

CME 253A

# INTRODUCTION TO HIGH PERFORMANCE COMPUTING AND PARALLEL (GPU) COMPUTING

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STANFORD SUMMER SESSION 1

24 June 2019 | Y2E2 111

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# CME 235A - Course information

Objectives | design a 3D parallel GPU Stokes / Elastic wave solver

- Resources
- Class schedule
- Course format
- Assignments
- Final project

# CME 235A - Course information

## Resources

- Online resources:  
Stanford canvas: <https://canvas.stanford.edu/courses/103823>
- Course material (slides and codes) will be uploaded to canvas prior (if needed) and after (in general) each session.
- Do not hesitate to contact me if needed  
email: [Iraess@stanford.edu](mailto:Iraess@stanford.edu)  
Slack: Ludovic Räss

# CME 235A - Course information

## Class schedule

- We will meet for 5 sessions:
  - Monday June 24 > Introduction + Matlab examples
  - Wednesday June 26 > GPU computing
  - Monday July 1 > Performance evaluation
  - Wednesday July 3 > Projects: 3D Elastic waves or Stokes flow
  - Monday July 15 > Final discussion
- 3:30pm to 5:20pm
- Location: Y2E2 111

# CME 235A - Course information

## Course format

- This course is a “hands-on” and is therefore interactive and dynamic
- General session structure: 1/ introduction to new material or next steps  
2/ quiet working time where you can ask for help/questions
- The assignment will be determined before the end of each session

# CME 235A - Course information

## Assignments

- Finalise the material and step we discussed in class
- Assignments will be given by the end of each session for the next one
- If you have to leave earlier or cannot attend a session, information will be available on Canvas or contact me via email ([Iraess@stanford.edu](mailto:Iraess@stanford.edu))

# CME 235A - Course information

## Final project

- Objective: 3D GPU accelerated Stokes / elastic wave propagation solver
- Hand in: 1a/ Short presentation (few slides) about project [preferred]  
(motivation, results, your background, what you learned, what was difficult)  
1b/ Concise report including similar material as a presentation [alternative]  
2 / Commented codes ready to run and produce a figure
- During the last session (or part of it) we will have time for a short presentations of everyone's project results in short presentation format

# CME 235A - Course information

## Technicalities and computing resources

- Used software: Matlab (Octave or Python are also an option)  
CUDA + C
- Laptop with Unix shell (native in Linux and macOS, install Putty under windows)
- Optional sftp file transfer software (Filezilla, cyberduck, Transmit, ...)
- Account on CEES mazama GPU servers

Please give me your SUNet ID if you are attending the class  
but are not registered in Stanford Canvas - for GPU cluster account



# CME 235A - Course information

Questions so far ?

CME 253A

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# Session 1 - PDEs

## Today's agenda

- Lecture: Introduction - scientific GPU computing
- Programming: 1/ diffusion and acoustic wave propagation in 1D  
2/ loop vs vectorised approach
- Tasks: 1/ from 1D to 2D and 3D  
2/ 2D acoustic to elastic  
3/ 2D elastic to viscous  
4/ 2D viscous vectorised to loop

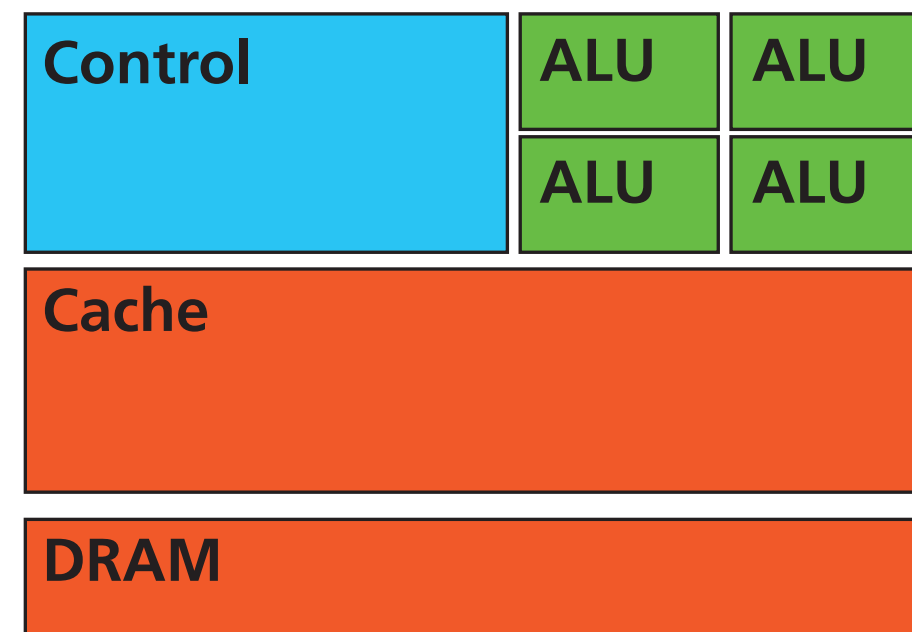
# Session 1 - PDEs

## Today's agenda

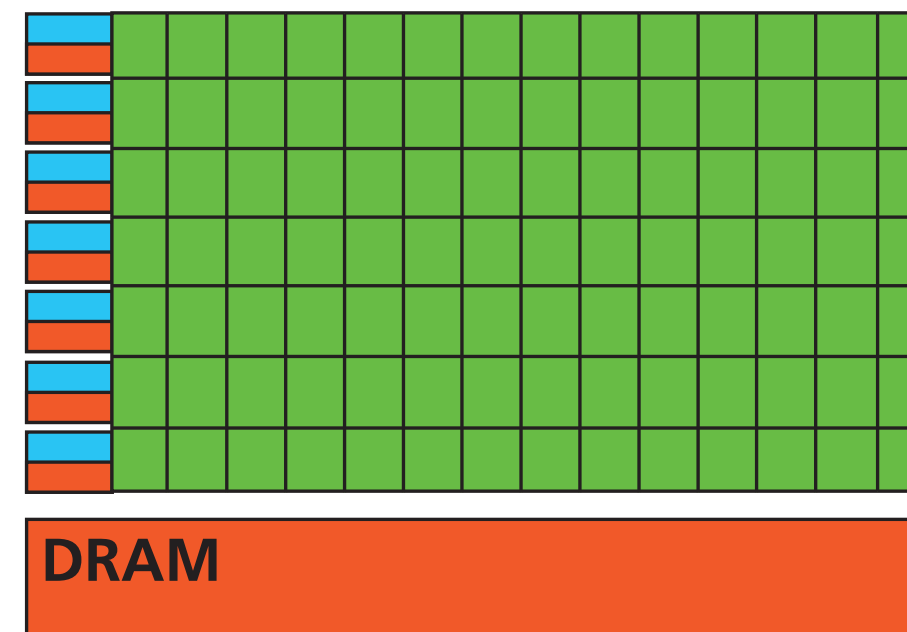
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# What is a GPU

