

1. Calculate the expectation for the uniform distribution on  $[a, b]$ .

**Solution**

$$\Rightarrow E(X) = \int_a^b \frac{x}{b-a} dx = \frac{1}{b-a} \left[ \frac{x^2}{2} \right], \text{ from } a \rightarrow b \Rightarrow \frac{b+a}{2} = \frac{1}{2}(b+a)$$

2. Calculate the distribution function for the exponential distribution with parameter  $\lambda$

**Solution**

$$\Rightarrow \text{From } f'(x) = -e^{-\Lambda x}, \text{ diff wrt } x \text{ we have, } f(x) = -\Lambda(-e^{-\Lambda x})$$

$$\Rightarrow \text{Therefore, } f(x) = \Lambda e^{-\Lambda x}, \text{ which is the probability distribution function for exponential distribution}$$