# Blockchains & Distributed Ledgers

Lecture 06

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#### Permissionless Protocols

- Bitcoin and similar PoW-based blockchain protocols operate in the permissionless setting:
  - Anyone can participate in the protocol and receive BTC as rewards by performing the PoWbased mining operation
  - Parties can come and go as they wish no permission is required.
- Minting new coins (via PoW) makes it feasible for anyone (possessing sufficient hashing power) to participate
- The ledger itself is public, readable and writeable by anyone
  - read (retrieve ledger information): connect to the network and download the ledger
  - write (insert new information to the ledger): obtain some bitcoins and create a transaction

#### Sybil resilience:

 Relies on computational power: it doesn't matter how many relays/nodes the adversary controls – what matters is its computational power.

## Dynamic Availability

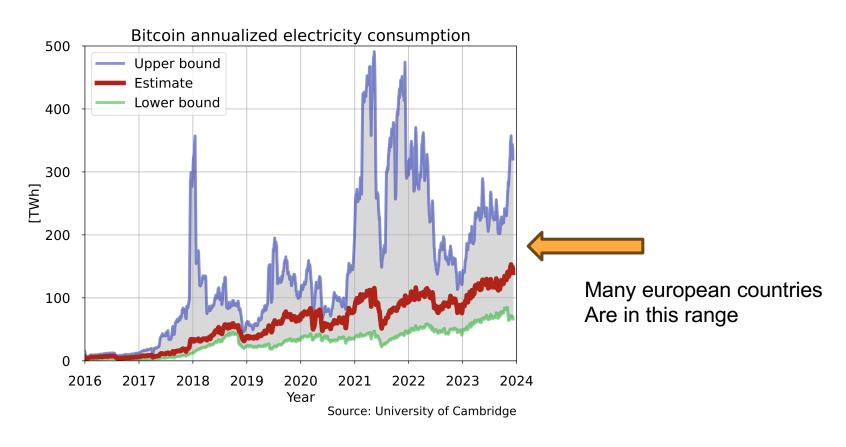
- Parties join and leave at will
- Need to bootstrap a chain when (re)joining):
  - Bitcoin's "longest chain rule" (most difficult chain)
- Number of online/offline parties changes over time
  - Analysis must account for that
- No a priori knowledge of participation levels
- Unannounced disappearance

Classic BFT protocols do not operate under general dynamic availability

## Bitcoin's Energy Problem

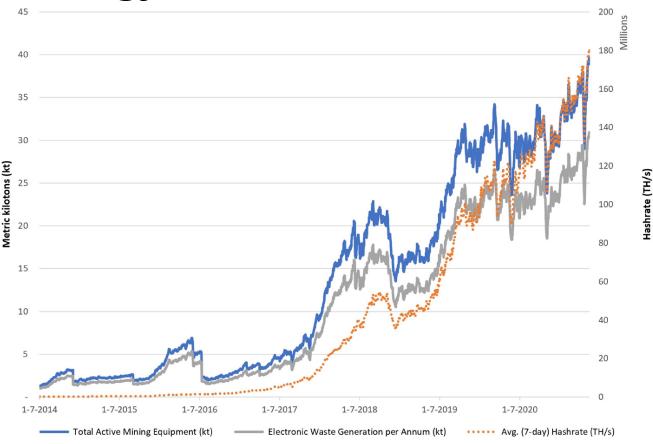
- Bitcoin resolves dynamic availability via PoW
  - Parties have limited access to a resource (computational power)
  - They repeatedly try to solve cryptographic puzzles (hashes)
  - A puzzle solution allows to create a block and append it to the chain
- Bitcoin is energy inefficient
  - The resource employed is physical (is this protocol the best use of it?)
  - The hash-based lottery consumes energy to ensure the protocol's security
    - An energy arms race between the good guys and the (potential) bad guys
  - Bitcoin presumes that it is under attack at all times

## Bitcoin's Energy Problem - electricity consumption



https://en.wikipedia.org/wiki/Environmental\_impact\_of\_bitcoin

## Bitcoin's Energy Problem - electronic waste



https://en.wikipedia.org/wiki/Environmental impact of bitcoin

## Bitcoin's Energy Problem - "digital crude"

#### Between 2016-2021:

- per coin climate damages from BTC were increasing, rather than decreasing as the industry matured
- during certain time periods, BTC climate damages exceed the price of each coin created
- on average, each \$1 in BTC market value created was responsible for \$0.35
   in global climate damages
  - between beef production and crude oil burned as gasoline
  - an order-of-magnitude higher than wind and solar power

Benjamin A. Jones, Andrew L. Goodkind & Robert P. Berrens.

