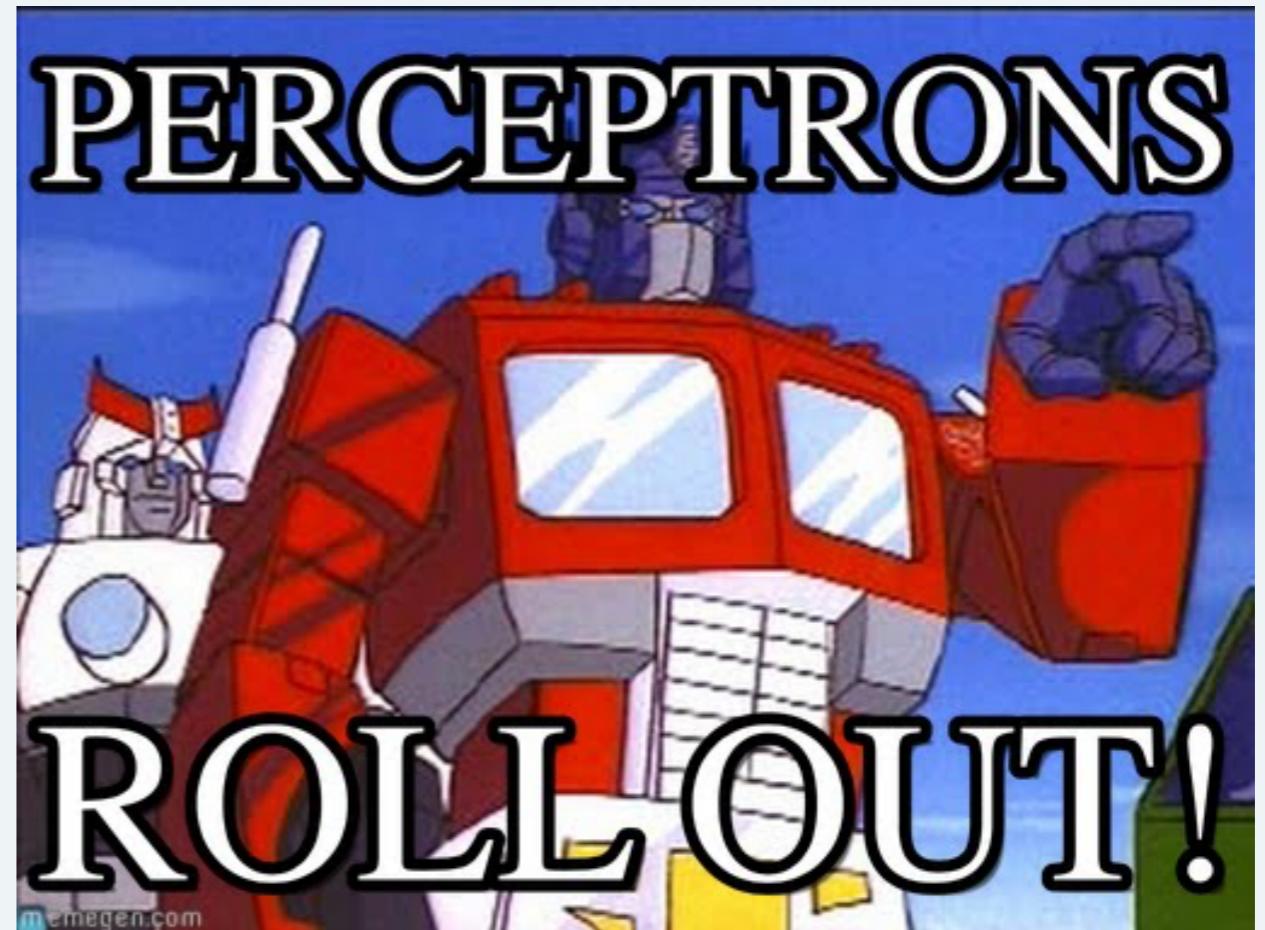


# COGS300

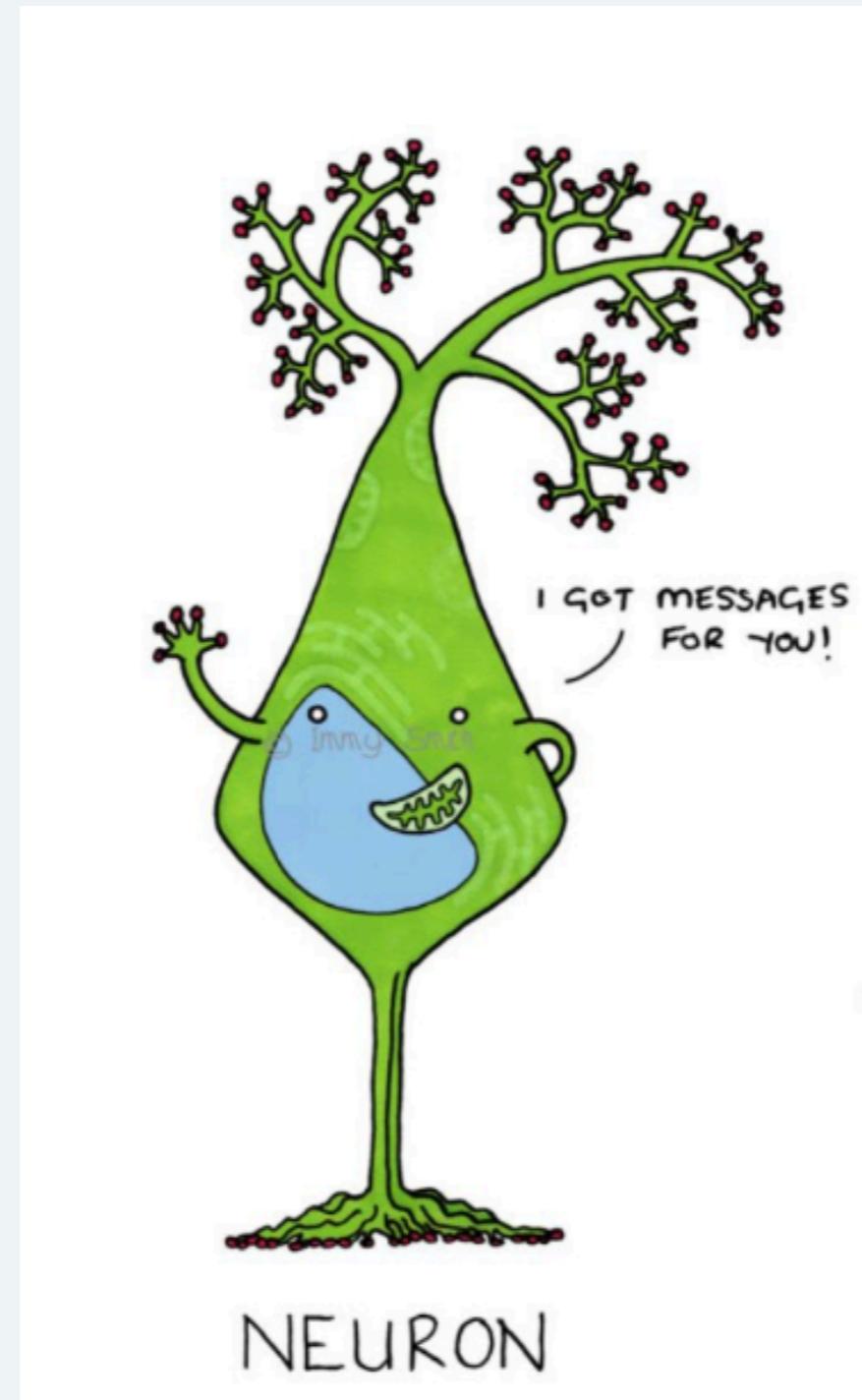
## The perceptron



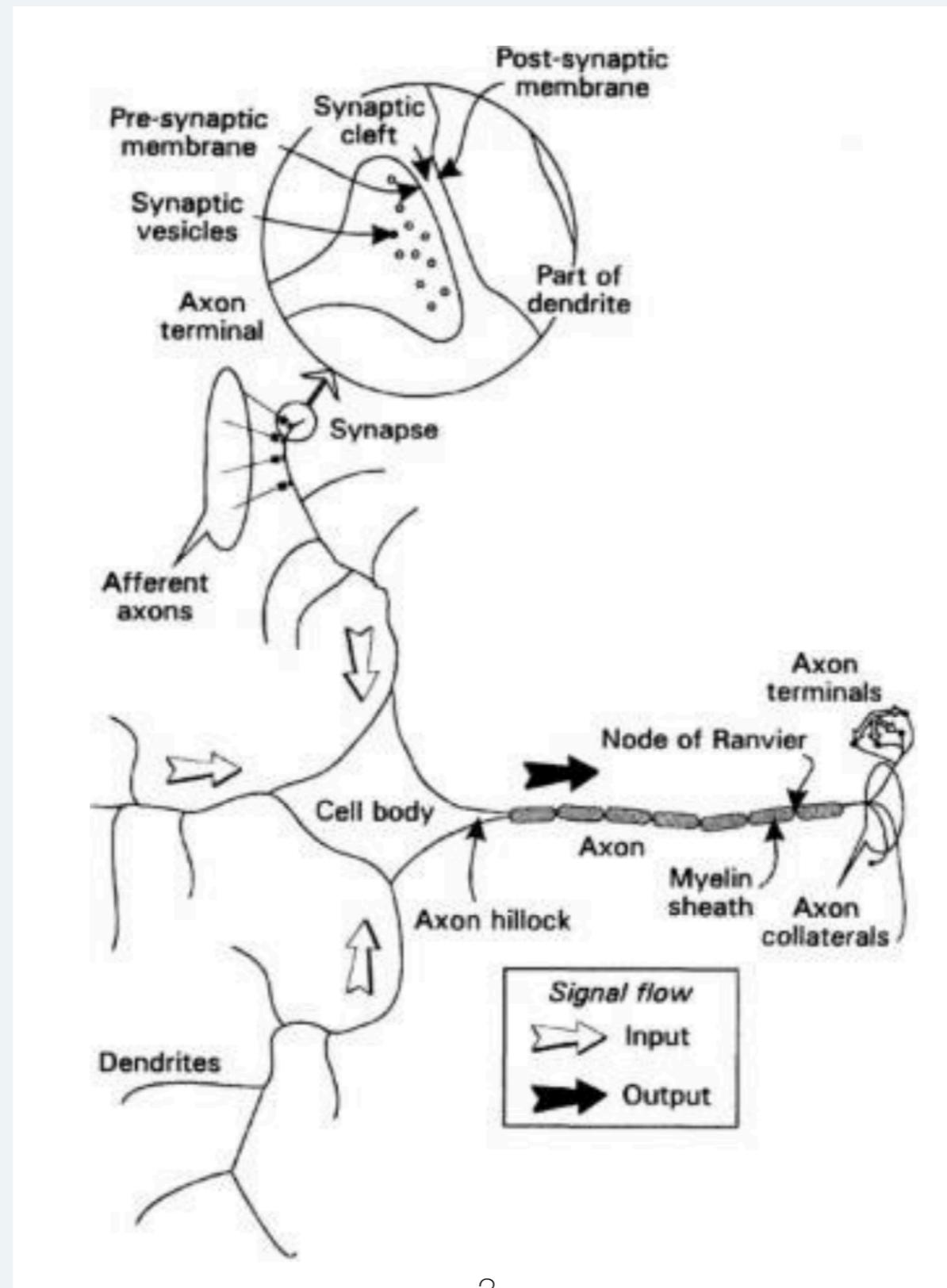
Instructor: Márton Sóskuthy  
[marton.soskuthy@ubc.ca](mailto:marton.soskuthy@ubc.ca)

TAs: Daichi Furukawa • Victoria Lim • Amy  
Wang  
[cogs.300@ubc.ca](mailto:cogs.300@ubc.ca)

