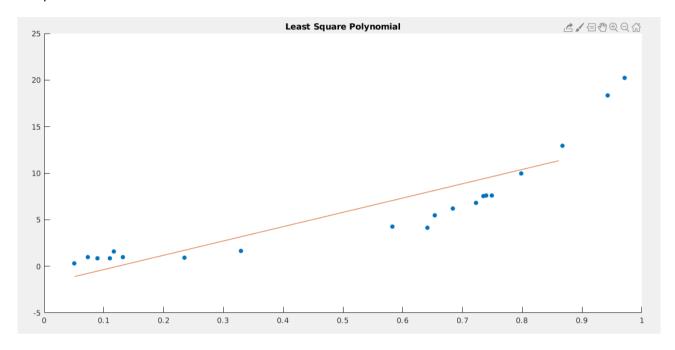
# Least Square

**Output: (Linear)**Least Square Interpolation Polynomial.....

Coefficients of the Polynomial:

15.363890 -1.889820

R-sq = 0.757172



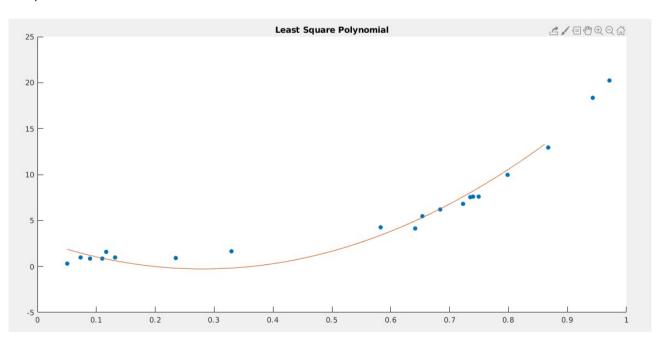
### **Output: (Quadratic)**

LeastSquare Interpolation Polynomial.....

Coefficients of the Polynomial:

40.279459 -22.625813 2.907038

R-sq = 0.976508



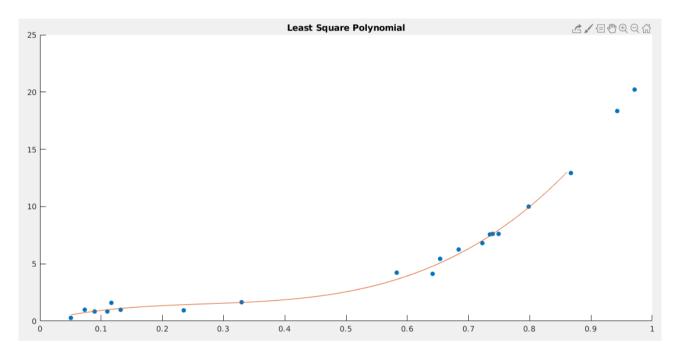
# **Output: (Cubic)**

LeastSquare Interpolation Polynomial.....

Coefficients of the Polynomial:

50.261700 -40.709692 12.917014 -0.009668

R-sq = 0.996541



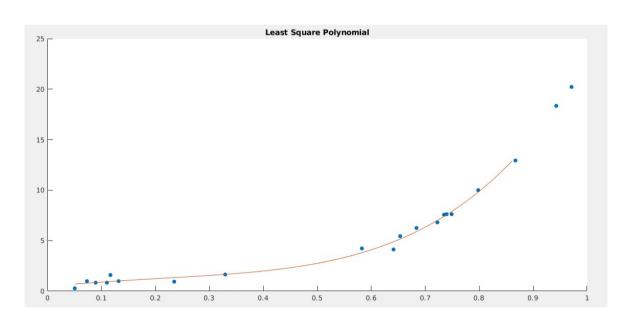
### **Output: (Quartic)**

LeastSquare Interpolation Polynomial.....

Coefficients of the Polynomial:

