In [77]: #Import libraries from sklearn.cluster import AgglomerativeClustering from scipy.cluster.hierarchy import dendrogram, linkage from matplotlib import pyplot as plt from sklearn.metrics import silhouette samples, silhouette score import matplotlib.cm as cm import numpy as np import pandas as pd #MinMaxScaler from sklearn.preprocessing import MinMaxScaler df als = pd.read csv("als data.csv") df als.head() In [79]: Albumin_max Albumin_median Albumin_min Out [79]: ID Age_mean Albumin_range ALSFRS_slope ALSFRS_Total_max ALSFRS_Total_me 0.066202 -0.965608 2 48 45.0 41.0 39.0 0.010453 -0.921717 37 24 2 3 50.0 47.0 45.0 0.008929 -0.914787 38 3 47.0 44.0 41.0 0.012111 -0.598361 30 63 63 47.0 45.5 42.0 0.008292 -0.444039 32 5 rows × 101 columns Remove any data that is not relevant to the patient's ALS condition df als = df als.drop(columns={'ID', 'SubjectID'}, axis=1) In [80]: In [81]: df als.head() Out[81]: Age_mean Albumin_max Albumin_median Albumin_min Albumin_range ALSFRS_slope ALSFRS_Total_max ALSFRS_Total_median 0 65 57.0 40.5 38.0 0.066202 -0.965608 30 28.0 48 45.0 41.0 39.0 0.010453 -0.921717 37 33.0 50.0 47.0 45.0 0.008929 -0.914787 3 63 47.0 44.0 41.0 0.012111 -0.598361 30 29.0 63 47.0 45.5 42.0 0.008292 -0.444039 32 27.5 5 rows × 99 columns Apply a standard scalar to the data In [82]: #Initialize MinMaxScaler scaler = MinMaxScaler() # transform data scaled data = scaler.fit transform(df als) In [83]: scaled_data array([[0.74603175, 0.6006006 , 0.36144578, ..., 0.25 , 0.25 Out[83]: 0.33333333], [0.47619048, 0.24024024, 0.39156627, ..., 0.5], 0.], [0.31746032, 0.39039039, 0.75301205, ..., 0.25], 0. 0.], [0.46031746, 0.27027027, 0.57228916, ..., 1. , 0.25 [0.3015873 , 0.36036036, 0.57228916, ..., 0.25 , 0. 0.], [0.47619048, 0.33033033, 0.63253012, ..., 0. , 0. 0.]]) Create a plot of the cluster silhouette score versus the number of clusters in a K-means cluster In [84]: #Import libraries from sklearn.cluster import KMeans from sklearn.metrics import silhouette_samples, silhouette_score import matplotlib.cm as cm In [85]: range_n_clusters = [2, 3, 4, 5, 6, 8] for n clusters in range_n_clusters: # Create a subplot with 1 row and 2 columns fig, (ax1, ax2) = plt.subplots(1, 2)fig.set_size_inches(18, 7) # The 1st subplot is the silhouette plot # The silhouette coefficient can range from -1, 1 but in this example all # lie within [-0.1, 1] ax1.set xlim([-0.1, 1]) # The (n_clusters+1) *10 is for inserting blank space between silhouette # plots of individual clusters, to demarcate them clearly. $ax1.set_ylim([0, len(df_als) + (n_clusters + 1) * 10])$ # Initialize the clusterer with n clusters value and a random generator # seed of 10 for reproducibility. clusterer = KMeans(n clusters=n clusters, random state=10) cluster_labels = clusterer.fit_predict(df_als) # The silhouette_score gives the average value for all the samples. # This gives a perspective into the density and separation of the formed # clusters silhouette avg = silhouette score(df als, cluster labels) print("For n clusters =", n clusters, "The average silhouette score is :", silhouette avg, # Compute the silhouette scores for each sample sample silhouette values = silhouette samples(df als, cluster labels) $y_lower = 10$ for i in range(n clusters): # Aggregate the silhouette scores for samples belonging to # cluster i, and sort them ith_cluster_silhouette_values = sample_silhouette_values[cluster_labels == i] ith_cluster_silhouette_values.sort() size cluster i = ith cluster silhouette values.shape[0] y_upper = y_lower + size_cluster_i color = cm.nipy_spectral(float(i) / n_clusters) ax1.fill betweenx(np.arange(y_lower, y_upper), ith_cluster_silhouette_values, facecolor=color, edgecolor=color, alpha=0.7, # Label the silhouette plots with their cluster numbers at the middle $ax1.text(-0.05, y_lower + 0.5 * size_cluster_i, str(i))$ # Compute the new y_lower for next plot y_lower = y_upper + 10 # 10 for the 0 samples ax1.set_title("The silhouette plot for the various clusters.") ax1.set xlabel("The silhouette coefficient values") ax1.set_ylabel("Cluster label") # The vertical line for average silhouette score of all the values ax1.axvline(x=silhouette avg, color="red", linestyle="--") ax1.set yticks([]) # Clear the yaxis labels / ticks ax1.set_xticks([-0.1, 0, 0.2, 0.4, 0.6, 0.8, 1]) # 2nd Plot showing the actual clusters formed colors = cm.nipy_spectral(cluster_labels.astype(float) / n_clusters) ax2.scatter(df als.iloc[:, 0], df als.iloc[:, 1], marker=".", s=30, lw=0, alpha=0.7, c=colors, edgecolor="k" # Labeling the clusters centers = clusterer.cluster centers # Draw white circles at cluster centers ax2.scatter(centers[:, 0], centers[:, 1], marker="o", c="white", alpha=1, s=200,edgecolor="k", for i, c in enumerate(centers): ax2.scatter(c[0], c[1], marker="\$%d\$" % i, alpha=1, s=50, edgecolor="k")ax2.set title("The visualization of the