CN101

Lecture 8-10

Functions

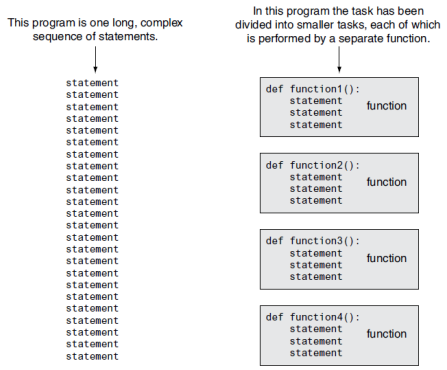
Topics

- Introduction to Functions
- Defining and Calling a Void Function
- Designing a Program to Use Functions
- Local Variables
- Passing Arguments to Functions
- Global Variables and Global Constants
- Introduction to Value-Returning Functions: Generating Random Numbers
- Writing Your Own Value-Returning Functions
- The `math` Module

Introduction to Functions

- Function: group of statements within a program that perform as specific task
  - Usually one task of a large program
    - Functions can be executed in order to perform overall program task
  - Known as *divide and conquer* approach
- Modularized program: program wherein each task within the program is in its own function

Using functions to divide and conquer a large task



Benefits of Modularizing a Program with Functions

- The benefits of using functions include:
  - Simpler code
  - Code reuse
    - write the code once and call it multiple times
  - Better testing and debugging
    - Can test and debug each function individually
  - Faster development
  - Easier facilitation of teamwork
    - Different team members can write different functions

Void Functions and Value-Returning Functions

- A void function:
  - Simply executes the statements it contains and then terminates.
- A value-returning function:
  - Executes the statements it contains, and then it returns a value back to the statement that called it.
    - The `input`, `int`, and `float` functions are examples of value-returning functions.

Defining and Calling a Function

- Functions are given names
  - Function naming rules:
    - Cannot use key words as a function name
    - Cannot contain spaces
    - First character must be a letter or underscore
    - All other characters must be a letter, number or underscore
    - Uppercase and lowercase characters are distinct

Defining and Calling a Function (cont'd.)

- Function name should be descriptive of the task carried out by the function
  - Often includes a verb
- Function definition: specifies what function does

```
def function_name():
    statement
    statement
    etc.
```

```
def message():
    print('I am Arthur,')
    print('King of the Britons.')
```


Defining and Calling a Function (cont'd.)

- Function header: first line of function
  - Includes keyword `def` and function name, followed by parentheses and colon
- Block: set of statements that belong together as a group
  - Example: the statements included in a function

Defining and Calling a Function (cont'd.)

- Call a function to execute it
  - When a function is called:
    - Interpreter jumps to the function and executes statements in the block
    - Interpreter jumps back to part of program that called the function
      - Known as function return

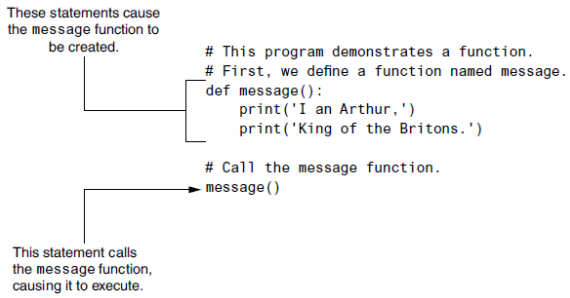
Program 5-1 (function_demo.py)

```
1  # This program demonstrates a function.
2  # First, we define a function named message.
3  def message():
4      print('I am Arthur,')
5      print('King of the Britons.')
6
7  # Call the message function.
8  message()
```

Program Output

```
I am Arthur,
King of the Britons.
```


The function definition and the function call



Defining and Calling a Function (cont'd.)

