Varun Magotera Tutomial 6 (a. P(H) = 1 : P(T) = 1-1 P(H at K+1th toss) = P(Tat K toss and Hat K+1 th)
= (1-d) k d b let M be number of tosses required to get the first had and let S: 4 F (M) As topses are independent and expectation is additive S= Ax 1+ (1-A) x (S+1) 821+8+1-15-1 :. SX=1 2. 1 -> Random variable a. Variance of X: Var (X) = F[(X-F[X])2]
To priore Var (X) = F[X2]-F[X]2 Open that Var (A) = E[(X-E[X])2] Var (X) = E [12 - 2x F(X] + F (X)2] Var (X) = F[X2] - F[X]2 b. E[x]=0 and E[x2]=1 To find: 1 Variance of X

Var(X) = E(X2) = E(X12 = 1-0

Var (X) 2 1

Y= a+ bx 2 [[x2] = [[(a +bx)2]

> E[Y2]: E[a2+2abx+b2x2] E[Y2]: a2 + 2ab = [X] + b2 = FX9* $E[Y^2] = a^2 + 2ab(0) + b^2(1)$ F (y2) = Q2+b2

E(y): E(a+bx): a+bE(x)

E[Y] = a+b(0) :. E[Y]= a

Vau (Y) = E[Y] - E[Y] = a2+b2-a2

Var (4) = 62

3. a Guen a horse, the probability that it wins P(B) = P(B, A) + P(BOA) P(B) = P(B|A) P(A) + P(B|A) P(A) $P(B) = 6.99 \times 10^{-5} + (1-6.999) \times (1-10^{-5})$ $P(B) = 199 \times 10^{-5} - 6$

Propositity that AKU predicts a blade beauty is wing P(A(B) 2 0.99 10 -5 2 0.497