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Computing, Engineering & Mathematics ASSIGNMENT / REPORT COVER SHEET

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Student name: Student number:	Sonali Marasini 19913230	Student name: Student number:			
Sections completed individually		Sections completed individually			
Unit name & number	Data Science: 301044				
Tutorial day and time:	Friday 11 am to 1 pm				
Title of Assignment:	World Happiness Report				
Student Submitting the Assignment:	Sonali Marasini				
Date submitted:	16/10/2020				
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World Happiness Report for Data Science Assignment

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Abstract—This paper reviews the correlation between the happiness score of several countries and socioeconomic factors using several data modelling and analysing techniques. These models have been tested and validated. In the end, it has been found that there is a direct relationship between several socioeconomic factors of a country and the happiness of the people of that country. However, since happiness is a tricky aspect to measure, a further detailed study needs to be conducted to discover what other factors could affect the happiness of an individual.

1. Introduction

A healthy mindset requires inner happiness. Despite mental health being as important as physical health, it is often overlooked. This happiness is a feeling and can be a difficult thing to measure.

A ground-breaking study of the state of global happiness, the World Happiness Report, rates 156 countries by how happy their people consider themselves to be. [1], [2] have reported this study in detail. This study mainly centres on the innovations, societal norms, disputes, and policies of the government that have been used in ranking these countries.

There are six factors used to determine the happiness score of each country and rank them in the happiness ladder. The six factors are levels of Gross Domestic Product (GDP), life expectancy, generosity, social support, freedom, and corruption.

This study has combined data from the years 2017 through 2019 to make the sample size large enough for accurate study. The typical annual sample they have collected 1000 people, meaning through 3 years they have collected 3000 samples per country.

2. Data Exploration and Pre-processing

2.1. Data Cleaning

There are 156 observations in the dataset. There are six independent variables namely, GDP per capita, Social support, Healthy life expectancy, Freedom to make life choices, Generosity, and Perceptions of corruption. The predictor

variable is the happiness score which is calculated using all these independent variables. Based on the happiness score, all the 156 countries are then ranked with 1 being the country with the highest happiness score and 156 being the country with the lowest happiness score.

A new column with the name Score Level has been added to the data set. This column has two values 'H' and 'L' depending on the value of the happiness score. If the happiness score is less than or equal to 5.99 then, the Score Level is 'L' indicating a low happiness score whereas, if the happiness score is more than 5.99 then the Score Level for that country is 'H' indicating a high happiness score.

A few values in the data set are found to be 0. The zeroes in the data set have been replaced with the mean value of the entire column values. This has been done so that the modelling gives a more accurate result.

2.2. Data Relationship

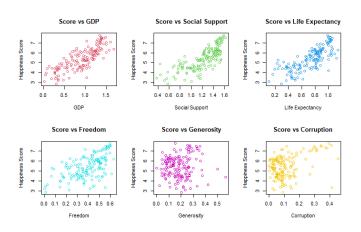


Figure 1. Data Relationship

The relationship between the independent variables and the outcome variable has been plotted in figure 1. There seems to be a strong linear relationship between the happiness score against GDP, social support, and life expectancy of a country. There does not seem to be a linear pattern between happiness score and generosity and happiness score and corruption. Lastly, the relationship between happiness score and freedom seems to be linear but a weak one.

2.3. Correlation

[3] has defined correlation coefficient as a kind of numerical measure to determine a statistical relationship between any two variables. To find out if the independent variables have a positive or a negative relationship with the outcome variable, the correlation values were calculated. All the variables have a positive correlation with the outcome variable. As expected, from the plots, GDP, social support, and life expectancy have a strong positive relationship with the happiness score with correlation coefficients of 0.7964624, 0.7727645, and 0.7709061 respectively. Generosity has the weakest relationship with a correlation coefficient of 0.07582369. The correlation coefficients of freedom and corruption are 0.5667418 and 0.3856131 respectively.

3. Aims and Objectives

The objective of this data science study is to analyse the happiness score data and determine if there is any pattern. The aim is to predict the happiness score of any country given the independent variable values. The goal is to see if out of the several socio-economic factors, which factors have the most impact on the happiness score.

4. Multiple Linear Regression

4.1. Fitting a Model

Multiple Linear Regression is a statistical technique that predicts the outcome of an outcome variable using multiple explanatory variables. [4] A multiple linear regression model has been constructed and the least square estimates of the model parameters have been calculated. The fitted model is as follows.

E(Happiness Score) = 1.6589 + 0.8570 GDP + 1.2354 SocialSupport + 0.9781 LifeExpectancy + 1.3963 Freedom + 0.5910 Generosity + 0.8384 Corruption

4.2. Testing the Significance

TABLE 1. P VALUES

Variables	P Values
GDP	0.000123
Social Support	1.19e-06
Life Expectancy	0.005350
Freedom	0.000306
Generosity	0.241562
Corruption	0.132554

Hypothesis testing has been conducted to test the significance of the model parameters, $H_0 = \beta_i \ vs \ H_1 \neq \beta_i$. The

p values of the coefficient parameters for different variables is given in table 1.

It can be observed that the p values for Generosity and Corruption are greater than 0.05. Thus, there is not enough evidence to reject null hypothesis for Generosity and Corruption. Thus, Generosity and Corruption do not have any significant effect on the happiness score. Hence, the resulting model can be obtained by removing these variables from the predictors. The model thus obtained is,

E(Happiness Score) = 1.7773 + 0.8924 GDP + 1.1315 SocialSupport + 1.0197 LifeExpectancy + 1.7710 Freedom

In this model, the R squared value is calculated to be 0.7686. This implies that about 76.86% of the variation in the dataset is explained by the model.

4.3. Assessing the Accuracy

The variance table has been analysed to assess the accuracy of the model. From the Anova table, F statistics = 125.4 on 4 and 151 degree of freedom which is greater than 2.431562. Hence, the model is adequate and GDP, Social Support, Life Expectancy, and Freedom variables have significant linear relationship with Happiness Score.

4.4. Residuals

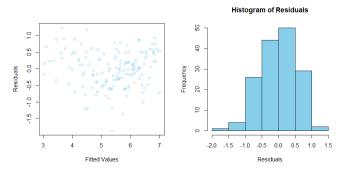


Figure 2. Residuals

In figure 2, the residuals from the model have been plotted against the predicted values and the histogram of the residuals has been created. It can be depicted that the mode is closer to zero and the residuals follow a normal distribution which is slightly positively skewed.

The residuals have been plotted in figure 3. We would expect the residuals versus predicted values plot to be random. The first graph shows a nonlinear pattern. Hence, the linearity assumption is violated. There is some pattern is the residual implying that the pattern in the dataset is not completely captured by the model.

