

For simplicity we let the following components be defined by the variables as follows: 1. $C_{CO_2} = A$ 2. $CH_2O = B$ 3. $O_{CO_2} = C$ 4. $O_{H_2O} = P$ -We first convert the Pdes (1) and (2) using the 'Method of Lines' so as to form a system of coupled Odes -we will then use the ODEINT function to solve the system -Finally we plot the results using matplotlib

In [75]:

```
# -*- coding: utf-8 -*-  
"""
```

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```
"""
```

```
#importing important libraries  
import numpy as np  
import matplotlib.pyplot as plt  
from scipy.integrate import odeint  
import pandas as pd
```

```
#writing the function for the coupled system of equations
```

```
def coupled_pde_func(x,t):
```

```
    #defining all the required constants
```

```
    k1=60
```

```
    k2=12
```

```
    k3=19.6
```

```
    k4=75.1
```

```
    k5=19.8
```

```
    kCo2=375.3
```

```
    Co2=0.1889
```

```
    ohmCo2=0.038
```

```
    N=20
```

```
    L=1
```

```
    dx=L/N
```

```
    DCo2=0.549
```

```
    DH2O=0.873
```

```
    dt=0.1
```

```
    t_final=150 #--final time(t=150)
```

```
    T0=0 #---initial time (t=0)
```

```
    #assigning each ODE a vector element (Conversion from scalar to vector  
components)
```

```
    A=x[0] # ---A= Cco2
```

```
    B=x[1] # ---B=CH2o
```

```
    C=x[2] # ---C=OCo2
```

```
    P=x[3] # ---P=OH2O
```

```
    t = np.linspace(0, 10, 150) #--defining the time vector ranging from 0-10(can be  
changed based on ones preference)
```

```
    dt = np.diff(t) #--defining the change in time (t)
```

```
    x=np.linspace(dx/2,L-dx/2,N) #--converting the x-components into a sort of array  
with given dimensions
```

```
    A=np.ones(N)*T0 #--initializing the vector functions to start at  
time (t=0)
```

```
    B=np.ones(N)*T0
```

```

C=np.ones(N)*T0
P=np.ones(N)*T0
dAdt=np.empty(N)          #--initializing the derivertives for components
A,B,C,P
dBdt=np.empty(N)
dCdt=np.empty(N)
dPdt=np.empty(N)
t1=np.arange(0,150,0.1)    #--defining a variable (t1) to setting the end point
for our derivertive functions

#defining the ODES
for j in range(1,len(t1)):  #running a nested for_loop to help in defining the
Odes
    for i in range(1,N-1):
        #the 4-system of coupled equations
        dAdt[i]=-(A[i+1]-A[i-1])/2*dx+(DCo2*(A[i+1]-2*A[i]+A[i-1]))/dx**2-(k1-
Co2)*(1-C[i]-P[i])

dBdt[i]=-(B[i+1]-B[i-1])/2*dx+(DH2O*(B[i+1]-2*B[i]+B[i-1]))/dx**2+k2*A[i]*P[i]-k3*(1-
C[i]-P[i])-(k4*B[i])/(1+Co2*A[i])
dCdt[i]=-((k1*Co2)*(1-C[i]-P[i]))/ohmCo2
dPdt=(k2*A*P)-k3*(1-C-P)-(k4*B*C)/(1+kCo2*A)+k5*A*C*P

#the function returns several outputs,so you can run each to see the
output
df0=[dAdt[0],dBdt[0],dCdt[0],dPdt[0]]
# df1=[dAdt[1],dBdt[1],dCdt[1],dPdt[1]]
# df2=[dAdt[2],dBdt[2],dCdt[2],dPdt[2]]
# df3=[dAdt[3],dBdt[3],dCdt[3],dPdt[3]]

return df0

#printing out some initial conditions
x0=[0.83,0.59,0.8,150]

#print(coupled_pde_func(x=x0,t=0))
s=(coupled_pde_func(x=x0,t=0))

##solving the system using odeint ----declaring a time vector

t=np.linspace(0,2,10)      #---you can change the values of the parameter
depending on the choice

x=odeint(coupled_pde_func,x0,t) #---calling the ODEINT function to solve our
coupled_system of equations

