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## Abstract

This is the Abstract!

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# Acknowledgements

I like to acknowledge ...
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titles?

## Contents

1	In	troduction	1
1	Intr	roduction and Overview	1
	1.1	Motivation	1
	1.2	History and evolution of batteries	1
	1.3	Lithium based batteries	4
	1.4	Magnesium batteries	7
	1.5	Earlier work	7
	1.6	Scope of the thesis	7
		1.6.1 Research Question	8
		1.6.2 Approach	8
	1.7	Structure of the thesis	9
II	<b>F</b>	Coundations	10
<b>2</b>	Bat	teries	10
	2.1	Cell operation principles and design	10
		2.1.1 The manufacturing process of an Alkaline battery	11
		2.1.2 Theoretical Cell voltage, Capacity, specific Energy, Energy density	12
	2.2	Cell limitations & definitions	14
		2.2.1 Polarization	14
	2.3		14
	۷.5	Battery chemistries	11
	2.4	Intercalation batteries and why Li	14

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	2.6	On Mg- and Li- batteries and their state today	18
3	Mad	chine Learning	19
	3.1	The basics of Machine Learning	19
		3.1.1 Example time!	19
		3.1.2 Supervised and Unsupervised Learning	20
		3.1.3 Regression and Classification Problems	20
		3.1.4 Data collection, Preparation, Features and Feature Selection	21
	3.2	Bias-variance tradeoff	21
	3.3	Random Forest	22
		3.3.1 Ensemble learning	22
		3.3.2 Decision tree	23
		3.3.3 Random forest	23
	3.4	Mean square error and Root mean square deviation	25
	3.5	$R^2$ score - The Coefficient of Variation	25
	3.6	Principle Component Analysis	26
	3.7	K-fold cross validation	26
	3.8	Mutual Information**	26
	3.9	Machine Learning × batteries	27
II	I I	Method	28
4	Son	ne Method title	28
	4.1	Data set and Experimental Environment	28
	4.2	Volumetric number density	29
	4.3	Void Fraction	29
	4.4	AP-RDF Descriptors of Electrode materials	30

Sond	Sondre Torp Master!				
4	.5	Algorithm	31		
IV	I	Result & Discussion	34		
5 F	les	sult section title	34		
5	.1	Random factors from database	34		
		5.1.1 Average Voltage	34		
		5.1.2 Capacity	34		
		5.1.3 Energy Density	34		
5	.2	Volumetric number density	34		
		5.2.1 Average Voltage	35		
		5.2.2 Capacity	36		
		5.2.3 Energy Density	36		
5	.3	Void fraction	36		
5	.4	AP-RDF	36		
5	.5	Stability	36		
5	.6	Geometrical descriptors	37		
$\mathbf{V}$	$\mathbf{S}_{1}$	ummary	38		
6 S	un	nmary and future work	38		
6	.1	Batteries	38		
6	.2	future work	38		
		6.2.1 improving method	38		
$\mathbf{Lis}$	t d	of Figures			
1		A voltaic pile, the first battery [33]	2		

Sondre Torp

A draft of a Daniell cell. The anode is a piece of zinc and the cathode a piece of copper. The salt bridge transports ions between the solutions and the electrons moves through an external circuit. Figure recovered from [34]	3
The two-dimensional trigonal omega-like structure of $\mathrm{TiS}_2$ . Observing from a slight angle along the b-axis. The titanium in grey, are occupying the octahedral holes of sulfur, in yellow. Lithium-ions would intercalate into the space between the $\mathrm{TiS}_2$ layers. Figure attained from materialspoject [26]	5
Schematic illustration of the first Li-ion battery $\text{LiCoO}_{2/}\text{Li}^+$ electrolyte/graphite), Figure acquired from [10]	6
Crystal structures of a)LiCoO <sub>2</sub> [35] b) LiMn <sub>2</sub> O <sub>4</sub> [36], c) LiFePO <sub>4</sub> [25]. The layers in $a$ ), the canals in $b$ ) and $c$ ) are illustrated	6
Simplified illustration showing the concepts of bias-variance problem. Left to right; high bias, low bias and low variance, high variance. Adopted from [31]	22
Combining a lot of different classifiers trained on the same data, which in combination can make a much better decision boundary on the target data. Adopted from $[15]$	23
A simple example of a decision tree for playing tennis. Root in red, leaf node in blue. Adapted from [7]	24
Mg- prediction accuracy results on the Targets; Average Voltage(AV), gravimetric capacity(GV), volumetric capacity(VC), specific energy(SE), and energy density(ED). Each row showes the number representing that type of test, as included in section(REF)	35
Li- prediction accuracy results on the Targets; Average Voltage(AV), gravimetric capacity(GV), volumetric capacity(VC), specific energy(SE), and energy density(ED). Each row showes the number representing that type of test, as included in section(REF)	35
Mg- prediction accuracy results on the Targets; Average Voltage(AV), gravimetric capacity(GV), volumetric capacity(VC), specific energy(SE), and energy density(ED). Each row showes the number representing that type of test, as included in section(REF)	36
Mg- prediction accuracy results on the Targets; Average Voltage(AV), gravimetric capacity(GV), volumetric capacity(VC), specific energy(SE), and energy density(ED). Each row showes the number representing that type of test, as included in section(REF). With the AP-RDF as predictor.	36
	an external circuit. Figure recovered from [34]

## List of Tables

## Part I

## Introduction

## 1 Introduction and Overview

Introduce the task at hand.

In this chapter the background and motivation for this paper is presented. The historical development of batteries are presented shortly and former work are presented.

#### 1.1 Motivation

The motivation for this work originates from the rapidly increasing demand for better batteries, both for vehicular and stationary applications. Better batteries mean better products, with longer life, lower cost, and adequate energy storage options. Due to the complexity of the chemical processes involved, it is of high importance to be able to develop predictive modeling methods to improve the search for better compositions and performances

## 1.2 History and evolution of batteries

Never been a more needing market for batteries. Tremendous amount of resources are used on an international level to produce batteries with higher capacity, voltage and energy density. The evolution of batteries started in Italy in the year 1800 by Alessandro Volta (1745 - 1827) that made the first known battery[30]. His invention was the voltaic pile, zinc and copper plates stacked on top of each other with sheets of bine-soaked cardboard between each plate. The revolutionary property of the voltaic pile was that it could produce a stable current over some time, and not just short sparks of electricity. This invention was the foundation of todays modern battery. 1



Figure 1: A voltaic pile, the first battery [33]

It took almost 40 years, 1836, before the British inventor John Frederic Daniell Voltas continuation with the discovery of the Daniell cell [6]. The Daniell cell is constructed with to half cells, one with a zinc electrode in a zinc sulfate dissolution, and another copper electrode in a copper sulfate solution. These half cells are connected by a salt bridge. This cell could give a voltage of 1.1 V through the reaction shown below, 1.1.

$$Zn_{(s)} + Cu_{(aq)}^{2+} \rightarrow Zn_{(aq)}^{2+} + Cu_{(s)}$$
 (1.1)

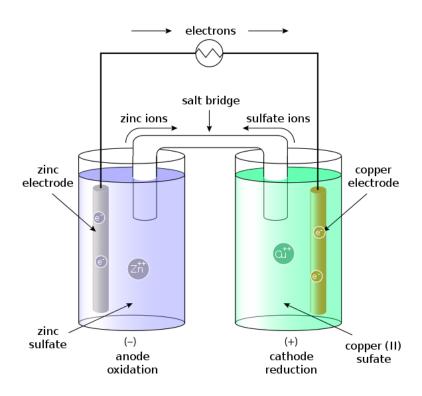


Figure 2: A draft of a Daniell cell. The anode is a piece of zinc and the cathode a piece of copper. The salt bridge transports ions between the solutions and the electrons moves through an external circuit. Figure recovered from [34]

In 1859 constructed the french physicist Gaston Planté the first led-acid battery. The battery could be charged by applying an external opposite potential, and it was the first secondary battery every made. Planté rolled two led plates into a spiral, separated by rubber stripps, so that the plates would not touch. The lead-acid battery was special due to the electrolyte being a active part of the chemical reaction in the battery. The electrodes in the battery were led anode, and led(IV) oxide cathode, immerse din sulfuric acid. The overall reaction is shown beneath: 1.2. Both the anode and the cathode are made into led(II) sulfate during discharged. The charge is depleted in the electrolyte when the battery is completely discharged (The sulfuric acid has a lower density). Charging changes the electrolyte back into concentrated sulfuric acid.

$$PbO_{2(s)} + Pb_{(s)}2 H_2SO_{4(s)} \rightarrow 2 PbSO_{4(s)} + 2 H_2O_{(l)}$$
 (1.2)

The open circuit voltage  $(V_{OC})$  for a led-acid battery are approximately 2 V. It is custom to attach these batteries in series to attain a higher voltage, typical 6 or 12 V. These batteries have a shelf- and cycle life. Normally more then 10 years or 1000-2000 cycles. They are still in use in modern cars. Led-acid batteries have a relative low *specific energy*, which means that the current is low compared to its weight, they are also renowned for their high environmental impact. Therefor, one of the many goals of battery producers are to replace led-acid batteries with better alternatives.