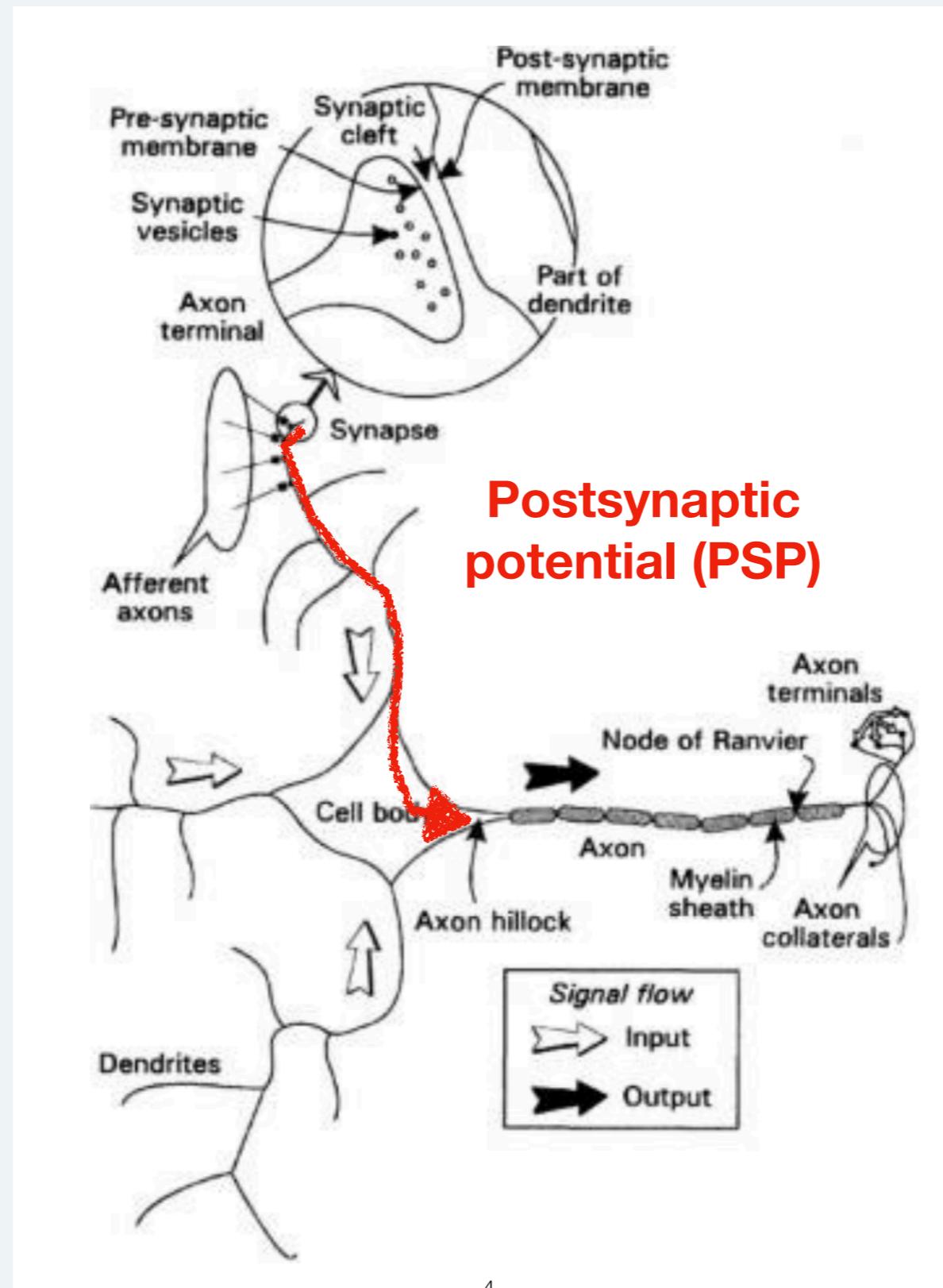
# Your new best friend: the neuron



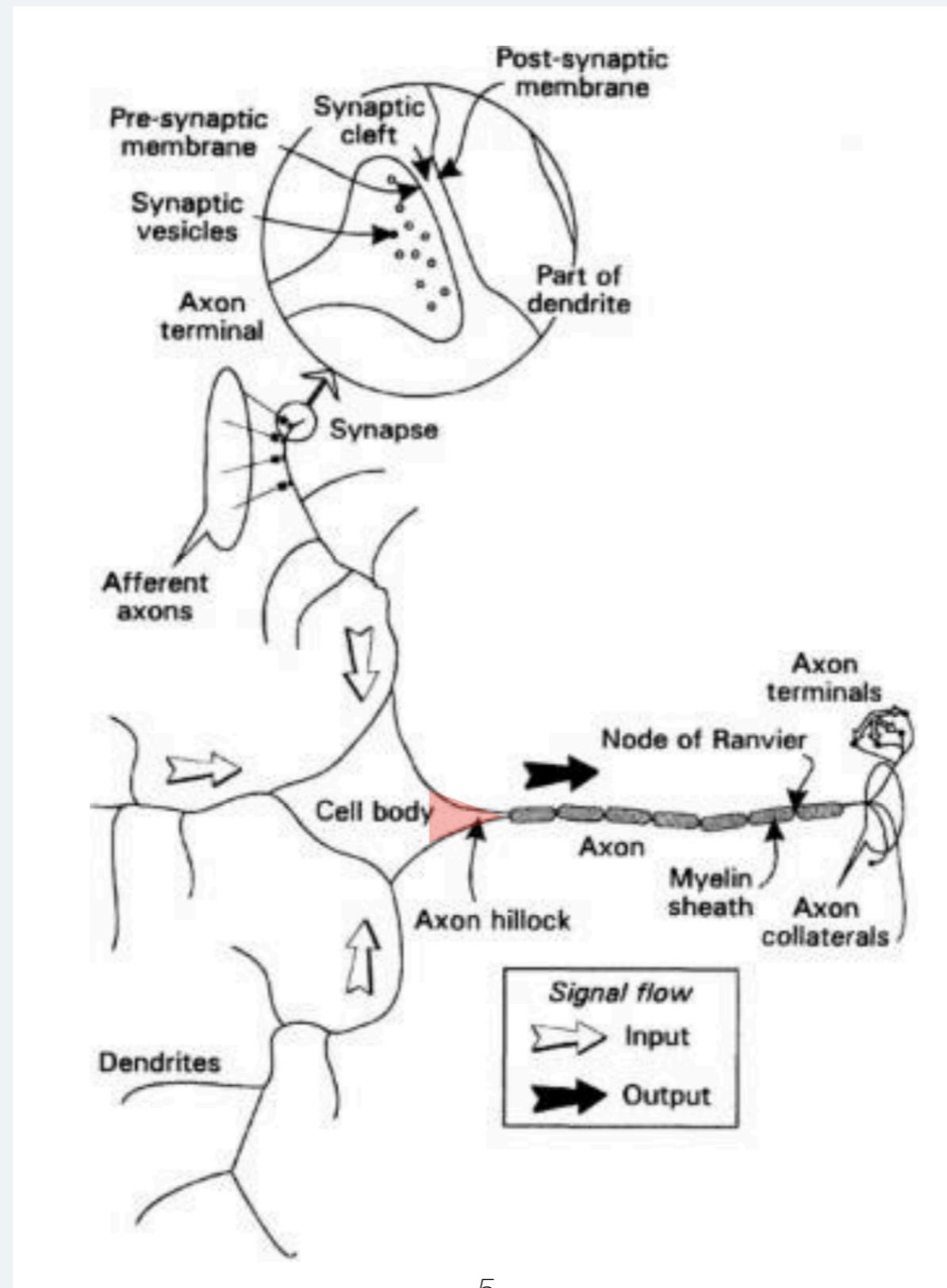
# Your new best friend: the neuron



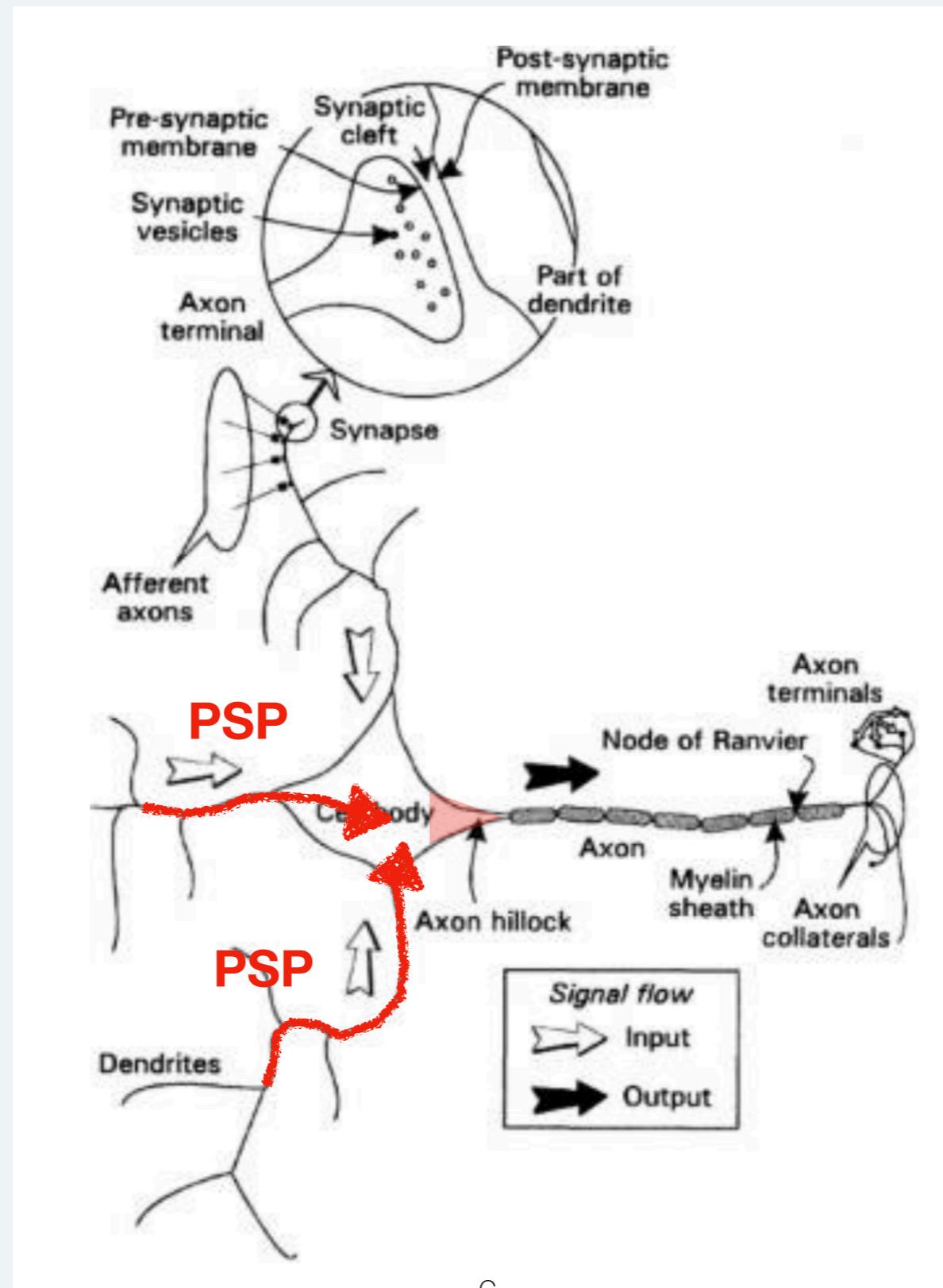
# Your new best friend: the neuron



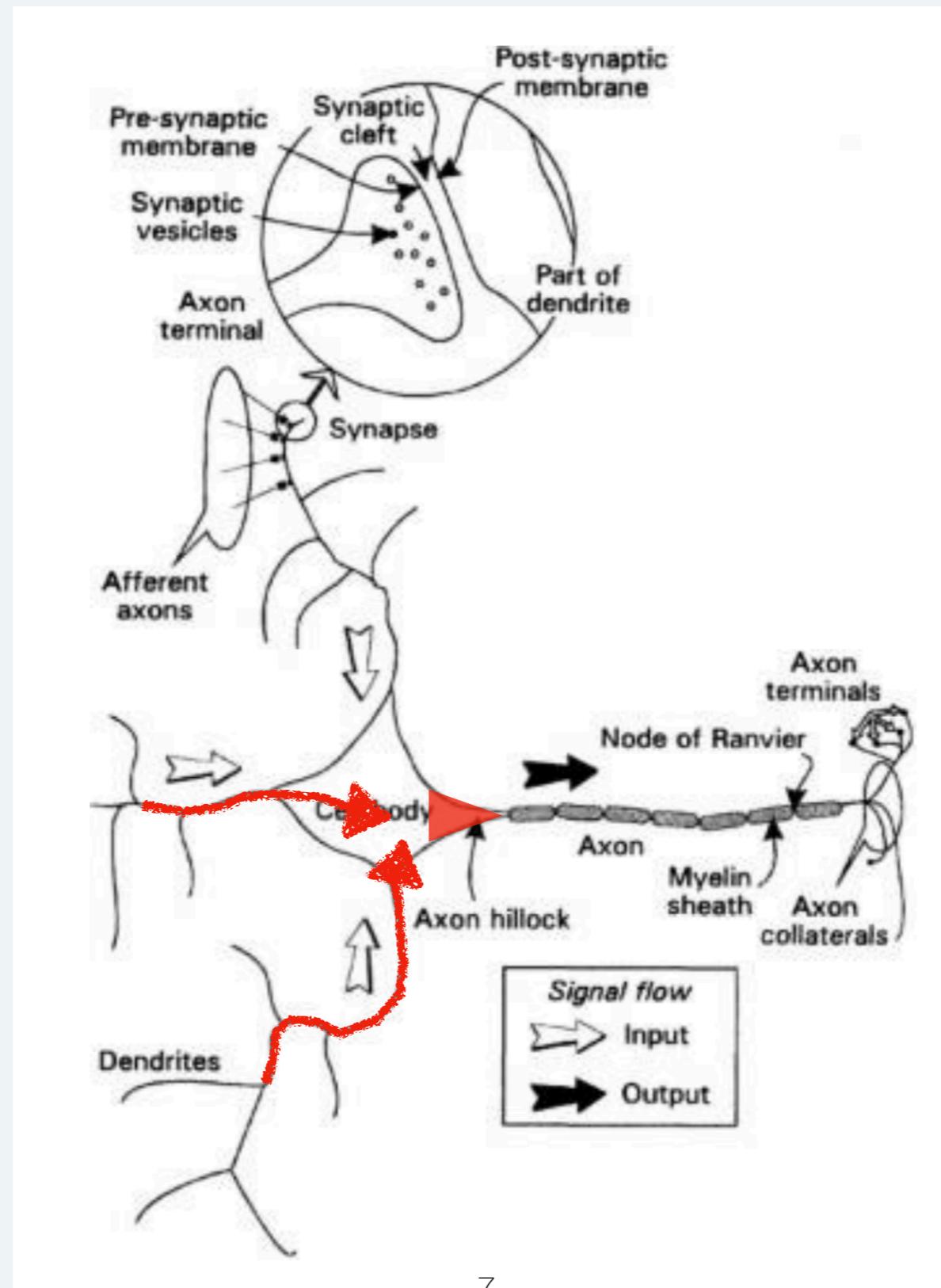
# Your new best friend: the neuron



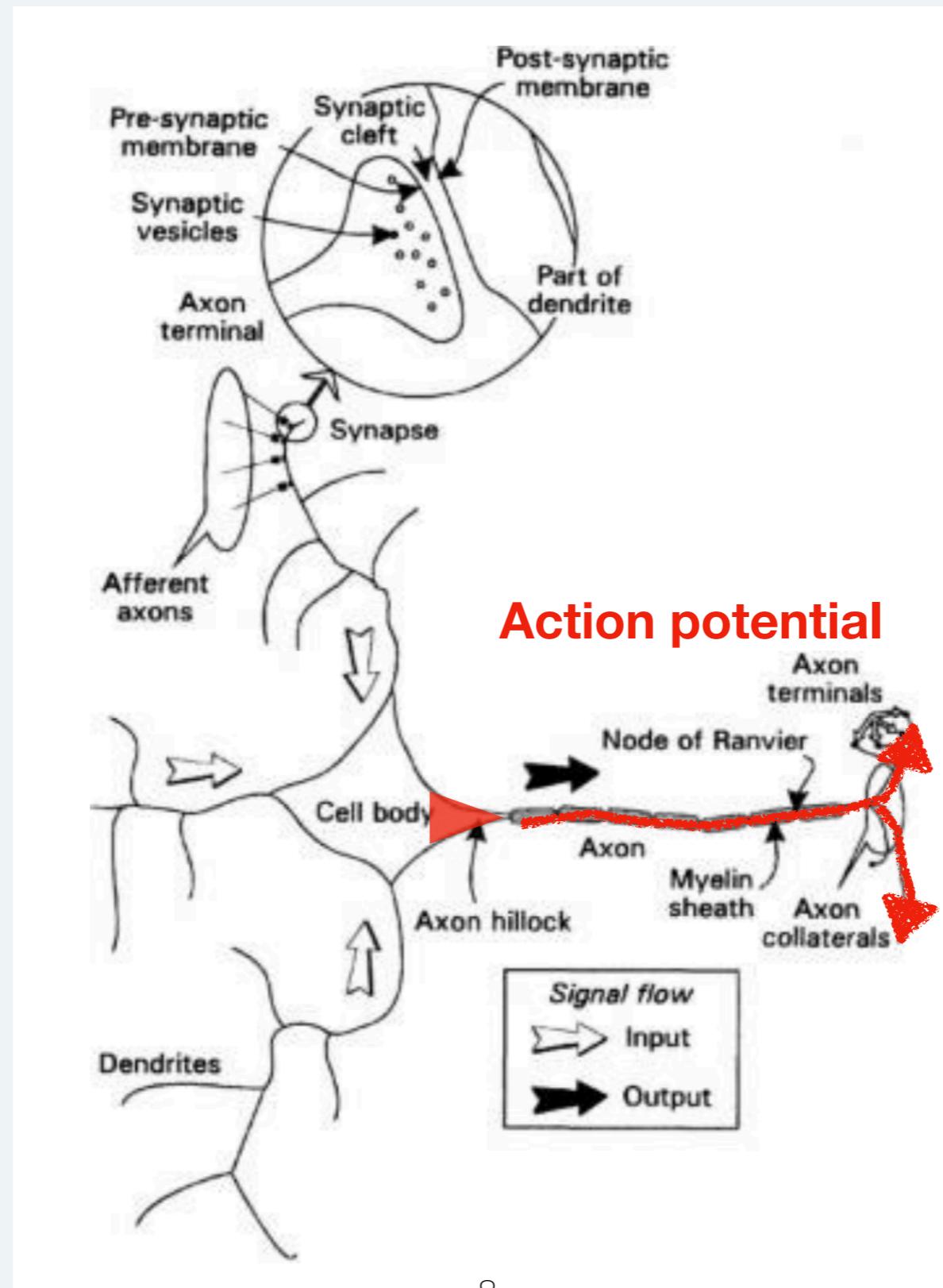
# Your new best friend: the neuron



# Your new best friend: the neuron

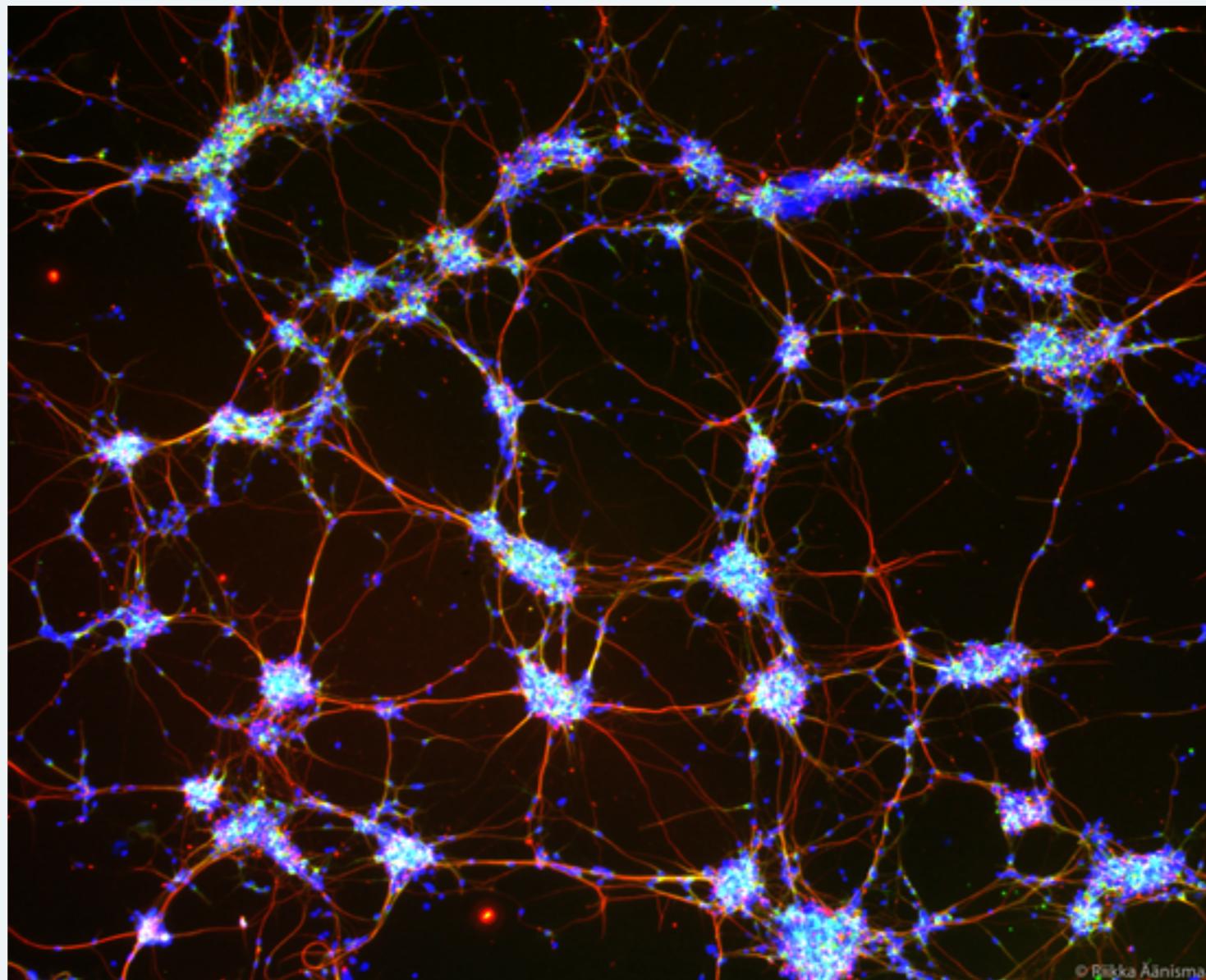


# Your new best friend: the neuron

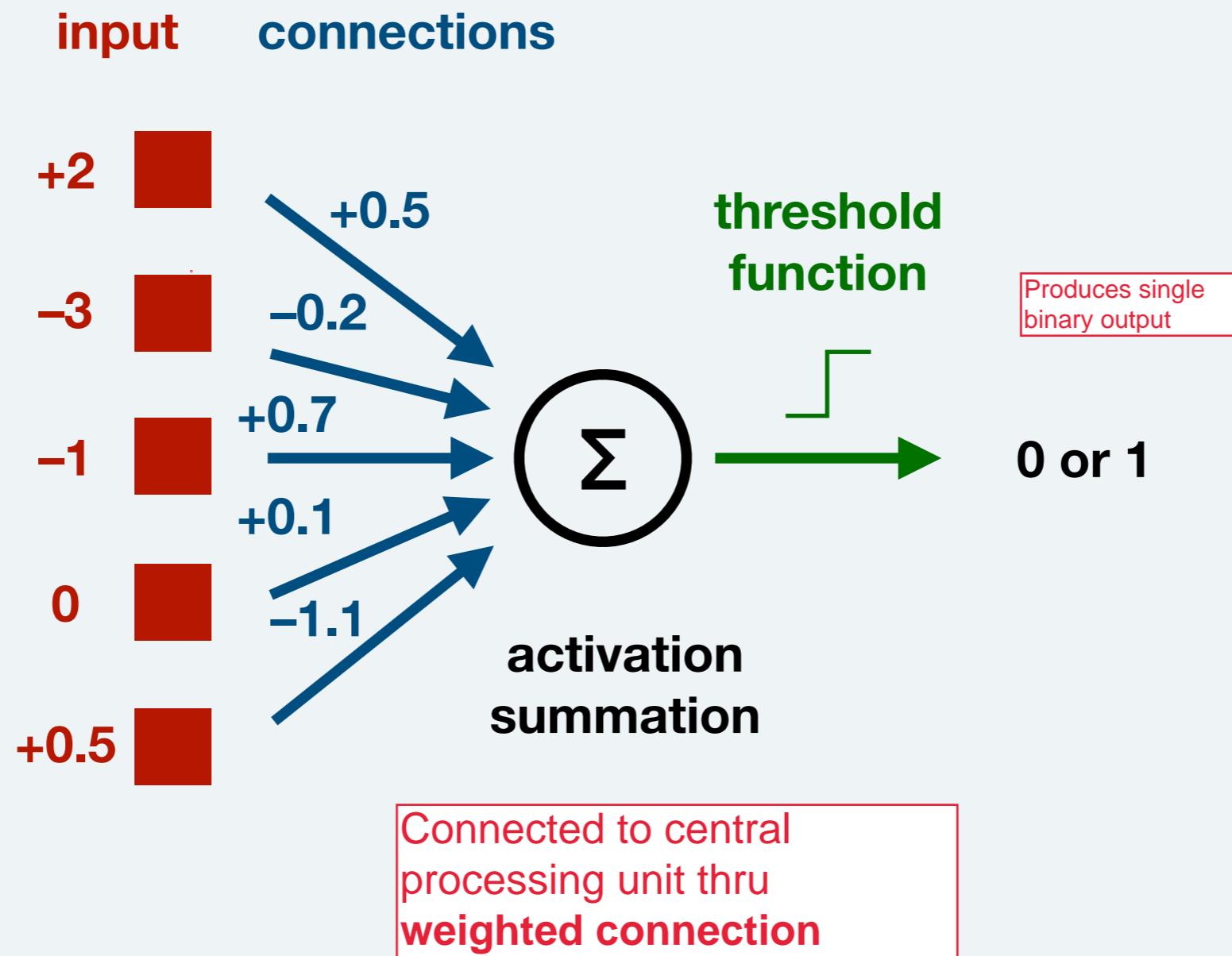


# Your new best friend: the neuron

NNs (bio or  
artificial) = self  
organizing, locally  
organized



# Perceptron: an artificial neuron



# Perceptron: an artificial neuron

input      connections  
(weight)