Economic estimation of Bitcoin mining's climate damages demonstrates

closer resemblance to digital crude than digital gold (2022)

## Proof-of-Stake (PoS)

#### The time slot

- Time is continuous
- Protocol breaks time in slots
  - Defines a "slot length" parameter (in seconds)
- Slot large enough
  - E.g., if network is assumed synchronous, slot length depends on graph's diameter, s.t. all
    parties receive a message within a time slot
- Slot not too large
  - Otherwise protocol is slow
  - E.g., in Bitcoin waiting until tx is published is 10 mins (until a block is created) or more (for safety, k blocks are needed)
- Parties act based on the time slot they are in
  - Requires synchronized clock

## Proof-of-Stake (PoS)

- Sybil resilience depends on "stake"
  - Stake: the amount of digital assets (tokens) a party controls
  - Akin to computational power in PoW, but stake is digital
  - Energy efficient: no need to consume high amounts of energy to run the stake-based lottery
- Parties produce blocks proportionally to the stake they control
  - Smallest rate: linearly proportional
- Assumption: Adversary does not control a stake majority
  - Corrupted parties control, on aggregate, less stake than the honest parties

#### Two broad categories:

- Nakamoto-style
- BFT-style

#### From PoW to PoS, Nakamoto style

#### The setting:

- The number of all assets is known
  - Tokens are recorded on the ledger
- The public key that controls each asset is known
  - o Stake transfers (e.g., payments) are recorded on the ledger
- One block should be created per slot

#### High level idea:

- At each slot, choose one of the assets at random
  - Relaxation: choose a very small number of assets at random
- The owner of the chosen asset is eligible to produce a block at that slot
  - Owner: the person with the private key that owns the asset

## PoS setting

- Assume (for now) that stake does not change hands
  - There are no changes in stake ownership
  - The initial set of stake owners is known (e.g., hardcoded in the genesis block)
- Let n be a node
  - $\circ$   $vk_n$ : the public key of n
  - stake<sub>n</sub>: the stake owned by n
  - Both vk<sub>n</sub> and stake<sub>n</sub> are known by all parties

#### Recall PoW

H: hash function

o ctr: PoW counter

o x: MTR of block's transactions

s: hash of previous block's header

T: difficulty threshold

- Require:  $H(x, s, vk_n) < T \cdot stake_n$ 
  - 1. threshold is proportional to stake of each party (right side of inequality)

- Require: H(x, s, vk<sub>n</sub>) < T · stake-factor<sub>n</sub>
  - 1. threshold is proportional to stake of each party (right side of inequality)

#### Grinding Attack on x:

• Attacker can try different x's (e.g., transaction MTRs) to find one that satisfies the inequality

- Require: H(s, vk<sub>n</sub>) < T · stake-factor<sub>n</sub>
  - 1. threshold is proportional to stake of each party (right side of inequality)
  - 2. inequality's left side does not depend on input x (to prevent grinding)

- Require: H(s, vk<sub>n</sub>) < T · stake-factor<sub>n</sub>
  - 1. threshold is proportional to stake of each party (right side of inequality)
  - 2. inequality's left side does not depend on MTR (to prevent grinding)

#### Stalling Hazard:

• With some probability (depending on T), no vk will satisfy the equation  $\rightarrow$  No block is created at that slot  $\rightarrow$  No parameter in the inequality changes  $\rightarrow$  The protocol stalls

- Require: H(s, vk<sub>n</sub>, ts) < T · stake-factor<sub>n</sub>
  - 1. threshold is proportional to stake of each party (right side of inequality)
  - 2. inequality's left side does not depend on MTR (to prevent grinding)
  - 3. ts (e.g., timestamp) changes as slots change (to prevent stalling)

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#### Content Malleability:

 Block's content (transactions) not represented in the header anymore → Attacker can alter the previous blocks' transactions without altering the headers (which are validated in the PoS mechanism)

- Require: H(s, vk<sub>n</sub>, ts) < T · stake-factor<sub>n</sub>
  - 1. threshold is proportional to stake of each party (right side of inequality)
  - 2. inequality's left side does not depend on MTR (to prevent grinding)
  - 3. ts (e.g., timestamp) changes as slots change (to prevent stalling)
  - 4. Use the signing key for vk<sub>n</sub> to sign each payload (to prevent content malleability)

