

# Lecture 21: Inferential Statistics

Friday, November 10, 2023

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Lectures: MWF 12:00 PM – 1:00 PM (003); 1:00 PM – 2:00 PM (004); 2:00 PM – 3:00 PM (010)

Office hours: Tuesdays 2:00 PM – 4:00 PM

## How to study?

- More retrieval reinforces learning, leads to better recall
- Focus on rereading indicative of emphasizing “encoding” aspect of memory, not the “retrieval” aspect of memory
  - But repeated retrieval actually prevents forgetting due to repeated practice

## How to study?

- What we obtained were mean differences between groups
  - How likely are these differences due to chance rather than a real effect of study method?

## How to study?

### Null Hypothesis

- Mean 1 = Mean 2
- $H_0$
- **True effect:** Study technique does not affect memory retention
- Differences between groups are most likely **due to random chance**

### Research Hypothesis

- Mean 1  $\neq$  Mean 2
- $H_1$  or  $H_A$
- **True effect:** Study technique affects memory retention
- Differences between groups are **unlikely to be due to random chance**

## Directional vs. Non-directional Hypotheses

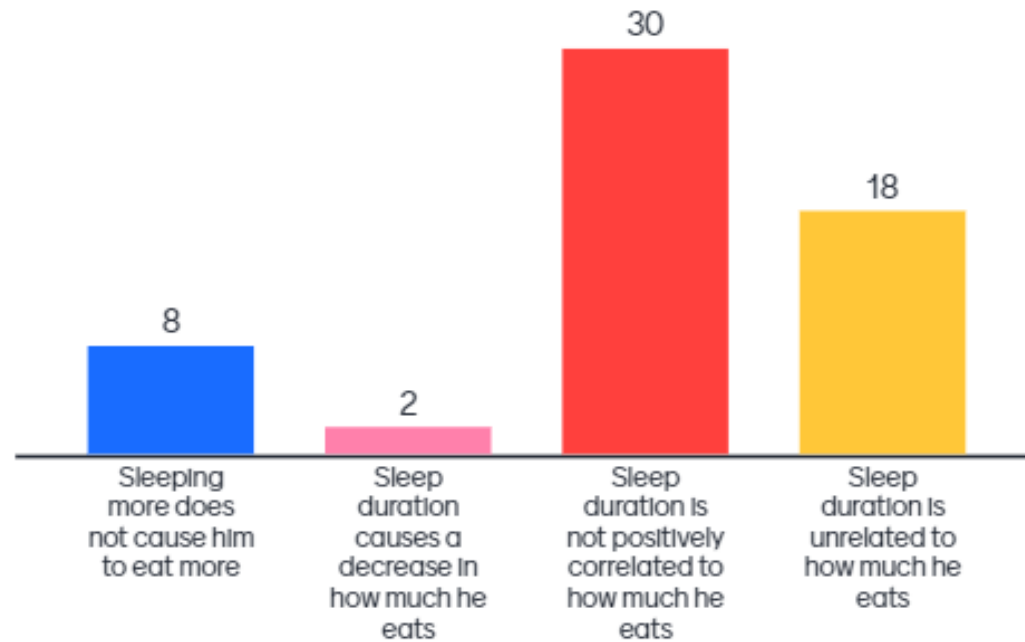
### Null Hypothesis

- $\text{Mean } 1 \leq \text{Mean } 2$
- $H_0$
- **True effect:** Repeated retrieval does not lead to better memory retention than solely studying
- **Random chance likely caused**  $\text{Mean } 1 > \text{Mean } 2$  in our sample

