LAB 5

Geometric (data) decomposition: heat diffusion equation

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Introduction

In the las session we are going to study the parallel performance of two heat diffusion algorithms, Jacobi and Gauss-Seidel. Then we are going to parallelize the code using OpenMP.

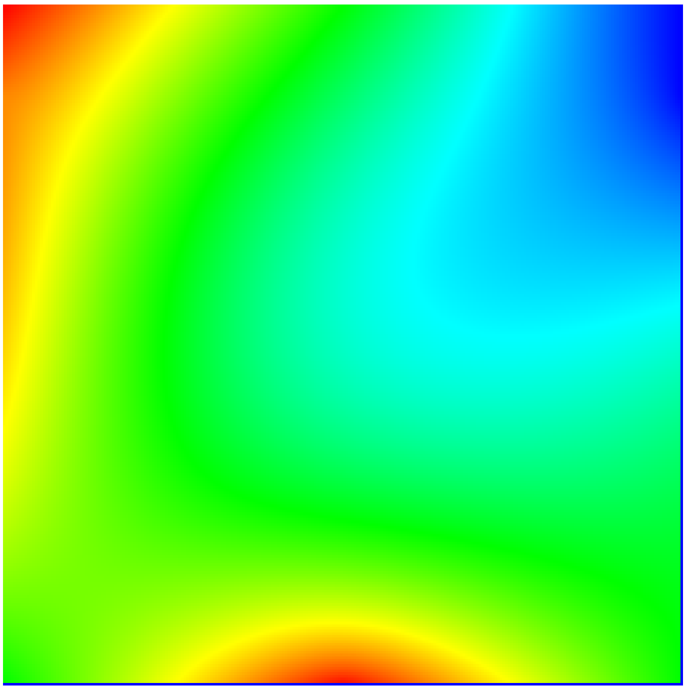
Sequential heat diffusion program

First of all, lets execute the sequential versions of heat, one using Jacobi algorithm and an otherone using Gauss-Seidel algorithm.

Jacobi solver:

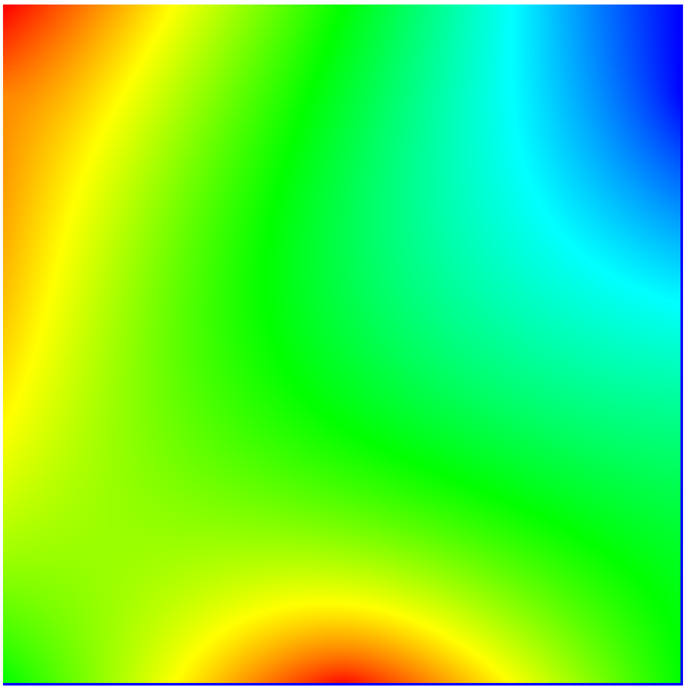
```
Iterations        : 25000
Resolution        : 254
Algorithm         : 0 (Jacobi)
Num. Heat sources : 2
   1: (0.00, 0.00) 1.00 2.50
   2: (0.50, 1.00) 1.00 2.50
Time: 5.365
Flops and Flops per second: (11.182 GFlop => 2084.06 MFlop/s)
Convergence to residual=0.000050: 15756 iterations
```

Result heat map:



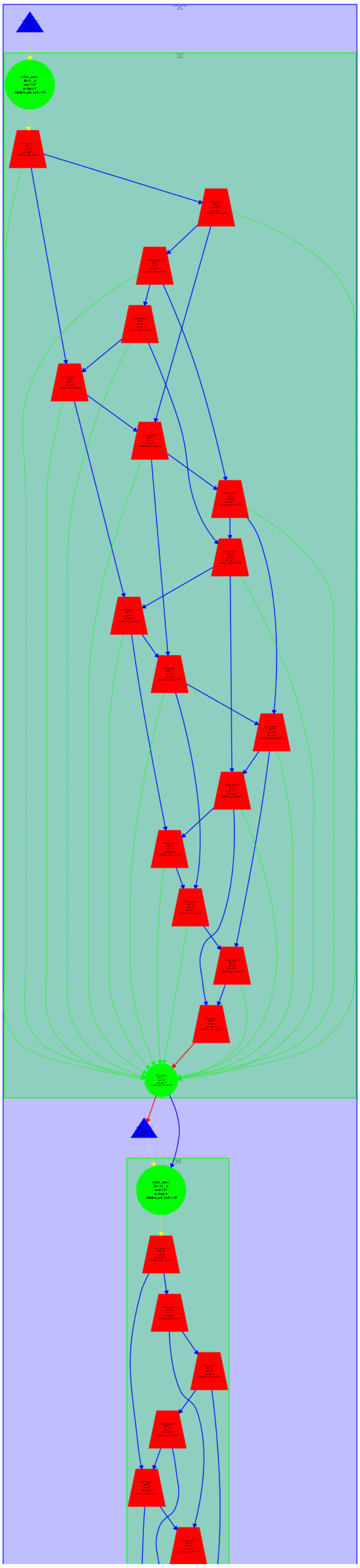
```
Iterations        : 25000
Resolution        : 254
Algorithm         : 1 (Gauss-Seidel)
Num. Heat sources : 2
   1: (0.00, 0.00) 1.00 2.50
   2: (0.50, 1.00) 1.00 2.50
Time: 6.305
Flops and Flops per second: (8.806 GFlop => 1396.78 MFlop/s)
Convergence to residual=0.000050: 12409 iterations
```

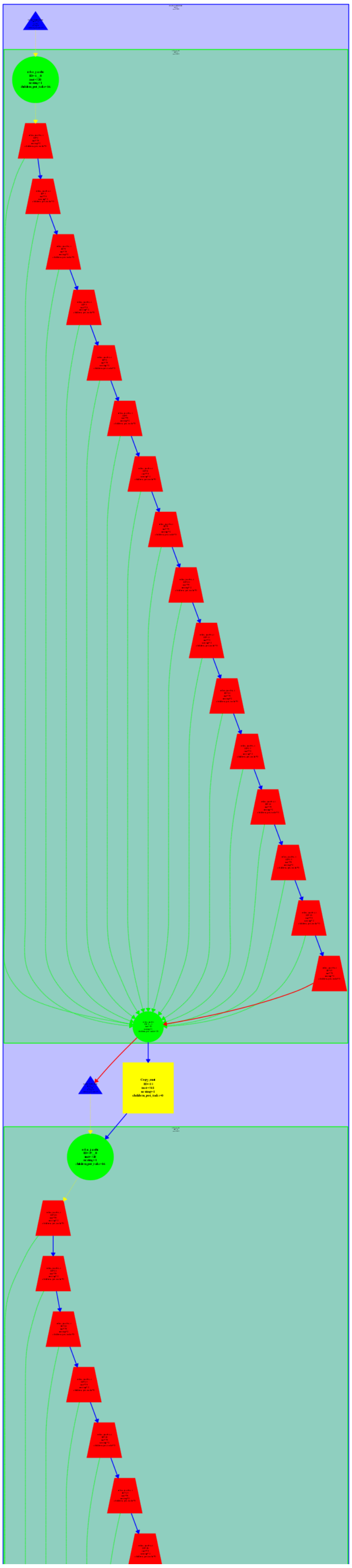
Result heat map:

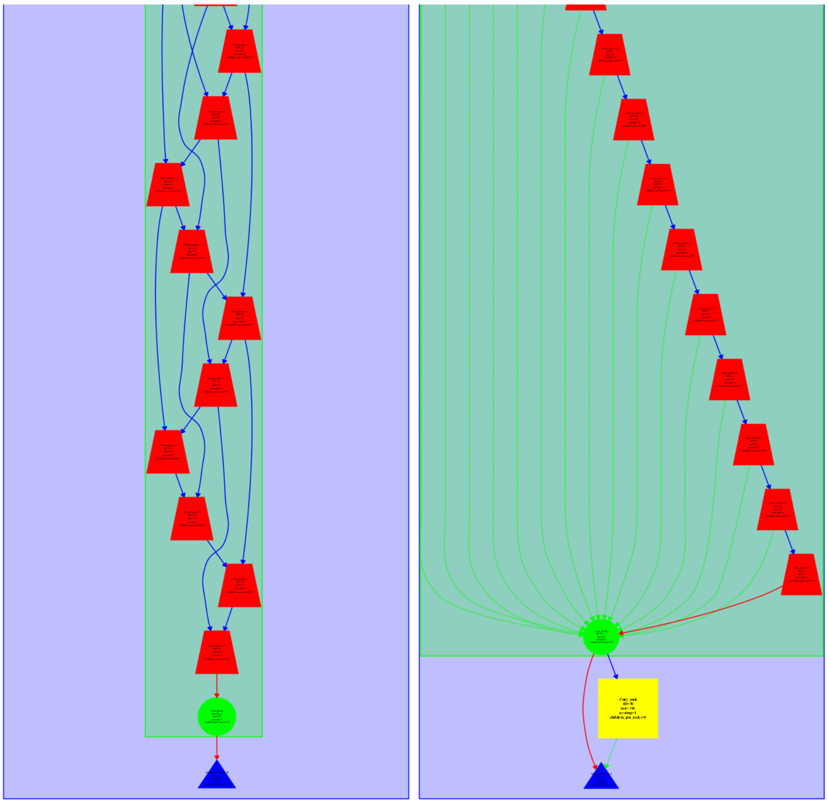


Analysis with Tareador

Now we are going to study tareador dependences graphs. We got two diferents gaphs, one with Jacovi solver algorithm and another with Gauss-Seidel algorithm.







Dependnece graph of the program using Gauss-Seidel and Jacovi algorthms.

Observing the first dependence graph we can conclude that there are data dependences from sum. Depencences come from two different iterations in some cases.

As we can observe at the jacobi graph also exists a data dependence between interations of jacobi_rexlax loop. The variable that cuase that dependence is sum form the previous iteration. It could be parallelized using a reduction.

Parallelization of Jacobi With OpenMP parallel

In order to parallelize the jacobi solver function we used a parallel region with a reduction sum and diff as a private varialbe.

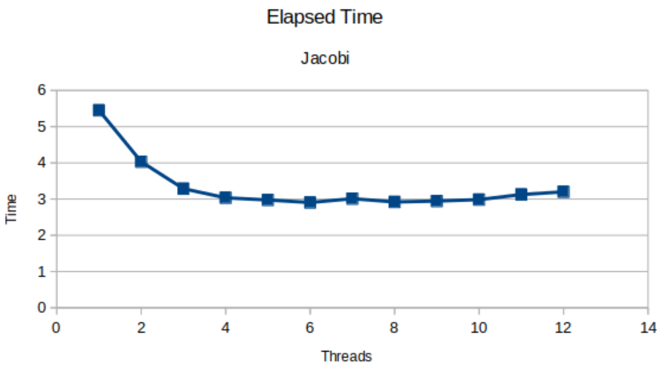
The resulting code is:

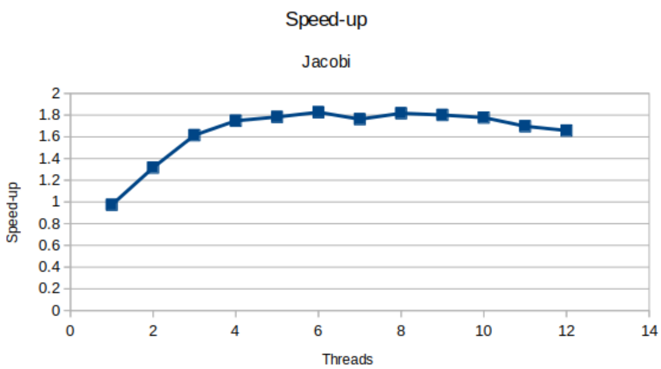
```
double relax_jacobi (double *u, double *utmp, unsigned sizex, unsigned
sizey)
{
  double diff, sum=0.0;
  #pragma omp parallel private(diff) reduction (+:sum)
  {
    int funci= omp_get_thread_num();
  int thre = omp_get_num_threads();
  int i_start = lowerb(funci, thre, sizex);
  int i_end = upperb(funci, thre, sizex);

  for (int i=max(1, i_start); i<= min(sizex-2, i_end); i++) {
    for (int j=1; j<= sizey-2; j++) {
      utmp[i*sizey+j]= 0.25 * ( u[ i*sizey + (j-1) ]+  // left
                                u[ i*sizey + (j+1) ]+  // right
                                u[ (i-1)*sizey + j ]+  // top
                                u[ (i+1)*sizey + j ]); // bottom
      diff = utmp[i*sizey+j] - u[i*sizey + j];
      sum += diff * diff;
    }
  }
  }
  return sum;
}
```