Nickel-cadmium(NiCd) batteries was first described by the swede Waldemar Jungner in 1899 [5].

These batteries rose fast in popularity due to their high energy density, low weight, long shelf life, and their relative fast recharge. Typically they yield a voltage of  $1.4\,\mathrm{V}$ . The cathode is made of Nickel oxide hydroxide, and the anode is made of metallic cadmium, while the alkaline electrolyte is a basic solution of potassium hydroxide. The Specific energy of a typical Nickel-cadmium is  $40-60\,\mathrm{Wh/kg}$ . Equation 1.3 shows the overall reaction of such a battery.

$$2 \operatorname{NiOOH} + \operatorname{Cd} + 2 \operatorname{H}_2 \operatorname{O} \to 2 \operatorname{Ni(OH)}_2 + \operatorname{Cd(OH)}_2$$
 (1.3)

Nickel-metal hydride (NiMH) batteries was first commercialized in the 1980's and had several similarities with the NiCd batteries. The main difference is the anode where in NiCd batteries it is Cd, while in NiMH it is replaced by an alloy that makes metal hydrides (MH). NiMH batteries has the same electrolyte as NiCd batteries, a watery solution of potassium hydroxide. The nominal cell voltage of such a battery is typically around  $1.2\,\mathrm{V}$  and the Specific energy is  $60-120\,\mathrm{Wh/kg}$ . Equation  $1.4\,\mathrm{Shows}$  the overall reaction of a NiMH battery.

$$Ni(OH)_2 + M \rightarrow NiO(OH) + MH$$
 (1.4)

A primary cell is a battery that can not be recharged after use. These batteries are normally used in remote controls, flashlights, and other small household appliances. Alkaline manganese batteries, or just alkaline batteries, are one of the most common primary cells in modern society. Anodes of zinc, cathodes of manganese oxide and a electrolyte of potassium hydroxide, from where it gets its nickname. A typical alkaline battery delivers a nominal cell voltage of 1.5 V. The overall reaction for a alkaline battery is shown below 1.5.

$$\operatorname{Zn} + 2\operatorname{MnO} + \operatorname{H}_2\operatorname{O} \to \operatorname{ZnO} + 2\operatorname{MnO}(\operatorname{OH})$$
 (1.5)

#### 1.3 Lithium based batteries

In 1975 discovered Micheal Stanley Whittingham the intercalation electrodes for lithium and other alkaline metals [32]. This led to the first lithium batteries with titanium disulfide (TiS<sub>2</sub>) as the cathode and metallic lithium as the anode. TiS<sub>2</sub> -structure is divided into layers and lithium-ions can easily move in and out of the structure without significant changes in the structure, which makes the reaction reversible. Figure 3 shows the layered structure of TiS<sub>2</sub>. During discharge of the battery, lithium-ions leave the anode of metallic lithium and moves through the electrolyte and into the empty octahedral position in the TiS<sub>2</sub>-structure, while titanium(IV) reduces to titanium(III). While applying an overpotential to the material, or charging, the lithium-ions moves out of the TiS<sub>2</sub>-structure and titanium oxides back to titanium(IV) again. This discovery was the start of a major research investment in cathode materials of sulfite and other chalcogens in the 70-80's.

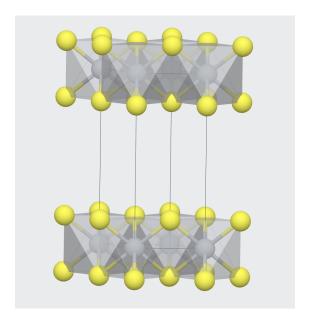


Figure 3: The two-dimensional trigonal omega-like structure of  $TiS_2$ . Observing from a slight angle along the b-axis. The titanium in grey, are occupying the octahedral holes of sulfur, in yellow. Lithiumions would intercalate into the space between the  $TiS_2$  layers. Figure attained from materialspoject [26].

It is of the utmost importans that the Lithium-ions in a lithium battery can easily be intercalated and extracted (Can I phrase it like this?) in a reversible manor, and such layered structures are especially good for this purpose. In 1980 introduced John B. Goodenough  $\text{LiCoO}_2$  as the cathode material for lithium batteries, a material that gave a  $V_{OC}$  of 4-5 V, which opened up many possibilities to alternate the negative electrodes, and earned him, M. Stanley Whittingham and Akira Yoshino the Nobel Prize in Chemistry. Goodenough and colleagues found a current density of up to  $4\,\text{mAcm}^{-2}$  [18] [9]. Even though the properties where exceptionally good at the time, the batteries were still not commercialized due to metallic lithium being unstable, and deemed to be an unsafe anode. This was due to dendrites growing out of the anode that short circuited the battery.

In 1990 introduces Sony lithium batteries on the commercial market. They had exchanged the metallic lithium anode for graphite which reduced the growth of dendrites on the anode. The electrolyte was a organic solvent with a lithium salt. A lithium-ion battery refers to a battery where lithium intercalates in both electrode materials, both the cathode and the anode. While lithium batteries has a anode of metallic lithium. This nomenclature is transferable to other type of batteries like, magnesium/magnesium-ion batteries.

Figure 4 shows a draft of a lithium-ion battery with  $\text{LiCoO}_2$  as the cathode and graphite as the anode. During discharged the lithium-ions moves from the anode, through the electrolyte and separator to the cathode. The electron moves from the anode to the cathode through a separat circuit, where the electrical energy can be extracted. The overall reaction is shown in equation: 1.6

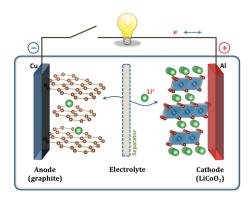


Figure 4: Schematic illustration of the first Li-ion battery  $\text{LiCoO}_{2/}\text{Li}^+$  electrolyte/graphite), Figure acquired from [10].

$$LiCoO_2 + C_6 \rightarrow Li_{1-x}CoO_2 + Li_xC_6$$
(1.6)

The cathode materials used in lithium-ion batteries have evolved since the 1990 until today. Normal cathode materials today are  $LiMn_2O_4$  and  $LiFePO_4$ . Neither of the two has a layered structure as in the  $SO_2$  structure, but  $LiMn_2O_4$  is a good ionic conductor due to the structure having canals in all three dimensions where lithium can be transported, see ??. While  $LiFePO_4$  has a lower ionic conductivity, due to it only having canals in one dimension, see figure 5c. It is still a popular material due to its high cycle life. There still exist layered structures that are in use in batteries.

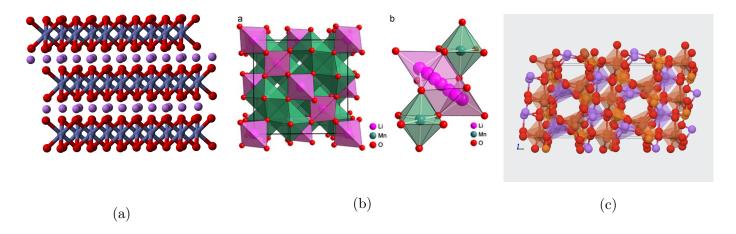


Figure 5: Crystal structures of a)LiCoO<sub>2</sub>[35] b) LiMn<sub>2</sub>O<sub>4</sub>[36], c) LiFePO<sub>4</sub>[25]. The layers in a), the canals in b) and c) are illustrated.

The most used anode materials for lithium-ion batteries are graphite and other forms of carbon based materials. Graphite has a high energy density, making the cathode material the limiting factor for energy density of Lithium-ion batteries. To improve the cathode material is therefore high in priority.

There is an ongoing search for candidates for solid-state electrolytes, due to energy density and safety being the main factors that govern the development of the rechargeable battery technology

[11]. This is not just limited to Lithium-ion batteries other active elements as Na and Mg are also being explored. Solid-state electrolytes would enable stable and reliable operation of all-solid-state Li-, Na-, and Mg-based batteries. Special focus is given to lightweight complex metal hydrides, due to them showing high ionic conductivity, and in some cases electrochemical properties that enable battery reversibility. move this to later.