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#### **Posterior Corruptions:**

 Attacker can corrupt parties after the slot passes when they create a block → Attacker can change part (or all) of the chain's history (costless simulation)

- Require: H(s, vk<sub>n</sub>, ts) < T · stake-factor<sub>n</sub>
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  - 5. Key Evolving Signatures (KES) (to prevent posterior corruptions)
    - Parties refresh their keys comtinuously (delete old keys, create new keys linked with old ones)

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#### Adaptive attack:

vk that satisfies inequality is publicly known before the time slot starts → Attacker can predict
the slot "leader schedule" → Can corrupt a party that is known to be leader of a specific future
slot

- Require: VRF(sk<sub>n</sub>, s || ts) < T · stake-factor<sub>n</sub>
  - 1. threshold is proportional to stake of each party (right side of inequality)
  - 2. inequality's left side does not depend on MTR (to prevent grinding)
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  - 5. Key Evolving Signatures (KES) (to prevent posterior corruptions)
    - Parties refresh their keys comtinuously (delete old keys, create new keys linked with old ones)
  - 6. Verifiable Random Function (VRF) (to prevent adaptive corruptions)
    - Intuition: a party runs the inequality using its secret key
    - The VRF output is verifiable *publicly* (i.e., with the party's public key)

## Dynamic Stake

- Stake changes hands via payments/transfers
  - New stakeholders (i.e., keys) are added
  - The stake of old stakeholders is reduced.
- Stake ownership distribution depends on the chain (i.e., branch)
  - Different blocks (in different chains) will contain different transactions

## Key Grinding Attack

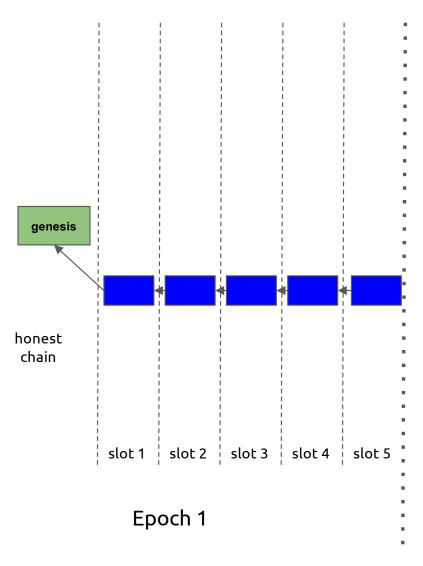
- Each user's key is created locally (by the user)
- Creating keys is (effectively) costless
- The adversary may be able to play multiple possible VRF calculations "in its head" prior to committing to a particular key.

