Lepton flavour violation in τ decays at Belle II



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Abstract

Statement of originality

1 | Lepton Flavour Violation and the Standard Model

Lepton flavour violation (LFV) is an exciting field of research at the frontier of particle physics. Searches for LFV probe a wide variety of new physics (NP) scenarios. **DISCUSS WHAT LFV IS AND WHERE LEPTON FLAVOUR FITS INTO THE SM** Charged LFV of the form $\tau \to \ell \gamma$. Of the tau processes, these modes are predicted to be the most sensitive to NP.

If this NP introduces Higgs-like particles, we would observe the NP more strongly in the τ sector, since τ 's couple more strongly to Higgs than do muons.

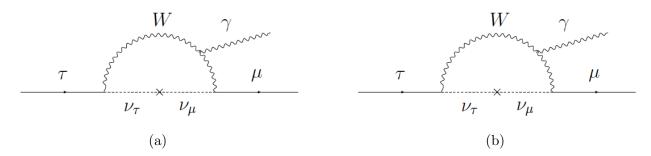


Figure 1.1: Feynman diagrams for (a) $\tau \to \mu \gamma$ and (b) $\tau \to e \gamma$ proceeding through SM processes.

LFV necessarily requires generation mixing between leptons to occur. Though this is prohibited in the Standard Model, the discovery of neutrino oscillations proves that flavour mixing does occur in our universe; that is, flavour is not conserved. We seek to discover whether this LFV can be observed in other areas of flavour physics.

In the Standard Model + massive neutrinos, the only source of LFV is from the operators responsible for neutrino mass. However, the relevant Feynman diagrams (see Figure) are "loop suppressed" and proportional to the GIM factor, given as $\left(\frac{m_{\nu}}{M_W}\right)^4$; as neutrino mass is very small $(\mathcal{O}(0.3\,\mathrm{eV}))$ we expect the LFV effects to be negligible! With these operators the branching ratio for, say, $\tau \to \mu \gamma$ is $\sim 10^{-40}$ [2]. With such little SM background, observation of an LFV process of the type $\tau \to \ell \gamma$ would be an unambiguous signature of NP.

$$\mathcal{B}(\tau \to \ell \gamma) = \frac{3\alpha}{32\pi} |U_{\tau i}^{\star} U_{\mu i} \frac{\Delta_{3i}^2}{m_W^2}|^2 \le 10^{-53} \sim 10^{-49}$$
(1.1)

1.1 Other LFV

In many NP models, LFV is not limited to just $\tau \to \ell \gamma$ decays. There have been searches for other LFV modes, such as $\mu \to e\gamma$, and $\tau \to 3\ell$. Current limits on the branching fractions are given in Figure 1.3 below [?].

LFV process		Future sensitivity
$\mu \to e\gamma$	5.7×10^{-13}	$\approx 6 \times 10^{-14}$
$\mu \to 3e$	1.0×10^{-12}	$\approx 10^{-16}$
$\tau \to e \gamma$	3.3×10^{-9}	$\sim 10^{-8} - 10^{-9}$
$ au o \mu \gamma$	4.4×10^{-9}	$\sim 10^{-8} - 10^{-9}$
au o 3e	2.7×10^{-8}	$\sim 10^{-9} - 10^{-10}$
$ au o 3\mu$	2.1×10^{-8}	$\sim 10^{-9} - 10^{-10}$

Table 1.1: Current experimental limits on various LFV processes

Moving into future sensitivities accessible from experiments such as Belle II, we see that the upper limits of branching fractions for $\tau \to \ell \gamma$ decays could be improved by 1-2 orders of magnitude!

1.2 Hints of LFV beyond the Standard Model

Motivations behind the search for LFV come from both theoretical and experimental results. The primary experimental motivations is the existence of neutrino mixing, though anomalous results such as the $h \to \tau \mu$ excess observed at CMS in 2015 also hint at LFV beyond the Standard Model. On the theoretical side, LFV is predicted in a variety of NP models. In fact, many models which introduce mechanisms to generate neutrino mass also inadvertantly allow LFV in other sectors of non-negligible order! We shall discuss these motivations below.

1.2.1 Neutrino mixing

The discovery that flavour mixing can occur in the neutrino sector [?] [?] proves that neutrinos have mass. Both the concept of massive neutrinos, and by extension the mechanisms which generate neutrino mass, are not predicted or explained by the SM. This tells us that the lepton sector is not fully understood.

There are many NP models which introduce mechanisms to give neutrinos mass. These include SUSY, seesaw models, and many others. In introducing these mechanisms, many of these models inadvertently introduce LFV! As a particle example, a Type-II seesaw model posits a scalar triplet of Higgs-like particles [2]. This triplet comprises a doubly-charged Higgs, a singly-charged Higgs, and a neutral Higgs. As show in Figure X below, lepton-flavour violating processes could proceed via leptons coupling to these scalars!

1.2.2 $h \rightarrow \tau \mu$ excess

Hints of LFV can come in the form of experimental results which are not consistent with the SM. One such "anomaly is the $h \to \tau \mu$ excess. In 2015, CMS found a 2.4 σ excess in the

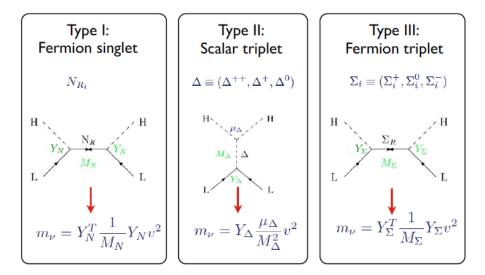


Figure 1.2: New particles introduced in seesaw models (Passemar, 2015)

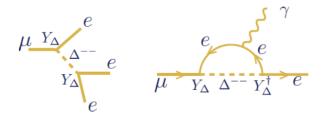


Figure 1.3: Scalars introduced in Type-II seesaw models mediating LFV decays (Passemar, 2015)

branching fraction of $h \to \tau \mu$ [?]. This process is lepton flavour violating, so in the SM its branching fraction is expected to be consistent with zero. However it was determined

$$\mathcal{B}(h \to \tau \mu) = (0.84^{+0.39}_{-0.37})\% \tag{1.2}$$

Also in 2015 was a similar search performed by ATLAS [?], in which an excess of 1.2σ was found in the $h \to \tau \mu$ decay.

$$B(h \to \tau \mu) = (0.77 \pm 0.66)\% \tag{1.3}$$

Though this 1.2σ result is less indicative of NP, it still provides hints as to where NP could occur. These results indicate possible new physics in the Higgs sector! Several models, including Two-Higgs Doublet Models (2HDM), introduce new Higgs-like particles; these particles can couple with leptons to allow lepton flavour violating processes [?]. In fact, LFV can occur naturally in any model with more than one Higgs doublet.

The present experimental result for $\mathcal{B}(h \to \tau \mu)$ is shown in horizontal blue band; current and future projections for $\mathcal{B}(\tau \to \mu \gamma)$ experimental sensitivity are represented with vertical light and dark gray bands. We note that certain 2HDM models predict a branching fraction for $\mathcal{B}(\tau \to \mu \gamma)$, consistent with the CMS results, at sensitivities which could be observed by Belle II. It is important to note that the Higgs sector could contribute to LFV in NP scenarios, and

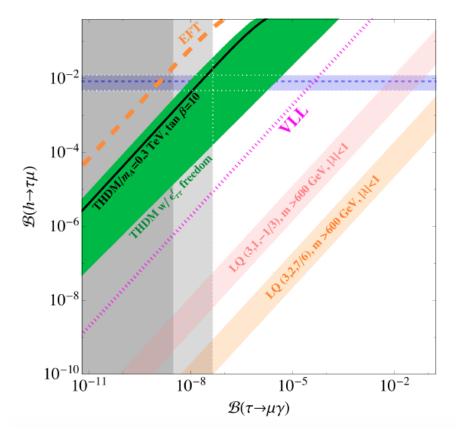


Figure 1.4: Correlation between $\mathcal{B}(h \to \tau \mu)$ and $\mathcal{B}(\tau \to \mu \gamma)$ in various NP scenarios (Dorsner et al., 2015)

that both theory and experimental limits on other LFV processes such as $h \to \tau \mu$ all interweave with limits on $\tau \to \ell \gamma$ branching fractions to provide information on NP, even just through reducing the available phase space for certain models [?].

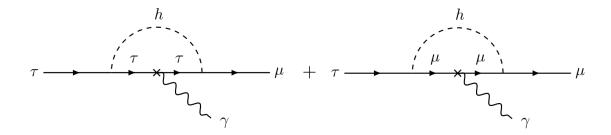


Figure 1.5: Diagrams contributing to $\tau \to \mu \gamma$ decay, mediated by a Higgs boson (Harnick et al., 2012).

As seen in Figure above, new Higgs particles can mediate LFV processes and allow for measurable amounts of LFV beyond the Standard Model [?].

1.2.3 Models predicting $\tau \to \ell \gamma$

As mentioned previously, LFV in the τ sector is introduced in many NP scenarios as a consequence of generating neutrino mass (and hence facilitating neutrino mixing). Branching fractions of the modes $\tau \to \ell \gamma$ are highly calculable - there is little theoretical uncertainty.

model	$\mathcal{B}(\tau \to \mu \gamma)$
mSUGRA + seesaw	10^{-7}
SUSY + SO(10)	10^{-8}
SM + seesaw	10^{-9}
Non-Universal Z'	10^{-9}
SUSY + Higgs	10^{-10}

Table 1.2: Upper limits of branching fractions from $\tau \to \mu \gamma$, predicted by models of new physics beyond the SM (various sources) [1].

Figure above lists a few NP models with their predictions of $\mathcal{B}(\tau \to \mu \gamma)$. We see that the phase space of some of these models has already been ruled out with our current experimental limits on LFV branching fractions.

1.3 Past searches for $\tau \to \ell \gamma$

The most recent searches for $\tau \to \ell \gamma$ were undertaken at Belle (2007) and Babar (2010), for both $\ell = \mu, e$ modes. These experiments both used e^+e^- colliders to generate physics events. A signal of the form $e^+e^- \to \tau^+\tau^-$, with one τ (signal-side) decaying $\tau \to \ell \gamma$ and the other τ (tag-side) decaying generically, with the requirement that the tag-side track is not ℓ .

1.3.1 Belle searches

The Belle detector records events from an asymmetric e^+e^- collider with electron (positron) energy of 8 GeV (3.5 GeV). A detailed discussion of the detector can be found at Ref. [?]. A search for $\tau \to \ell \gamma$ was performed over 535 fb⁻¹ and set constraints [?] on $\tau \to \ell \gamma$ branching fractions as

$$\mathcal{B}(\tau \to \mu \gamma) < 4.5 \times 10^{-8},$$

$$\mathcal{B}(\tau \to e \gamma) < 1.2 \times 10^{-7}.$$

Events were selected by applying selection criteria to twenty event-related variables including momentas and energies; the signal regions for $\tau \to \mu \gamma$ and $\tau \to e \gamma$ after selection are shown in Figures 1.6a and 1.6b respectively. Signal efficiencies, defined as the ratio of generated events to events remaining, in the 2σ regions were $\epsilon_{\tau \to \mu \gamma} = 5.07\%$ and $\epsilon_{\tau \to e \gamma} = 2.99\%$. For the muon mode, dominant backgrounds (non-signal events also produced in e^+e^- collisions) were found to be $e^+e^- \to \tau^+\tau^-$ events with the decay $\tau^\pm \to \mu^\pm \nu_\mu \nu_\tau$ or $\tau^\pm \to \pi^\pm \nu_\tau$, and radiative mu-pair processes $e^+e^- \to \mu^+\mu^-$. Background sources in the electron mode were found to be radiative Bhabha $e^+e^- \to e^+e^-\gamma$ and radiative tau-pair processes $e^+e^- \to \tau^+\tau^-\gamma$.

