

# Proof-of-Importance

[https://youtu.be/B\\_k6pK6\\_rAo](https://youtu.be/B_k6pK6_rAo)

Pol (Proof-of-Importance)

Importance Score

Future Work

# Pol (Proof-of-Importance)

- NEM 암호화폐에서 사용하는 합의알고리즘 (XEM)
- PoS(Proof-of-Stake)의 단점을 해결하기 위하여 개발
- 기득 통화량, 코인 거래량, 노드 간 상호 연결도에 따라 채굴 확률이 증가한다.
- 즉, 네트워크 내 기여도에 따라서 달라지는 셈



- 채굴 과정

블록 생성 (블록 당 1분  $\pm 0.5s$ )

-> 계정의 중요도 점수 계산

-> 조건이 만족되었는지 확인  $\{hit < target$

-> 채굴 완료

# Pol (Proof-of-Importance)

$$hit = 2^{54} \left| \ln \left( \frac{h}{2^{256}} \right) \right|$$
$$target = 2^{64} \frac{b}{d} t$$

$$hit < target$$

$h = H(\text{generation hash of previous block, public key of account})$

interpreted as 256-bit integer

$t = \text{time in seconds since last block}$

$b = 8999999999 \cdot (\text{importance of the account})$

$d = \text{difficulty for new block}$

$$d = \frac{1}{n} \sum_{i=1}^n (\text{difficulty of block } i)$$

$$t = \frac{1}{n} \sum_{i=1}^n (\text{time to create block } i)$$

$$\text{difficulty} = d \frac{60}{t}$$

Initial difficulty =  $10^{14}$

# Importance Score

- Importance Score,  $\psi$

$$\psi = (\text{normalize}_1(\max(0, \nu + \sigma w_o)) + \hat{\pi} w_i) \chi,$$

**normalize**<sub>1</sub>( $v$ ) is:  $\frac{v}{\|v\|}$

$\nu$  is the vested amount of XEM

$\sigma$  is the weighted, net outlinking XEM

$\hat{\pi}$  is the NCDawareRank [10] score

$\chi$  is a weighting vector that considers the structural topology of the graph

$w_o, w_i$  are suitable constants

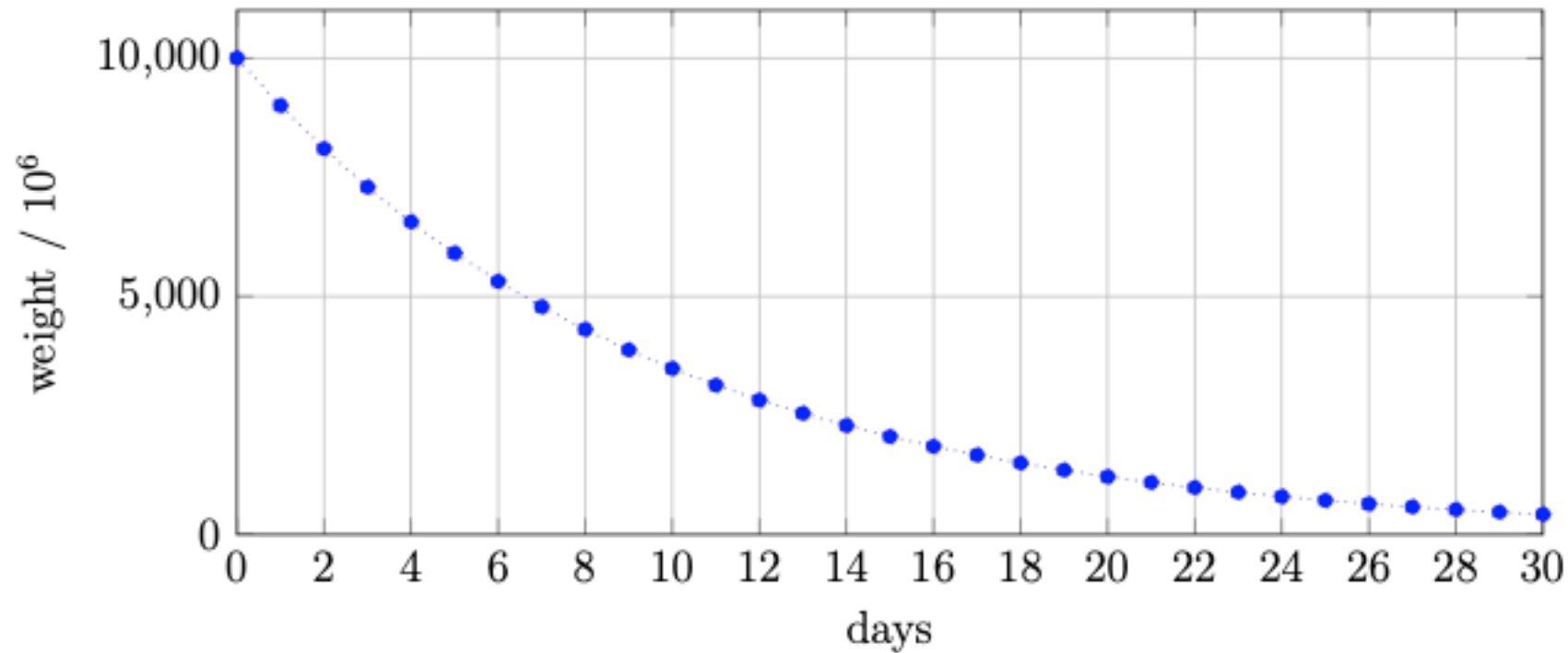
$w_o$  is 1.25 and  $w_i$  is 0.1337.

