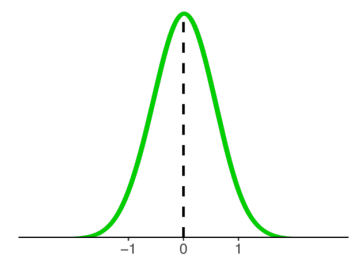
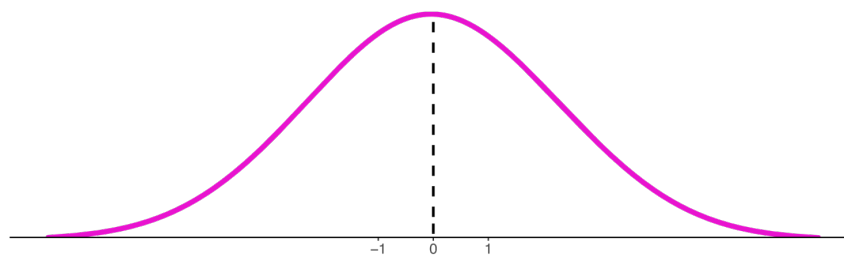
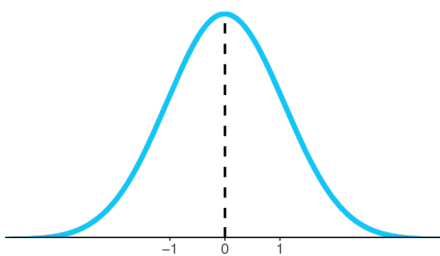


Learning Objectives

- **Describe** three models/measures of *variability*
 - Range
 - Standard Deviation
 - Variance
- **Calculate** variability by hand (& calculator)
- **Interpret** models of variability

Central Tendency, Skew & Variability

- *Central tendency, skew, and variability* describe the distribution of observations
 - Variability quantifies how spread out scores are



3 Models of Variability

1. Range

Range?

2. Standard Deviation

s , σ , std, s.d.

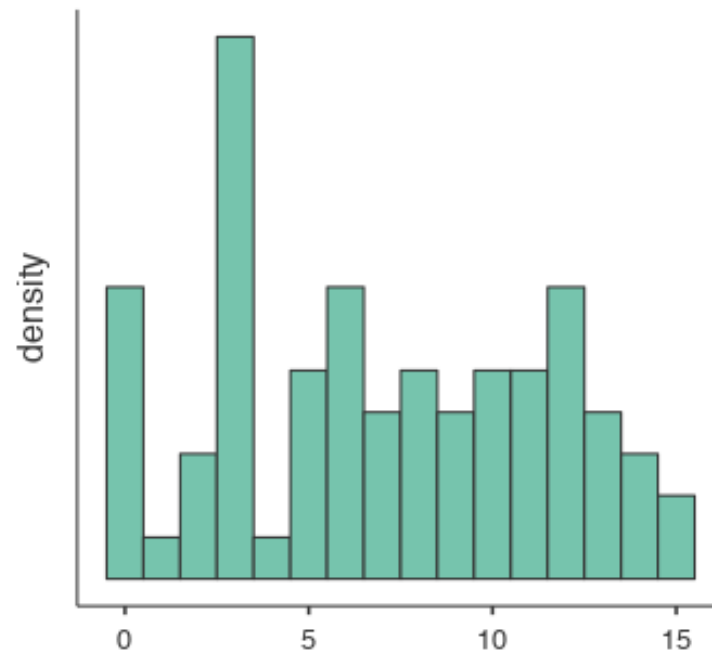
3. Variance

s^2 , σ^2 , var

Range

- **Range** is the absolute difference between the most extreme scores
 - Data = Nutritional values from ($N=77$) cereals

Density Histogram. Grams sugar per 28g of cereal.



Range

Formula:

$$\text{Range} = \text{Max} - \text{Min}$$

$$= X_{\text{Smacks}} - X_{\text{SW}}$$



Cereal	g/Sugar
All Bran	5
Cap'n Crunch	12
Corn Flakes	2
Kix	3
Lucky Charms	12
Shredded Wheat	1
Smacks	15
Special K	3
Trix	12
Wheaties	3

Deviation Score

- Amount an observation deviates from the sample mean

Formula:

$$X_i - \bar{X}$$

What is the deviation score for X_{trix} ?

Hint $\bar{X} = \frac{\sum X_i}{N}$



Cereal	g/Sugar
All Bran	5
Cap'n Crunch	12
Corn Flakes	2
Kix	3
Lucky Charms	12
Shredded Wheat	1
Smacks	15
Special K	3
Trix	12
Wheaties	3

Summed Deviation

Formula:

$$\Sigma(X_i - \bar{X})$$

What is the summed deviation?

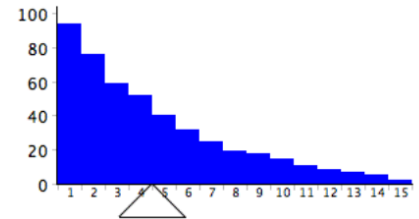
Remember $\bar{X} = 6.8$

Cereal	g/Sugar
All Bran	5
Cap'n Crunch	12
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Deviations

Problem: Summing or averaging deviation scores will give us 0

- Remember the mean is a fulcrum



Solution: Square each deviation score

- All negative deviations become positive
- **Then** sum these squared deviations together for the *sum of squared deviations* (or *SS*)

$$SS = \Sigma (X_i - \bar{X})^2$$

Standard Deviation

- SS is the total **sum** of squared deviations
 - Dividing this by N gives us **mean** squared deviation (aka, *variance*)
 - Taking the *square root* gives us mean deviation or ***standard deviation***
 - But, this needs a slight correction for bias (in samples)*

$$S = \sqrt{\frac{\sum (X_i - \bar{X})^2}{N - 1}}$$

Sample vs. Population

$$s = \sigma_{\text{est}} = \sqrt{\frac{\Sigma(X_i - \bar{X})^2}{N - 1}}$$

$$\sigma = \sigma_{\text{pop}} = \sqrt{\frac{\Sigma(X_i - \mu)^2}{N}}$$

Statisticians suck

- “*What’s the deal with skew?*”
- “*Why no symbol for range?*” ☹
- Regular letters = *Italicized*; Greek = not



‘Sigma’	
Σ	σ

Formula Review

$$\Sigma(X_i - \bar{X})^2 = \text{Sum of squares (SS)}$$

$$\sqrt{\frac{\Sigma(X_i - \bar{X})^2}{N - 1}} = \text{Standard deviation}$$

(sample not pop.)

Formula Review

$$\Sigma(X_i - \bar{X})^2 = \text{Sum of squares (SS)}$$

$$\sqrt{\frac{\Sigma(X_i - \bar{X})^2}{N - 1}} = \text{Standard deviation}$$

(sample not pop.)

$$= \text{Variance!}$$

Alternative Formulas

$$\sum X^2 - \frac{(\sum X)^2}{N} = \text{Sum of squares (SS)}$$

$$\sqrt{\frac{SS}{N - 1}} = \text{Standard deviation (s)}$$

$$= \text{Variance (s}^2\text{)}$$