

# Visionary Course

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## System and Modeling

# System

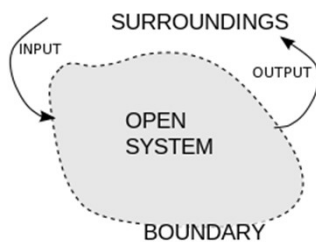


- What is the definition of system?
  - A system is a group of interacting or interrelated elements that act **according to a set of rules** to form a unified whole.

# System



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  - A system is a group of interacting or interrelated elements that act according to a set of rules to form a unified whole.



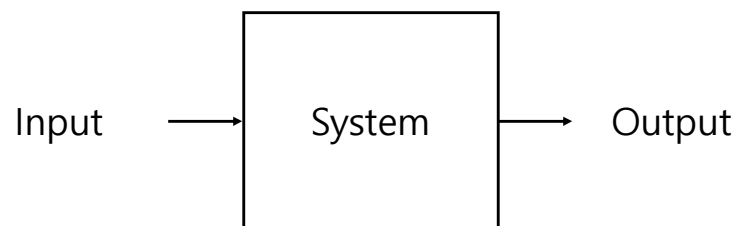
*Open systems* have input and output flows, representing exchanges of matter, energy or information with their surroundings.

# System Model



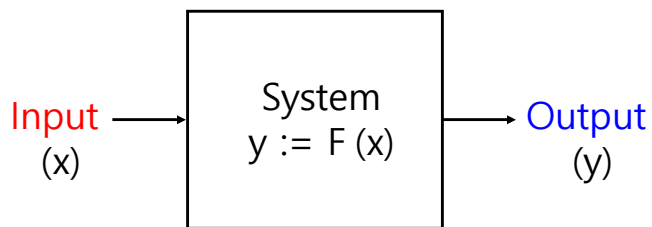
- What is the definition of model?
  - A model is an informative representation of an object, person or system.

## Modeling A System

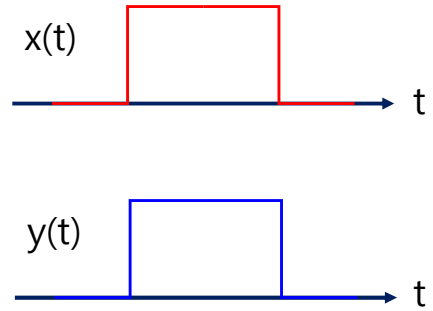


How to define the system?

## Example 1)

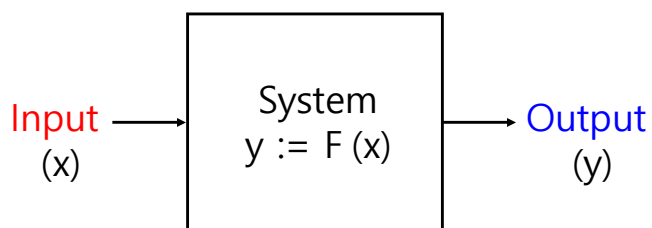


If  $x = y$ , then  $F(x) = x$

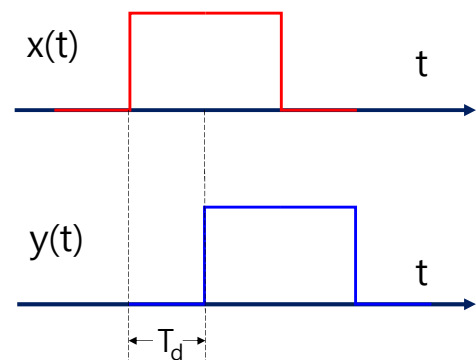


Real life example?