26.746661 -4.250426 -4.972829 4.773275 0.465837

R-sq = 0.996784



# **Splines**

### **Output:** (Linear spline)

+++ Output of Linear Spline Interpolation on given data set. +++

Coefficients of the equations in tabular form :

```
i c1 c0
```

1 0.198800 0.237300

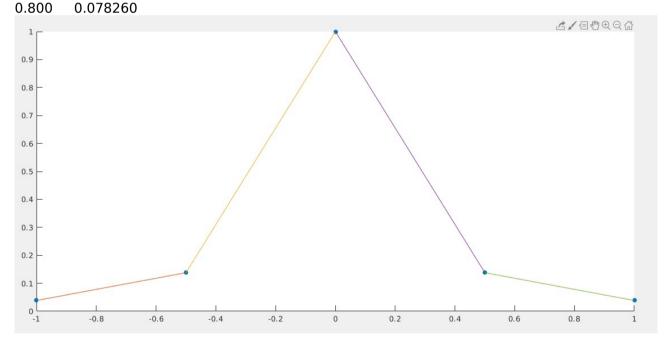
2 1.724200 1.000000

3 -1.724200 1.000000

4 -0.198800 0.237300

### Interpolated values y\* at give x\*:

```
x* y*
-0.800 0.078260
-0.200 0.655160
0.200 0.655160
```



# **Output:(Natural spline)**

Coefficients of the equations in tabular form:

```
i c3 c2 c1 c0
```

1 2.728571 8.185714 7.702371 2.283729

2 -7.541257 -7.219029 -0.000000 1.000000

3 7.541257 -7.219029 0.000000 1.000000

4 -2.728571 8.185714 -7.702371 2.283729

### 1st derivative and 2nd derivative at each node :

i 1st der 2nd der

0 -0.483343 0.000000

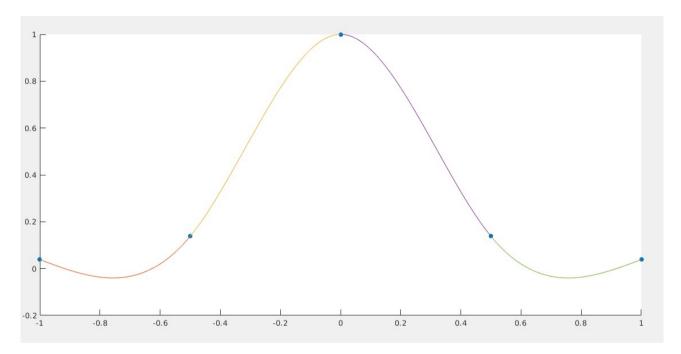
1 1.563086 8.185714

```
2 0.000000 -14.438057
3 -1.563086 8.185714
```

4 0.483343 0.000000

Interpolated values y\* at give x\*:

```
x* y*
-0.800 -0.036340
-0.200 0.771569
0.200 0.771569
0.800 -0.036340
```



# Output: (Not a knot spline)

Coefficients of the equations in tabular form:

```
i c3 c2 c1 c0
```

1 -4.973800 -5.935300 0.000000 1.000000 2 -4.973800 -5.935300 -0.000000 1.000000 3 4.973800 -5.935300 0.000000 1.000000 4 4.973800 -5.935300 -0.000000 1.000000

### 1st derivative and 2nd derivative at each node :

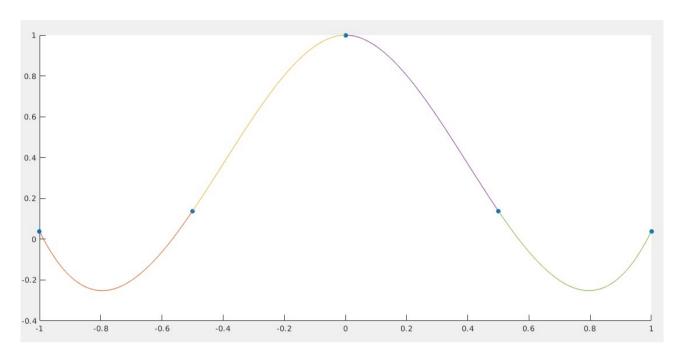
i 1st der 2nd der

0 -3.050800 17.972200
1 2.204950 3.050800
2 0.000000 -11.870600
3 -2.204950 3.050800
4 3.050800 17.972200

### Interpolated values y\* at give x\*:

x\* y\*

-0.800-0.252006-0.2000.8023780.2000.8023780.800-0.252006



### **Output: (Quadratic Spline)**

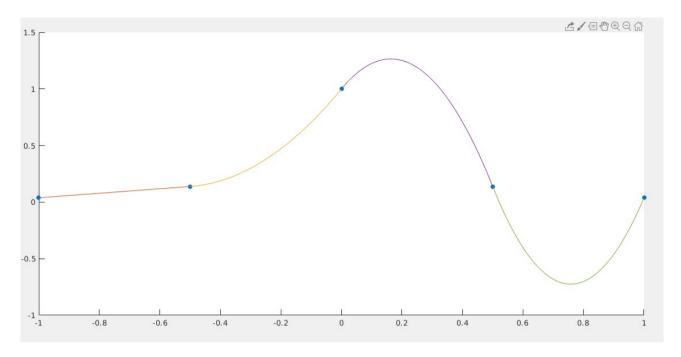
+++ Output of Quadratic Spline Interpolation on given data set. +++