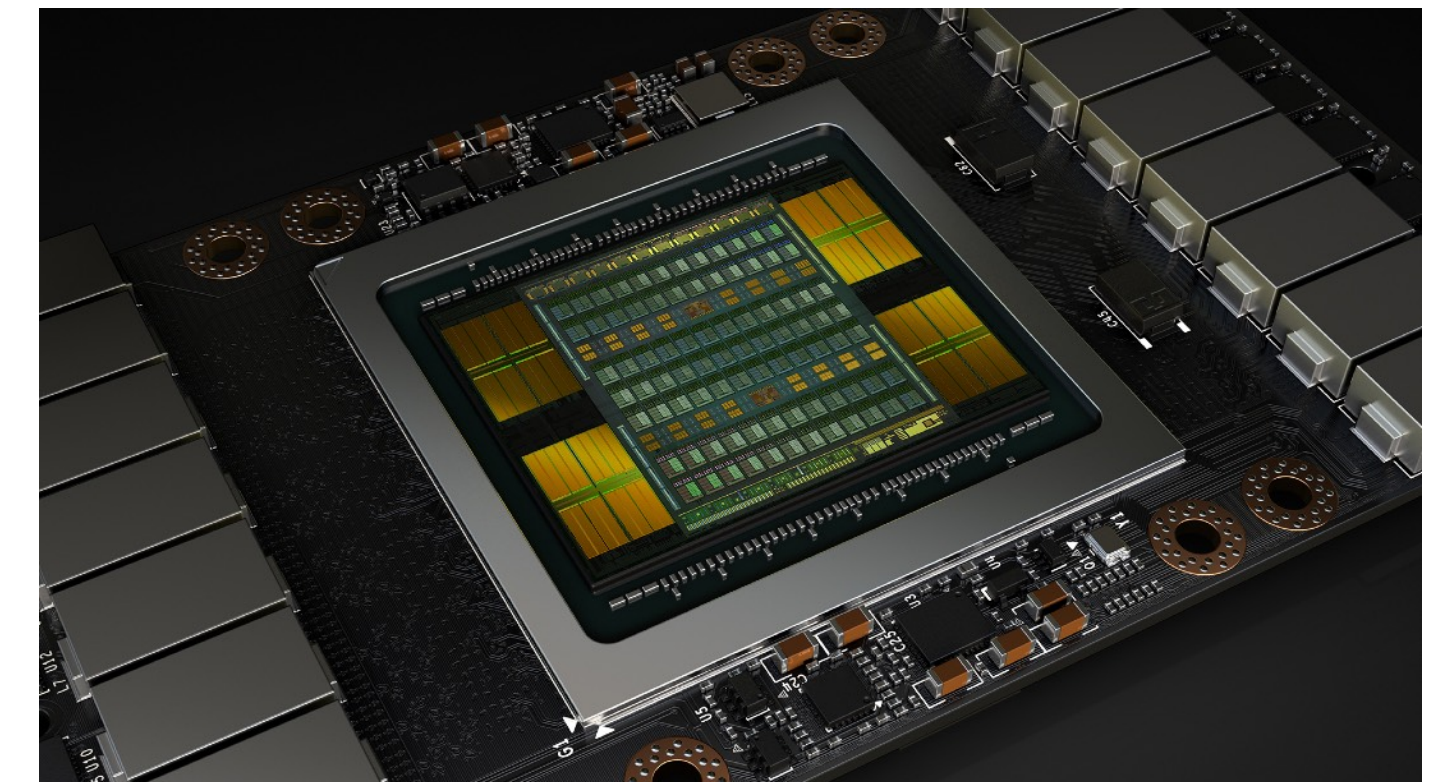
- Graphical Processing Unit (to paint the screen)
- Many small cores all doing the same job
- Large chip, close to memory
- High memory bandwidth - important for PDEs !



CPU



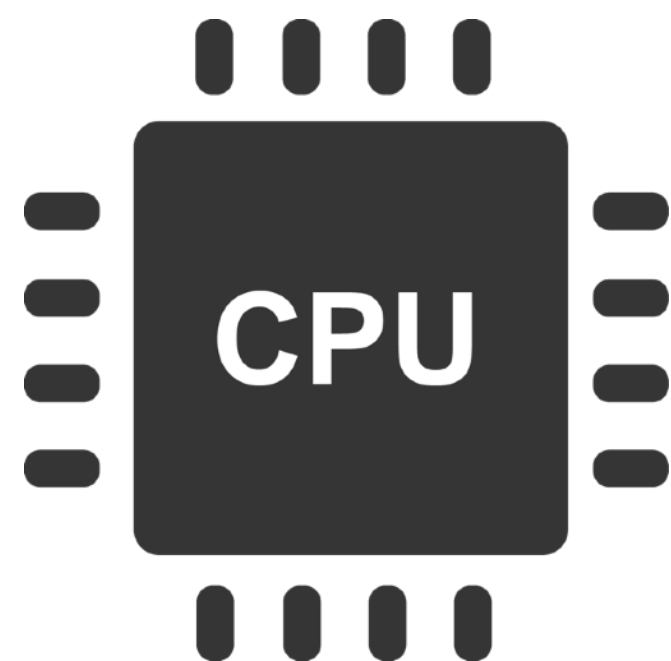
GPU





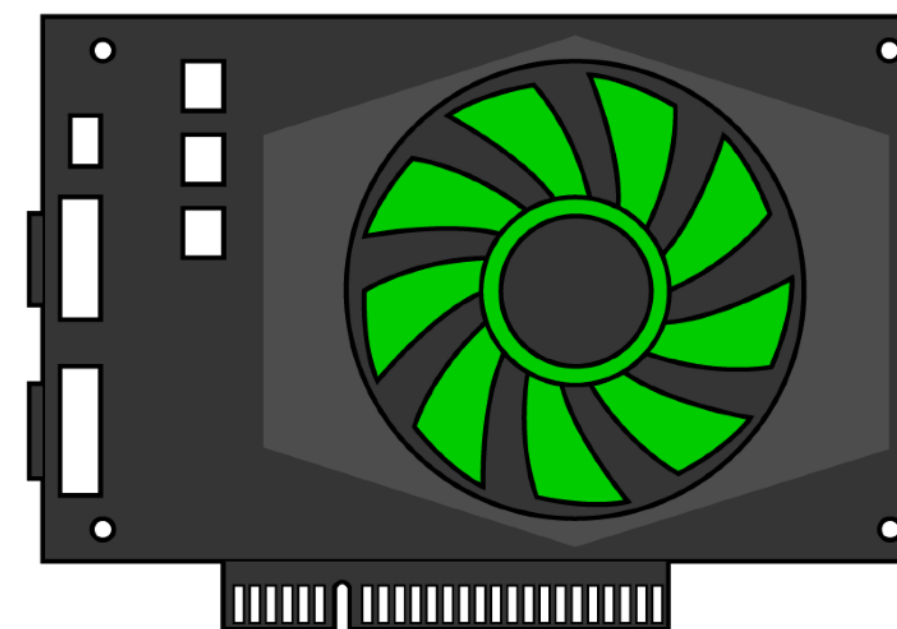
# Why to use a GPU

- Serial vs parallel execution > loop vs vectorised code
- Simultaneous calculations > increased concurrency
- Order of magnitude higher memory bandwidth & flop/s count