## Example 2) Delay $T_d$

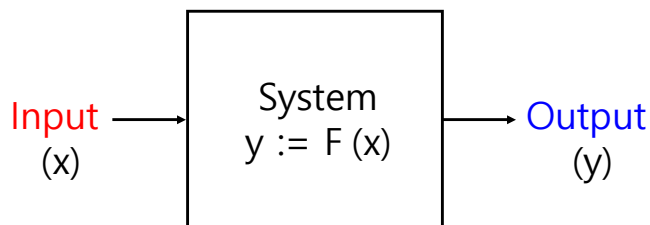


$y(t) = x(t - T_d)$



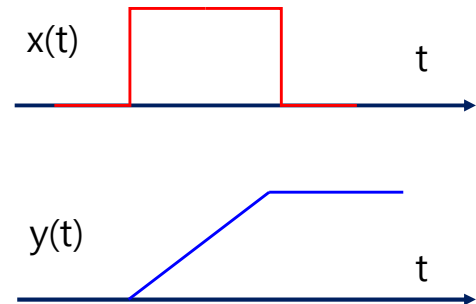
Real life example?

## Example 3)



$$y(t) = \int x(t) dt$$

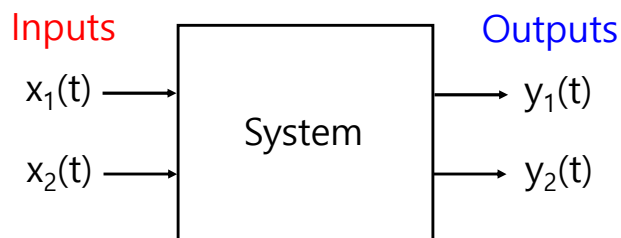
$$y'(t) = x(t)$$



Real life example?

## Example 4) MIMO Linear System

- 2x2 MIMO System



$$\begin{bmatrix} y_1(t) \\ y_2(t) \end{bmatrix} = \begin{bmatrix} 0.5 & 0.5 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x_1(t) \\ x_2(t) \end{bmatrix}$$

Linear Algebra, Vector, Matrix ...

$$y_1(t) = x_1(t) + 2 \cdot x_2(t)$$

$$y_2(t) = x_2(t)$$

Real life example?

# Categories of Systems

- # of inputs and outputs
  - Multiple Inputs and Multiple Output (MIMO)
  - Single Input and Single Output (SISO)
- Input and output types
  - Continuous system
  - Discrete system
- Relationship
  - Linear system
  - Non-linear system

# Group Discussion and Presentation

Make a 3-page ppt and give a 3-min presentation!

- Pick a system  
(e.g. mechanical, electrical, biological, economical, communication, automatic control ...)
- Define inputs and outputs of your system
- Describe the behaviors / dynamics / rules for the system  
(Is it possible to make a mathematical/logical representation?)

## Example 5) Forced Spring Mass System

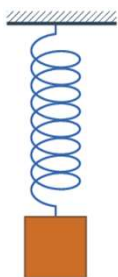


Dynamics equation:  $mx''(t) + kx(t) = f(t)$

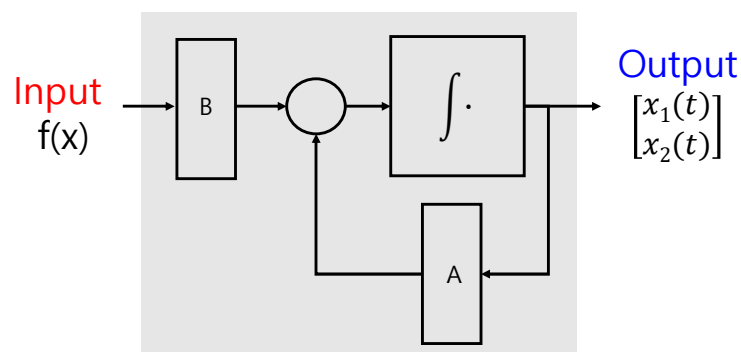
$$\begin{aligned} x_1(t) &= x(t) \\ x_2(t) &= x_1'(t) \end{aligned} \quad \Rightarrow \quad \begin{aligned} x_1'(t) &= x_2(t) \\ x_2'(t) &= x_1''(t) = -\frac{k}{m}x_1(t) + \frac{1}{m}f(t) \end{aligned}$$

$$\begin{bmatrix} x_1'(t) \\ x_2'(t) \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -\frac{k}{m} & 0 \end{bmatrix} \begin{bmatrix} x_1(t) \\ x_2(t) \end{bmatrix} + \begin{bmatrix} 0 \\ \frac{1}{m} \end{bmatrix} f(t)$$