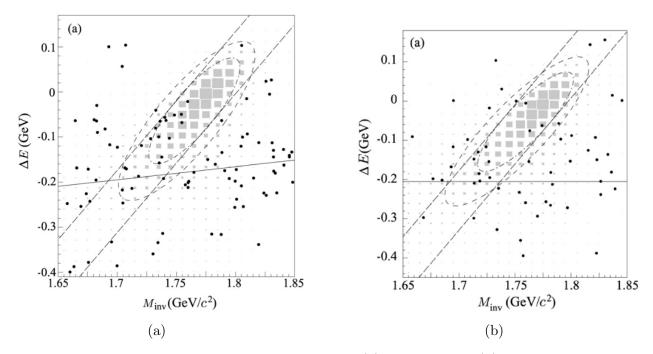


Figure 1.6: $M_{\rm inv}$ - ΔE distribution in the search for (a) $\tau \to \mu \gamma$ and (b) $\tau \to e \gamma$ at Belle over a 535 fb⁻¹ data set. $M_{\rm inv}$ is the reconstructed mass of the τ from these processes, ΔE is the energy difference between this reconstructed τ and half center-of-mass frame beam energy. Dots are the data and shaded boxes indicate the signal MC. The dashed ellipse shows the 3σ region and the dot-dashed ellipse is the 2σ signal region.

1.3.2 Babar searches

Similar to Belle, the Babar detector records events from an asymmetric e^+e^- collider, with electron (positron) energy of 9 GeV (3.1 GeV). A detailed discussion of the detector can be found at Ref. [?]. The most recent search for $\tau \to \ell \gamma$ was performed in 2010 by the Babar Collaboration [?], over a 515.5 fb⁻¹ dataset, setting constraints on $\tau \to \ell \gamma$ branching fractions as

$$\mathcal{B}(\tau \to \mu \gamma) < 4.4 \times 10^{-8},$$

$$\mathcal{B}(\tau \to e \gamma) < 3.3 \times 10^{-8}.$$

1.4 The role of this analysis (rephrase plz)

Collection of data at Belle II is scheduled to begin in 2017. A physics program has been designed for the experiment, detailing specific decays to investigate and areas of particle physics to probe. It is important before data collection begins to perform sensitivity studies on these decay processes, to find areas in which the analysis performs better or worse than expected. In some cases we may find that background rejection is greater than previously modelled due to, for example, good performance in particle identification by the detector. It is also important if areas for improvement are found, such as beam background degrading analysis performance. Finding areas for improvement during the development stage informs future development, in-

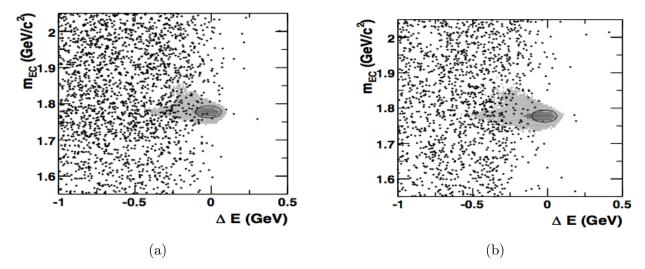


Figure 1.7: $M_{\rm bc}$ - ΔE distribution in the search for (a) $\tau \to \mu \gamma$ and (b) $\tau \to e \gamma$ at Babar over a 515.5 fb⁻¹ data set. $M_{\rm bc}$ is the beam-constrained mass of the τ from these processes, ΔE is the energy difference between this reconstructed τ and half center-of-mass frame beam energy. Data are shown as dots and contours containing 90% (50%) of signal MC events are shown as light- (dark-) shaded regions.

cluding tracking and reconstruction software and hardware-based beam background mitigation techniques, and leads to more optimal conditions for physics events to be investigated.

This analysis is the first τ physics study for Belle II. Some key points studied are muon and electron track reconstruction and the effects of beam background on XXXXX (???). Information on these areas of event analysis is not only useful for $\tau \to \ell \gamma$ searches at Belle II — the physics program for the experiment includes a range of τ decay processes (see Table 1.3) of which many require muon and electron track reconstruction. Low-multiplicity events require XXXXXX, so XXXXXX.

LFV process	Present bound	Future sensitivity
$\tau \to e \gamma$	3.3×10^{-9}	$\sim 10^{-8} - 10^{-9}$
$\tau \to \mu \gamma$	4.4×10^{-9}	$\sim 10^{-8} - 10^{-9}$
$ au^{\pm} ightarrow e^{\pm} e^{\mp} e^{\pm}$	2.7×10^{-8}	$\sim 10^{-9} - 10^{-10}$
$ au^{\pm} o \mu^{\pm} \mu^{\mp} \mu^{\pm}$	2.1×10^{-8}	$\sim 10^{-9} - 10^{-10}$

Table 1.3: Current experimental limits on various LFV processes

Results from this analysis will be published in the Belle II physics book, which is currently being compiled by members across all working groups in the collaboration. The book aims to (????); this study will provide the basis for future τ LFV studies at Belle II. This study also validates the projected increase in sensitivity for $\tau \to \ell \gamma$ branching fractions from Belle to Belle II.

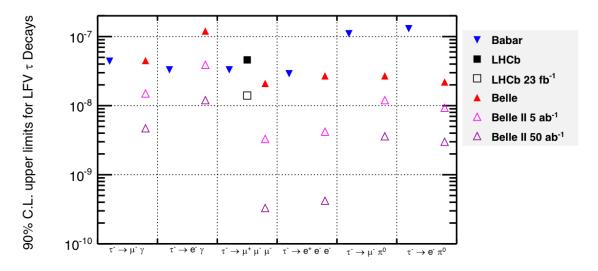


Figure 1.8: Current and future sensitivities on τ LFV branching fractions (*Urquijo*, 2016). **NOTE:** remove the unrelated LFVs

2 | The Belle and Belle II detectors

Located in Tsukuba, Japan, the KEKB particle detector was used for the Belle experiment from 1999 to 2010 and collided high energy electrons and positrons of 8 GeV and 3.5 GeV respectively. This experiment made important discoveries on the flavour structure of elementary particles, notably in the quark section where CP symmetry violation was discovered. Efforts by the Belle collaboration culminated in the 2008 Nobel Prize awarded to Makoto Kobayashi and Toshihide Maskawa for their theory of CP violation. Over its lifetime, the Belle detector collected a total time-integrated luminosity of 1 ab⁻¹, corresponding to 919 000 000 tau-pair events. An upgrade to the KEKB collider known as SuperKEKB is expected to be complete by 2017 as part of the Belle II experiment.

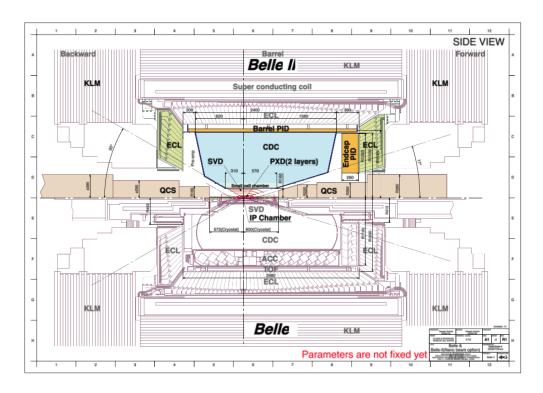


Figure 2.1: Super-KEKB detector design, side-view.

Over the course of the experiment, it is projected that Belle II will collect a total time-integrated luminosity of $50 \,\mathrm{ab^{-1}}$. This is a much larger data sample than the $1 \,\mathrm{ab^{-1}}$ collected at Belle. Electron-positron beam energies differ from those used at Belle, with high-energy-ring (HER) electron beam energy of $7 \,\mathrm{GeV}$ and low-energy-ring (LER) positron beam energy of $4 \,\mathrm{GeV}$. Design luminosity in the detector is increased by $40 \,\mathrm{over}$ Belle; this increases background

hit rate (???) by a factor of 20, while physics event rate is expected to be 50 times higher than at Belle.

Key components of the detector are the vertex detector (VXD), the central drift chamber (CDC), the electromagnetic calorimeter (ECL), the time-of-flight/Cerenkov aerogel chamber (TOP), and the K_L/μ detector (KLM). Many of these will be upgraded in Belle II to provide better performance; in some cases the full reconstruction software is rewritten even when the hardware is not upgraded.

Coordinates in the detector, such as polar angles and positions along the z-axis, are often referred to in the paper, so we shall define them here. The z-axis is the XXXXX; polar angle is the azimuthal angle from the z-axis. The detector is rotationally symmetric around the z-axis; rotation angles are not discussed in this analysis. The angular acceptable of the detector is from 17° (forward) to 150° (backward) — particles with a polar angle within the angular acceptance will be recorded by the detector.

The role of detector components in event reconstruction is discussed in Section 4.1.

2.1 Vertex Detector

Determing the decay vertices of particles — that is, the point inside the detector which the decay occurs — was performed at Belle by the Silicon Vertex Detector (SVD2), comprising four layers of double-sided silicon detectors (DSSDs). By the end of its lifetime SVD2 the innermost layer had an average occupancy of 10%, defined as the fraction of channels hit in each triggered event. This level of occupancy leads to worsened track resolution and reconstruction ("due to merging of clusters with lead to incorrect track association").

With beam luminosity at Belle II projected to increase by factor 20 over Belle, the greater rate of events due to beam-related backgrounds would worsen SVD2 occupancy and degrade detector performance. As such the vertexing detector received a redesign moving to Belle II, with a focus on reducing occupancy. This is achieved by the introduction of a two-layer Pixel Detector (PXD) replacing the the DSSDs closest to beam interaction point, and a four-layer Silicon Vertex Detector (SVD) beyond the PXD.

Vertexing is important BECAUSE XXXXX.

2.1.1 Pixel Detector

The PXD at Belle II has a far larger number of channels than DSSDs - 3.072 million pixels in the inner layer, and 4.608 million pixels in the outer layer. This affords a much smaller occupancy even with higher event rate. Pixel layers are located at 14 mm and 22 mm from the beampipe.

2.1.2 Silicon Vertex Detector

Along with the PXD and the CDC, the SVD is used to measure decay vertices and to extrapolate tracks from charged particles. Track data from the CDC is used in association with SVD data to extrapolate tracks back to the PXD with high efficiency. The SVD comprises four layers of DSSDs at increasing radius from the interaction point: 38, 80, 115, and 140 mm. As the layers

have a larger radius than at Belle, a greater cross-sectional area is covered by the DSSDs, and the quality of reconstruction of charged tracks is improved.

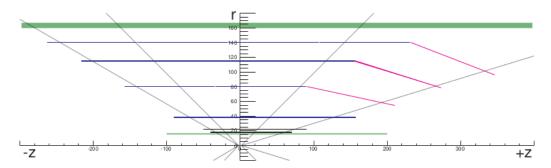


Figure 2.2: Configuration of the four SVD layers (blue), and the two PXD layers (black). Slanted sensors (pink) are used in the forward regions of the outer SVD layers to greatly reduce amount of DSSDs required to cover angular acceptance.

2.2 Central Drift Chamber

The CDC serves as the primary tracking device of the Belle II detector – it can precisely determine the momenta of charged tracks passing through, and, with vertex and impact parameter information from the PXD and SVD, facilitates efficient reconstruction of these particle tracks. Particle identification is also assisted by the CDC, with precise dE/dx measurements for charged particles being good indicators of particle species.

The CDC comprises of many cells filled with neutral gas inside a 1.5 T magnetic field. The cells are occupied by "sense wires"; charged particles passing through the CDC cause ionisation of the neutral gas, with the ionised particles colliding with the sense wires.

The Belle II upgrade will reduce cell size and increase the volume of the CDC, shifting the inner radius from 77 mm to 160 mm and extending the outer radius from 880 mm to 1130 mm. Cell sizes are reduced to operate at high event rates with background levels increased from Belle. The number of sense wires is increased from 8400 to 14336. A visual representation of this upgrade is shown in Figure 2.3.

2.3 Electromagnetic Calorimeter

The ECL consists of two distinct sections within the detector - a 3 m long barrel section with inner radius of 1.25 m, and annular endcaps located 1.96 m forward from the interaction point (IP) along the z-axis and 1.02 m backwards from the IP along the z-axis. At Belle, the barrel section contained 6624 CsI(Tl) scintillator crystals of truncated pyramid shape and average size $6 \times 6 \times 30$ cm³ (cross-section multiplied by crystal depth); the endcaps consisted of 2112 CsI(Tl) crystals, with a total of 8736 crystals in the ECL.

Two main tasks of the ECL are the precise detection of photons and their energy and position within the detector, and identification of electrons. Photons and electrons incident on the barrel and end-cap crystals deposit energy and cause scintillation of the crystals recorded by the detector.