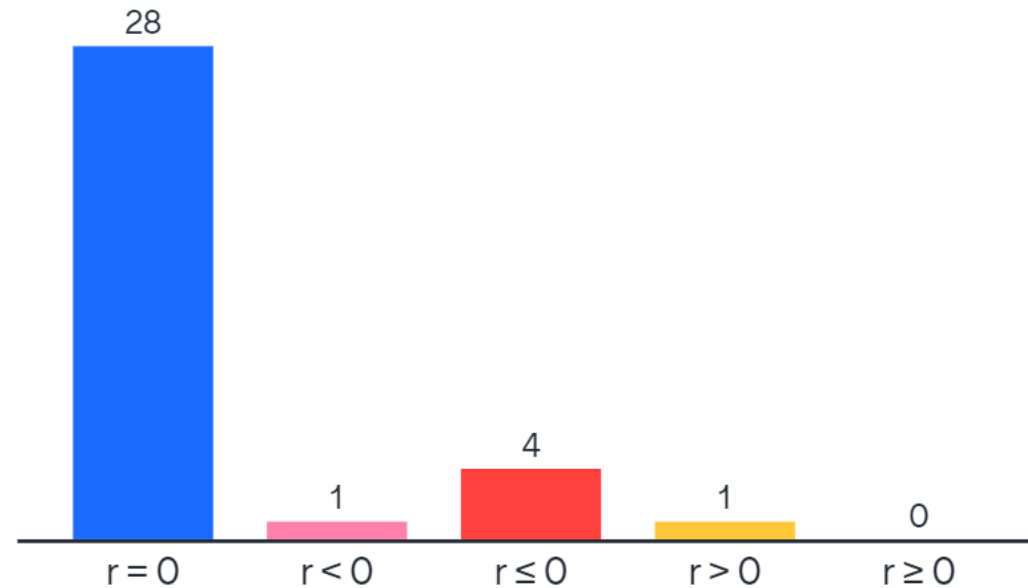
### Research Hypothesis

- $\text{Mean } 1 > \text{Mean } 2$
- $H_1$  or  $H_A$
- **True effect:** Repeated retrieval leads to better memory retention than solely studying
- **Random chance is a very *unlikely*** explanation that  $\text{Mean } 1 > \text{Mean } 2$  in our sample

Charles is doing a study to see if there's a relationship between how much he sleeps and how much food he can eat.



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## Due to chance...?

- Key part of interpretation:
  - Was the difference due to chance, or does it reflect a real difference in the population?
- Whether something is due to chance is always the most parsimonious alternative explanation for any research finding
  - When analysing data, start by assuming that the null hypothesis is true
  - Can we reject the null hypothesis?



## Learning objectives

- By the end of this class, you'll be able to
  - Explain the relationship between a sample and a population
  - Explain how a sampling distribution is made
  - List the 3 steps in hypothesis testing
  - Explain the logic of the numerator and the denominator in the  $t$ -ratio
  - Differentiate between Type I and Type II errors

## Large vs. small samples

- Small samples subject to more error in estimating population value
- Even with random assignment, problem still remains
- Random assignment works best with large sample sizes
  - Chance plays major role in statistical analysis and research methods!

Precursor for next session: When an effect does not exist in the population, but we conclude that there is an effect → Type 1 error

## Statistically significance? Easy as 1- 2-3!

1. Calculate a statistic that captures the effect.
  - E.g., % (Chi square), mean difference ( $t$  or  $F$  value) , correlation ( $r$ )...
2. Refer to a sampling distribution for comparison
  - For this sample size, what is an expected statistic value *if there actually is NO effect going on*.
3. Make a decision
  - Is our statistic value sufficiently rare to consider it *significant*?
  - If yes, reject the null hypothesis (LET'S PUBLISH!)
  - If no, retain the null hypothesis (CRY IN A CORNER!)