- `main` function: called when the program starts
  - Calls other functions when they are needed
  - Defines the *mainline logic* of the program

Program 5-2 (two_functions.py)

```
1  # This program has two functions. First we
2  # define the main function.
3  def main():
4      print('I have a message for you.')
5      message()
6      print('Goodbye!')
7
8  # Next we define the message function.
9  def message():
10     print('I am Arthur,')
11     print('King of the Britons.')
12
13 # Call the main function.
14 main()
```

Program Output

```
I have a message for you.
I am Arthur,
King of the Britons.
Goodbye!
```

Calling the main function

The interpreter jumps to the `main` function and begins executing the statements in its block.

```
# This program has two functions. First we
# define the main function.
def main():
    print('I have a message for you.')
    message()
    print('Goodbye!')

# Next we define the message function.
def message():
    print('I am Arthur,')
    print('King of the Britons.')

# Call the main function.
main()
```

Calling the message function

The interpreter jumps to the `message` function and begins executing the statements in its block.

```
# This program has two functions. First we
# define the main function.
def main():
    print('I have a message for you.')
    message()
    print('Goodbye!')

# Next we define the message function.
def message():
    print('I am Arthur,')
    print('King of the Britons.')

# Call the main function.
main()
```

The message function returns

When the `message` function ends, the interpreter jumps back to the part of the program that called it and resumes execution from that point.

```
# This program has two functions. First we
# define the main function.
def main():
    print('I have a message for you.')
    message()
    print('Goodbye!')

# Next we define the message function.
def message():
    print('I am Arthur,')
    print('King of the Britons.')

# Call the main function.
main()
```

The main function returns

When the `main` function ends, the interpreter jumps back to the part of the program that called it. There are no more statements, so the program ends.

```
# This program has two functions. First we
# define the main function.
def main():
    print('I have a message for you.')
    message()
    print('Goodbye!')

# Next we define the message function.
def message():
    print('I am Arthur,')
    print('King of the Britons.')

# Call the main function.
main()
```

Indentation in Python

- Each block must be indented
  - Lines in block must begin with the same number of spaces
    - Use tabs or spaces to indent lines in a block, but not both as this can confuse the Python interpreter
    - IDLE automatically indents the lines in a block
  - Blank lines that appear in a block are ignored

The last indented line is the last line in the block.

These statements are not in the block.

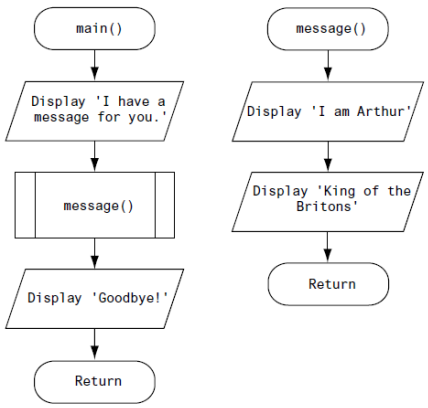
```
def greeting():
    print('Good morning!')
    print('Today we will learn about functions.')

print('I will call the greeting function.')
greeting()
```


Designing a Program to Use Functions

- In a flowchart, function call shown as rectangle with vertical bars at each side

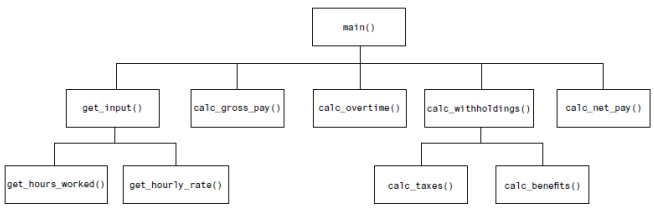
  - Function name written in the symbol
  - Typically draw separate flow chart for each function in the program
    - End terminal symbol usually reads `Return`



Designing a Program to Use Functions (cont'd.)

