

question 1

$$3x_1 + x_2 + 2x_3 = 1$$

$$2x_1 + 3x_2 - 2x_3 = 2$$

$$2x_1 + x_2 + x_3 = 3$$

(i) $Ax = B$

$$A = \begin{bmatrix} 3 & 1 & 2 \\ 2 & 3 & -2 \\ 2 & 1 & 1 \end{bmatrix} \quad x = \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} \quad B = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$$

(ii) $x = A^{-1} * B$

$$A = \begin{bmatrix} 3 & 1 & 2 \\ 2 & 3 & -2 \\ 2 & 1 & 1 \end{bmatrix}$$

$$A^{-1} = \frac{\text{Adj}(A)}{\det(A)}$$

$$\begin{aligned} \det(A) &= 3(3+2) - 1(2+4) + 2(2-6) \\ &= 15 - 6 - 8 \end{aligned}$$

$$A^{-1} = \begin{bmatrix} 5 & 1 & -8 \\ -6 & -1 & 10 \\ -4 & -1 & 7 \end{bmatrix}$$

$$X = \begin{bmatrix} 5 & 1 & -8 \\ -6 & -1 & 10 \\ -4 & -1 & 7 \end{bmatrix} \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix} = \begin{bmatrix} -17 \\ 22 \\ 15 \end{bmatrix}$$

$$x_1 = -17, x_2 = 22, x_3 = 15$$