0.5 TFlop/s

50 GB/s



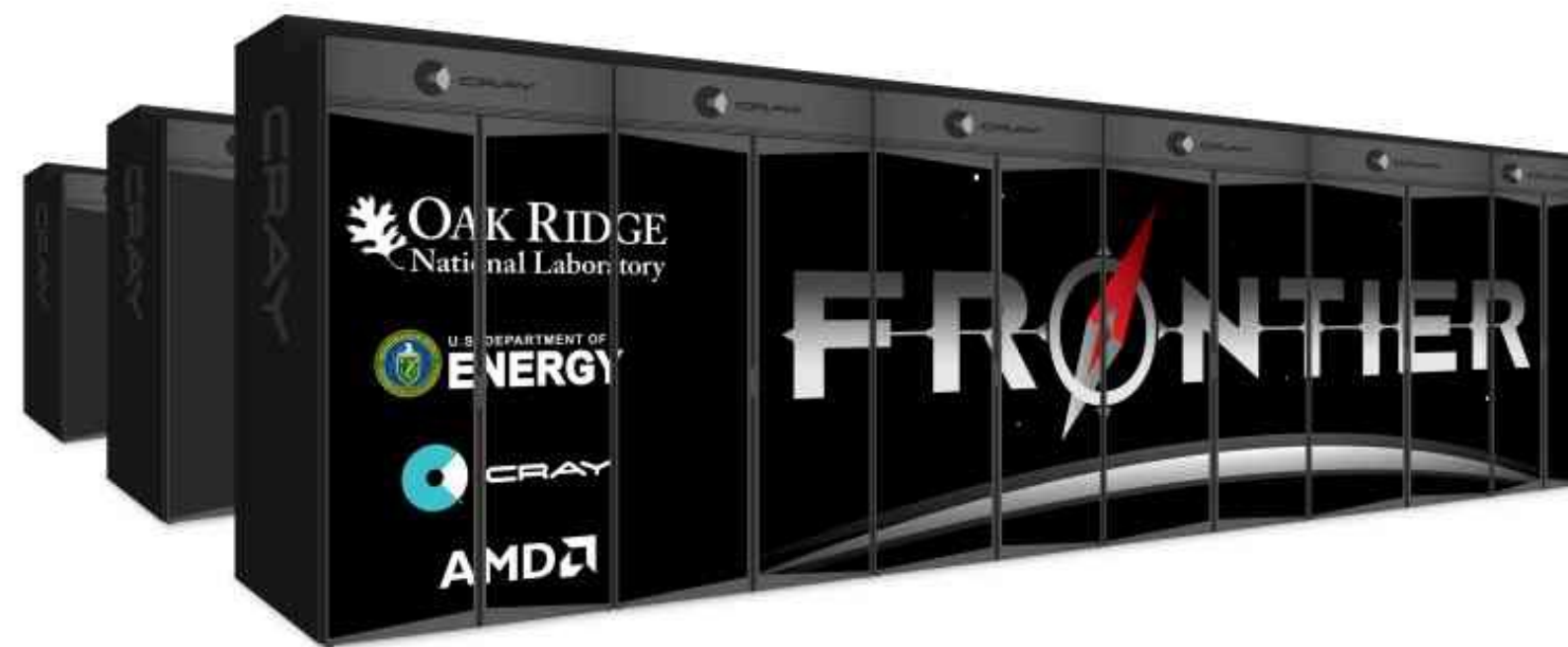
15 TFlop/s

700 GB/s

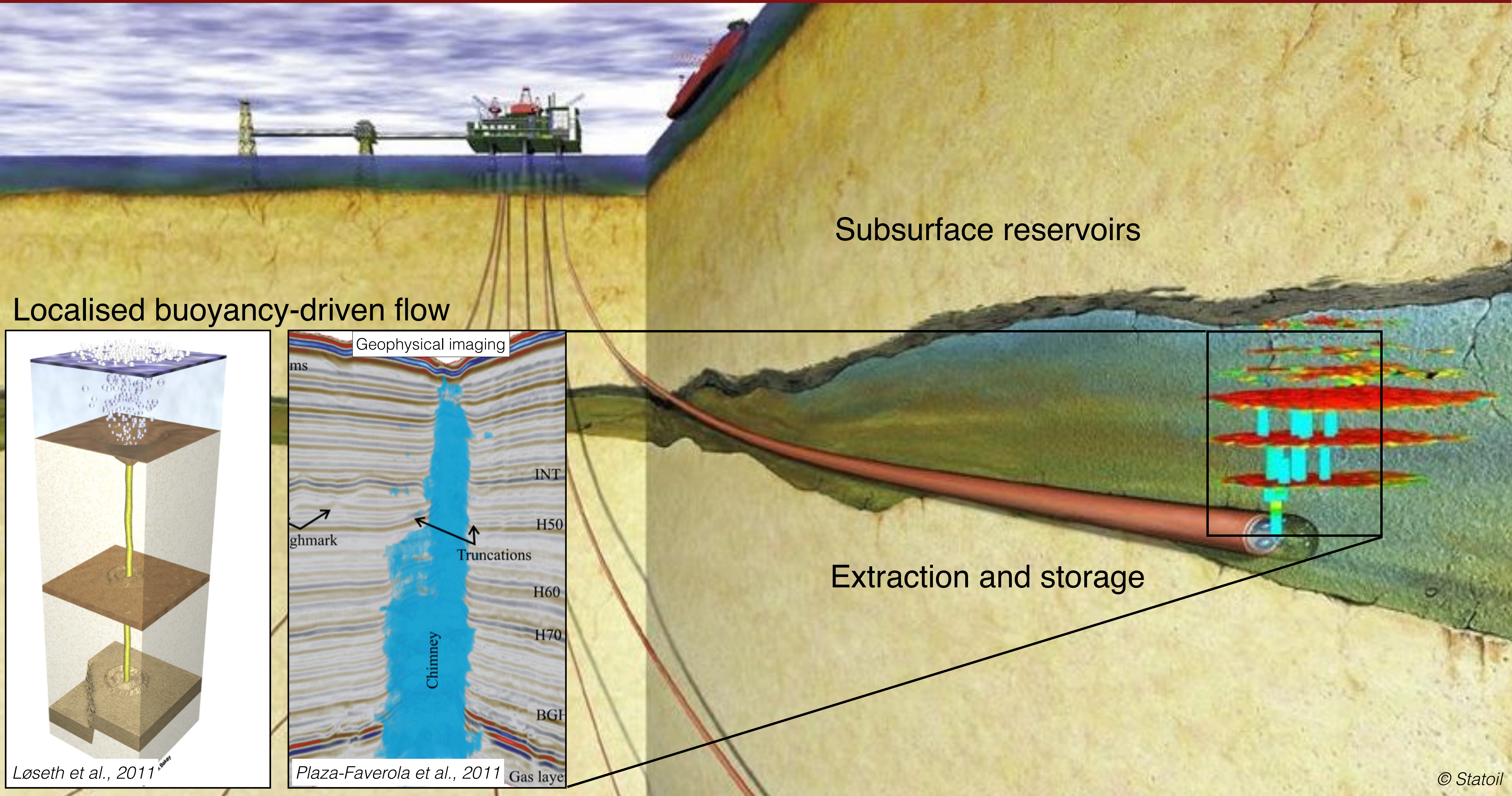
- Supercomputing available on your desk !