- Top-down design: technique for breaking algorithm into functions
- Hierarchy chart: depicts relationship between functions
  - AKA structure chart
  - Box for each function in the program, Lines connecting boxes illustrate the functions called by each function
  - Does not show steps taken inside a function
- Use `input` function to have program wait for user to press enter

A hierarchy chart



Local Variables

- Local variable: variable that is assigned a value inside a function
  - Belongs to the function in which it was created
    - Only statements inside that function can access it, error will occur if another function tries to access the variable
- Scope: the part of a program in which a variable may be accessed
  - For local variable: function in which created

Program 5-4 (bad_local.py)

```
1  # Definition of the main function.
2  def main():
3      get_name()
4      print('Hello', name)      # This causes an error!
5
6  # Definition of the get_name function.
7  def get_name():
8      name = input('Enter your name: ')
9
10 # Call the main function.
11 main()
```

Local Variables (cont'd.)

- Local variable cannot be accessed by statements inside its function which precede its creation
- Different functions may have local variables with the same name
  - Each function does not see the other function's local variables, so no confusion

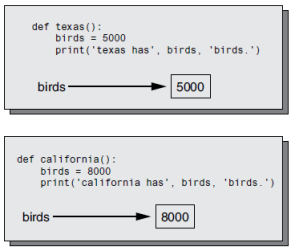
Program 5-5 (birds.py)

```
1  # This program demonstrates two functions that
2  # have local variables with the same name.
3
4  def main():
5      # Call the texas function.
6      texas()
7      # Call the california function.
8      california()
9
10 # Definition of the texas function. It creates
11 # a local variable named birds.
12 def texas():
13     birds = 5000
14     print('texas has', birds, 'birds.')
15
16 # Definition of the california function. It also
17 # creates a local variable named birds.
18 def california():
19     birds = 8000
20     print('california has', birds, 'birds.')
21
22 # Call the main function.
23 main()
```

Program Output

```
texas has 5000 birds.
california has 8000 birds.
```

Each function has its own birds variable



Passing Arguments to Functions

- Argument: piece of data that is sent into a function
  - Function can use argument in calculations
  - When calling the function, the argument is placed in parentheses following the function name
- Parameter variable: variable that is assigned the value of an argument when the function is called
  - The parameter and the argument reference the same value
  - General format:
  - `def function_name(parameter):`
  - Scope of a parameter: the function in which the parameter is used

```
def show_double(number):
    result = number * 2
    print(result)
```

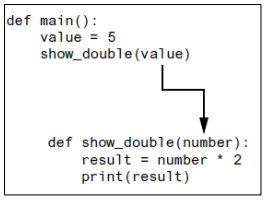

Program 5-6 (pass_arg.py)

```
1  # This program demonstrates an argument being
2  # passed to a function.
3
4  def main():
5      value = 5
6      show_double(value)
7
8  # The show_double function accepts an argument
9  # and displays double its value.
10 def show_double(number):
11     result = number * 2
12     print(result)
13
14 # Call the main function.
15 main()
```

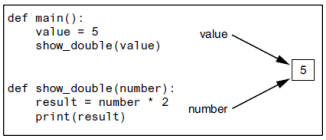
Program Output

```
10
```

The value variable is passed as an argument



The value variable and the number parameter reference the same value



Passing Arguments to Functions (cont'd.)

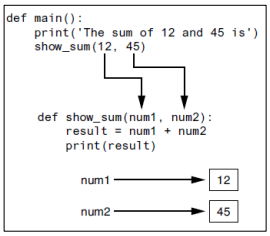
- Parameter variable: variable that is assigned the value of an argument when the function is called
  - The parameter and the argument reference the same value
  - General format:
  - `def function_name(parameter):`
  - Scope of a parameter: the function in which the parameter is used

Passing Multiple Arguments

- Python allows writing a function that accepts multiple arguments
  - Parameter list replaces single parameter
    - Parameter list items separated by comma
- Arguments are passed *by position* to corresponding parameters
  - First parameter receives value of first argument, second parameter receives value of second argument, etc.