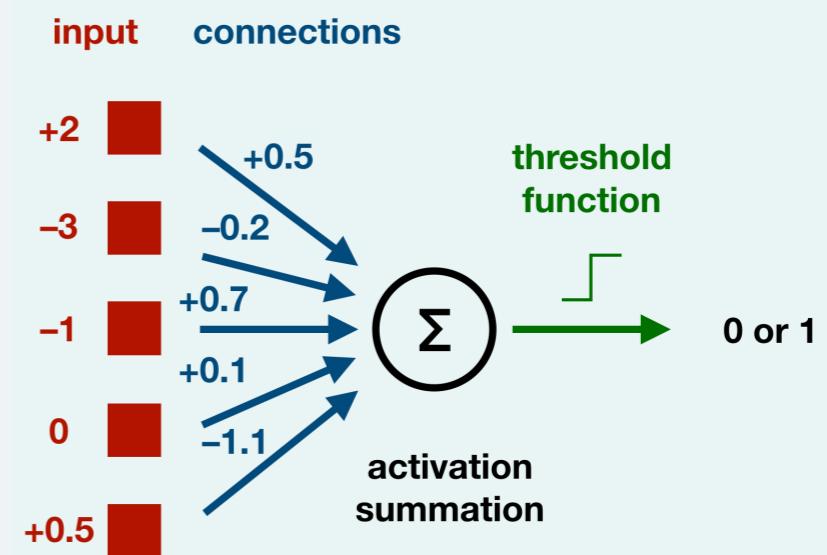
+2    x    +0.5

-3    x    -0.2

-1    x    +0.7

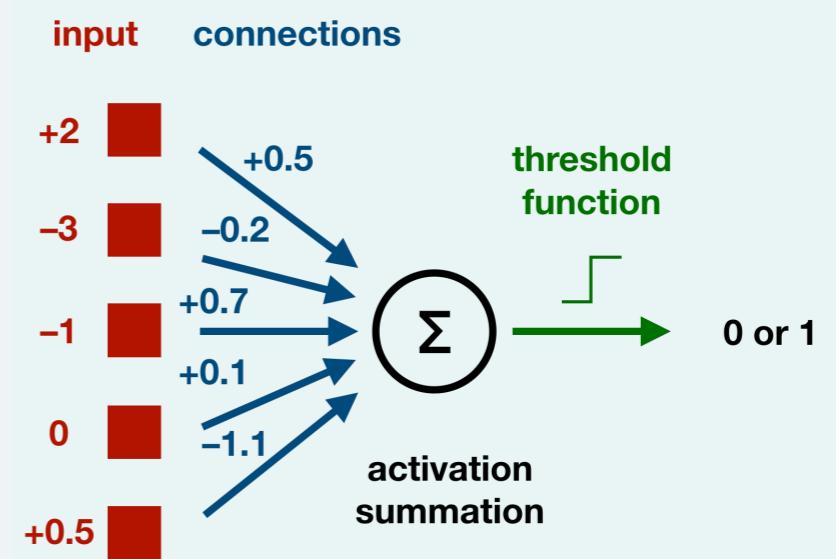
0    x    +0.1

+0.5    x    -1.1



# Perceptron: an artificial neuron

1  
+0.6  
-0.7  
0  
-0.55

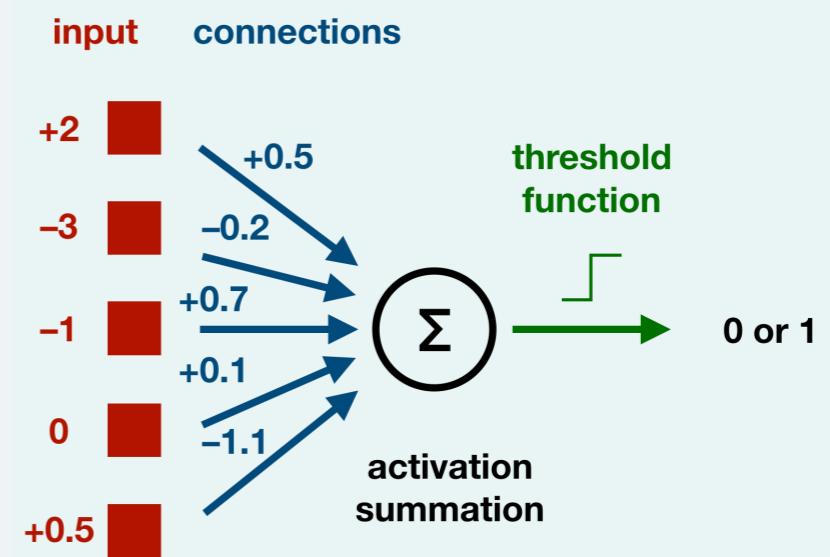


# Perceptron: an artificial neuron

**summation**

(in processing unit)

$$\begin{array}{r} 1 \\ + \\ +0.6 \\ + \\ -0.7 \\ + \\ 0 \\ + \\ -0.55 \end{array}$$



# Perceptron: an artificial neuron

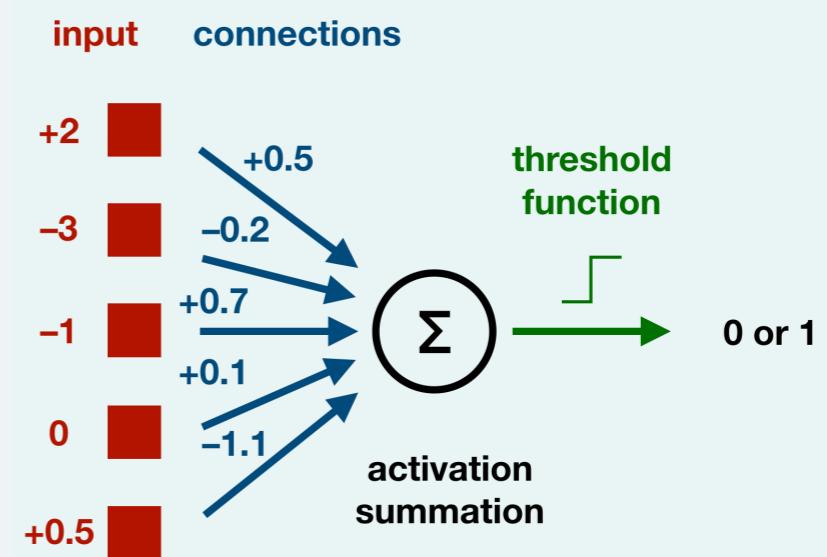
threshold  
function

theta = threshold

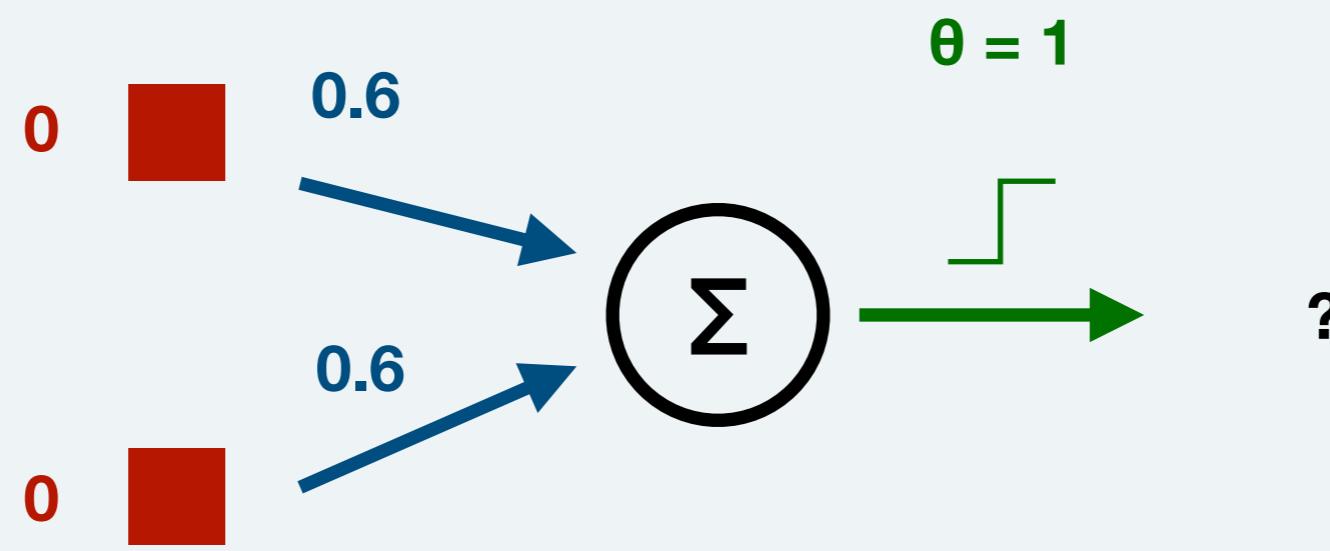
e.g.  $\theta = 2$

$$\left. \begin{array}{ll} 1 & \text{if } x > \theta \\ 0 & \end{array} \right\} \quad 0$$