# Why to use a GPU

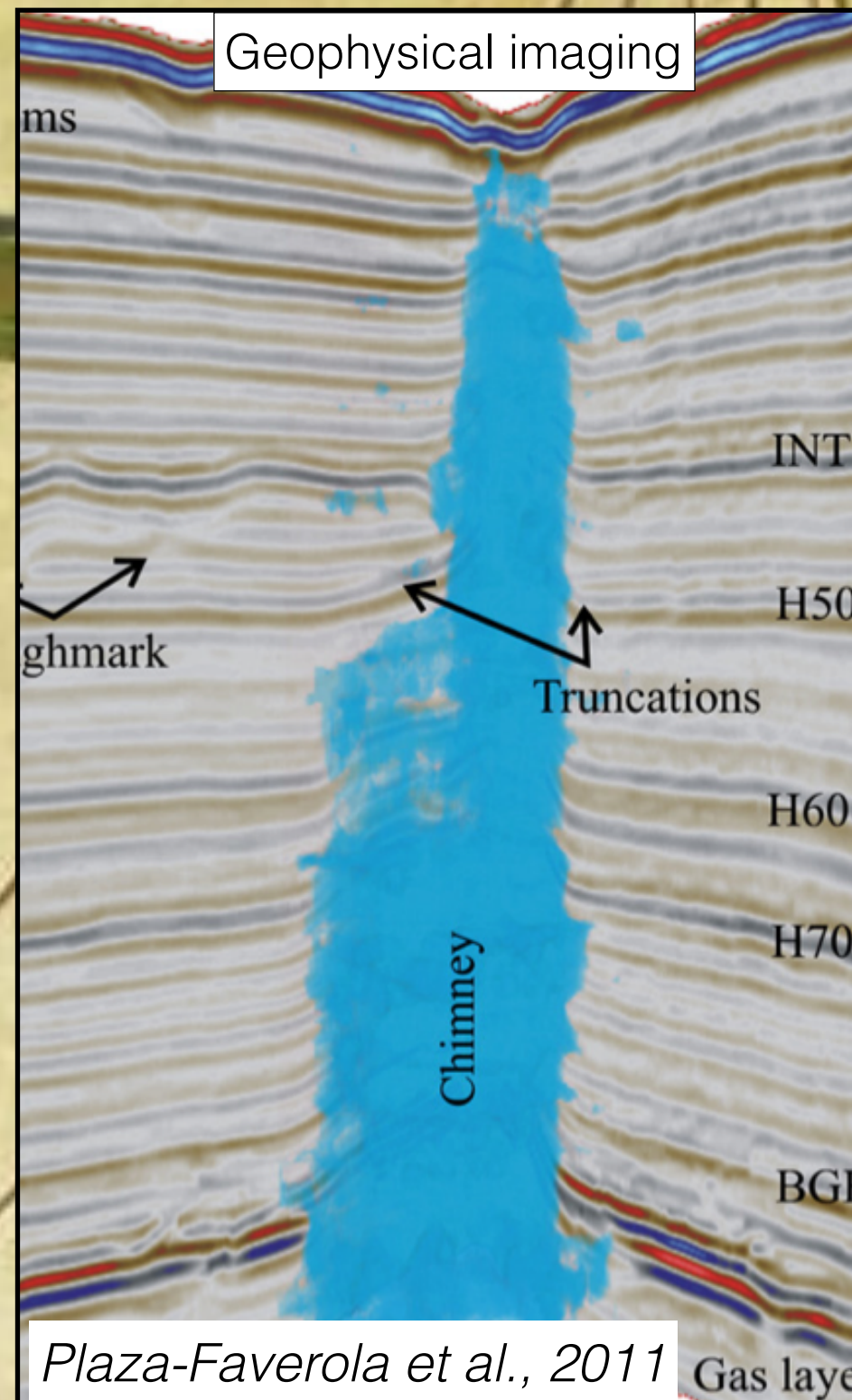
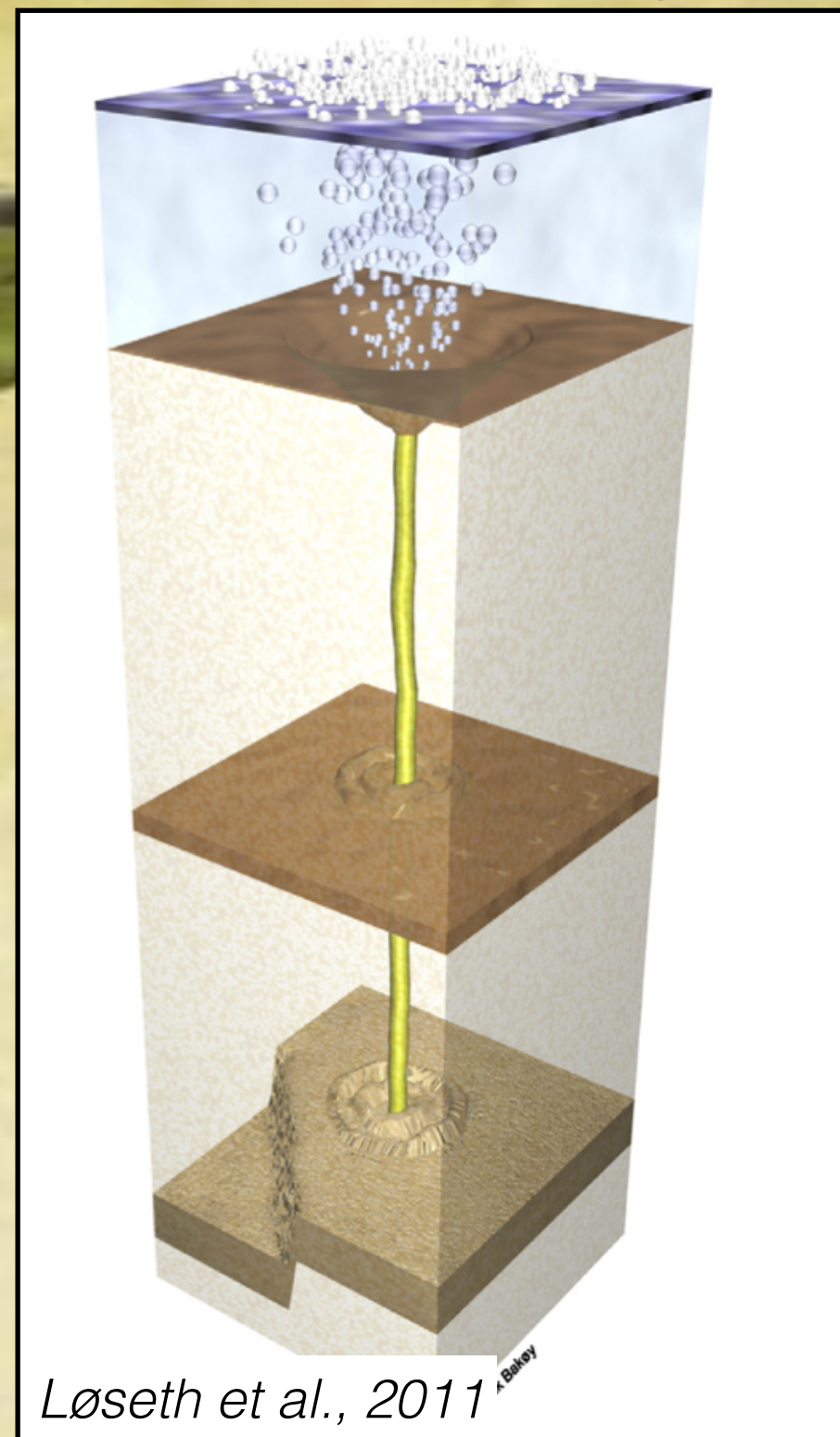
- HPC and supercomputing on your desktop
- World's fastest supercomputer Summit features 27'648 Nvidia V100 GPUs
- Future exascale machines all feature GPUs (Intel + AMD)