Program 5-8 (multiple_args.py)

```
1  # This program demonstrates a function that accepts
2  # two arguments.
3
4  def main():
5      print('The sum of 12 and 45 is')
6      show_sum(12, 45)
7
8  # The show_sum function accepts two arguments
9  # and displays their sum.
10 def show_sum(num1, num2):
11     result = num1 + num2
12     print(result)
13
14 # Call the main function.
15 main()
```



Program Output

```
The sum of 12 and 45 is
57
```


Program 5-9 (string_args.py)

```
1  # This program demonstrates passing two string
2  # arguments to a function.
3
4  def main():
5      first_name = input('Enter your first name: ')
6      last_name = input('Enter your last name: ')
7      print('Your name reversed is')
8      reverse_name(first_name, last_name)
9
10 def reverse_name(first, last):
11     print(last, first)
12
13 # Call the main function.
14 main()
```

Program Output (with input shown in bold)

```
Enter your first name: Matt Enter
Enter your last name: Hoyle Enter
Your name reversed is
Hoyle Matt
```


Making Changes to Parameters

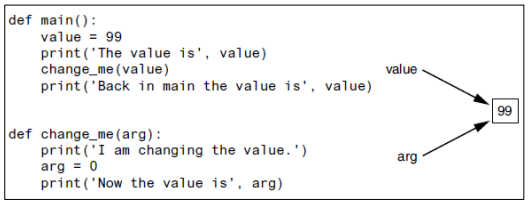
- Changes made to a parameter value within the function do not affect the argument
  - Known as *pass by value*
  - Provides a way for unidirectional communication between one function and another function
    - Calling function can communicate with called function

Program 5-10 (change_me.py)

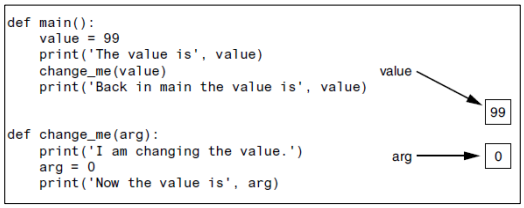
```
1  # This program demonstrates what happens when you
2  # change the value of a parameter.
3
4  def main():
5      value = 99
6      print('The value is', value)
7      change_me(value)
8      print('Back in main the value is', value)
9
10 def change_me(arg):
11     print('I am changing the value.')
12     arg = 0
13     print('Now the value is', arg)
14
15 # Call the main function.
16 main()
```

Program Output

```
The value is 99
I am changing the value.
Now the value is 0
Back in main the value is 99
```

The `value` variable passed to the `change_me` function cannot be changed by it



Keyword Arguments

- Keyword argument: argument that specifies which parameter the value should be passed to
  - Position when calling function is irrelevant
  - General Format:
  - `function_name(parameter=value)`
- Possible to mix keyword and positional arguments when calling a function
  - Positional arguments must appear first

Program 5-11 (keyword_args.py)

```
1  # This program demonstrates keyword arguments.
2
3  def main():
4      # Show the amount of simple interest, using 0.01 as
5      # interest rate per period, 10 as the number of periods,
6      # and $10,000 as the principal.
7      show_interest(rate=0.01, periods=10, principal=10000.0)
8
9  # The show_interest function displays the amount of
10 # simple interest for a given principal, interest rate
11 # per period, and number of periods.
12
13 def show_interest(principal, rate, periods):
14     interest = principal * rate * periods
15     print('The simple interest will be $',
16           format(interest, ',.2f'),
17           sep='')
18
19 # Call the main function.
20 main()
```

Program Output

```
The simple interest will be $1000.00.
```


Program 5-12 (keyword_string_args.py)

```
1  # This program demonstrates passing two strings as
2  # keyword arguments to a function.
3
4  def main():
5      first_name = input('Enter your first name: ')
6      last_name = input('Enter your last name: ')
7      print('Your name reversed is')
8      reverse_name(last=last_name, first=first_name)
9
10 def reverse_name(first, last):
11     print(last, first)
12
13 # Call the main function.
14 main()
```

Program Output (with input shown in bold)

```
Enter your first name: Matt Enter
Enter your last name: Hoyle Enter
Your name reversed is
Hoyle Matt
```


