

Q.6.

As the formula for getting the new data is as given

$$P(x=F|y_1^1, y_1^2) = \frac{P(x=F|y_1^1) P(x=F|y_1^2) P(x=F|y_0^1, y_0^2)}{P(F|y_0^1) P(F|y_0^2)} \quad - ①$$

∴ from ① we can get the value of $P(x=F|y_0^1, y_0^2)$ as

$$P(x=F|y_0^1, y_0^2) = \frac{P(x=F|y_1^1, y_1^2) \times P(F|y_0^1) P(F|y_0^2)}{P(x=F|y_1^1) P(x=F|y_1^2)} \quad - ②$$

using eq ② we can get the values for $x=F, x=M$ and $x=A$.

Now

• For $x=F$

$$P(x=F|y_0^1, y_0^2) = \frac{P(x=F|y_1^1, y_1^2) \times P(F|y_0^1) P(F|y_0^2)}{P(x=F|y_1^1) P(x=F|y_1^2)}$$

$$= \frac{0.88 \times 0.4 \times 0.6}{0.7 \times 0.8}$$

$$P(x=F|y_0^1, y_0^2) = 0.3771$$

• For $x = M$

$$P(x=M | y_0^1, y_0^2) = \frac{P(x=M | y_1^1, y_1^2) P(F|y_0^1) P(F|y_0^2)}{P(x=F|y_1^1) P(x=F|y_1^2)}$$

$$= \frac{0.11 \times 0.4 \times 0.3}{0.29 \times 0.15}$$

$$= 0.3034$$

• For $x = A$

$$P(x=A | y_0^1, y_0^2) = \frac{P(x=A | y_1^1, y_1^2) P(A|y_0^1) P(A|y_0^2)}{P(x=A|y_1^1) P(x=A|y_1^2)}$$

* Note: \rightarrow As in question the value of $P(x=A | y_1^1, y_1^2) = 0.2$ which exceeds the total value of more than 1 we have assumed it to be 0.02

Now using $P(x=A | y_1^1, y_1^2) = 0.02$ we get.

$$= \frac{0.02 \times 0.2 \times 0.1}{0.01 \times 0.05}$$

$$= 0.8$$

Now adding the probability to check value w.r.t 1.

$$= P(x=F|y_0^1, y_0^2) + P(x=M|y_0^1, y_0^2) + P(x=A|y_0^1, y_0^2)$$

$$= 0.3771 + 0.3034 + 0.8$$

$$= 1.4805$$

as the value is greater than 1 we will normalize it.

∴ Normalize values are

For $x = F$

$$P(x=F|y_0^1, y_0^2) = \frac{0.3771}{1.4805}$$

$$= 0.2547$$

For $x = M$

$$P(x=M|y_0^1, y_0^2) = \frac{0.3034}{1.4805}$$

$$= 0.2049$$

For $x = A$

$$P(x=A|y_0^1, y_0^2) = \frac{0.8}{1.4805}$$

$$= 0.5404$$

Now adding value to check closeness to 1.

$$= P(x=F|y_0^1, y_0^2) + P(x=M|y_0^1, y_0^2) + P(x=A|y_0^1, y_0^2)$$

$$= 0.2547 + 0.2049 + 0.5404$$

$$= 1$$

* Case : Note : As in question even with the value of 0.02 the total probability for the fixed Data exceeds 1. we take a value of $P(x=A|y_1^1, y_1^2) = 0.01$

∴ the new data is.

For $x=A$

$$P(x=A|y_0^1, y_0^2) = \frac{P(x=A|y_1^1, y_1^2) \cdot P(x=A|y_0^1) P(x=A|y_1^2)}{P(x=A|y_0^1) P(x=A|y_0^2)}$$

$$= \frac{0.01 \times 0.2 \times 0.1}{0.01 \times 0.05}$$

$$= 0.4$$

Now adding value to check if it is 1.

$$= P(x=F|y_0^1, y_0^2) + P(x=M|y_0^1, y_0^2) + P(x=A|y_0^1, y_0^2)$$

$$= 0.3771 + 0.3034 + 0.4$$

$$= 1.0805$$

\therefore we normalize the values as if exceeds 1.

\therefore

• For $x = F$

$$\begin{aligned} P(x = F | y_0^1, y_0^2) &= \frac{0.3771}{1.0805} \\ &= 0.3490 \end{aligned}$$

• For $x = M$

$$\begin{aligned} P(x = M | y_0^1, y_0^2) &= \frac{0.3034}{1.0805} \\ &= 0.2808 \end{aligned}$$

• For $x = A$

$$\begin{aligned} P(x = A | y_0^1, y_0^2) &= \frac{0.4}{1.0805} \\ &= 0.3702 \end{aligned}$$

Now adding to check

$$\begin{aligned} &= P(x = F | y_0^1, y_0^2) + P(x = M | y_0^1, y_0^2) + P(x = A | y_0^1, y_0^2) \\ &= 0.3490 + 0.2808 + 0.3702 \\ &= 1. \end{aligned}$$