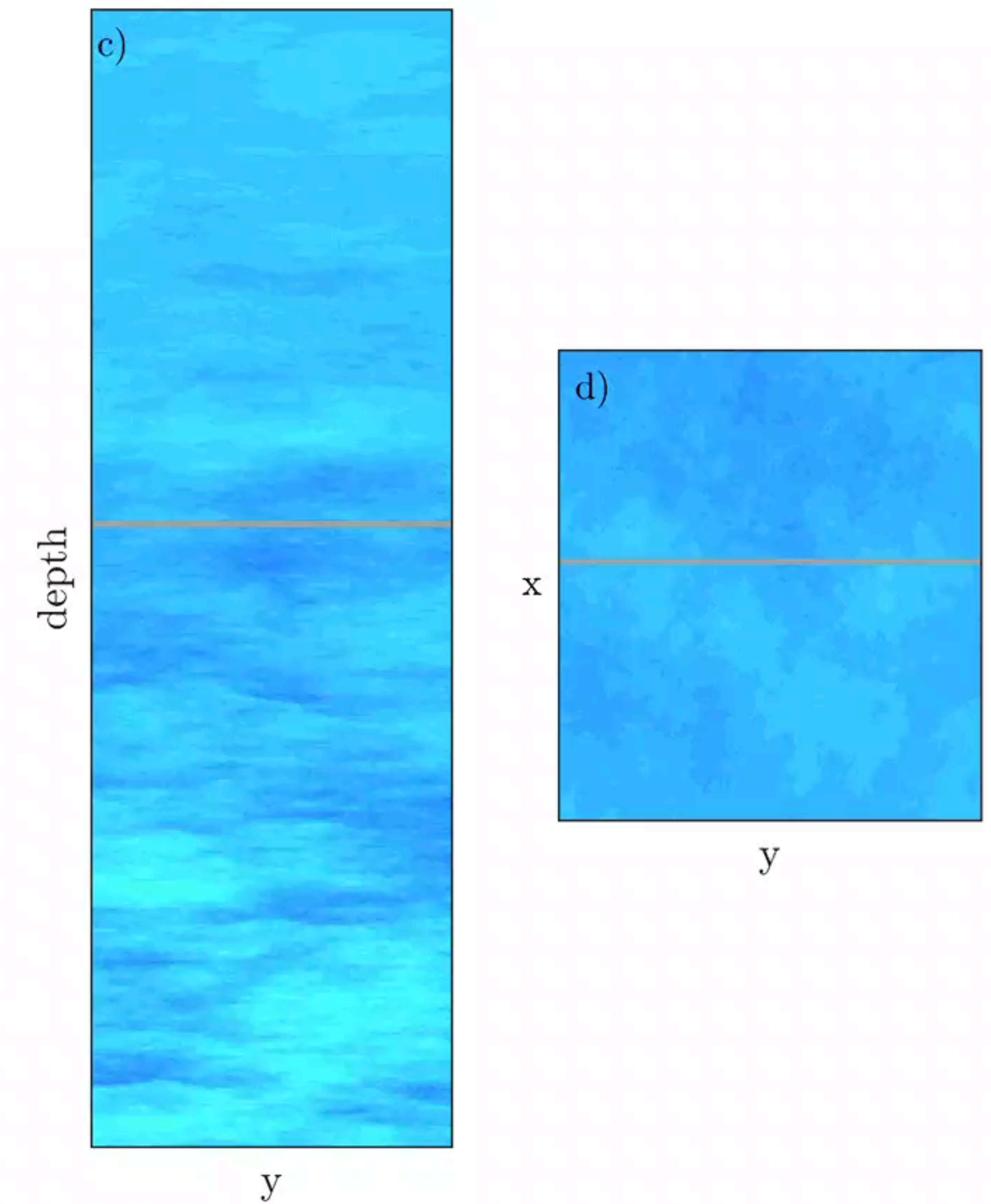
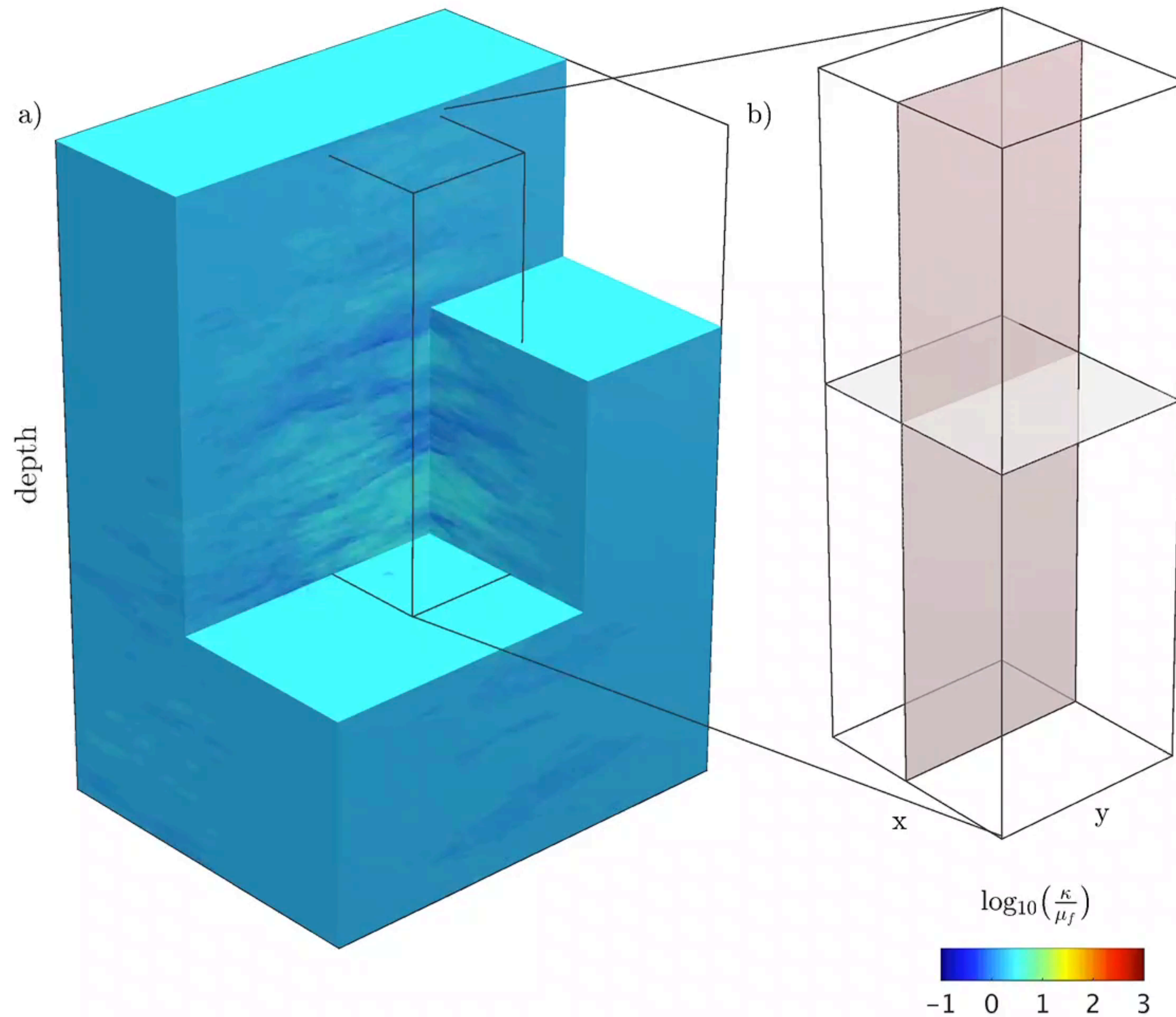