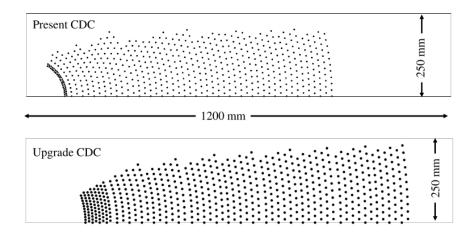


Figure 2.3: A comparison of the central drift chambers for Belle (top) and Belle II (bottom). The upgraded CDC has a larger volume and greater number of sense wires.

Electronics and event-readout for the ECL will be improved for Belle II, and the endcap scintillator crystals will be replaced with pure CsI crystals, which have a faster event response and and more radiation-tolerant. Upgrades to the ECL will considerably improve photon energy resolution. Pile-up of unimportant physics events will also be greatly reduced. Since we are required to reconstruct a signal photon, this improved photon resolution will for better analysis of $\tau \to \ell \gamma$ modes at Belle II.

2.4 Time-of-flight/Cerenkov aerogel chamber

"Particle identification is to be performed by entirely new devices using Cerenkov imaging with faster readouts than in Belle."

TOP: Particle identification in barrel region. Sixteen modules, each containing: Two 2.7m long quartz bars. A spherical mirror. An expansion prism. An array of photodetectors.

Aerogel: Particle identification in forward endcap. Components: Aerogel radiator -¿ produces Cherenkov photons. Expansion volume. 2D array of photon detectors (420 Hybrid Avalanche Photo Detectors). Readout system for photon detectors.

Focusing constructed to separate K and pi photons across most of their momentum range. The TOP counter is useful for K/π separation.

2.5 K_L /muon detector

The outermost detector component at Belle II is the KLM, used in K_L and muon detection. Most electrons and photons generated in a collision do not reach the KLM — the remaining particles are often muons or charged hadrons (π^{\pm} or K^{\pm}). The KLM exists outside the magnetic field of the detector and consists of alternating sandwich of iron plates of thickness 4.7 cm, and active detector elements. As with the ECL, the KLM has barrel and end-cap components.

At Belle the active detector elements were glass-electrode resistive plate chambers (RPC). These elements have worsened efficiency under high background fluxes due to their long dead time; at Belle II the end-cap and innermost barrel RPCs have been replaced with scintillators.

We can discriminate charged hadrons such as pions from muons by penetration depth in the KLM. Pions reaching the KLM interact strongly with the hadronic material in the iron plates and produce hadronic showers detected in the ECL or KLM. In doing so the pions lose a lot of energy, and so only shallow penetrate the KLM. Muons do not interact hadronically and so can and can be identified by their long penetration depth. These particles often travel along nearly straight lines through the KLM and exit the detector. High momentum charged pions can appear as 'fake' muons in the KLM — these particles can penetrate the KLM deeply before they are slowed due to hadronic interactions.

2.6 Particle identification

Particle tracks in the detector can be identified by a combination of discriminants, such as dE/dx measured by the CDC and shower shape in the ECL. Probability density functions (PDFs) for these discriminants are known for a range of possible particles, including e, μ , π and K. Based on each PDF, likelihood probabilities can be calculated then combined to produce a final likelihood variable. This is known as the likelihood ratio \mathcal{L}_{μ} (in this case a muon likelihood ratio), with range 0 to 1. For an example track, the greater \mathcal{L}_{μ} is the more probable that track is a muon. Likelihood ratio is also referred to as particle identification probability, or PID.

Electron candidates are identified using electron likelihood ratio \mathcal{L}_e , which is based on dE/dx information from the CDC, the ratio of energy energy in the ECL and the charged track momentum measured by the SVD and CDC, shower shape at the ECL, matching between positions of a cluster at the ECL and charged track position extrapolated to the ECL, and time-of-flight as measured by the TOF. Identification of muons uses \mathcal{L}_{μ} , which is based on the difference between penetration depth of the track in the KLM as calculated from particle momentum and the measured depth. Kaon and pion candidates are identified using \mathcal{L}_K and \mathcal{L}_{π} respectively, which are based on the dE/dx measurement from the CDC, TOF measurement, and the number of photoelectrons in the ACC.

2.7 Beam backgrounds

[?]

Beam background is an important issue in B-factories, and especially so for the upgraded energies of SuperKEKB. Key sources of this beam background are synchrotron radiation (SR), beam-gas scattering, and Touschek radiation.

Scattered particles and photons generated by these processes collide with the beam pipe and generate showers of photons, leptons and hadrons. Additionally, other particles can be generated at the interaction point of the collision between opposite beams; these are mostly electron-positron pairs. These particles then interact with the detector, and are called beam background. This background can make searches for interesting physics events difficult, due to the large number of clusters and tracks introduced.

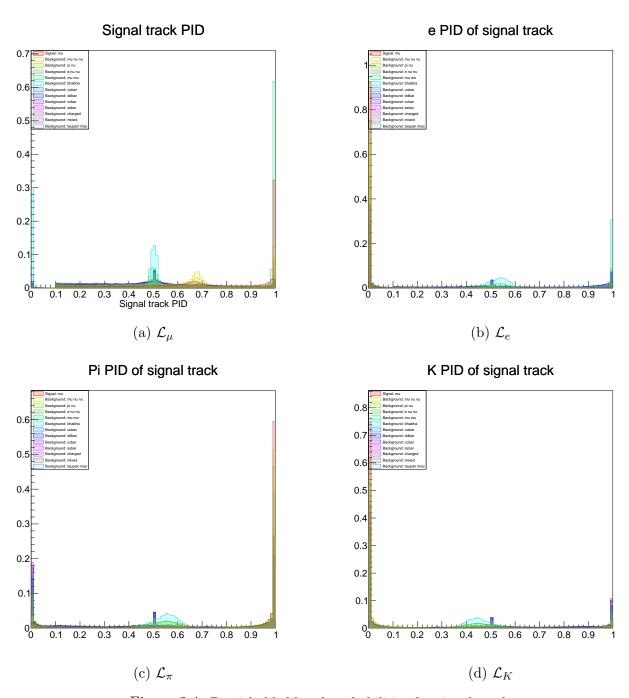


Figure 2.4: Particle likelihood probabilities for signal track.

Tag track PID 0.25 | Signal: mv | Badground: mu nu nu | Badground: mu nu | Badground: mu nu | Badground: mu nu | Badground: mu mu | Badground: bubha | Badground: char | Badground: bubha | Badground: bu

Figure 2.5: Muon likelihood probability for tag-side track.

0.4 0.5 0.6 Tag track PID

0.7 0.8 0.9

0.2 0.3

2.7.1 Synchrotron radiation

As charged beam particles are bent by magnets while travelling through the accelerator, they emit synchrotron radiation (SR). This radiated energy is dependent on particle momentum, and so most SR in SuperKEKB comes from the high-energy ring (HER). SR background is comprised of upstream SR directed towards the IP, and backscattering of SR from downstream. (?????) Beam backgrounds of both type have been studied and have informed the design of the interaction region to reduce its effect.

2.7.2 Beam-gas scattering

The region inside the beam pipe is not a perfect vacuum; the designed gas pressure for SuperKEKB is 10^{-7} Pa. Most of this gas is composed of neutral H₂ and CO₂. Beam particles can collide with the gas molecules, resulting in elastic scattering where energy is unchanged but direction is changed (Coulomb scattering), or inelastic scattering whereby a photon is emitted from the scattered particle (bremsstrahlung).

2.7.2.1 Coulomb scattering

Beam electrons and positrons can elastically scatter off beam gas particles, changing direction such that the scattered particle does not reach the interaction point. Figure 2.6a depicts Coulomb scattering of an electron off a beam-gas particle.

2.7.2.2 Bremsstrahlung

Beam-gas scattering can also occur as bremsstrahlung, where electrons (or positrons) recoil off gas nuclei and emit photons as shown in Figure 2.6b. The photon carries away for fraction of the scattered particle's energy.

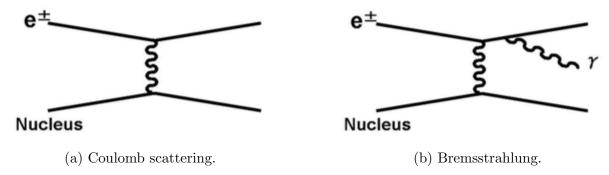


Figure 2.6: Diagrams for beam-gas scattering in the detector.

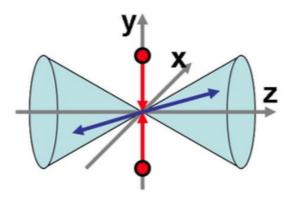


Figure 2.7: An illustration of Touschek scattering in the bunch frame

2.7.3 Touschek scattering

Particle beams do not exist as continuous "lines" of electrons and positrons marching through the accelerator in single file. Instead, we have tightly packed beam bunches, containing $10^{10} - 10^{11}$ particles each. In SuperKEKB the bunches have a designed cross-section perpendicular to the beam trajectory of XXXXX, up from XXXXXX in KEKB (LENGTH??). These bunches are aligned almost perfectly parallel so that beam particles do not collide with the beam pipe during their many cycles around the accelerator.

Within these bunches the particles oscillate in a direction perpendicular to the beam trajectory, so that in addition to interacting with beam-gas, particles within a beam bunch collide with each other resulting in an transfer of energy and momentum. Trajectories of these particles may be changed by this interaction, so that they do not reach the interaction point.

3 | Monte Carlo production and background events

Electron-positron collisions at Belle II will produce a wide range of different physics events. Within these, we hope to find the signal modes $\tau \to \mu \gamma$ and $\tau \to e \gamma$. However, a gallimaufry of non-signal mode events are also produced; these events which are referred to as background (or sometimes physics background, distinct from beam-background) must be suppressed in order to properly investigate signal processes. We discriminate signal from background through applying selection criteria such as energy, momentum, angular relations and event shape variables. This criteria is optimised by examining Monte Carlo (MC) simulated signal and background events. MC events are produced using physics event generators and the response of the detector is simulated.

3.1 Physics backgrounds

It is unfeasible to study MC in-depth for every possible physics background; we focus on high event rate processes and events with final states similar to our signal. In this analysis, we investigate all generically decaying tau-pair processes, mu-pair events $(e^+e^- \to \mu^+\mu^-(\gamma))$, Bhabha scattering $(e^+e^- \to e^+e^-(\gamma))$, $e^+e^- \to q\bar{q}$ events (where q=u,d,c,s) usually referred to as continuum background, and generic BB processes $(e^+e^- \to B^+B^- \text{ or } e^+e^- \to B^0\bar{B}^0)$. Of the tau-pair processes, we isolate the modes $\tau \to \mu\nu\nu$, $\tau \to e\nu\nu$, and $\tau \to \pi\nu$ (for charged pions π^{\pm}) for investigation, as these have the largest branching fractions of generic τ decays. Feynman diagrams of the backgrounds are shown in Figure 3.1a - 3.1e. Note that $e^+e^- \to B\bar{B}$ proceeds though production of the meson $\Upsilon(4S)$.

Fiducial cross-sections for these backgrounds are given in Table 3.1. These values are for collisions at center-of-mass beam energies of 10.573 GeV and with Belle II detector geometry.

3.2 Event generation

All MC was generated in the Belle II Analysis Framework (basf2) with geometry and energies from SuperKEKB using physics event generators given in Table 3.1. All generators use the same beam parameters such as vertex positions and beam energies, as well as geometry information including highly accurate location, thickness and material values. Magnetic field strength through the detector is also known and included in event generation. The detector components are simulated by the generator, so that timing information and energy deposition is recorded for these components as MC particles interact with them. Following the simulation of a physics

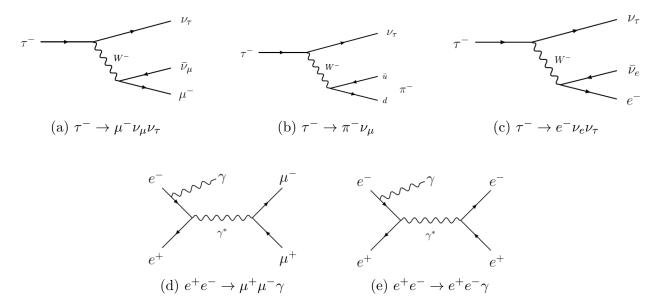


Figure 3.1: Feynman diagrams for the dominant leptonic physics backgrounds for $\tau \to \mu \gamma$. The radiative photon mu-pair and Bhabha processes in 3.1d and 3.1e can originate from any of the four charged particles. We analyse both radiative and non-radiative (without a final state photon) processes in this analysis.

event, information from the sub-detectors is used to reconstruct tracks (correponding to charged particles) and clusters (referring to cells of the ECL with which a particle has interacted with, corresponding to photons).