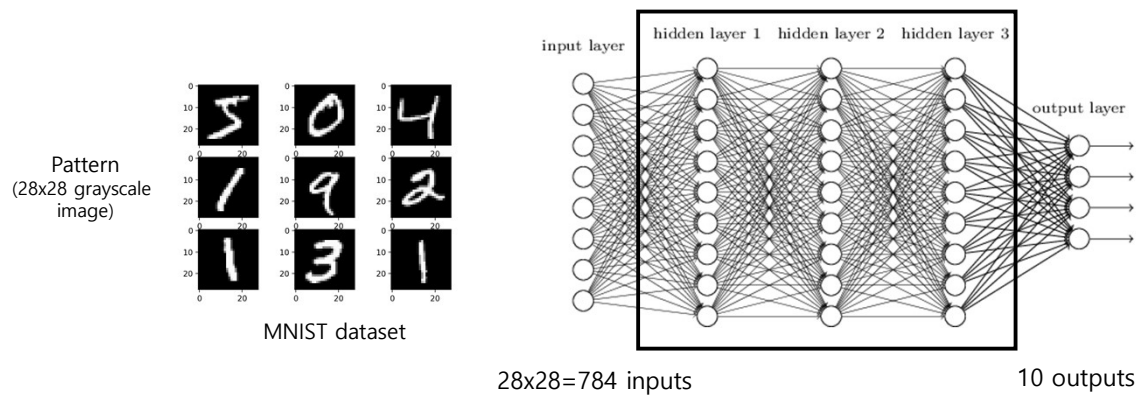
## Example 5) Forced Spring-Mass System



$$\begin{bmatrix} x_1'(t) \\ x_2'(t) \end{bmatrix} = \underbrace{\begin{bmatrix} 0 & 1 \\ -\frac{k}{m} & 0 \end{bmatrix}}_A \underbrace{\begin{bmatrix} x_1(t) \\ x_2(t) \end{bmatrix}}_B + \begin{bmatrix} 0 \\ \frac{1}{m} \end{bmatrix} f(t)$$



## Example 6) Artificial Neural Network



## Signals



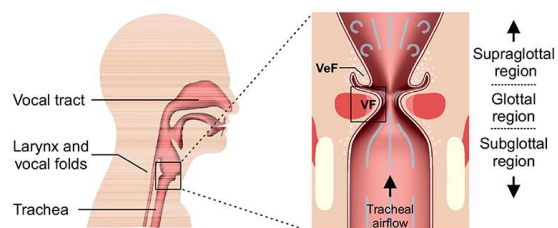
# Signal



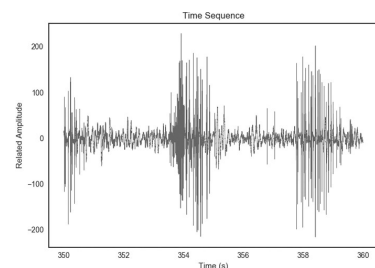
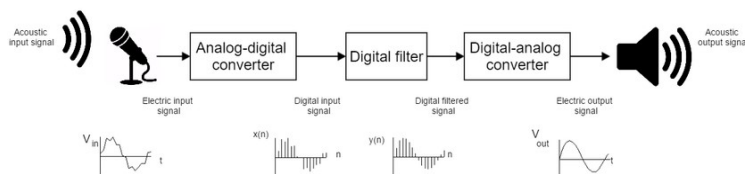
- In signal processing, a signal is a **function that conveys information** about a phenomenon.
- In electronics and telecommunications, it refers to any time **varying voltage, current, or electromagnetic wave** that carries information.
- A signal may also be defined as **an observable change in a quality** such as quantity.

