2019W2_ELEC_221_201

Assignment Problem_Set_4 due 02/11/2020 at 11:59pm PST

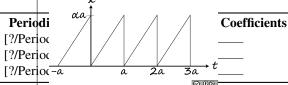
For each of the signals given in the table below, indicate whether cients, enter NA.

> Signal $12 + 10\cos(6\pi t) + 7\cos(18t + \frac{\pi}{5})$

 $[14 + \cos(2\pi t)]\sin(10\pi t + \frac{\pi}{5})$

 $4 + \sin(3t + \frac{\pi}{4}) + 15\cos(5t) + 10\cos(3t) + 11\sin(6t)$

it is periodic or not. For the periodic signals, write the following seven coefficients in a comma separated list as: X_0, X_1, X_2, X_3 , X_4 , X_5 , X_6 and enter 0 for each coefficient that you find to be zero. If it is not possible to calculate the Fourier Series coeffi-



• 0.866667*yp+y = x

and $\alpha = 3$.

1/(1+0.866667*j*w)

• 0.755689*cos(t+(-0.714091))

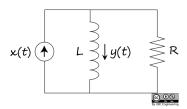
Correct Answers:

1

2

- Aperiodic
- NA
- Periodic
- 0, 0, 0, 0, $e^{(j*pi/5)/(4*j)}$, $14*e^{(j*pi/5)/(2*j)}$,
- Periodic
- 4, 0, 0, $e^{(j*pi/4)/(2*j)+5}$, 0, 7.5, 11/(2*j)

Consider an LTI system that is implemented as an RL circuit shown in the figure below $(R = 15 \Omega, L = 13 H)$. The input signal, x(t), is generated by the current source and the output, y(t), is measured as the current through the inductor.



a) Find the differential equation that describes this system.

To enter the first $(\frac{dy(t)}{dt})$ or second $(\frac{d^2y(t)}{dt^2})$ derivatives of a function y(t), use "yp" and "ypp" respectively. Also enter "y" for y(t).

b) Find the frequency response of the system, $H(\omega)$.

 $H(\omega) =$ Enter ω as w.

c) Suppose that the current source produces current x(t) =cos(t). What is the inductor's current?

$$y(t) =$$

Correct Answers:

a) Find an equation for $x_c(t)$, the signal that describes one cycle of x(t), in terms of the unit step function $u(t).x_c(t) =$

A periodic signal, x(t) is given in the figure below, where a = 7,

- \circ b) jFind \circ the 4Laplace transform, $X_c(s)$ of the signal in part $\mathbf{a}.X_c(s) = \underline{}$
- c) Calculate the Fourier Series coefficients of the signal x(t), X_k for $k \neq 0$ using the Laplace transform from part $\mathbf{b}.X_k = \underline{\hspace{1cm}}$
- **d)** Is it possible to find the Fourier Series coefficient, X_0 using the Laplace transform method? [?/Yes/No]e) Compute the Fourier Series coefficient, X_0 , using the integral definition. $X_0 = \underline{\hspace{1cm}}$

Part **d** will only be marked correct if part **c** is correct.

Correct Answers:

- 3*t*[u(t)-u(t-7)]
- $3*[1/(s^2)*[1-e^(-7*s)]-7/s*e^(-7*s)]$
- 21*j/(2*pi*k)
- No
- 10.5

The frequency response of an LTI system is:

$$|H(\omega)| = \begin{cases} 9 & |\omega| \le 5\\ 0 & otherwise \end{cases}$$

$$\angle H(\omega) = \begin{cases} -\frac{\pi}{5} & \omega \ge 0\\ \frac{\pi}{5} & \omega < 0 \end{cases}$$

Given a periodic input signal with the Fourier series of $x(t) = \sum_{k=1}^{\infty} \frac{3}{k^3} cos(\frac{8kt}{4})$, find the steady state response of the sys-

$$y_{ss}(t) =$$

Correct Answers:

• 27*[cos(8*t/4-pi/5)+0.125*cos(16*t/4-pi/5)]

JY Note Feb 7, 2020: A correction has been made to one of the coefficients. Thank you to the student who brought the error to my attention. For the 3 students who have attempted this problem already, the number of attempts has effectively been reset for you.

Consider a causal LTI system whose input, x(t), and output, y(t), are related by the differential equation, $\frac{d}{dt}y(t) + 6y(t) = 6x(t)$.

Given the input signal $x(t) = 5cos(2\pi t) + sin(18\pi t) + cos(4\pi t + \frac{\pi}{4})$, find the Fourier series representation of the output as in $y(t) = \sum_{k=-\infty}^{\infty} b_k e^{jk\omega_0 t}$, and enter the values of b_k in the table below.

b_{-18}	
b_{-9}	
b_{-4}	
b_{-2}	
b_{-1}	
b_0	
b_1	
b_2	
b_4	
b_9	
b_{18}	

Correct Answers:

- 0
- -6/[2*j*(6-2*j*9*pi)]
- 0
- 6*e^(-j*pi/4)/(12-4*j*2*pi)
- 30/(12-4*j*pi)
- 0
- 30/(12+4*j*pi)
- 6*e^(j*pi/4)/(12+4*j*2*pi)
- 0
- 6/[2*j*(6+2*j*9*pi)]

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• 0

The transfer function of an LTI system is given by: $H(s) = \frac{Y(s)}{X(s)} = \frac{s+8}{s^2+7s+5}$

Given the input $x(t) = 9.5 + cos(t + \frac{\pi}{9})$, use the eigenfunction property of the LTI system to find the steady-state output.

$$y_{ss}(t) =$$

Correct Answers:

• 15.2+1*cos(t+(-0.578229))

Let x(t) be a periodic signal of fundamental frequency $\omega_0 = \frac{2\pi}{T_0}$ that has Fourier series coefficients, X_k . For each of the signals y(t) given in the table below, first determine if they are periodic or not. Then, for the periodic signals, determine their period in terms of T_0 , and calculate their Fourier coefficients Y_0 and Y_k in terms of X_0 and X_k , the corresponding Fourier coefficients of x(t).

In your answers, enter "Xk" for X_k and "X0" for X_0 , "w" for ω_0 , and "T" for T_0 . Enter "NA" for the aperiodic signals.

Signal, $y(t)$	Periodic/Aperiodic	Period	Y_0	Y_k
6x(t) - 3	[?/Periodic/Aperiodic]			
$x(\pi t) + 4x(t-5)$	[?/Periodic/Aperiodic]			
x(t-8) + 6x(t)	[?/Periodic/Aperiodic]			

Correct Answers:

- Periodic
- T or 2*pi/w
- 6*X0-3
- 6*Xk
- Aperiodic
- NA
- NA
- NA
- Periodic
- T or 2*pi/w
- 7*X0
- $(6+e^{(-8i)*k*2*pi/T})*Xk$ or $(6+e^{(-8i)*k*w})*Xk$