3.2.1 Signal generation

Signal MC was produced using the KKMC generator, the default generator for tau-pair and mupair final state processes $e^+e^- \to \mu^+\mu^-(\gamma)$ and $e^+e^- \to \tau^+\tau^-(\gamma)$ [?]. Decays proceeded as $e^+e^- \to \tau^+\tau^-$, with one tau decaying to the signal mode $\tau \to \ell\gamma$ (the signal-side), and the other (the tag-side) decaying to all experimentally measured SM decay modes of the τ (called generic decay), scaled by their branching ratio. $\tau^+ \to \ell^+\gamma$ and $\tau^- \to \ell^-\gamma$ modes were both generated to account for differences due to charge. A total of 3 100 000 events were generated for the muon mode, and 2 550 000 for the electron mode.

3.2.2 Background generation

Samples for a range of background events were produced by the Belle II collaboration; the generators used for each background process are given in Table 3.1. Initial state radiation (ISR) and final state radiation (FSR) of multiple photons is generated by KKMC and BABAYAGA.NLO generators. Beam backgrounds are not generated using standard event generators are given in Table 3.1 and are instead generated using dedicated software then later mixed with physics background MC.

Background process	Cross-section [nb]	Generator	
$ au o \mu \nu \nu$	0.160	KKMC, TAUOLA	
$ au ightarrow \pi u$	0.100	KKMC, TAUOLA	
$ au o e \nu u$	0.164	KKMC, TAUOLA	
$\tau \to \text{generic}$	0.919	KKMC, TAUOLA	
$e^+e^- \to \mu^+\mu^-(\gamma)$	1.148	KKMC	
$e^+e^- \rightarrow e^+e^-(\gamma)$	300	BABAYAGA.NLO	
$e^+e^- \to u\bar{u}$	1.61	KKMC	
$e^+e^- o d\bar{d}$	0.40	KKMC	
$e^+e^- \to s\bar{s}$	0.38	KKMC	
$e^+e^- \to c\bar{c}$	1.30	KKMC	
$e^+e^- \rightarrow B^+B^-$	0.525	EvtGen 1.3, PYTHIA 8.2	
$e^+e^- \to B^0\bar{B}^0$	0.525	EvtGen 1.3, PYTHIA 8.2	

Table 3.1: Fiducial cross-sections for backgrounds at Belle II.

3.3 Event scaling

Belle II is projected to collect a time-integrated luminosity of $50 \,\mathrm{ab^{-1}}$ over the length of the experiment. Instead of running over the equivalent amount of background events expected in such a sample size we can run over a smaller number of events then scale results. This is done for computing reasons, as the number of background events recorded for these luminosities quickly becomes prohibitively large. **REPHRASE**.

We choose to scale up to a luminosity of 1 ab^{-1} ; this is the total time-integrated luminosity of the complete Belle dataset, and so is useful as a point of comparison to previous searches. The scale factor for each event type is calculated by

$$n_{1 \text{ ab}^{-1}} = n_{\text{generated}} \times \text{scale factor},$$
 (3.1)

where $n_{1 \text{ ab}^{-1}} = \mathcal{L}\sigma$, and $n_{\text{generated}}$ is the number of events generated. Scaled event numbers are presented in Table 3.2 below.

Event type	$\mathbf{n}_{ ext{generated}}$	scale factor	$\mathbf{n}_{1\mathrm{ab}^{-1}}$
$\tau \to \mu \gamma$	3200000	2.58×10^{-5}	83
$\tau \to e \gamma$	2550000	8.65×10^{-5}	221
$\tau \to \mu \nu \nu$	127998320	1.250	159997900
$ au o \pi u$	267245200	1.250	334056500
$\tau \to e \nu \nu$	131086160	1.250	163857700
$\tau \to \text{generic}$	208870320	1.250	261087900
$e^+e^- \rightarrow \mu^+\mu^-(\gamma)$	148600000	7.725	1148000000
$e^+e^- \rightarrow e^+e^-(\gamma)$	15630000	19193.858	300000000000
$e^+e^- \to u\bar{u}$	1268991935	1.269	1610000000
$e^+e^- o d\bar{d}$	317048262	1.262	400000000
$e^+e^- o c\bar{c}$	1039855756	1.250	1300000000
$e^+e^- \to s\bar{s}$	289900586	1.310	380000000
$e^+e^- \rightarrow B^+B^-$	451320000	1.219	550000000
$e^+e^- o B^0 \bar{B}^0$	427680000	1.286	550000000

Table 3.2: Scaled event numbers

Unless explicitly stated, scaled event numbers will be used throughout this analysis as to provide accurate points of comparison between events.

3.4 Version differences

The software framework on which event generation was performed is undergoing continuous development; a majority of signal and background MC was produced on the same release version to ensure accuracy between MC types. This version was made available on XXXXX, and was one of the most up-to-date releases at the time of analysis. However, the backgrounds $\mu^+\mu^-(\gamma)$ and $e^+e^-(\gamma)$ (mu-pair and bhabha, respectively) did not have any events generated using this release, and instead used an older release dated XXXXX.

A full investigation into the differences in generated MC between releases has not been performed in this analysis, as it is assumed they are negligible in most relevant cases. Changes relate mostly to generation of beam backgrounds (??); however one major change is in the reporting of timing data from the ECL. From the release dated XXXX onwards, these associated times will be reported in nanoseconds, rather than uncalibrated clock ticks (REF). In comparing samples of background MC generated in both the older and newer releases, Figure 3.2a and 3.2b below, as well as private correspondance with the developer responsible for these changes, it was found that conversion to the newer scale could be achieved by adding 80 units to the cluster timing values.

https://docs.belle2.org/record/344/files/BELLE2-NOTE-TE-2016-006.pdf

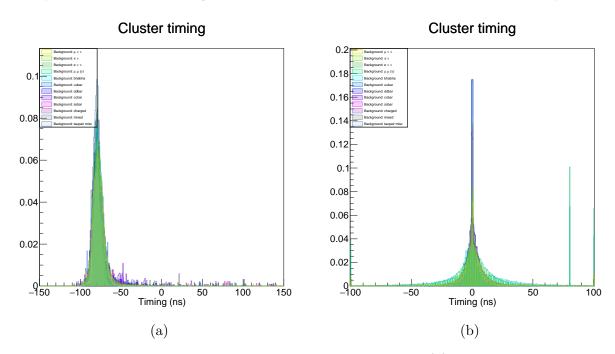


Figure 3.2: Comparisons of cluster timing with background MC (a) prior to ECL timing change and (b) after ECL timing change. Note the shift in peak by 80 units between versions.

3.5 Implementation of beam backgrounds

Signal and background MC was generated with simulated beam background. The most important sources have been generated by a dedicated accelerator group software within the Belle II collaboration. This software simulates particles travelling the detector and records the position and momentum of particles which leave the nominal beam trajectory and collide with the beam pipe or collimator (???). Detector response simulation is then processed for these particles to produce background samples of a given type. Separate backgrounds were made for electron (HER) and positron (LER) beams, due to differences in energies and currents. Implemented background types are listed in Table 3.3.

type	source	rate [MHz]
radiative Bhabha	HER	1320
radiative Bhabha	LER	1294
radiative Bhabha (wide angle)	HER	40
radiative Bhabha (wide angle)	LER	85
Touschek scattering	HER	31
Touschek scattering	LER	83
beam-gas interactions	HER	1
beam-gas interactions	LER	156

Table 3.3: Beam background types simulated at Belle II (REF - Belle II Simulation (Belle II note)). Rate is calculated

For comparison, some samples of MC were generated without beam background. Comparisons between some measureables are shown in Figures 3.3a and 3.3b, 3.4a and 3.4b below.

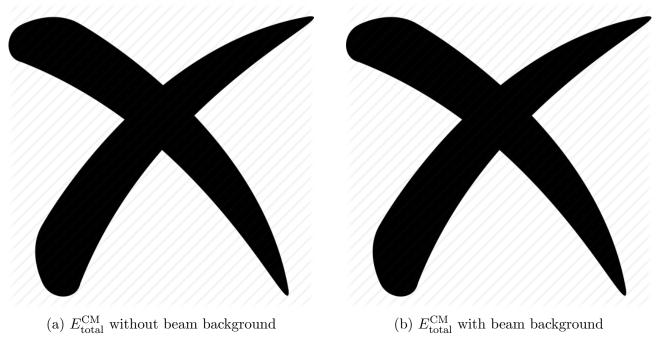
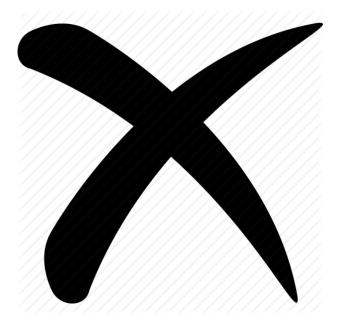


Figure 3.3: Comparison of total center-of-mass energies for signal and background distributions with and without beam background.





(a) Total center-of-mass energies \mathbf{w}/\mathbf{o} beam background

(b) Total center-of-mass energies w/ beam background

There are many differences between MC with and without beam background; only a few key points will be discussed here. Most obvious is the number of tracks recorded. Taking, for instance, our signal mode, we would expect for most events 2 or 4 tracks - one signal-side track corresponding to μ/e , and one or three tracks on the tag-side (one- or three-pronged) coming from standard model τ decays, which are dominantly one- or three-pronged. Beam background particles in the detector produce a number of new tracks (as well as clusters) which are tracked by sub-detector components, then later reconstructed.

Kinematic variables such as energy and momentum are also obviously affected by beam background. We observe an increase in low energy and low momentum tracks; in these cases low energy beam background particles have been misidentified as signal- or tag-side particles originating from tau-pair processes.

4 Reconstruction

Reconstruction of events was performed through basf2. Reconstruction of events can be separated into three sections - tracking, calorimeter reconstruction, and particle identification.

Belle II Note: Belle II Reconstruction Software and Performance

4.1 Reconstruction process

- 4.1.1 Tracking
- 4.1.2 Calorimeter reconstruction
- 4.1.3 Particle identification
- 4.1.3.1 Charged particle identification
- 4.1.3.2 Neutral particle identification

4.2 Reconstruction of $\tau \to \ell \gamma$

To reconstruct events, we fill lists of particles by categorising tracks as specific charged particles - muons, electrons or pions, and by associating clusters with photons. These categorisations are performed with loose criteria to remove obvious background events. Tracks with PID values greater than 0.1 (or 0.5?) are considered muons, and similar for electrons and pions; the photon list is populated by clusters passing a "goodness" test.

DISCUSS SIGNAL SIDE/TAG SIDE (+signal track, signal photon).

We define the signal track to be reconstructed track associated with the final state electron or muon from $\tau \to \ell \gamma$; similarly the signal photon describes the cluster associated with the final state photon. The signal-side particles do not necessarily refer to the physical charged particle or photon coming from the signal modes under analysis; misidentified particles (such as a pion being identified as a muon during reconstruction) or particles from different decay processes (such as a muon from the tau process $\tau \to \mu\nu\nu$).

We reconstruct the signal side tau as $\tau \to \mu \gamma$ for the muon mode, or $\tau \to e \gamma$ for the electron mode. The tag side tau is reconstructed by requiring at least one muon, electron or charged pion. In addition to PID cuts, we also apply loose cuts to our ΔE and $M_{\rm inv}$. We define our signal region variables as

$$\Delta E = E_{\text{signal }\tau}^{\text{CM}} - E_{\text{beam}}/2, \tag{4.1}$$

$$M_{\rm inv} = \text{invariant mass of reconstructed signal side tau},$$
 (4.2)

where $E_{\text{signal }\tau}^{\text{CM}}$ is the center-of-mass energy of the reconstructed signal-side tau, and E_{beam} is the total center-of-mass energy of the electron-positron beam system. Nominally we expect signal events to have $\Delta E \sim 0$ and $M_{\text{inv}} \sim m_{\tau}$; signal region selection is further discussed in Section XXXX.

