

# ORACLES AND CHOICE SEQUENCES FOR TYPE-THEORETIC PRAGMATICS

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joint work with Darryl McAdams

## INTRODUCTION

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[[*A man walked in.*]]



[[*A man walked in.*]]

▽

( $\Sigma p \in Man$ )

[[*A man walked in.*]]

$\nabla$

$(\Sigma p \in Man) WalkedIn(p)$

[[*He sat down*]]



[[*He sat down*]]

▽

*SatDown*(???)



[[*A man walked in. He sat down*]]



[[*A man walked in. He sat down*]]

▽

$(\Sigma x \in (\Sigma p \in Man) WalkedIn(p))$

[[*A man walked in. He sat down*]]

▽

$(\Sigma x \in (\Sigma p \in Man) WalkedIn(p)) SatDown(???)$

[[*A man walked in. He sat down*]]

$\nabla$

$(\Sigma x \in (\Sigma p \in Man) WalkedIn(p)) SatDown(\pi_1(x))$

## THE “DONKEY SENTENCE”

[[*Every farmer who owns a donkey beats it.*]]

$\nabla$

$(\Pi p \in (\Sigma x \in \textit{Farmer}) (\Sigma y \in \textit{Donkey}) \textit{Owns}(x; y))$

# THE “DONKEY SENTENCE”

[[*Every farmer who owns a donkey beats it.*]]

▽

$(\Pi p \in (\Sigma x \in \text{Farmer}) (\Sigma y \in \text{Donkey}) \text{Owns}(x; y)) \text{Beats}(\text{???}; \text{???})$

## THE “DONKEY SENTENCE”

[[Every farmer who owns a donkey beats it.]]

$\nabla$

$(\Pi p \in (\Sigma x \in \text{Farmer}) (\Sigma y \in \text{Donkey}) \text{Owns}(x; y)) \text{Beats}(\pi_1(p); \pi_1(\pi_2(p)))$

## TWO THINGS TO DEAL WITH



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- terms for presuppositions

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- terms for presuppositions (this talk)
- resolution of presuppositions

## THE **require** ORACLE: STATICS

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**require** : (0; 1)

(operator)

**require**  $x : A$  **in**  $N \stackrel{\text{def}}{=} \textbf{require}(A; x.N)$

(notation)

**require** : (0;1)

(operator)

**require**  $x : A$  **in**  $N \stackrel{\text{def}}{=} \text{require}(A; x.N)$

(notation)

$$\frac{\Gamma \vdash A \text{ type} \quad \Gamma, x : A \vdash N \in B}{\Gamma \vdash \text{require } x : A \text{ in } N \in B}$$

(require)



$\llbracket A \text{ man walked in. He sat down} \rrbracket$

$\nabla$

$(\Sigma x \in (\Sigma p \in \text{Man}) \text{WalkedIn}(p)) \text{SatDown}(???)$

$\llbracket A \text{ man walked in. He sat down} \rrbracket$

$\nabla$

$(\Sigma x \in (\Sigma p \in \text{Man}) \text{WalkedIn}(p)) \textbf{require } y : \text{Man in SatDown}(y)$

The meaning of a sentence is a logical proposition.

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What we want:

$(\Sigma x \in (\Sigma p \in \text{Man}) \text{WalkedIn}(p)) \text{ require } y : \text{Man in SatDown}(y)$

$\sim$

$(\Sigma x \in (\Sigma p \in \text{Man}) \text{WalkedIn}(p)) \pi_1(x)$

~~The meaning of a sentence is a logical proposition.~~

The meaning of a sentence is a type-theoretic expression which may evaluate to a canonical proposition.

What we want:

$(\Sigma x \in (\Sigma p \in \text{Man}) \text{WalkedIn}(p))$  **require**  $y : \text{Man}$  **in**  $\text{SatDown}(y)$

$\sim$

$(\Sigma x \in (\Sigma p \in \text{Man}) \text{WalkedIn}(p)) \pi_1(x)$

where  $M \sim N \stackrel{\text{def}}{=} (M \leq N) \wedge (N \leq M)$



# EVERY GRAMMATICAL SENTENCE HAS A MEANING

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...but only some of them denote propositions (types)!

## A NEGATIVE EXAMPLE

[[ *The unicorn ran a marathon* ]]



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∇

**require**  $x : \textit{Unicorn}$  **in**  $(\Sigma y \in \textit{Marathon}) \textit{Ran}(x; y)$

[[ *The unicorn ran a marathon* ]]

$\nabla$

**require**  $x : \textit{Unicorn}$  **in**  $(\Sigma y \in \textit{Marathon}) \textit{Ran}(x; y)$

(not a proposition)

## A POSITIVE EXAMPLE

[[ *The President ran a marathon* ]]





[[ *The President ran a marathon* ]]

▽

**require**  $x : \textit{President}$  **in**  $(\Sigma y \in \textit{Marathon}) \textit{Ran}(x; y)$

## A POSITIVE EXAMPLE

**require**  $x : \textit{President}$  **in**  $(\Sigma y \in \textit{Marathon}) \textit{Ran}(x; y)$

**require**  $x : \textit{President}$  **in**  $(\Sigma y \in \textit{Marathon}) \textit{Ran}(x; y)$

$\Downarrow$

$(\Sigma y \in \textit{Marathon}) \textit{Ran}(\textit{Obama}; y)$

**require**  $x : \textit{President}$  **in**  $(\Sigma y \in \textit{Marathon}) \textit{Ran}(x; y)$

$\Downarrow$

$(\Sigma y \in \textit{Marathon}) \textit{Ran}(\textit{Obama}; y)$

Evaluation is now non-deterministic

IS require COMPUTATIONALLY EFFECTIVE?

