

① Given an array of $[4, -2, 5, 3, 10, -5, 2, 8, -3, 6, 7, -4, 1, 9, -1, 0, -6, 8, 11, 9]$ integers. Find the maximum and minimum Product that can be obtained by multiply two integers from the array.

Sol: array is $[4, -2, 5, 3, 10, -5, 2, 8, -3, 6, 7, -4, 1, 9, -1, 0, -6, 8, 11, 9]$
we need to consider the target and smallest product that can be formed by selecting two consider from the array.

1) Sort the array.

Sorted array

$[-9, -8, -6, -5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11]$

Identify the possible candidates for maximum product

Identify the possible candidates for minimum product

calculating maximum product:

\Rightarrow The two longest positive numbers and $10 \times 11 = 110$.

\Rightarrow The two smallest negative numbers are -9 and $-8 = 72$

The maximum product is 0.

calculating minimum product:

The largest positive and negative number 11 and -9.

$$11 \times -9 = -99$$

The smallest positive and negative numbers are $-9 \times 8 = -72$

-99 is smaller than -72

maximum product = 110, and minimum product = -99

② Demonstrate the priority search method to search for the key = 23 from the array = {2, 5, 8, 12, 16, 25, 38, 56, 72, 91}

Sol) Given array = {2, 5, 8, 12, 16, 23, 38, 56, 72, 91}

1. Initialize pointers

$$\text{low} = 0 \text{ and } \text{high} = 9$$

$$\text{calculate mid} = \left\lfloor \frac{\text{low} + \text{high}}{2} \right\rfloor = \frac{0 + 9}{2} = 4$$

Compare arr[mid] with key:

$$\text{arr}[4] = 16$$

Since $16 < 23$ update $\text{low} = \text{mid} + 1 = 5$

$$\text{calculate mid} = \left\lfloor \frac{\text{low} + \text{high}}{2} \right\rfloor = \frac{5 + 9}{2} = 7$$

Compare arr[mid] with key:

$$\text{arr}[7] = 56$$

Since $56 > 23$ update $\text{high} = \text{mid} - 1 = 6$

$$\text{mid} = \left\lfloor \frac{5 + 6}{2} \right\rfloor = 5$$

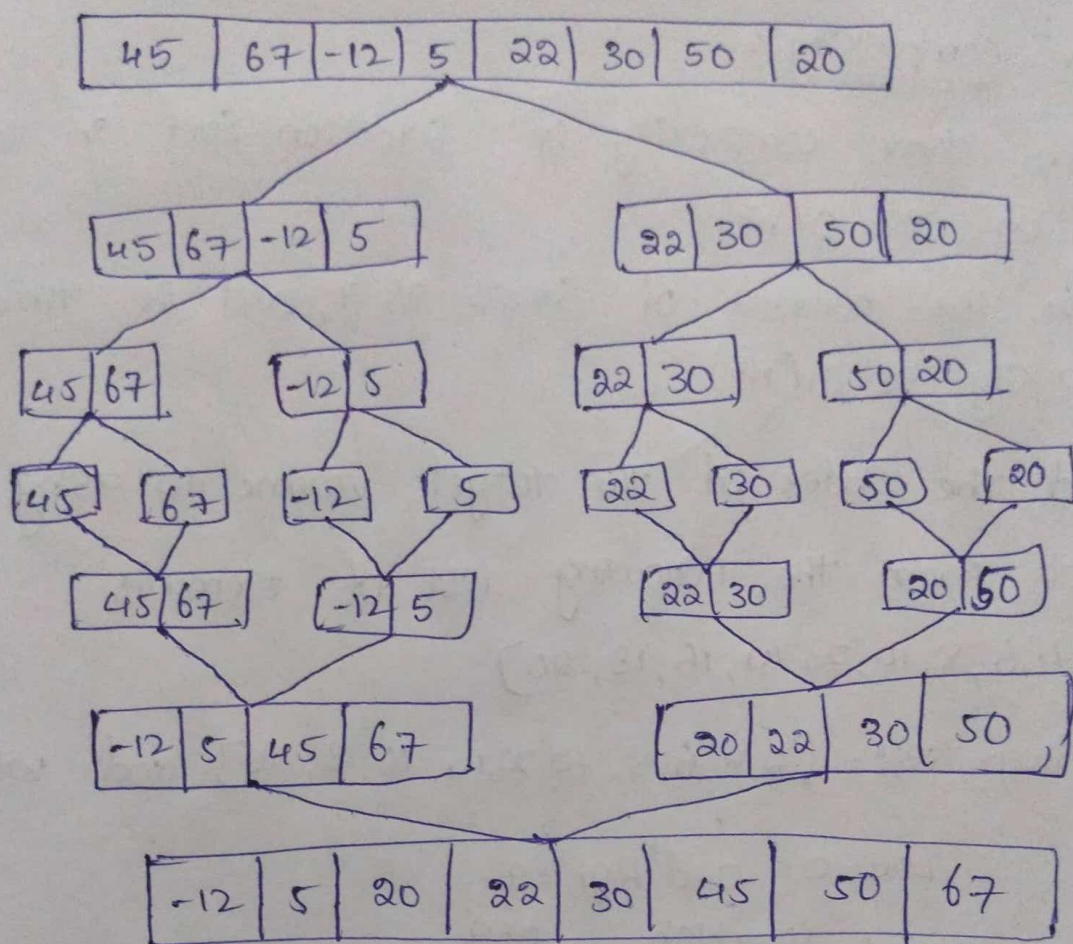
$$\text{arr}[\text{mid}] = \text{arr}[5] = 23$$

$23 == 23$ The is Found at index 5

\therefore The key = 23 is Found at index 5.

③ Apply merge sort and other list of 8 elements, data $d = \{4, 5, 6, 7, -12, 5, 22, 30, 50, 20\}$. Setup a recursive relation for the number of key comparison made by merge sort.

Sol: merge sort



∴ The Sorted list = (-12, 5, 20, 22, 30, 45, 50, 67)

(4) Find the no. of times to perform solving Swapping
For Selection Sort also estimate the time complexity
For the other of notation Set S(12, 7, 5, -2, 18, 6, 13, 4)

Sol: The selection sort algorithm always makes exactly $n-1$ swaps in the worst case, where n is the no. of elements in the list

given $S = \{12, 7, 5, -2, 18, 6, 13, 4\}$

NO. of elements, $n = 8$

No. of Swaps $n=8$, $n-1=7$

Time Complexity :-

The time complexity of Selection Sort in Big-O notation is $O(n^2)$

So, the numbers of Swaps is 7, and the time complexity is $O(n^2)$

⑤ Find the index of the target value 10 using binary search from the following list of elements

[2, 4, 6, 8, 10, 12, 14, 16, 18, 20]

Sol) Given list = [2, 4, 6, 8, 10, 12, 14, 16, 18, 20] and value = 10

Low = 0 and high = 9

$$\text{mid} = \frac{\text{low} + \text{high}}{2} = \frac{0 + 9}{2} = 4$$

Ex: = List(4), mid = 10 mid == value

Since $10 == 10$ the target is Found at index 4.

∴ The Target value = 10 is Found at index 4.