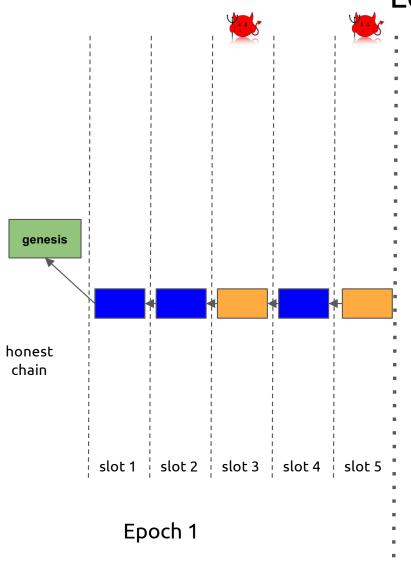
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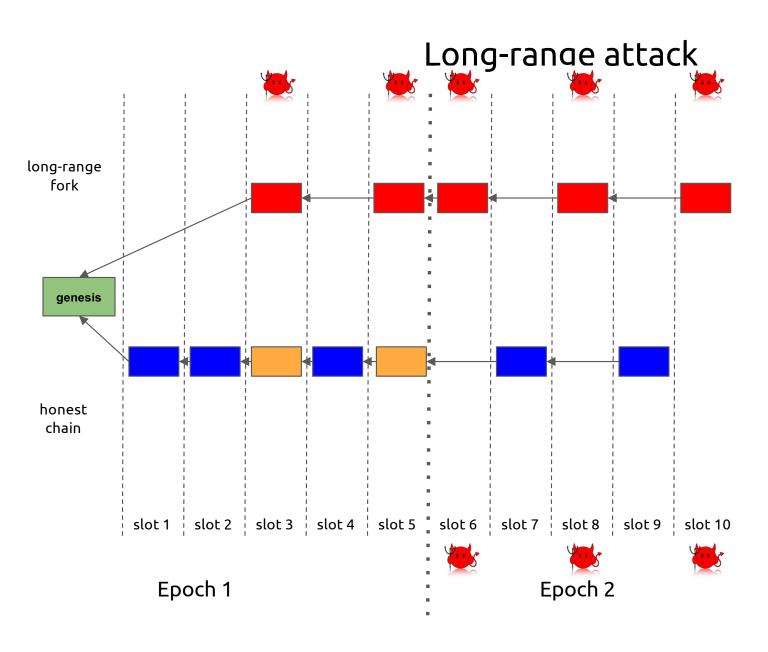
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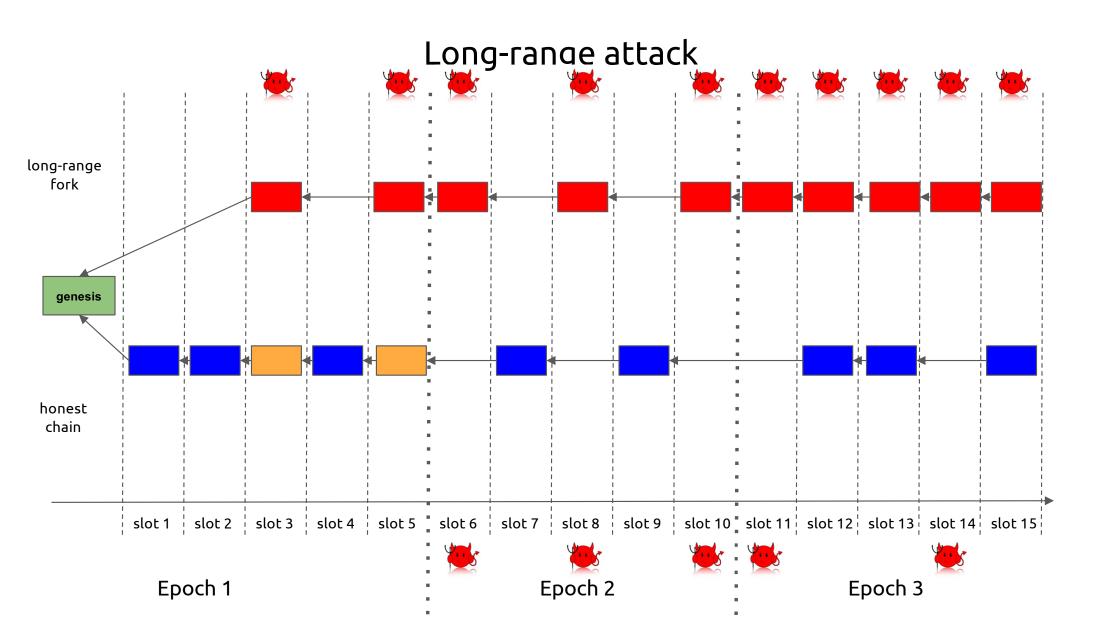
#### Solutions:

- Have all parties commit to their keys
- Generate randomness to include into the VRF calculation.
  - Key point: hashing a prior VRF value sequence may suffice!
- Time is divided into epochs: each epoch has its own stakeholder distribution and randomness.