Global Variables and Global Constants

- Global variable: created by assignment statement written outside all the functions
  - Can be accessed by any statement in the program file, including from within a function
  - If a function needs to assign a value to the global variable, the global variable must be redeclared within the function
    - General format: `global variable_name`

Program 5-13 (global1.py)

```
1  # Create a global variable.
2  my_value = 10
3
4  # The show_value function prints
5  # the value of the global variable.
6  def show_value():
7      print(my_value)
8
9  # Call the show_value function.
10 show_value()
```

Program Output

```
10
```


Program 5-14 (global2.py)

```
1  # Create a global variable.
2  number = 0
3
4  def main():
5      global number
6      number = int(input('Enter a number: '))
7      show_number()
8
9  def show_number():
10     print('The number you entered is', number)
11
12 # Call the main function.
13 main()
```

Program Output

```
Enter a number: 55 Enter
The number you entered is 55
```

Global Variables and Global Constants (cont'd.)

- Reasons to avoid using global variables:
  - Global variables making debugging difficult
    - Many locations in the code could be causing a wrong variable value
  - Functions that use global variables are usually dependent on those variables
    - Makes function hard to transfer to another program
  - Global variables make a program hard to understand

Global Constants

- Global constant: global name that references a value that cannot be changed
  - Permissible to use global constants in a program
  - To simulate global constant in Python, create global variable and do not re-declare it within functions

Program 5-15 (retirement.py)

```
1  # The following is used as a global constant
2  # the contribution rate.
3  CONTRIBUTION_RATE = 0.05
4
5  def main():
6      gross_pay = float(input('Enter the gross pay: '))
7      bonus = float(input('Enter the amount of bonuses: '))
8      show_pay_contrib(gross_pay)
9      show_bonus_contrib(bonus)
10
11 # The show_pay_contrib function accepts the gross
12 # pay as an argument and displays the retirement
13 # contribution for that amount of pay.
14 def show_pay_contrib(gross):
15     contrib = gross * CONTRIBUTION_RATE
16     print('Contribution for gross pay: $',
17           format(contrib, ',.2f'),
18           sep='')
19
```



```
20 # The show_bonus_contrib function accepts the
21 # bonus amount as an argument and displays the
22 # retirement contribution for that amount of pay.
23 def show_bonus_contrib(bonus):
24     contrib = bonus * CONTRIBUTION_RATE
25     print('Contribution for bonuses: $',
26           format(contrib, ',.2f'),
27           sep='')
28
29 # Call the main function.
30 main()
```

Program Output (with input shown in bold)

```
Enter the gross pay: 80000.00 Enter
Enter the amount of bonuses: 20000.00 Enter
Contribution for gross pay: $4000.00
Contribution for bonuses: $1000.00
```


Introduction to Value-Returning Functions: Generating Random Numbers

- void function: group of statements within a program for performing a specific task
  - Call function when you need to perform the task
- Value-returning function: similar to void function, returns a value
  - Value returned to part of program that called the function when function finishes executing

Standard Library Functions and the `import` Statement

- Standard library: library of pre-written functions that comes with Python
  - *Library functions* perform tasks that programmers commonly need
    - Example: `print`, `input`, `range`
    - Viewed by programmers as a "black box"
- Some library functions built into Python interpreter
  - To use, just call the function

Standard Library Functions and the `import` Statement (cont'd.)

- Modules: files that stores functions of the standard library
  - Help organize library functions not built into the interpreter
  - Copied to computer when you install Python
- To call a function stored in a module, need to write an `import` statement
  - Written at the top of the program
  - Format: `import` *`module_name`*

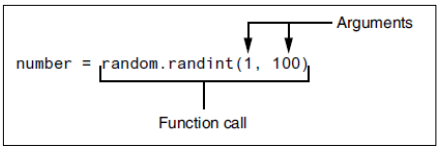
Generating Random Numbers

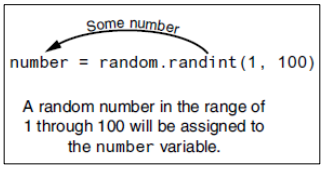
- Random number are useful in a lot of programming tasks
- `random` module: includes library functions for working with random numbers
- Dot notation: notation for calling a function belonging to a module
  - Format: `module_name.function_name()`

Generating Random Numbers (cont'd.)