## 1) Acoustic Signal

- Voice production

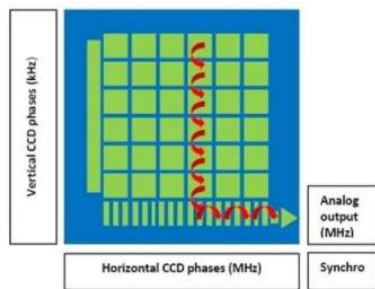


- Capture and signal processing "system"



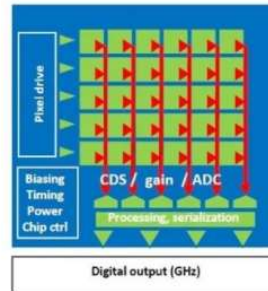
## 2) Image Signal

Charge Coupled Devices (CCDs)



CCD = Photon-to-electron conversion (analog)

Complementary Metal-Oxide-Semiconductor (CMOS) Sensor



CIS = Photon-to-Voltage conversion (digital)

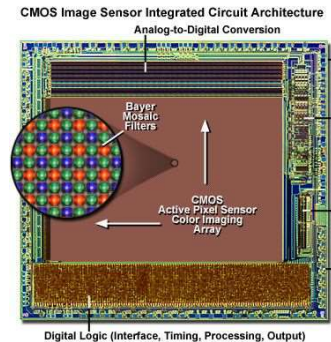


Figure 1

<https://www.azom.com/article.aspx?ArticleID=16321>

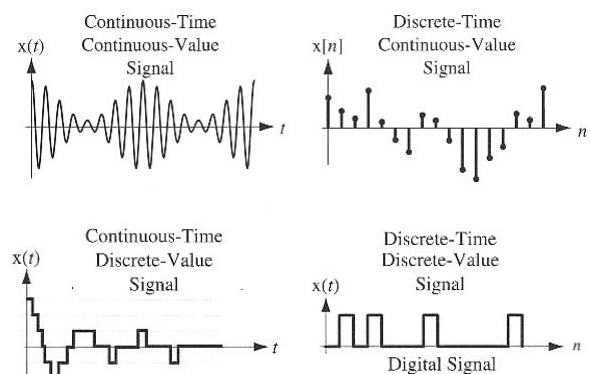
<https://www.olympus-lifescience.com/ko/microscope-resource/primer/digitalimaging/cmosimagesensors/>

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## Signal Types

|                 | Continues Time                       | Discrete Time |
|-----------------|--------------------------------------|---------------|
| Continues Value | Analog                               | Discrete      |
| Discrete Value  | Continues-Time Discrete Value Signal | Digital       |



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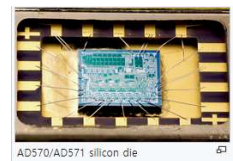
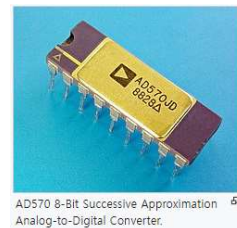
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# Analogy to Digital Conversion

- Sampling and quantization

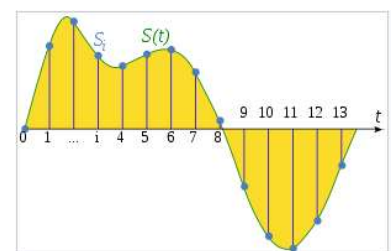
|                 | Continues Time                       | Discrete Time |
|-----------------|--------------------------------------|---------------|
| Continues Value | Analog                               | Discrete      |
| Discrete Value  | Continues-Time Discrete Value Signal | Digital       |

Sampling (Analog → Discrete)  
Quantization (Discrete → Digital)