## 1.4 Magnesium batteries

The abundance of magnesium in the earth's crust, combined with its low atomic weight, low cost, and electrochemically active nature, makes magnesium a great candidate for battery applications. It can serve as a potential negative electrode with its electrochemical potential of -2.37 V. It is environmentally friendly due to its by-products being safely excreted through urin.

renowned as a primary battery

secondary battery rising! The first prototype of a Magnesium secondary cell was produced

### 1.5 Earlier work

## 1.6 Scope of the thesis

Write more about: PV, wind, solar -> storage.

"At what cost can one charge stationary secondary batteries with solar/wind power efficiently, and provide a centralized energy storage? For what shelf and cycle life? with how rapid a respons a power outage or fluctuation in the grid. And with how large a capacity, at a competitive cost? " where?

Batteries are vastly complex and much efforts have been devoted to the development of these. Yet, with all the efforts put in to electrochemical cells, there are still a never ending chase for batteries that can push the limits of their properties even further. The demand for better batteries are growing faster then ever. The global electric car fleet, for instance, exceeding 5.1 milion[1], almost doubling the number of new electric car registrations in the last year. And if we follow the policies of the EV30@30 Scenario which aims to reach a 30% market share for EVs in all models except two wheelers by 2030, due to one quarter of global greenhouse gas(GHG) emissions comes from this sector. The EV sales per year are then predicted to be more then 43 milion, and the stock numbering more than 250 milion.

This work proposes a methodology to predict these properties accurately without the need of big scale simulations, or computer heavy calculations. Using state of the art machine learning, and base properties of all ready existing databases, we propose a set of predictors to see if we can predict the properties of new, undiscovered electrodes, or even new properties in already well known electrodes.

Some of the most important cell properties are; voltage, energy density, specific energy or capacity, flammability, available cell constructions, operating temperature range, shelf life or self discharge, low cost, and worldwide consumer distribution. Most of these properties are to an extent dictated by

battery chemistry. And it is of the general publics interest to improve several of these characteristics, both for once pleasure (i.e. several more hours to play candy crush), and the peoples general safety (i.e. electric car crashes, and Samsung phones). In this work we will focus on the base properties; voltage, energy density, specific energy, and the physical stability of the materials. No real battery fulfills all of these requirements. And most real batteries underperforms We therefore leave the safety issues to the experimentalists.

The idea behind the designe of a battery is fairly simple, due to their similar procedure to create electricity. Two of the most important parts are the Anode and the Cathode. A cell produces electricity when placed into a medium that has conductive properties, namely the electrolyte.

Today some of the main methods for theoretical advances in battery science are density functional theory (DFT), molecular dynamic simulations and

## 1.6.1 Research Question

How to better batteries?

RQ1: Is there potential for the use machine learning to easy the search for better battery materials?

RQ2: Which ML method would be the most optimal for such a search?

RQ3: What predictors are the most suited for such a task, and which would yield the most efficient training.

RQ4: How does the size of the database affect the results?

## 1.6.2 Approach

The choice of features examined in this work is inspired by an extensive survey done on similar project especially in the field of Metal Organic Framework(MOFS) done by my supervisors in Crete, and dictated, to some degree by the lack of more data.(REF)

To answer the questions s

In order to evaluate the effect of different features, a prediction approach using principle component analysis was utilized. First we used physical descriptors, geometrical properties of the unit cell, for instance. This because it was greatly efficient in similar studies (REF) on MOFS, and is straightforward. Other descriptors are needed, and the void fraction seemed like the next obvious one, that is both geometrical and easy to obtain. Afte

## 1.7 Structure of the thesis

First the most essential concepts from the fields of batteries, machine learning, and work already explored on these two fields conjoined, are introduced. Then the method will be explained before rounding up our results so far before trying to put this all into perspective.

## Part II

## **Foundations**

## 2 Batteries

The basis of batteries needs an introduction. In this section, batteries and how they are designed and how they operate will be explained. A special focus will be dedicated to electrodes which are the part of the battery that this work is focused on. Some of the more essential properties related to the chemistry of the work will also be introduced.

"The most advantageous combination of cathode and anode materials are those that will be lightest and give a high cell voltage and capacity. [27]"

Some of the most important properties in an anode are; Hight coulombic output(Ah/g), good conductivity, stability.

"Practically anodes are metalls. Li- are a good example of this, it is the lightest metal with a high value of electrochemical equivalence. With the development of intercalation electrodes, lithiated carbons are finding wide use. Lithium alloys are also being explored for use as anodes in lithium-ion battery. The cathode must be a good oxidizing agent, be stable, when in contact with a electrolyte, and have a

The cathode must be a good oxidizing agent, be stable, when in contact with a electrolyte, and have a useful working voltage.

## 2.1 Cell operation principles and design

Batteries and fuel cells are electrochemical devices. They stort chemical energy that can be converted into electrical energy. This is done by a oxidation-reduction (redox) reaction where one of the species in the reaction gain or lose an electron by changing the oxidation number.

A battery consists of one or more *cells*. A cell is composted of three parts; the anode, the cathode, and the electrolyte.

The anode is an negative electrode, which refers to the direction of current through the electrode. It is a metal that would oxidize if given the opportunity. For a conventional current flow the electron moves from the anode to the cathode. The anode is normally low voltage.

The cathode is a positive electrode. The cathode is a metal that is normally combined with oxygen and is where the reduction occurs. A common example of a oxide is iron oxide, this oxide is very fragile, but their are oxides that are strong enough to be shaped before used in the cell. The cathode is normally high voltage.

The electrolyte is the material that, when introduced to the anode and the cathode, provides an electrically conducting medium for transfer of charge. The anode draws oxygen atoms toward it, creating an electrical flow, with electrons moving from the end of the anode to the end of the cathode not emerged in the electrolyte. The electrolyte is typically a liquid, to impart ionic conductivity. It is

2 BATTERIES Page 10 of 41

often alkaline and when this is the case the battery is a alkaline battery. It can be a solid, but this is less common. The cell will not produce electricity without a circuit that is complete. The electrolyte can, in some designes, act as both the electrolyte and the anode or cathode. If the anode is made from pure metal and has an external cathode of ambient air it is referred to as a metal-air electrochemical cell. These batteries have a much higher theoretical energy density. However there are technical issues confronting their development. [14]

The difference between high- and low voltage is referred to as the cell voltage, which is the driving force for the discharge of the battery. For secondary batteries, as are the one in question (Not really true, we are only looking at Electrodes.), it is possible to recharge batteries by reversing this process by applying an external electrical power source, so that it creates a over-potential - a higher voltage than the one produced by the cell, with the same polarity.

Changes in the design of the cell dictates the cells performance. If the compositions of the anode and cathode are changed, the cell will yield more or less electricity. Adjustments in the cell can affect the amount of electricity, the rate of production, the voltage, and the cell's ability to function in different temperatures. There is almost an endless amount of possibilities, even though the most common cell has been 1.5 volt alkaline batteries. Other types of batteries include Lithium batteries, Magnesium batteries, Zinc batteries, Mercury batteries and others. Should cover these shorty in another subsection? Write something about Magnesium and Li- as a minimum.

## 2.1.1 The manufacturing process of an Alkaline battery

In alkaline batteries the cathode is used both as the container and the cathode. Manganese dioxide, graphite, and the electrolyte are mixed and ganulated and pressed into hollow cylinders called preforms. The preforms can be stacked or replaced by an extruded ring of the same material. The preforms are then combined with nickel-plated steal. These are then the containers of the battery.

A separator is then soaked in the electrolyte solution and inserted between the cathode and where the anode is supposed to be. The anode is then put into the can, in a Alkaline battery like this, it is a gel composed of zinc powder and other materials like potassium hydroxide electrolyte. The gel does not fill the whole can, so that their is room for the chemical reaction to occur.

The can is then sealed with three connected components. The first being a current collector, going to thirds of the way trough the anode with a plastic seal at the top before it is all closed by a metal cover with a metal cap. The current collector goes all the way through the plastic seal and is connected to the metal cap. The seal is thinner in some places, in case of gas build ups. In some battery designes, wax are used instead of a plastic seal, so excessive gas can push through the wall. Lastly a label is attached to the battery, with the necessary information about the battery.

The battery is then take through a complex quality control, to certify the batteries ability to resist corrosion, maintain a good shelf life, usage life, and other factors.

useless section?