- `randint` function: generates a random number in the range provided by the arguments
  - Returns the random number to part of program that called the function
  - Returned integer can be used anywhere that an integer would be used
  - You can experiment with the function in interactive mode

A statement that calls the random function





Program 5-16 (random_numbers.py)

```
1  # This program displays a random number
2  # in the range of 1 through 10.
3  import random
4
5  def main():
6      # Get a random number.
7      number = random.randint(1, 10)
8      # Display the number.
9      print('The number is', number)
10
11 # Call the main function.
12 main()
```

Program Output

```
The number is 7
```

Program 5-17 (random_numbers2.py)

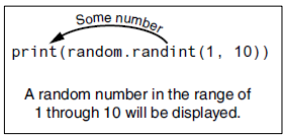
```
1  # This program displays five random
2  # numbers in the range of 1 through 100.
3  import random
4
5  def main():
6      for count in range(5):
7          # Get a random number.
8          number = random.randint(1, 100)
9          # Display the number.
10         print(number)
11
12 # Call the main function.
13 main()
```

Program Output

```
89
7
16
41
12
```


Program 5-18 (random_numbers3.py)

```
1  # This program displays five random
2  # numbers in the range of 1 through 100.
3  import random
4
5  def main():
6      for count in range(5):
7          print(random.randint(1, 100))
8
9  # Call the main function.
10 main()
```



Program 5-19 (dice.py)

```
1  # This program the rolling of dice.
2  import random
3
4  # Constants for the minimum and maximum random numbers
5  MIN = 1
6  MAX = 6
7
8  def main():
9      # Create a variable to control the loop.
10     again = 'y'
11
12     # Simulate rolling the dice.
13     while again == 'y' or again == 'Y':
14         print('Rolling the dice ...')
15         print('Their values are:')
16         print(random.randint(MIN, MAX))
17         print(random.randint(MIN, MAX))
18
19         # Do another roll of the dice?
20         again = input('Roll them again? (y = yes): ')
21
22 # Call the main function.
23 main()
```

Program Output (with input shown in bold)

```
Rolling the dice ...
Their values are:
3
1
Roll them again? (y = yes): y Enter
Rolling the dice ...
Their values are:
1
1
Roll them again? (y = yes): y Enter
Rolling the dice ...
Their values are:
5
6
Roll them again? (y = yes): y Enter
```


Program 5-20 (coin_toss.py)

```
1  # This program simulates 10 tosses of a coin.
2  import random
3
4  # Constants
5  HEADS = 1
6  TAILS = 2
7  TOSSES = 10
8
9  def main():
10     for toss in range(TOSSES):
11         # Simulate the coin toss.
12         if random.randint(HEADS, TAILS) == HEADS:
13             print('Heads')
14         else:
15             print('Tails')
16
17 # Call the main function.
18 main()
```

Program Output

```
Tails
Tails
Heads
Tails
Heads
Heads
Heads
Tails
Heads
Tails
```


Generating Random Numbers (cont'd.)

- `randrange` function: similar to `range` function, but returns randomly selected integer from the resulting sequence

```
number = random.randrange(0, 101, 10)
```

  - Same arguments as for the `range` function
- `random` function: returns a random float in the range of 0.0 and 1.0

```
number = random.random()
```

  - Does not receive arguments
- `uniform` function: returns a random float but allows user to specify range

```
number = random.uniform(1.0, 10.0)
```

Random Number Seeds

- Random number created by functions in random module are actually pseudo-random numbers
- Seed value: initializes the formula that generates random numbers
  - Need to use different seeds in order to get different series of random numbers
    - By default uses system time for seed
    - Can use `random.seed()` function to specify desired seed value