Once background has been sufficiently reduced through use of selection criteria, signal candidates will be chosen from events in the ΔE vs. $M_{\rm inv}$ phase space. As such we cut (???) only very loosely on these criteria wherever possible; in reconstruction we require $-0.4\,{\rm GeV} < \Delta E < 0.2\,{\rm GeV}$ and $1.6\,{\rm GeV} < M_{\rm inv} < 1.9\,{\rm GeV}$ for the signal side tau.

4.3 Reconstruction efficiencies

The number of events over which reconstruction was performed, and the reconstruction efficiency ϵ_{recon} , is shown in Table 4.1.

Event type	events in	events out	$\epsilon_{ m recon}$
$ au o \mu \gamma$	3200000	5435660	169.86%
$ au o e \gamma$	2550000	4155023	162.94%
$\tau \to \mu \nu \nu$	127998320	542504	0.42%
$ au o \pi u$	267245200	861406	0.32%
$ au o e \nu \nu$	131086160	87848	0.07%
$\tau \to \text{generic}$	208870320	1843380	0.88%
$e^+e^- \rightarrow \mu^+\mu^-(\gamma)$	148600000	5159295	3.47%
$e^+e^- \rightarrow e^+e^-(\gamma)$	15630000	370496	2.37%
$e^+e^- \to u\bar{u}$	1268991935	52373200	4.13%
$e^+e^- o d\bar{d}$	317048262	12987072	4.10%
$e^+e^- \to c\bar{c}$	1039855756	48007101	4.62%
$e^+e^- \to s\bar{s}$	289900586	11122646	3.84%
$e^+e^- o B^+B^-$	451320000	46498047	10.30%
$e^+e^- \to B^0\bar{B}^0$	427680000	46912228	10.97%

Table 4.1: Reconstruction efficiency (unscaled events)

Reconstruction efficiencies for $\tau \to \mu \gamma$ and $\tau \to e \gamma$ are shown to be greater than 100 %. This is due to some signal events having multiple candidates —

4.4 Track counting

Low-momentum tracks can "curl" around in the detector and be counted twice.

We expect our signal mode to be have two or four charged particle tracks in most cases - a muon on the signal-side, and one (or less often three) charged particles on the tag-side according to SM decays. However due to tracks introduced by beam backgrounds (and not-omniscient reconstruction) we cannot naively select events with only two or four tracks without removing prominent amounts of signal. Instead we require the number of reconstructed tracks to be less than 15 to suppress hadronic backgrounds.

5 Event signatures

We discuss expected energies, kinematics and signal-side event topologies with comparison to MC events. Knowledge of event signatures is important in optimising selection criteria and hence the ratio of signal-to-background. This also serves as validation of the MC, as we compare physical expectation of certain variables to the simulated events.

5.1 Signal

5.1.1 Muon mode

The mode $\tau \to \mu \gamma$ has a simple signal side, with only one track and one photon, and no missing energy (in the form of neutrinos). If we assume that on average both τ particles generated in the e^+e^- collision share equally the energy generated in the interaction, we expect the mean signal-side center-of-mass frame energy to be 5.5 GeV. No physical preference is given to the energy distribution between the signal muon and signal photon, so their center-of-mass energies should be normally distributed around 2.75 GeV. Recalling the relation between energy, momentum and mass,

$$E^2 = p^2 + m^2, (5.1)$$

since the muon energy is much greater than its mass of $105.66 \,\mathrm{MeV/c^2}$ this can simplify to

$$E^2 \approx p^2, \tag{5.2}$$

noting that p is the magnitude of the particle's 3-momentum.

We can predict and compare with MC several topological measureables, such as polar angle (i.e. angle from an axis parallel to the beam trajectory) as well as opening angles between particles; this is done for several key measureables. The average opening angle between the signal muon and signal photon in the center-of-mass frame can be calculated by boosting the expected back-to-back pair from the signal τ frame into the lab frame.

CALCULATIONS.

Similarly for SOME OTHER PAIRING,

CALCULATIONS.

As shown in Figures 5.3 - ?? below, the MC matches the predicted kinematics and topologies for the muon mode.

Centre-of-mass $\boldsymbol{\mu}$ momentum

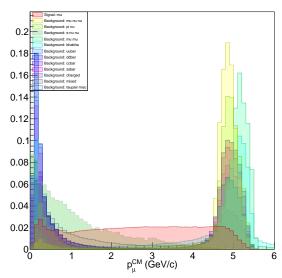


Figure 5.1: Center-of-mass frame momentum of signal muon.

Total centre-of-mass energy of system

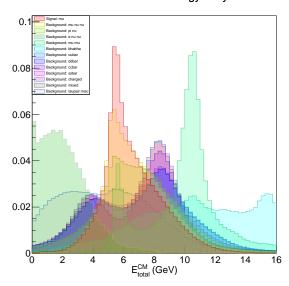


Figure 5.3: Total center-of-mass energy of the system.

Energy of signal γ

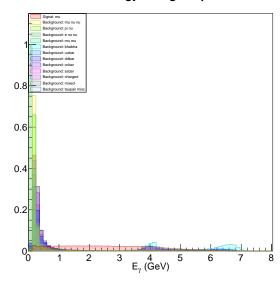


Figure 5.2: Lab frame energy of signal photon.

No. of tracks

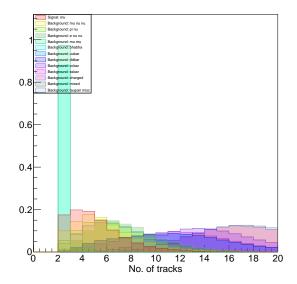


Figure 5.4: Number of reconstucted tracks.

5.1.2 Electron mode

Much of the kinematics and topologies as described for the signal muon mode also applies to the signal electron mode. However, it is prudent to note the major difference between the two final state charged particles - specifically the difference in mass. Muons have mass $105.66 \,\mathrm{MeV/c^2}$, over 200 times heavier than electrons, with mass of $0.511 \,\mathrm{MeV/c^2}$. Due to their lighter mass, electrons lose far more energy due to bremsstrahlung (braking radiation), as given by

$$P = \text{radiated power} = \frac{e^2 a^2 \gamma^4}{6},\tag{5.3}$$

where

$$e = \text{electron charge},$$
 (5.4)

$$a = \text{particle acceleration},$$
 (5.5)

$$\lambda = \text{relativistic factor},$$
 (5.6)

(5.7)

and we have of course taken particle physics units $c = \pi = \epsilon_0 = 1$. Since $E = \gamma mc^2$, radiated power from bremsstrahlung goes as m^{-4} ; electrons lose more energy via bremsstrahlung than muons by factor $(m_{\mu}/m_e)^4 \sim 200^4$.

This energy in the form of photons is deposited in the ECL clusters; a non-negligible amount of radiation from beam background is also deposited in these clusters, making accurate energy reconstruction of the signal electron difficult (??? is this right, or is it just that the electron has less energy? What is the "energy/momentum" variable.... E/P at creation?). Due to this energy loss we see a different energy and momentum signature for the signal track compared to the muon mode; peaks for both are located around XXXX GeV, but a large fraction of events have energies much lower.

Accurate reconstruction via basf2 is more difficult for these lighter particles, with only a fraction of $\tau \to e\gamma$ events having a reconstructed τ invariant mass peak anywhere near the τ mass.

5.2 Backgrounds

5.2.1 Tau-pair processes

A key difference between tau-pair backgrounds and the signal modes investigated is the lack of signal-side photon, and the existence of signal-side neutrinos.

In tau-pair processes, the signal-side τ of energy 5.5 GeV decays dominantly into a single charged track and a neutrino (or neutrinos, in the pion modes). Light neutrinos carry away only a fraction of the energy from its mother particle; we expect the signal track to have a peak in energy of ≈ 5.5 GeV. However, the electron will lose a significant fraction of its energy due to bremsstrahlung as it passes through the detector and hence have a lower average energy. This is consistent with Figure 5.1.



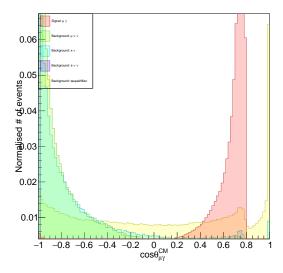


Figure 5.5: Cosine of the opening angle between signal track and signal photon in the center-of-mass frame; comparison between $\tau \to \mu \gamma$ and background tau-pair processes.

In most cases for tau-pair processes, the reconstructed signal photon comes from ISR, FSR or more often beam backgrounds. Photons produced as beam background are often low energy, especially compared to the average photon energy from signal processes of $\sim 2.25\,\mathrm{GeV}$. Signal photon energy is shown in Figure 5.1; we note the peak energy of $E_{\gamma} < 1\,\mathrm{GeV}$ for tau-pair processes.

Since the signal photon does not originate from the signal-side τ , the signal tracks appears "boosted" by comparison. This boost leads to the signal track and signal photon travelling almost back-to-back in the center-of-mass frame, in contrast to the signal mode where these final state particles have only a small opening angle between them (see Figure 5.5).

5.2.2 Mu-pair processes

Muons are very cleanly reconstructed by the detector; they do not lose any significant amount of energy through bremsstrahlung radiation, and they penetrate deeply leaving a distinct signal. Unlike the tau-pair processes or the signal modes discussed above, mu-pair processes $e^+e^- \to \mu^+\mu^-(\gamma)$, both signal- and tag-side channels consist of only a single charged track each, sometimes with a final state photon. Hence, mu-pair processes are reconstructed very well. This is evidenced by the majority of events with only two reconstructed tracks (see Figure XXXX); this is stark comparison to the spread of tracks from two up to fifteen in tau-pair events. Total reconstructed energy peaks around 10.5 GeV.

By momentum conservation, the signal and tag tracks are generated back-to-back for $\mu\mu$ final states (XXX % of all mu-pair processes), or with an opening angle similar to the signal mode for radiative $\mu\mu\gamma$ final states (XXXX % of all mu-pair processes). The signal photon is often reconstructed from low energy beam background photons, as with background tau-pair processes. A similar photon energy spectrum can be seen in Figure 5.2.

5.2.3 Bhabha

Bhabha events $e^+e^- \to e^+e^-(\gamma)$ have similar event signatures to mu-pair processes $e^+e^- \to \mu^+\mu^-(\gamma)$ across a range of variables, for obvious reasons. However, as is case with electrons in the detector, both signal- and tag-track particles lose a significant portion of their energy to bremsstrahlung and are not reconstructed as cleanly as muons.

Smearing of energies and momenta occurs for Bhabha event reconstruction, with measureables not peaking as strongly as for mu-pair events and instead spreading across a values. These features are shown in Figures 5.6 and 5.7 below, comparing distributions for mu-pair events to bhabha events. Much of the event topology is still common between these processes, however.

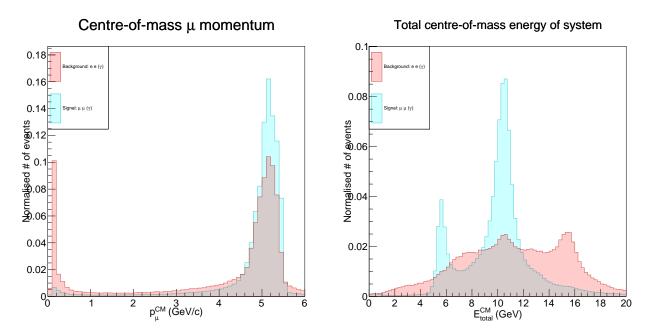


Figure 5.6: Comparison of center-of-mass frameFigure 5.7: Comparison of total energy of the syssignal track momentum for Bhabha and mu-pairtem in center-of-mass frame for Bhabha and mu-events.

5.2.4 Continuum and $B\bar{B}$

Hadronic backgrounds at Belle II come from the events $e^+e^- \to q\bar{q}$ and $e^+e^- \to B\bar{B}$. The event rate for the energies at which we investigate is dominated by these processes, however their event signatures are distinct from leptonic processes in many variables allowing good separation.

HMMM DON'T KNOW WHAT TO WRITE ABOUT. SOMETHING ABOUT JETS?