## Basics of sampling distribution

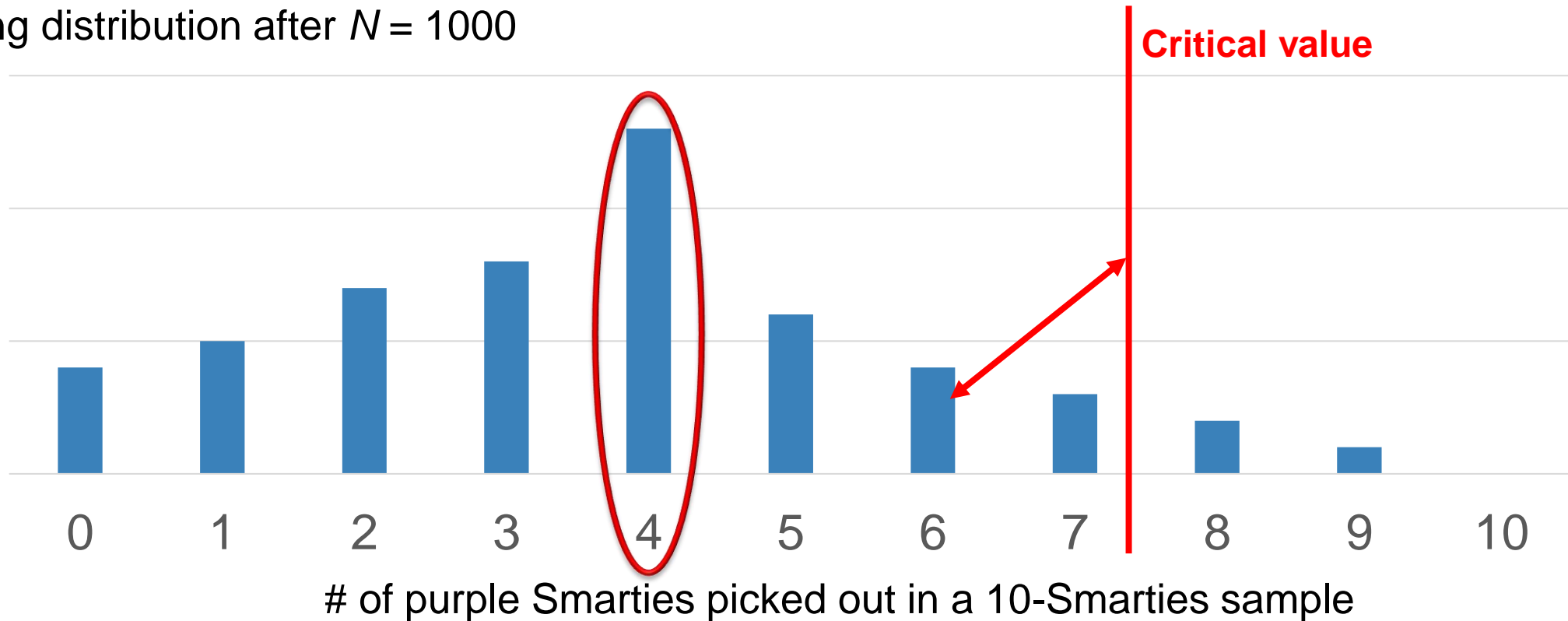
- Sampling distribution:
  - Probability distribution of any statistic of interest assuming the null hypothesis is true (i.e. random chance)
  - What it answers: What statistical result would you get from your data if your effects were only due to random chance?

## Basics of sampling distribution

- My claim: While blindfolded, I have magical powers that no one else has, so more than half that I pick out will be purple Smarties in a sample of 10 Smarties
- What we need to know: How many purple Smarties would someone pull out at random in 10 Smarties?
- What we want: Sampling distribution for the number of purple Smarties in a sample of 10 Smarties
  1. First: Get 1000 blindfolded students to take samples of 10 Smarties from a giant Smarties bag
  2. Then: Determine how likely it is to pick out any number of purple Smarties by chance

# Basics of sampling distribution

Sampling distribution after  $N = 1000$



- Decide on what's a rare # of purples as threshold = Critical value
- How does my performance compare to critical value?
- Similar to sampling distributions for other statistics

## Statistically significance? Easy as 1- 2-3!

1. Calculate a statistic that captures the effect.
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Get ready, because...