2 BATTERIES Page 11 of 41

## 2.1.2 Theoretical Cell voltage, Capacity, specific Energy, Energy density

In a cell there are essentially two areas or sites in the device where the redox reactions occur. In general these half-cell reactions can be expressed as one reduction and one oxidation reaction:

$$aA + ne = cC$$

where a is the number of molecules of substans A taken up by n electrons to form c molecules of C, and the oxidation reaction defined in the same way:

$$bB \leftrightharpoons dD + ne$$

with the overall reaction being:

$$aA + bB \leftrightharpoons cC + dD \tag{2.1}$$

Whenever there is a reaction, there is a decrease in the free energy of the system, namely standard Gibbs energy, and is defined as:

$$\Delta G^0 = -nFE^0$$

Where n is the number of electrons in the reaction, and F is the Faraday constant.

 $E^0$  is the standard potential of the cell is determined by the type of active material in the cell, and can be calculated from the free energy. The standard potential of a cell can be calculated form the standard electrode potential.

$$Anode + cathode = standard potential$$

#### example?

In the situation where we are not in the standard state, the voltage E of a cell is given by the Nernst equation.

$$E = E^0 - \frac{RT}{nF} \ln \frac{a_C^c a_D^d}{a_A^a a_B^b}$$

where  $a_i$  is the activity of the species. R is the gas constant, and T is the absolute temperature.

Gibbs free energy of the reaction is the driving force of the battery, and enables it to deliver energy to an external circuit.

The theoretical *capacity* is determined by the amount of active material in the cell. If the calculation are based on only the active materials participating in the electrochemical reaction the theoretical capacity of a  $Zn/Cl_2$  cell is 0.394Ah/g

2 BATTERIES Page 12 of 41

$${\rm Ze+Cl_2 \rightarrow ZnCl_2}$$
 
$$1.22 {\rm g/Ah} + 1.32 {\rm g/Ah} = 2.54 {\rm g/Ah}$$

Capacity can be defined as:

$$C = \int I(t) \cdot dt \tag{2.2}$$

And is the i number of electrons or cations exchanged between the negative and positive electrodes. I(t) is the current, i.e. the number of electrons flowing over the external circuit per time interval dt which is integrated over the discharge period. The capacity is normally expressed as Ah/kg. Theoretically, 1 gram equivalent weights of the active material in grams divided by the number of electrons in the reaction.

The battery can deliver a power that is defined as

$$P(t) = V(t)I(t) \tag{2.3}$$

Where I(t) is defined as earlier, and drawn at a cell voltage V(t). The amount of work that can be done by the battery, or; the energy contained in the battery, is then defined as the power delivered over the discharge period

$$W = \int P(t) \cdot dt = \int V(t)I(t) \cdot dt$$
 (2.4)

Specific capacity and energy densities of battery materials can be compared relative to mass, volume and cost. The more electrode material that a battery contains, the greater is its capacity and energy. The higher the cell voltage the greater its power and energy.

The active materials of the electrodes allow the reversible uptake and release of Mg, or Li ions. This may happen by; movement of the ions; into, i.e. intersection or intercalation or out of, i.e. extraction or deintercalation, their chemical structures, phases. This is done by conversion of the materials between ion poor and rich i.e. alloying, or rich and poor, e.g. dealloying phases, this can also be done by conversion of the electrode material into other more ion rich/poor chemical forms or mixtures. Referred to as conversion or displacement reaction, with the average ion content of the entire electrode varying.

The total Li or Mg content in the electrodes will thus either be varied by changing the composition of one phase or the ratio between coexisting phases. In this work ?we will only look at *intercalation* type batteries, due to the *database*, more on this later.

## Specific Energy

Specific Energy, or gravimetric energy density, defines battery capacity in weight, energy density, or volumetric energy density, defined as:

$$Watthours/gram = Voltage \times Ampere-hours/gram$$
 (2.5)

2 BATTERIES Page 13 of 41

#### 2.2 Cell limitations & definitions

In this paper, especially under the section on general properties of battery, an amount of technical terms related to material details, from is used. Here I will clarify what we mean by these terms.

#### 2.2.1 Polarization

Polarizability is a tabulated atomic properties, it is the ability to form instantaneous dipoles(REF), and is defined as:

$$\alpha = \frac{P}{E}$$

Where  $\alpha$  is the polarizability in isotropic media, p is the induced dipole moment of an atom to the electric field E that, is the field that produces the dipole momentum.

## 2.3 Battery chemistries

## 2.4 Intercalation batteries and why Li

"Among the rechargeable battery technologies (Fig. 11), the current Li-ion battery technology offers the best useable energy and tap density, dominating the worldwide market for mobile electronic devices 2 for decades. Li-ion batteries have minimal (unwanted) side reactions when a Li ion intercalates into or desorbs from the cathode/anode materials. Their energy efficiency may be further enhanced by lowering the internal resistance of the battery, and they exhibit limited self-discharge, and no memory effects that limit energy density after many cycles. Li-ion batteries as a result, receive considerable attention at both fundamental and applied research levels.

The development of stable novel materials is the key to the success of development of novel and advanced rechargeable batteries. Current research and development has focused on upgrading the energy density of Li-ion batteries.

Most practical rechargeable batteries deliver capacities and energy densities far below their theoretical values (med kilder) due to limited utilization efficiency of the active materials that participate in electrochemical reactions. The major reasons for such limitations include effects that result from slow electrode process kinetics with high polarization and low ionic diffusion or electronic conductivity rates, particularly at the electrolyte–electrode interfaces. Material stability issues caused by a low Li content can also impact on its degree of charging. Therefore, the improvement in existing rechargeable battery systems involves exploring key materials and focusing our attention on the atomic, ionic, or molecular diffusion and transport. Charge transfer, the optimization of surface and interface structure, and the regulation of electrochemical reactions within Li-ion systems may pave the way for improved (i) capacity, and energy and power density, (ii) reactivity, reversibility, and structural stability during

2 BATTERIES Page 14 of 41

charge—discharge cycles, (iii) ionic diffusion and electronic transfer at high charge—discharge rate, and (iv) lower cost, increased safety and environmental compatibility

inkluder litt om dette? og med bilder kanskje?

The schematic diagram of the current Li-ion battery based on a carbon based anode (LixC6), cathode (LiCoO2), liquid electrolyte (LiPF6 dissolved in a mixture of EC and DMC or equivalent), and separator is shown in Fig. 2.9 In the foreseeable future, Li-ion batteries will be the most practical solution to a wide range of electrical energy storage applications.10

. The majority new cathode materials for Li-ion batteries under research and development are transition metal oxides, which tend to provide lower discharge potential as the electric-capacity density increases. Carbon-based materials (usually graphite) are currently used as anode materials in Li-ion batteries. The other variety of carbon-based materials and pure Li metal are currently proposed as alternate anode materials, but many need further improvement with respect to electrode potential and charge—discharge cycle life concerns

"[3]

Working principle of Li-ion cell.

When a Li-ion battery discharges, a  ${\rm Li}^+$  moves from the anode (i.e. graphite) to the cathode (i.e.  ${\rm LiMO}_2$  where M is a transition metal), through the electrolyte that commonly is  ${\rm Li}^+$ -containing salt. The reaction, as discussed above 2.1, are:

$$\label{eq:LiMO2} \begin{split} \operatorname{LiMO_2} &\leftrightharpoons \operatorname{Li}_{1-x} \operatorname{MO_2} + x \operatorname{Li}^+ + x e^- \text{ (cathode)} \\ & x \operatorname{Li}^+ + x e^- + x \operatorname{C}_6 \leftrightharpoons x \operatorname{LiC_6} \text{ (anode)} \end{split}$$

The overall reaction:

$$\mathrm{LiMO_2} + 6\,\mathrm{C} \leftrightarrows \mathrm{Li_{1-x}MO_2} + \mathrm{xLiC_6}$$

The anode is graphite, thus there is noe metallic Li, which makes the Li-ion battery less reactive, therefor safer, and the graphite anode offers a longer cycle life than their Li-metal counterpart. To progress the performance of Li-ion batteries a few design changes are needed; A cathode with a chemical potential that matches the electrolytes highest occupied molecular orbital, and an anode matching the lowest unoccupied molecular orbital of the electrolyte. A non-aqueous electrolyte of high Li<sup>+</sup> ion conductivity under practical temperatures.

#### 2.5 Electrodes and features

In this section the features used in ML as predictors will be introduces. First will the pair properties be introduced, before going into the more electrode specific features.