Localised buoyancy-driven flow



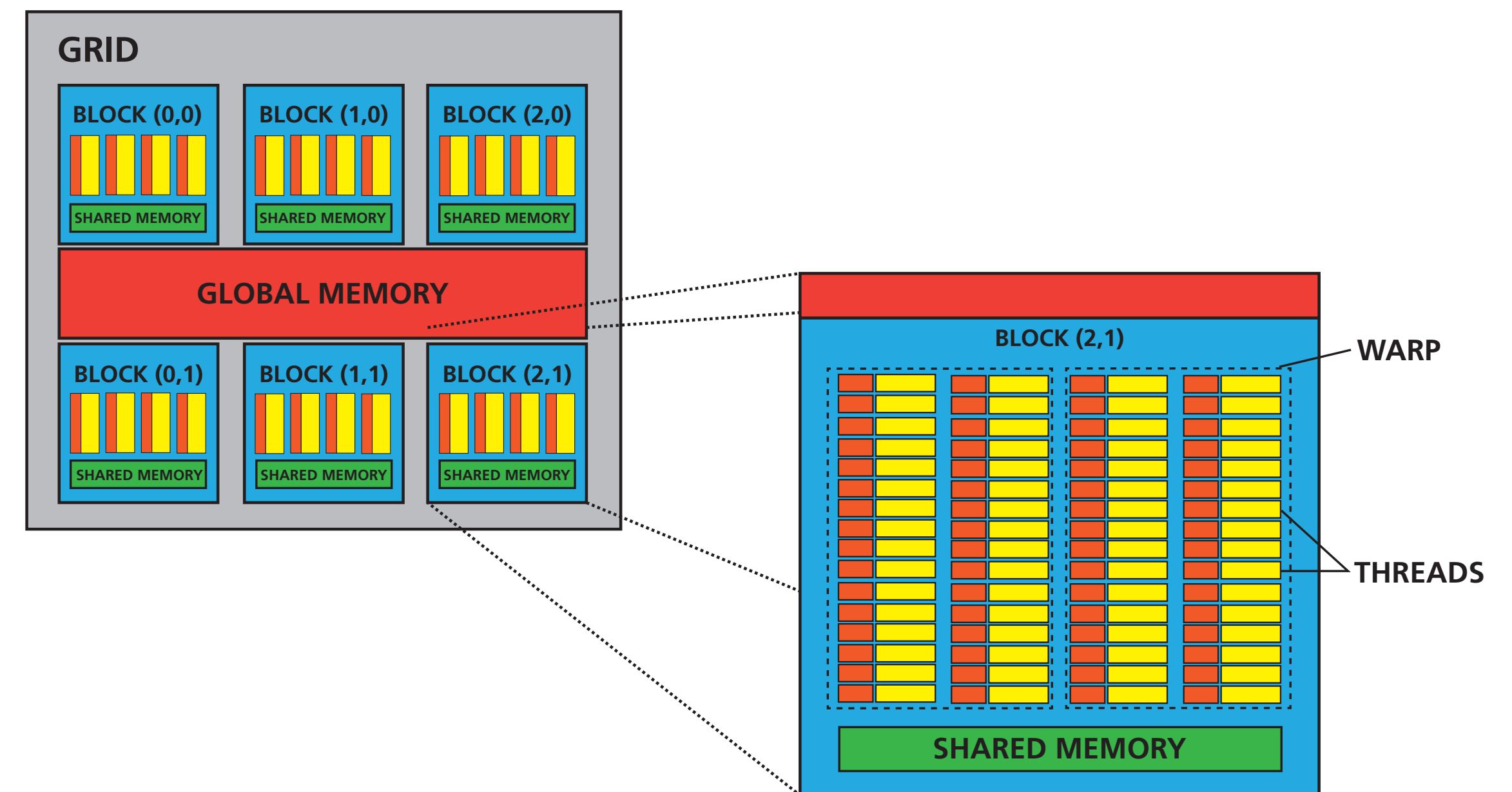




time/ $\tau_c = 1.59\text{e-}03$

# Programming the GPU: CUDA

- CUDA: provides vectorised indexes to C / C++ for parallel execution
- Building elements: `thread`, `block`, `grid`
- Max. 1024 threads per block !
- Assign one thread per grid point
- All threads read the same code  
loop bounds > if statements



# Session 1 - PDEs

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# 1/ diffusion and acoustic wave propagation in 1D

## Diffusion

$$\frac{\partial T}{\partial t} = -\frac{\partial q_x}{\partial x}$$

$$q_x = -D \frac{\partial T}{\partial x}$$

```
% Physics
Lx = 10;
D = 1;
% Numerics
nx = 100;
dx = Lx/nx;
nt = 200;
dt = dx^2/D/2.1;
x = (-Lx+dx)/2:dx:(Lx-dx)/2;
% Initial conditions
T = exp(-x.^2);
```

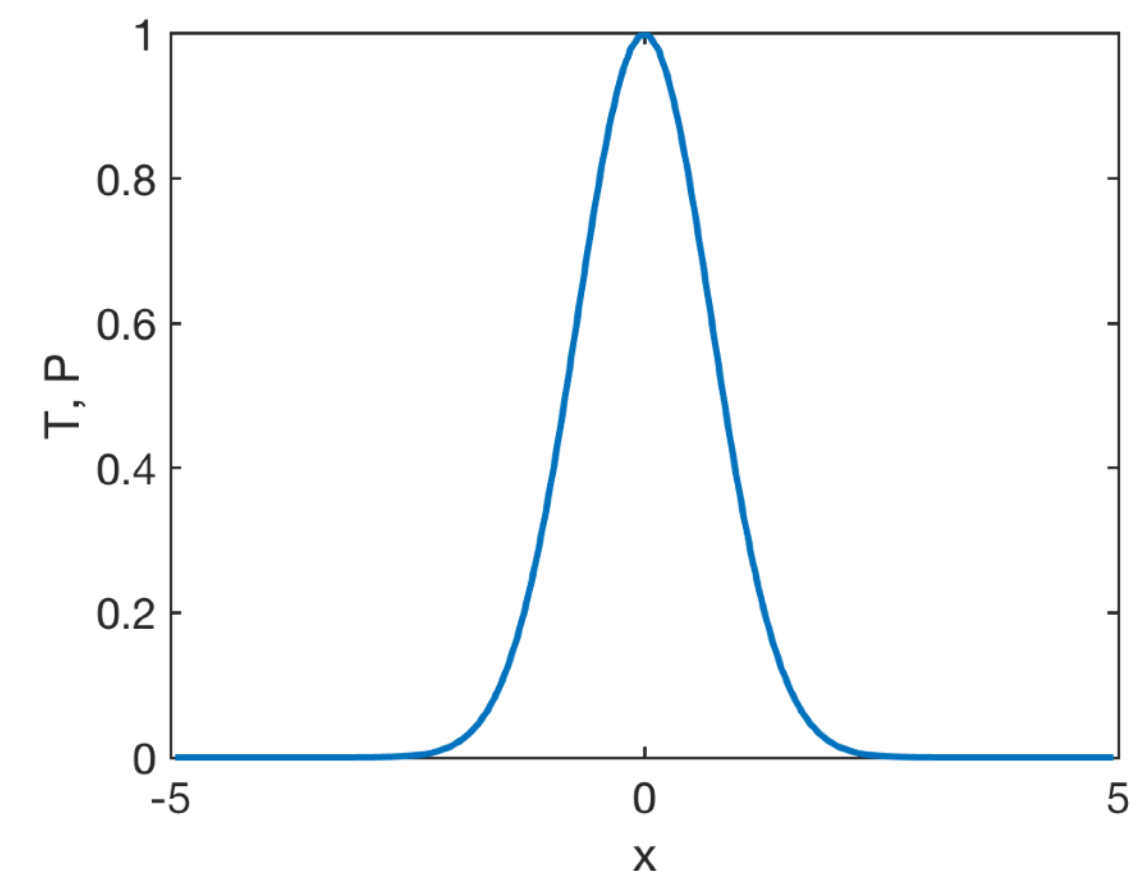
## Acoustic wave

$$\frac{1}{k} \frac{\partial P}{\partial t} = -\frac{\partial v_x}{\partial x}$$

$$\rho \frac{\partial v_x}{\partial t} = -\frac{\partial P}{\partial x}$$

```
% Physics
Lx = 10;
k = 1;
rho = 1;
% Numerics
nx = 100;
dx = Lx/nx;
nt = 200;
dt = dx/sqrt(k/rho)/2.1;
x = (-Lx+dx)/2:dx:(Lx-dx)/2;
% Initial conditions
P = exp(-x.^2);
V = [0*P 0];
```