## $t$ -test

- A statistical technique: is difference between two means something to be expected from random chance ... *if the null hypothesis is true?*
- If  $t$  obtained exceeds critical  $t$  value: suggests that the  $H_0$  might not be true

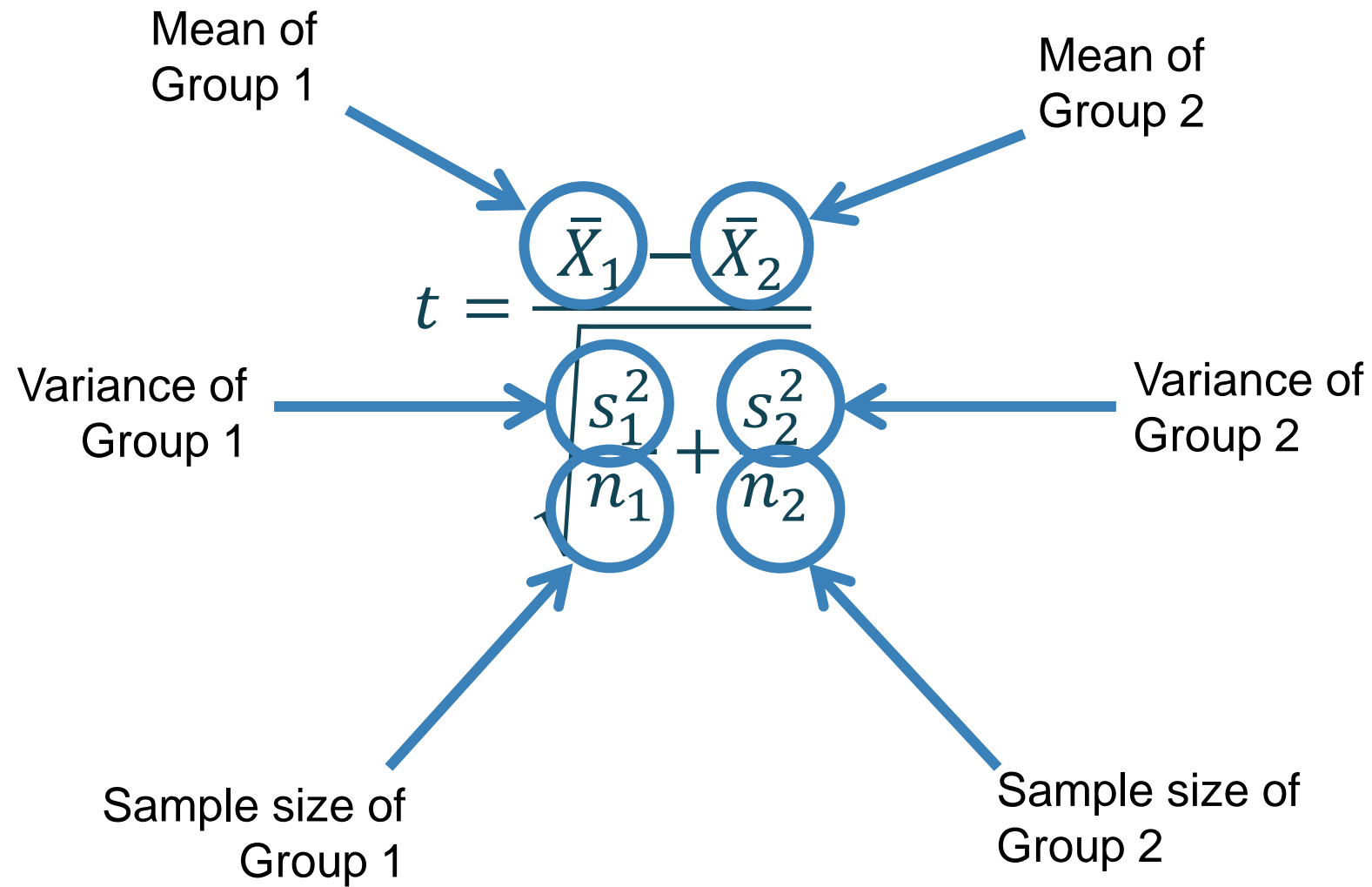
## Determining if two means are significantly different from each other

