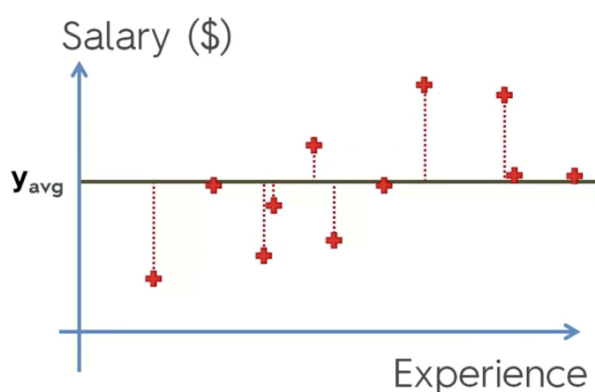


Adjusted R Squared Intuition

Adjusted R²

Simple Linear Regression:



$$SS_{res} = \text{SUM } (y_i - \hat{y}_i)^2$$

$$SS_{tot} = \text{SUM } (y_i - y_{avg})^2$$

$$R^2 = 1 - \frac{SS_{res}}{SS_{tot}}$$

Adjusted R²

$$R^2 = 1 - \frac{SS_{\text{res}}}{SS_{\text{tot}}}$$

$$y = b_0 + b_1 \cdot x_1$$

$$y = b_0 + b_1 \cdot x_1 + b_2 \cdot x_2$$

Adjusted R²

$$R^2 = 1 - \frac{SS_{\text{res}}}{SS_{\text{tot}}}$$

$$y = b_0 + b_1 \cdot x_1$$

$$y = b_0 + b_1 \cdot x_1 + b_2 \cdot x_2$$

$$SS_{\text{res}} \rightarrow \text{Min}$$

Adjusted R²

$$R^2 = 1 - \frac{SS_{\text{res}}}{SS_{\text{tot}}}$$

R² – Goodness of fit
(greater is better)

$$y = b_0 + b_1 \cdot x_1$$

Problem:

$$y = b_0 + b_1 \cdot x_1 + b_2 \cdot x_2 \leftarrow + b_3 \cdot x_3$$

$$SS_{\text{res}} \rightarrow \text{Min}$$

Adjusted R²

$$R^2 = 1 - \frac{SS_{\text{res}}}{SS_{\text{tot}}}$$

R² – Goodness of fit
(greater is better)

$$y = b_0 + b_1 \cdot x_1$$

Problem:

$$y = b_0 + b_1 \cdot x_1 + b_2 \cdot x_2 \leftarrow + b_3 \cdot x_3$$

$$SS_{\text{res}} \rightarrow \text{Min} \longrightarrow R^2 \text{ will never decrease}$$

Adjusted R²

$$R^2 = 1 - \frac{SS_{\text{res}}}{SS_{\text{tot}}}$$

$$\text{Adj } R^2 = 1 - (1 - R^2) \frac{n - 1}{n - p - 1}$$

p - number of regressors

n - sample size