No. of tracks 0.22 | Signat: # 7 | 0.2 | Background: subar | 0.18 | Background: dobar | 0.18 | Background: charged | 0.10 | 0.12 | 0.12 | 0.14 | 0.02 | 0.04 | 0.02 | 0.04 | 0.02 | 0.06 | 0.04 | 0.02 | 0.06 | 0.04 | 0.05 | 0.06 | 0.04 | 0.05 | 0.06 | 0.04 | 0.05 | 0.06 | 0.04 | 0.05 | 0.06 | 0.04 | 0.05 | 0.06 | 0.04 | 0.05 | 0.06 | 0.04 | 0.05 | 0.06 | 0.04 | 0.05 | 0.06 | 0.04 | 0.05 | 0.06 | 0.04 | 0.05 | 0.06 | 0.04 | 0.05 | 0.06 | 0.04 | 0.05 | 0.06 | 0.05 | 0.06 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.0

Figure 5.8: Number of tracks in continuum and $B\bar{B}$ events.

6 Preselection

Following reconstruction, preselection criteria were applied to the reconstructed events. Preselection criteria are defined as distinct from selection criteria in that they remove a minimal amount of signal while removing the more obvious background components; in choosing selection criteria we seek to maximise $S/\sqrt{S+B}$, which may necessarily involve the exclusion of a non-negligible amount of signal.

The preselection criteria were selected by inspection of plots of various topology and energy based variables. Different preselection and selection criteria are chosen for each final state mode, due to the different event signatures. A total of 5 variables where chosen for preselection.

6.1 Muon mode

Figures xxx - xxx below show the variables on which preselection criteria were applied, with the specific values for preselection listed in Table xxx. Signal and background efficiencies after preselection are shown in Table XXXX.

98.06% of reconstructed $\tau \to \mu \gamma$ signal events pass the preselection criteria; around 1,000,000,000 background events out of 2,000,000,000 are removed through this process. Most notably affected by preselecton are the continuum events of which only XXXX% remain. This reduction is greatly attributed to the clear separation between signal and continuum background in the $E_{\rm total}^{\rm CM}$.

v	description	\mathbf{lower}	upper
$p_{ m tag}^{ m CM}$	CM momentum of tag track	_	$5.2\mathrm{GeV}$
$\cos heta_{ m signal}$	Cosine of polar angle of signal track	-0.9	
$cos heta_{ m signal} \ E_{ m total}^{ m CM}$	Center-of-mass energy of total system		$15\mathrm{GeV}$
thrust	Magnitude of signal thrust vector*	0.92	
$E_{ m sum}^{ m CM}$	Center-of-mass energy of photons and tracks	$4.5\mathrm{GeV}$	_

Table 6.1: Preselection cuts (muon mode)

We also place a loose requirement of $M_{\rm inv}$, requiring 1.65 $< M_{\rm inv} <$ 1.85. Although this is one of our signal region variables, we are justfied in applying loose preselection on it because events outside this selection will lie outside the final signal region, and hence be unimportant to the analysis.

MC type	events in (scaled)	events out	$\epsilon_{ m ps}$
$\tau \to \mu \gamma$	140	135	96.32%
$ au o \mu \nu \nu$	678130	631235	93.08%
$ au o \pi u$	1076758	822028	76.34%
$\tau \to e \nu \nu$	109810	70675	64.36%
$\tau \to \text{generic}$	2304225	636954	27.64%
$e^+e^- \to \mu^+\mu^-(\gamma)$	39857811	21938180	55.04%
$e^+e^- \rightarrow e^+e^-(\gamma)$	7111247601	1457005758	20.49%
$e^+e^- \to u\bar{u}$	66447114	29767142	44.80%
$e^+e^- \to d\bar{d}$	16384978	7307320	44.60%
$e^+e^- \to c\bar{c}$	6017200	23401910	38.99%
$e^+e^- \to s\bar{s}$	14579500	6299797	43.21%
$e^+e^- \rightarrow B^+B^-$	56664730	22083348	38.97%
$e^+e^- \to B^0\bar{B}^0$	60329511	23372366	61.26%

Table 6.2: Preselection efficiency (muon mode).

6.2 Electron mode

Separate preselection criteria was chosen for the electron mode. These criteria do not differ much, as expected, however due to the prevalence of bremsstrahlung in the electron mode the energy variables differ greatly. Due to this we set an upper limit on $E_{\text{sum}}^{\text{CM}}$ rather than a lower limit as for the muon mode.

$\operatorname{symbolic}$	description	lower	upper
$p_{\mathrm{tag}}^{\mathrm{CM}}$	CM momentum of tag track		$5\mathrm{GeV}$
$\cos \theta_{ m signal}$	Cosine of polar angle of signal track	-0.975	
$\cos heta_{ m signal} \ E_{ m total}^{ m CM}$	Center-of-mass energy of total system		$14\mathrm{GeV}$
thrust	Magnitude of signal thrust vector*	0.92	
$E_{\text{sum}}^{\text{CM}}$	Center-of-mass energy of photons and tracks	$4.5\mathrm{GeV}$	

Table 6.3: Preselection cuts (electron mode)

Again, a loose requirement of $1.65 < M_{\rm inv} < 1.85$ is required for event preselection. Following reconstruction

Note the dramatic drop in the number of $\tau \to e\gamma$ signal events. This is due to the restriction of $M_{\rm inv}$. We expect a peak around the invariant mass of the τ , $m_{\tau} \sim 1.777\,{\rm GeV/c^2}$; see Figure 6.1. For the electron mode a peak occurs slightly after that mass, around $1.8\,{\rm GeV/c^2}$. More important, however, is the high multiplicity of events at $M_{\rm inv} = 0$. Obviously this is an unphysical value — we determine that this feature is due to the large number of signal electron tracks which are not reconstructed properly (**ELABORATE ON THIS**).

After preselection, the signal electron mode has an efficiency of only 9.95%. The total efficiency of the signal muon mode after all selection criteria have been applied (Section XXXXX) is, in comparison, 7.23% - we would expect that the efficiency of the electron mode would get considerably worse after event selection. Due to this poor reconstruction and minimal number of events remaining only after preselection, we do not continue to full event selection in MC for $\tau \to e\gamma$. Unless otherwise specified, the remainder of the analysis will concern the mode $\tau \to \mu \gamma$ only.

MC type	events in (scaled)	events out	$\epsilon_{ m ps}$
$ au o e \gamma$	140	29	13.25%
$ au o \mu \nu \nu$	678130	645716	95.22%
$ au o \pi u$	1076758	872186	81.00%
$ au o e \nu \nu$	109810	0	0%
$\tau \to \mathrm{generic}$	2304225	758109	%
$e^+e^- \to \mu^+\mu^-(\gamma)$	39857811	18676083	%
$e^+e^- \rightarrow e^+e^-(\gamma)$	7111247601	1483493282	20.49%
$e^+e^- \to u\bar{u}$	66447114	35306780	%
$e^+e^- \to d\bar{d}$	16384978	8692996	%
$e^+e^- \to c\bar{c}$	6017200	30600420	%
$e^+e^- \to s\bar{s}$	14579500	7675121	%
$e^+e^- \rightarrow B^+B^-$	56664730	28912567	%
$e^+e^- \rightarrow B^0\bar{B}^0$	60329511	30716377	61.26%

Table 6.4: Preselection efficiency (electron mode).

Note: should perhaps investigate/talk more about the underlying issues.

Invariant mass of reconstructed signal $\boldsymbol{\tau}$

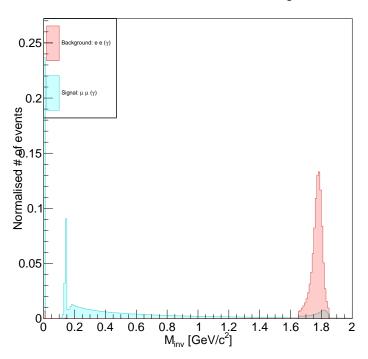


Figure 6.1: Comparison of $M_{\rm inv}$ for signal muon and signal electron modes. Note that we expect a peak around $m_{\tau} \sim 1.777\,{\rm GeV/c^2}$.

7 | Signal optimisation

There are many reasonable ways to quantify signal optimisation compared to background in a particle physics analysis. For this analysis, we have chosen the measure of signal optimisation $S/\sqrt{S+B}$. S is the expected number of signal events remaining after event selection has been performed; note that we scale for our signal events dependent on their associated LFV branching fractions, which are currently experimental upper bounds. Hence the measure $S/\sqrt{S+B}$ will vary for different branching fraction hypotheses. Similarly B is the expected number of background events remaining after event selection; specifically this is the sum of all events remaining across all background MC used in analysis. Since not all possible background processes have been included we would expect the empirical value of B to be higher; this is mostly unimportant for our analysis since we need only compare changes in $S/\sqrt{S+B}$ between different selection criteria, not to know the absolute value.

To maximise $S/\sqrt{S+B}$, the number of background events must be reduced while not removing too many sgnal events. This is especially important given the low branching fraction of our signal - taking the experimental upper limit of the $\tau \to \mu \gamma$ branching fraction, we expect only 83 signal events, after reconstruction and preselection, in a $1\,\mathrm{ab^{-1}}$ dataset, compared to over $1\,500\,000\,000$ (1.5 billion) background events in the same luminosity.

Forty selection criteria were used in selecting for $\tau \to \mu \gamma$ events. Some variables were taken from the previous search for $\tau \to \ell \gamma$ at Belle (REF); more were added as the analysis progressed to achieve better greater signal separation. Some of these variables were not included in the final analysis. Notable were those related to missing momentum and mass, as some uncertainty was held regardly the accurate reconstruction of these variables. Others such as tagtrack transverse momentum and signal-track momentum were not included due to significant overlap of background exclusion with other variables (most obviously center-of-mass tag track momentum and center-of-mass signal-track momentum) causing selection on these measureables to have little to no impact on signal optimisation.

I could include cosTBz, missingMassSqr here....

The thresholds were chosen via a manually iterative process, continually improving the ratio $S/\sqrt{S+B}$ by adding or refining criteria. Initial criteria were informed by a combination of automatic iteration over a range of threshold values for around 20 variables, and by visual inspection.

The accomplish the former, selection was repeatedly performed over all MC with only a single criteria applied. The lower or upper threshold of this criteria was modified by a small increment each time. The resulting value of $S/\sqrt{S+B}$ was then plotted against the selection threshold; this plot is called a *figure-of-merit* plot. An obvious peak, as in Figure 7.1, indicates a **beneficial???** value for selection. For many variables, no peak was apparent and so no initial threshold could be chosen through this method.

Figure of merit plot for cut0

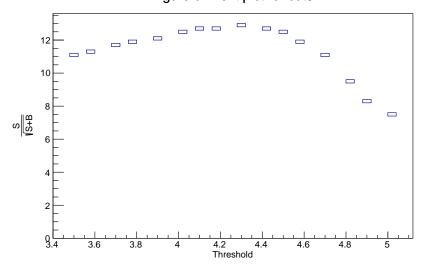


Figure 7.1: Figure-of-merit plot for $p_{\text{signal}}^{\text{CM}}$.

Initial visual inspection was performed by finding obvious separation between signal and many background variables. This was informed by knowledge of event signatures (Chapter 5), as well as some figure-of-merit plots as described above. Figures XXXX and XXXXX are examples of good and poor selection variables. In Figure XXXX, large background peaks occuring at less than $1\,\mathrm{GeV/c}$ and greater than $4.3\,\mathrm{Gev}$ lead to great separation from signal, which does not peak anywhere in those regions. Figure XXXX offers less than optimal threshold positions, as there is no apparent way to remove any amount of background without also removing a large amount of signal; note that this variable was not included during event selection.

Centre-of-mass µ momentum

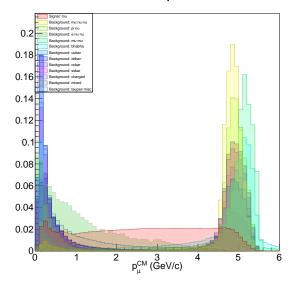


Figure 7.2: Center-of-mass frame momentum of signal track.

Cosine of polar angle of missing momentum

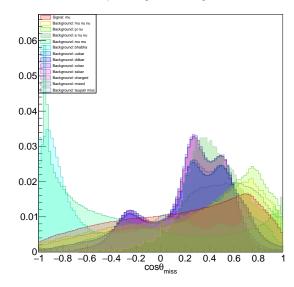


Figure 7.3: Cosine of polar angle of missing momentum.