Coefficients of the equations in tabular form :

i c2 c1 c0 -0.002400 0.195200 0.236100 1 2 3.053200 3.250800 1.000000 1.000000 3 -9.950000 3.250800 4 13.000800 -19.700000 6.737700

Interpolated values y\* at give x\*:

x\* y\*
-0.800 0.078404
-0.200 0.471968
0.200 1.252160
0.800 -0.701788



### **Output: (Periodic Spline)**

Coefficients of the equations in tabular form:

```
i c3 c2 c1 c0
```

- 1 4.775000 11.937500 9.748800 2.624800
- 2 -8.223400 -7.560100 0.000000 1.000000
- 3 8.223400 -7.560100 0.000000 1.000000
- 4 -4.775000 11.937500 -9.748800 2.624800

### 1st derivative and 2nd derivative at each node :

- i 1st der 2nd der
- 0 0.198800 -4.775000
- 1 1.392550 9.550000
- 2 0.000000 -15.120200
- 3 -1.392550 9.550000
- 4 -0.198800 -4.775000

### Interpolated values y\* at give x\*:

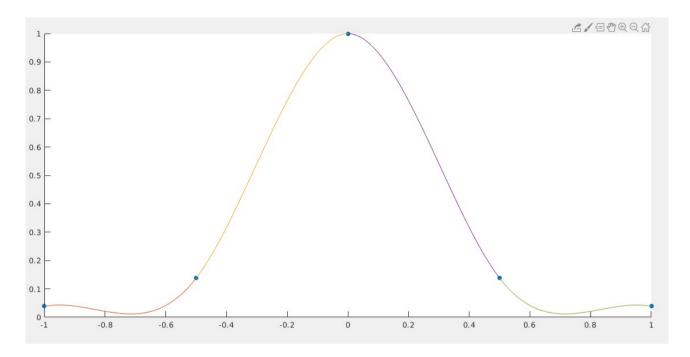
x\* y\*

-0.800 0.020960

-0.200 0.763383

 $0.200 \quad 0.763383$ 

0.800 0.020960



### **Output: (Clamped Spline)**

Coefficients of the equations in tabular form :

```
i
    с3
            c2
                   c1
                           c0
```

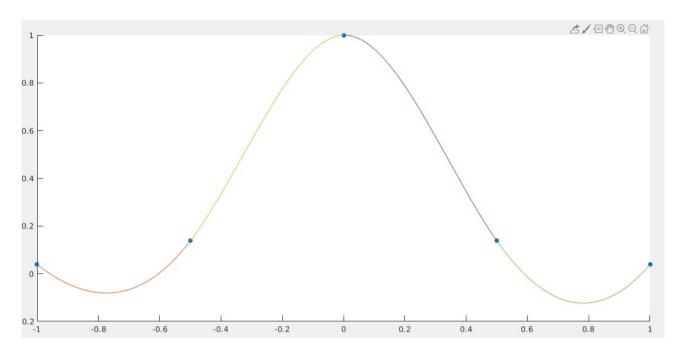
- 1.142886 5.254814 6.080971 2.007543
- 2 -6.917457 -6.835700 0.035714 1.000000 3 6.631743 -6.835700 0.035714 1.000000
- 4 0.285686 2.683386 -4.723829 1.793257

### 1st derivative and 2nd derivative at each node :

- 2nd der 1st der
- 0 -1.000000 3.652314
- 1 1.683321 7.080971
- 2 0.035714 -13.671400
- 3 -1.826179 6.223829
- 4 1.500000 7.080886

### Interpolated values y\* at give x\*:

```
y*
 x*
-0.800
        -0.079311
-0.200
        0.774769
0.200
        0.786769
0.800
        -0.122168
```



**Tutorial 9** 

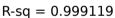
# **Question 1-a)**

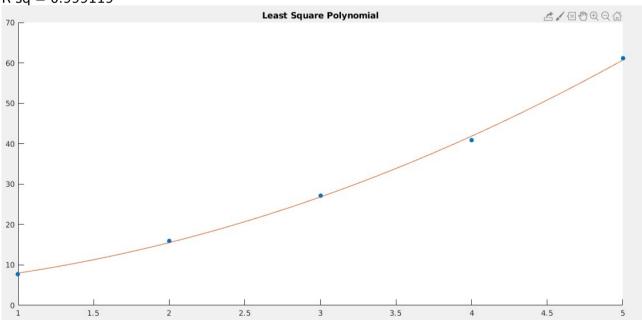
# Output:

LeastSquare Interpolation Polynomial.....