As a general note. These features are based on optimal design and discharge conditions. These values are helpful to set a number on the "goodness" of a battery, the actual performance may vary under normal conditions of use. Nice to give this note?

2 BATTERIES Page 15 of 41

## Average Voltage

The theoretical voltage and capacity of a cell are function of the anode and cathode materials, with the composition of the electrolyte, and the temperature, normally 25°C.

The active materials contained in the cell determines the standard potential,  $E^0$ , which can be calculated from the free-energy. The standard potential of a cell can be calculated from the standard electrode potential:

Anode(oxidation potential) + cathode (reduction potential) = standard cell potential (2.6)

The cell voltage is also dependent on other factors including concentration and temperature, as expressed om the nernst equation. (REF) *Average Voltage* as we use, is defined as the voltage average during the discharge. It is lower then the theoretical voltage.

## Physical stability

What we refer to as Physical stability is Energy above hull. The energy that is demanded for decomposition of the material into the set of most stable materials at that chemical composition. Some positive value indicates that the material is not stable. While a zero energy above hull indicates that this is the most stable material at its composition.

## 2.5.1 Properties of materials

Are These (or some of them) theoretically computed properties. If yes provide some details about how they computed (i.e. DFT methods)

Total Magnetic Moment ( $\mu_{\rm B}$ ) is calculated for the unit cell within the magnetic ordering provided.

The Formation Energy per Atom is calculated from the formation energy from the elements normalized to per atom in the unit cell.

Energy Above Hull per Atom The energy of decomposition of the material into the set of most stable materials at this chemical composition, in eV per atom. Stability is tested against all potential chemical combinations that result in the material's composition. For example a  ${\rm Mg_3Sb_2}$  structure would be tested against other  ${\rm Mg_3Sb_2}$  structures, against Mg and Sb mixtures, and against MgSb and Sb<sub>2</sub> mixtures.

Density, here defined as the calculated bulk crystalline density, typically underestimated due to the calculated cell volume being overestimated on average by 3%(+-6%).

The Band Gaps are calculated a little different. In general, band gaps are computed with common exchange-correlation functionals such as the LDA [23] and GGA are severely underestimated [22]. Typically the disagreement is reported to be 50% in the literature. Some internal testing by the

2 BATTERIES Page 16 of 41

Material Project supports these statements; typically, they found that band gaps are underestimated by  $\tilde{4}0\%$ . We additionally find that several known insulators are predicted to be metallic.

Cycle life Rate capability RC Self discharge SDEnergy per atom EpA volume Volume of the unit cell defined as Formation energy per atom Fepa

## Band gap

The band gaps of a solid is simply the range of energies an electrode in a solid can not have. While the bandstructurs. How much to include? Should I here have a page on quantum physics and the bandstructure? - Only include relevant stuff.

2 BATTERIES Page 17 of 41

## Total magnetization

Tm

Elasticity

 $\mathbf{E}$ 

#### Porous Electrodes

In a fuel cell system, the reactant is supplied from the electrolyte phase toe the catalytic electrode surface. Electrodes are often composites made of active reactants, binders and fillers, in batteries. To minimize the energy loss of both activation and concentration polarizations at the electrode surface and to increase the electrode efficiency or utilization, it is often preferd to have a large electrode surface area. This can be done by have a porous electrode design. A porous design can provide an interfacial area per unit volume that is considerable higher den that of a planar electrode.

A porous electrode is a electrode that concists of porous matrice of solids and void space. The electrolyte penetrates the void space of a porous matrix. In such an active porous mass, the mass transfer condition in conjunction with the electrochemical reaction occurring at the interface is very complicated. In a given time druing cell operation, the rate of reaction within the pores may vary significantly depending on the location. The distribution of current density within the porous electrode depends on the physical structure(pore size), the conductivity of the solid matrix and the electrolyte, and the electrochemical kinetic parameters of the electrochemical processes.

## 2.6 On Mg- and Li- batteries and their state today

2 BATTERIES Page 18 of 41

## 3 Machine Learning

In this chapter we summarize some concepts of machine learning and related ideas. The first section introduces the basic ideas behind machine learning and \*some of the best known examples\* will be presented. Secondly the concepts of supervised and unsupervised learning will be presented with a clarification on the difference between regression and classification problems, so that we can define where in the field of machine learning this work resides in. Basics of methods utilized in this work will be introduced, emphasizing Random forest. Subsequently a short description of the validation methods used is given. These are; K-fold cross validation and how it is used in optimizing our random forest method, mean square error (MSE), root mean square error (RMSE) and R-squared  $(R^2)$ .

Before we round of this section with a brief explanation on the role of data, how features can affect the effectiveness of a model, and finalizing with the concepts of over- and under-fitting, and how these are related to the bias-variance-trade-off.

Sondre: Did you forget something? Come back to this when done with the section.

## 3.1 The basics of Machine Learning

Machine learning comes from the field of pattern recognition and learning theory, and is defined as the field of study that gives computers the ability to learn without being explicitly programmed. Or more precise: "... A computer program is said to learn from experience E with respect to some class of tasks T and performance measure P, if its performance at tasks in T, as measured by P, improves with the experience E..."([17]). At its core the ability to learn by detecting patterns in usually huge amounts of data that, more often then not, is impossible to perceive for a human.

## 3.1.1 Example time!

As an introduction on how machine learning was applied to learn and recognize patterns in our work, it will be useful to start with a simple example applied to the recognition of the handwritten number "5". (PICTURE TIME!)

How two people writes a single digit may vary to an extensive degree. It might seem to be a easy problem, but if the recognition is to be done manually million of times, it is no longer a trivial task for any one human being. Therefore a model which can recognize these digits would be useful. A model that takes a picture of a digit and outputs that digit in a way that is recognizable for a machine, that is, a digital format.

Machine learning only works when you have data, preferably a large amount of data. For instance data from the MNIST test dataset([13]). This database contain 60,000 images of handwritten numbers that is commonly used for both various training, and testing in the field of machine learning. The images all are 18x18 pixels. The data is divided into two sets, one training set:  $X_{Train}$  and one test set:  $X_{test}$ 

How do one represent an image as something that makes logical sense to a computer? Most learning algorithms take numbers as input. To a computer one image is nothing more than a grid of numbers that represent how dark a pixel is. So each picture contains a gray-scale value that ranges from 0 to 255. Where each sample can be viewed as a vector consisting of 324 features. Every sample has a corresponding label value, or target, which is the digital equivalent to the handwritten sample. We let the corresponding targets be denoted:  $Y_{train}$  and  $Y_{test}$ , for training and testing data. Next we designate our learner denoted by function A. A is then given our training set S, where  $S = (X_{train1}, Y_{train2}), ..., (X_{trainN}, Y_{trainN})$  and returns a prediction rule:  $h: X \to Y$ . This rule is also called a predictor, in general, a classifier, or a regressor, depending on the problem in question.

The training phase is a prosess where the learning algorithm gets tweaked to best capture the correlating structure of the data set, so that it can better predict new data. As mentioned in the last paragraph the output from the training phase is called a predictor. The next step is to introduce the predictor for new, unseen data, so that it can be classified. Then we compare the  $Y_{test}$  to our predicted value  $Y_{pred}$  given by h to see if our model generalizes well to unseen data in  $X_{test}$ .

## 3.1.2 Supervised and Unsupervised Learning

One of the most basic separations in machine learning is the partition between supervised learning and unsupervised learning. [8]

In the case of supervised learning one knows the answer to a problem, and let the computer deduce its own logic to figure out how we get to that result, thus the name complete-date problem is commonly used. This is the most common type of learning. With unsupervised learning the machine is tasked with finding patterns and relationships in data sets without any prior knowledge of the system, incomplete-data problems. Some authors operate with a third and a forth category, namely reinforcement learning, where the machine learns by trial-and-error(marsland2014machine), and evolutionary learning, where they account for the biological evolution and that it can be seen as a learning process.

In this thesis we only consider supervised learning. Algorithms and challenges specifically related to unsupervised learning, reinforcement learning, and evolutionary learning, is therefore not further examined.

## 3.1.3 Regression and Classification Problems

A respons variable can either be qualitative or quantitative in nature. For the qualitative respons variable, let's assume a set of data points  $\vec{x}$  and a goal of finding the value of the output y when x=0.5. The value x=0.5 is not in the data points given so it is needed a way to predict the value. Given in the example above, we assume that there exists a function h that the value comes from. When that function is found one can find any given y for any given x. This is what is known as a regression problem - The respons takes form of a continuous numerical value. The regression problem is a problem of function approximation or interpolation. It may occur a scenario where there are multiple functions, lets say h and g, that fits the given data perfectly. If this is the case one need to pick a value in between our data points and use our functions h and g to predict its values and compere the result to see which is better. mby connect it tighter with the handwritten example? This does not seems as very intelligent

behavior, but the problems of interpolation can be very difficult in higher dimensional space. This will also be observed in classification, the other aspect of what our algorithms can do.

