

Question 1.

Algorithm Algorithm_one()

Output: the max difference between two integers

Ints \leftarrow new Array[1000]	2
n \leftarrow ints.length	2
count \leftarrow 0	1
for i \leftarrow 0 to n do	n + 2
Ints[i] \leftarrow Math.Random	2(n + 1)
if ints[i] % 2 = 0 then	2(n + 1)
increment count	2(n + 1)
evenNymbers \leftarrow new int[count]	2
j \leftarrow 0	1
for i \leftarrow 0 to n do	n + 1
if ints[i] % 2 = 0 then	2(n + 1)
evenNumbers[j] \leftarrow ints[i]	2(n + 1)
increment j	2(n + 1)
max \leftarrow 0	1
n \leftarrow evenNumbers.length	2
for i \leftarrow 0 to n do	n + 2
for j \leftarrow 0 to n do	n ² + 2
k \leftarrow eventNumber[i] - eventNumber[j]	(n ² + 2) * 4
if k > max	(n ² + 2) * 4
max \leftarrow k	(n ² + 2) * 4
 return k	 1

$$13n^2 + 15n + 55 \rightarrow O(n^2)$$

Algorithm Algorithm_Two ()

Output: the max difference between two integers

We have a helper static method RandomNumber to generate a Random Number and return an Array with the Randomly generated numbers.

Ints \leftarrow new Array[1000]	2
ints \leftarrow RandomNumber	n
n \leftarrow ints.length	2
max \leftarrow 0;	1
for i \leftarrow 0 to n-1 do	n + 1
if ints[i]%2=0 then	2(n)
for j \leftarrow i to n-1 do	2(n ²)
if ints[j]%2=0 then	2(n ² -1)
k \leftarrow ints[i] – ints[j]	2(n ² -1)
if max<k then	2(n ² -1)
max \leftarrow k	2(n ² -1)
Return max	1

$$10n^2 + 4n - 1 \text{ ---- } O(n^2)$$

Algorithm Algorithm_Three ()

Output: the max difference between two integers

We have a helper static method RandomNumber to generate a Random Number and return an Array with the Randomly generated numbers. And assuming the min a number can be is -1000 and max a number can be is 1000.

ints \leftarrow new Array[1000]	2
ints \leftarrow RandomNumber	n
n \leftarrow ints.length	2
max \leftarrow -1000	1
min \leftarrow 1000	1
for i \leftarrow 0 to n-1 do	n + 2
if ints[i] % 2 = 0 then	2n
if max < ints[i] then	2n
max \leftarrow ints[i]	2n
if min > ints[i] then	2n
min \leftarrow ints[i]	2n
Return max-min	1

$$12n + 9 \rightarrow O(n)$$

Question 2.

$10,1$	$\Theta(1)$
$\log n$	$\Theta \log n$
$(\log n)^2$	$\Theta(\log n)^2$
\ln	$\Theta(\ln)$
$n^{1/k} \quad k>3$	$\Theta(n^{1/3}) \quad k>3$
$n^{1/3}$	$\Theta n^{1/3}$
$n^{1/2}$	$\Theta n^{1/2}$
$n^{1/3} \log n$	$\Theta n^{1/3} \log n$
$n^{1/2} \log n$	$\Theta n^{1/2} \log n$
$n \log n$	$\Theta n \log n$
$\log n^n$	$\Theta \log n^n$
n^2	Θn^2
n^3	Θn^3
$n^k \quad k>3$	$\Theta n^k \quad k>3$
2^n	$\Theta 2^n$
3^n	$\Theta 3^n$
$n!$	$\Theta n!$
n^n	Θn^n