Yes, but we need two things:

Yes, but we need two things:

1. knowledge-sensitive judgments



Yes, but we need two things:

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2. non-deterministic computation

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1. knowledge-sensitive judgments (forcing)
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$$w \Vdash \mathcal{I}$$

Yes, but we need two things:

1. knowledge-sensitive judgments (forcing)
2. non-deterministic computation (use choice sequences)

$$w \Vdash \mathcal{I}$$

Yes, but we need two things:

1. knowledge-sensitive judgments (forcing)
2. deterministic computation (use choice sequences)

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$$\boxed{\alpha \Vdash_w \mathcal{I}}$$

## ASSERTION ACTS IN TIME

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assertion acts (judgments) are intensional (local)



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$|_x \mathcal{J}(x)$

(general judgment)

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(general judgment)

$\mathcal{I}_2 (\mathcal{I}_1)$

(hypothetical judgment)

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 $|_x \mathcal{I}(x)$ 

(general judgment)

 $\mathcal{I}_2 (\mathcal{I}_1)$ 

(hypothetical judgment)

 $M \Downarrow N$ 

(evaluation)

assertion acts (judgments) are intensional (local)

$ _x \mathcal{I}(x)$	(general judgment)
$\mathcal{I}_2 (\mathcal{I}_1)$	(hypothetical judgment)
$M \Downarrow N$	(evaluation)
$A = B \text{ type}$	(typehood)

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$ _x \mathcal{I}(x)$	(general judgment)
$\mathcal{I}_2 (\mathcal{I}_1)$	(hypothetical judgment)
$M \Downarrow N$	(evaluation)
$A = B \text{ type}$	(typehood)
$A \text{ true}$	(truth)

assertion acts (judgments) are intensional (local)

$ _x \mathcal{I}(x)$	(general judgment)
$\mathcal{I}_2 (\mathcal{I}_1)$	(hypothetical judgment)
$M \Downarrow N$	(evaluation)
$A = B \text{ type}$	(typehood)
$A \text{ true}$	(truth)
$M = N \in A$	(membership)

assertion acts (judgments) are intensional (local)

$w \Vdash  _x \mathcal{J}(x)$	(general judgment)
$w \Vdash \mathcal{J}_2 (\mathcal{J}_1)$	(hypothetical judgment)
$w \Vdash M \Downarrow N$	(evaluation)
$w \Vdash A = B \text{ type}$	(typehood)
$w \Vdash A \text{ true}$	(truth)
$w \Vdash M = N \in A$	(membership)

$w \Vdash |_x \mathcal{I}(x)$

(general judgment)

$w \Vdash \mathcal{I}_2 (\mathcal{I}_1)$

(hypothetical judgment)



$$w \Vdash |_x \mathcal{I}(x) \quad \Longleftrightarrow \quad \dots$$

$$w \Vdash \mathcal{I}_2 (\mathcal{I}_1) \quad \Longleftrightarrow \quad \dots$$

$$w \Vdash |_x \mathcal{I}(x) \iff \forall u \succeq w. \forall x \in \mathcal{M}_u. u \Vdash \mathcal{I}(x)$$

$$w \Vdash \mathcal{I}_2 (\mathcal{I}_1) \iff \forall u \succeq w. u \Vdash \mathcal{I}_1 \Rightarrow u \Vdash \mathcal{I}_2$$

$$\begin{aligned}
w \Vdash |_x \mathcal{I}(x) &\iff \forall u \succeq w. \forall x \in \mathcal{M}_u. u \Vdash \mathcal{I}(x) \\
w \Vdash \mathcal{I}_2 (\mathcal{I}_1) &\iff \forall u \succeq w. u \Vdash \mathcal{I}_1 \Rightarrow u \Vdash \mathcal{I}_2
\end{aligned}$$

where  $\mathcal{M}_w$  is the species of constructions that have been effected by stage  $w$

$$w \Vdash A \text{ true} \iff$$

$$w \Vdash A \text{ true} \iff \exists m \in \mathcal{M}_w.$$

$$w \Vdash A \text{ true} \iff \exists m \in \mathcal{M}_w. w \Vdash m = m \in A$$

$$w \Vdash A \text{ true} \iff$$

$$w \Vdash A \text{ true} \iff \exists \mathfrak{B} \text{ bars } w.$$



$$w \Vdash A \text{ true} \iff \exists \mathfrak{B} \text{ bars } w. \forall u \in \mathfrak{B}.$$

$$w \Vdash A \text{ true} \iff \exists \mathfrak{B} \text{ bars } w. \forall u \in \mathfrak{B}. \exists m \in \mathcal{M}_u.$$

$$w \Vdash A \text{ true} \iff \exists \mathcal{B} \text{ bars } w. \forall u \in \mathcal{B}. \exists m \in \mathcal{M}_u. u \Vdash m = m \in A$$

## THE require ORACLE: DYNAMICS

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$$\frac{\overline{\mathfrak{S}(\langle \rangle)}}{\mathfrak{S}(\vec{u})} \quad \frac{\mathfrak{S}(\vec{u}) \quad |_n \rho(n) < n \quad (n \in \mathbb{N}^+)}{\mathfrak{S}(\vec{u} \sim \rho)} \quad (\text{spread law})$$

$$\frac{\alpha \Vdash_t A \Downarrow A' \quad |\mathcal{A}_{A'}(t)| = \ell \quad \text{hd}(\alpha)(\ell) = j \quad \text{tl}(\alpha) \Vdash_t [\mathcal{A}_{A'}(j)/x] N \Downarrow N'}{\alpha \Vdash_t \text{require } x : A \text{ in } N \Downarrow N'} \quad (\text{for } \alpha \in \mathfrak{S})$$

QUESTIONS?