Coefficients of the Polynomial:

1.878571 1.898571 4.220000



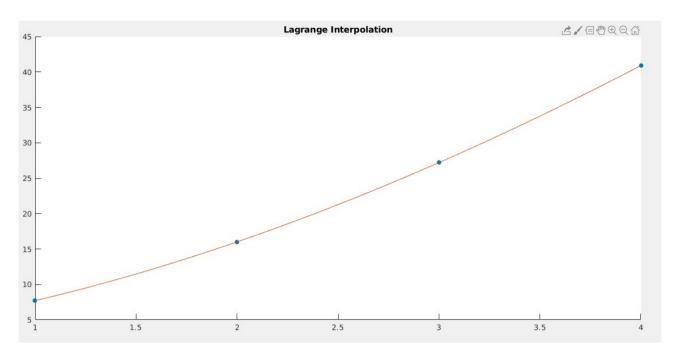


# **Question 1-b) Output:**

Lagrange Interpolation Polynomial.....

Coefficients of the Polynomial:

-0.066667 1.850000 3.216667 2.700000

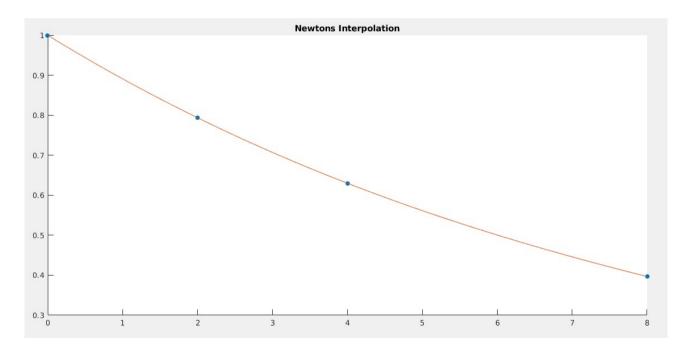


# **Question-2)a Output:**

Newton Interpolation Polynomial....

Coefficients of the Polynomial:

-0.000175 0.006375 -0.115200 1.000000

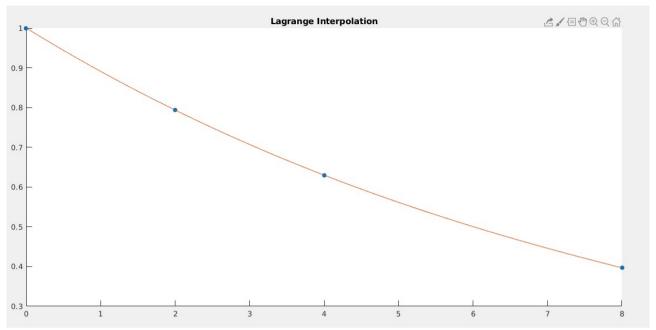


# **Question 2b Output:**

<u>Lagrange Interpolation Polynomial....</u>

Coefficients of the Polynomial:

-0.000175 0.006375 -0.115200 1.000000



# **Question 2c**

# **Output:**

### <u>Coefficients of the equations in tabular form :</u>

i c3 c2 c1 c0

1 0.001133 0.000000 -0.107683 1.000000

2 -0.000341 0.008843 -0.125370 1.011791

3 -0.000396 0.009509 -0.128030 1.015339

### 1st derivative and 2nd derivative at each node :

i 1st der 2nd der

0 -0.107683 0.000000

1 -0.094085 0.013598

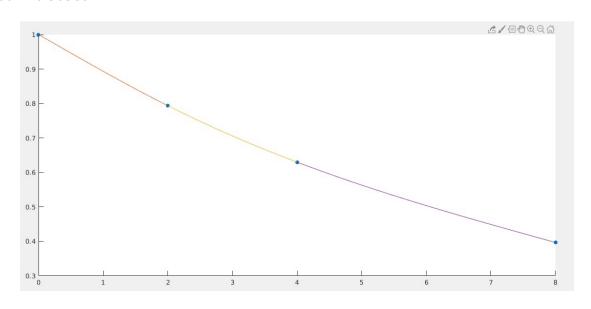
2 -0.070978 0.009509

3 -0.051961 0.000000

### Interpolated values $y^*$ at give $x^*$ :

x\* y\*

6.000 0.503891



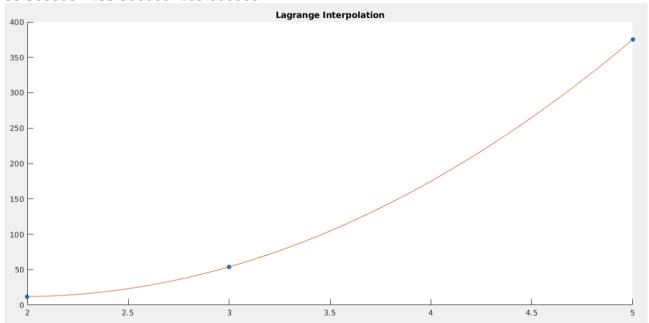
# **Question 3a**

### **Output:**

### Lagrange Interpolation Polynomial.....

Coefficients of the Polynomial:

39.500000 -155.500000 165.000000



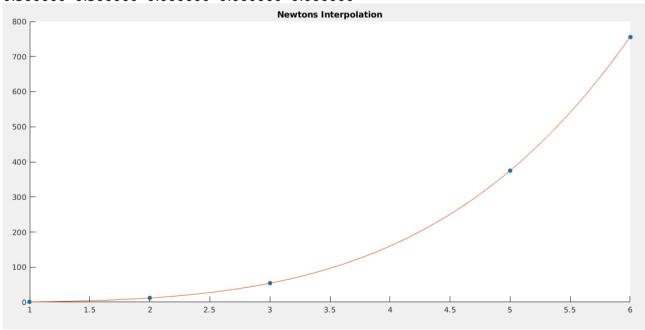
# **Question 3b**

### **Output:**

Newton Interpolation Polynomial.....

Coefficients of the Polynomial:

 $0.500000 \ 0.500000 \ 0.000000 \ 0.000000 \ 0.000000$ 



# **Question 4a**

### **Output:**

Coefficients of the equations in tabular form :

```
i c3 c2 c1 c0

1 0.668886 0.000000 1.130179 1.000000

2 0.022771 0.969171 0.645593 1.080764

3 1.423229 -3.232200 4.846964 -0.319693

4 -2.114886 12.689314 -19.035307 11.621443
```

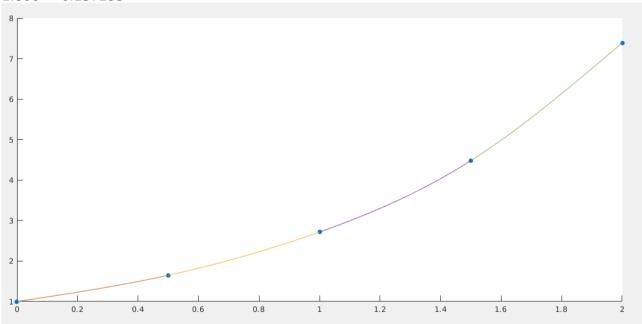
1st derivative and 2nd derivative at each node :

```
i 1st der 2nd der
0 1.130179 0.000000
1 1.631843 2.006657
2 2.652250 2.074971
3 4.757157 6.344657
4 6.343321 0.000000
```

Interpolated values  $y^*$  at give  $x^*$ :

x\* y\*

1.800 6.137255



# **Question 4b**

### **Output:**

### <u>Coefficients of the equations in tabular form :</u>

```
i c3 c2 c1 c0

1 0.304800 0.384600 1.028900 1.000000

2 0.304800 0.384600 1.028900 1.000000

3 0.659200 -0.678600 2.092100 0.645600

4 0.659200 -0.678600 2.092100 0.645600
```

1st derivative and 2nd derivative at each node :

i 1st der 2nd der

0 1.028900 0.769200

1 1.642100 1.683600

2 2.712500 2.598000

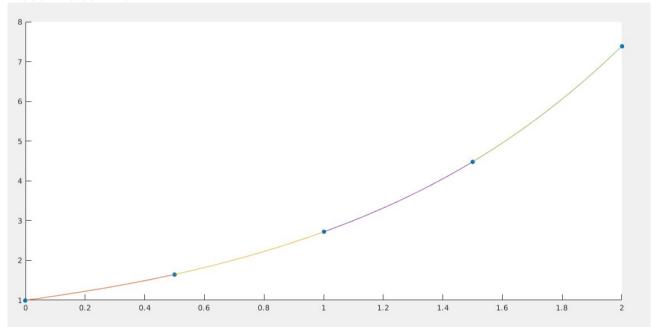
3 4.505900 4.575600

4 7.288100 6.553200

Interpolated values y\* at give x\*:

x\* y\*

1.800 6.057170



# **Tutorial 8**

# **Question 6**

### **Output:**

# LeastSquare Interpolation Polynomial.....

Coefficients of the Polynomial:

 $0.000976 - 0.011858 \ 0.055337 - 0.125882 \ 0.209676$ 

R-sq = 1.000000

