

21.

$$(1) \hat{p} = \frac{105}{250} = 0.42$$

$$0.42 \pm Z_{0.05} \sqrt{\frac{0.42 \times 0.58}{250}}$$

$$= 0.42 \pm 1.645 \times 0.03$$

$$= 0.42 \pm 0.05$$

$$\Rightarrow (0.37, 0.47)$$

(2)

$$(a) \hat{p} = 0.3 \quad e = 0.03 \quad 1 - \alpha = 0.95$$

$$e = \frac{\sigma}{\sqrt{n}} \times Z$$

$$n = \left(\frac{Z}{e} \right)^2 \times \hat{p} \times (1 - \hat{p})$$

$$n = \left(\frac{1.96}{0.03} \right)^2 \times 0.3 \times 0.7 = 896.37$$

$$\approx 897$$

(b)

$$\hat{p} = 0.42$$

$$n = \left(\frac{1.96}{0.03} \right)^2 \times 0.42 \times 0.58 = 1039.19$$

$$\approx 1040$$

$$(c) \hat{p} = 0.15$$

$$n = \left(\frac{1.96}{0.03} \right)^2 \times 0.15 \times 0.85 = 1067.11 \approx 1068$$

0.98

33.8

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