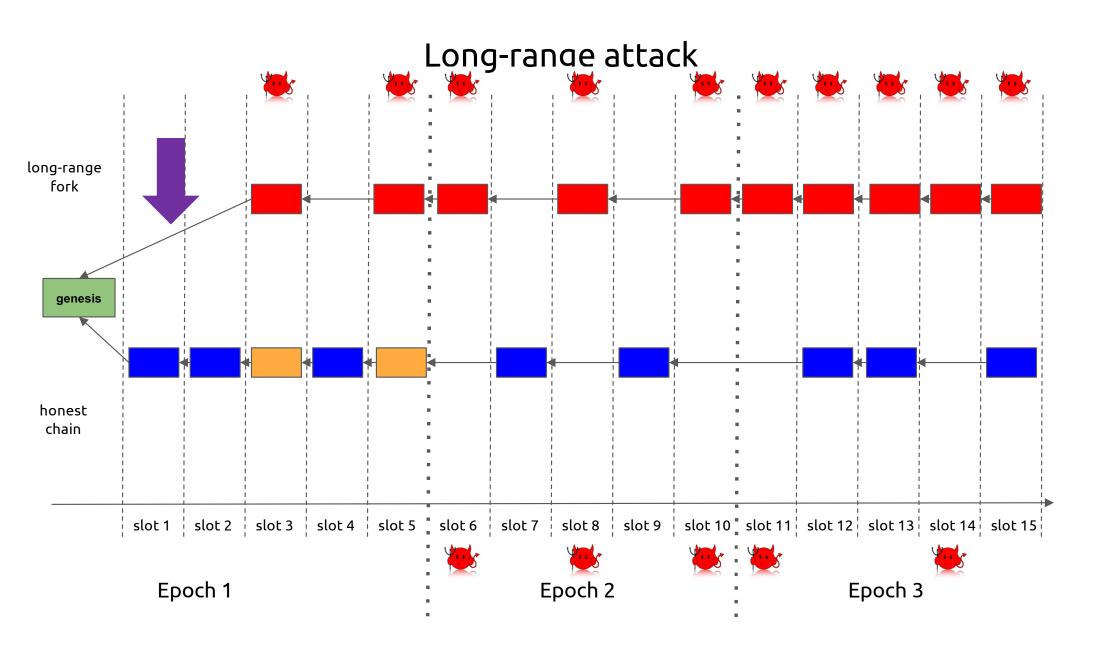


#### The attack:

- Starting from an old block, the attacker creates a chain of adversarial-only blocks
- In this chain, it collects the rewards for every block
  - In this branch/"fork", the attacker's stake is increased
- After some point, the attacker gets stake majority in this fork
- Because of costless simulation, the attacker can create an arbitrarily long chain in "its head"
  - The adversary can easily confuse a freshly joining party

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- Solution#1: checkpointing
  - Joining parties receive trusted checkpoint

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  - Because of costless simulation, the attacker can create an arbitrarily long chain in "its head"
- Solution#1: checkpointing
- Solution#2: chain density
  - Basic idea: immediately after the fork, the honest chain's blocks are more "dense" compared to the attacker's (forked) chain
  - A new node that joins the system, chooses a path at each fork by following the most dense branch
  - The idea behind Ouroboros Genesis



# Permissioned Ledgers

### Permissioned Protocols

- Participation is restricted:
  - Producing transactions and/or blocks can only be performed after being authorized by (some)
     other nodes
- In the simplest case, the set of nodes is static:
  - the set of participating nodes is fixed and determined at the onset of protocol's execution

### Permissioning How-To

- Most straightforward approach:
  - employ a PKI (Public-Key Infrastructure)
- Use digital signatures / authentication protocols
- Certificate authorities can authorize other entities
  - o authorization includes a signature from the CA on the entity's public-key, identity info etc
  - example: TLS/SSL
- Sharing certificate authority information is necessary
  - All computer systems come with preloaded certificates from certificate authorities a setup assumption
- Certificates need to be revoked in case the corresponding secret keys become exposed or the algorithms used are not safe anymore

### X.509 Certificates

- Internet standard since 1988
  - o <a href="http://www.ietf.org/rfc/rfc3280.txt">http://www.ietf.org/rfc/rfc3280.txt</a>
- Hierarchical

Version
Serial Number
Algorithm / Parameters
Issuer
Period of Validity: not before date not after date
Subject
Algorithm/ Parameters/ Key
x509v3 extensions
Signature

X.509
does not
specify
cryptographic
algorithms

### Digital Signatures and Certificates

- A certificate contains a digital signature
- Cryptographic design of digital signatures involves typically:
  - A cryptographic signing operation that acts on a fixed input of a specific type and has a publicverifiability feature
  - A cryptographic hash function that takes arbitrary strings and maps them to the data type suitable for the signing operation
  - Common setting today: SHA2 with RSA or DSA

### Secure channels and certificates

- Possession of mutually acceptable certificates:
  - o permits authenticated communication (exchanging signed mechanism between two entities)
  - allows building a secure channel
- TLS 1.3 can be used to build such secure channel:
  - Based on cryptographic protocols like Diffie-Hellman key exchange
  - Data confidentiality ensured

### Static Permissioned Ledger

- Prior to system's start:
  - the nodes register their certificates
  - these certificates are included in the genesis block
- Using these certificates, all nodes are capable of:
  - authenticating each participant
  - o allowing interaction with the shared state, in a way prescribed by the participants' credentials
- The set of participants remains the same throughout the execution
- This is the simplest form of a PKI / public-key directory
- [Compare this to PoS protocols]