7.1 Selection variables

Table 7.1 shows the number of signal and background events remaining after selection has been applied. Specific discussion and justification of selection criteria is given below.

Event process	events generated	events out
$ au o \mu \gamma$	135	6
$ au o \mu \nu u$	631235	163
$ au o \pi u$	822028	40
$\tau \to e \nu \nu$	70675	0
$\tau \to \text{generic}$	636954	0
$e^+e^- \to \mu^+\mu^-(\gamma)$	21938180	15
$e^+e^- \rightarrow e^+e^-(\gamma)$	1457005758	0
$e^+e^- \to u\bar{u}$	29767142	9
$e^+e^- \to d\bar{d}$	7307320	3
$e^+e^- \to c\bar{c}$	23401910	0
$e^+e^- \to s\bar{s}$	6299797	3
$e^+e^- \rightarrow B^+B^-$	22083348	0
$e^+e^- o B^0 \bar{B}^0$	23372366	0

Table 7.1: Events remaining after selection (muon mode)

7.1.1 Energy-momentum

I need some way to say this without saying "we require" repeatedly. Could borrow from Hayasaka-san

We require $p_{\mu}^{\rm CM}$ greater than $1\,{\rm GeV/c}$ and less than $4.3\,{\rm GeV/c}$, to remove low-momentum tracks from continuum events and to remove high-momentum tracks from leptonic processes without high-energy final state photons, that is, generic tau-pair processes, mu-pair processes, and bhabha. Muon transerve momentum $p_{\mu}^{\rm t}$ is required to be greater than $0.1\,{\rm GeV/c}$; tracks with a lesser transverse momentum could not reach the CDC sub-detector component so we do not select these events. Low-energy tracks from continuum events often do not satisfy this criteria, however most low-energy tracks are excluded through selection on $p_{\mu}^{\rm CM}$. To suppress $\mu^+\mu^-$ and Bhabha backgrounds we require center-of-mass momentum of the tag track $p_{\rm tag\,track}^{\rm CM}$ less than $2.5\,{\rm GeV}$. Through conservation of momentum we expect the signal and tag tracks of the processes $e^+e^- \to \ell^+\ell^-(\gamma)$ we to have momentum peaks around $5\,{\rm GeV}$, which are excluded by this selection. Since most background processes reconstruct the signal photon from low-energy photons, we require the energy of the signal photon E_{γ} to be $0.8\,{\rm GeV}$. This selection criteria is effective in removing background events across different processes. Total energy in the center-of-mass frame $E_{\rm total}^{\rm CM}$ is required to be less than $12\,{\rm GeV}$ to suppress $\mu^+\mu^-$ events.

NOTE: variables I didn't use but could have used = $p_{\text{tag track}}^{\text{t}}$, p_{μ} , $E_{\text{sum}}^{\text{CM}}$

7.1.2 Angular relations

As discussed in Chapter 5, angular distributions of reconstruction particles depend strongly on the decay process and hence can be used as discriminating variables. For this analysis, $\cos \theta_{\mu}$ is required to be in the range -0.8 to 0.9 to suppress continuum, mupair and Bhabha processes.

Cosine of the signal photon polar angle $\cos \theta_{\gamma}$ is required to be less than 0.85. We require the polar angle of the reconstructed signal τ in the center-of-mass frame to be between 1 and 2.2. Note that these variables are correlated and overlap in the background which is removed by this selection. Selection is also made on the cosine of the helicity angle $\cos \theta_{\rm H}$, requiring $-0.8 < \cos \theta_{\rm H} < 0.8$. The helicity angle is the opening angle between the signal muon in the signal τ frame, and the boost direction of the τ in the center-of-mass frame.

7.1.3 Particle likelihoods

Signal-side tracks are identified as muons by requiring $\mathcal{L}_{\mu} > 0.8$. To reduce the effect of double-counting, mostly for signal events, we require $\mathcal{L}_{K} < 0.08$ and $\mathcal{L}_{e} < 0.005$. We also require $\mathcal{L}_{\pi} > 0.8$. On the tag-side, we require $\mathcal{L}_{\mu} < 0.85$ to identify the tag-track as not a muon. Definitions of particle likelihoods and related plots are discussed at Section 2.6.

7.1.4 Background suppression using event shape

The thrust axis for a collection of N particles with momenta \mathbf{p}_i (i = 1, ..., N) is defined as the unit vector along with the total projection of these momenta is maximised. The thrust scalar, or thrust, is defined as

$$T = \frac{\sum_{i=1}^{N} |\mathbf{T} \cdot \mathbf{p}_i|}{\sum_{i=i}^{N} |\mathbf{p}_i|}.$$
 (7.1)

Signal thrust and rest-of-event thrust variables are used for selection. The signal thrust axis is constructed from all particles used to reconstruct the signal-side τ ; for our signal mode these are the signal muon and signal photon. On average these particles have similar momentum and a small opening between them, so that signal thrust has a clear peak around 0.942. We consider the signal thrust axis for the other dominant leptonic processes. For most events the signal-side is reconstructed from a high-energy charged track and a low-energy photon generated from bremsstrahlung, beam background or similar (radiative mu-pair or Bhabha events can generate higher energy final-state photons). Regardless of opening angle, the difference in momentum between signal track and signal photon leads to signal thrust for this event peaking around 1. A requirement for signal thrust to be in the range 0.936 to 0.944 to suppress leptonic backgrounds as shown in Figure 7.4.

We construct another thrust axis is also built using rest-of-event (ROE) data. ROE comprises all tracks and clusters not associated with the signal-side reconstruction, and so ROE thrust is influenced by tag-side events. Hadronic processes such as $B\bar{B}$ events and continuum have on average a lower rest-of-event thrust than leptonic processes due to the number of tracks and photons produced due to interactions with the detector. The magnitude of this ROE thrust vector is required to be in the range from 0.85 and 0.98. As shown in Figure XXXX, events produce very clean Gaussian-like distributions with little trailing tail. As such, while this selection removes a non-negligible amount of signal, it suppresses continuum events very strongly and almost completely excludes $B\bar{B}$ events. Event selection is also performed using the angle between thrust axes. We require the cosine of the angle between the signal thrust vector and rest-of-event thrust vector to be greater than 0.7.

Several continuum suppression variables were chosen by inspection after many more obvious criteria had been applied. These are CLEO cones, Super Fox-Wolfram moments, and the

Magnitude of thrust vector

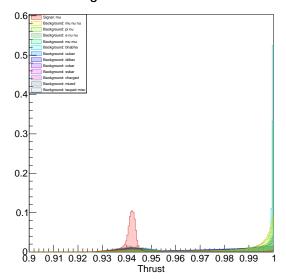


Figure 7.4: Signal thrust.

Magnitude of rest-of-event thrust axis

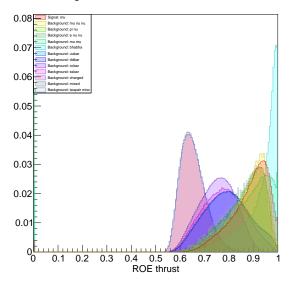


Figure 7.5: Rest-of-event thrust.

reduced Fox-Wolfram moment (the ratio of the second to the zeroth Fox-Wolfram moments).

Inherent differences in event shape can be used to suppress backgrounds. Some useful disciminant variables are the CLEO cones, named as such due to being introduced in a 1995 paper by the CLEO collaboration (REF). To calculate these variables, the space around the signal thrust axis is divided into cones at nine polar angle intervals of 10° each, with the i^{th} interval covering angles from $(i-1)\times 10^{\circ}$ to $i\times 10^{\circ}$ from the thrust axis (see Figure 7.6). Forward and backward intervals are combined. CLEO cone variables cci are defined as the lab-frame momentum flow of the i^{th} cone; momentum flow in each cone is calculated as the scalar sum of all tracks and clusters in that cone. Requirements on CLEO cones are given in Table 7.7.

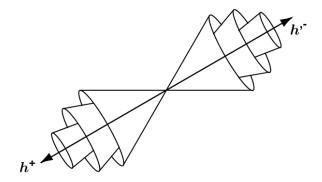


Figure 7.6: Illustration of CLEO cones.

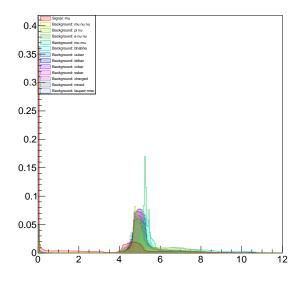
CLEO cone	lower	upper
cc1	_	5
cc2	2.4	_
cc3	_	_
cc4	_	1.7
cc5	_	0.9
cc6	_	0.7
cc7	_	0.5
cc8	_	_
cc9	_	0.4

Figure 7.7: CLEO cone selection criteria.

Fox-Wolfram moments (FWM) are event shape variables which describe energy flow from high-energy particle collision events, introduced to describe e^+e^- annihilation event shapes. Variables h_i^{so} (i=2,4) and h_i^{oo} are the normalised FWM, defined as

$$h_l^k = \frac{\sum_{m,n} |\vec{p_m}| |\vec{p_n}| P_l(\cos \theta_{mn})}{\sum_{m,n} |\vec{p_m}| |\vec{p_n}|},$$
(7.2)

Cleo cone 2



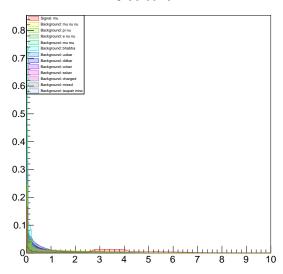


Figure 7.8: CLEO cone 1.

Figure 7.9: CLEO cone 2.

where $\vec{p_m}$ and $\vec{p_n}$ are the momenta of particles m and n and $P_l(\cos\theta_{mn})$ is the l-th other Legendre polynomial of cosine of the angle θ_{mn} between $\vec{p_m}$ and $\vec{p_n}$. We categorise the type of FWM with k = so, oo. For h_i^{so} , m is from signal particles and n is from ROE; for h_j^{oo} both m and n are from ROE.

\mathbf{FWM}	lower	upper
Hso(0,0)	0.05	1
Hso(0,1)	-0.05	0.3
Hso(0,2)	_	0.48
Hso(0,3)	-0.1	0.25
Hso(2,0)	-0.1	1
Roo(1)	-0.018	0.08
Roo(3)	-0.01	0.007

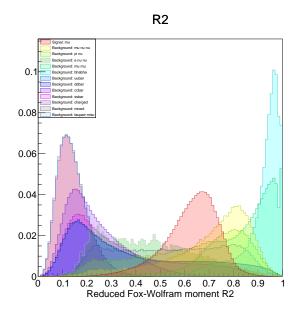
Table 7.2: Super Fox-Wolfram moment selection criteria

Note: not entirely sure what Hso(0,0) etc. means

Two other event shape variable requirement are required on the reduced Fox-Wolfram moment R_2 — the ratio of the second to the zeroth Fox-Wolfram moments — and the cosine of the angle between the signal thrust axis and the beam axis $\cos \theta_{\rm TBz}$. We require $R_2 > 0.4$ and $\cos \theta_{\rm TBz} < 0.8$, with both variables providing good background suppression as seen from Figures 7.10 and 7.11.

7.1.5 Remaining criteria

We require the number of reconstructed tracks to be less than 15 to suppress hadronic backgrounds; discussion of track counting is found in Section XXXXX. Selection is also made on the total energy deposited across all ECL clusters by neutral particles, in the range of 2 to 6 GeV to suppress XXXXXXX. The ratio of energies in the inner 3x3 and 5x5 cells of the ECL,



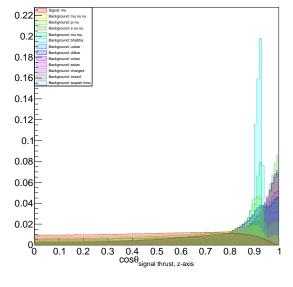


Figure 7.10: Reduced Fox-Wolfram moment R_2 .

Figure 7.11: Cosine of the angle between the thrust axis of the signal track and z-axis.

or E9E25, peaks close to 1 for the signal mode, since the signal photon carries a large fraction of total energy deposited in the ECL. We require E9E25 greater than 0.95 to suppress tau-pair backgrounds.

