Neural Networks and Deep Learning: Exercises

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January 7, 2020

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Chapter 1

Using Neural Networks to Recognize Handwritten Digits

Exercise 1. Consider a network of perceptrons. Suppose that we multiply all weights and biases by a positive constant c > 0. Show that the behaviour of the network does not change.

Solution. First consider a single perceptron. Assume that weights and bias are w_1, \ldots, w_n and b, respectively. Then $\sum_i w_i \cdot x_i + b$ and $c \cdot (\sum_i w_i \cdot x_i + b)$ have exactly the same sign and hence multiplying the weights and the bias by c will not change the behaviour of this single perceptron. Now if all perceptrons in a network have their weights and biases multiplied by c > 0, then each individual perceptron behaves as before and hence the network behaves as before.