### A Centralised Permissioned Ledger

- Assume just a "LOG" of transactions
- One of the participants acts as a server and maintains the LOG
- Readers and writers to the LOG authenticate with the server and can perform read and write operations
- Consistency of the LOG is guaranteed, assuming the server is trusted
- Liveness of the LOG is guaranteed, assuming the server is trusted and functional
- If server is corrupted, the ledger is compromised
- Sometimes referred to as Proof of Authority, PoA

### Comparison to Bitcoin's Permissionless Ledger

- The genesis block contains no certificate information
- Reading from the LOG is open
  - anyone can do it, without credentials
- Writing to the LOG requires a specific type of credentials
  - write: insert data into the log
  - Nodes can obtain valid credentials (accounts) by generating a public and secret-key and:
    - mine a block (and be rewarded with BTC) or
    - buy BTC from another node
- Once the LOG records their account credit, they can issue transactions (and pay the necessary fees)
- In essence: crediting a bitcoin account is akin to creating a certificate that imparts the account holder with certain permissions w.r.t. the ledger

### Distributed Permissioned Ledger

- A number of servers maintain the ledger (LOG) individually
- All share the same genesis block that identifies all participants
- Assuming a synchronous operation, at each round, readers and writers:
  - authenticate with the servers
  - interact with the LOG in a prescribed fashion

# Distributed Permissioned Ledger

- A number of servers maintain the ledger (LOG) individually
- All share the same genesis block that identifies all participants
- Assuming a synchronous operation, at each round, readers and writers:
  - authenticate with the servers
  - interact with the LOG in a prescribed fashion
- Readers authenticate to each server and obtain read access
- Writers authenticate to each server and provide their inputs
- Servers run a consensus protocol to agree what inputs should be included in the LOG

### Read Requests

- Is it possible to restrict read requests, as in the centralized setting?
  - Hint: Nodes keep blocks of transactions private and issue them only to authenticated users
- TLS can be used to build a secure channel between the reader and the responding node
- Requirement that all servers remain honest (as they all share the LOG)
- Is is possible to impose read restrictions on servers as well?
  - Hint: Threshold signatures

# Reader/Writer Management

- Readers and writers can authenticate to each server referring to the information in the genesis block
- It is possible to introduce additional readers and writers by suitably issuing certificates to other users
- Note that each participant would then need to show a valid certificate chain,
   that establishes their privileges for the requested read or write access

# BFT Protocol Example

### "Classical" BFT Consensus (example)

- Focus on write requests: we want to ensure LOG liveness and consistency
- We will build a "byzantine fault tolerant" (BFT) agreement protocol that uses two important tools:
  - a graded broadcast
  - a binary consensus protocol

### **Graded Consensus**

- Parties involved :
  - a single sender
  - several receivers
- The i-th receiver outputs  $(M_i, G_i)$ 
  - *M<sub>i</sub>*: the output message
  - $G_i \in \{0, 1, 2\}$ : the grade of the message

#### **Properties**

- If the sender is **honest**, then  $M_i = M_j$  for all i, j and  $G_i = 2$
- If the sender is malicious and one receiver outputs (M, 2), then all other honest receivers output (M, G<sub>i</sub>) with G<sub>i</sub> ∈ {1, 2}

### Graded Broadcast Protocol

#### **Communication**

- Round 1. The sender sends the message *M* to all receivers
- Round 2. The *i*-th receiver, who obtained  $M_{1,i}$  in round 1, sends it to all receivers
- Round 3. The *i*-th receiver, who obtained  $M_{2,j,i}$  from the *j*-th receiver in round 2:
  - o if there is a single message that was sent by at least 2n/3 receivers, it sends it to all receivers
  - else does nothing

### Graded Broadcast Protocol

#### **Communication rounds**

- 1. The sender sends the message *M* to all receivers
- 2. The *i*-th receiver, who obtained  $M_{1,i}$  in round 1, sends it to all receivers
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  - o if there is a single message that was sent by at least 2n/3 receivers, it sends it to all receivers
  - else does nothing

#### **Output Generation**

The honest *i*-th receiver does the following:

- If a single message was received from at least 2n/3 receivers in round 3, output that message as  $M_i$  and set  $G_i = 2$
- If a single message was received from at least n/3 receivers in round 3, output that message as  $M_i$  and set  $G_i = 1$
- In any other case, output *fail* as  $M_i$  and set  $G_i = 0$

# Graded Broadcast Protocol (Analysis: t < n/3)

#### Theorem #1

If the sender is honest and broadcasts M, then all honest receivers  $P_i$  will output  $G_i = 2$  and M in the output generation stage.