## Sampling

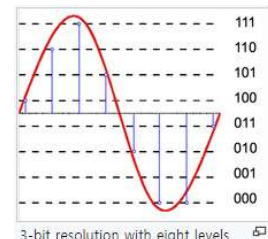
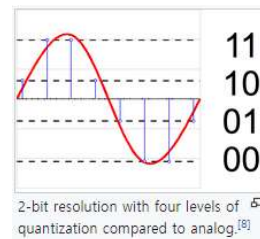
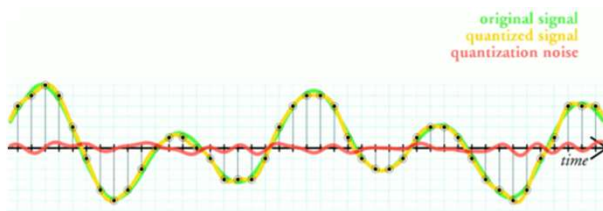
- In signal processing, sampling is the reduction of a continuous-time signal to a discrete-time signal.
- A common example is the conversion of a sound wave to a sequence of "samples".
- A sample is a value of the signal at a point in time and/or space.



Signal sampling representation. The continuous signal  $S(t)$  is represented with a green colored line while the discrete samples are indicated by the blue vertical lines.

# Quantization

- Quantization, in mathematics and digital signal processing, is the process of mapping input values from a large set (often a continuous set) to output values in a (countable) smaller set, often with a finite number of elements.



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Any tradeoff?

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## Group Discussion and Presentation

Make a 3-page ppt and give a 3-min presentation!

- Pick one of your smartphones
- Investigate its hardware and software including Apps.
- Any signal, sampling, quantization techniques are used?
- What are the specification of ADC/DAC?

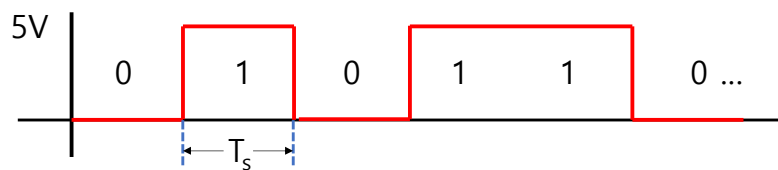
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### 3) Communication Signal

For a given series of binary values,  
how can we generate a signal (waveform)? → Modulation

010110 ...



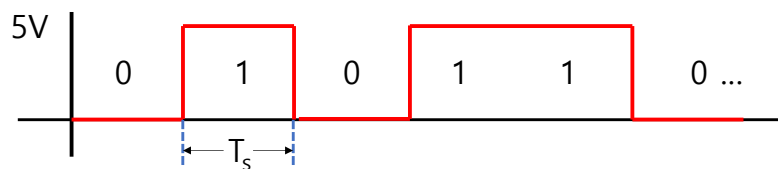
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### 3) Communication Signal

For a given series of binary values,  
how can we generate a signal (waveform)?

010110 ...



Transmit Speed: 1 bit/ $T_s$

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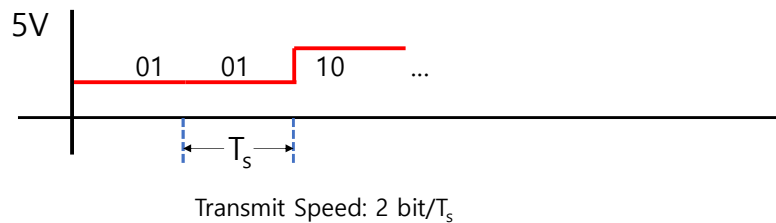
Can be higher?