Initial gaussian perturbation



# 1/ diffusion and acoustic wave propagation in 1D

- Finite-difference method

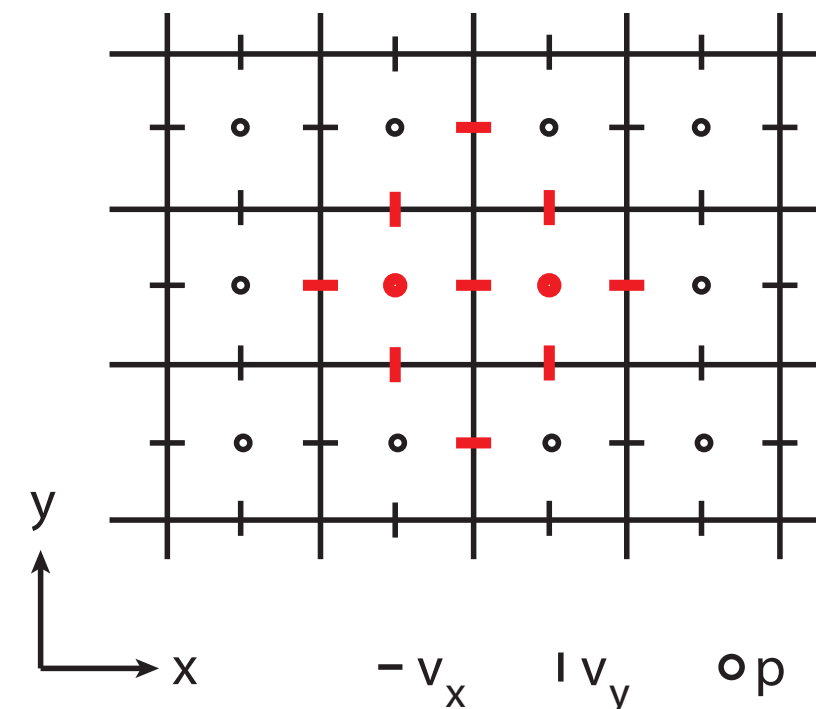
$$\frac{\partial A}{\partial x} \approx \frac{A(ix+1) - A(ix)}{\Delta x}$$

- CFL time step stability for diffusion and wave propagation

$$\text{CFL}_{\text{diff}} = \frac{\min(\Delta x_i)^2}{D \cdot 2.1 n_{\text{dim}}}$$

$$\text{CFL}_{\text{acoust}} = \frac{\min(\Delta x_i)}{\sqrt{k/\rho} \cdot 2.1}$$

- Staggered grid for computation





## 2/ loop vs vectorised approach

- Replace all vectorised statements by for loops

Vectorised version	Loop version
<pre>V(2:end-1) = V(2:end-1) - dt*diff(P)/dx/rho;</pre>	<pre>for ix = 2:nx     V(ix) = V(ix) - dt*(P(ix)-P(ix-1))/dx/rho; end</pre>

# Session 1 - PDEs

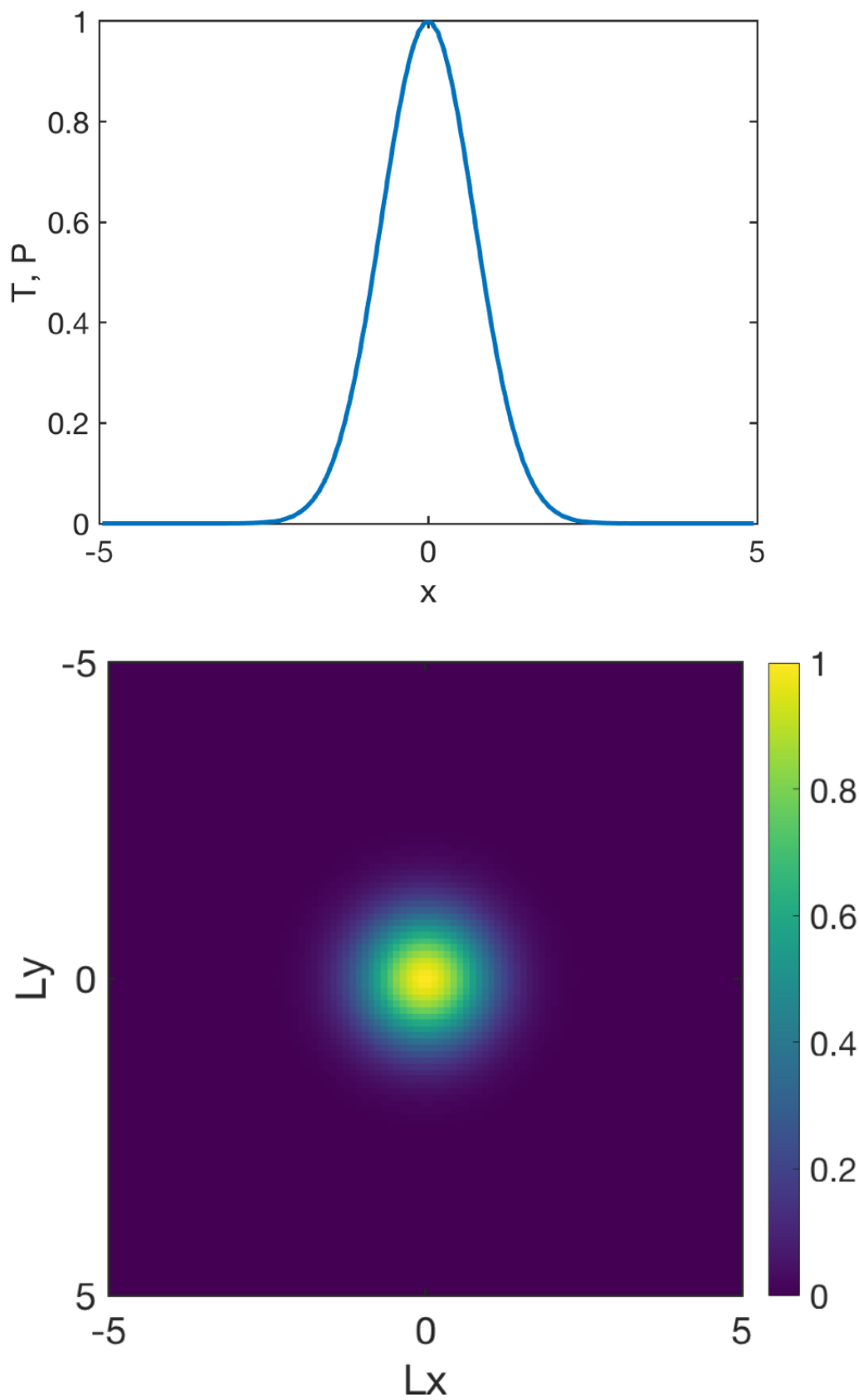
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Task 1/ from 1D to 2D