solver-omp.c

With that parallelization strategy we got the following plots:





As we can apreciate at the plots there is a inflation pint at 4 threads.

Parallelization of Gauss-Seidel with OpenMP ordered

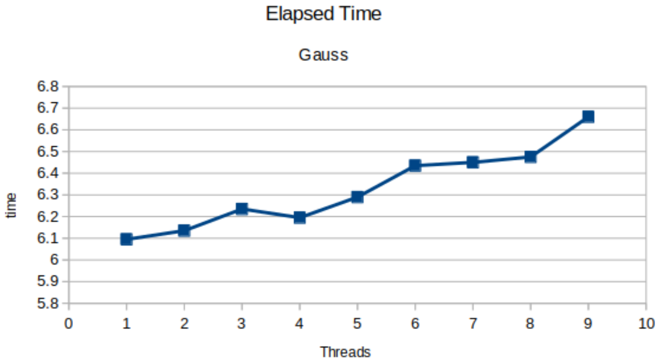
To parallelize the gauss algorithm we must use ordered clausure. It indicate a block of code that has to be executed sequentially, additionally you can specify a number of variables as a dependency of that execution.

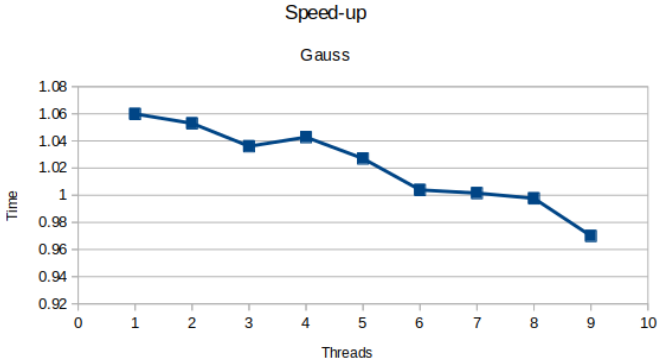
Using that principle the resulting code is:

```
double relax_gauss (double *u, unsigned sizex, unsigned sizey)
{
  double unew, diff, sum=0.0;
  int chunkx = sizex/omp_get_num_threads();
  int chunky = sizey/omp_get_num_threads();
  int howmany=4;
  #pragma omp parallel for reduction(+:sum) ordered(2)
    for(int bx = 0; bx < sizex/chunkx; ++bx){
      for(int by = 0; by < sizey/chunky; by++){
        int i_start = bx*chunkx;
        int i_end = chunkx*(1+bx);
        int j_start = by*chunky;
        int j_end = chunky*(1+by);
        #pragma omp ordered depend(sink:bx,by-1) depend(sink:bx-1 by)
        {
          for (int i=max(1, i_start); i<= min(sizex-2, i_end); i++) {
          for (int j=max(1, j_start); j<= min(sizey-2, j_end); j++) {
            unew= 0.25 * ( u[ i*sizey + (j-1) ]+    // left
                           u[ i*sizey + (j+1) ]+    // right
                           u[ (i-1)*sizey + j ]+    // top
                           u[ (i+1)*sizey j ]);     // bottom
            diff = unew - u[i*sizey+ j];
            sum += diff * diff;
            u[i*sizey+j]=unew;
          }
        }
      }
    }
  }
  return sum;
}
```

solver-omp.c

The result of the execution of that code





Optional: alternative parallel version for Gauss-Seidel using #pragma omp task and task dependences

Conclusions