# Importance Score

1.  $\nu$  is the vested amount of XEM

매일 보유 XEM의 10%가 vested됨

\* harvester가 되기 위해선 총 10,000 XEM이 vested 되어야 함 \*



*Figure 8: amount decay of 10000 XEM*

# Importance Score

## 2. $\sigma$ is the weighted, net outlinking XEM

- Transferred an amount of at least 1,000 XEM
- Happened within the last 43,200 blocks (approximately 30 days)

### Block weight

$$w_{ijk} = amount \cdot \exp \left( \ln(0.9) \left[ \frac{h - h_{ijk}}{1440} \right] \right)$$

$$\tilde{w}_{ij} = \sum_k w_{ijk}$$

### Weighted net flow => outlink matrix

$$\tilde{o}_{ij} = \begin{cases} \tilde{w}_{ji} - \tilde{w}_{ij} & \text{if } \tilde{w}_{ji} - \tilde{w}_{ij} > 0 \\ 0 & \text{otherwise} \end{cases}$$
$$o_{ij} = \begin{cases} \frac{\tilde{o}_{ij}}{\sum_i \tilde{o}_{ij}} & \text{if } \sum_i \tilde{o}_{ij} > 0 \\ 0 & \text{otherwise} \end{cases}$$

i, j: account

h: block-height

k: k-th Transaction

# Importance Score

3.  $\hat{\pi}$  is the NCDawareRank [10] score

- PageRank와 유사
- PageRank에 inter-level proximity matrix와  $\mu$ 가 추가된 형태
- 그래프를 분해 가능한 구조로써 활용 가능



# Importance Score

3.  $\hat{\pi}$  is the NCDawareRank [10] score

$$\hat{\pi} = \mathbf{O}\eta\pi + \mathbf{M}\mu\pi + \mathbf{E}(1 - \eta - \mu)\pi$$

$\mathbf{O}$  is the outlink matrix

$\mathbf{M}$  is the inter-level proximity matrix

$\mathbf{E}$  is the teleportation matrix

$\pi$  is the NCDawareRank

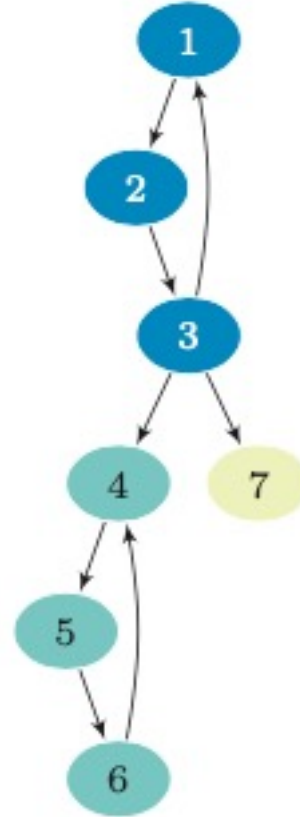
$\eta$  is the fraction of importance that is given via outlinks