If the response variable is quantitative the problem is referred to as a classification problem. Such a problem consists of taking several input vectors and deciding which of N classes they belong to. This decision or prediction comes from training on examples of each class. I underline again that classification problems are of a discrete nature - The input only belongs to one class.

In this work we want to predict characteristics of batteries , meaning that our task is a regression problem.

## 3.1.4 Data collection, Preparation, Features and Feature Selection

Normally the data collection is a enormous part of the work and not easily available, or, at the very least, needs to be assembled and prepared. If the problem is completely new it might be natural to engulf this step with the next one. (Which is, more or less, what this work tries to do.) With a small dataset with many different features one can experiment and try to figure out what features are the most useful before picking those and collecting a full dataset based on them before doing a complete analysis.

A common problem is that there is too much data that can be relevant, but that data is hard to find or represent in a way that makes sense for the machine. This can be because it requires too many measurements, or, something thing that is prevalent in this work(How much should I refer to this here and not later?), that they are in a variety of places and formats. For instance; if the measurements are already taken, but at vastly different temperatures they might be hard to compare or merge. It is important to have a *clean* dataset, this means that the dataset does not have missing data, significant errors, and so on. On top of all of this, supervised learning requires a target y, which demands time and involvement of experts.

The specific input to a model is normally referred to as a feature, that is, numerical representation of raw data. The amount of features are of importance for the machine learning algorithm to successfully make a good prediction. If there are to few relevant features one can not make an accurate prediction due to the lack of necessary data. And if there are to many features, or many of the features are irrelevant to the task the model will be more expensive.

The amount of information needed is extensive, and should be of high quality. A bigger dataset demands a higher cost, and predicting the amount of data required is a futile endeavor. Luckily Machine Learning is still less computationally costly than modeling full systems at a micro or nanoscale, which makes it interesting in the field of material science.

#### 3.2 Bias-variance tradeoff

As the algorithm learns we need to make sure that it generalizes well to data not in our training set. Obviously the algorithm can not generalize beyond the limits of the training data. Therefore it is important to minimize the two sources of errors known as bias and variance. This is known as the

bias-variance trade off. It is the property of trying to minimize the two errors simultaneously, and should not be confused with the *irreducible error* of a model which is a result of the noise of the data. These three together are the terms used to analyze an algorithms expected *generalization error*, which will be handled later(Ref).

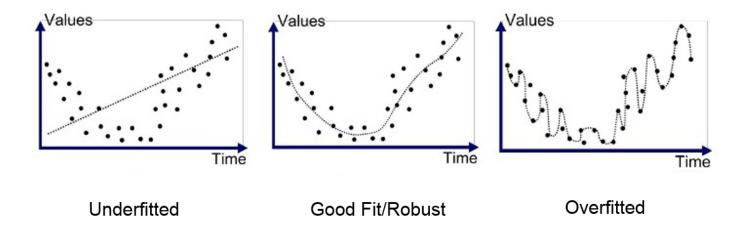


Figure 6: Simplified illustration showing the concepts of bias-variance problem. Left to right; high bias, low bias and low variance, high variance. Adopted from [31]

Our machine is bias if it generalizes to much. The error is due to low variability in our training data, or that it did not adapt to the training data appropriately. The machine misses the relevant relations in the data set between the features and the output. This effect leads to that which is commonly referred to as under-fitting, see left on figure 6.

Variance is the error that stems from high variability, and the number of degrees of variability in most machine learning algorithms is huge([15]). In simple terms there is a low degree of generalization. It might be a perfect fit, but as soon as new data is introduces our predictions plummet. This is commonly referred to as over-fitting, see right on figure 6.

A good way to understand the idea of bias-variance tradeoff is that a more complex model with an increased number of features is not necessarily better at predicting what you want to predict.

#### 3.3 Random Forest

Should I use more math? I am trying to expain these things as simple as possible with little mathematical syntax

## 3.3.1 Ensemble learning

There are many different machine learning algorithms, in this work we have focused on the *ensemble* method;  $Random\ forest[4]$ . The idea of ensemble learning is that two heads are better than one, so why

not have many learners that all get slightly different results on the same data, and then combine them.

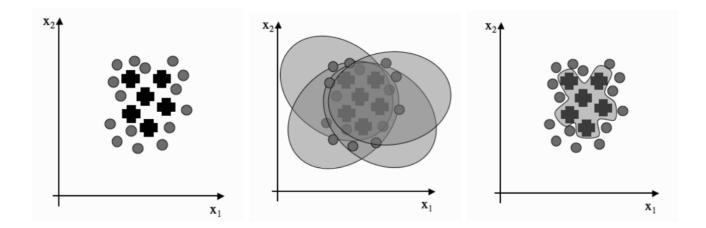


Figure 7: Combining a lot of different classifiers trained on the same data, which in combination can make a much better decision boundary on the target data. Adopted from [15]

Ensemble methods are particularly usefull in machine learning when there is little data, as well as when there is much data, this is heavily due to cross-validation, see(Ref to other section on cross-validation).

#### 3.3.2 Decision tree

A decision tree is a low cost binary flowchart-like structure. It is one of the most common data structures in the field of computational science, both because of the low cost to make the tree, but also because the cost of using the tree is even lower;  $\mathcal{O}(\log N)$ , where N is the number of datapoints.[15].

Decision trees are structured much like a regular tree8; at the top there is a base, or a *root*, down the branches there are chance nodes, and at the end of the branches there are *leaves*, or end nodes. Every internal node is structured like an conditional statement on a feature. Example? If overcast, play. Rain -> more questions The chance nodes are the results from these tests, and the leaves are the class labels. The full route from root to leaf is the classification rule. An advantage of random forest being based in decision trees is that the algorithm is much more like a "white box" compared to Neural networks black box approach, because we can retrace the decisions of each tree. This is especially helpful in the research done in this work where we want to figure out the roll of every feature, and how they affect the result.

#### 3.3.3 Random forest

Random forest is ensamble such a learning method, the idea is that one decision tree is good and many trees, or a forest, is better. The most interesting part of random forest is the randomness that is

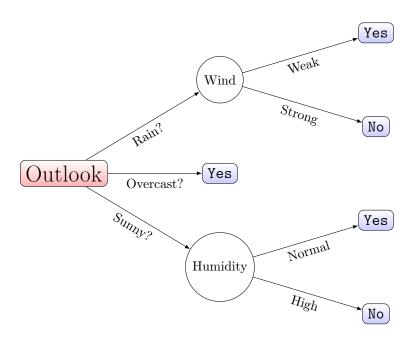


Figure 8: A simple example of a decision tree for playing tennis. Root in red, leaf node in blue. Adapted from [7]

introduces. Several classifiers are achieved by using the simple combination method *bagging*. Bagging stands for *bootstrap* aggregating. Bootstrapping is the process of taking a sample from the original dataset at random, and replacing parts of it with other original data, so that it is not equal to the original data. There will then be several samples where some of the data is equal, while others are completely different. For the bootstrapping in random forest, one sample is taken from the dataset for each tree.

Then a new parameter is introduced, at each node a random subset of features are given to the tree, and it can only make decisions based on that specific subset, and not the original tree. This increases the randomness in the creation of each tree, and it speeds up the learning process. The reason to add randomness to the algorithm is to reduce variance without effecting bias. It also removes the need for decision tree *pruning*, that is, reducing the complexity of decision tree by removing the parts of the tree that does not help the classifier. This reduces overfitting. The process of creating trees is repeated until the error stops decreasing.

When the forest is done, we use a majority vote system, which is a comparison of the mean response for regression. For a point by point algorithm, see the appendix (REF to appendix). The reason for not using cross-validation in the learning algorithm, which is common in other machine learning methods (Ref to cross-val), is that our bootstrap method only uses about 65% of the data, leaving 35% on average which can give a estimated test error.

The main reason we decided to opt in for random forest is due to an article by .... that clearly states that random forest is the go to machine learning algorithm when you are not sure where to start.