A=x[:,0]    #storing the outputs of the ODEINT results in the following defined
vector components
B=x[:,1]
C=x[:,2]
P=x[:,3]

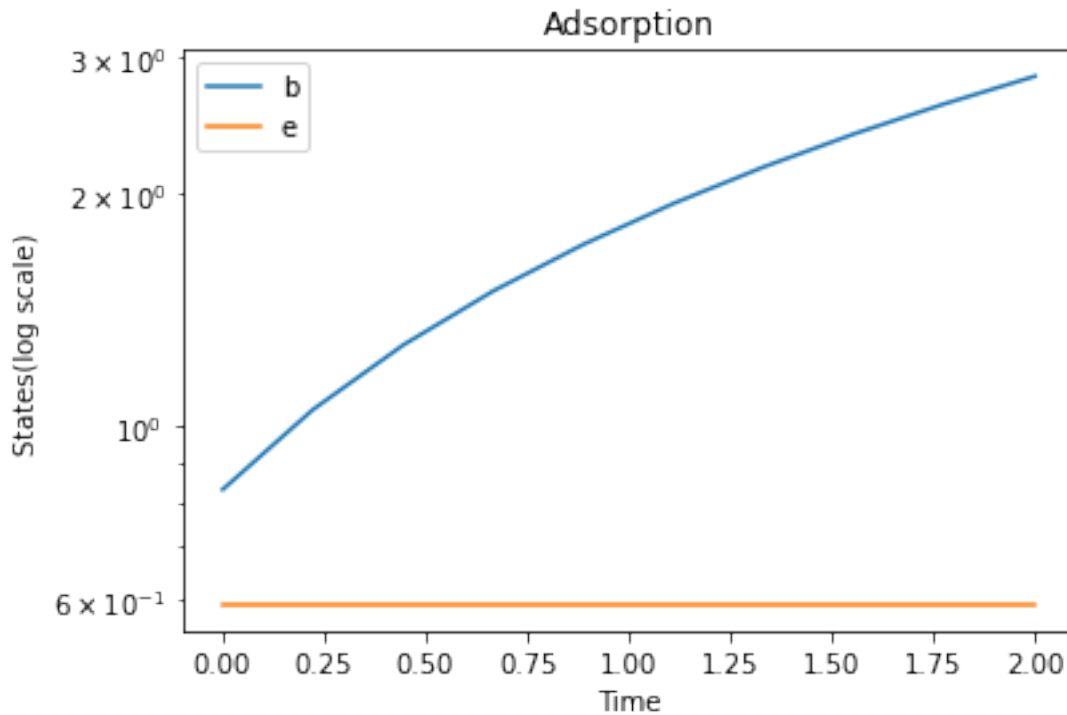
plt.semilogy(t,A,label='Cco2') #--plotting the Components Cco2,CH2O,0Co2,0H2O

```

```
plt.semilogy(t,B,label='CH2o')    #--using the semilogy function for a better scaling
for exponentially increasing components
plt.ylabel('States(log scale)')
plt.title('Adsorption')
plt.xlabel('Time')
plt.legend('best')
plt.show
```

Out[75]:

```
<function matplotlib.pyplot.show(close=None, block=None)>
```



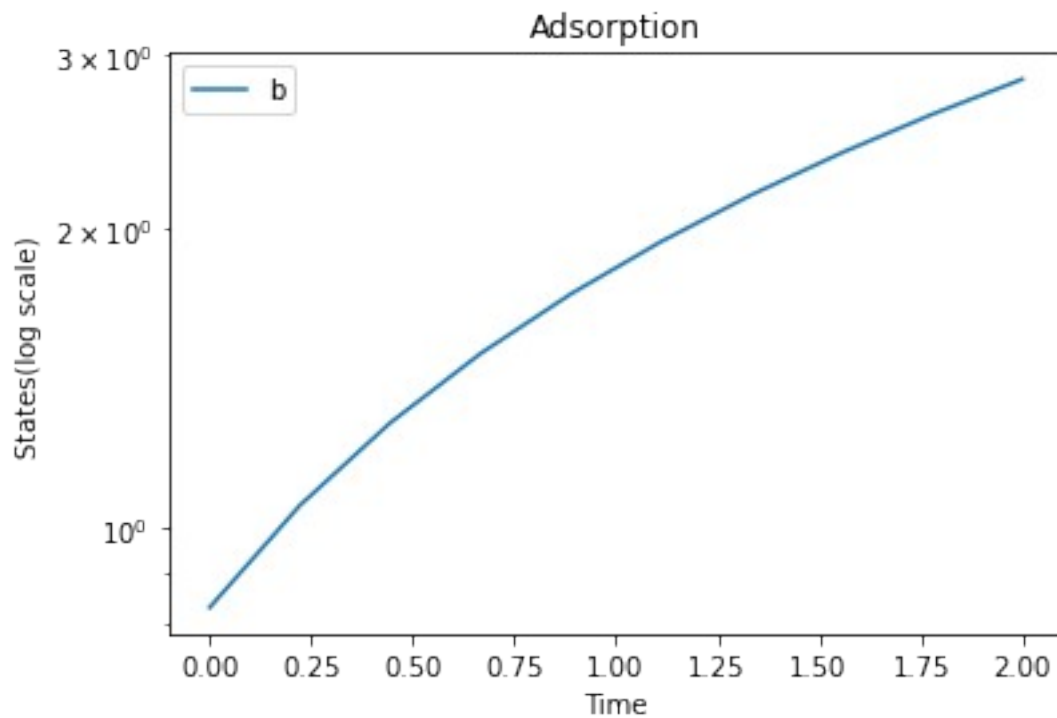
Plotting each component independently

In [76]:

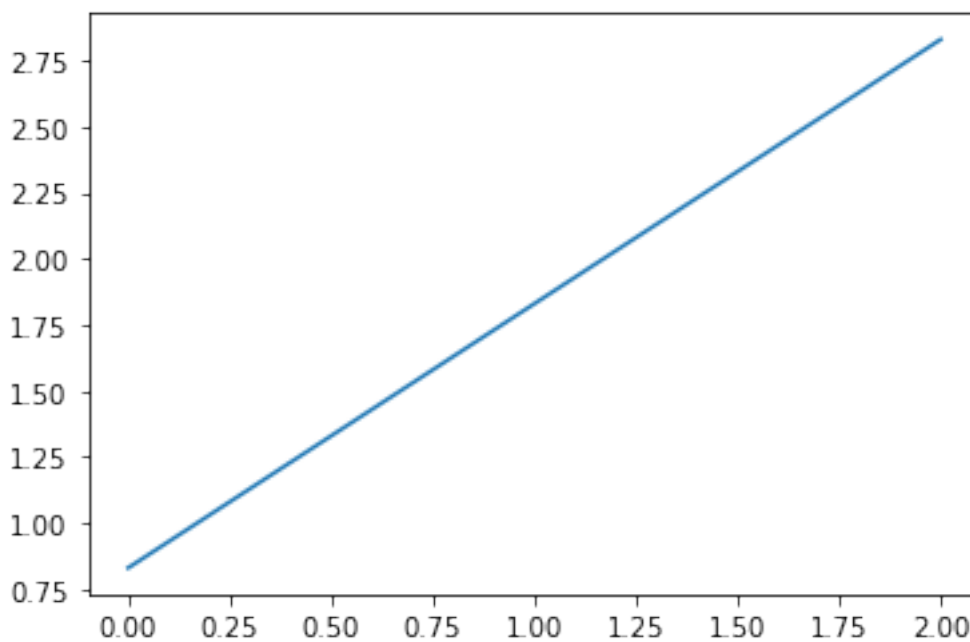
```
plt.semilogy(t,A,label='Cco2')    #--plot for component Cco2
plt.ylabel('States(log scale)')
plt.title('Adsorption')
plt.xlabel('Time')
plt.legend('best')
plt.show
```

Out[76]:

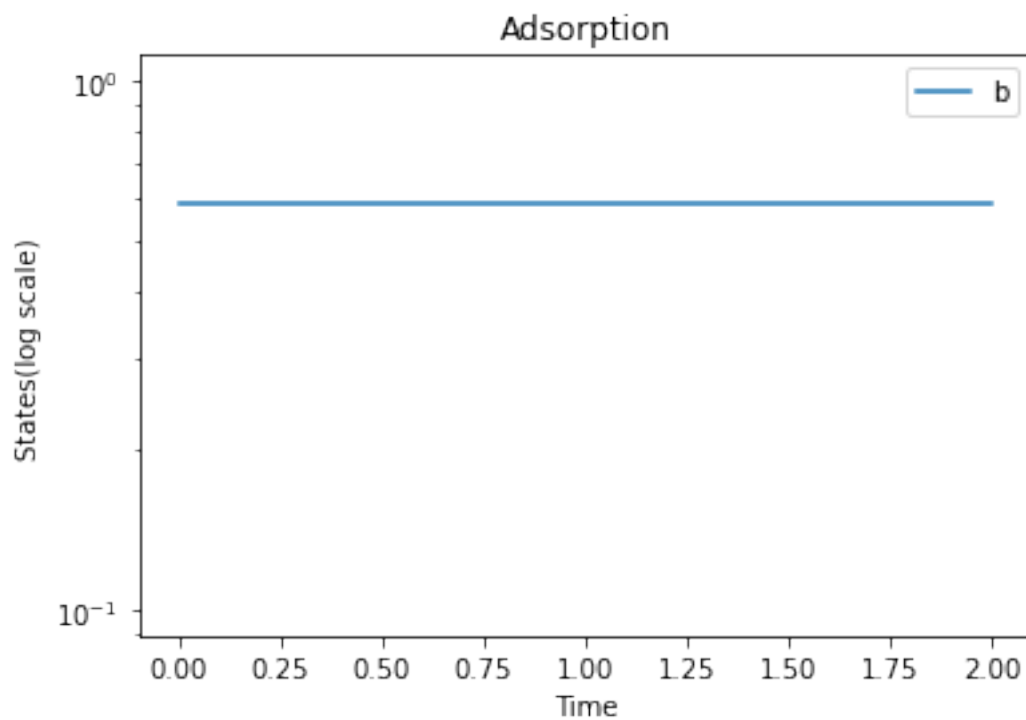
```
<function matplotlib.pyplot.show(close=None, block=None)>
```



