not regular

Your answer is correct.

The correct answers are: If L is regular then L' is regular ,
 There exists a non-regular language L such that L' is regular

Question **21**

Complete

Marked out of
10.00**Question 21.** Consider the CFG G given by the following production rules

$$\begin{aligned}
 S &\longrightarrow S_1 C \mid A S_2 \\
 S_1 &\longrightarrow a S_1 b \mid \epsilon \\
 S_2 &\longrightarrow b S_2 c \mid \epsilon \\
 A &\longrightarrow a A \mid \epsilon \\
 C &\longrightarrow c C \mid \epsilon
 \end{aligned}$$

- (a) (2 points) The language of G ,
 $L(G) = \{w \in \{a, b, c\}^* \mid \underline{\hspace{15cm}}\}$
- (b) (4 points) Give a string of length 6 in $L(G)$ that has a unique parse tree with respect to G . Draw the parse tree.
- (c) (4 points) Give a string of length 6 in $L(G)$ that has two parse trees with respect to G . Draw the two parse trees.

 [_qsn21.pdf](#)Question **22**

Complete

Marked out of
10.00**Question 22.** (10 points) Give a CFG for the language

$$L = \{a^i b^j c^k \mid j \leq i + k \leq 2j, i, j, k \geq 0\}.$$

For each variable used in your CFG, describe the language generated by the variable.

 [_qsn22.pdf](#)Question **23**

Complete

Marked out of
5.00**Question 23.** (5 points) Prove that no infinite subset of the language $L = \{0^n 1^n \mid n \geq 0\}$ is regular. [_qsn23.pdf](#)Question **24**

Complete

Marked out of
10.00**Question 24.** (10 points) Let $A \subseteq \{0, 1\}^*$ and let

$$A' = \{xy \mid x1y \in A\}.$$

That is, A' contains all strings obtained from a string in A by deleting exactly one 1. Show that if A is regular, then A' is also regular (give the construction only). [_qsn24.pdf](#)[◀ Quiz 1](#)

Jump to...