

Q.2. As Node A can hear the beacons located at (4,2) and (2,5) and Node B can hear beacons located at (2,5) and (3,7) we can find the distance b/w beacon points and the given position for the sensors. As the range is 2m the distance should be less than equal to 2m.

- for position (3, 3.5) for Node A.

a) the distance from (4,2) is

$$\begin{aligned} d &= \sqrt{(4-3)^2 + (2-3.5)^2} \\ &= \sqrt{1 + (-1.5)^2} \\ &= \sqrt{3.25} \\ &= 1.803 \end{aligned}$$

b) the distance from (2,5) is

$$\begin{aligned} d &= \sqrt{(2-3)^2 + (5-3.5)^2} \\ &= \sqrt{(-1)^2 + (1.5)^2} \\ &= \sqrt{1 + 2.25} \\ &= 1.803 \end{aligned}$$

• for position $(3, 4.5)$ for Node A

a) the distance from $(4, 2)$ is

$$d = \sqrt{(4-3)^2 + (2-4.5)^2}$$

$$= \sqrt{(1)^2 + (-2.5)^2}$$

$$= \sqrt{1 + 6.25}$$

$$= 2.693$$

b) the distance from $(2, 5)$

$$d = \sqrt{(2-3)^2 + (5-4.5)^2}$$

$$d = \sqrt{(-1)^2 + (0.5)^2}$$

$$d = \sqrt{1 + 0.25}$$

$$d = 1.118$$

Now the position of Node A is $(3, 3.5)$ as it can hear beacon at positions $(4, 2)$ and $(2, 5)$ and the distance from both this points to $(3, 3.5)$ is less than 2. \therefore the position is $(3, 3.5)$ as the other point has a distance > 2 from one of the beacon shown above.

• for position (2,6) for Node B.

a) the distance from (2,5) is

$$d = \sqrt{(2-2)^2 + (5-6)^2}$$

$$d = \sqrt{(1)^2}$$

$$d = 1$$

b) the distance from (3,7) is

$$d = \sqrt{(3-2)^2 + (7-6)^2}$$

$$d = \sqrt{1^2 + 1^2}$$

$$d = \sqrt{2}$$

$$d = 1.414$$

• for position (4,5) for Node B to position (3,7)

a)
$$d = \sqrt{(4-3)^2 + (5-7)^2}$$

$$= \sqrt{(1)^2 + (-2)^2}$$

$$= \sqrt{1+4}$$

$$= \sqrt{5}$$

$$d = 2.236$$

b) the distance from $(2,5)$ is .

$$d = \sqrt{(2-4)^2 + (5-5)^2}$$

$$d = \sqrt{(2)^2}$$

$$d = 2$$

\therefore As from the distance above it is clear that position for Node B is $(2,6)$ as the distance from both the beacons is less than 2 where this is not the case with position $(4,5)$. Hence position of B is $(2,6)$.

* In Addition this can also be verified by Node Centroid theory.

• the centroid for the two beacon for Node A is

$$= \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}$$

$$= \frac{4+2}{2}, \frac{5+2}{2}$$

$$= (3, 3.5)$$

\therefore the position of Node A is $(3, 3.5)$

• the Centroid for two beacons for Node B is

$$= \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}$$

$$= \frac{2+3}{2}, \frac{12}{2}$$

$$= (2.5, 6)$$

∴ the position for B has to be close to $(2.5, 6)$ which is $(2, 6)$ in this case hence the answers or position are verified.