```
In [82]:
plt.plot(t,A, label='Cco2')
Out[82]:
[<matplotlib.lines.Line2D at 0x22ff67a61f0>]
```

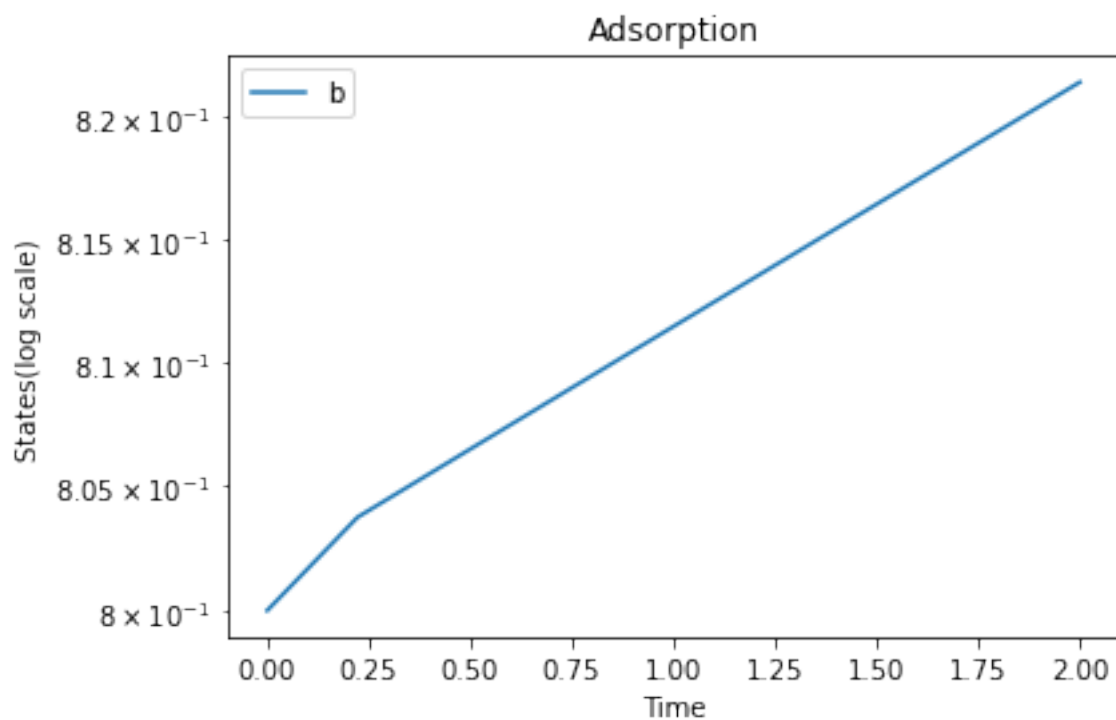