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### 3) Communication Signal

Change amplitude: 00 → 0V, 01 → 1.6V, 10 → 3.3V, 11 → 5V

010110 → 01/01/10 → 1.6V/1.6V/3.3V

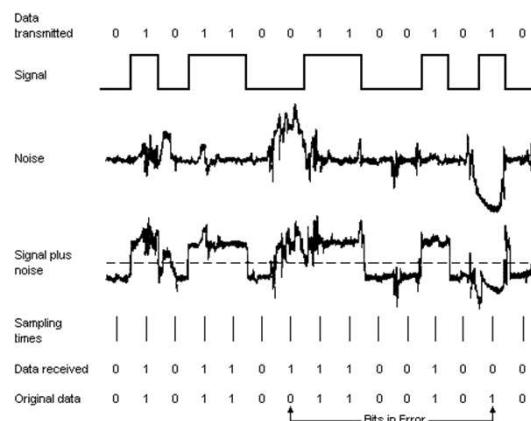


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Can be higher and higher?  
Any Tradeoff?

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### Noisy Signal



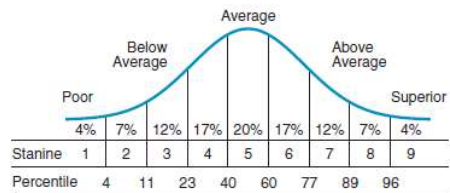
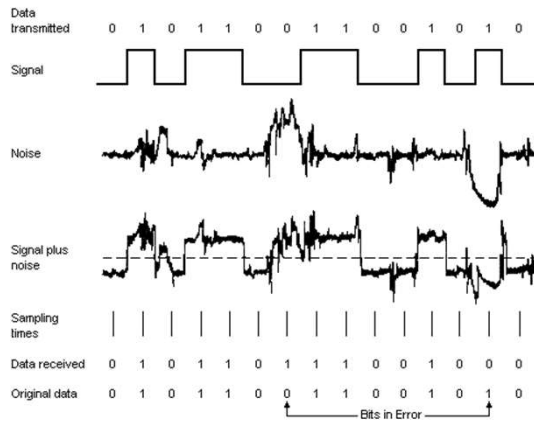
<https://www.autodesk.com/products/eagle/blog/top-5-techniques-terminating-transmission-lines/>

Calculate bit error rate?

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# Noisy Signal



Normal distribution

Statistics, probability, distribution

# Noisy Signal



The original image. Noisy image (noise density 50%). Image denoised with linear interpolation and median filter.



# Noisy Signal

- How much noisy is the signal?

# Noisy Signal

- How much noisy is the signal?
- Signal-to-noise ratio (SNR)  
Signal-to-interference-plus-noise ratio (SINR)