If we start a new interactive session and repeat these statements, we get the same sequence of pseudorandom numbers, as shown here:

```
>>> import random Enter
>>> random.seed(10) Enter
>>> random.randint(1, 100) Enter
58
>>> random.randint(1, 100) Enter
43
>>> random.randint(1, 100) Enter
58
>>> random.randint(1, 100) Enter
21
>>>
```

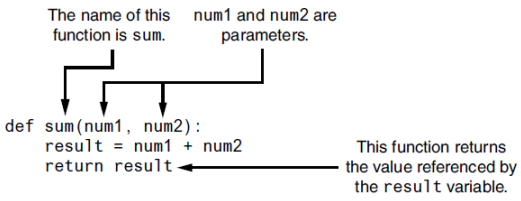
```
>>> import random Enter
>>> random.seed(10) Enter
>>> random.randint(1, 100) Enter
58
>>> random.randint(1, 100) Enter
43
>>> random.randint(1, 100) Enter
58
>>> random.randint(1, 100) Enter
21
>>>
```

Writing Your Own Value-Returning Functions

- To write a value-returning function, you write a simple function and add one or more `return` statements
  - Format: `return` *`expression`*
    - The value for *`expression`* will be returned to the part of the program that called the function
  - The expression in the `return` statement can be a complex expression, such as a sum of two variables or the result of another value- returning function

```
def function_name():
    statement
    statement
    etc.
    return expression
```

Writing Your Own Value-Returning Functions (cont'd.)



How to Use Value-Returning Functions

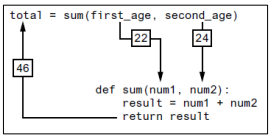
- Value-returning function can be useful in specific situations
  - Example: have function prompt user for input and return the user's input
  - Simplify mathematical expressions
  - Complex calculations that need to be repeated throughout the program
- Use the returned value
  - Assign it to a variable or use as an argument in another function

Program 5-21 (total_ages.py)

```
1  # This program uses the return value of a function.
2
3  def main():
4      # Get the user's age.
5      first_age = int(input('Enter your age: '))
6
7      # Get the user's best friend's age.
8      second_age = int(input("Enter your best friend's age: "))
9
10     # Get the sum of both ages.
11     total = sum(first_age, second_age)
12
13     # Display the total age.
14     print('Together you are', total, 'years old.')
15
16 # The sum function accepts two numeric arguments and
17 # returns the sum of those arguments.
18 def sum(num1, num2):
19     result = num1 + num2
20     return result
21
22 # Call the main function.
23 main()
```

Program Output (with input shown in bold)

```
Enter your age: 22 Enter
Enter your best friend's age: 24 Enter
Together you are 46 years old.
```



Because the return statement can return the value of an expression, you can eliminate the result variable and rewrite the function as:

```
def sum(num1, num2):
    return num 1 + num 2
```


Program 5-22 (sale_price.py)

```
1  # This program calculates a retail item's
2  # sale price.
3
4  # DISCOUNT_PERCENTAGE is used as a global
5  # constant for the discount percentage.
6  DISCOUNT_PERCENTAGE = 0.20
7
8  # The main function.
9  def main():
10     # Get the item's regular price.
11     reg_price = get_regular_price()
12
13     # Calculate the sale price.
14     sale_price = reg_price - discount(reg_price)
15
16     # Display the sale price.
17     print('The sale price is $', format(sale_price, ',.2f'), sep='')
18
```



```
19 # The get_regular_price function prompts the
20 # user to enter an item's regular price and it
21 # returns that value.
22 def get_regular_price():
23     price = float(input("Enter the item's regular price: "))
24     return price
25
26 # The discount function accepts an item's price
27 # as an argument and returns the amount of the
28 # discount, specified by DISCOUNT_PERCENTAGE.
29 def discount(price):
30     return price * DISCOUNT_PERCENTAGE
31
32 # Call the main function.
33 main()
```

