

# Assignment - 2

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## PROBLEM

**1. Find the in-center of the triangle formed by the following points lie,**

**i.  $5x-12y=0$ , ii.  $5x+12y+60=0$ , iii.  $5x+12y-60=0$**

## SOLUTION

First, we need to find the intersection point of given three lines,

Let's find the intersection of line (i) and (ii),

Let's write it vector form,

$$\begin{pmatrix} 5 & -12 \\ 5 & 12 \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix} = \begin{pmatrix} 0 \\ -60 \end{pmatrix}$$

By solving above equation, we are getting the intersection point of line (i) and (ii),  
Let's call it as M:

$$M = \begin{pmatrix} X \\ Y \end{pmatrix} = \begin{pmatrix} -6 \\ -2.5 \end{pmatrix} \quad (1)$$

In the same way, intersection of line (ii) and (iii) is,

$$\begin{pmatrix} 5 & 12 \\ 12 & 5 \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix} = \begin{pmatrix} -60 \\ 60 \end{pmatrix}$$

By solving above equation, we are getting the intersection point of line (ii) and (iii),  
Let's call it as N:

$$N = \begin{pmatrix} X \\ Y \end{pmatrix} = \begin{pmatrix} 8.571 \\ -8.571 \end{pmatrix} \quad (2)$$

In the same way, intersection of line (i) and (iii) is,

$$\begin{pmatrix} 5 & -12 \\ 12 & -5 \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix} = \begin{pmatrix} 0 \\ 60 \end{pmatrix}$$

By solving above equation, we are getting the intersection point of line (i) and (iii),  
Let's call it as O:

$$O = \begin{pmatrix} X \\ Y \end{pmatrix} = \begin{pmatrix} 4.260 \\ 1.775 \end{pmatrix} \quad (3)$$

Now we need to find difference between each vectors,

Difference between vectors N and O:

$$N = \begin{pmatrix} 8.571 \\ -8.571 \end{pmatrix}, O = \begin{pmatrix} 4.260 \\ 1.775 \end{pmatrix}$$

$$O-N = \begin{pmatrix} -4.311 \\ 10.345 \end{pmatrix}$$

$$\|O - N\| = \sqrt{(-4.311)^2 + 10.345^2}$$

$$\|O - N\| = 11.207 \quad (D_1)$$

Difference between vectors M and O:

$$M = \begin{pmatrix} -6 \\ -2.5 \end{pmatrix}, O = \begin{pmatrix} 4.260 \\ 1.775 \end{pmatrix}$$

$$O-M = \begin{pmatrix} 10.26 \\ 4.275 \end{pmatrix}$$

$$\|O - M\| = \sqrt{10.260^2 + 4.275^2}$$

$$\|O - M\| = 11.115 \quad (D_2)$$

Difference between vectors M and N:

$$M = \begin{pmatrix} -6 \\ -2.5 \end{pmatrix}, N = \begin{pmatrix} 8.571 \\ -8.571 \end{pmatrix}$$

$$N-M = \begin{pmatrix} 14.571 \\ -6.071 \end{pmatrix}$$

$$\|N - M\| = \sqrt{14.571^2 + 6.071^2}$$

$$\|N - M\| = 15.785 \quad (D_3)$$

Formula for finding in-center (I) of triangle with three given coordinates is,

$$\left( \frac{D_1M + D_2N + D_3O}{D_1 + D_2 + D_3}, \frac{D_1M + D_2N + D_3O}{D_1 + D_2 + D_3} \right)$$

By putting all the values,

$$\left( \frac{(11.207)(-6) + (11.115)(8.571) + (15.785)(4.260)}{11.207 + 11.115 + 15.785}, \frac{(11.207)(-2.5) + (11.115)(-8.571) + (15.785)(1.775)}{11.207 + 11.115 + 15.785} \right)$$

$$I = \begin{pmatrix} 2.500 \\ -2.499 \end{pmatrix}$$

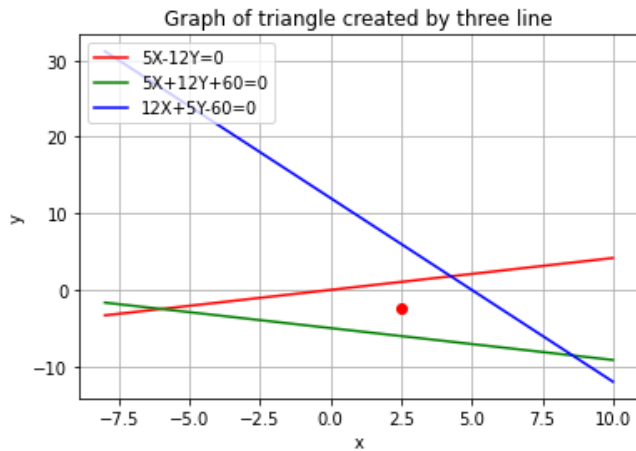


Fig. 1. Triangle created by three lines