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Note sheet: FTC 1: if f is contonuous on [a, b], then the function g defined by
g(x) = \int_{a}^{x} f(t) dt
                                   a \le x \le b
is an antiderivitive of f, that is, g'(x) = f(x) for a < x < b
Substitution Rule:
 \int f(g(x))g'(x) dx = \int f(u) du
 \int x^3 \cos(x^4 + 2) dx
u = x^4 + 2
du = 4x^3 dx
 \frac{1}{4} du = x^3 dx
Integration by Parts:
\int f(x)g'(x) dx = f(x)g(x) - \int g(x)f'(x) dx
\int u \, \mathrm{d}v = uv - \int v \, \mathrm{d}u
 \int x \sin x \, dx
u = x, u' = 1
v = -\cos(x), v' = \sin(x)
= -x\cos(x) - \int -\cos(x) dx
= -x\cos(x) + \sin(x) + C
FTC 2:
F(x) = \int_a^x f(t) dt
Summation:
\Delta x = \frac{b-a}{N}
x_i = a + i\Delta x
\bar{x}_i = \frac{1}{2}(x_{i-1} + x_i)
R_n = \sum_{i=1}^{N} f(x_i) \cdot \Delta x
L_n = \sum_{i=0}^{N-1} f(x_i) \cdot \Delta x \ M_n = \sum_{i=1}^{N} f(\bar{x}_i) \Delta x
T_n = \frac{1}{2} (\sum_{i=1}^{N} (f(x_{i-1}) \Delta x) + \sum_{i=1}^{N} (f(x_i) \Delta x))
T_n = \frac{\Delta x}{2} [f(x_0) + 2f(x_1) + 2f(x_2) + \dots + 2f(x_{n-1}) + f(x_n)]
S_n = \frac{\Delta x}{3} [f(x_0) + 4f(x_1) + 2f(x_2) + 4f(x_3) + \dots + 2f(x_{n-2}) + 4f(x_{n-1}) + f(x_n)]
Error:
|f''(x)| \le K for a \le x \le b
|E_T| \le \frac{K(b-a)^3}{12N^2}
|E_M| \le \frac{K(b-a)^3}{24N^2}
|E_S| \le \frac{K(b-a)^5}{180N^4}
\sin x = \frac{1}{\csc x}, \cos x = \frac{1}{\sec x}, \csc x = \frac{1}{\sin x}, \sec x = \frac{1}{\cos x}, \cot x = \frac{1}{\tan x}
\sin^2 x = \cos^2 x = 1 + \tan^2 x = \sec^2 x + \cot^2 x = \csc^2 x
\tan x = \frac{\sin x}{\cos x}, \cot x = \frac{\cos x}{\sin x}
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