0.35      0 if  $x \leq \theta$

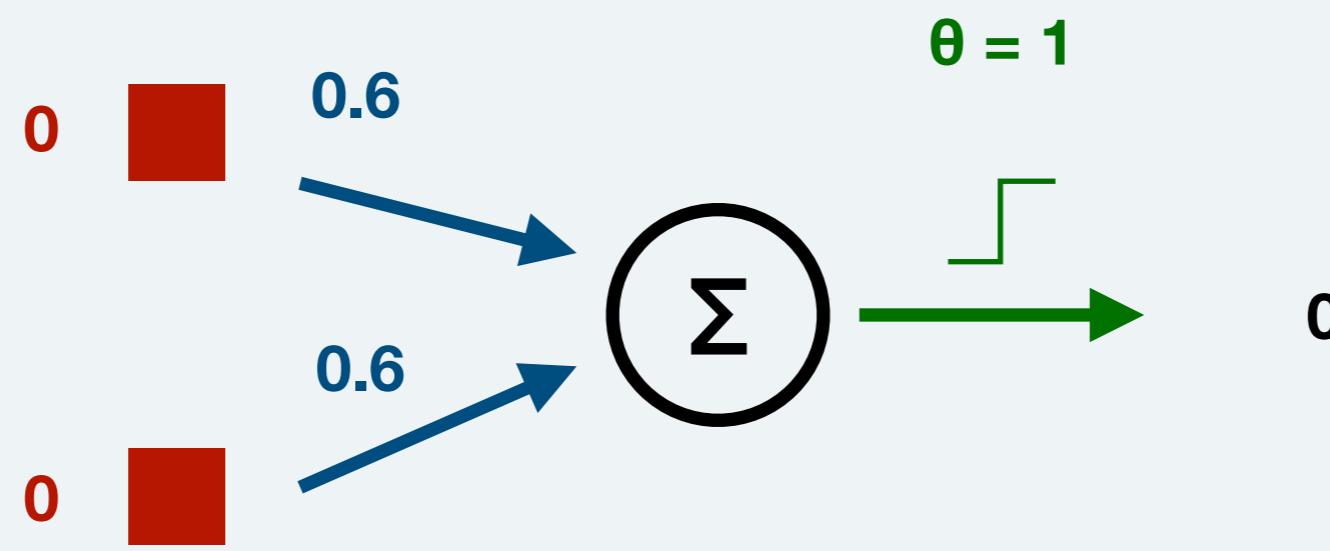


# Perceptron: an artificial neuron

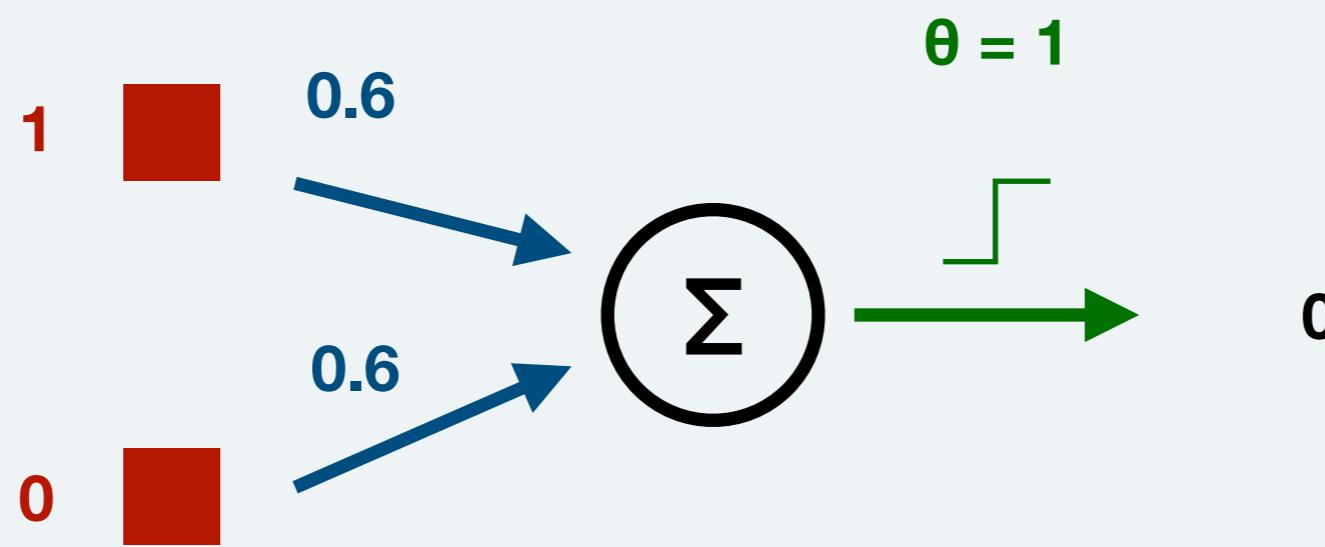


Produces 0:  $0*.6+0*.6 = 0 < 1$

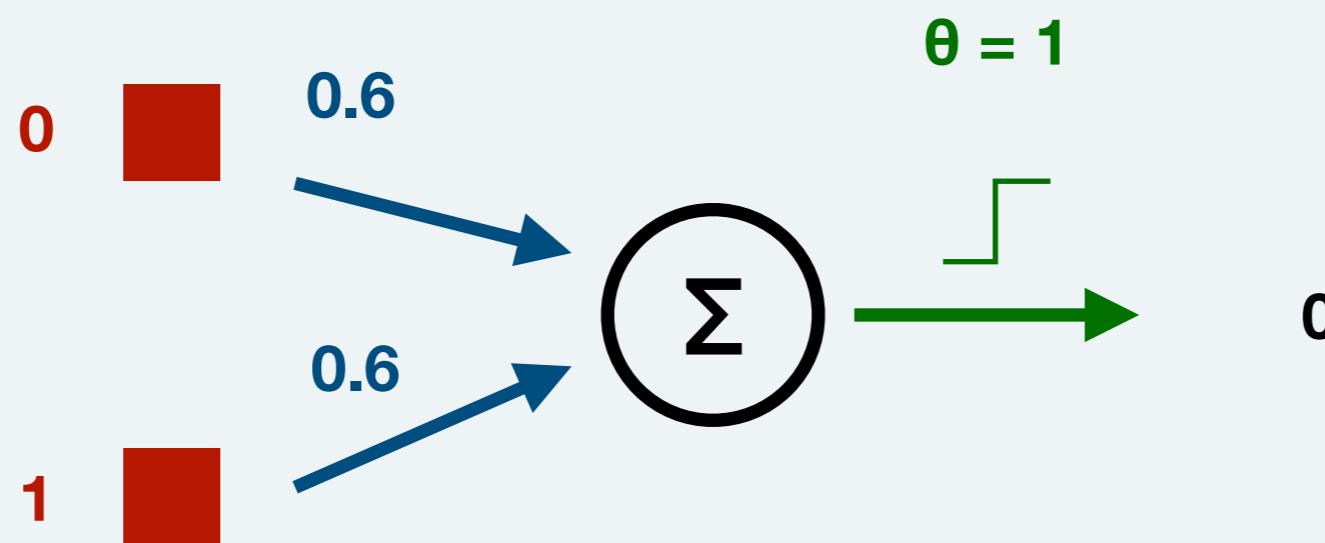
# Perceptron: an artificial neuron



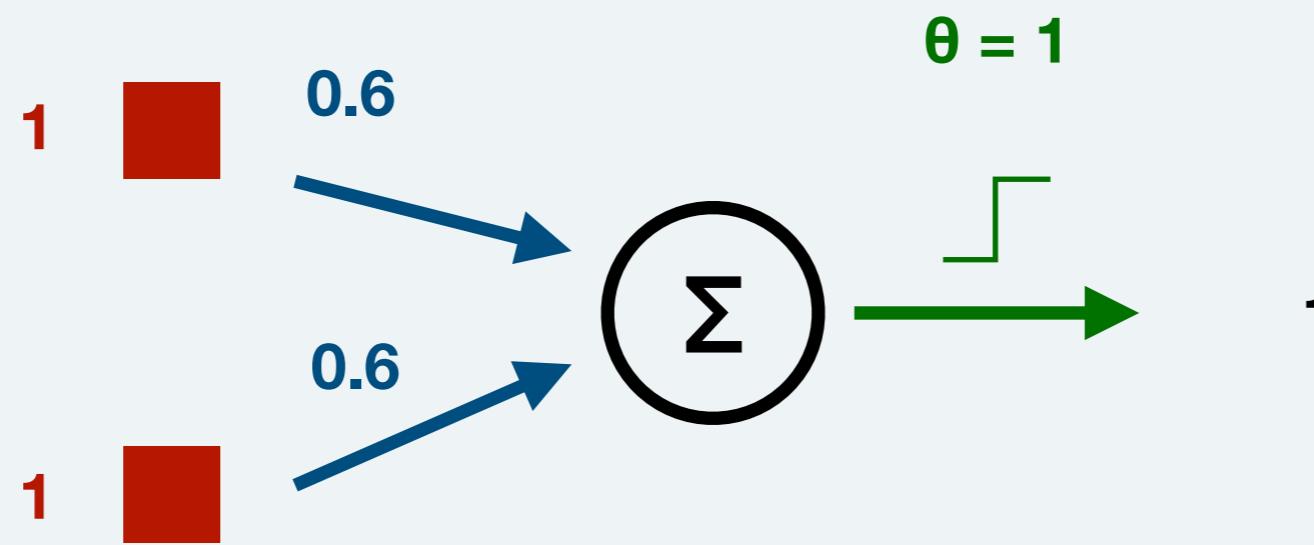
# Perceptron: an artificial neuron



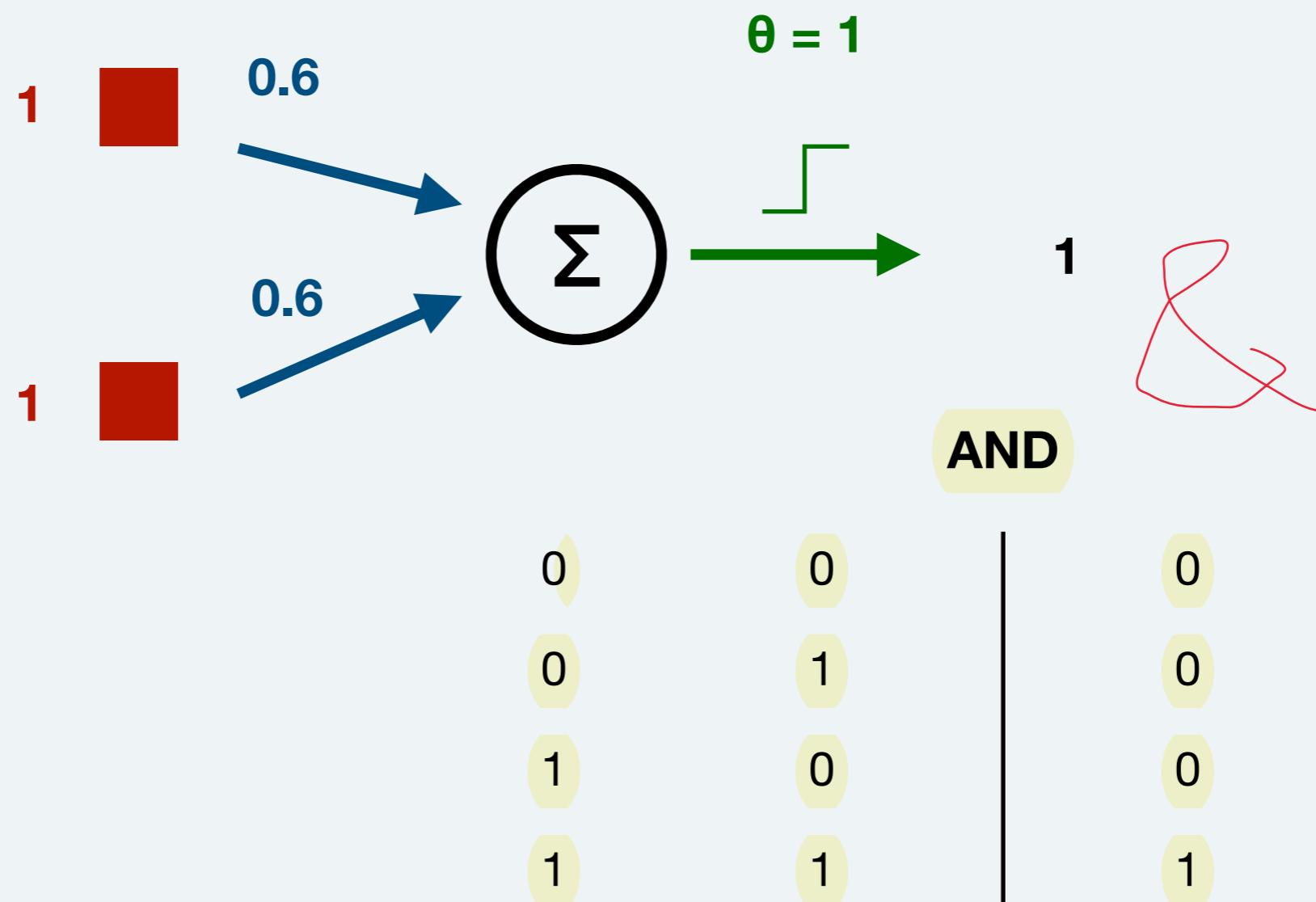
# Perceptron: an artificial neuron



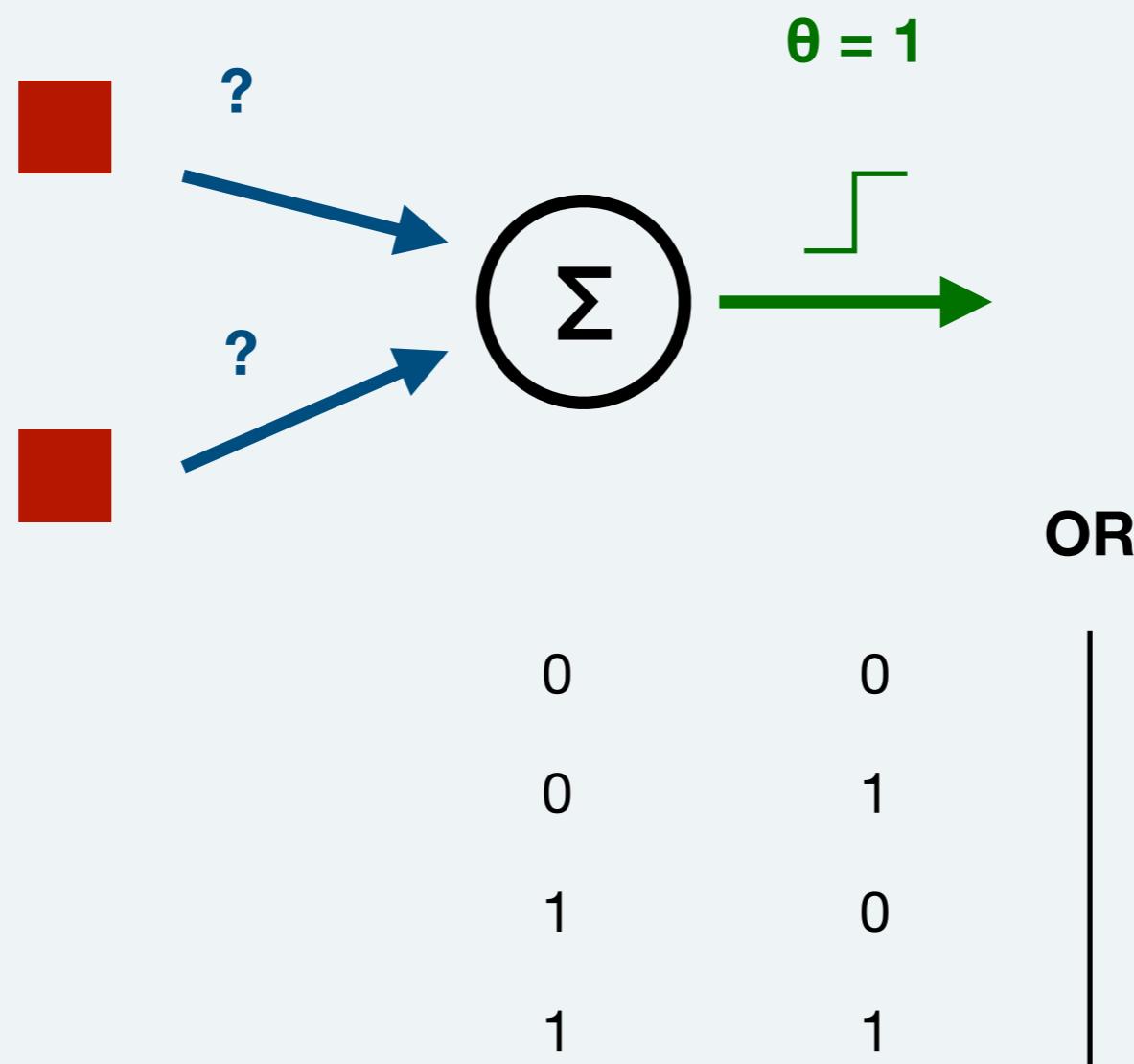
# Perceptron: an artificial neuron



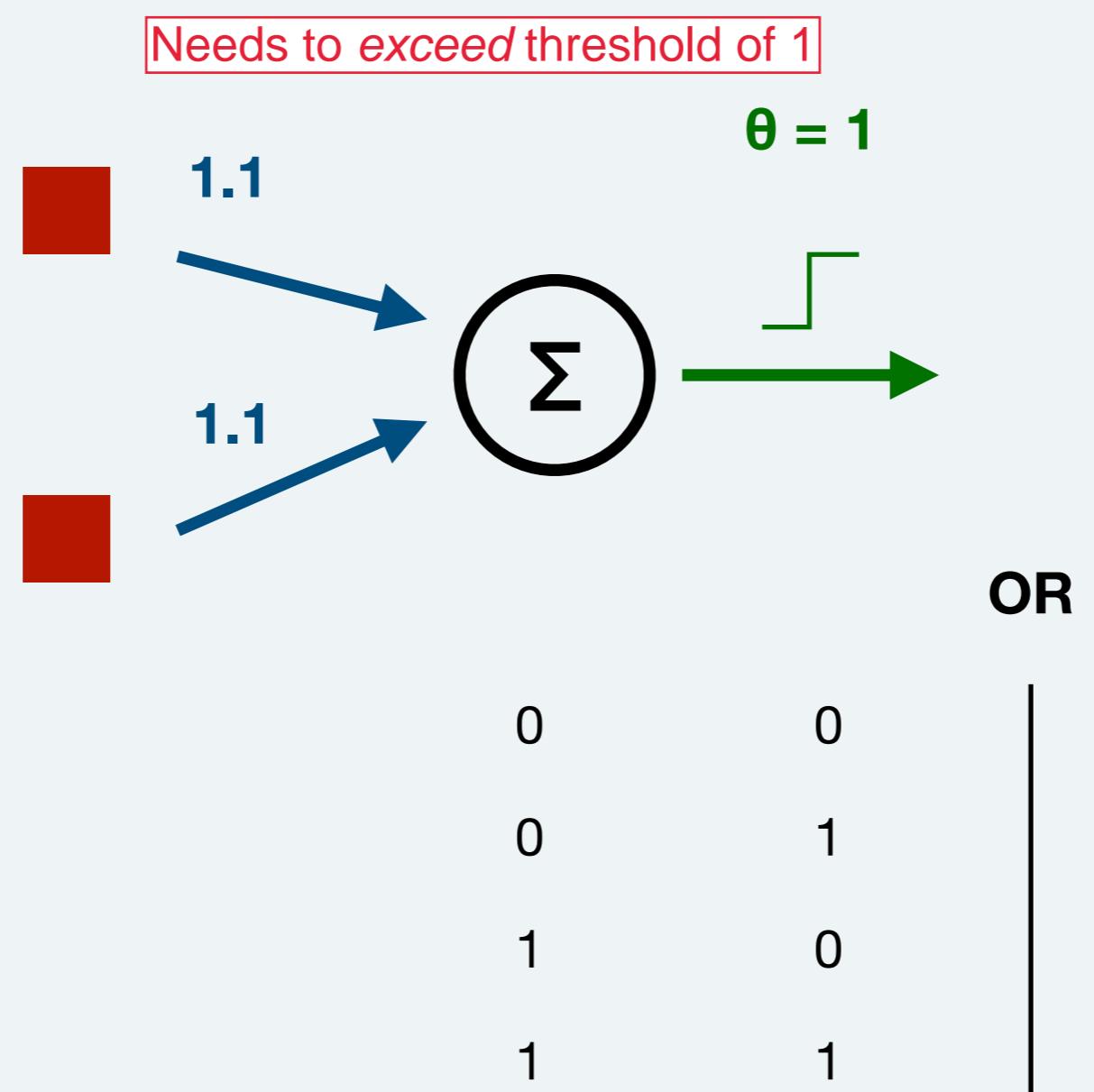
# Perceptron: an artificial neuron



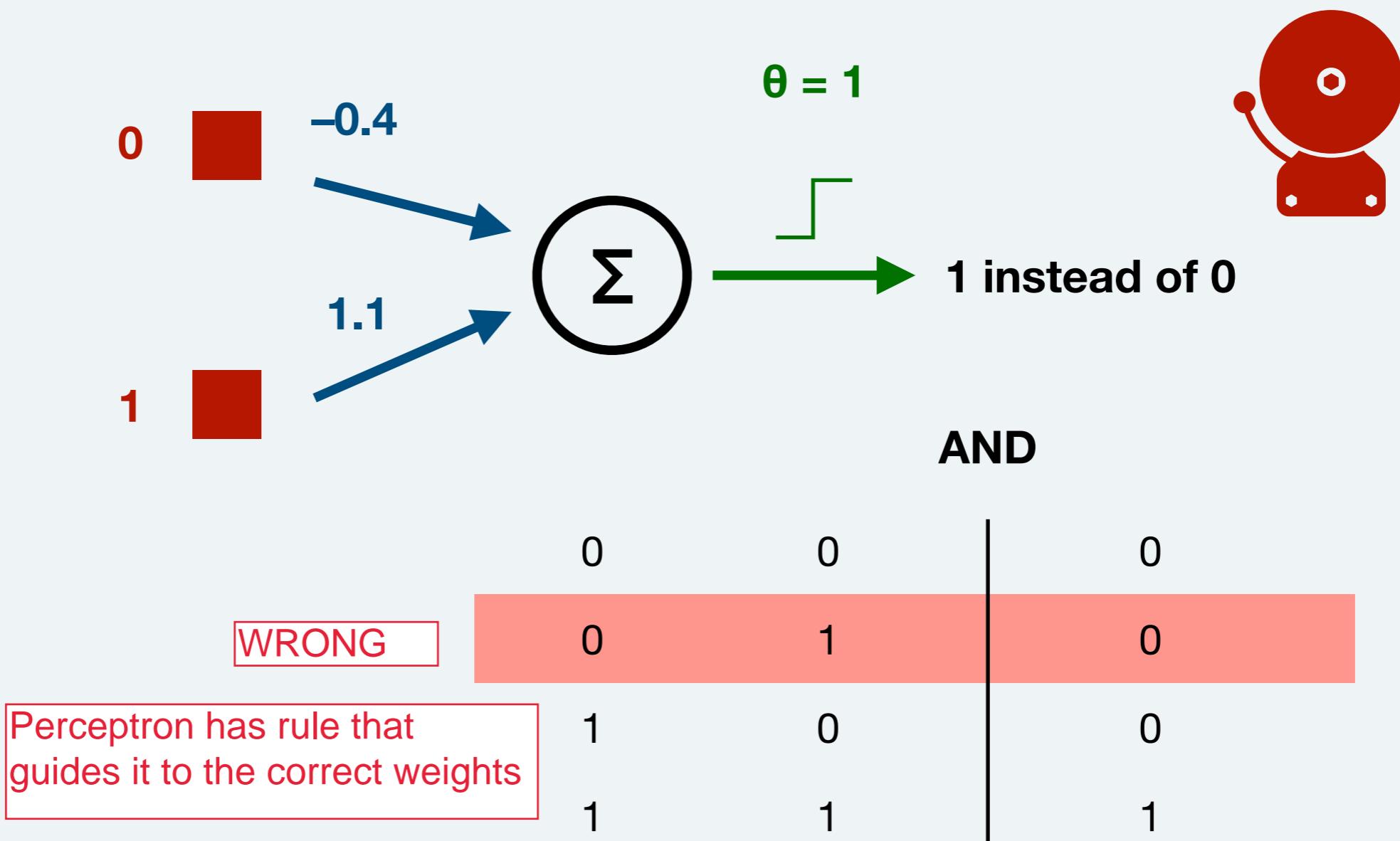
# Perceptron: an artificial neuron



# Perceptron: an artificial neuron



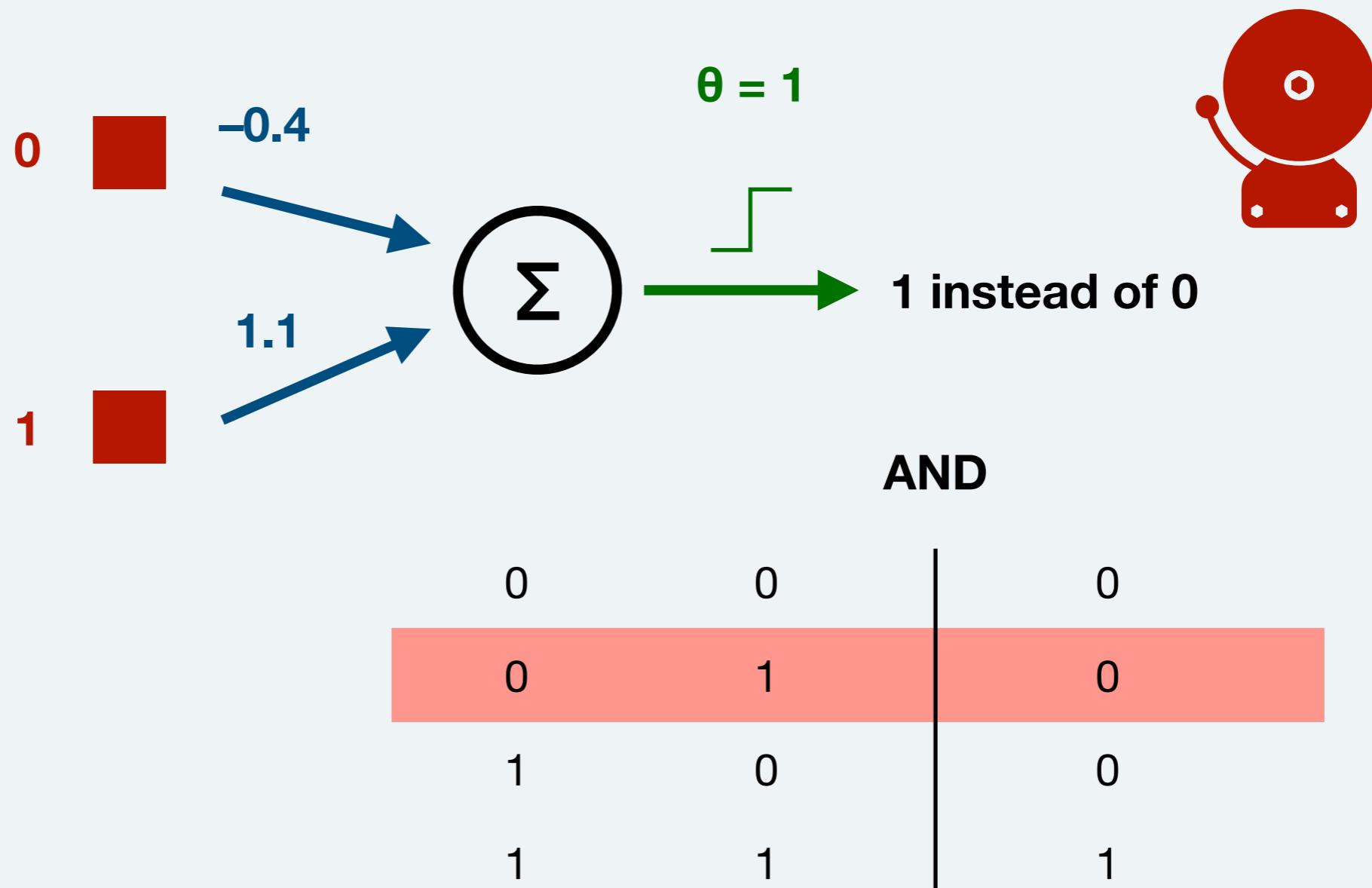
# The perceptron learning rule



# The perceptron learning rule

modify weights by:

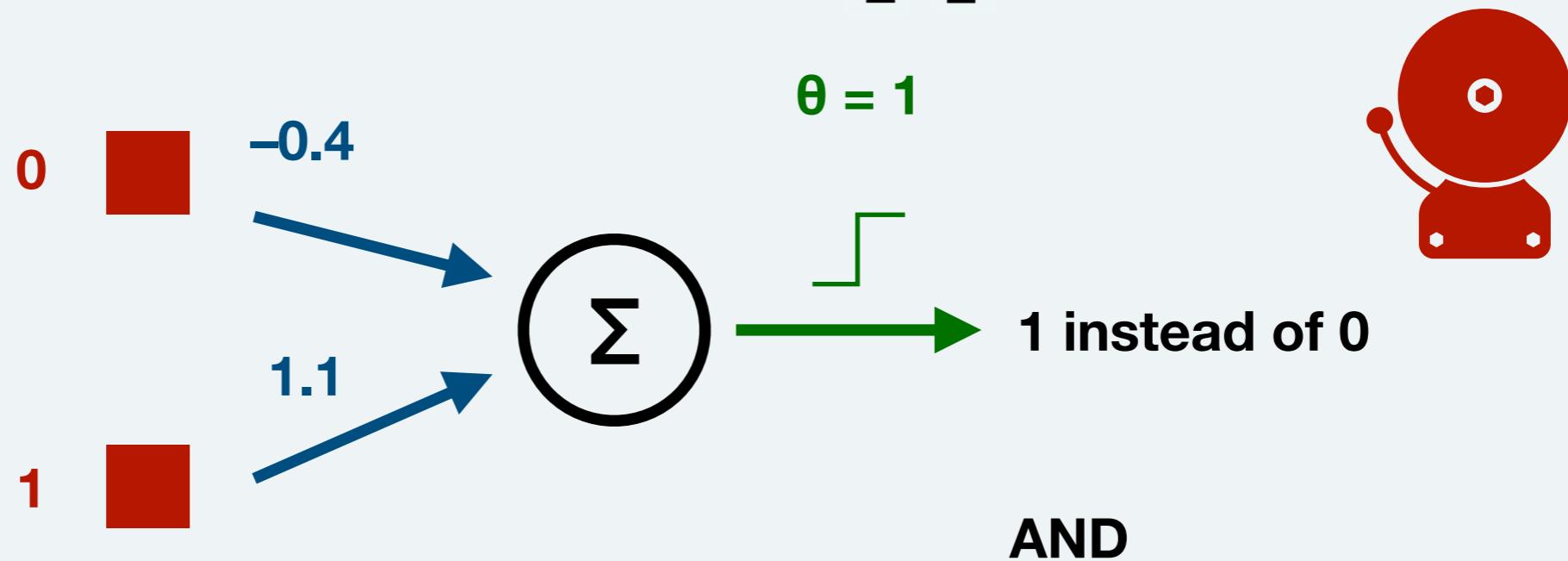
`small_number × (target_output – actual_output) × input_vector`



# The perceptron learning rule

modify weights by:

$$0.1 \times (0 - 1) \times \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

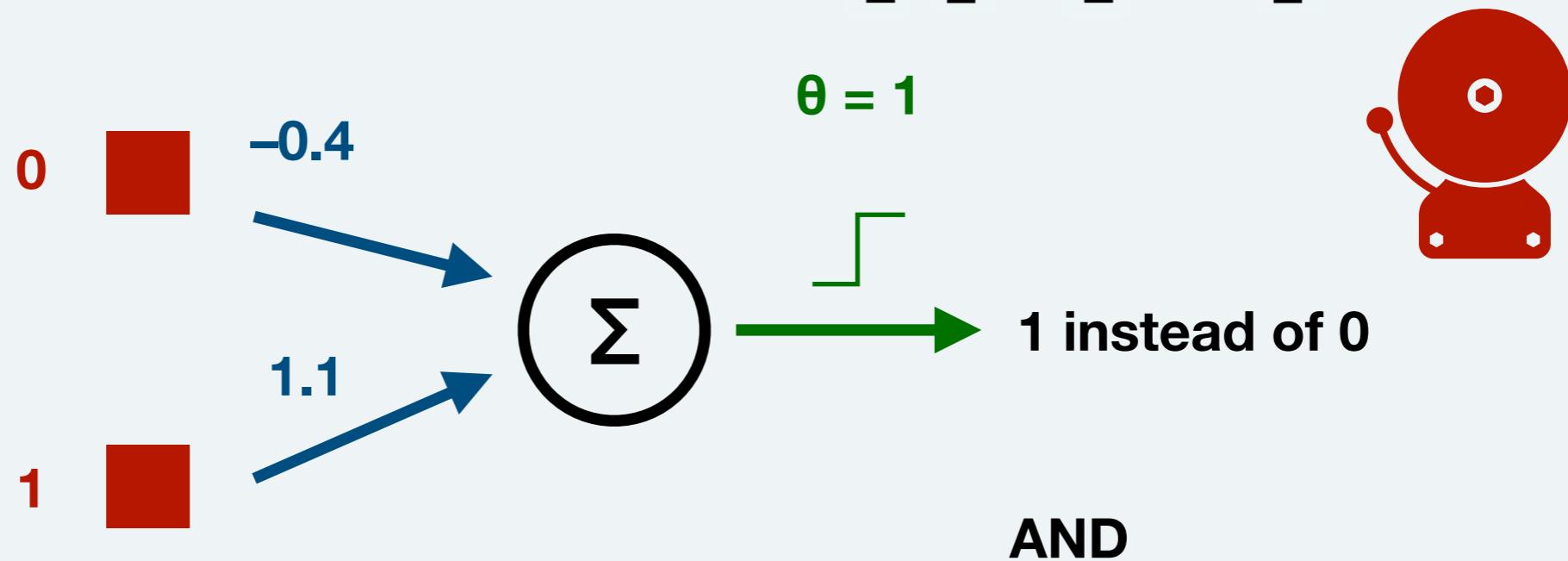


|   |   |   |
|---|---|---|
| 0 | 0 | 0 |
| 0 | 1 | 0 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

# The perceptron learning rule

modify weights by:

$$0.1 \times (0 - 1) \times \begin{bmatrix} 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 0 \\ -0.1 \end{bmatrix}$$

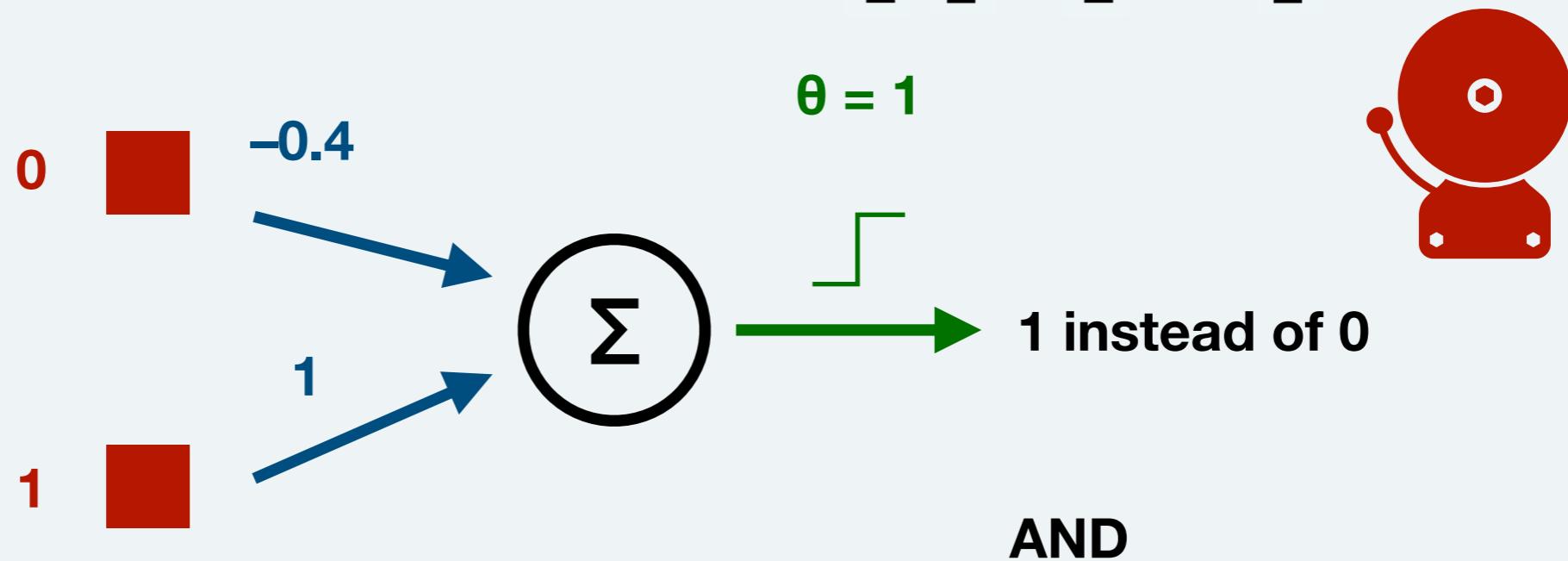


|   |   |   |
|---|---|---|
| 0 | 0 | 0 |
| 0 | 1 | 0 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

# The perceptron learning rule

modify weights by:

$$0.1 \times (0 - 1) \times \begin{bmatrix} 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 0 \\ -0.1 \end{bmatrix}$$

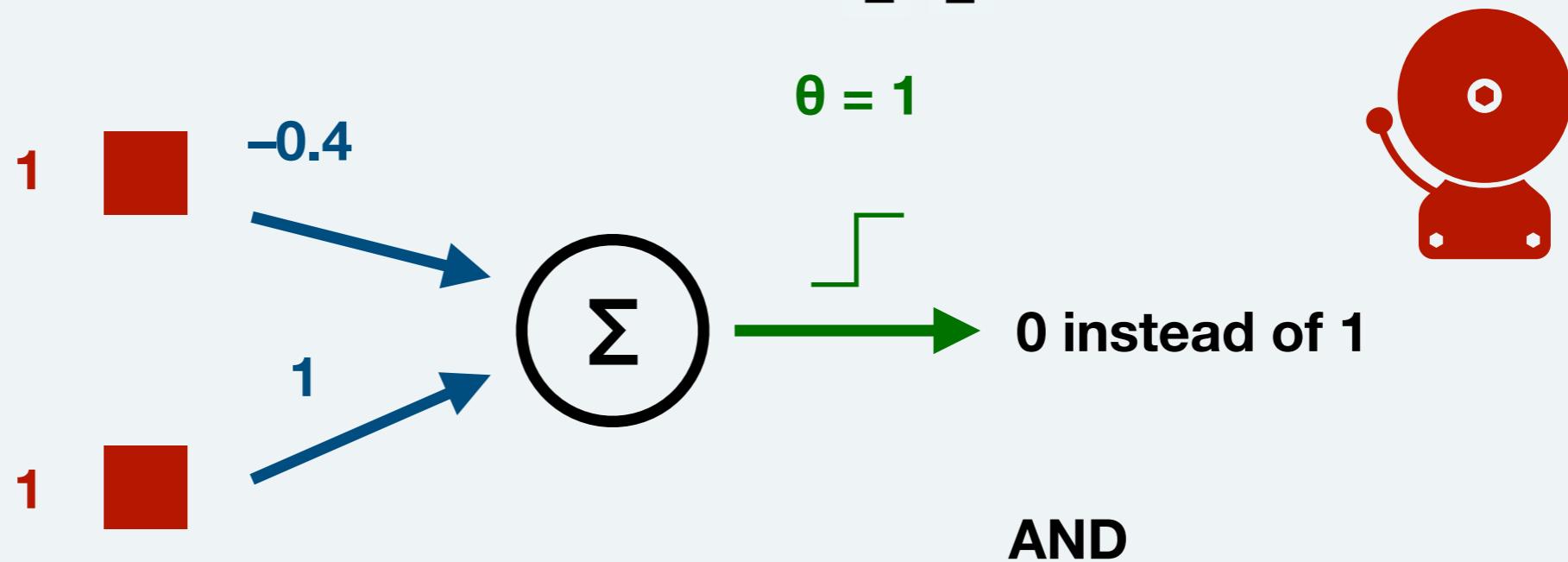


|   |   |   |
|---|---|---|
| 0 | 0 | 0 |
| 0 | 1 | 0 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

# The perceptron learning rule

modify weights by:

$$0.1 \times (1 - 0) \times \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

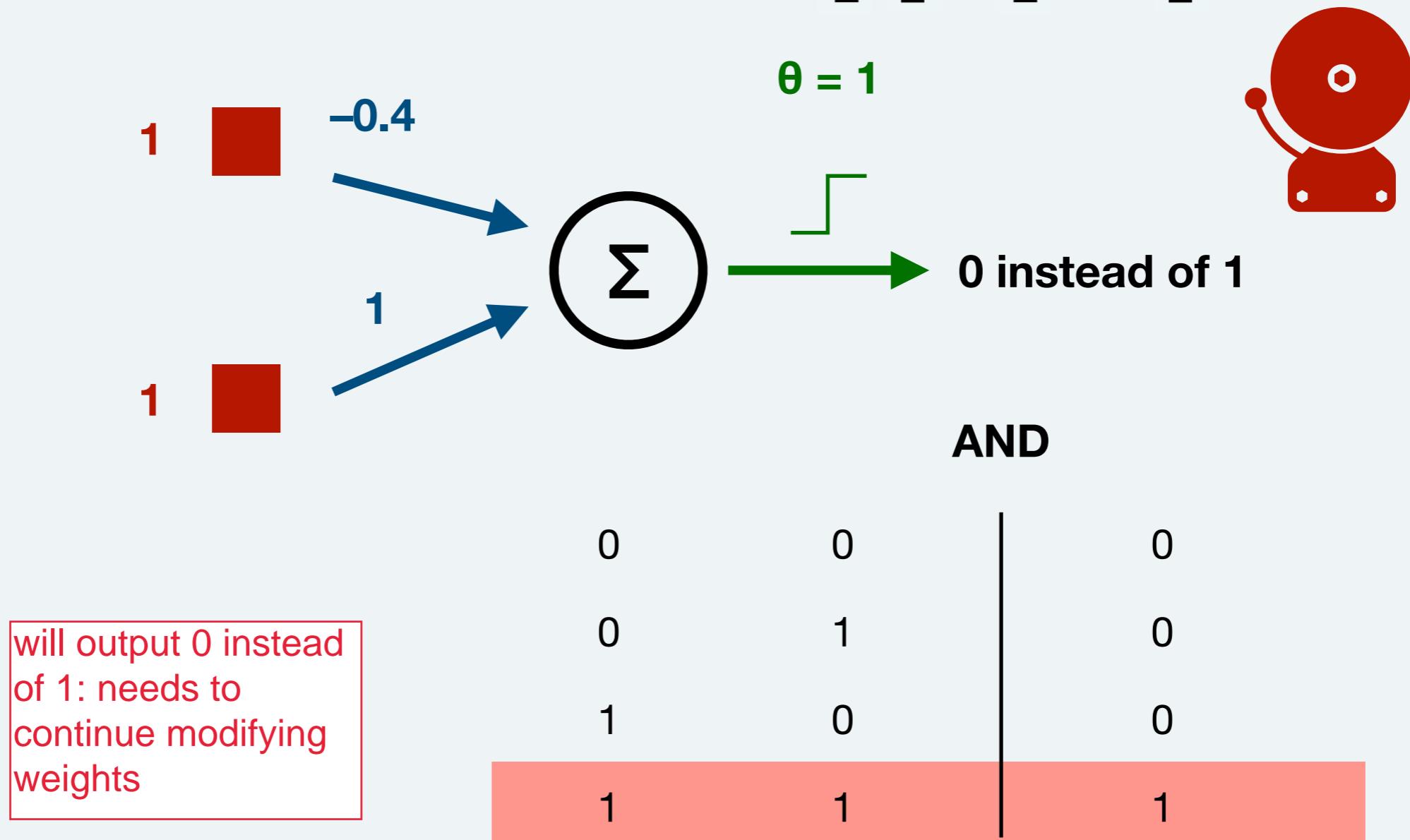


|   |   |   |
|---|---|---|
| 0 | 0 | 0 |
| 0 | 1 | 0 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

# The perceptron learning rule

modify weights by:

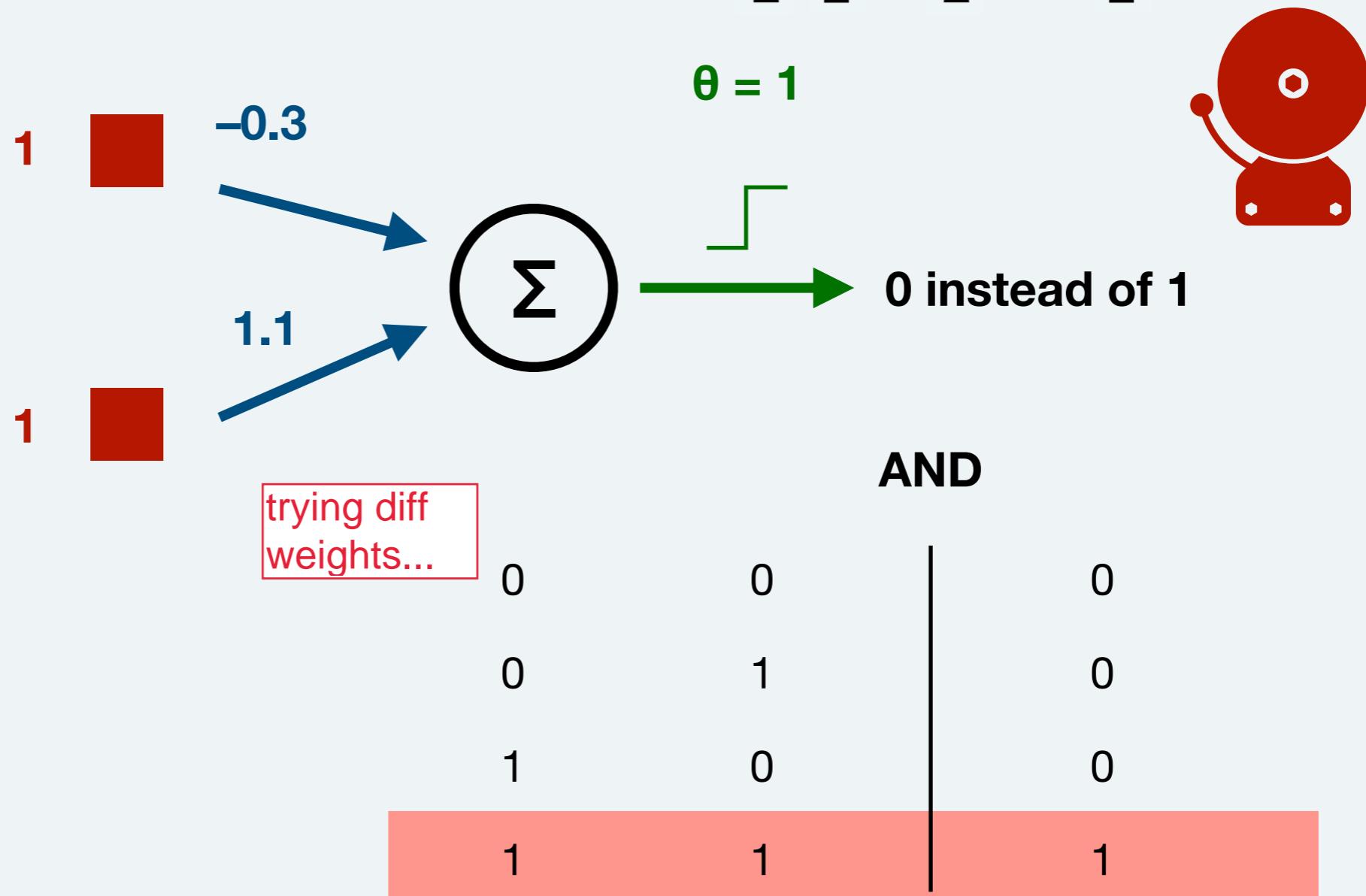
$$0.1 \times (1 - 0) \times \begin{bmatrix} 1 \\ 1 \end{bmatrix} = \begin{bmatrix} 0.1 \\ 0.1 \end{bmatrix}$$



# The perceptron learning rule

modify weights by:

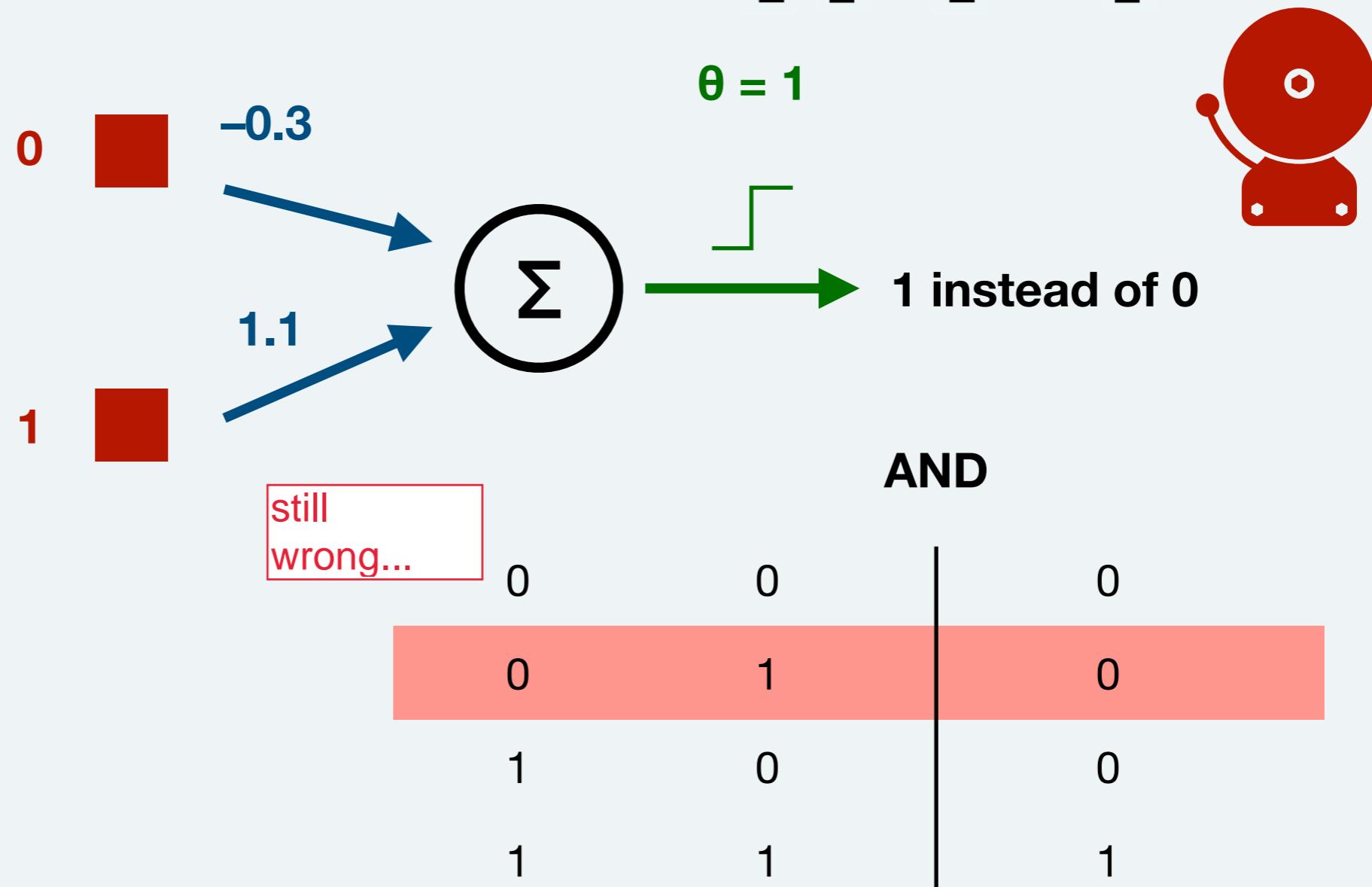
$$0.1 \times (1 - 0) \times \begin{bmatrix} 1 \\ 1 \end{bmatrix} = \begin{bmatrix} 0.1 \\ 0.1 \end{bmatrix}$$



# The perceptron learning rule

modify weights by:

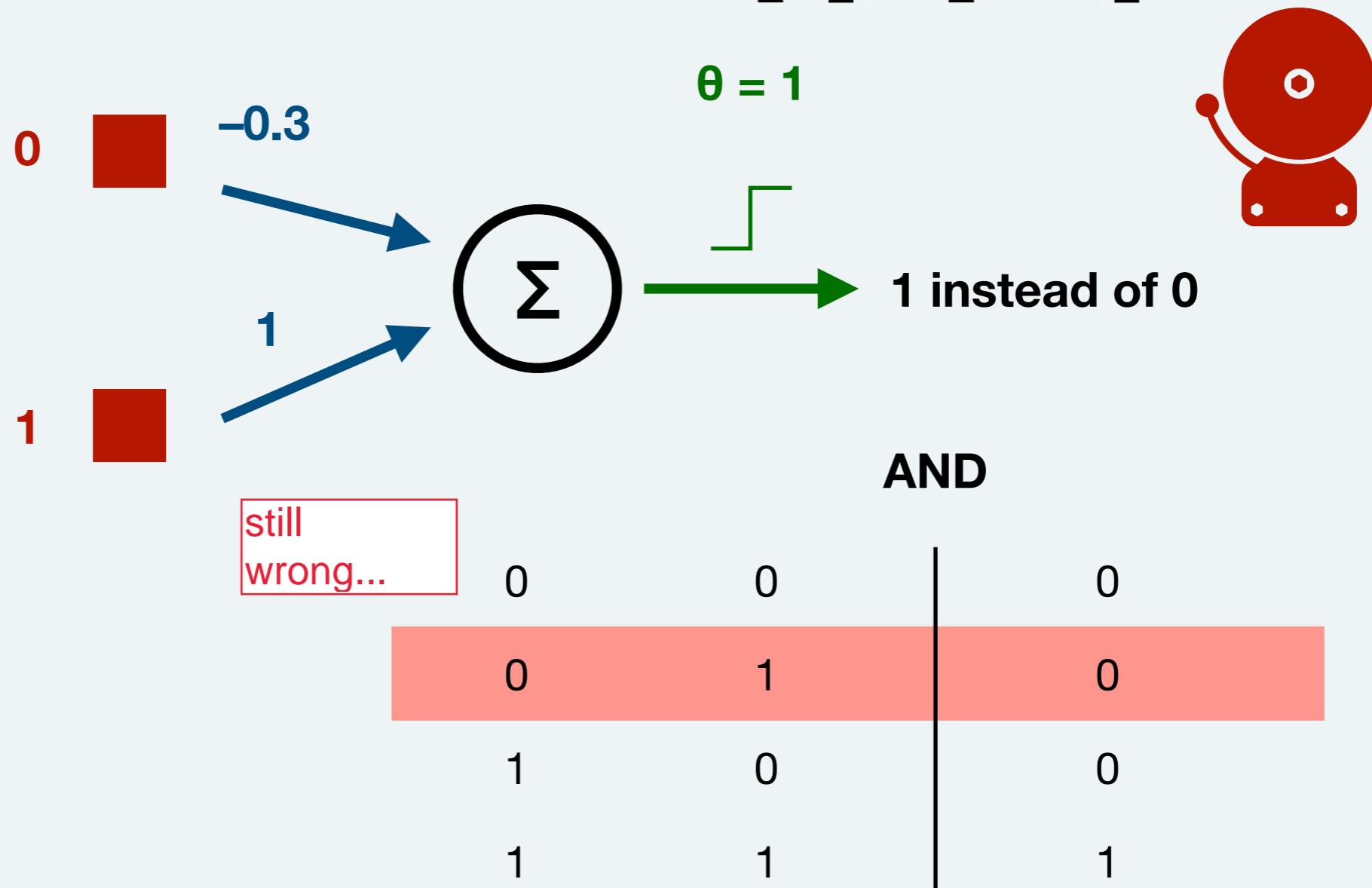
$$0.1 \times (0 - 1) \times \begin{bmatrix} 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 0 \\ -0.1 \end{bmatrix}$$



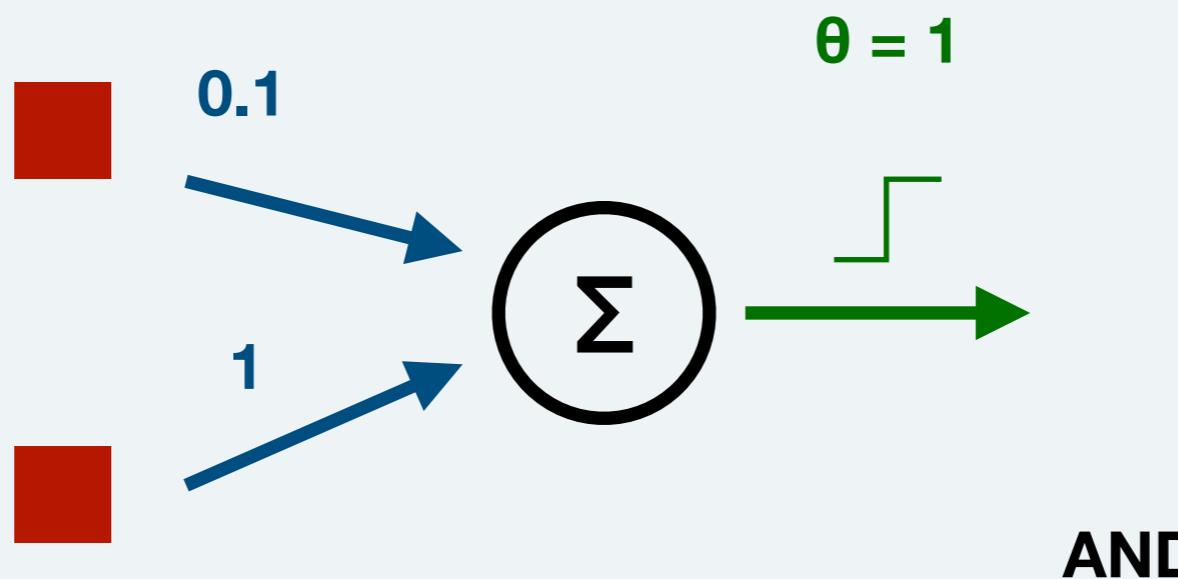
# The perceptron learning rule

modify weights by:

$$0.1 \times (0 - 1) \times \begin{bmatrix} 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 0 \\ -0.1 \end{bmatrix}$$



# The perceptron learning rule



AND

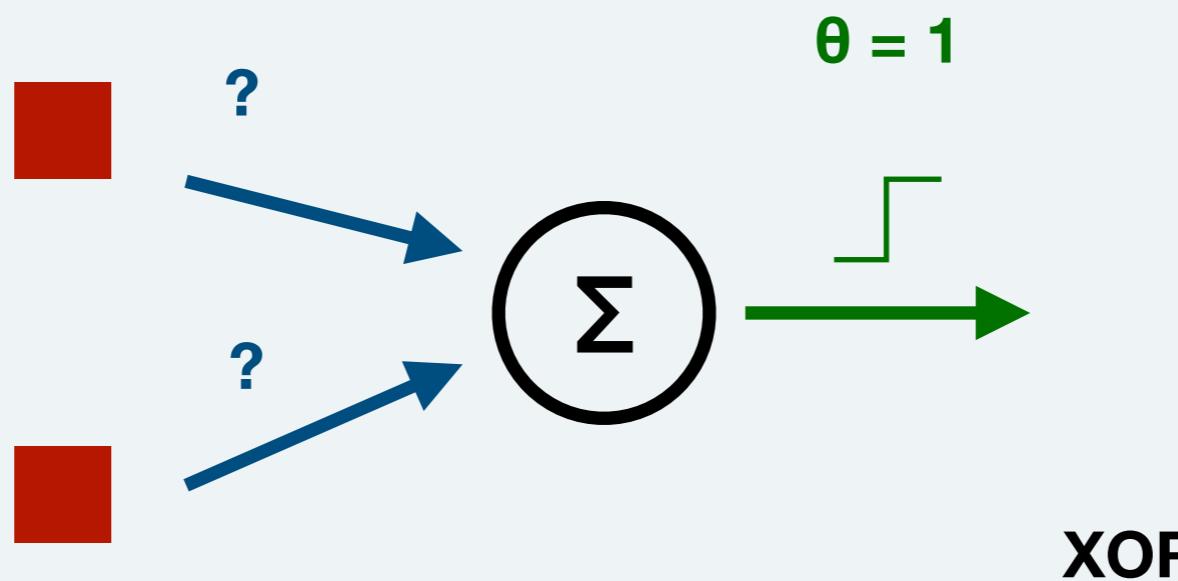
Correct  
weighting!

You did it  
perceptron

Perceptron is guaranteed to  
find the correct weights  
eventually (might be slow at  
large # inputs/weights)

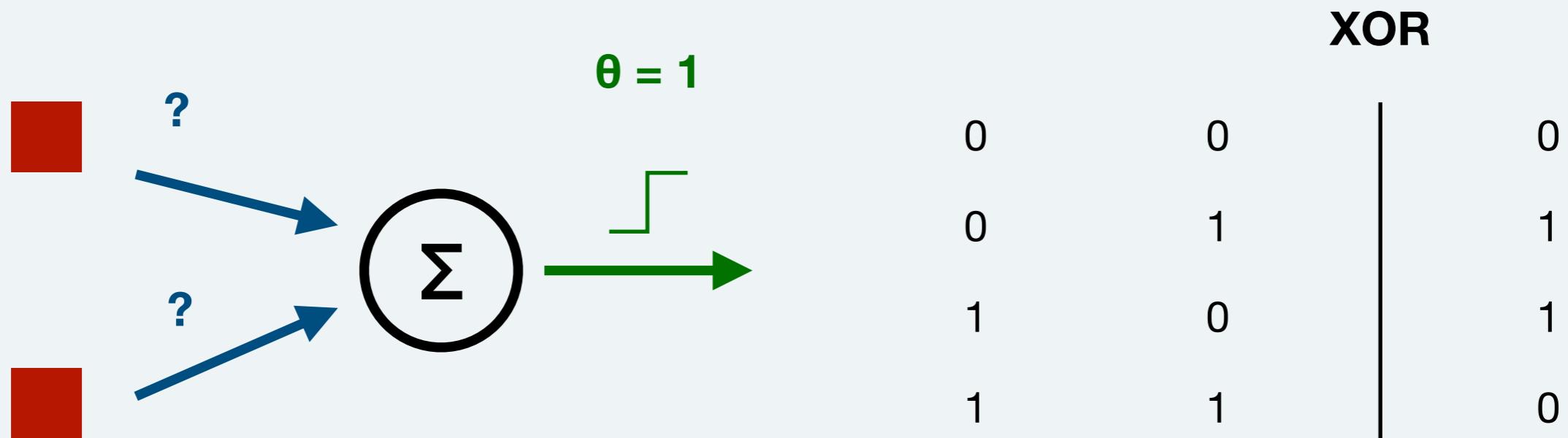
|   |   |   |
|---|---|---|
| 0 | 0 | 0 |
| 0 | 1 | 0 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

# Perceptron: an artificial neuron



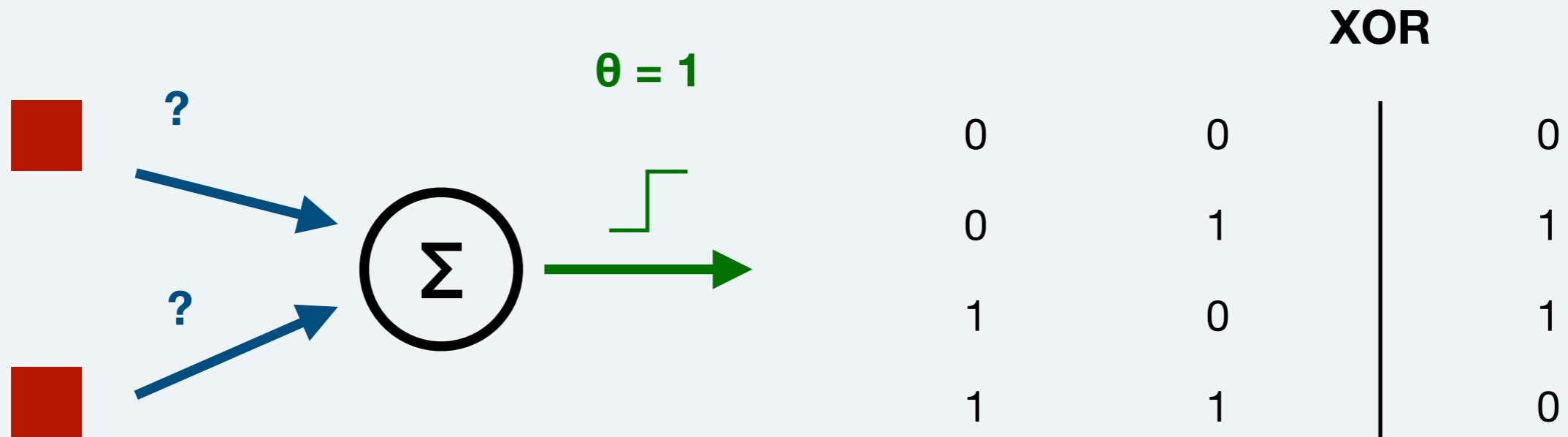
|   |   |   |   |
|---|---|---|---|
| <b>you can't!</b>   | 0 | 0 | 0 |
| Perceptron only has one layer of processing: very limited | 0 | 1 | 1 |
|   | 1 | 0 | 1 |
|   | 1 | 1 | 0 |