$$SINR = \frac{S}{I + N}$$

$S$  : signal power,  $I$  : interference power,  $N$  : noise



# Shannon Limit

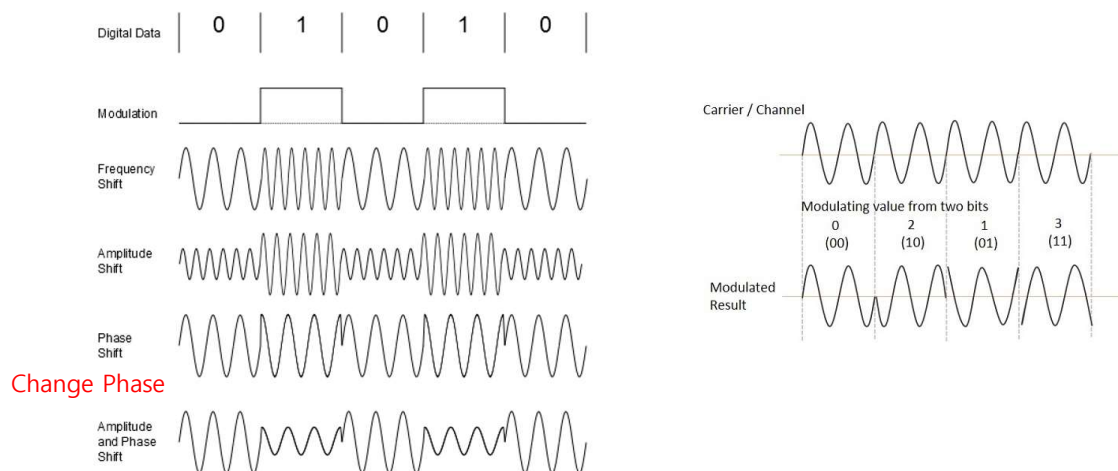
- Shannon-Hartley theorem

- Proved by Bell Labs research Claude Shannon in 1948.
- Gives the capacity of a communication channel.
- Many communication systems in use do not achieve the capacity, however, it provides a useful upper bound.

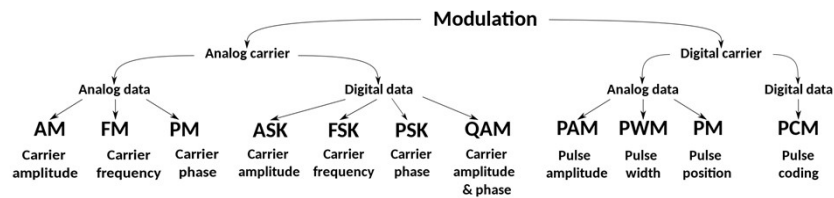
- C: max capacity in bits per second
- W: bandwidth in Hertz

$$C \leq W \log_2 \left( 1 + \frac{S}{N} \right)$$

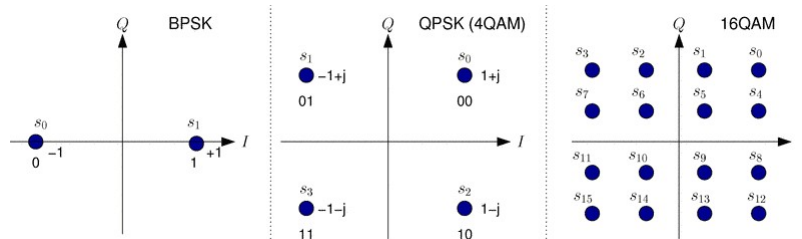
## 3) Communication Signal



### 3) Communication Signal



<https://www.wikiwand.com/en/Modulation>



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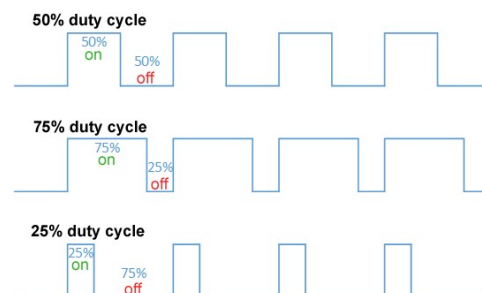
Complex number

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### 4) Pulse-width Modulation (PWM)



- Pulse-width modulation (PWM), or pulse-duration modulation (PDM), is a method of reducing the average power delivered by an electrical signal, by effectively chopping it up into discrete parts.

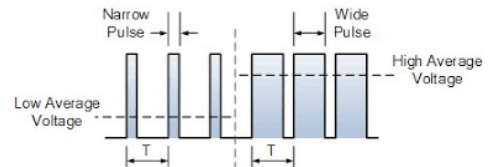


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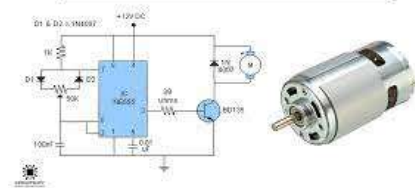
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## 4) Pulse-width Modulation (PWM)

- The average value of voltage (and current) fed to the load is controlled by turning the switch between supply and load on and off at a fast rate.
- The longer the switch is on compared to the off periods, the higher the total power supplied to the load.
- PWM is particularly suited for running inertial loads such as motors, which are not as easily affected by this discrete switching, because their inertia causes them to react slowly.



### DC Motor Control PWM



## Any Questions?

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