## 3.4 Mean square error and Root mean square deviation

The Mean Square Error (MSE) can give a measure of the quality of our estimator. (ref) It is defined as

$$MSE(\epsilon) = \frac{1}{n} \sum_{n=1}^{n-1} \epsilon^2 = \frac{1}{n_{\text{samples}}} \sum_{n=1}^{n_{\text{samples}}-1} (y_i - \hat{y}_i)^2$$
(3.1)

Where  $\hat{y}_i$  is the predicted value of the *i*-th sample, and  $y_i$  is the corresponding true value. As such it can be thought of as the average of the square of our residuals. Therefore the MSE can never have negative values, and smaller values mean that we have a better prediction, where at zero there is a perfect fit.

The Root mean square deviation, or root mean square Error(RSME), is the squared for the MSE:

$$RMSE = \sqrt{MSE} = \sqrt{\frac{\sum_{n=1}^{n-1} (y_i - \hat{y}_i)^2}{n}}$$

And is thus the distance, on average, of a data point from the fitted line, measured along a vertical line. The RSME is directly interpretable in terms of measurement units, and so is a better measure of goodness of fit than a correlation coefficient.

## 3.5 $R^2$ score - The Coefficient of Variation

In regression validation the  $R^2$  is the standard when it comes to measuring goodness of fit.(REF=?[coef]] Needs new ref.) In straight terms it is the proportion of the variance in the dependent variable that is predictable from the independent variable (S).

$$R^{2} = 1 - \frac{SS_{res}}{SS_{tot}} = 1 - \frac{\sum (y_{i} - f_{i})^{2}}{\sum (y_{i} - \bar{y}_{i})^{2}}$$
(3.2)

Where  $y_i$  are the indexed response variables (data to be fitted) and  $f_i$  the predictor variables from the model with  $\epsilon_i = y_i - f_i$ . The average of the response variables is denoted  $\bar{y}_i$ . The second term can also be considered as the ratio of MSE to the variance (the 1/n factors null each other out in a fraction), or the total sum of squares  $(SS_{tot})$ .

If the residual sum of squares  $(SS_{res})$  is low the fit is good. However, this should be compared to the spread of the response variables. After all, if the response variables are all nicely distributed close to the mean, then getting a good  $SS_{res}$  is not suspicious. We therefore do a normalization in the fraction, taking the scale of data into consideration. In the simplest polynomial fit, using a zero order polynomial (a constant), our model would just be a constant function of the mean. The sums being equal, returning unity on the fraction and the total  $R^2$  score would be zero. In the other extreme, if the model fits perfectly, then  $SS_{res}$  would be zero and the  $R^2$  score would be one. In this sense we have a span of possible  $R^2$  scores between zero and one, from the baseline of the simplest model at zero, and a perfect fit at one. In contradiction to most scores the value can be negative, because the model can get arbitrarily worse, thus giving negative values. The  $R^2$  score is useful as a measure of how good our model is at predicting future samples.

## 3.6 Principle Component Analysis

Principle Component Analysis (PCA) is a procedure that uses orthogonal linear transformation to reduces the amount of feature subspaces. It goes under different names in different fields, but the most recognizable might be Singel Value Decomposition. This is done by converting a set of possible correlated variables into a set of uncorrelated variables, called principle components (PC).

The PC are arrange so that the first PC has the largest variance, meaning that it accounts for as much of the variability in the data given as possible. The next PC does the same, it accounts for as much of the variability as possible with the constraint that it is orthogonal to all the former components. These orthogonal vectors are linear combinations being an uncorrelated orthogonal basis set. Graphically the shortest vectors effects the predictions the least. PCA is sensitive to the relative scaling of the original variables, so in sklearn.decomposition.PCA the input data is centered but not scaled for each feature before the SVD of the date is applied.

#### 3.7 K-fold cross validation

K-folding is a cross validation technique that allows us to generalize the trends in our data set to an independent data set. In this way we can circumvent typical problems like over-fitting and selection bias.(ref=[cross-valid]) The approach for the technique is simple. Instead of doing a regression on the entire data set, it is first segmented into k number of subsets of equal size (making sure to pick out the variables randomly before distributing them to the subsets).

Now one subset can be chosen to be the 'control' or 'validation' set while the rest of the subsets are the training sets. The desirable regression is then applied on the training set, arriving at some data fitting that is the prediction. From here it is a straight forward process to analyze how well our predicted variables compare to the validation variables, for example through the  $R^2$  score function. However, even though the subsets are picked randomly, the validation subset used could potentially not be a representative selection of the entire set. Therefore the process is repeated k times, each time using a new subset as the validation subset. After all this is done one can simply calculate the average of the scores to get the predictive power of our model. As an added benefit, since the calculations are done anyways, the average of the predictions can be used as the final fit.

Cross validation techniques are extremely useful when the gathering of new data is difficult or, sometimes, even impossible, as we are using the extra computational power at our disposal to squeeze the most amount of relevant information out of our data.

FIGURE? link to good crossvalidation. https://scikit-learn.org/stable/modules/cross\_validation.html#cross-validation

## 3.8 Mutual Information\*\*

Ranking of features. This can be useful.

## 3.9 Machine Learning $\times$ batteries

State of the art. What has been done in this field? Similar predictions of the kind we are interested in, have been done by Sandek: [28]

B MACHINE LEARNING Page 27 of 41

## Part III

## Method

#### 4 Some Method title

In this section we will introduce the overall approach to the research. First introducing the data set and experimental environment, before going through technicalities in the methods used to represent physical and chemical properties of the electrode materials.

All codes are written in Python 3.7[29] or Fortran98[2] and can be found here: https://github.com/sondrt/Creten\_Stuff gitrep private, change?. And all computations are done on a (give computer specifics.), if nothing else is notedAny libraries that uses this? read machine architecture. The main frameworks and libraries we used for our data mining and data analysis are Python with NumPy[19], JSON [24], Pandas[16], and Scikit-learn [21]. To make the AP-RDF files Fortran90 was used.

## 4.1 Data set and Experimental Environment

The techniques used in this work are the *volumetric number density*(n), the *Void fraction*(Vf) and the *atomic property weighted radial distribution function*(AP-RDF). Other properties used where introduces in the foundation section 2.1.2. Lastly we quickly mentions the basics of our algorithm.

The first needed for this tas was a database(db), we found several, but opted into materialsproject[12](mp), due to their investment in a battery explorer (www.materialsproject.org/batteries), which made, the otherwise main task of this work, collecting the data, much easier. The db has a sizable amount of information on electrodes available. Mp has 16128 conversion electrode and 4401 intercalation electrodes. We decided to go for the intercalation electrodes only, due to them seeming more promising for our use.

First of all mp had the reduced cell formula with consistent CIF files for all voltage pairs, that is; both the charged and discharged material. Secondly many different characteristics or voltage pair properties are present. Some of these characteristics, that we used as targets in this work, are; Average voltage, Gravimetric and volumetric Capacity, Specific Energy (Wh/kg), Energy density (Wh/l), and a measurement of the stability; energy above hull measured in eV/atom. Other properties that where in the mp db and to some extent tested as predictors for each material, both charged, and discharged are; the space group, energy per atom, volume of the unit cell, volume change in percentage, band gap, density, total magnetization, number of sites, and elasticity.

The database contains more than 4400 intercalation electrodes, where we have used 2291 Lithiumion batteries, and 360 Magnesium-ion batteries, for our analysis. This could easily be expanded to the 321 Natrium-ion batteries, and 481 Calcium-ion batteries in the db. With new compounds being added to the database continuously, including many new structural predictors, there is a high likelihood of an

increase in accuracy over time, due to the db growing. Our method were tested on Mg-intercalation electrodes as well as Li-intercalation electrodes, then compared to each other to identify correlations on the valuableness of our predictors.

It is important to note that we have a minimum of two predictor per property of the material at any given run. This is due to how we defined each battery. They have at least one charged and one discharged state, and only one target(ref to theory machine learning). For any given property we have one value calculated for the charged material, and one for the discharged material. This means that we predict for a specific charged- or discharged half cell configuration.

Example: Look at the battery  $Mg(CrS_2)_2$  with the battery ID: mvc - 1200000091, it has two material ID's, one for the discharged-(mvc - 91), and one for the charged (mvc - 14769) material. This pair will be referred to in this section.

## 4.2 Volumetric number density

Volumetric number density, n, is used to describe concentration of countable objects. And is defined as:

$$n = \frac{\text{#of atoms}}{\text{Volume}} \tag{4.1}$$

Where *Volume* is the volume of the unit cell.