#### **Proof**

- If the sender is honest, then all honest receivers will receive the same message M in round 1.
- Since t < n/3, each receiver will receive M at least 2n/3 times in rounds 2 and 3 (from the honest parties).

#### **Communication rounds**

- 1. The sender sends the message *M* to all receivers
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• If a single message was received from at least 2n/3 receivers in round 3, outputs that message as  $M_i$  and set  $G_i = 2$ 

# Graded Broadcast Protocol (Analysis: t < n/3)

#### Lemma #1

If two honest receivers send a message in round 3, it *must be* the same.

#### **Proof**

Suppose an honest party P sends message *M* in round 3:

- 1. P has received *M* by at least 2n/3 parties in round 2 (by definition)
- 2. Let **h** be the number of *honest parties* that sent M in round 2:  $h \ge (2n/3) t > n/3$  (by assumption)
- 3. Let **p** be the parties *capable* of sending a *different* message *M*′ ≠ *M* in round 2: p = n h < 2n/3 (by step 2, i.e., since h honest parties sent M)
- 4. Therefore, any other honest party in round 3 will send *M* or do nothing

#### **Communication rounds**

- 1. The sender sends the message *M* to all receivers
- 2. The *i*-th receiver, who obtained  $M_{1,i}$  in round 1, sends it to all receivers
- 3. The *i*-th receiver, who obtained  $M_{2,j,i}$  from the *j*-th receiver in round 2:
  - if there is a single message that was sent by at least 2n/3 receivers, it sends it to all receivers
  - else does nothing

# Graded Broadcast Protocol (Analysis: t < n/3)

#### Theorem #2

Suppose the i-th receiver returns  $G_i$  = 2 and a message  $M_i$ ; for the j-th honest receiver's output  $(M_j, G_j)$ , it holds  $M_i = M_j$ ,  $G_i \in \{1, 2\}$ .

#### **Proof**

First, we show that it cannot be that  $M_i = fail$ :

- 1. The i-th party received  $M_i$  from at least 2n/3 receivers in round 3 (of which at most t<n/3 adversarial)
- 2. So, more than n/3 honest parties sent  $M_i$  in round 3 Now, suppose  $M_i \neq M_i$ :
  - 1. M<sub>j</sub> was sent by at least n/3 receivers in round 3 (by definition)
  - 2. At least one of them is honest (since t < n/3)
  - 3. By Lemma #1, it holds  $M_i = M_i$  [contradiction]

#### **Communication**

Round 3. The *i*-th receiver, who obtained  $M_{2,j,i}$  from the *j*-th receiver in round 2:

• if a single message was sent by at least 2n/3 receivers, send it to all receivers

#### **Output Generation**

The honest *i*-th receiver:

- If a single message was received from at least 2n/3 receivers in round 3, outputs that message as  $M_i$  and set  $G_i = 2$
- If a single message was received from at least n/3 receivers in round 3, output that message as M<sub>i</sub> and set G<sub>i</sub> = 1
- In any other case, output fail as M<sub>i</sub> and set G<sub>i</sub> = 0

### From Graded Broadcast to a BFT-Ledger

If grade  $G_i = 2$ , party  $P_i$  knows that other honest parties have received  $M_i$ 

Graded broadcast is not enough:

• If grade  $G_i = 1$ , party  $P_i$  cannot know if other honest parties received the message

#### Solution:

Perform binary consensus to detect whether everyone has grade 2 or not.

### From Graded Broadcast to a BFT-Ledger

#### A simple approach:

- execute n/3 phases (to guarantee at least one honest sender encountered)
- in each phase:
  - A designated sender organizes all valid transactions as M and performs a graded broadcast
  - A binary consensus protocol determines whether everyone's grade is 2 or not:
    - If true, each node signs the output to generate a public endorsement and appends *M* to their LOG (together with the signatures)
    - otherwise, LOG remains the same

### Byzantine Binary Consensus

- (RECALL) n parties, t adversarial
- $v_i \in \{0, 1\}$  the input of party i
- Honest parties should decide on values u<sub>i</sub> ∈ {0, 1} satisfying the following properties:
  - Termination: values u<sub>i</sub> are well defined for all honest parties
  - o **Agreement**: if parties i and j are honest, then  $u_i = u_j$
  - **Validity**: if, for every honest party i, there exists  $v \in \{0, 1\}$  such that  $v_i = v$ , then each honest party i outputs  $u_i = v$