$\mu$  is the fraction of importance given to proximal accounts ( $\eta$  is 0.7 and  $\mu$  is 0.1) in NEM

# Importance Score

- $\mathbf{M}$  is the inter-level proximity matrix

$$M_{v,u} \triangleq \begin{cases} \frac{1}{N_u |A_{(v)}|} & \text{if } v \in \chi_u \\ 0 & \text{otherwise} \end{cases}$$



$$\mathbf{M} = \begin{bmatrix} 1/3 & 1/3 & 1/3 & 0 & 0 & 0 & 0 \\ 1/3 & 1/3 & 1/3 & 0 & 0 & 0 & 0 \\ 1/9 & 1/9 & 1/9 & 1/9 & 1/9 & 1/9 & 1/3 \\ 0 & 0 & 0 & 1/3 & 1/3 & 1/3 & 0 \\ 0 & 0 & 0 & 1/3 & 1/3 & 1/3 & 0 \\ 0 & 0 & 0 & 1/3 & 1/3 & 1/3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

- $\mathbf{W}$  is set of all **harvesting-eligible accounts**.
- For  $u \in \mathbf{W}$ ,  $\mathbf{G}_u$  is the set of account that have received more in value transfers from account “u” than have sent “u”.
- **NCD (Nearly Completely Decomposable) blocks** of  $\mathbf{W}$  are defined as  $\{\mathbf{A}_1, \mathbf{A}_2, \mathbf{A}_3, \dots, \mathbf{A}_N\}$ .
- $\mathbf{X}_u$  is the **proximal accounts** of each “u”
- $\mathbf{N}_u$  is the **number of NCD blocks** in  $\mathbf{X}_u$ .

$$\chi_u \triangleq \bigcup_{w \in (u \cup \mathbf{G}_u)} A_{(w)}$$

# Importance Score

- Clustering the transaction graph

- $\Gamma$  is the **set cardinality** and the set of **structurally connected accounts** (inclusive of self)

$$\Gamma(u) = \{v \in V \mid \{u, v\} \in E\} \cup \{u\}$$

- $\sigma$  is the **similarity** between two accounts “u” and “v”

$$\sigma(u, v) = \frac{|\Gamma(u) \cap \Gamma(v)|}{\sqrt{|\Gamma(u)| |\Gamma(v)|}}$$

- $N_\epsilon(u)$  is the **set of structurally connected accounts** that have structural similarity with an account over a pre-determined threshold  $\epsilon$

$$N_\epsilon(u) = \{v \in \Gamma(u) \mid \sigma(u, v) \geq \epsilon\}$$

- $K_{\epsilon, \mu}(u)$  are **core nodes** that used for pivoting and expanding clusters

$$K_{\epsilon, \mu}(u) \Leftrightarrow |N_\epsilon(u)| \geq \mu$$

$\epsilon$  is 0.3 and  $\mu$  is 4

# Importance Score

- Direct structure reachability

$$u \mapsto_{\epsilon, \mu} v \Leftrightarrow K_{\epsilon, \mu}(u) \wedge v \in N_{\epsilon}(u)$$

- Account that are two-hops away from the pivot accounts

$$H(u) = \{v \in V \mid (u, v) \notin E \wedge (v, w) \in E\}$$

# Importance Score

- $\mathbf{E}$  is the teleportation matrix

$$\mathbf{E} \triangleq \mathbf{e}\mathbf{v}^T$$

- “ $\mathbf{e}$ ” is the vector with all components set to 1.
- “ $\mathbf{v}^T$ ” is a teleportation probability vector.

# Importance Score

$\pi$  is the NCDawareRank

$$NCDawareRank^r(i) = (1 - \eta - \mu) \frac{1}{|G|} + \\ \eta \sum_{k=1}^s o_{ik} NCDawareRank^{r-1}(k) + \\ \mu \sum_{k=1}^s m_{ik} NCDawareRank^{r-1}(k)$$

$$\left( \sum_{i \in G} \left| NCDawareRank^r(i) - NCDawareRank^{r-1}(i) \right| \right) < \varepsilon$$

# Future Work

$h = H(\text{generation hash of previous block, public key of account})$   
interpreted as 256-bit integer

$t = \text{time in seconds since last block}$

$b = 8999999999 \cdot (\text{importance of the account}) \rightarrow \text{Shapley Value}$

$d = \text{difficulty for new block}$

Q & A