Program Output (with input shown in bold)

```
Enter the item's regular price: 100.00 Enter
The sale price is $80.00
```


Returning Strings

- You can write functions that return strings
- For example:

```
def get_name():
    # Get the user's name.
    name = input('Enter your name: ')
    # Return the name.
    return name
```

Returning Boolean Values

- Boolean function: returns either `True` or `False`
  - Use to test a condition such as for decision and repetition structures
    - Common calculations, such as whether a number is even, can be easily repeated by calling a function
  - Use to simplify complex input validation code

```
def is_even(number):
    # Determine whether number is even. If it is,
    # set status to true. Otherwise, set status
    # to false.
    if (number % 2) == 0:
        status = True
    else:
        status = False
    # Return the value of the status variable.
    return status
```


Returning Multiple Values

- In Python, a function can return multiple values
  - Specified after the `return` statement separated by commas
    - Format: `return expression1, expression2, etc.`
  - When you call such a function in an assignment statement, you need a separate variable on the left side of the = operator to receive each returned value

```
def get_name():
    # Get the user's first and last names.
    first = input('Enter your first name: ')
    last = input('Enter your last name: ')
    # Return both names.
    return first, last
```

```
first_name, last_name = get_name()
```


The `math` Module

- `math` module: part of standard library that contains functions that are useful for performing mathematical calculations
  - Typically accept one or more values as arguments, perform mathematical operation, and return the result
  - Use of module requires an `import math` statement

`math` Module Function	Description
`acos(x)`	Returns the arc cosine of x, in radians.
`asin(x)`	Returns the arc sine of x, in radians.
`atan(x)`	Returns the arc tangent of x, in radians.
`ceil(x)`	Returns the smallest integer that is greater than or equal to x.
`cos(x)`	Returns the cosine of x in radians.
`degrees(x)`	Assuming x is an angle in radians, the function returns the angle converted to degrees.
`exp(x)`	Returns e^x
`floor(x)`	Returns the largest integer that is less than or equal to x.
`hypot(x, y)`	Returns the length of a hypotenuse that extends from (0, 0) to (x, y).
`log(x)`	Returns the natural logarithm of x.
`log10(x)`	Returns the base-10 logarithm of x.
`radians(x)`	Assuming x is an angle in degrees, the function returns the angle converted to radians.
`sin(x)`	Returns the sine of x in radians.
`sqrt(x)`	Returns the square root of x.
`tan(x)`	Returns the tangent of x in radians.

The `math` Module (cont'd.)

- The `math` module defines variables `pi` and `e`, which are assigned the mathematical values for *pi* and *e*
  - Can be used in equations that require these values, to get more accurate results
- Variables must also be called using the dot notation
  - Example:

```
circle_area = math.pi * radius**2
```


Program 5-25 (hypotenuse.py)

```
1  # This program calculates the length of a right
2  # triangle's hypotenuse.
3  import math
4
5  def main():
6      # Get the length of the triangle's two sides.
7      a = float(input('Enter the length of side A: '))
8      b = float(input('Enter the length of side B: '))
9
10     # Calculate the length of the hypotenuse.
11     c = math.hypot(a, b)
12
13     # Display the length of the hypotenuse.
14     print('The length of the hypotenuse is', c)
15
16 # Call the main function.
17 main()
```

Program Output (with input shown in bold)

```
Enter the length of side A: 5.0 Enter
Enter the length of side B: 12.0 Enter
The length of the hypotenuse is 13.0
```

Summary

- This chapter covered:
  - The advantages of using functions
  - The syntax for defining and calling a function
  - Methods for designing a program to use functions
  - Use of local variables and their scope
  - Syntax and limitations of passing arguments to functions
  - Global variables, global constants, and their advantages and disadvantages

Summary (cont'd.)

- Value-returning functions, including:
  - Writing value-returning functions
  - Using value-returning functions
  - Functions returning multiple values
- Using library functions and the `import` statement
- Modules, including the `random` and `math` modules