- 1. Find “obtained  $t$ ” value
  - Use formula to convert the mean difference and standard deviation into a  $t$  value
- 2. Refer to sampling distribution of  $t$  values
  - Find “critical  $t$ ” value for that df and alpha
  - From the table (Appendix C, Table C.2)
  - *Don't need to find this for 217*
- 3. Make a decision
  - Is our statistic value sufficiently rare to consider it *significant*?
  - Is absolute value of  $|t_{\text{obt}}| > |t_{\text{crit}}|$ ?
    - If yes, reject the null hypothesis
    - If no, retain the null hypothesis

# Inferential Statistics Overview

- Null & Research Hypotheses
- Sampling distribution
- $t$ -test logic
- Statistically significant
- Type 1 and Type 2 errors
- Apply your understanding

# Finding $t_{\text{obt}}$



## Finding $t_{\text{obt}}$

$$t = \frac{\bar{X}_1 - \bar{X}_2}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$$

**Numerator:**  
How big is the difference?

**Denominator:**  
How much variation exists around the means?

# Finding $t_{\text{obt}}$

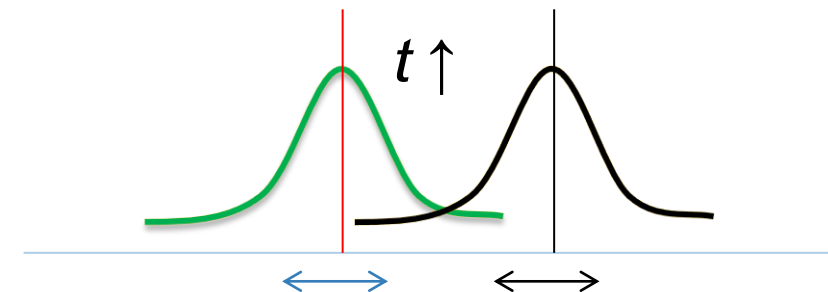
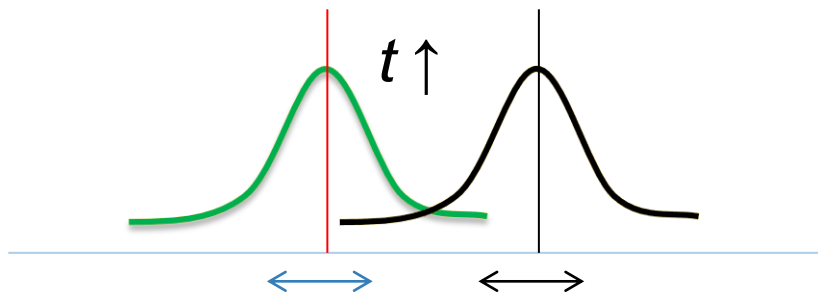
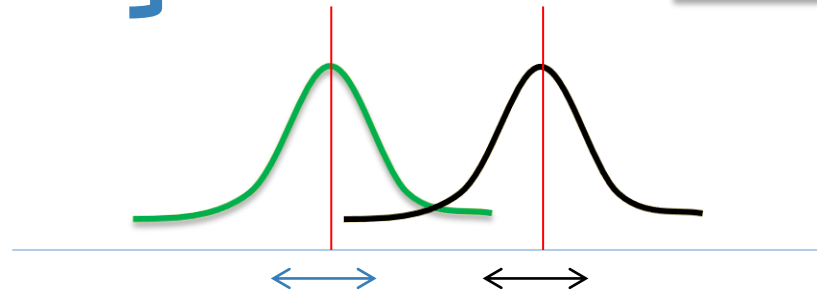
$$t = \frac{\bar{X}_1 - \bar{X}_2}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$$

Signal / Effect

Noise / Error

Between-Group  
Difference

Within-Group  
Variability



# Rank the following in terms of $t(\text{obt})$ with greatest value being Rank 1