5. Cross Validation

Cross-validation is a technique of resampling used on a small data set to validate models. Six different models with

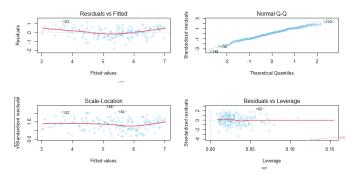


Figure 3. Residual Plots

different variables and combination of these variables have been created. A validation set approach for each of these models have been used and the goal is to select the model with minimum validation error.

The data set has been divided into training and validation in the ratio of 60:40. The data is then fitted in the six different models. Out of these six models, the first model has one variable, second model has two variables, third model has three variables and so on. Using these model, the target variable is predicted for training data and validation data. Similarly, Leave One Out Cross Validation (LOOCV) and K-Fold Validation is done in these six models. The value of K is considered as 10. The errors calculated from these four different cross validation approaches has been shown in table 2.

TABLE 2. ERRORS

	Model1	Model2	Model3	Model4	Model5	Model6
Training	0.3849502	0.3294415	0.3146589	0.2715977	0.2674578	0.2516869
Validation	0.5488410	0.4050460	0.3814438	0.3090415	0.3051749	0.3287890
10-Fold	0.4593798	0.3793884	0.3583951	0.3085208	0.3098113	0.3150800
LOOCV	0.4610816	0.3671266	0.3543573	0.3047021	0.3044499	0.3065170

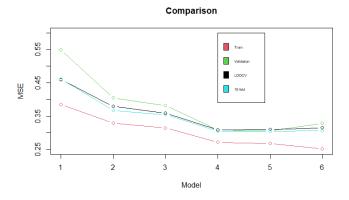


Figure 4. Validation Set Approach

The mean squared values for training, validation, LOOCV and 10-Fold for these six models are plotted in

figure 4. Upon observing the plot, it can be deduced that that the best selection would be model 4. Model 4 has been created using variables GDP, social support, life expectancy, freedom and generosity.

6. Decision Trees

6.1. Classification Tree

There is a categorical variable with the name of Score Level created in the data set in the preprocessing stage. This variable has been converted into a factor variable. The data set has been divided into training and testing data set. A classification decision tree has been fitted on the training data set. The decision tree is shown in figure 5.

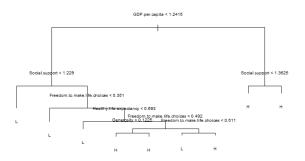


Figure 5. Decision Tree

In this decision tree, there are 9 terminal nodes. The variables that are actually included in the tree construction are GDP, social support, freedom, life expectancy and generosity. Corruption has not been considered while making this tree. We can deduce that this variable is not needed to make the model more significant.

6.2. Pruning

The cross-validation plot is shown in figure 6. According to the cross-validation plot, a rapid decrease can be observed from order 1 to order 2. From this point, there is a constant decrease till order 7 and the plot is somewhat constant after. Therefore, it can be deduced that the best size of the tree model is 7.

The pruned classification tree as shown in figure 7 has 7 terminal nodes. The variables that have been included in this pruned tree are GDP, social support, life expectancy and freedom. From the classification decision tree, it can be concluded that higher the GDP the higher the happiness score. Similarly, life expectancy and freedom also have a positive impact on happiness score.

6.3. Testing the Accuracy

The accuracy of the model on the training data is 0.05645 or 5.6%. It is obvious that the model would perform well in the training data set.

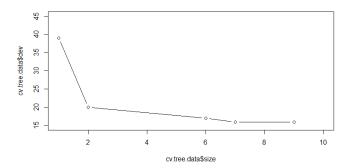


Figure 6. Cross Validation Plot

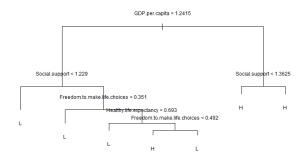


Figure 7. Pruned Tree

To determine if the model has good accuracy, it needs to perform well on the test data set. The target variable for the test data set have been predicted. The predicted values have been compared against the actual values. The confusion matrix for the test data set is shown in table 3.

TABLE 3. CONFUSION MATRIX

		Predicted		
		Η	L	
A atrial	Η	12	4	
Actual	L	1	15	

Therefore, it the misclassification rate for the testing data is calculated to be 0.15625 or 15.625%. This training misclassification rate is significantly higher than the testing misclassification rate. Therefore, it could be said that the model is overfitting in the training data set.

7. Principal Component Analysis

Principle Component Analysis (PCA) is an unsupervised learning technique which has been performed to increase the interpretability of the data set without the loss of information. [5] First, the mean and the variance of the independent variables have been observed as seen on table 4.

TABLE 4. MEAN AND VARIANCE

	GDP	SocSupp	LifExp	Freedom	Generos	Corrup
Mean	0.9051474	1.2088141	0.7252436	0.3925705	0.1848462	0.1106026
Variance	0.9051474	1.2088141	0.7252436	0.3925705	0.1848462	0.1106026

Scaling has been done to avoid the variable with the highest mean dominate the first principle component. The coefficients required to calculate the six different principle component is given in table 5.

TABLE 5. PCA

	PC1	PC2	PC3	PC4	PC5	PC6
GDP	-0.51459462	0.2278181	-0.02380878	0.2404018	-0.183763758	-0.76887077
Social Support	-0.49064918	0.2202837	0.28141961	-0.0633134	0.771259058	0.18081020
Life Expectancy	-0.51056655	0.1922719	0.02808632	0.2748057	-0.509355608	0.60547761
Freedom	-0.38095770	-0.3521218	0.11855036	-0.8104252	-0.240066817	-0.04905325
Generosity	-0.05948407	-0.6935067	0.58081716	0.4189146	-0.005250993	-0.05142470
Corruption	-0.29173692	-0.5076063	-0.75368730	0.1743609	0.232996913	0.06701907

Using these coefficients, the principle components can be represented as below,

PC1 = -0.51583025 * GDP - 0.48232080 * Social Support - 0.50821063 * Life Expectancy - 0.38551214 * Freedom - 0.05806569 * Generosity - 0.30168944 * Corruption

PC2 = 0.2082045 * GDP + 0.2223429 * Social Support + 0.2141943 * Life Expectancy - 0.3435152 * Freedom - 0.7039110 * Generosity - 0.4978373 * Corruption

PC3 = -0.07765971 * GDP + 0.35572318 * Social Support - 0.05577799 * Life Expectancy + 0.24935585 * Freedom + 0.48379134 * Generosity - 0.75371507 * Corruption

PC4 = 0.22026792 * GDP + 0.02339788 * Social Support + 0.26912517 * Life Expectancy - 0.78471459 * Freedom + 0.51123624 * Generosity + 0.03696948 * Corruption

PC5 = -0.27711289 * GDP + 0.76435099 * Social Support - 0.43511439 * Life Expectancy - 0.23541908 * Freedom - 0.06950865 * Generosity + 0.29899478 * Corruption

PC6 = -0.7478164713 * GDP + 0.0813105789 * Social Support + 0.6564896736 * Life Expectancy + 0.0004850166 * Freedom - 0.0298279513 * Generosity + 0.0478589759 * Corruption

The plot of the resultant principal components is given in figure 8. It can be observed that for PC1 the variables GDP, Social Security and Life Expectancy have contributed the

most whereas the highest contribution to PC2 is Generosity followed by Corruption and Freedom.