Note: We examine the synchronous setting

# Exponential Information Gathering Algorithm (EIG)

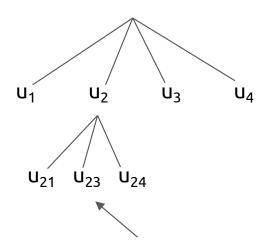
#### Algorithm Sketch:

- At round 1, send everyone your input
- At round r+1, send everyone all messages you received at round r (avoiding redundant messages – see below)

#### Each party arranges the messages in its own EIG tree:

- Let u<sub>1</sub>,...,u<sub>n</sub> be the messages received in the first round (including own message)
- $u_{i1i2...ik}$  is a value v s.t. ( $i_k$  told i) that ( $i_{k-1}$  told  $i_k$ ) that ... that ( $i_1$  told  $i_2$ ) that  $i_1$ 's initial value was v

(Food for thought) What is the size of the tree?



u<sub>23</sub>: The value party 3 told me that party 2 sent them in the previous round.

### **EIG Termination**

The EIG algorithm terminates after t+1 rounds. The output value of each party is defined as follows:

- For each leaf v in the EIG tree, set z<sub>v</sub>=u<sub>v</sub>
- For an internal node v, set  $z_v$  equal to the majority of the z-values of its children; if the majority is not defined, set  $z_v$ =0 (without loss of generality)
- Define the output as z<sub>root</sub>

(Food for thought) Prove that EIG satisfies: i) agreement; ii) validity. (Hint)

# Impossibility results - asynchronous setting

- Theorem [LSP1982]: Impossible for n < 3t + 1.
- Theorem [FL1982]: Impossible in t rounds.
  - Example: The EIG algorithm with t = 1 needs at least 2 rounds:
    - If a party received a single 1, its output should be 0. (Because the 1 could be coming from the adversary.)
    - If a party received two 1s, its output should be 0. (Because one of them could have been sent from the adversary, while another party could have received a single 1 and will decide 0 according to the previous statement.)
    - And so on... (by induction, the output will always be 0, contradicting validity)
- Theorem[GM1998]: Doable for n > 3t in t + 1 rounds.
- Theorem [DS83]: Doable for n > 2t assuming a PKI.

# Impossibility results - asynchronous setting

- Theorem [BT1985]: Asynchronous Byzantine Consensus is impossible with n < 3t + 1, even if the parties have agreed on a PKI (setup).</li>
  - Partition parties into sets A, B, C of size at most t and consider 3 scenarios:
    - A malicious, B and C honest with inputs 0. The adversary sends no messages. The honest parties should decide on 0 until some time T<sub>A</sub>.
    - ii. B malicious, A and C honest with inputs 1. The adversary sends no messages. The honest parties should decide on 1 until some time T<sub>B</sub>.
    - iii. C malicious, B and A honest with inputs 0 and 1 respectively. The adversary communicates with B as the honest C in scenario A and with A as the honest C in scenario B. At the same time every communication between A and B is delayed for time at least max{T<sub>A</sub>, T<sub>B</sub>}.
  - The crux is that A has the same view in scenarios B and C. Similarly for B, in scenarios A and
     C. Agreement in scenario C is impossible, if validity is achieved in scenarios A and B.

### Back to PoS

• ... using ideas from BFT protocols

### BFT-style PoS

#### High level idea:

- At each slot, subselect a committee of stakeholders
  - Getting elected to the committee is proportional to the party's owned stake
- The committee runs a BFT protocol to agree on the new block
- Each block is finalized per the BFT protocol rules
- The idea behind <u>Algorand</u>

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#### Some security considerations:

- Where does the randomness come from (for the committee selection)?
- How to prevent grinding attacks?
- How to prevent adaptive corruptions?
- How to prevent long-range attacks?

### Food for thought in Ledger protocols

- How to ensure that parties have a synchronised clock?
  - How do parties coordinate in terms of the time progress?
  - How do parties agree on which time slot is active at any point in time?
  - Reference: <u>Ouroboros Chronos</u> (PoS-based), <u>Permissionless Clock Synchronization</u> (PoW-based)
- Will rational parties delete their keys?
  - Key erasures (in KES) are necessary to prevent posterior attacks.
  - Do parties get any benefit by not deleting their keys? Can an attacker incentivize this?
  - Can the protocol provide incentives (or counter incentives) to promote key erasure?
    - "economic security"
- What happens if an attacker gets a majority during one epoch?
  - Can the system recover from temporary adversarial majority?
  - Can PoW systems recover (without "social consensus")? What about PoS?
  - Reference: <u>Self-healing blockchains</u>