

In the relevant probability space $(\Omega, \mathcal{F}, \mathbb{P})$, define the filtration

$$\mathcal{F}_0 = \sigma(\{D_i(0) : i = 1, 2\}),$$

and, $\mathcal{F}_t = \sigma(\{D_i(s) : 0 \leq s \leq t, 1 \leq i \leq s + 2\}) \quad \forall t \geq 1.$

We now find the conditional expectation $\mathbb{E}(D_i(t + 1) \mid \mathcal{F}_t)$.

$$\begin{aligned} \mathbb{E}(D_i(t + 1) \mid \mathcal{F}_t) &= \mathbb{E}(D_i(t) + D_i(t + 1) - D_i(t) \mid \mathcal{F}_t) \\ &= D_i(t) + \mathbb{E}(D_i(t + 1) - D_i(t) \mid \mathcal{F}_t). \end{aligned}$$