## **Differential Equations**

The updated system of equations, considering a higher alien death rate due to environmental adaptation ( $\gamma = 0.01$ ) and recruitment ceasing when aliens are eliminated, is given by:

$$\frac{dH}{dt} = r_H H - \beta MA - \delta HA - kH$$
 
$$\frac{dM}{dt} = kH - \beta MA$$
 
$$\frac{dA}{dt} = r_A A - \alpha MA - \gamma A - C\lambda H$$

Where recruitment (kH) ceases if A=0.

## Constants and Their Meanings

- $r_H = 0.03$ : Human civilian population growth rate. Represents the natural growth of the civilian population.
- k = 0.02: Recruitment rate of civilians into the military. Determines how many civilians join the military. Recruitment ceases if aliens (A) are eliminated.
- $r_A = 0.005$ : Alien population growth rate. Represents the natural growth of the alien population.
- $\alpha = 0.0005$ : Death rate of aliens due to military combat. Determines the effectiveness of military forces against aliens.
- $\beta = 0.005$ : Death rate of human military due to aliens. Indicates how lethal aliens are to the military.
- $\gamma = 0.01$ : Death rate of aliens due to environmental adaptation challenges. Increased to model aliens struggling to adapt to Earth's environment.
- $\lambda = 0.00002$ : Death rate of aliens due to non-military human actions. Represents the impact of civilians resisting the aliens.
- $\delta = 0.00001$ : Death rate of civilians due to alien actions. Models the lethality of alien attacks on civilians.
- $\bullet$  C=0.0005: Probability factor for civilians killing aliens. Adjusts the impact of non-military human resistance on aliens.

## Terms in the Equations

- $r_H H$ : Natural growth of the civilian population.
- $\beta MA$ : Losses to civilians and military due to combat with aliens.
- $\delta HA$ : Civilian losses due to alien attacks.
- $\bullet$  kH: Civilians recruited into the military. Recruitment ceases if aliens (A) are eliminated.
- $kH \beta MA$ : Recruitment increases military population, but combat reduces it.
- $r_AA$ : Natural growth of the alien population.
- $\alpha MA$ : Alien losses due to military combat.
- $\gamma A$ : Alien losses due to environmental factors. Increased to model higher adaptation challenges.
- $C\lambda H$ : Alien losses due to civilian resistance.