clustered data.") ax2.set xlabel("Feature space for the 1st feature") ax2.set_ylabel("Feature space for the 2nd feature") plt.suptitle("Silhouette analysis for KMeans clustering on sample data with n clusters = %d" % n clusters, fontsize=14, fontweight="bold", plt.show() For n clusters = 2 The average silhouette score is : 0.5646624453149653For n clusters = 3 The average silhouette score is: 0.46074229932446703 For n clusters = 4 The average silhouette score is: 0.37737357000015487 For n clusters = 5 The average silhouette score is : 0.3195837892820233For n clusters = 6 The average silhouette score is: 0.28880834686513246 For n_clusters = 8 The average silhouette_score is : 0.24945193518394654 Silhouette analysis for KMeans clustering on sample data with n_clusters = 2 The silhouette plot for the various clusters. The visualization of the clustered data 70 65 the 2nd feature 60 1 Cluster labe 55 space for 50 **(1)** 50 0.4 The silhouette coefficient values Feature space for the 1st feature Silhouette analysis for KMeans clustering on sample data with n_c clusters = 3 The silhouette plot for the various clusters. The visualization of the clustered data 70 65 Feature space for the 2nd feature 60 Cluster label 50 45 40 0 -0.1 0.0 0.2 0.6 The silhouette coefficient values Feature space for the 1st feature Silhouette analysis for KMeans clustering on sample data with n_clusters = 4 The silhouette plot for the various clusters. The visualization of the clustered data 70 65 Feature space for the 2nd feature 60 Cluster labe 55 50 45 40 0.2 20 Silhouette analysis for KMeans clustering on sample data with n_c lusters = 5 The visualization of the clustered data The silhouette plot for the various clusters. 70 65 Feature space for the 2nd feature 60 Cluster labe 55 45 -0.1 0.0 0.6 The silhouette coefficient values Silhouette analysis for KMeans clustering on sample data with n_clusters = 6 The visualization of the clustered data The silhouette plot for the various clusters. 65 Feature space for the 2nd feature Cluster label 45 0 0.6 0.8 80 -0.1The silhouette coefficient values Silhouette analysis for KMeans clustering on sample data with n_c clusters = 8 The silhouette plot for the various clusters The visualization of the clustered data 70 65 Feature space for the 2nd feature 60 Cluster label 55 45 0.8 30 50 0.6 The silhouette coefficient values Feature space for the 1st feature Use the plot created in (3) to choose on optimal number of clusters for K-means. Justify your choice Silhouette score represents the similarity of objects within the clusters. Silhouette score rangese from -1 to 1. Higher score indicates that the object is well matched. In our case, n_cluster = 2 has the highest score (0.564) amongst others. As n_cluster value increases silhouette_score decreases. We can confirm that n_clusters 3 and above are bad choices and n_clusters = 2 is the best choice. Optimal number of clusters for K-means is 2 i.e., n_clusters = 2 Fit a PCA transformation with two features to the scaled data In [119... from sklearn.decomposition import PCA pca = PCA(n_components = 15) Fit a K-means model to the data with the optimal number of clusters chosen in part (4) In [120... X_pca = pca.fit_transform(scaled_data) kmeans = KMeans(n clusters=2, random state=10) y pred = clusterer.fit predict(scaled data) Make a scatterplot the PCA transformed data coloring each point by its cluster value In [121... | plt.scatter(X_pca[:,0], X_pca[:,1], c=y_pred) plt.title('PCA Data Scatterplot for n clusters = 2') plt.show() PCA Data Scatterplot for n_clusters = 2 1.5 1.0 0.5 0.0 -0.5-1.0In [122... # Show the variance between the two features within the PCA. explained_variance = pca.explained_variance_ratio_ explained variance array([0.24005692, 0.1304401 , 0.09912642, 0.05770486, 0.05151021, Out[122]: 0.04085792, 0.02907999, 0.02785823, 0.02569873, 0.02296304, 0.01747365, 0.01571195, 0.01429157, 0.01253185, 0.01179188]) In [133... print ("Components: ", pca.n_components_ , "\nExplained Variance Ratio: ", round (pca.explained variance ratio .sum(),2), "\nExplained Variance Ratio Percentage: ", round((pca.explained variance ratio .sum()*100),0), "%") Components: 15 Explained Variance Ratio: 0.8 Explained Variance Ratio Percentage: 80.0 % Summarize your results and make a conclusion. Explained Variance Ratio is a metric to evaluate the usefulness of principal components and to choose how many components to use in PCA model. Ideally, we need to choose the number of components to include in your model by adding the explained variance ratio of each component until you reach a total of around 0.8 or 80% to avoid overfitting. I have used trial and error method to get the explained ratio by increasing the n_components from 2 to 15. While if we are choosing n_components as 16, its going over 81%. So, I have choosen 15 as the best n_components for PCA.