The emission of a photon after the short τ lifetime via $\tau \to \mu \gamma$ gives cluster timing peak around zero with a tight width, so we require this variable to be in the range $-1\,\mathrm{ns}$ to $1\,\mathrm{ns}$. POCA STUFF: Point-of-closest-approach (POCA); $-0.05 < d_0 < 0.05, -0.06 < z_0 < 0.06$; signed distance to the POCA in the r-phi plane; z coordinate of the. These impact parameter variables become more important when analysing actual data rather than MC, due to XXXXXX. Hence while these selection criteria to not discriminate background in a major way in MC, they may become more important when running over Belle II data.

Total energy of all neutral ECL clusters

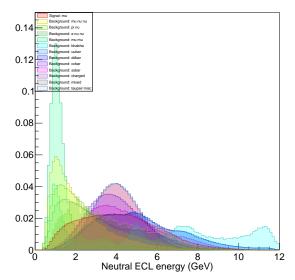


Figure 7.12: Total energy deposited in ECL clusters by neutral particles.

d0 of signal track

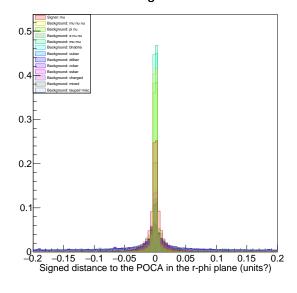


Figure 7.14: Point-of-closest approach - D0.

No. of tracks

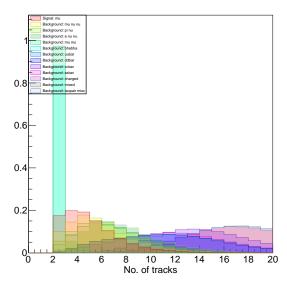


Figure 7.13: Number of reconstructed tracks.

z0 of signal track

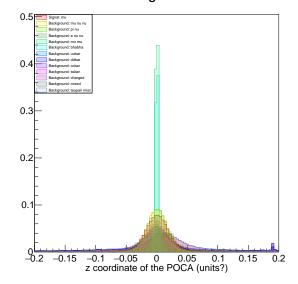


Figure 7.15: Point-of-closest approach - Z0.

variable	description
	CM momentum of signal track
$p_{ m signal}^{ m CM} \ p_{ m tag}^{ m CM}$	CM momentum of tag track
$p_{t ext{ signal}}$	Transverse momentum of signal track
	Transverse momentum of tag track
$p_{t \text{ tag}} \\ \cos \theta_{ ext{signal}}$	Cosine of polar angle of signal track
$\cos heta_{ m tag}$	Cosine of polar angle of tag track
$E_{ m total}^{ m CM}$	Center-of-mass energy of total system
$t_{ m total} \atop thrust_{ m signal}$	Magnitude of signal thrust vector*
μ -ID $_{ m signal}$	μ PID of signal track
μ -ID $_{ m signal}$	μ PID of tag track
E_{γ}	Energy of signal photon
$\cos \theta_{\gamma}$	Cosine of polar angle of signal photon
$\cos heta_{ ext{signal}-\gamma}^{\gamma}$	Cosine of center-of-mass frame angle between signal track and signal photon
$F^{\text{COS } v}_{\text{signal} - \gamma}$	
$E_{\mathrm{sum}}^{\mathrm{CM}}$	Center-of-mass energy of photons and tracks
$\cos \theta_{ m signal, \ tag \ track}^{ m CM}$	Opening angle between signal and tag track
$\cos heta_{ m H}$	Cosine of the helicity angle
n_{tracks}	Number of charged tracks
$\text{K-ID}_{\text{signal}}$	K PID of signal track
π -ID _{signal}	π PID of signal track
e-ID _{signal}	e PID of signal track
clusterTiming	timing of this cluster
cosTBz	Cosine of the angle between the signal thrust axis and z-axis
cosTBTO	Cosine of the angle between the signal thrust axis and ROE thrust axis
thrust _{ROE}	Rest-of-event thrust
tauCMtheta	Center-of-mass frame polar angle of reconstructed signal τ
E _{neutral ECL}	Energy in ECL clusters deposited by neutral particles
sigD0	D0 of signal track
$\operatorname{sig}\mathbf{Z}0$	Z0 of signal track
cc1	Cleo cone 1
cc2	Cleo cone 2
cc4	Cleo cone 4
cc5 cc6	Cleo cone 5 Cleo cone 6
$egin{array}{c} cc7 \\ cc9 \\ \end{array}$	Cleo cone 7 Cleo cone 9
${ m hso}00 \ { m hso}01$	Hso(0,0) Hso(0,1)
hso01	Hso(0,1) $Hso(0,2)$
hso03	
hso 20	Hso(0,3) Hso(2,0)
hoo1	R(1)
hoo2	R(1) $R(2)$
hoo4	R(4)

Table 7.3: Selection criteria

8 | Signal region analysis

After selection, we are left with a far reduced number of background events and a non-zero amount of expected signal events. We can now analyse events within the signal region. This is a region in ΔE vs $M_{\rm inv}$ space, with $-0.4 < \Delta E < 0.2$, and $1.65 < M_{\rm inv} < 1.85$.

 ΔE and $M_{\rm inv}$ are fit with asymmetric Gaussians to determine mean and σ . We find mean $\Delta E \approx 47\,{\rm MeV}$ and $M_{\rm inv} \approx 1.79\,{\rm GeV/c^2}$; this is consistent with our expectation of $\Delta E \sim 0$ and $M_{\rm inv} \sim m_{\tau}$. The signal region is shown in Figure 8.1, with signal and background MC distributions overlayed.

Signal region with tauMG MC

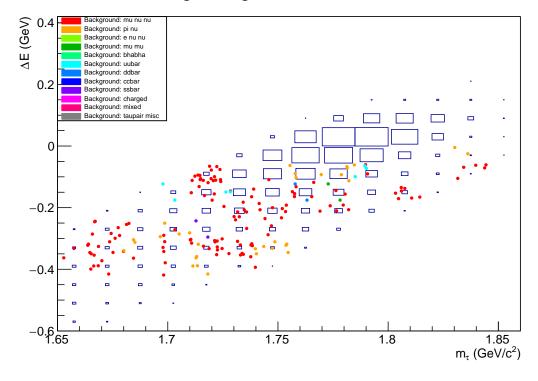


Figure 8.1: $M_{\rm inv} - \Delta E$ signal region for $\tau \to \mu \gamma$. Shaded boxes is the event distribution for $\tau \to \mu \gamma$; dots are unscaled background events.

In the entire signal region we find 6 $\tau \to \mu \gamma$ events, and 163 $\tau \to \mu \nu \nu$ events, 40 $\tau \to \pi \nu$ events, 15 $e^+e^- \to \mu^+\mu^-(\gamma)$ events, 9 $e^+e^- \to u^+u^-$ events, 3 $e^+e^- \to d^+d^-$ events, and 3 $e^+e^- \to s^+s^-$ events. This totals to 6 signal events and 232 ± 1 background events. We then produce a rotated plot to decorrelate the x- and y-axes. In this plot we set a elliptical region of phase space centred near the means for $M_{\rm inv}$ and ΔE . The selected signal region contains 0

Rotated signal region with $\tau \rightarrow \mu \gamma$ MC

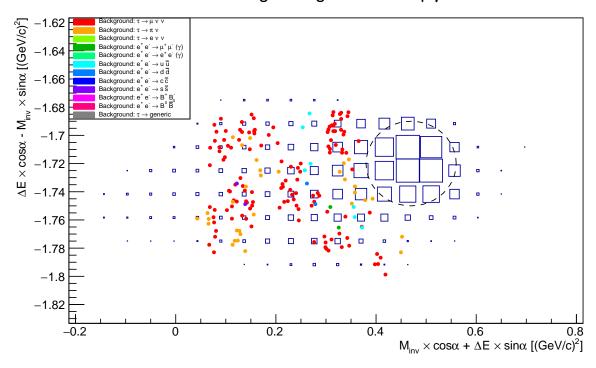


Figure 8.2: Rotated $M_{\rm inv} - \Delta E$ signal region for $\tau \to \mu \gamma$. Shaded boxes is the event distribution for $\tau \to \mu \gamma$; dots are unscaled background events coloured according to the legend. $\alpha = 72^{\circ}$. The dotted ellipse represents a region of 3.811(59) signal events and 0 background events.

background events and has a signal efficiency of 4.59%.

To determine an upper limit on the branching fraction of $\tau \to \mu \gamma$, we select a smaller section of the total signal region. We define $n_{\text{upper limit}}$ as the upper limit of events expected in our signal region — that is, the number of background events from MC – and n_{τ} as the number of τ 's expected in a $1\,\mathrm{ab^{-1}}$ luminosity sample at Belle II. Assuming that the background is Poisson distributed, we expect $n_{\text{upper limit}} = 2.30$ at 90 % confidence limit (CL). We calculate an upper limit on the branching fraction of $\tau \to \mu \gamma$ as

$$\mathcal{B}(\tau \to \mu \gamma) < \frac{n_{\text{upper limit}}}{\epsilon \times n_{\tau}}, \tag{8.1}$$

$$= \frac{2.30}{4.59 \% \times 9190000000 \times 2}, \tag{8.2}$$

$$=\frac{2.30}{4.59\% \times 919\,000\,000 \times 2},\tag{8.2}$$

$$=2.726\times10^{-8}. (8.3)$$

This is value is an improvement on the $\tau \to \mu \gamma$ branching fraction determined at Belle,

$$\mathcal{B}(\tau \to \mu \gamma)_{\text{Belle, 2010}} < 4.5 \times 10^{-8}$$
.

Comparable values of branching fraction is a strong indicator of good reconstruction and event selection performance at Belle II, especially with greater beam background than at Belle.

9 Conclusion

We performed a study of LFV modes $\tau \to \ell \gamma$ on an $1\,\mathrm{ab^{-1}}$ sample of Belle II MC comprising a range of backgrounds, which were reconstructed and simulated in basf2 using Belle II energies and geometries. The signal electron in the mode $\tau \to e\gamma$ was poorly reconstructed, so most of the analysis focused on $\tau \to \mu \gamma$. Following selection over forty variables, we were able to provide and upper limit to the branching fractions,

$$\mathcal{B}(\tau \to \mu \gamma) < 2.726 \times 10^{-8} \text{ at } 90 \% \text{ CL},$$

with a signal efficiency of 4.59 % and 3.8119 events in our selected signal region. This branching fraction is consistent with previously determined upper limits on $\tau \to \mu \gamma$.

9.1 Future work

Selection criteria could be optimised to increase signal efficiency through use of XXXXX, such as the Toolkit for Multivariate Analysis (TMVA). Additional selection variables could be investigated, in particular those related to missing mass and momenta which were key variables in Belle's 2010 analysis. Signal region analysis can be extended to utilise $M_{\rm inv}$ and ΔE resolutions and provide a statistics-motivated signal region. Fitting of probability density functions (PDFs) to background MC in the signal region would be useful.

The framework set up over the course of the analysis allows for the work to be extended to run over Belle data. The full data set of $1 \, \text{fb}^{-1}$ is available, and it is possible for this data to be reconstructed in basf2 after conversion from the Belle data format to the Belle II data format. Previous searches at Belle have used $200 \, \text{fb}^{-1}$ (???) and $535 \, \text{fb}^{-1}$ luminosity data samples; a search over higher luminosity could improve the accuracy of some τ LFV branching fractions due to increase statistics, as well as possibly improved reconstruction and selection techniques.

Issues with electron reconstruction were a constant in this analysis, most notably in the reconstruction of the mother τ in signal $\tau \to e \gamma$ events. Further research to determine the cause of these errors would be beneficial; full signal region analysis of $\tau \to e \gamma$ could become possible.

9.2 Expected impact on Belle II

This research is the first to investigate τ LFV at Belle II using full analysis of MC. It will serve as a reference for future τ LFV searches on actual data. Improved reconstruction from Belle was evident, as good signal separation was obtained despite greatly increase beam background. This helps validate work done towards beam background mitigation at Belle II. Hints of electron

reconstruction	onumber not onumber	performing	at	${\it expected}$	levels	could	lead	to	an	improvement	with	future
updates of basf	2.											

Bibliography

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