	Diffusion	Acoustic wave
1D	$\frac{\partial T}{\partial t} = -\frac{\partial q_x}{\partial x}$ $q_x = -D\frac{\partial T}{\partial x}$	$\frac{1}{k}\frac{\partial P}{\partial t} = -\frac{\partial v_x}{\partial x}$ $\rho\frac{\partial v_x}{\partial t} = -\frac{\partial P}{\partial x}$
2D	$\frac{\partial T}{\partial t} = -\left(\frac{\partial q_x}{\partial x} + \frac{\partial q_y}{\partial y}\right)$ $q_x = -D\frac{\partial T}{\partial x}$ $q_y = -D\frac{\partial T}{\partial y}$	$\frac{1}{k}\frac{\partial P}{\partial t} = -\left(\frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y}\right)$ $\rho\frac{\partial v_x}{\partial t} = -\frac{\partial P}{\partial x}$ $\rho\frac{\partial v_y}{\partial t} = -\frac{\partial P}{\partial y}$
hint	<code>[x2,y2] = ndgrid(x,y);</code>	<code>[x2,y2] = ndgrid(x,y);</code>

Initial gaussian perturbation





## Task 1/ from 2D to 3D

	Diffusion	Acoustic wave
2D	$\frac{\partial T}{\partial t} = - \left( \frac{\partial q_x}{\partial x} + \frac{\partial q_y}{\partial y} \right)$ $q_x = -D \frac{\partial T}{\partial x}$ $q_y = -D \frac{\partial T}{\partial y}$	$\frac{1}{k} \frac{\partial P}{\partial t} = - \left( \frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} \right)$ $\rho \frac{\partial v_x}{\partial t} = - \frac{\partial P}{\partial x}$ $\rho \frac{\partial v_y}{\partial t} = - \frac{\partial P}{\partial y}$
3D	$\frac{\partial T}{\partial t} = - \left( \frac{\partial q_x}{\partial x} + \frac{\partial q_y}{\partial y} + \frac{\partial q_z}{\partial z} \right)$ $q_x = -D \frac{\partial T}{\partial x}$ $q_y = -D \frac{\partial T}{\partial y}$ $q_z = -D \frac{\partial T}{\partial z}$	$\frac{1}{k} \frac{\partial P}{\partial t} = - \left( \frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} + \frac{\partial v_z}{\partial z} \right)$ $\rho \frac{\partial v_x}{\partial t} = - \frac{\partial P}{\partial x}$ $\rho \frac{\partial v_y}{\partial t} = - \frac{\partial P}{\partial y}$ $\rho \frac{\partial v_z}{\partial t} = - \frac{\partial P}{\partial z}$

## Task 2/ 2D acoustic to elastic

## Acoustic waves

$$\frac{1}{k} \frac{\partial P}{\partial t} = - \left( \frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} \right)$$

$$\rho \frac{\partial v_x}{\partial t} = - \frac{\partial P}{\partial x}$$

$$\rho \frac{\partial v_y}{\partial t} = - \frac{\partial P}{\partial y}$$

## Elastic waves

$$\frac{1}{k} \frac{\partial P}{\partial t} = - \left( \frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} \right)$$

$$\rho \frac{\partial v_x}{\partial t} = - \frac{\partial P}{\partial x} + \frac{\partial \tau_{xx}}{\partial x} + \frac{\partial \tau_{xy}}{\partial y}$$

$$\rho \frac{\partial v_y}{\partial t} = - \frac{\partial P}{\partial y} + \frac{\partial \tau_{yy}}{\partial y} + \frac{\partial \tau_{xy}}{\partial x}$$

$$\frac{\partial \tau_{xx}}{\partial t} = 2G \left( \frac{\partial v_x}{\partial x} - \frac{1}{3} \left( \frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} \right) \right)$$

$$\frac{\partial \tau_{yy}}{\partial t} = 2G \left( \frac{\partial v_y}{\partial y} - \frac{1}{3} \left( \frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} \right) \right)$$

$$\frac{\partial \tau_{xy}}{\partial t} = 2G \frac{1}{2} \left( \frac{\partial v_x}{\partial y} + \frac{\partial v_y}{\partial x} \right)$$

## Task 3/ 2D elastic to viscous

Elastic waves	Viscous flow
$\frac{1}{k} \frac{\partial P}{\partial t} = - \left( \frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} \right)$	$\frac{1}{k} \frac{\partial P}{\partial t} = - \left( \frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} \right)$
$\rho \frac{\partial v_x}{\partial t} = - \frac{\partial P}{\partial x} + \frac{\partial \tau_{xx}}{\partial x} + \frac{\partial \tau_{xy}}{\partial y}$	$\rho \frac{\partial v_x}{\partial t} = - \frac{\partial P}{\partial x} + \frac{\partial \tau_{xx}}{\partial x} + \frac{\partial \tau_{xy}}{\partial y}$
$\rho \frac{\partial v_y}{\partial t} = - \frac{\partial P}{\partial y} + \frac{\partial \tau_{yy}}{\partial y} + \frac{\partial \tau_{xy}}{\partial x}$	$\rho \frac{\partial v_y}{\partial t} = - \frac{\partial P}{\partial y} + \frac{\partial \tau_{yy}}{\partial y} + \frac{\partial \tau_{xy}}{\partial x}$
$\frac{\partial \tau_{xx}}{\partial t} = 2G \left( \frac{\partial v_x}{\partial x} - \frac{1}{3} \left( \frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} \right) \right)$	$\tau_{xx} = 2\eta \left( \frac{\partial v_x}{\partial x} - \frac{1}{3} \left( \frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} \right) \right)$
$\frac{\partial \tau_{yy}}{\partial t} = 2G \left( \frac{\partial v_y}{\partial y} - \frac{1}{3} \left( \frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} \right) \right)$	$\tau_{yy} = 2\eta \left( \frac{\partial v_y}{\partial y} - \frac{1}{3} \left( \frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} \right) \right)$
$\frac{\partial \tau_{xy}}{\partial t} = 2G \frac{1}{2} \left( \frac{\partial v_x}{\partial y} + \frac{\partial v_y}{\partial x} \right)$	$\tau_{xy} = 2\eta \frac{1}{2} \left( \frac{\partial v_x}{\partial y} + \frac{\partial v_y}{\partial x} \right)$

# Task 4/ 2D viscous vectorised to loop

- Use linear 1D indexing in 2D and 3D:

$$P(ix, iy) \Rightarrow P(ix + iy * nx)$$

$$P(ix, iy, iz) \Rightarrow P(ix + iy * nx + iz * nx * ny)$$

- Check bounds with loop start and end index

Vectorised version	Loop version
<pre>txy = zeros(nx+1,ny+1); txy(2:end-1,2:end-1) = ...;</pre>	<pre>txy = zeros((nx+1)*(ny+1),1); for iyM=2:ny, iy=iyM-1;     for ix=2:nx         txy(ix+iy*(nx+1)) = ...;     end end</pre>

# Outlook - Session 2

- Topic: Intro to GPU computing
- Programming: Wave propagation in 1D and 2D (GPU CUDA C version)
- Tasks: 2D and 3D acoustic, elastic and/or viscous
- Mandatory for session 2: 2D acoustic/elastic/viscous loop code.

Please give me your SUNet ID if you are attending the class  
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That's it for today

- ● ● [wp.unil.ch/geocomputing/](http://wp.unil.ch/geocomputing/)

- ● ● [Iraess@stanford.edu](mailto:Iraess@stanford.edu)