# Perceptron: an artificial neuron



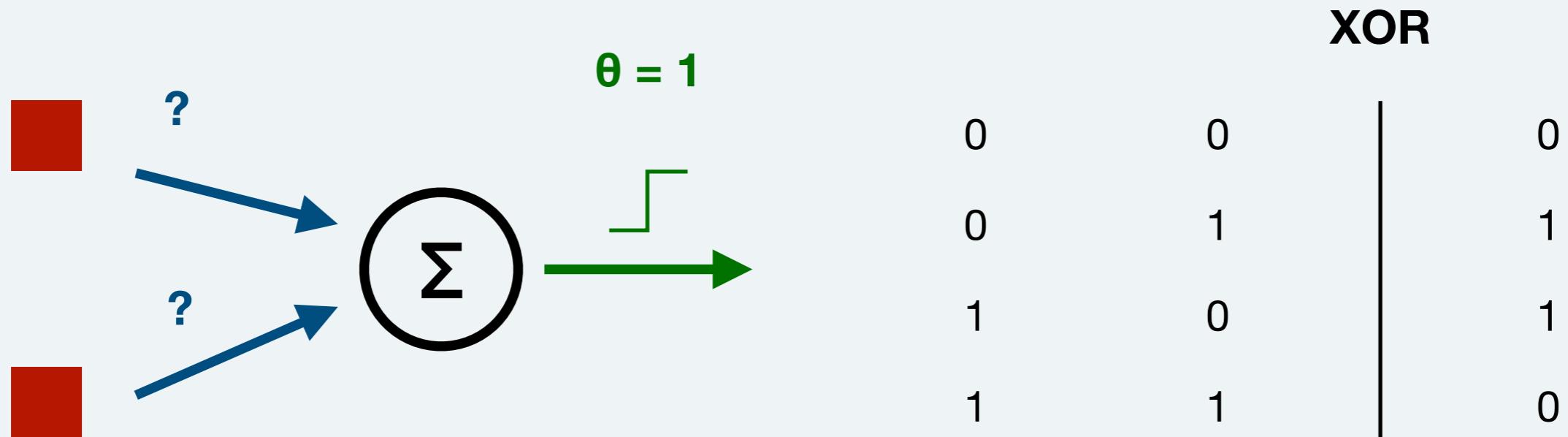
$$xw_x + yw_y = \theta$$

# Perceptron: an artificial neuron



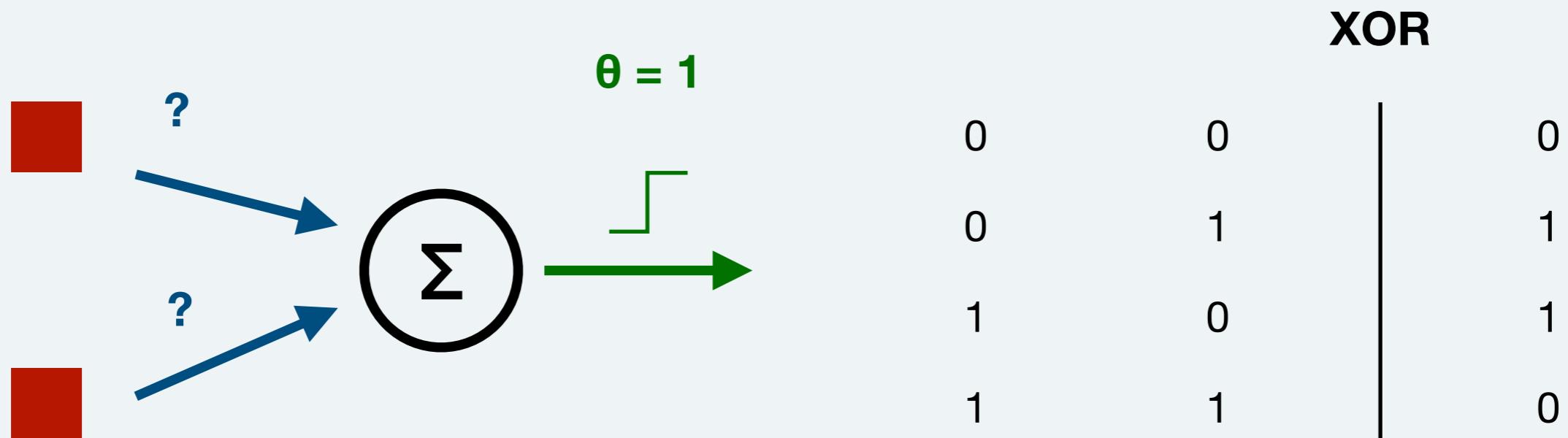
$$y w_y = \theta - x w_x$$

# Perceptron: an artificial neuron



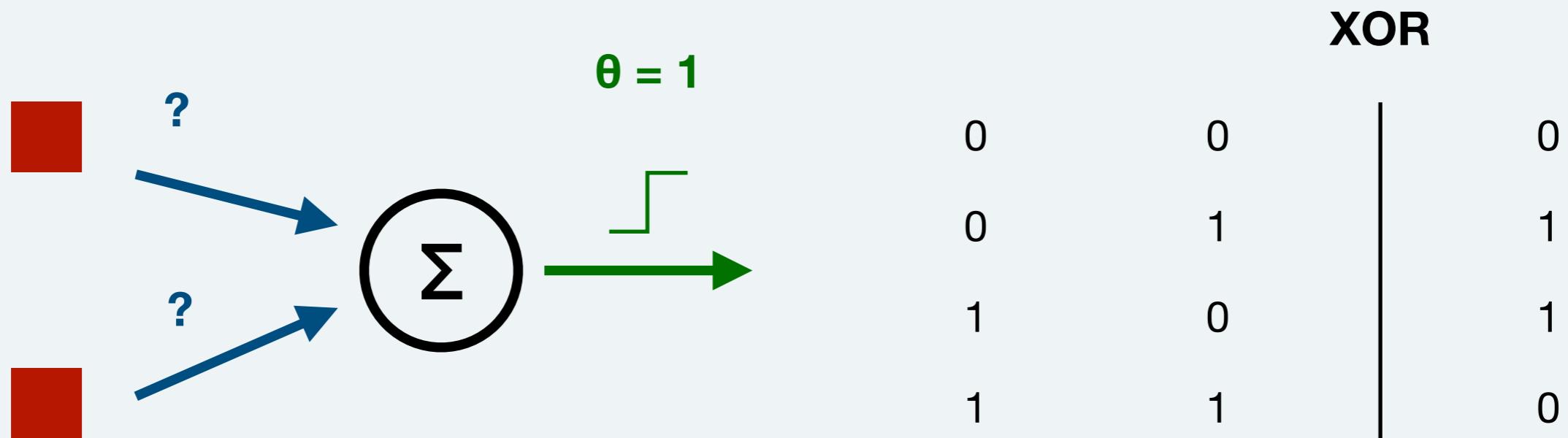
$$y = \theta/w_y - xw_x/w_y$$

# Perceptron: an artificial neuron



$$y = \underbrace{\theta / w_y}_{a} - \underbrace{xw_x / w_y}_{b}$$

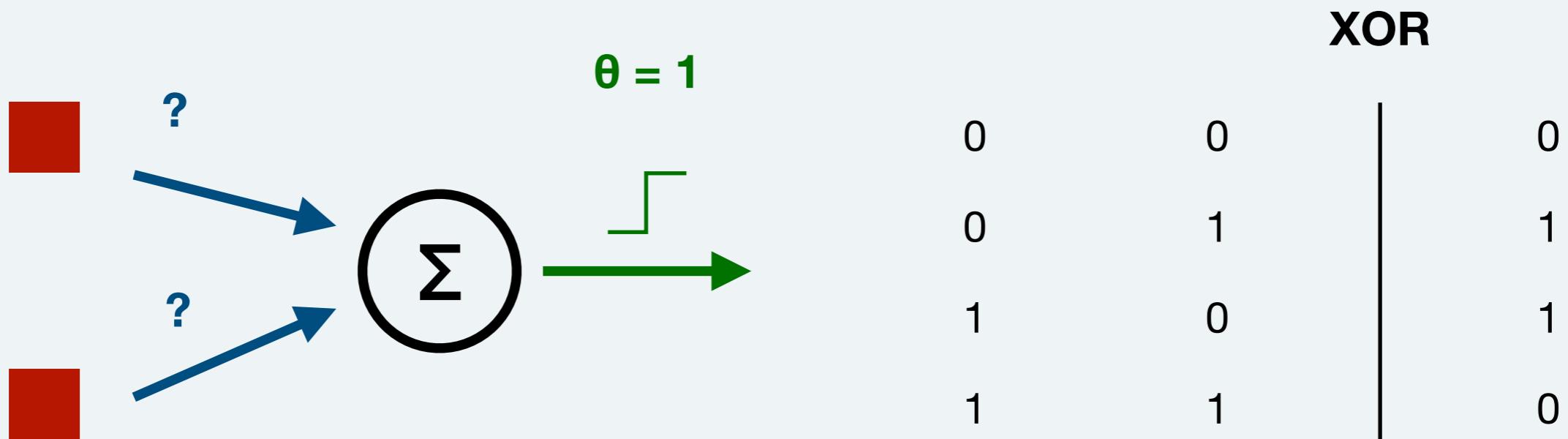
# Perceptron: an artificial neuron



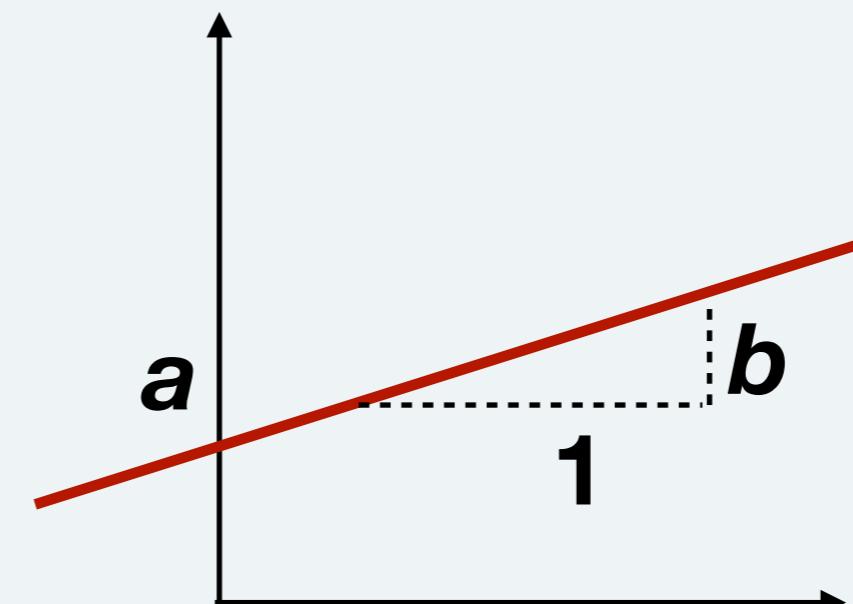
Equation for slope of a line..  
duh

$$y = a + bx$$

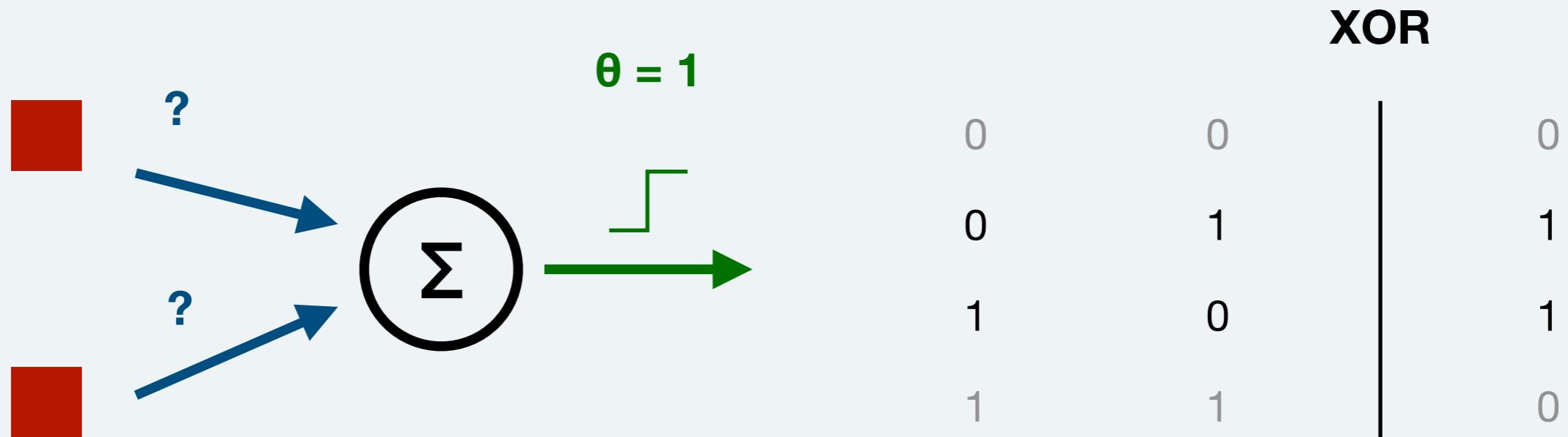
# Perceptron: an artificial neuron



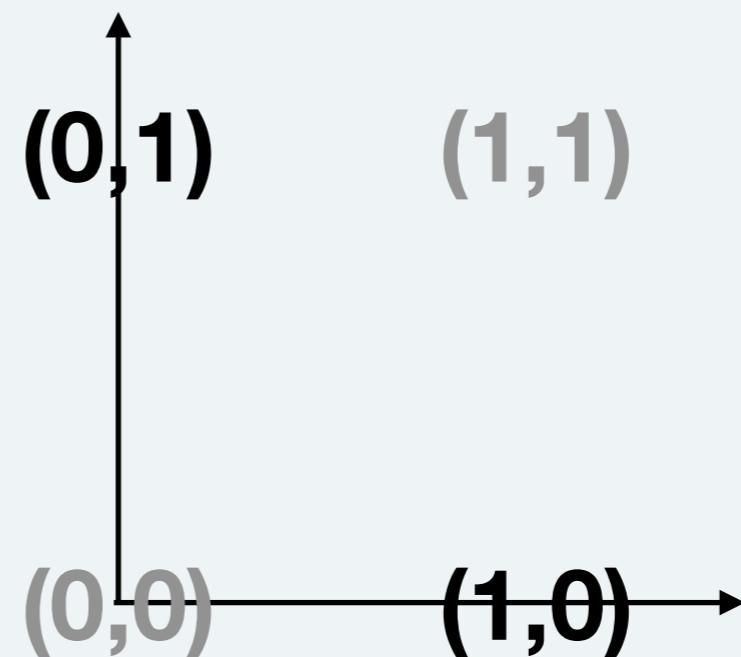
$$y = a + bx$$



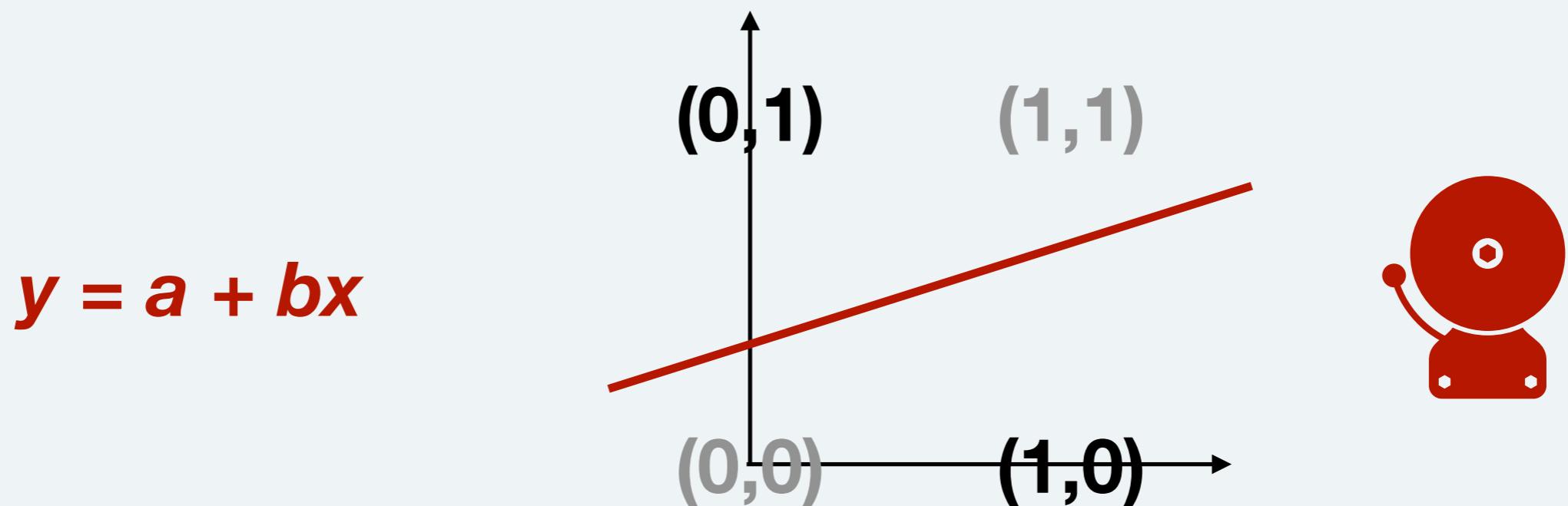
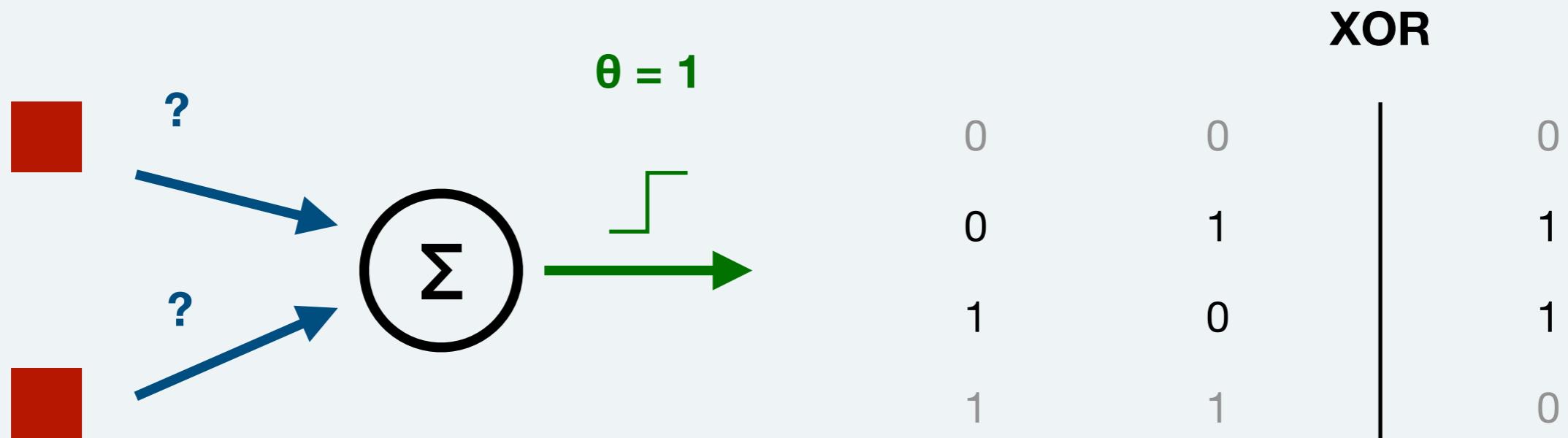
# Perceptron: an artificial neuron