```
In [88]:
plt.semilogy(t,B, label='CH2o')    #--plot for component CH2o
plt.ylabel('States(log scale)')
plt.title('Adsorption')
plt.xlabel('Time')
plt.legend('best')
plt.show
Out[88]:
<function matplotlib.pyplot.show(close=None, block=None)>
```



```
In [89]:
plt.semilogy(t,C,label='0Co2')      #--plot for component 0Co2
plt.ylabel('States(log scale)')
plt.title('Adsorption')
plt.xlabel('Time')
plt.legend('best')
plt.show
```

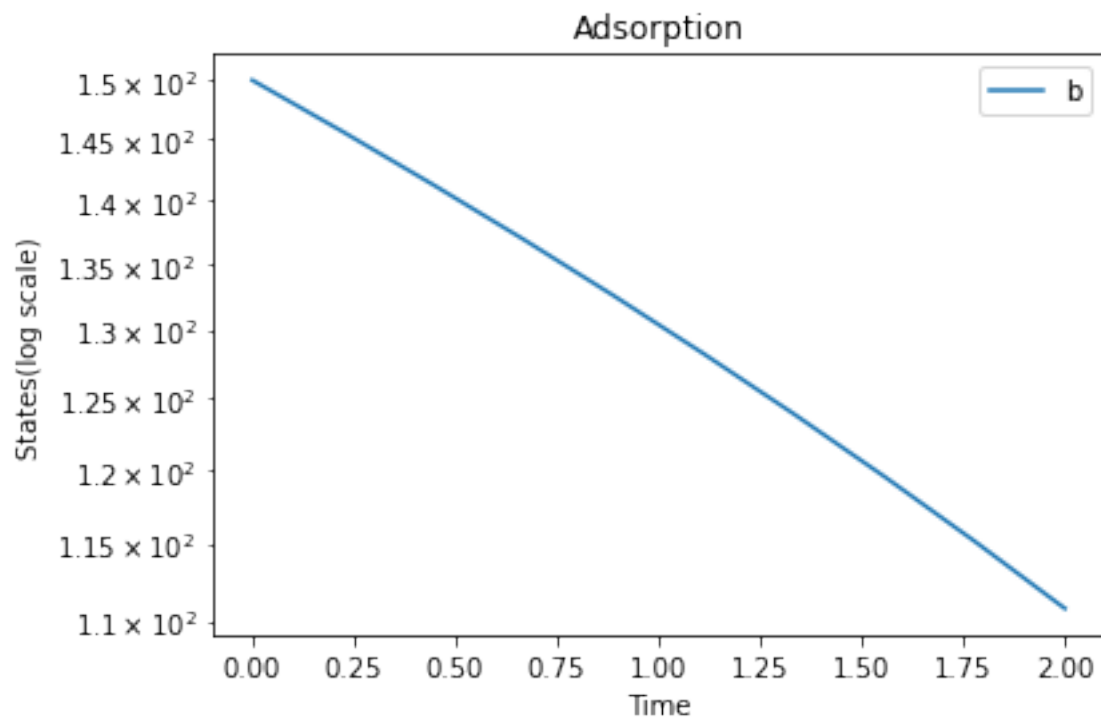
```
Out[89]:
<function matplotlib.pyplot.show(close=None, block=None)>
```



```
In [90]:
plt.semilogy(t,P,label='0H2o')      #--plot for component 0H2o
plt.ylabel('States(log scale)')
plt.title('Adsorption')
plt.xlabel('Time')
plt.legend('best')
plt.show
```

Out[90]:

```
<function matplotlib.pyplot.show(close=None, block=None)>
```



In []: