assignment_2

November 25, 2024

[215]: from IPython.display import Image
Image(filename='images.png')

[215]:



BIRZEIT UNIVERSITY

Electrical and Computer Engineering Department

Machine Learning and Data Science - ENCS5341

Assignment #2

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Instructor: Dr. Yazan Abu Farha Date: Oct 30, 2024

Topic: Machine Learning Assignment: 1 https://github.com/sondosshahin/Machine-Learning-Project-Regression-Analysis-and-Model-Selection-

0.1 1 - Import Dataset YallaMotors

The main objective of this dataset is to predict car prices, making it ideal for developing regression models to understand the relationship between various features (e.g., car make, model, year, mileage, engine size, etc.) and the target variable (car price).

```
[220]: import os
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
```

```
missing_values = [" ", "NA", "N/A", "N A", "NaN"]
       data = pd.read_csv("cars.csv", na_values=missing_values)
       data.head()
[220]:
                                   car name
                                                             price engine_capacity \
       0
                   Fiat 500e 2021 La Prima
                                                                                0.0
       1
             Peugeot Traveller 2021 L3 VIP
                                                       SAR 140,575
                                                                                2.0
       2
          Suzuki Jimny 2021 1.5L Automatic
                                                        SAR 98,785
                                                                                1.5
       3
            Ford Bronco 2021 2.3T Big Bend
                                                       SAR 198,000
                                                                                2.3
             Honda HR-V 2021 1.8 i-VTEC LX Orangeburst Metallic
       4
                                                                                1.8
                                                              brand country
               cylinder horse_power
                                      top_speed
                                                     seats
          N/A, Electric
                              Single
                                      Automatic
                                                       150
                                                               fiat
                                                                         ksa
       1
                                 180
                                       8 Seater
                                                       8.8
                                                            peugeot
                                                                         ksa
       2
                       4
                                 102
                                             145
                                                 4 Seater
                                                             suzuki
                                                                         ksa
       3
                       4
                                 420
                                       4 Seater
                                                       7.5
                                                               ford
                                                                         ksa
       4
                                 140
                                             190 5 Seater
                                                              honda
                                                                         ksa
[222]: data.info()
      <class 'pandas.core.frame.DataFrame'>
      RangeIndex: 6308 entries, 0 to 6307
      Data columns (total 9 columns):
           Column
                             Non-Null Count
                                              Dtype
           ____
                             _____
       0
           car name
                             6308 non-null
                                              object
       1
           price
                             6308 non-null
                                              object
       2
                             6308 non-null
                                              object
           engine_capacity
       3
                             5684 non-null
           cylinder
                                              object
       4
           horse_power
                             6308 non-null
                                              object
       5
                             6265 non-null
           top_speed
                                              object
       6
           seats
                             6205 non-null
                                              object
       7
           brand
                             6308 non-null
                                              object
                             6308 non-null
           country
                                              object
      dtypes: object(9)
      memory usage: 443.7+ KB
[224]:
      data.describe()
[224]:
                                        car name price engine_capacity cylinder \
       count
                                             6308
                                                   6308
                                                                    6308
                                                                             5684
       unique
                                             2546
                                                   3395
                                                                     129
                                                                               10
               Mercedes-Benz C-Class 2022 C 300
                                                    TBD
                                                                     2.0
                                                                                4
       top
                                               10
                                                    437
                                                                    1241
                                                                             2856
       freq
              horse_power top_speed
                                         seats
                                                         brand country
                     6308
                                6265
                                          6205
                                                                   6308
                                                          6308
       count
```

```
unique
               330
                          168
                                      81
                                                      82
                                                               7
                          250
top
               150
                               5 Seater mercedes-benz
                                                             uae
freq
               162
                         1100
                                   3471
                                                    560
                                                            1248
```

```
[226]: from sklearn.preprocessing import LabelEncoder
      # Print unique values to check
      print(data['brand'].unique())
      print(data['country'].unique())
      print(data['car name'].unique())
      #encode categorical features
      label_encoder = LabelEncoder()
                                        # Initialize the LabelEncoder
      categorical_features = ['brand', 'country', 'car name']
      for column in categorical_features:
           # Fit the LabelEncoder and transform the column
          data[column] = label_encoder.fit_transform(data[column])
          print(data[column])
      # Display encoded dataset
      print("Dataset after Encoding:")
      print(data)
      # 2. Visualize numeric columns
      numeric_columns = ['price', 'engine_capacity', 'cylinder', 'horse_power', __
       # Create distribution plots for numeric columns
      plt.figure(figsize=(15, 10)) # Set figure size
      for i, column in enumerate(numeric_columns, 1):
          plt.subplot(2, 3, i) # Arrange subplots in 2 rows and 3 columns
          sns.histplot(data[column], kde=True, bins=30, color='blue', alpha=0.7) #_U
       \hookrightarrow Histogram with KDE
          plt.title(f"Distribution of {column}", fontsize=12) # Add a title
          plt.xlabel(column, fontsize=10) # Label x-axis
          plt.ylabel("Frequency", fontsize=10) # Label y-axis
          plt.grid(axis='y', linestyle='--', alpha=0.6) # Add grid for better_
       \rightarrow readability
      # Adjust layout to prevent overlap
      plt.tight_layout()
      plt.show()
```

```
['fiat' 'peugeot' 'suzuki' 'ford' 'honda' 'renault' 'aston-martin' 'gac'
  'toyota' 'genesis' 'hyundai' 'lincoln' 'mg' 'chevrolet' 'mercedes-benz'
  'kia' 'volkswagen' 'land-rover' 'lotus' 'volvo' 'porsche' 'mini'
  'lamborghini' 'nissan' 'mclaren' 'changan' 'great-wall' 'bmw'
  'rolls-royce' 'audi' 'infiniti' 'ram' 'chrysler' 'gmc' 'borgward' 'jeep'
```

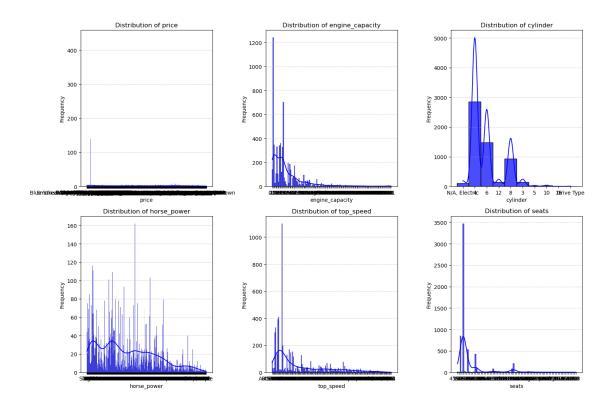
```
'alfa-romeo' 'chery' 'skoda' 'lexus' 'jaguar' 'maxus' 'cadillac'
 'ferrari' 'mazda' 'mitsubishi' 'bestune' 'jetour' 'hongqi' 'maserati'
 'geely' 'byd' 'Foton' 'subaru' 'haval' 'isuzu' 'ssang-yong' 'dodge'
 'bentley' 'bugatti' 'opel' 'zotye' 'soueast ' 'dorcen' 'citroen'
 'brilliance' 'seat' 'proton' 'soueast' 'ds' 'jac' 'lada' 'kinglong'
 'baic' 'morgan' 'mahindra' 'tata' 'dfm' 'acura' 'abarth' 'zna' 'tesla']
['ksa' 'egypt' 'bahrain' 'qatar' 'oman' 'kuwait' 'uae']
['Fiat 500e 2021 La Prima' 'Peugeot Traveller 2021 L3 VIP'
 'Suzuki Jimny 2021 1.5L Automatic' ...
 'BMW M8 Convertible 2021 4.4T V8 Competition xDrive (625 Hp)'
 'BMW M8 Coupe 2021 4.4T V8 Competition xDrive (625 Hp)'
 'Lamborghini Aventador Ultimae 2022 LP 780-4']
        25
0
1
        62
2
        74
3
        26
4
        33
6303
        7
6304
        24
6305
        67
6306
        45
6307
        7
Name: brand, Length: 6308, dtype: int32
0
        2
1
        2
2
        2
3
        2
4
        2
6303
        6
6304
        6
6305
        6
6306
        6
6307
        6
Name: country, Length: 6308, dtype: int32
0
         564
1
        1980
2
        2235
3
         574
4
         811
6303
         333
6304
         552
6305
        2119
6306
        1246
6307
         334
Name: car name, Length: 6308, dtype: int32
```

Dataset after Encoding:

	car name	price	engine_capacity	cylinder	\
0	564	TBD	0.0	N/A, Electric	
1	1980	SAR 140,575	2.0	4	
2	2235	SAR 98,785	1.5	4	
3	574	SAR 198,000	2.3	4	
4	811	Orangeburst Metallic	1.8	4	
6303	333	DISCONTINUED	6.8	8	
6304	552	AED 1,766,100	4.0	8	
6305	2119	AED 1,400,000	6.6	12	
6306	1246	AED 1,650,000	6.5	NaN	
6307	334	DISCONTINUED	6.8	8	

	horse_power	top_speed	seats	brand	country
0	Single	Automatic	150	25	2
1	180	8 Seater	8.8	62	2
2	102	145	4 Seater	74	2
3	420	4 Seater	7.5	26	2
4	140	190	5 Seater	33	2
6303	505	296	5 Seater	7	6
6304	25	800	Automatic	24	6
6305	624	250	4 Seater	67	6
6306	740	350	2 Seater	45	6
6307	530	305	5 Seater	7	6

[6308 rows x 9 columns]



Name: car name dtype: int32

```
car name
1625
         10
564
          7
          7
2001
1995
          7
1204
          7
1029
          1
903
          1
488
          1
1105
          1
1251
```

Name: count, Length: 2546, dtype: int64

```
Name: brand dtype: int32
brand
55
    560
5
    398
    394
9
77 378
26 323
   . . .
75
  2
71
    2
    2
13
20
     1
12
Name: count, Length: 82, dtype: int64
______
Name: country dtype: int32
country
6
   1248
2
   996
3
   932
5
   925
4
   910
0
   906
1
    391
Name: count, dtype: int64
Name: price dtype: object
price
TBD
            437
            238
Following
DISCONTINUED
            140
Follow
              27
Grigio Maratea
             23
            . . .
             1
BHD 23,900
BHD 24,300
              1
```

BHD 24,100

```
BHD 24,700 1
AED 1,650,000 1
```

Name: count, Length: 3395, dtype: int64

Name: engine_capacity dtype: object

```
engine_capacity
     1241
2.0
3.0
      703
3.5
      359
1.5
      347
   340
4.0
3342
      1
2476
        1
4400
        1
3470
         1
1595
         1
```

Name: count, Length: 129, dtype: int64

Name: cylinder dtype: object

cylinder

4	2856
6	1480
8	924
3	139
12	136
N/A, Electric	107
10	21
5	17
Drive Type	3
16	1
NT . 1.	

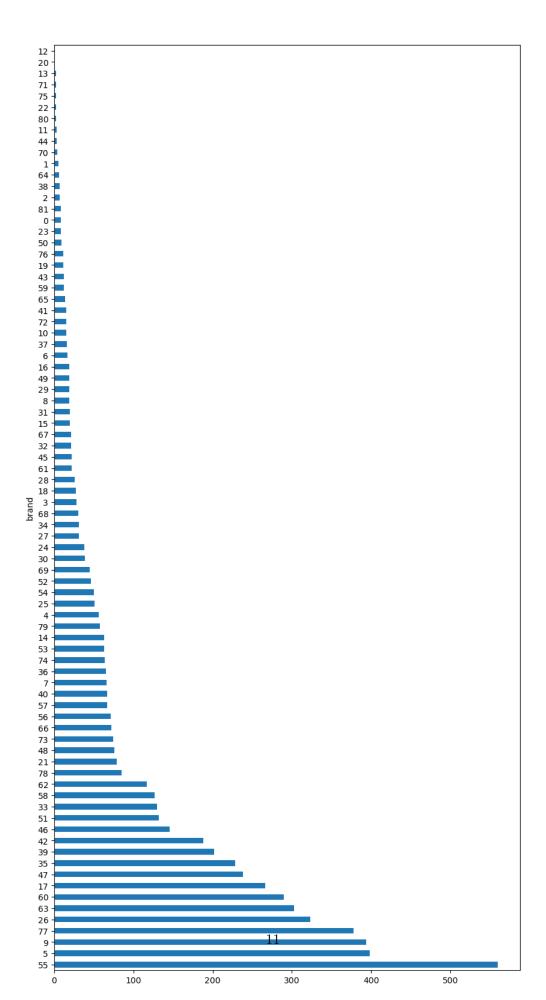
Name: count, dtype: int64

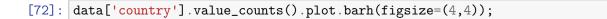
Name: horse_power dtype: object

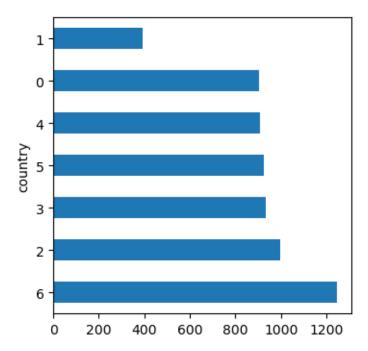
horse_power 150 162

```
355
      116
400
    111
184
    109
300
   103
87
126
394
236
      1
720
       1
Name: count, Length: 330, dtype: int64
Name: top_speed dtype: object
top_speed
250
     1100
      410
180
200
      392
170
      332
190
     294
     . . .
   1
307
130
       1
966
       1
262
       1
324
Name: count, Length: 168, dtype: int64
Name: seats dtype: object
seats
5 Seater 3471
4 Seater 847
7 Seater 532
2 Seater 428
8 Seater 211
          . . .
         1
24.1
12.3
            1
230
            1
220
            1
```

2.8







0.2 2- Data Cleaning

To handle missing values in numerical columns using the median, the fillna() method in Pandas is used, applying the median value for each column where missing values (NaN) are present.

- **price**: create a custom function in order to extract price and currency. that car prices are listed in various currencies. To ensure consistency, all prices are standardized to a common currency, for a uniform target variable.
- car name, country and brand: need encoding to convert them to numerical features.
- engine_capacity, cylinder, horse_power, top_speed: simple conversion to float and set a limit (standarization)

```
float(value)
return True
except ValueError:
return False
```

```
[229]: def apply_price_adj(price):
           try:
               c = price[:3]
               price_str = price[4:].replace(',', '')
               p = float(price_str)
               pd = p
               conversion_rates = {
               'AED': 0.27,
               'KWD': 3.33,
               'OMR': 2.63,
               'BHD': 2.63,
               'QAR': 0.27,
               'SAR': 0.27,
               'EGP': 0.0333
               }
               if c in conversion_rates:
                   pd = p * conversion_rates[c]
               return pd
           except (ValueError, IndexError):
               return -1
```

```
import pandas as pd
import numpy as np
from sklearn.preprocessing import StandardScaler, MinMaxScaler
from sklearn.preprocessing import LabelEncoder

# Define the missing values
missing_values = [" ", "NA", "N/A", "N A", "NaN"]

# Read the data and replace the missing values with NaN
data = pd.read_csv("cars.csv", na_values=missing_values)
df_upd = data.copy()

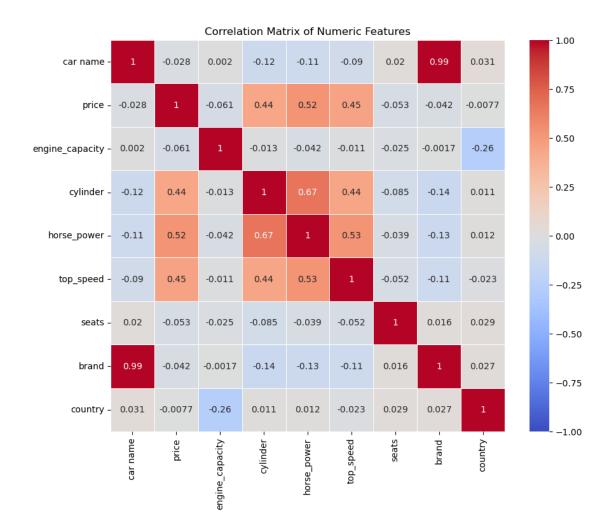
# Print the dataframe before any changes
print("Before filling missing values:")
print(df_upd.head())
```

```
label_encoder = LabelEncoder()
                                  # Initialize the LabelEncoder
categorical_features = ['brand', 'country', 'car name']
for column in categorical_features:
    # Fit the LabelEncoder and transform the column
    df_upd[column] = label_encoder.fit_transform(df_upd[column])
    print(df_upd[column])
# Apply price adjustment function (ensure 'apply_price_adj' is defined)
df_upd['price'] = df_upd['price'].apply(apply_price_adj)
# Function to convert non-numeric values to NaN
def to_numeric(value):
    trv:
        return pd.to_numeric(value, errors='coerce') # Coerce non-numeric_
 \rightarrow values to NaN
    except Exception as e:
        return np.nan
# Apply the conversion to numeric for the relevant columns
df_upd['cylinder'] = df_upd['cylinder'].apply(to_numeric)
df_upd['horse_power'] = df_upd['horse_power'].apply(to_numeric)
df_upd['engine_capacity'] = df_upd['engine_capacity'].apply(to_numeric)
df_upd['top_speed'] = df_upd['top_speed'].apply(to_numeric)
df_upd['seats'] = df_upd['seats'].astype(str).str.extract(r'(\d+)')[0].apply(pd.
 →to_numeric, errors='coerce')
print("\n\n")
columns_to_fill = ['car name', 'brand', 'country', 'price', 'cylinder', |
 →'horse_power', 'top_speed', 'seats','engine_capacity']
for column in columns_to_fill:
    # Calculate the median, ignoring NaN values
    median_value = df_upd[column].median()
    print(f"Median value for {column}: {median_value}")
    df_upd[column] = df_upd[column].fillna(median_value)
# Print the dataframe after filling missing values
print("\nAfter filling missing values:")
print(df_upd.head())
Before filling missing values:
```

```
car name price engine_capacity \
0 Fiat 500e 2021 La Prima TBD 0.0
```

```
Peugeot Traveller 2021 L3 VIP
                                               SAR 140,575
                                                                        2.0
1
2 Suzuki Jimny 2021 1.5L Automatic
                                                SAR 98,785
                                                                        1.5
3
     Ford Bronco 2021 2.3T Big Bend
                                               SAR 198,000
                                                                        2.3
4
      Honda HR-V 2021 1.8 i-VTEC LX Orangeburst Metallic
                                                                        1.8
        cylinder horse_power top_speed
                                             seats
                                                       brand country
  N/A, Electric
                       Single Automatic
                                               150
                                                        fiat
                                                                 ksa
                          180
                                8 Seater
                                               8.8
1
                                                    peugeot
                                                                 ksa
2
                          102
                                     145 4 Seater
                                                     suzuki
                                                                 ksa
3
               4
                          420
                                4 Seater
                                               7.5
                                                        ford
                                                                 ksa
4
               4
                          140
                                     190 5 Seater
                                                       honda
                                                                 ksa
0
        25
1
        62
2
        74
3
        26
4
        33
6303
         7
6304
        24
6305
        67
6306
        45
         7
6307
Name: brand, Length: 6308, dtype: int32
        2
1
        2
2
        2
3
        2
4
        2
       . .
6303
        6
6304
        6
6305
        6
6306
        6
6307
Name: country, Length: 6308, dtype: int32
0
         564
1
        1980
2
        2235
3
         574
4
         811
        . . .
6303
         333
6304
         552
6305
        2119
6306
        1246
6307
         334
Name: car name, Length: 6308, dtype: int32
```

```
Median value for car name: 1299.5
     Median value for brand: 46.0
     Median value for country: 3.0
     Median value for price: 33817.5
     Median value for cylinder: 4.0
     Median value for horse_power: 255.0
     Median value for top_speed: 211.0
     Median value for seats: 5.0
     Median value for engine_capacity: 2.7
     After filling missing values:
                     price engine_capacity cylinder horse_power top_speed \
        car name
     0
                                         0.0
                                                   4.0
                                                                          211.0
             564
                     -1.00
                                                               255.0
                                         2.0
     1
            1980 37955.25
                                                   4.0
                                                               180.0
                                                                          211.0
     2
            2235 26671.95
                                         1.5
                                                   4.0
                                                               102.0
                                                                          145.0
     3
             574 53460.00
                                         2.3
                                                   4.0
                                                              420.0
                                                                          211.0
     4
             811
                     -1.00
                                         1.8
                                                   4.0
                                                               140.0
                                                                          190.0
        seats brand
                      country
     0 150.0
                  25
                             2
          8.0
     1
                  62
                             2
                             2
     2
          4.0
                  74
     3
          7.0
                  26
                             2
     4
          5.0
                  33
                             2
[87]: # ##correlation
      data_numeric = df_upd.apply(pd.to_numeric, errors='coerce')
      # Calculate the correlation matrix
      correlation_matrix = data_numeric.corr()
      # Plot the heatmap to visualize correlations
      plt.figure(figsize=(10, 8))
      sns.heatmap(correlation_matrix, annot=True, cmap='coolwarm', vmin=-1, vmax=1,__
       \rightarrowlinewidths=0.5)
      plt.title('Correlation Matrix of Numeric Features')
      plt.show()
```



0.2.1 3 - Split the dataset

Split the dataset into training, validation, and test sets. A common split would be 60% for training, 20% for validation, and 20% for testing.

```
[254]: # First, split the data into 80% training+validation and 20% testing from sklearn.model_selection import train_test_split from sklearn.preprocessing import LabelEncoder

X = df_upd.drop(columns='price') # price is the target column y = df_upd['price']

X_train_val, X_test, y_train_val, y_test = train_test_split(X , y, test_size=0.

$\times 2$, random_state=42$)

# Then, split the 80% training+validation into 60% training and 20% validation X_train, X_val, y_train, y_val = train_test_split(X_train_val, y_train_val, u)

$\times test_size=0.25$, random_state=42$)
```

```
# Print the sizes of each split
print("Training set size:", X_train.shape, y_train.shape)
print("Validation set size:", X_val.shape, y_val.shape)
print("Test set size:", X_test.shape, y_test.shape)
```

```
Training set size: (3784, 8) (3784,)
Validation set size: (1262, 8) (1262,)
Test set size: (1262, 8) (1262,)
```

0.2.2 4-Standardization

```
[257]: from sklearn.preprocessing import StandardScaler
      import numpy as np
      columns_to_standardize = ['top_speed', 'horse_power', 'car name',_
      scaler_standard = StandardScaler()
      # Calculate range before standardization
      print("Range before standardization:")
      for col in columns_to_standardize:
          value_range = np.max(X_train[col]) - np.min(X_train[col])
          print(f"Column: {col}")
          print(f" Range: {value_range:.4f}")
      print("\nStandardizing data...")
      X_train[columns_to_standardize] = scaler_standard.
       →fit_transform(X_train[columns_to_standardize])
      X_val[columns_to_standardize] = scaler_standard.
       →transform(X_val[columns_to_standardize])
      X_test[columns_to_standardize] = scaler_standard.
       →transform(X_test[columns_to_standardize])
      y_train = np.array(y_train).reshape(-1, 1)
      y_val = np.array(y_val).reshape(-1, 1)
      y_test = np.array(y_test).reshape(-1, 1)
      y_train = scaler_standard.fit_transform(y_train)
      y_val = scaler_standard.transform(y_val)
      y_test = scaler_standard.transform(y_test)
      # Calculate range after standardization
      print("\nRange after standardization:")
      for col in columns_to_standardize:
          value_range = np.max(X_train[col]) - np.min(X_train[col])
```

```
print(f"Column: {col}")
    print(f" Range: {value_range:.4f}")
Range before standardization:
Column: top_speed
  Range: 846.0000
Column: horse_power
  Range: 5038.0000
Column: car name
  Range: 2544.0000
Column: engine_capacity
  Range: 6752.0000
Column: brand
  Range: 81.0000
Column: country
  Range: 6.0000
Standardizing data...
Range after standardization:
Column: top_speed
  Range: 17.9885
Column: horse_power
  Range: 26.2387
Column: car name
  Range: 3.5079
Column: engine_capacity
  Range: 12.4028
Column: brand
  Range: 3.5966
Column: country
  Range: 2.9666
```

1 2-Building Regression Models

1.0.1 Linear Regression

```
[243]: import numpy as np
  import matplotlib.pyplot as plt
  from sklearn.linear_model import LinearRegression
  from sklearn.metrics import mean_squared_error, r2_score

model = LinearRegression()
  model.fit(X_train, y_train)

coefficients = model.coef_
  intercept = model.intercept_
```

```
# Check if intercept is an array and handle it
if isinstance(intercept, np.ndarray):
    intercept = intercept[0] # Extract the first intercept if it's an array
print("Linear regression equation:")
equation = f"y = {intercept:.2f} "
for i, coef in enumerate(coefficients[0]): # Use coefficients[0] for single__
 → target variable
    equation += f"+ ({coef:.2f}) * {X_train.columns[i]} "
print(equation)
y_pred_train = model.predict(X_train)
mse_train = mean_squared_error(y_train, y_pred_train)
r2_train = r2_score(y_train, y_pred_train)
print("\n\n")
print(f"Training Mean Squared Error: {mse_train:.2f}")
print(f"Training R2 Score: {r2_train:.2f}")
y_val_pred = model.predict(X_val)
mse = mean_squared_error(y_val, y_val_pred)
r2 = r2_score(y_val, y_val_pred)
print(f"Validation Mean Squared Error: {mse:.2f}")
print(f"Validation R2 Score: {r2:.2f}")
y_test_pred = model.predict(X_test)
mse = mean_squared_error(y_test, y_test_pred)
r2 = r2_score(y_test, y_test_pred)
print(f"Testing Mean Squared Error: {mse:.2f}")
print(f"Testing R<sup>2</sup> Score: {r2:.2f}")
plt.figure(figsize=(8, 6))
plt.scatter(y_val, y_val_pred, alpha=0.6)
plt.plot([y_val.min(), y_val.max()], [y_val.min(), y_val.max()], color='red',__
 \hookrightarrowlinestyle='-', linewidth=2)
plt.xlabel("Actual Prices")
plt.ylabel("Predicted Prices")
plt.title("Actual vs Predicted Prices (Validation Set)")
plt.show()
Linear regression equation:
y = -0.61 + (0.20) * car name + (-0.05) * engine_capacity + (0.12) * cylinder +
(0.21) * horse_power + (0.24) * top_speed + (-0.00) * seats + (-0.17) * brand +
```

(-0.03) * country

Training Mean Squared Error: 0.69

Training R² Score: 0.31

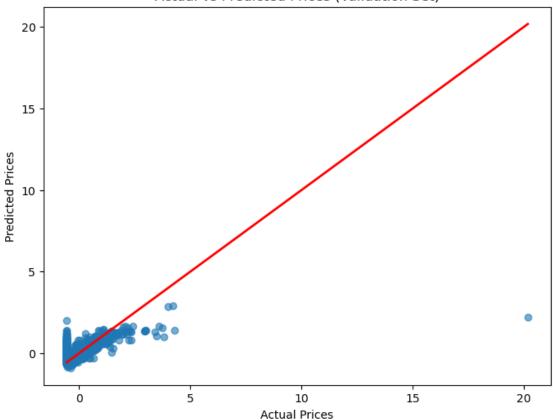
Validation Mean Squared Error: 0.49

Validation R² Score: 0.33

Testing Mean Squared Error: 0.56

Testing R² Score: 0.34

Actual vs Predicted Prices (Validation Set)



1.1 Linear regression using closed form solution

 $weights = (X_transpose \;.\; X) \hat{\;\;} -1 \;.\; (X_transpose \;.\; y)$

```
[247]: import numpy as np
    from sklearn.metrics import mean_squared_error, r2_score

X_train_with_intercept = np.c_[np.ones(X_train.shape[0]), X_train]

X_transpose = X_train_with_intercept.T

X_transpose_X = np.dot(X_transpose, X_train_with_intercept)
```

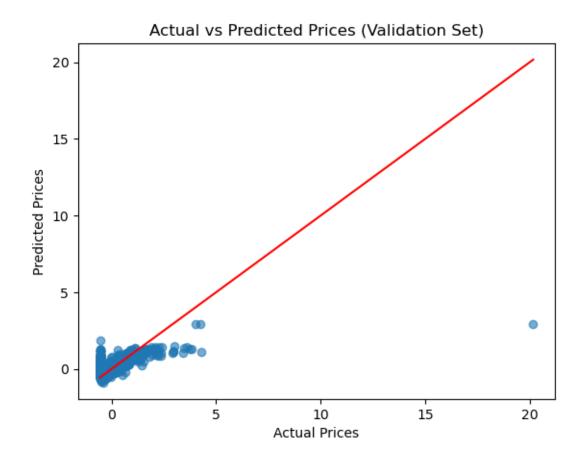
```
X_transpose_X_inv = np.linalg.inv(X_transpose_X)
X_transpose_y = np.dot(X_transpose, y_train)
w = np.dot(X_transpose_X_inv, X_transpose_y)
feature_names = ['intercept'] + list(X_train.columns)
equation_terms = []
for i, coef in enumerate(w):
    equation_terms.append(f"({coef[0]:.2f}) * {feature_names[i]}")
equation = " + ".join(equation_terms)
print("using closed form solution")
print(f"Linear regression equation: y = {equation}")
# Add intercept to validation data and make predictions
X_val_with_intercept = np.c_[np.ones(X_val.shape[0]), X_val]
y_pred_val = np.dot(X_val_with_intercept, w)
# Calculate MSE and R<sup>2</sup> for validation data
mse = mean_squared_error(y_val, y_pred_val)
r2 = r2_score(y_val, y_pred_val)
print(f"Validation Mean Squared Error: {mse:.2f}")
print(f"Validation R2 Score: {r2:.2f}")
# Add intercept to testing data and make predictions
X_test_with_intercept = np.c_[np.ones(X_test.shape[0]), X_test]
y_pred_test = np.dot(X_test_with_intercept, w)
# Calculate MSE and R2 for validation data
mse = mean_squared_error(y_test, y_pred_test)
r2 = r2_score(y_test, y_pred_test)
print(f"Testing Mean Squared Error: {mse:.2f}")
print(f"Testing R<sup>2</sup> Score: {r2:.2f}")
using closed form solution
Linear regression equation: y = (-0.61) * intercept + (0.20) * car name +
(-0.05) * engine_capacity + (0.12) * cylinder + (0.21) * horse_power + (0.24) *
top_speed + (-0.00) * seats + (-0.17) * brand + (-0.03) * country
Validation Mean Squared Error: 0.49
Validation R<sup>2</sup> Score: 0.33
Testing Mean Squared Error: 0.56
Testing R<sup>2</sup> Score: 0.34
```

1.2 Linear regression using the gradient descent method.

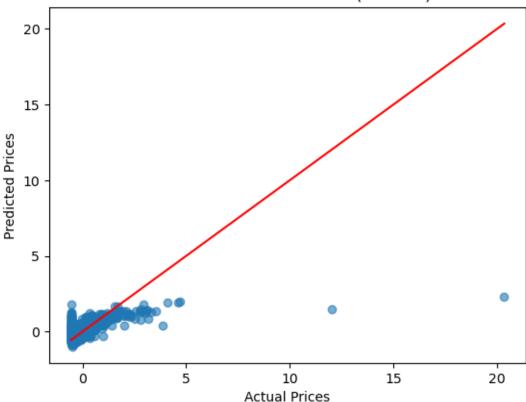
This part is implemented without using any external APIs or libraries for linear regression

```
[285]: import numpy as np
      import matplotlib.pyplot as plt
      from sklearn.preprocessing import StandardScaler
      from sklearn.metrics import mean_squared_error, r2_score
      # Gradient Descent for Linear Regression
      def linear_regression_gd(X, y, learning_rate=0.01, epochs=1000):
           # Add intercept term (bias)
          X = np.c_{[np.ones(X.shape[0]), X]} # Add a column of ones for the intercept
       \rightarrow term
          m = len(y) # Number of samples
          n = X.shape[1] # Number of features + 1 (for intercept term)
          weights = np.zeros(n) # Initialize weights
          for epoch in range(epochs):
              predictions = np.dot(X, weights)
              errors = predictions - y
              gradient = (2 / m) * np.dot(X.T, errors)
              weights -= learning_rate * gradient
          return weights
      # Ensure y is a 1D array
      y_train = y_train.flatten()
      y_val = y_val.flatten()
      # Train model
      learning_rate = 0.001
      epochs = 4000
      weights = linear_regression_gd(X_train, y_train, learning_rate, epochs)
      # Extract intercept and coefficients
      intercept = weights[0]
      coefficients = weights[1:]
      feature_names = ['car name', 'engine_capacity', 'cylinder', 'horse_power', _
       print("solution using gradient descent:")
      equation = f"y = {intercept:.2f} "
      for i, coef in enumerate(coefficients): # Use coefficients for single target
       \rightarrow variable
          equation += f"+ ({coef:.2f}) * {feature_names[i]} " # Access each feature_1
       ⇒by name
      print(equation)
```

```
# Validate predictions
y_val_pred = np.dot(np.c_[np.ones(X_val.shape[0]), X_val], weights)
# Calculate metrics
mse = mean_squared_error(y_val, y_val_pred)
r2 = r2_score(y_val, y_val_pred)
print(f"Validation MSE: {mse:.2f}")
print(f"Validation R2: {r2:.2f}")
# Plot Actual vs Predicted (validation set)
plt.scatter(y_val, y_val_pred, alpha=0.6)
plt.plot([y_val.min(), y_val.max()], [y_val.min(), y_val.max()], color='red')
plt.xlabel("Actual Prices")
plt.ylabel("Predicted Prices")
plt.title("Actual vs Predicted Prices (Validation Set)")
plt.show()
# Plot Actual vs Predicted (test set)
plt.scatter(y_test, y_test_pred, alpha=0.6)
plt.plot([y_test.min(), y_test.max()], [y_test.min(), y_test.max()], color='red')
plt.xlabel("Actual Prices")
plt.ylabel("Predicted Prices")
plt.title("Actual vs Predicted Prices (Test Set)")
plt.show()
NaN in y_val_pred: True
NaN in weights: True
X_val shape: (1262, 8)
weights shape: (9,)
solution using gradient descent:
y = -0.28 + (0.03) * car name + (-0.05) * engine_capacity + (0.06) * cylinder +
(0.28) * horse_power + (0.26) * top_speed + (-0.00) * seats + (-0.00) * brand +
(-0.02) * country
Validation MSE: 0.47
Validation R<sup>2</sup>: 0.36
```

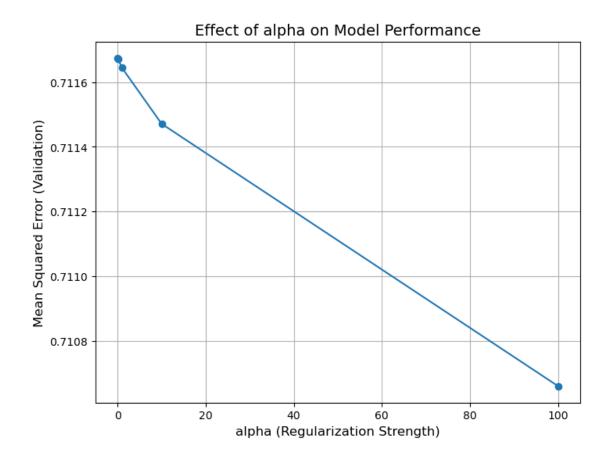


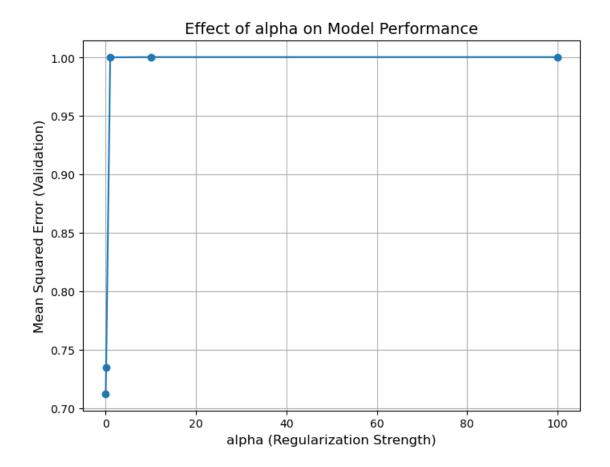




```
[134]: import matplotlib.pyplot as plt
       import pandas as pd
       from sklearn.metrics import mean_squared_error, make_scorer
       from sklearn.model_selection import GridSearchCV
       from sklearn.linear_model import Ridge, Lasso
       def perform_grid_search_and_plot(model, param_grid, X_train, y_train):
           grid_search = GridSearchCV(
               estimator=model,
               param_grid=param_grid,
               scoring=make_scorer(mean_squared_error, greater_is_better=False),
               cv=5,
               verbose=0
           grid_search.fit(X_train, y_train)
           results = pd.DataFrame(grid_search.cv_results_)
           param_name = list(param_grid.keys())[0]
           plt.figure(figsize=(8, 6))
           plt.plot(
```

```
results[f"param_{param_name}"],
       -results["mean_test_score"],
       marker='o'
   plt.xlabel(f"{param_name} (Regularization Strength)", fontsize=12)
   plt.ylabel("Mean Squared Error (Validation)", fontsize=12)
   plt.title(f"Effect of {param_name} on Model Performance", fontsize=14)
   plt.grid(True)
   plt.show()
   return grid_search
# Define the parameter grids
ridge_param_grid = {"alpha": [0.01, 0.1, 1, 10, 100]}
lasso_param_grid = {"alpha": [0.01, 0.1, 1, 10, 100]}
# Perform Grid Search and plot results for Ridge and Lasso
grid_search_ridge = perform_grid_search_and_plot(Ridge(), ridge_param_grid,__
→X_train, y_train)
grid_search_lasso = perform_grid_search_and_plot(Lasso(), lasso_param_grid,_u
# Extract and print the best alpha values from the grid search results
best_alpha_ridge = grid_search_ridge.best_params_['alpha']
best_alpha_lasso = grid_search_lasso.best_params_['alpha']
print(f"Best alpha for Ridge: {best_alpha_ridge}")
print(f"Best alpha for Lasso: {best_alpha_lasso}")
```





Best alpha for Ridge: 100 Best alpha for Lasso: 0.01

1.2.1 2-Ridge regression with grid search for hyperparameter tuning

```
import matplotlib.pyplot as plt
import pandas as pd
from sklearn.metrics import mean_squared_error, r2_score
from sklearn.model_selection import GridSearchCV
from sklearn.linear_model import Ridge

# Function to perform Grid Search and plot results
def perform_grid_search_and_plot(model, param_grid, X_train, y_train):
    grid_search = GridSearchCV(
        estimator=model,
        param_grid=param_grid,
        scoring='neg_mean_squared_error',
        cv=5,
        verbose=0
    )
```

```
grid_search.fit(X_train, y_train)
    results = pd.DataFrame(grid_search.cv_results_)
    param_name = list(param_grid.keys())[0]
    plt.figure(figsize=(8, 6))
    plt.plot(
        results[f"param_{param_name}"],
        -results["mean_test_score"],
       marker='o'
    plt.xlabel(f"{param_name} (Regularization Strength)", fontsize=12)
    plt.ylabel("Mean Squared Error (Validation)", fontsize=12)
    plt.title(f"Effect of {param_name} on Model Performance", fontsize=14)
    plt.grid(True)
   plt.show()
    return grid_search
# Function to perform Ridge regression grid search and plot
def perform_ridge_grid_search_and_plot(X_train, y_train, ridge_param_grid,_u
→feature_names, X_val, y_val):
    ridge = Ridge()
    grid_search_ridge = GridSearchCV(ridge, ridge_param_grid, cv=10,__
→scoring='neg_mean_squared_error', return_train_score=True)
    grid_search_ridge.fit(X_train, y_train)
    #best_alpha_ridge = grid_search_ridge.best_params_['alpha']
    best_alpha_ridge=10
    ridge_model = grid_search_ridge.best_estimator_
    intercept = float(ridge_model.intercept_)
    coefficients = ridge_model.coef_.flatten()
    # Print the Ridge regression equation
    print("Ridge Regression Equation:")
    equation = f"y = {intercept:.2f}"
    for coef, feature in zip(coefficients, feature_names):
        equation += f" + ({coef:.2f}) * {feature}"
    print(equation)
    # Predictions on training data
    y_pred_train = ridge_model.predict(X_train)
    mse_train = mean_squared_error(y_train, y_pred_train)
    r2_train = r2_score(y_train, y_pred_train)
    # Predictions on validation data
    y_pred_val = ridge_model.predict(X_val)
```

```
mse_val = mean_squared_error(y_val, y_pred_val)
   r2_val = r2_score(y_val, y_pred_val)
   y_pred_test = ridge_model.predict(X_test)
   mse_tes = mean_squared_error(y_test, y_pred_test)
   r2_tes = r2_score(y_test, y_pred_test)
   # Print performance metrics
   print(f"Training Mean Squared Error: {mse_train:.2f}")
   print(f"Training R<sup>2</sup> Score: {r2_train:.2f}")
   print(f"Validation Mean Squared Error: {mse_val:.2f}")
   print(f"Validation R2 Score: {r2_val:.2f}")
   print(f"testing Mean Squared Error: {mse_tes:.2f}")
   print(f"testing R2 Score: {r2_tes:.2f}")
   print("-" * 50)
   plt.figure(figsize=(8, 6))
   plt.scatter(y_val, y_pred_val, alpha=0.6)
   plt.plot([y_val.min(), y_val.max()], [y_val.min(), y_val.max()],__
plt.xlabel("Actual Prices")
   plt.ylabel("Predicted Prices")
   plt.title(f"Actual vs Predicted Prices (Ridge on Validation Set)")
   plt.show()
   results = pd.DataFrame(grid_search_ridge.cv_results_)
   param_name = list(ridge_param_grid.keys())[0]
   plt.figure(figsize=(8, 6))
   plt.plot(
       results[f"param_{param_name}"],
       -results["mean_test_score"],
       marker='o'
   plt.xlabel(f"{param_name} (Regularization Strength)", fontsize=12)
   plt.ylabel("Mean Squared Error (Validation)", fontsize=12)
   plt.title("Effect of Alpha on Mean Squared Error", fontsize=14)
   plt.grid(True)
   plt.show()
ridge_param_grid = {"alpha": [0.01, 0.1, 1, 10, 100]}
feature_names = ['car_name', 'engine_capacity', 'cylinder', 'horse_power', __
→'top_speed', 'seats', 'brand', 'country']
```

```
perform_ridge_grid_search_and_plot(X_train, y_train, ridge_param_grid, ⊔ 

→feature_names, X_val, y_val)
```

Ridge Regression Equation:

 $y = -0.63 + (0.05) * car_name + (-0.05) * engine_capacity + (0.12) * cylinder + (0.21) * horse_power + (0.23) * top_speed + (-0.00) * seats + (-0.02) * brand + (-0.02) * country$

Training Mean Squared Error: 0.69

Training R² Score: 0.31

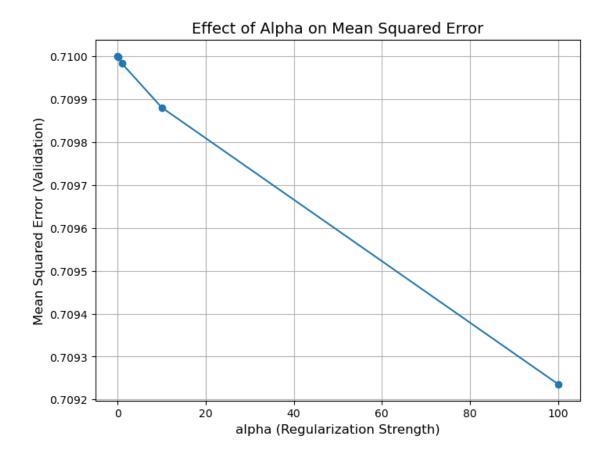
Validation Mean Squared Error: 0.49

Validation R² Score: 0.33

testing Mean Squared Error: 0.57

testing R² Score: 0.34

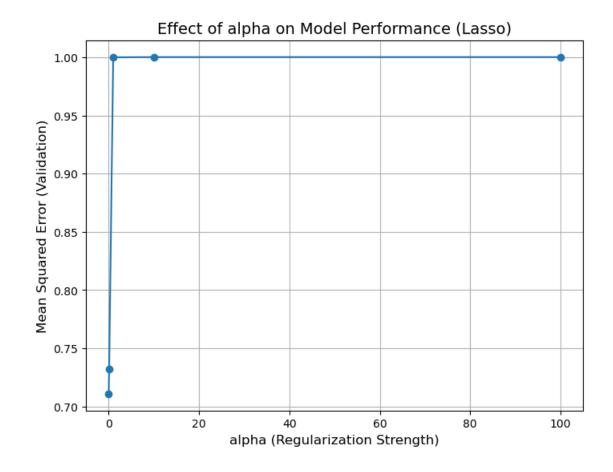
Actual vs Predicted Prices (Ridge on Validation Set) 20 15 5 0 Actual Prices Actual Prices Actual Prices