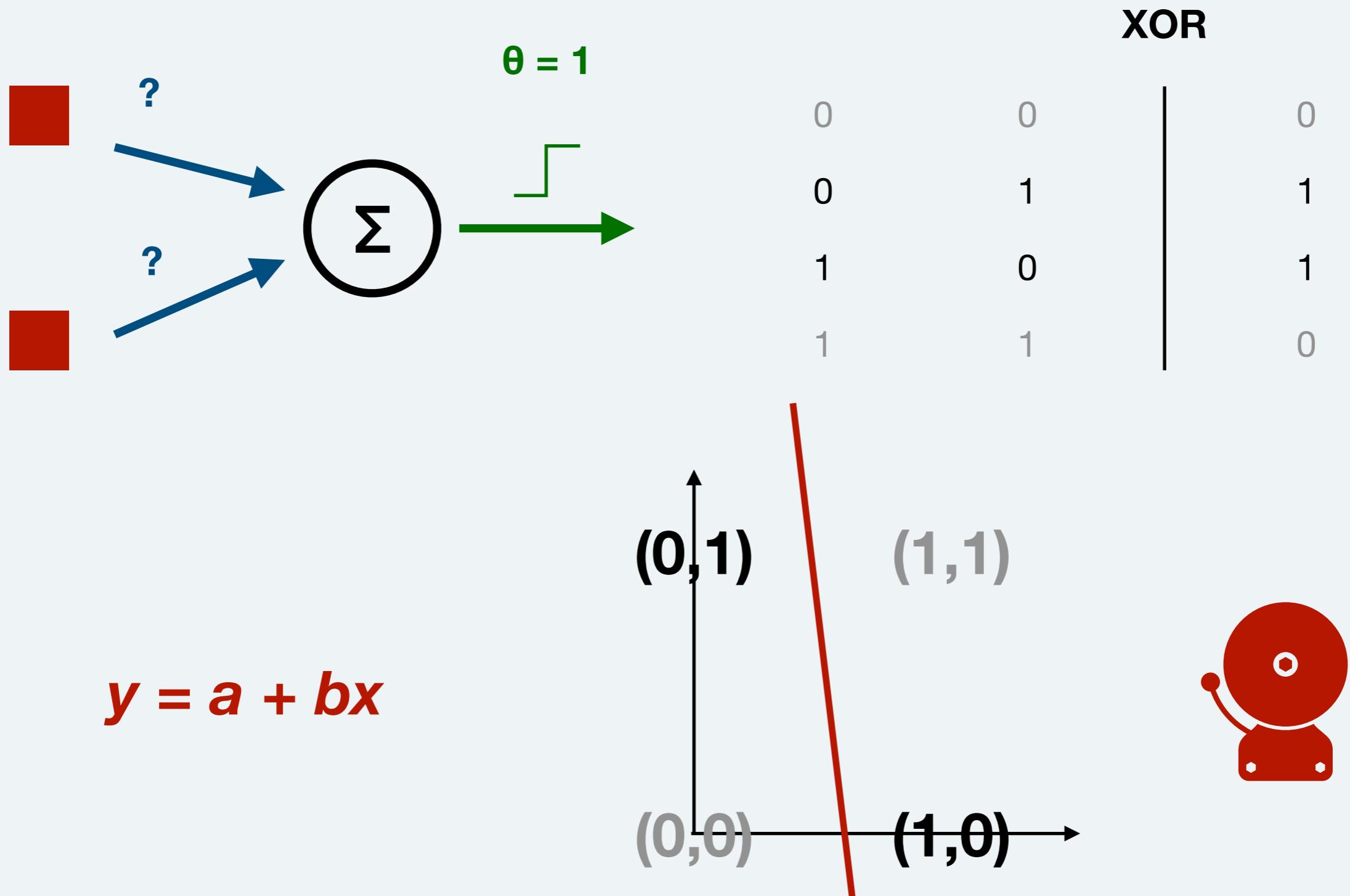
$$y = a + bx$$



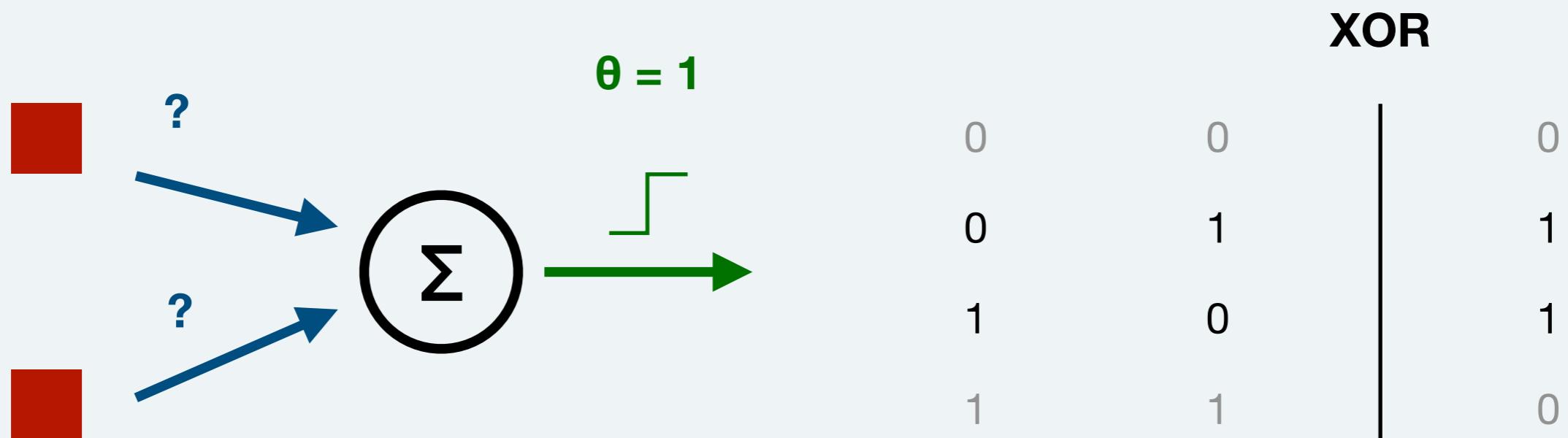
# Perceptron: an artificial neuron



# Perceptron: an artificial neuron

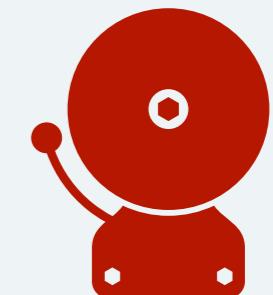
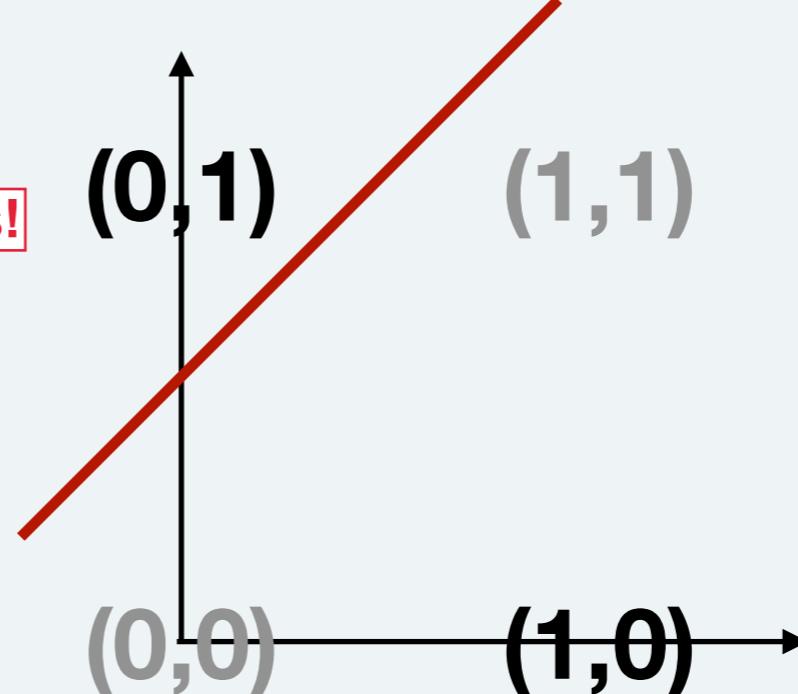


# Perceptron: an artificial neuron



Doesn't work for non-linear functions!

$$y = a + bx$$

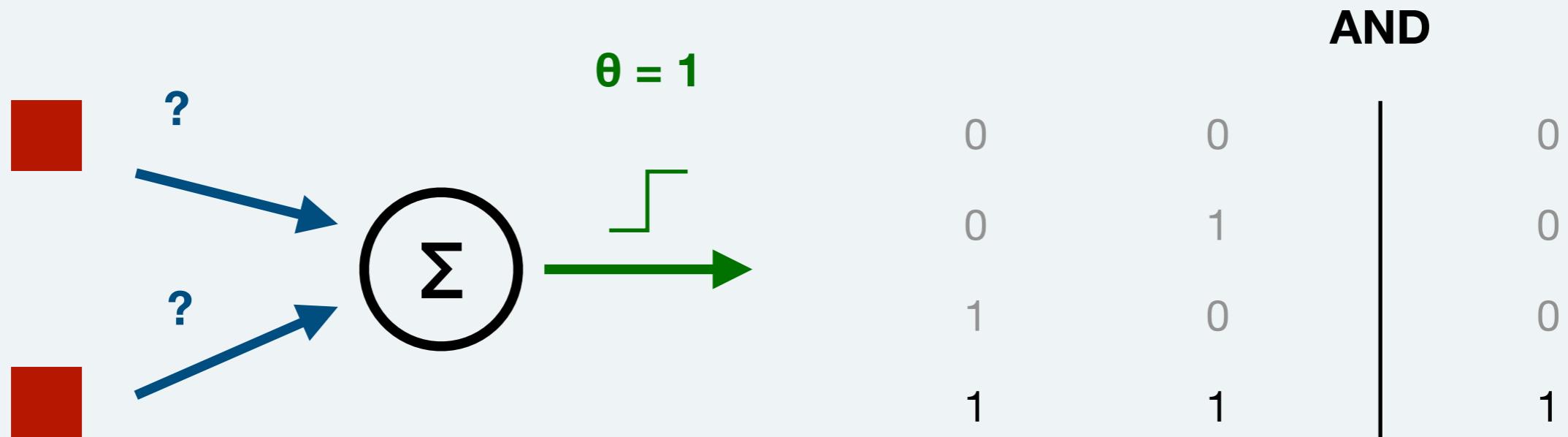


# Perceptron: an artificial neuron

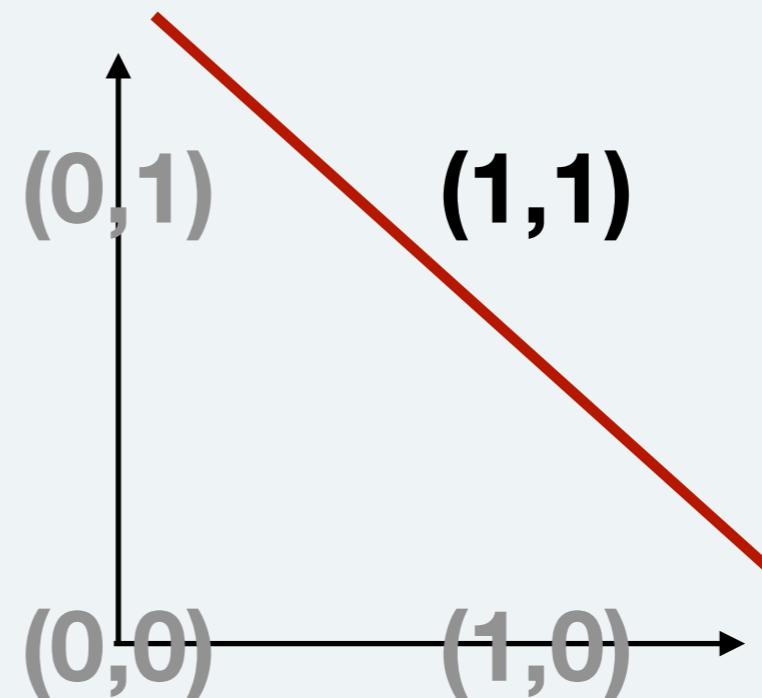
SAD



# Perceptron: an artificial neuron



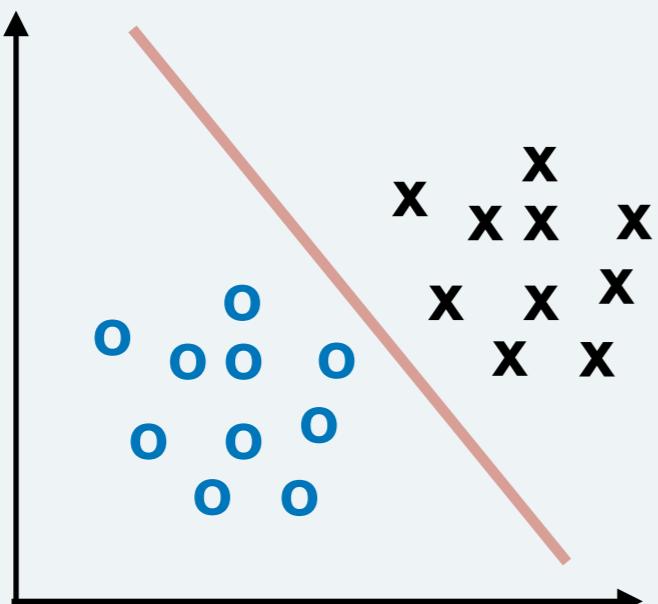
$$y = a + bx$$



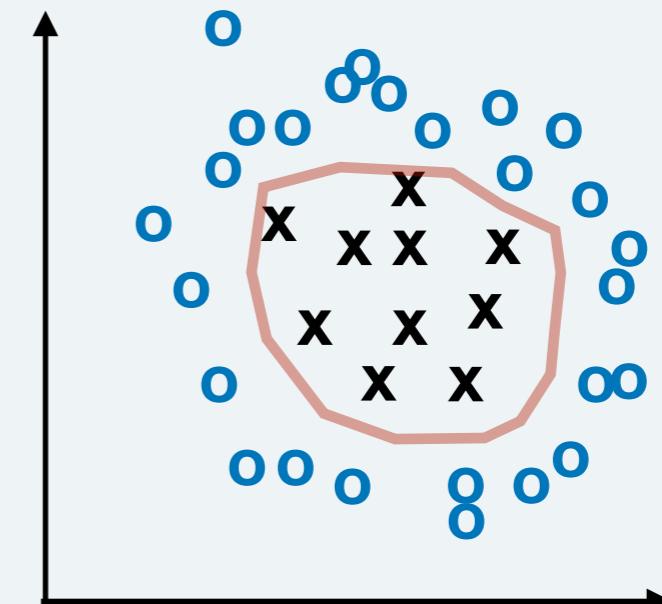
# Perceptron: an artificial neuron

Perceptron can only handle linearly separable

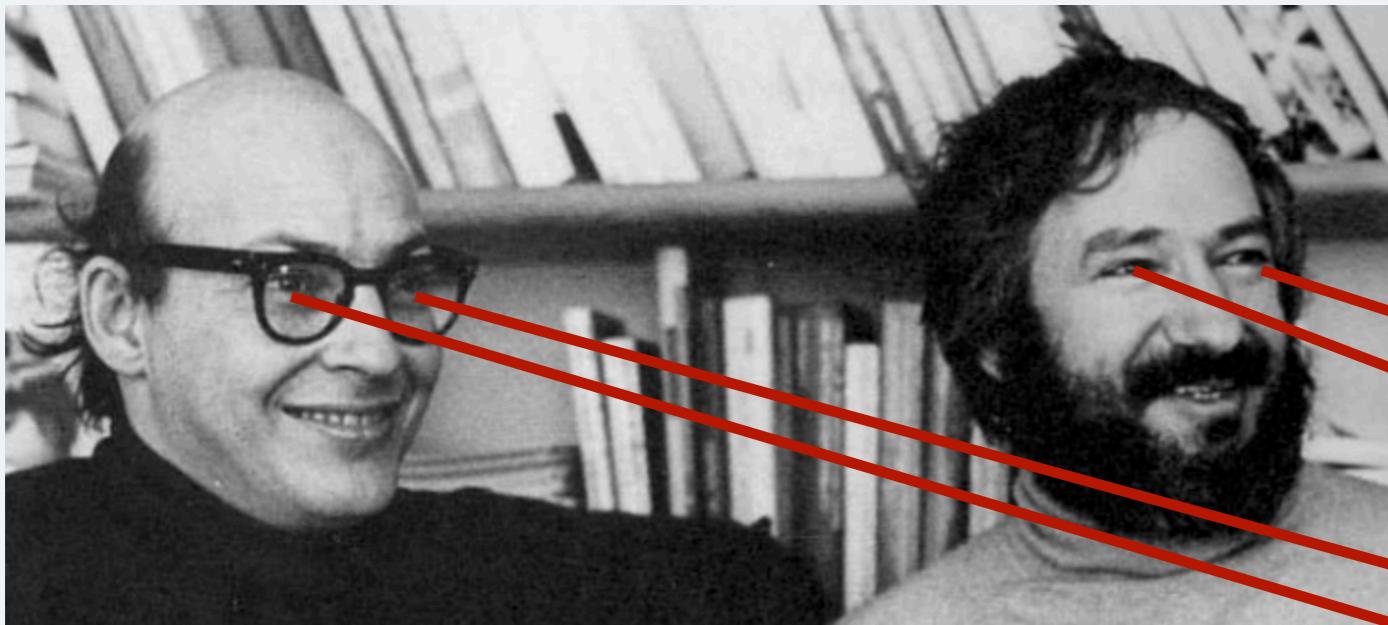
**linearly separable**



**not linearly separable**



# Scientists at each other's throats – again!



# Scientists at each other's throats – again!

**Marvin  
Minsky**



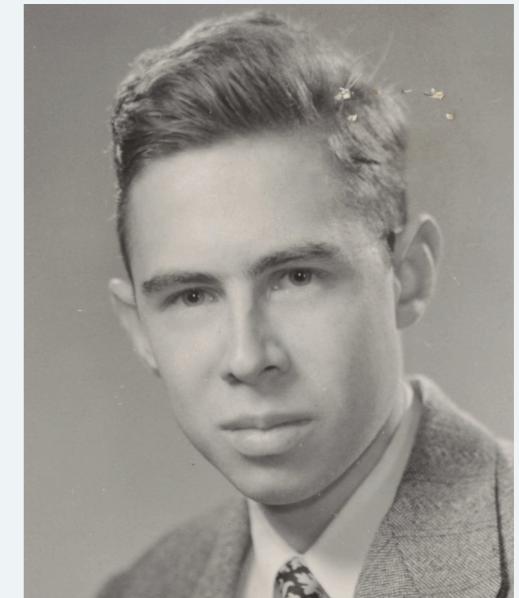
TBT PHIL  
351!

**Seymour  
Papert**

**Team Symbolic AI (aka: PSS)  
(key date: 1969)**

**Team Perceptron  
(key date: 1957)**

**Frank Rosenblatt**



"AI winter": people  
didn't work on  
ANNs for a while