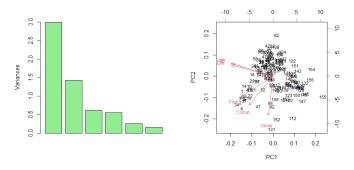


Figure 8. PCA

The proportional variances explained by each principle component have been computed. These values have been plotted in 9. It can be observed that the first principle component explains about 49.8% of the variation in the data, the second principle component covers about 23.7% of the variation, the third principle component covers about 10.1% of the variation and 9% of the variation is covered by the fourth principle component. Therefore, more than 90% of the variation of the data set is covered by the first four principle components.

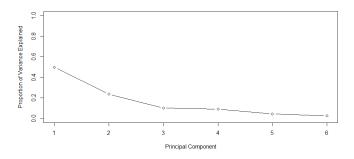


Figure 9. PVE

8. Models Comparison

TABLE 6. MULTIPLE LINEAR REGRESSION COMPARISION

	R squared	F statistic	P Value
Model 1	0.7673	86.16 on 6 and 149 DF	< 2.2e-16
Model 2	0.7625	125.4 on 4 and 151 DF	< 2.2e-16

The models which have been created in this study have given similar result. Upon analysing the p values in the multiple linear regression model, as shown in table 1, it has been deduced that generosity and corruption do not have significant impact on the happiness score. This deduction has been further solidified by the cross validation approach. Looking at the error comparison as seen in figure 4, it can be concluded that the model created with only GDP, social security, life expectancy and freedom is the best model. The statistical values of the two linear regression models which were created earlier can be seen in table 6.

TABLE 7. DECISION TREE COMPARISION

	Terminal Nodes	Residual Mean Deviance	Error Rate
Model 1	9	0.2226	0.05645
Model 2	7	0.2699	0.06452

In the decision tree model, the misclassification error rate has not been changed by pruning. It has been deemed redundant to apply the pruning on the decision tree as there has been no improvement in the accuracy. The statistical comparision between the decision tree model before and after pruning is given in 7.

Lastly, from Principle Component Analysis, it has been inferred that more than 90% of the variation in the data is explained by the first four principle components.

9. Results and Recommendation

Upon the completion of this data analysis study, it can be concluded that factors such as GDP, social security, life expectancy and freedom have a huge impact on the perception of happiness of people. Objectively, it can be said that if these factors are positive in a country, the people of the country are deemed happier. It has also been proved that corruption and generosity have no significant impact on the happiness score.

It is recommended that factors like unemployment rate, literacy rate and crime rate be taken into account while calculating the happiness score. It would be interesting to see the relationship between these factors and the impact they might have on the people.

This research study has been an extremely fruitful and informative learning experience.

Acknowledgments

The author would like to thank Dr. Liwan Liyanage for the opportunity to conduct this research study. The knowledge provided by Dr. Liyanage along with Lakmini Weiss in Data Science class has been instrumental in the successful completion of this report. The author would also like to acknowledge Western Sydney University for providing the requisite resources for this research study.

References

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- [4] R. H. Myers and R. H. Myers, Classical and modern regression with applications. Duxbury press Belmont, CA, 1990, vol. 2.
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Appendix

Sonali Marasini

29/09/2020

```
#packages
library(dplyr)
## Warning: package 'dplyr' was built under R version 4.0.2
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
library(tree)
## Warning: package 'tree' was built under R version 4.0.2
library(boot)
#reading data
data<-read.csv('C:/Users/sonal/Desktop/WSU/2020 Spring/Data Science/Assignment/2019.csv')
head(data)
     Overall.rank Country.or.region Score GDP.per.capita Social.support
##
## 1
                            Finland 7.769
                                                                    1.587
                1
                                                    1.340
## 2
                2
                            Denmark 7.600
                                                    1.383
                                                                    1.573
## 3
                3
                             Norway 7.554
                                                    1.488
                                                                    1.582
## 4
                4
                            Iceland 7.494
                                                    1.380
                                                                    1.624
## 5
                5
                                                                    1.522
                        Netherlands 7.488
                                                    1.396
## 6
                        Switzerland 7.480
                                                    1.452
                                                                    1.526
##
     Healthy.life.expectancy Freedom.to.make.life.choices Generosity
## 1
                       0.986
                                                     0.596
                                                                 0.153
## 2
                       0.996
                                                     0.592
                                                                 0.252
## 3
                       1.028
                                                     0.603
                                                                 0.271
```

0.591

0.354

1.026

4

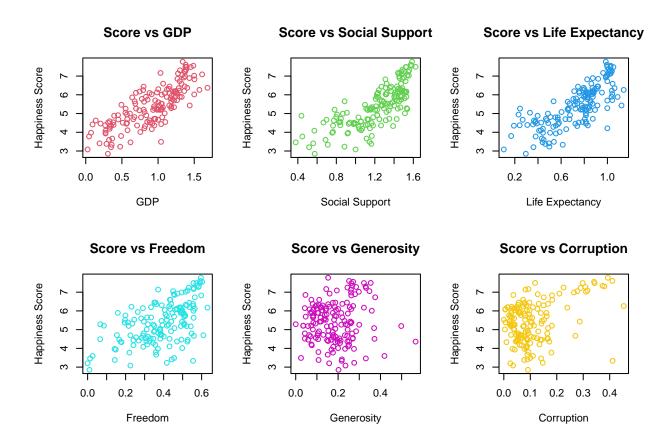
```
## 5
                                                     0.557
                                                                0.322
                       0.999
## 6
                       1.052
                                                     0.572
                                                                0.263
    Perceptions.of.corruption
## 1
                         0.393
## 2
                         0.410
## 3
                         0.341
## 4
                         0.118
                         0.298
## 5
## 6
                         0.343
#checking if all the independent variables are numeric or not
sapply(data,class)
##
                   Overall.rank
                                            Country.or.region
##
                      "integer"
                                                  "character"
##
                          Score
                                               GDP.per.capita
##
                      "numeric"
                                                    "numeric"
##
                 Social.support
                                     Healthy.life.expectancy
                                                    "numeric"
##
                      "numeric"
## Freedom.to.make.life.choices
                                                   Generosity
                      "numeric"
                                                    "numeric"
##
##
      Perceptions.of.corruption
##
                      "numeric"
#data cleaning
#replacing Os with NA
data[data == 0] <- NA</pre>
View(data)
#replacing NAs with the mean of the column
data$GDP.per.capita[is.na(data$GDP.per.capita)] <- round(mean(data$GDP.per.capita, na.rm = TRUE))
data$Social.support[is.na(data$Social.support)] <- round(mean(data$Social.support, na.rm = TRUE))
data$Healthy.life.expectancy[is.na(data$Healthy.life.expectancy)] <- round(mean(data$Healthy.life.expec
data$Freedom.to.make.life.choices[is.na(data$Freedom.to.make.life.choices)] <- round(mean(data$Freedom.
data$Generosity[is.na(data$Generosity)] <- round(mean(data$Generosity, na.rm = TRUE))
data$Perceptions.of.corruption[is.na(data$Perceptions.of.corruption)] <- round(mean(data$Perceptions.of
View(data)
#adding new column
data_new <- data %>%
  mutate(Score.Level = if else(data$Score > 5.99, 'H', 'L'))
View(data_new)
summary(data_new)
##
     Overall.rank
                     Country.or.region
                                             Score
                                                         GDP.per.capita
                     Length: 156
                                              :2.853
                                                         Min. :0.0260
## Min. : 1.00
                                        Min.
## 1st Qu.: 39.75
                     Class : character
                                         1st Qu.:4.545
                                                         1st Qu.:0.6170
## Median : 78.50
                     Mode :character
                                        Median :5.380
                                                         Median :0.9715
```

```
: 78.50
                                                  :5.407
##
    Mean
                                           Mean
                                                            Mean
                                                                    :0.9116
##
    3rd Qu.:117.25
                                           3rd Qu.:6.184
                                                            3rd Qu.:1.2325
##
            :156.00
                                           Max.
                                                  :7.769
                                                            Max.
                                                                    :1.6840
    Social.support
                     Healthy.life.expectancy Freedom.to.make.life.choices
##
##
    Min.
            :0.378
                             :0.1050
                                                       :0.0000
    1st Qu.:1.056
                     1st Qu.:0.5540
                                               1st Qu.:0.3080
##
    Median :1.272
                     Median: 0.7920
                                               Median: 0.4170
##
                     Mean
            :1.215
                             :0.7317
                                               Mean
                                                       :0.3926
##
    Mean
##
    3rd Qu.:1.452
                     3rd Qu.:0.8858
                                               3rd Qu.:0.5072
    Max.
            :1.624
                                               Max.
                                                       :0.6310
##
                     Max.
                             :1.1410
##
      Generosity
                      Perceptions.of.corruption Score.Level
            :0.0000
                      Min.
                              :0.0000
                                                  Length: 156
##
    Min.
##
    1st Qu.:0.1087
                      1st Qu.:0.0470
                                                  Class : character
    Median :0.1775
                      Median :0.0855
                                                  Mode : character
##
##
            :0.1848
                              :0.1106
    Mean
                      Mean
##
    3rd Qu.:0.2482
                      3rd Qu.:0.1412
##
    Max.
            :0.5660
                      Max.
                              :0.4530
```

#Relationship

par(mfrow=c(2,3))

plot(data_new\$Score~data_new\$GDP.per.capita,main='Score vs GDP',xlab='GDP',ylab='Happiness Score',col=2 plot(data_new\$Score~data_new\$Social.support,main='Score vs Social Support',xlab='Social Support',ylab='Dot(data_new\$Score~data_new\$Healthy.life.expectancy,main='Score vs Life Expectancy',xlab='Life Expectancy',xlab='Life Expectancy',xlab='Life Expectancy',xlab='Freedom',ylab='Dot(data_new\$Score~data_new\$Freedom.to.make.life.choices,main='Score vs Freedom',xlab='Freedom',ylab='Dot(data_new\$Score~data_new\$Generosity,main='Score vs Generosity',xlab='Generosity',ylab='Happiness Score',col=2



```
#Correlation
cor(data_new$Score,data_new$GDP.per.capita) #0.7964624
## [1] 0.7964624
cor(data_new$Score,data_new$Social.support) #0.7727645
## [1] 0.7727645
cor(data_new$Score,data_new$Healthy.life.expectancy) #0.7709061
## [1] 0.7709061
cor(data_new$Score,data_new$Freedom.to.make.life.choices) #0.5667418
## [1] 0.5667418
cor(data_new$Score,data_new$Generosity) #0.07582369
## [1] 0.07582369
cor(data_new$Score,data_new$Perceptions.of.corruption) #0.3856131
## [1] 0.3856131
#Mutliple Linear Regression
summary(lin.reg)
##
## Call:
## lm(formula = data_new$Score ~ data_new$GDP.per.capita + data_new$Social.support +
      data_new$Healthy.life.expectancy + data_new$Freedom.to.make.life.choices +
##
##
      data_new$Generosity + data_new$Perceptions.of.corruption)
##
## Residuals:
##
                1Q
                    Median
## -1.73766 -0.36135 0.05866 0.37605 1.29967
##
## Coefficients:
##
                                      Estimate Std. Error t value Pr(>|t|)
                                                  0.2214 7.494 5.50e-12 ***
## (Intercept)
                                        1.6589
## data_new$GDP.per.capita
                                        0.8570
                                                  0.2173 3.943 0.000123 ***
                                                  0.2439 5.065 1.19e-06 ***
## data_new$Social.support
                                        1.2354
## data_new$Healthy.life.expectancy
                                                  0.3460 2.827 0.005350 **
                                        0.9781
## data_new$Freedom.to.make.life.choices
                                                  0.3777
                                                          3.697 0.000306 ***
                                        1.3963
                                                          1.176 0.241562
## data_new$Generosity
                                        0.5910
                                                  0.5027
## data_new$Perceptions.of.corruption
                                        0.8384
                                                  0.5543 1.512 0.132554
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.537 on 149 degrees of freedom
## Multiple R-squared: 0.7763, Adjusted R-squared: 0.7673
## F-statistic: 86.16 on 6 and 149 DF, p-value: < 2.2e-16
#Remove Generosity and Corruptions
lin.reg2=lm(data_new$Score~data_new$GDP.per.capita+data_new$Social.support+data_new$Healthy.life.expect
summary(lin.reg2)
##
## Call:
## lm(formula = data_new$Score ~ data_new$GDP.per.capita + data_new$Social.support +
      data_new$Healthy.life.expectancy + data_new$Freedom.to.make.life.choices)
##
## Residuals:
##
       Min
                 1Q
                    Median
                                   30
## -1.86825 -0.36054 0.02308 0.43481 1.23763
## Coefficients:
##
                                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                          1.7773
                                                     0.2092 8.495 1.74e-14 ***
## data_new$GDP.per.capita
                                          0.8924
                                                     0.2153 4.146 5.63e-05 ***
## data_new$Social.support
                                                     0.2400 4.714 5.46e-06 ***
                                          1.1315
## data_new$Healthy.life.expectancy
                                          1.0197
                                                     0.3476
                                                             2.934 0.00387 **
                                                     0.3428 5.167 7.43e-07 ***
## data_new$Freedom.to.make.life.choices 1.7710
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.5425 on 151 degrees of freedom
## Multiple R-squared: 0.7686, Adjusted R-squared: 0.7625
## F-statistic: 125.4 on 4 and 151 DF, p-value: < 2.2e-16
#overall accuracy
anova(lin.reg2)
## Analysis of Variance Table
##
## Response: data_new$Score
                                         Df Sum Sq Mean Sq F value
                                          1 121.828 121.828 413.9358 < 2.2e-16
## data_new$GDP.per.capita
## data new$Social.support
                                          1 15.106 15.106 51.3271 3.216e-11
                                              2.818
## data_new$Healthy.life.expectancy
                                          1
                                                      2.818
                                                            9.5759
                                                                       0.00235
## data_new$Freedom.to.make.life.choices
                                          1
                                             7.857
                                                      7.857 26.6942 7.430e-07
## Residuals
                                        151 44.442
                                                      0.294
##
## data_new$GDP.per.capita
                                        ***
## data_new$Social.support
## data_new$Healthy.life.expectancy
                                        **
## data_new$Freedom.to.make.life.choices ***
## Residuals
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

qf(0.95,4,151) #2.431562

[1] 2.431562

#Residuals

predict(lin.reg2)

```
3
                                            5
## 6.829720 6.855365 7.011361 6.939214 6.750334 6.885441 6.743003 6.784061
         9
                 10
                          11 12 13 14
                                                        15
## 6.792036 6.652365 6.796063 6.300695 6.268623 6.850117 6.519664 6.804719
        17
                18
                          19
                                   20
                                           21
                                                    22
                                                             23
## 6.530830 6.532254 6.399938 6.339746 6.501132 6.674797 5.873927 6.462122
        25
                 26
                          27
                                   28
                                           29
                                                    30
                                                             31
## 6.169757 5.930966 5.635256 6.152898 6.636804 6.328071 6.276031 5.809973
        33
                 34
                          35
                                   36
                                           37
                                                    38
                                                             39
## 6.272769 6.983658 5.457244 6.084286 6.378034 6.080860 6.140123 6.237419
                 42
                          43
                                   44
                                           45
                                                    46
                                                             47
## 6.060576 5.945778 5.941647 6.593807 5.517677 5.597339 6.104585 5.867712
                50
                          51
                                   52
                                          53
                                                   54
                                                             55
## 6.069751 5.842732 6.305352 6.139341 5.789756 5.655588 6.377974 5.906383
        57
                 58
                          59
                                   60
                                           61
                                                    62
                                                             63
## 6.058812 6.464613 5.490941 5.999848 5.462659 5.641217 5.911848 6.122046
                 66
                          67
                                                    70
                                                             71
                                   68
                                           69
## 5.752143 6.404418 4.483820 5.807755 5.618643 5.608365 5.078669 5.606294
                          75
                 74
                                   76
                                           77
                                                    78
                                                             79
## 5.492216 4.880687 5.696704 6.428809 5.942834 5.229080 5.541102 5.935866
             82
                         83
                                  84
                                          85
                                                    86
                                                             87
## 5.607857 5.276558 5.597163 5.584177 4.659786 5.533004 5.824062 4.936786
        89
                 90
                          91
                                   92
                                          93
                                                    94
                                                             95
## 4.914607 5.411659 5.256633 5.511869 5.801775 5.790962 5.422770 4.309166
                                                           103
        97
                 98
                          99
                                100
                                         101
                                                  102
## 5.845584 4.475017 4.059296 5.030321 5.419657 3.645372 4.458766 5.163822
       105
                106
                        107
                             108
                                      109
                                                   110
                                                           111
## 5.155119 5.329819 5.151401 5.342238 5.287151 4.858293 4.561375 4.722755
       113
               114
                        115
                                116
                                          117
                                                   118
                                                            119
## 5.243946 3.712618 4.106642 5.061804 5.052265 4.024784 4.701107 4.227587
                122
                        123
                                 124
                                          125
                                                   126
## 4.702208 4.221952 4.347560 4.857499 4.999399 4.829058 3.974558 4.264371
                130
                         131
                                  132
                                          133
                                                   134
## 3.762067 5.735255 5.242904 3.460317 5.150642 4.397683 5.375127 4.365350
                                                   142
                138
                         139
                                 140
                                          141
## 4.851180 4.687924 3.606903 4.798186 3.992679 3.644790 3.886308 4.343518
       145
                146
                        147
                                 148
                                          149
                                                   150
                                                            151
## 3.101233 4.445268 3.347910 5.356253 3.229094 3.870680 4.074730 4.511149
                154
                         155
## 4.450789 3.042742 3.437561 3.019517
```

resid(lin.reg2)

1 2 3 4 5 6 ## 0.939279684 0.744634810 0.542639206 0.554786484 0.737665677 0.594558880

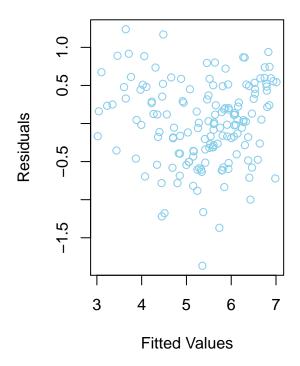
```
##
                                                  8
                                                                          9
                                                                                                10
       0.599997086 0.522938619 0.485963548 0.593635004 0.431937056 0.866304851
##
##
                                                14
                                                                       15
                                                                                                16
                             0.239883156
                                                       0.534336183 0.216281148 0.454169832
       0.870377005
                                                                                                                                 0.390746310
##
##
                        19
                                                20
                                                                         21
                                                                                                 22
       0.492061511 0.512253707
                                                       0.323867733
                                                                                                                                 0.129878200
##
                                                                              0.051202714 0.721072556
##
                        25
                                                26
                                                                         27
                                                                                                 28
                                                                              0.222101632 -0.262804073
                               0.513033738
                                                       0.800743795
##
       0.276242855
                                                                                                                                 0.025929470
##
                        31
                                                32
                                                                         33
                                                                                                 34
                                                                                                                         35
                               0.490027429
                                                        0.020231165 -0.721657903 0.795756266
##
       0.044969224
                                                                                                                                 0.138713762
                        37
                                                38
                                                                         39
                                                                                                 40
       -0.179034332 0.117139537
                                                       0.051876733 -0.055418732 0.113423542
##
                                                                                                                                 0.203222054
##
                        43
                                                44
                                                                         45
                                                                                                46
                                                                                                                         47
       0.183352587 -0.475806885
                                                       0.587322617  0.502661472  -0.018584917
                                                50
##
                        49
                                                                         51
                                                                                                52
                                                                                                                         53
       -0.023751068    0.185268211    -0.284352303    -0.131341477    0.150244368
                                                                                                                                 0.239412086
##
                                                56
                                                                                                                         59
                        55
                                                                        57
                                                                                                58
      -0.484974313 -0.016382736 -0.170812235 -0.578612759 0.369059431 -0.190848067
                        61
                                                62
                                                                       63
                                                                                                64
                                                                                                                         65
##
##
       0.316341488 0.116782628 -0.168848147 -0.404045560 -0.055142849 -0.711418431
##
                        67
                                                68
                                                                        69
                                                                                                70
                                                                                                                         71
        1.169180279 -0.159754598 0.012357257 -0.005364686 0.450331274 -0.081293817
##
                                                74
                                                                        75
                                                                                                 76
                                                                                                                         77
                        73
       ##
##
                        79
                                                80
                                                                        81
                                                                                                 82
                                                                                                                         83
      -0.168101699 -0.596865648 -0.284856872 0.010442425 -0.312162830 -0.310176789
##
                        85
                                              86
                                                                       87
                                                                                                88
                                                                                                                         89
       0.605213622 \ -0.272004324 \ -0.577061959 \ \ 0.274213574 \ \ 0.293393080 \ -0.203659090
##
                                              92
                                                                     93
##
                        91
                                                                                                94
                                                                                                                       95
      -0.059633119 -0.319868738 -0.610774505 -0.615961705 -0.340769567 0.734834370
##
                        97
                                                98
                                                                       99
                                                                                               100
      -0.834584392    0.520982809    0.884703936    -0.117320673    -0.513656609    1.237627716
##
                                              104
                                                                      105
                                                                                             106
                                                                                                                       107
       0.353234335 \ -0.364821685 \ -0.359118628 \ -0.607819223 \ -0.432401401 \ -0.6352377418628 \ -0.607819223 \ -0.432401401 \ -0.6352377418628 \ -0.607819223 \ -0.432401401 \ -0.6352377418628 \ -0.607819223 \ -0.432401401 \ -0.6352377418628 \ -0.607819223 \ -0.432401401 \ -0.6352377418628 \ -0.607819223 \ -0.432401401 \ -0.6352377418628 \ -0.607819223 \ -0.432401401 \ -0.6352377418628 \ -0.607819223 \ -0.432401401 \ -0.6352377418628 \ -0.607819223 \ -0.432401401 \ -0.6352377418628 \ -0.607819223 \ -0.432401401 \ -0.6352377418628 \ -0.607819223 \ -0.432401401 \ -0.6352377418628 \ -0.607819223 \ -0.432401401 \ -0.6352377418628 \ -0.607819223 \ -0.432401401 \ -0.6352377418628 \ -0.607819223 \ -0.432401401 \ -0.6352377418628 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.607819223 \ -0.60781923 \ -0.6078192
##
                      109
                                              110
                                                                      111
                                                                                            112
                                                                                                                       113
##
      -0.587151008 -0.162293036 0.119624760 -0.054755420 -0.604945987
                                                                                                                                 0.915381520
##
                                              116
                                                                      117
                                                                                             118
       0.480357997 \ -0.502803840 \ -0.504265339 \ \ 0.509216101 \ -0.182106541
##
                                                                                                                                0.288412980
##
                      121
                                              122
                                                                      123
                                                                                               124
                                                                                                                       125
      -0.193208274 \quad 0.268047898 \quad 0.118439744 \quad -0.396498549 \quad -0.543399401 \quad -0.392057934
                      127
                                              128
                                                                      129
                                                                                              130
                                                                                                                       131
       0.443442046 \quad 0.125628915 \quad 0.611933260 \quad -1.369255453 \quad -0.882903902 \quad 0.889683341
##
##
                      133
                                              134
                                                                      135
                                                                                               136
                                                                                                                       137
      -0.818641672 -0.111682922 -1.163126590 -0.176350411 -0.685179968 -0.580924309
##
                      139
                                              140
                                                                      141
                                                                                               142
                                                                                                                      143
       0.478096744 -0.783186306 -0.017679366 0.328210125 0.046691717 -0.541517819
##
                      145
                                              146
                                                                      147
                                                                                               148
                                                                                                                       149
       0.673766708 - 0.782268458 \quad 0.249089897 - 1.868253214 \quad 0.232905640 - 0.460679586
                                              152
                                                                      153
                                                                                               154
                                                                                                                       155
## -0.694729657 -1.177149034 -1.219788767 0.160257709 -0.354560879 -0.166516830
```

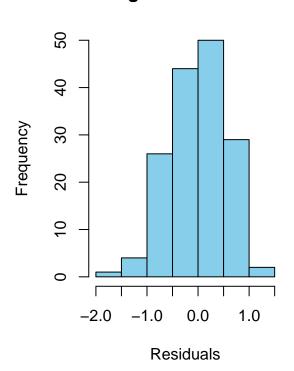
par(mfrow=c(1,2))

*plotting the residuals against the predicted values

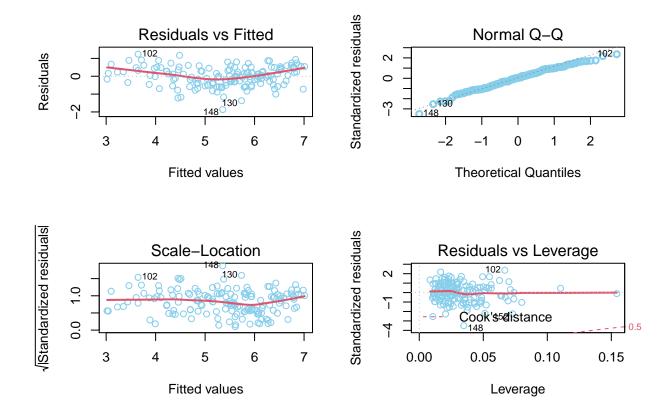
```
plot(predict(lin.reg2),resid(lin.reg2), xlab = "Fitted Values", ylab = "Residuals",col='skyblue')
#histogram of the residuals
hist(resid(lin.reg2), main = paste("Histogram of Residuals"), xlab = "Residuals",col='skyblue')
```

Histogram of Residuals





```
#residual plots
par(mfrow=c(2,2))
plot(lin.reg2,lwd=2,col='skyblue',pch=1)
```



```
#Cross Validation
data_cv=data_new[,3:9]
m1=glm(Score~GDP.per.capita,data=data_cv)
m2=glm(Score~GDP.per.capita+Social.support,data=data_cv)
m3=glm(Score~GDP.per.capita+Social.support+Healthy.life.expectancy,data=data_cv)
m4=glm(Score~GDP.per.capita+Social.support+Healthy.life.expectancy+Freedom.to.make.life.choices,data=da
m5=glm(Score~GDP.per.capita+Social.support+Healthy.life.expectancy+Freedom.to.make.life.choices+Generos
m6=glm(Score-GDP.per.capita+Social.support+Healthy.life.expectancy+Freedom.to.make.life.choices+Generos
#training, testing, cv dataset
#Validation-set approach 60/40
#set.seed(2)
tr.id <- sample(1:nrow(data_cv),nrow(data_cv)*.6)</pre>
#train dataset
train_cv <- data_cv[tr.id , ]</pre>
#validation dataset
validation_cv <- data_cv[-tr.id , ]</pre>
```

[1] 93 7

dim(train_cv) # 93 7

```
dim(validation_cv) #63 7
## [1] 63 7
```

```
#error estimates
#create initial error vector with values 0's
train_error <- rep(0,6)
#create initial error vector with values 0's
validation_error <- rep(0,6)</pre>
m1t = glm(m1, subset = tr.id) #fit model1 for training data
score_hat1 <- predict (m1t ,data_cv) #predict happiness score</pre>
train_error[1] <- mean((data_cv$Score-score_hat1)[tr.id]^2) #calculate training error</pre>
validation_error[1] <- mean((data_cv$Score-score_hat1)[-tr.id]^2) #calculate validation error</pre>
m2t = glm(m2, subset = tr.id) #fit model1 for training data
score hat2 <- predict (m2t ,data cv) #predict happiness score</pre>
train_error[2] <- mean((data_cv$Score-score_hat2)[tr.id]^2) #calculate training error</pre>
validation_error[2] <- mean((data_cv$Score-score_hat2)[-tr.id]^2) #calculate validation error</pre>
m3t = glm(m3, subset = tr.id) #fit model3 for training data
score hat3 <- predict (m3t ,data cv) #predict happiness score</pre>
train_error[3] <- mean((data_cv$Score-score_hat3)[tr.id]^2) #calculate training error</pre>
validation_error[3] <- mean((data_cv$Score-score_hat3)[-tr.id]^2) #calculate validation error</pre>
m4t = glm(m4, subset = tr.id) #fit model4 for training data
score_hat4 <- predict (m4t ,data_cv) #predict happiness score</pre>
train_error[4] <- mean((data_cv$Score-score_hat4)[tr.id]^2) #calculate training error
validation_error[4] <- mean((data_cv$Score-score_hat4)[-tr.id]^2) #calculate validation error</pre>
m5t = glm(m5, subset = tr.id) #fit model5 for training data
score_hat5 <- predict (m5t ,data_cv) #predict happiness score</pre>
train_error[5] <- mean((data_cv$Score-score_hat5)[tr.id]^2) #calculate training error</pre>
validation_error[5] <- mean((data_cv$Score-score_hat5)[-tr.id]^2) #calculate validation error</pre>
m6t = glm(m6, subset = tr.id) #fit model6 for training data
score_hat6 <- predict (m6t ,data_cv) #predict happiness score</pre>
train_error[6] <- mean((data_cv$Score-score_hat6)[tr.id]^2) #calculate training error</pre>
validation_error[6] <- mean((data_cv$Score-score_hat6)[-tr.id]^2) #calculate validation error</pre>
#loocv
loocv_error=rep(0,6)
loocv_error[1] = cv.glm(data_cv,m1)$delta[1]
loocv_error[2]=cv.glm(data_cv,m2)$delta[1]
loocv_error[3]=cv.glm(data_cv,m3)$delta[1]
loocv_error[4] = cv.glm(data_cv,m4)$delta[1]
loocv_error[5] = cv.glm(data_cv,m5)$delta[1]
loocv_error[6] = cv.glm(data_cv,m6)$delta[1]
#kfold
cv_errorKF= rep (0,6)
```

```
#set.seed(2) #seed can be any value
cv_errorKF[1] <- cv.glm(data_cv,m1, K=10)$delta[1]</pre>
cv_errorKF[2] <- cv.glm(data_cv,m2, K=10)$delta[1]</pre>
cv_errorKF[3] <- cv.glm(data_cv,m3, K=10)$delta[1]</pre>
cv_errorKF[4] <- cv.glm(data_cv,m4, K=10)$delta[1]</pre>
cv_errorKF[5] <- cv.glm(data_cv,m5, K=10)$delta[1]</pre>
cv_errorKF[6] <- cv.glm(data_cv,m6, K=10)$delta[1]</pre>
#mse values
train_error
## [1] 0.4039207 0.3323384 0.3153765 0.2671776 0.2629036 0.2466433
validation_error
## [1] 0.5358354 0.3901411 0.3740266 0.3146881 0.3081892 0.3325908
cv_errorKF
## [1] 0.4584381 0.3653040 0.3537523 0.3062573 0.3099824 0.3022022
loocv_error
## [1] 0.4610816 0.3671266 0.3543573 0.3047021 0.3044499 0.3065170
#plotting
model \leftarrow c(1:6)
plot(model, train_error, type = "b", xlab = "Model", ylab = "MSE", col = 2, main = "Comparison", ylim=c(
{ lines(validation_error, type = "b", col = 3)
  lines(cv_errorKF, type = "b", col = 9)
 lines(loocv_error, type = "b", col = 5)
}
cols=c(2,3,9,5)
legend(x = 4, y = 0.6,cex=0.5, c("Train", "Validation", "LOOCV", "10-fold"), fill=cols)
#Decision Tree
#keeping only the decision variables and score level
data_tree=data_new[,c(-1:-3)]
View(data_tree)
#converting character variable to factor variable
data_tree$Score.Level = as.factor(data_tree$Score.Level)
sapply(data_tree,class)
```

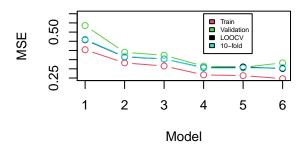
Social.support

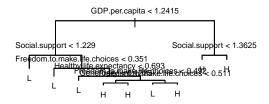
GDP.per.capita

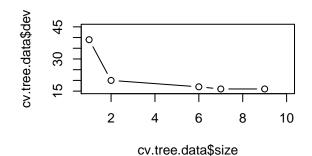
##

```
##
                       "numeric"
                                                    "numeric"
##
        Healthy.life.expectancy Freedom.to.make.life.choices
##
                      "numeric"
                                                    "numeric"
##
                     Generosity
                                   Perceptions.of.corruption
##
                       "numeric"
                                                    "numeric"
##
                    Score.Level
##
                       "factor"
#fitting a tree on training data
set.seed(2)
train.dt = sample(1:nrow(data_tree), nrow(data_tree)/1.25)
test.dt=data_tree[-train.dt,]
length(train.dt) #124
## [1] 124
length(test.dt) #7
## [1] 7
tree.data=tree(Score.Level~.,data_tree,subset=train.dt)
summary(tree.data)
##
## Classification tree:
## tree(formula = Score.Level ~ ., data = data_tree, subset = train.dt)
## Variables actually used in tree construction:
                                      "Social.support"
## [1] "GDP.per.capita"
## [3] "Freedom.to.make.life.choices" "Healthy.life.expectancy"
## [5] "Generosity"
## Number of terminal nodes: 9
## Residual mean deviance: 0.2226 = 25.6 / 115
## Misclassification error rate: 0.05645 = 7 / 124
\#0.05645 = 7 / 124 \quad misclassified
0.05645*100
## [1] 5.645
#plotting
plot(tree.data)
text(tree.data, pretty=0, cex=0.6)
#cross validation
cv.tree.data=cv.tree(tree.data,FUN = prune.misclass)
plot(cv.tree.data$size, cv.tree.data$dev,type="b",xlim=c(1,10),ylim=c(15,45))
#6
#pruning
prune.tree.data=prune.tree(tree.data,best=7)
plot(prune.tree.data)
text(prune.tree.data, pretty=0, cex=0.75)
```

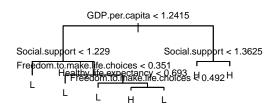
Comparison







L 1 15



summary(prune.tree.data)

##

```
##
## Classification tree:
## snip.tree(tree = tree.data, nodes = 47:46)
## Variables actually used in tree construction:
## [1] "GDP.per.capita"
                                      "Social.support"
## [3] "Freedom.to.make.life.choices" "Healthy.life.expectancy"
## Number of terminal nodes: 7
## Residual mean deviance: 0.2699 = 31.58 / 117
## Misclassification error rate: 0.06452 = 8 / 124
#0.1129 = 14 / 124
#testing model accuracy
tree_predicted<-predict(tree.data, test.dt, type="class")</pre>
#confusion matrix
table(tree_predicted,test.dt$Score.Level)
##
## tree_predicted H L
                H 12 4
##
```

```
#calculating misclassifiction rate
matrix<-table(tree_predicted,test.dt$Score.Level)</pre>
misrate<-((matrix[1,2]+matrix[2,1])/sum(matrix))
paste("Misclassification error rate is ",misrate)
## [1] "Misclassification error rate is 0.15625"
# 0.15625
#Principle Component Analysis
#keeping only the independent variables
pca.data=data_new[,4:10]
head(pca.data)
    GDP.per.capita Social.support Healthy.life.expectancy
##
## 1
             1.340
                            1.587
                                                    0.986
## 2
             1.383
                            1.573
                                                    0.996
## 3
             1.488
                            1.582
                                                    1.028
## 4
             1.380
                            1.624
                                                    1.026
## 5
             1.396
                            1.522
                                                    0.999
## 6
             1.452
                            1.526
                                                    1.052
##
    Freedom.to.make.life.choices Generosity Perceptions.of.corruption Score.Level
## 1
                           0.596
                                      0.153
                                                                0.393
## 2
                           0.592
                                      0.252
                                                                0.410
                                                                                Н
## 3
                           0.603
                                      0.271
                                                                0.341
                                                                                Η
## 4
                           0.591
                                      0.354
                                                                0.118
                                                                                Н
## 5
                           0.557
                                      0.322
                                                                0.298
                                                                                Η
## 6
                                                                                Н
                           0.572
                                      0.263
                                                                0.343
#renaming for simplification purpose
colnames(pca.data)[c(1:6)]=c("GDP", "SS", "Life", "Free", "Gener", "Corrup")
#mean and variance
sapply(pca.data[,1:6],mean)
##
        GDP
                   SS
                           Life
                                     Free
                                              Gener
                                                       Corrup
## 0.9115577 1.2152244 0.7316538 0.3925705 0.1848462 0.1106026
sapply(pca.data[,1:6],var)
          GDP
                       SS
                                 Life
                                             Free
                                                        Gener
                                                                   Corrup
## 0.153445100 0.080328149 0.055676305 0.020531872 0.009073408 0.008937402
obj = prcomp(pca.data[,1:6], scale. = TRUE)
names(obj)
```

"scale"

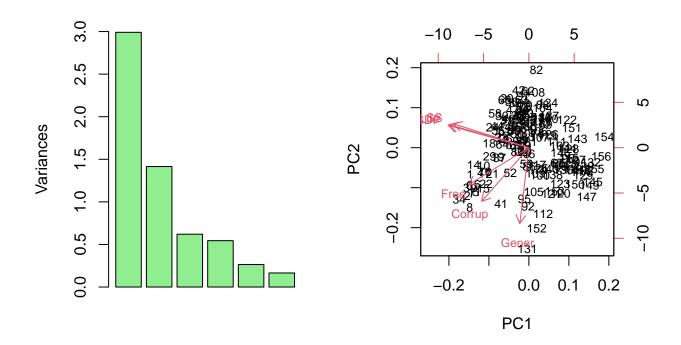
"rotation" "center"

[1] "sdev"

"x"

```
obj$rotation
```

```
PC2
                                          PC3
                                                                  PC5
##
                  PC1
                                                      PC4
                                                                                 PC6
## GDP
          -0.51583025 \quad 0.2082045 \quad -0.07765971 \quad 0.22026792 \quad -0.27711289 \quad -0.7478164713
## SS
         -0.48232080 0.2223429 0.35572318 0.02339788 0.76435099 0.0813105789
## Life -0.50821063 0.2141943 -0.05577799 0.26912517 -0.43511439 0.6564896736
## Free
         -0.38551214 -0.3435152 0.24935585 -0.78471459 -0.23541908 0.0004850166
## Gener -0.05806569 -0.7039110 0.48379134 0.51123624 -0.06950865 -0.0298279513
## Corrup -0.30168944 -0.4978373 -0.75371507 0.03696948 0.29899478 0.0478589759
obj
## Standard deviations (1, .., p=6):
## [1] 1.7294757 1.1894226 0.7876006 0.7379261 0.5139982 0.4063791
## Rotation (n x k) = (6 \times 6):
##
                  PC1
                                          PC3
                                                      PC4
                                                                  PC5
                                                                                 PC6
                             PC2
          -0.51583025 \quad 0.2082045 \quad -0.07765971 \quad 0.22026792 \quad -0.27711289 \quad -0.7478164713
## GDP
         -0.48232080 0.2223429 0.35572318 0.02339788 0.76435099 0.0813105789
## SS
## Life -0.50821063 0.2141943 -0.05577799 0.26912517 -0.43511439 0.6564896736
## Free -0.38551214 -0.3435152 0.24935585 -0.78471459 -0.23541908 0.0004850166
## Gener -0.05806569 -0.7039110 0.48379134 0.51123624 -0.06950865 -0.0298279513
## Corrup -0.30168944 -0.4978373 -0.75371507 0.03696948 0.29899478 0.0478589759
par(mfrow=c(1,2))
#screeplot
screeplot(obj,col='lightgreen',main='',ylim=c(0,3))
#biplot
biplot(obj,cex=0.75)
```



```
#sd of each pc
obj$sdev
```

[1] 1.7294757 1.1894226 0.7876006 0.7379261 0.5139982 0.4063791

