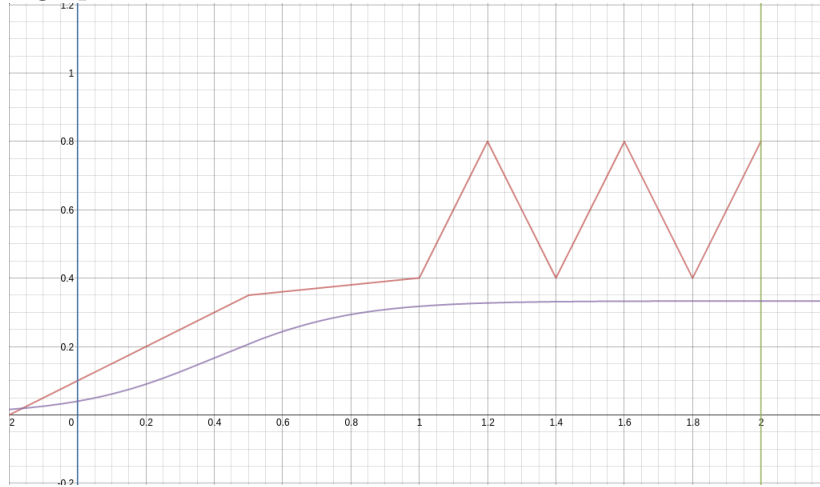


3D printer nozzle for 3 mm diameter filament with a rough approximation of screw threading  
Used *Ti-nspire* to solve integrals, and Wolfram Alpha when my calculator was out of arm's reach

1 graph unit = 1 cm



$$y = x < 0.5 : 0.5x + 0.1, x < 1 : 0.1x + 0.3, x < 2 : \frac{2}{5\pi} \cdot \arcsin\left(\sin\left(4\pi \cdot x - \frac{3\pi}{2}\right)\right) + 0.6$$

$$y = \frac{1}{3(1+e^{-(5x-2)})}$$

Area under piecewise function:

$$\int_0^{0.5} \frac{1}{2}x + \frac{1}{10} dx = 0.1125$$

$$\int_{0.5}^1 \frac{1}{10}x + \frac{3}{10} dx = 0.1875$$

$$\int_1^2 \frac{2}{5\pi} \arcsin\left(\sin\left(4\pi \cdot x - \frac{3\pi}{2}\right)\right) + 0.6 dx = 0.6$$

Total: 0.9

Area under sigmoid function:

$$A(x) = \int \frac{1}{3(1+e^{-(5x-2)})} = \frac{1}{15} \cdot \ln(e^{5x} + e^2)$$

$$A(x)|_0^2 = \frac{1}{15} \cdot \ln(e^{10} + e^2) - \frac{1}{15} \cdot \ln(e^0 + e^2)$$

$$= \frac{1}{15} \cdot (2 - \ln(1 + e^2) + \ln(1 + e^8))$$

$$\approx 0.525$$

Area between functions:

$$0.375$$

Volume:

$$\int_0^{0.5} 2\pi((0.5x + 0.1) - (\frac{1}{3(1+e^{-(5x-2)})})) dx$$

$$\approx 0.352$$

$$\int_{0.5}^1 2\pi((0.1x + 0.3) - (\frac{1}{3(1+e^{-(5x-2)})})) dx$$

$$\approx 0.309$$

$$\int_1^2 2\pi((\frac{2}{5\pi} \cdot \arcsin(\sin(4\pi \cdot x - \frac{3\pi}{2})) + 0.6) - \frac{1}{3(1+e^{-(5x-2)})}) dx$$

$$\approx 1.70$$

$$\text{Total} = 0.352 + 0.309 + 1.7 = 2.361\text{cm}^3$$

Use for shape: Nozzle for 3D printer hotends; attaches to heater block and melts a filament of plastic 3mm in diameter and extrudes it at 0.4mm.

Material of choice: Brass.

Density of brass:  $8.7 \text{ g/cm}^3$

Total weight of object:  $8.7 * 2.361 = 20.5407g$

Sketch: