

## Sparse Table

$$\text{arr} = \{a_0, a_1, a_2, a_3, a_4, a_5\}$$

$$\begin{array}{l|l} \text{table}[0][0] = a_0 & \text{table}[0][1] = \min(a_0, a_1) \\ \text{table}[1][0] = a_1 & \text{table}[1][1] = \min(a_1, a_2) \\ \text{table}[2][0] = a_2 & \text{table}[2][1] = \min(a_2, a_3) \\ \vdots & \text{table}[3][1] = \min(a_3, a_4) \\ \text{table}[5][0] = a_5 & \text{table}[4][1] = \min(a_4, a_5) \end{array}$$

$$\text{table}[i][j]$$

$$[0, 14]$$

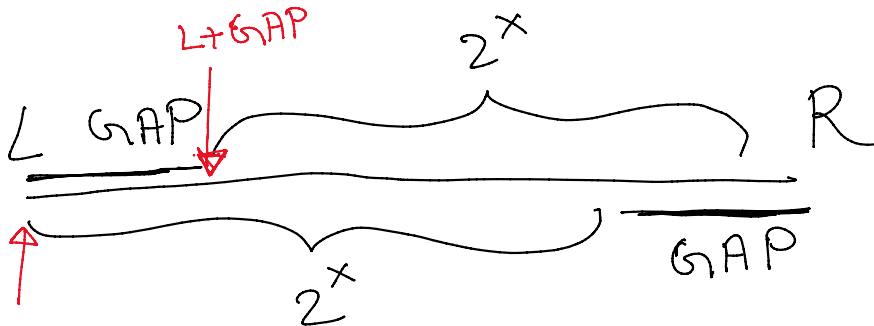
$$[0, 7], [8, 11], [12, 13]$$

$$\text{table}[0][2] = \min(a_0, a_1, a_2, a_3) = \text{table}[0][1], \text{table}[1][1]$$

$$\text{table}[1][2] = \min(a_1, a_2, a_3, a_4) = \text{table}[1][1], \text{table}[2][1]$$

$$\text{table}[2][2] = \min(a_2, a_3, a_4, a_5)$$

$$[0, 7], [7, 14]$$

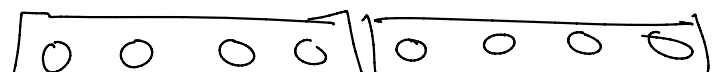


$$\min(\text{table}[L][x], \text{table}[L + \text{GAP}][x]);$$

## Dynamic Programming:

$$T[0][3] = \min(\text{table}[0][2], \text{table}[4][2]);$$

$$\begin{array}{cc} \text{len} = 8 & \text{len} = 4 \\ [0 \dots 7] & [0 \dots 3] \end{array}$$



$[0 \dots 7]$   
0, 1, 2, 3, 4, 5, 6, 7

$[0 \dots 3]$   
0, 1, 2, 3



$$T[i][2^j] = \min(T[i][2^{j-1}], T[\underline{i+2^{j-1}}][2^{j-1}]) + T[\text{startingIdx}][\log_2(\text{length})]$$

$$T[i][j] = \min(T[i][j-1], T[i + (1 \ll (j-1))][j-1])$$

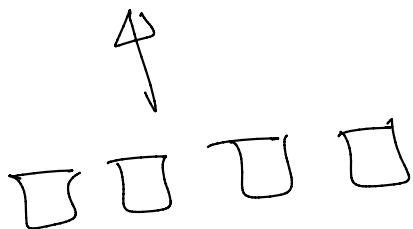
$$\begin{array}{r} 2^3 \cdot 5^1 \cdot 7^0 \\ \hline a_0 \quad a_1 \quad a_2 \quad a_3 \quad a_4 \\ \hline 2^2 \cdot 5^2 \cdot 7^3 \\ \dots \end{array}$$

$$\begin{array}{r} 2^2 \cdot 5^1 \cdot 7^0 \\ 2 \cdot 5 \cdot 7^0 \end{array}$$

sparse table + LCA

LCA = Lowest Common Ancestor

$$\text{Gap} = L[v] - L[u]$$



$$14$$

$$8 + 4 + 2$$

$N, Q \rightarrow u, v$