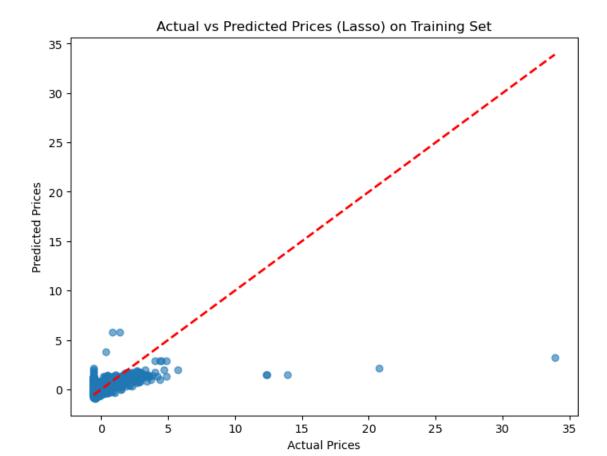


```
[139]: import matplotlib.pyplot as plt
      import pandas as pd
      from sklearn.metrics import mean_squared_error, r2_score
      from sklearn.model_selection import GridSearchCV
      from sklearn.linear_model import Lasso
      def perform_lasso_grid_search_and_plot(X_train, y_train, lasso_param_grid, ⊔
       →feature_names):
          # Define the Lasso model
          lasso = Lasso()
          # Perform Grid Search with cross-validation
          grid_search_lasso = GridSearchCV(lasso, lasso_param_grid, cv=10,_
       grid_search_lasso.fit(X_train, y_train)
          # Best model from Grid Search
          lasso_model = grid_search_lasso.best_estimator_
          best_alpha_lasso = grid_search_lasso.best_params_['alpha']
```

```
# Get the coefficients and intercept
intercept = float(lasso_model.intercept_)
coefficients = lasso_model.coef_.flatten()
# Print the Lasso regression equation
print("Lasso Regression Equation:")
equation = f"y = {intercept:.2f}" # intercept is scalar
for coef, feature in zip(coefficients, feature_names):
    equation += f" + ({coef:.2f}) * {feature}"
print(equation)
# Predictions on training data
y_pred_train = lasso_model.predict(X_train)
mse_train = mean_squared_error(y_train, y_pred_train)
r2_train = r2_score(y_train, y_pred_train)
# Predictions on validation data
y_pred_val = lasso_model.predict(X_val)
mse_val = mean_squared_error(y_val, y_pred_val)
r2_val = r2_score(y_val, y_pred_val)
y_pred_test = lasso_model.predict(X_test)
mse_tes = mean_squared_error(y_test, y_pred_test)
r2_tes = r2_score(y_test, y_pred_test)
# Print performance metrics
print(f"Training Mean Squared Error: {mse_train:.2f}")
print(f"Training R<sup>2</sup> Score: {r2_train:.2f}")
print(f"Validation Mean Squared Error: {mse_val:.2f}")
print(f"Validation R2 Score: {r2_val:.2f}")
print(f"testing Mean Squared Error: {mse_tes:.2f}")
print(f"testing R2 Score: {r2_tes:.2f}")
print("-" * 50)
# Plot the effect of alpha on MSE
results = pd.DataFrame(grid_search_lasso.cv_results_)
param_name = list(lasso_param_grid.keys())[0]
plt.figure(figsize=(8, 6))
plt.plot(
    results[f"param_{param_name}"],
    -results["mean_test_score"],
    marker='o'
plt.xlabel(f"{param_name} (Regularization Strength)", fontsize=12)
plt.ylabel("Mean Squared Error (Validation)", fontsize=12)
```

```
plt.title(f"Effect of {param_name} on Model Performance (Lasso)", _
 →fontsize=14)
    plt.grid(True)
    plt.show()
    # Plot Actual vs Predicted
    y_val_pred_lasso = lasso_model.predict(X_train)
    plt.figure(figsize=(8, 6))
    plt.scatter(y_train, y_val_pred_lasso, alpha=0.6)
    plt.plot([y_train.min(), y_train.max()], [y_train.min(), y_train.max()],
 plt.xlabel("Actual Prices")
    plt.ylabel("Predicted Prices")
    plt.title(f"Actual vs Predicted Prices (Lasso) on Training Set")
    plt.show()
    return grid_search_lasso, best_alpha_lasso
# Define the parameter grid for Lasso
lasso_param_grid = {"alpha": [0.01, 0.1, 1, 10, 100]}
# Define the feature names (adjust this list based on your actual dataset)
feature_names = ['car_name', 'engine_capacity', 'cylinder', 'horse_power', __
 →'top_speed', 'seats', 'brand', 'country']
# Perform Grid Search and plot results for Lasso
perform_lasso_grid_search_and_plot(X_train, y_train, lasso_param_grid,_
 →feature_names)
Lasso Regression Equation:
y = -0.63 + (0.02) * car_name + (-0.04) * engine_capacity + (0.12) * cylinder +
(0.20) * horse_power + (0.23) * top_speed + (-0.00) * seats + (0.00) * brand +
(-0.01) * country
Training Mean Squared Error: 0.69
Training R<sup>2</sup> Score: 0.31
Validation Mean Squared Error: 0.49
Validation R<sup>2</sup> Score: 0.33
testing Mean Squared Error: 0.57
testing R<sup>2</sup> Score: 0.33
```





1.3 Non-linear Models

1.3.1 Polynomial Models

```
import numpy as np
import matplotlib.pyplot as plt
from sklearn.preprocessing import PolynomialFeatures
from sklearn.linear_model import LinearRegression
from sklearn.kernel_ridge import KernelRidge
from sklearn.metrics import mean_squared_error
from mlxtend.feature_selection import SequentialFeatureSelector as SFS

# Polynomial Regression
degrees = [2, 5, 7, 10]
```

```
# ##with forward feature selection
for degree in degrees:
    print(f"Fitting degree {degree}")
    poly = PolynomialFeatures(degree=degree)
    model = LinearRegression()
    # Run forward selection
    selected_features, mse_history = forward_selection(X_train, X_test, y_train,_
→y_test, model, max_features=5)
    # Print the selected features and corresponding MSE history
    print(f"Selected Features: {selected_features}")
    for feature, mse in mse_history:
        print(f"Feature: {feature}, MSE: {mse:.4f}")
    # Train final model with selected features
    model.fit(X_train[selected_features], y_train)
    y_pred = model.predict(X_train[selected_features])
    mse = mean_squared_error(y_train, y_pred)
   print(f"Degree {degree}: MSE on training set = {mse:.4f}")
   # model.fit(X_val[selected_features], y_val)
    y_pred = model.predict(X_val[selected_features])
    mse_val= mean_squared_error(y_val, y_pred)
    print(f"Degree {degree}: MSE on validation set = {mse:.4f}")
    y_pred = model.predict(X_test[selected_features])
    final_mse = mean_squared_error(y_test, y_pred)
    print(f"Final Model MSE on Test Set: {final_mse:.4f}")
    print(f"Finished fitting degree {degree}")
    print("\n\n\n")
#without forward feature selection
#Evaluate models with Mean Squared Error
# print("Polynomial Regression Errors:")
# for degree in degrees:
     poly = PolynomialFeatures(degree=degree)
#
     X_train_poly = poly.fit_transform(X_train)
#
     X_val_poly = poly.transform(X_val)
     X_test_poly = poly.transform(X_test)
     model = LinearRegression()
#
     model.fit(X_train_poly, y_train)
      y_pred = model.predict(X_train_poly)
```

```
mse = mean_squared_error(y_train, y_pred)
#
      print(f"Degree {degree}: MSE on training set = {mse:.4f}")
#
      model.fit(X_val_poly, y_val)
#
      y_pred = model.predict(X_val_poly)
      mse_val= mean_squared_error(y_val, y_pred)
 #
      print(f"Degree {degree}: MSE on validation set = {mse:.4f}")
 #
      model.fit(X_test_poly, y_test)
 #
      y_pred = model.predict(X_test_poly)
      mse = mean_squared_error(y_test, y_pred)
      print(f"Degree {degree}: MSE on test set = {mse:.4f}")
Fitting degree 2
Selected Features: ['horse_power', 'car name', 'engine_capacity', 'country',
'seats']
Feature: horse_power, MSE: 0.5311
Feature: car name, MSE: 0.5299
Feature: engine_capacity, MSE: 0.5290
Feature: country, MSE: 0.5281
Feature: seats, MSE: 0.5275
Degree 2: MSE on training set = 0.7751
Degree 2: MSE on validation set = 0.7751
Final Model MSE on Test Set: 0.5275
Finished fitting degree 2
Fitting degree 5
Selected Features: ['horse_power', 'car name', 'engine_capacity', 'country',
'seats']
Feature: horse_power, MSE: 0.5311
Feature: car name, MSE: 0.5299
Feature: engine_capacity, MSE: 0.5290
Feature: country, MSE: 0.5281
Feature: seats, MSE: 0.5275
Degree 5: MSE on training set = 0.7751
Degree 5: MSE on validation set = 0.7751
Final Model MSE on Test Set: 0.5275
Finished fitting degree 5
Fitting degree 7
Selected Features: ['horse_power', 'car name', 'engine_capacity', 'country',
'seats']
Feature: horse_power, MSE: 0.5311
Feature: car name, MSE: 0.5299
```

```
Degree 7: MSE on validation set = 0.7751
Final Model MSE on Test Set: 0.5275
Finished fitting degree 7

Fitting degree 10
Selected Features: ['horse_power', 'car name', 'engine_capacity', 'country', 'seats']
Feature: horse_power, MSE: 0.5311
Feature: car name, MSE: 0.5299
Feature: engine_capacity, MSE: 0.5290
Feature: country, MSE: 0.5281
Feature: seats, MSE: 0.5275
Degree 10: MSE on training set = 0.7751
Degree 10: MSE on validation set = 0.7751
```

1.3.2 Feature Selection with Forward Selection

Final Model MSE on Test Set: 0.5275

Finished fitting degree 10

Feature: engine_capacity, MSE: 0.5290

Degree 7: MSE on training set = 0.7751

Feature: country, MSE: 0.5281 Feature: seats, MSE: 0.5275

```
# Train and validate the model using selected features
           model.fit(X_train[current_features], y_train)
           y_pred = model.predict(X_test[current_features])
           mse = mean_squared_error(y_test, y_pred) # Calculate MSE on the_
\rightarrow test set
           feature_mse[feature] = mse # Store the MSE for this feature
       # Select the feature with the minimum MSE
       best_feature = min(feature_mse, key=feature_mse.get)
       best_mse_for_feature = feature_mse[best_feature]
       # If the best feature improves the model, add it to selected features
       if best_mse_for_feature < best_mse:</pre>
           selected_features.append(best_feature)
           remaining_features.remove(best_feature)
           best_mse = best_mse_for_feature # Update the best MSE
           mse_history.append((best_feature, best_mse)) # Log the feature and_
\hookrightarrow MSE
       else:
           break # Stop if adding more features doesn't improve the model
   return selected_features, mse_history
```

1.3.3 Radial Basis Function (RBF)

```
[152]: from sklearn.metrics import mean_squared_error, r2_score
      import matplotlib.pyplot as plt
      from sklearn.kernel_ridge import KernelRidge
      from sklearn.linear_model import Ridge
      # RBF Kernel Regression
                      # Regularization parameter for RBF Kernel
      alpha = 1.0
      gamma = 0.1
                        # Kernel coefficient (low value smooths out predictions)
      rbf_model = KernelRidge(kernel="rbf", alpha=alpha, gamma=gamma)
      rbf_model.fit(X_train, y_train)
      # Predictions on training data for RBF Kernel
      y_rbf_train_pred = rbf_model.predict(X_train)
      mse_rbf_train = mean_squared_error(y_train, y_rbf_train_pred)
      # Predictions on validation data for RBF Kernel
      y_rbf_val_pred = rbf_model.predict(X_val)
      mse_rbf_val = mean_squared_error(y_val, y_rbf_val_pred)
      # Predictions on testing data for RBF Kernel
```

```
y_rbf_test_pred = rbf_model.predict(X_test)
mse_rbf_test = mean_squared_error(y_test, y_rbf_test_pred)
# Ridge Regression
ridge_model = Ridge(alpha=1.0) # Use the same alpha for Ridge regression
# Fit the Ridge model
ridge_model.fit(X_train, y_train)
# Predictions on training data for Ridge Regression
y_pred_train = ridge_model.predict(X_train)
mse_train = mean_squared_error(y_train, y_pred_train)
r2_train = r2_score(y_train, y_pred_train)
# Predictions on validation data for Ridge Regression
y_pred_val = ridge_model.predict(X_val)
mse_val = mean_squared_error(y_val, y_pred_val)
r2_val = r2_score(y_val, y_pred_val)
# Predictions on testing data for Ridge Regression
y_pred_test = ridge_model.predict(X_test)
mse_test = mean_squared_error(y_test, y_pred_test)
r2_test = r2_score(y_test, y_pred_test)
# Print performance metrics for Ridge Regression
print(f"Training Mean Squared Error: {mse_train:.2f}")
print(f"Training R<sup>2</sup> Score: {r2_train:.2f}")
print(f"Validation Mean Squared Error: {mse_val:.2f}")
print(f"Validation R2 Score: {r2_val:.2f}")
print(f"Testing Mean Squared Error: {mse_test:.2f}")
print(f"Testing R2 Score: {r2_test:.2f}")
print("-" * 50)
# Visualization of Actual vs Predicted for Ridge Regression (Validation Set)
plt.figure(figsize=(8, 6))
plt.scatter(y_val, y_pred_val, alpha=0.6)
plt.plot([y_val.min(), y_val.max()], [y_val.min(), y_val.max()], color='red',__
→linestyle='--', linewidth=2)
plt.xlabel("Actual Prices")
plt.ylabel("Predicted Prices")
plt.title("Actual vs Predicted Prices (Ridge on Validation Set)")
plt.show()
```

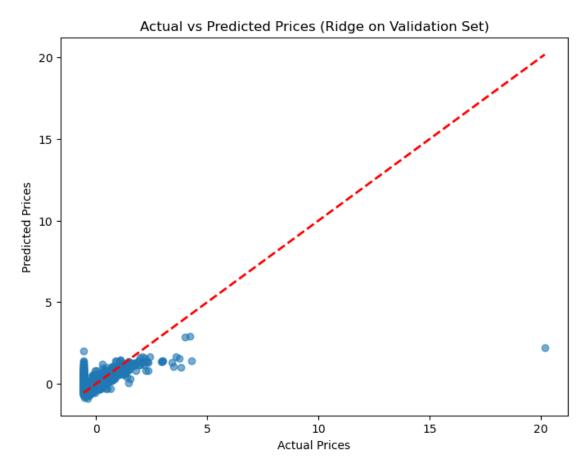
Training Mean Squared Error: 0.69

Training R² Score: 0.31

Validation Mean Squared Error: 0.49

Validation R² Score: 0.33

Testing Mean Squared Error: 0.56



```
y_rbf_test_pred = rbf_model.predict(X_test)
      mse_rbf = mean_squared_error(y_test, y_rbf_test_pred)
      print(f"RBF Kernel: MSE on testing set = {mse_rbf:.4f}")
      RBF Kernel: MSE on training set = 0.3213
      RBF Kernel: MSE on validation set = 0.2956
      RBF Kernel: MSE on testing set = 0.3817
[156]: import numpy as np
      import pandas as pd
      from sklearn.model_selection import train_test_split
      from sklearn.linear_model import LinearRegression, Ridge, Lasso
      from sklearn.preprocessing import PolynomialFeatures
      from sklearn.metrics import mean_squared_error, mean_absolute_error, r2_score
      import matplotlib.pyplot as plt
      models = {
           'Linear Regression': LinearRegression(),
          # 'Ridge Regression': Ridge(alpha=1),
          # 'Lasso Regression': Lasso(alpha=0.1),
          # 'Polynomial Regression (Degree 2)': Pipeline([
                ('poly', PolynomialFeatures(degree=2)),
                 ('model', LinearRegression())
          # ])
      }
       # Dictionary to store metrics for each model
      model_metrics = {}
       # Train and evaluate each model
      for model_name, model in models.items():
          # Fit the model
          model.fit(X_train, y_train)
          # Predict on the validation set
          y_val_pred = model.predict(X_val)
          # Calculate metrics
          mse = mean_squared_error(y_val, y_val_pred)
          mae = mean_absolute_error(y_val, y_val_pred)
          r2 = r2_score(y_val, y_val_pred)
          # Store metrics in the dictionary
          model_metrics[model_name] = {'MSE': mse, 'MAE': mae, 'R2': r2}
           # Print model performance
          print(f"Model: {model_name}")
```

```
print(f"Validation Mean Squared Error (MSE): {mse:.2f}")
    print(f"Validation Mean Absolute Error (MAE): {mae:.2f}")
    print(f"Validation R2 Score: {r2:.2f}")
    print("-" * 50)
\# # Compare models based on MSE, MAE, and R^2
best_model = min(model_metrics, key=lambda x: model_metrics[x]['MSE'])
# print(f"The best model based on the lowest MSE is: {best_model}")
best_model_fit = models[best_model]
y_val_pred_best_model = best_model_fit.predict(X_val)
plt.figure(figsize=(8, 6))
plt.scatter(y_val, y_val_pred_best_model, alpha=0.6)
plt.plot([y_val.min(), y_val.max()], [y_val.min(), y_val.max()], color='red',__
→linestyle='--', linewidth=2)
plt.xlabel("Actual Prices")
plt.ylabel("Predicted Prices")
plt.title(f"Actual vs Predicted Prices ({best_model} on Validation Set)")
plt.show()
```

Model: Linear Regression

Validation Mean Squared Error (MSE): 0.49 Validation Mean Absolute Error (MAE): 0.32

Validation R² Score: 0.33