Technically, in the volumetric number density, there is a predictor for each individual element. That is; if the intercalation battery framework is  $Mg(CrS_2)_2$  then the the number density for; magnesium, chromium, and oxygen, related only to that material, will be predictors. The charged material will have the predictors with the values:  $S_{vol} = 36.6292$  and  $Cr_{vol} = 18.3150$ . While the discharged material will have the predictors with the values:  $S_{vol-dis} = 30.1286$ ,  $Cr_{vol-dis} = 18.3150$ , and  $Mg_{vol-dis} = 7.5321$ . All other elements still exists as predictors for this framework, both charged and discharged, and exist as possible branches in the decision threes, but they are given the value 0. This quality is uniq for the volumetric number density, and all other predictors minimize "empty" columns.

It is probable that such a direct measurement of a geometrical aspect could be a good predictor due to the physical significants of the information. If RF were applied on to the entirety of the CIF file, it is probable that it would make a bad fit, due to the bias-Variance-trade-off as mentioned in section 3.2, and because of the difference in complexity of some of these files. ref to two vastly different files in the appendix or on github?

#### 4.3 Void Fraction

#### rewrite

Void Fraction, or the porosity, is a measurement of the void space in the material. Calculated ab initio with Poreblazer[20]. We measure the accessible void, that is, the total amount of void space

accessible from the surface. The pore volume is obtainable experimentally under the assumption that Gurvich rule is valid. It states that "if the density of the saturated nitrogen in the pores is assumed equal to its liquid density, regardless of the shape of the internal void network and, because of the weak interactions, regardless of the chemistry of the framework." The pore volume  $(v_{pore})$  and the porosity  $(\theta)$  are computed from:

$$v_{pore} = \frac{n_{N_2}^{ads,satd}}{\rho_{N_2}^{liq}} \tag{4.2}$$

$$\theta = v_{pore} \cdot \rho_{crust} \tag{4.3}$$

Where  $n_{N_2}^{ads,satd}$  is the specific amount of nitrogen adsorbed,  $\rho_{N_2}^{liq}$  is the density of liquid nitrogen, and  $\rho_{cryst}$  is the density of the crystal in question.

Two different pore volumes are calculated, the geometric pore volume,  $Ge_{pv}$ , which is defined as all the free volume of the unit cell, and Helium pore volume,  $He_{pv}$ , where the unit cell that can fit a probe with realistic intermolecular potential is tested. The calculation are done on the fixed 0K temperature.

Void Fraction is a good characterization method for microporous crystals and have had great success in metal organic frameworks (MOFS), as demonstrated also by the team of supervisors.

In case of dens materials like the one we consider in this work, the void fraction should not be a good predictor. However we decided to include it in our tests in case the space occupied by the ion in the discharged material would impact our prediction, as will be discussed later. (REF)rewrite.

## 4.4 AP-RDF Descriptors of Electrode materials

Atomic property weighted radial distribution function (AP-RDF)?? was found to be a good predictor which also, when tested by the PCA(REF to theory part), exhibited good discrimination of geometrical and other properties, in one of their cases, gas uptake.

One of the methods found, that seemed to yield good predictions dependent on chemical properties where the Atomic property weighted radial distribution function, successfully used on MOFS. ?? Due to it looking reasonable we decided to try it out.

The radial Distribution Function(RDF) is the interatomic separation histogram representing the weighted probability of finding a pair of atoms separated by a given distance.(REF) In a crystalline solid, the RDF plot has an infinite number of sharp peaks where the separation and height are characteristic of the lattice structure. We used the minimum image convention (boundary condition)Do I need a ref here? and the RDF scores will be uniquely defined inside of the unit cell, per material-ID. The RDF can be expressed as:

$$RDF^{P}(R) = f \sum_{i,j}^{\text{all atom pairs}} P_{i}P_{j}e^{-B(r_{ij}-R)^{2}}$$

$$(4.4)$$

In our case the RDF scores in a electrode framework has been interpreted as the weighted probability distribution to find a atom pair in a spherical volume of radius R inside the unit cell according

to equation above. 4.4

Summing over all the atom pairs, where  $R_{ij}$  is the minimum image convention distance of these pairs, B is a smoothing parameter, and F is a scaling or normalization factor. Our Own approach to this is written in Fortran, and can be found in the appendix with an operational pdf.(REF)

The RDF can be weighted to fit the requirements of the chemical information to be represented, by introducing the atomic properties,  $P_i$  and  $P_j$ . We weighted the radial probabilities by three tabulated atomic properties namely electronegativity, polarizability, and Van der Waals volume, which gives us the AP-RDF. While a regular RDF function encodes geometric features, the atomic property weighted RDF additionally characterizes the chemical features within a material. An atomic property weighted RDF can be seen on the screen.

To test our method, we used it to reproduce the results for the two MOFS, namely *IRMOF-1* and *MIL-45* found in the article by Fernandez.??. We confirmed their findings .. though with drawback related to the size... which are flawed in our case. In our opinion, we think that this is a fundamental drawback, and the results depends on the size of the simulation cell(which can be made by replicating the unit cell).

INSERT BILDET AV PLOT AV AP-RDF.

## 4.5 Algorithm

First of all, a wrote a program for "scraping" the *materialsproject* webpage for batteries (0). This gave us the possibility to gather all the available resources on the batteries in the database in a fast and effective manor, as well as updating these CSV files of battery-IDs. (ref)

We then run a second program that downloads all the information on the materials that matches a material-ID correlated to a battery-ID(1,2). (ref) Before constructing a CIF file structured so that all the battery-IDs, charged-material-IDs, and dischargerd-material-IDs are correlated with the information on the charged and discharged properties.

After, the volumetric density fraction is calculated(3) and added to the main CSV file for both charged and discharged materials. While the CIF files are being processed for Poreblazer(4) where the void fraction is calculated(5,6).

Then we merge all our CSV files based on what properties that we are interested in and makes a CSV file called for\_ML.csv(7,8) that we feed into our random forest algorithm(9). We then run cross validation, MSE, and plot what we are interested in(10).

In addition we also tested for different machine learning algorithms, as mentioned (ref), but these were only to test the reliability of our model, and will be discussed in the discussion section (ref)

```
maybe add this in the appendix?
```

```
Algorithm:
Steps for use of python scripts:
        mp battery scraper.py
    Scrape batteries with a given working ion from the Materials Project battery explorer
(https://www.materialsproject.org/#search/batteries)
        fillproperties.py
    Download all materials that match a material id correlated to a battid.
        Output files: directory cif_info_dir/<material_id>_prop.dat
        add features.py
    Gets and adds the material specific features from the JSON dump to a csv.
        Output files: material properties.csv
        elements.py
    Calculate the density fractions for all materials.
3:
        Output files: out_csv_dis.csv
        for Poreblazer.pv
    Download the CIF files as JSON for all materials correlated to a battid.
        Output files: directory cif_for_poreblazer/<material_id>_cif.dat
        process_cif.py
    Extract the CIF information from the previous JSON data.
5:
        Output files: directory cif for poreblazer/cif files/<material id> cif.dat.csv
        process_cif.py
    Extract void fraction with poreblazer using the CIF files.
        Output files: helvol_geomvol.csv
        merger.py
    Merge charged and discharged for all properties
        Output files: allFiles.csv
        prep csv.py
    Select predictors and targets for ML
```

```
Output files: for_ML.csv

randomforest.py

9: Run randomforrest
    Output files: Depending on what being saved: ./Results/*

crossvalidation.py

10: Run cross-validation, remove outliers.

11: ????
```

#### Part IV

# Result & Discussion

#### 5 Result section title

MSE, PCA, R2, compair. Ordered by target:

Write a paragraph on how the "extra" entries affected the prediction result, and how you removed the once with less then 3-5 entries.

#### 5.1 Random factors from database.

- 5.1.1 Average Voltage
- 5.1.2 Capacity
- 5.1.3 Energy Density

## 5.2 Volumetric number density

Volumetric number density or n as described (section ref), are shown (Tablature ref), for the Liand Mg- databases. There are a couple of different results that are particularly interesting. First of all; n is overall better at predicting VC and with that GC naturally follows. In the first figure (??), the Mg-database, every prediction has a lower 'score' than in the Li-database. This is probably due to it being a much smaller database.

As can be seen clearly; the evaluations of this method is somewhat splitt. The MSE is generally better for the Li-database, and is best at the AV. The CV is better for the capacities but there is somewhat a high degree of uncertainty. This is probably due to the database being small. As expected the results for volumetric capacity is the peak of these runs.

One can from these results conclude that volumetric number density is worth bringing on as a predictor, as it clearly ha a part of the pusle.

$\frac{Target:\rightarrow}{Accuracy:\downarrow}$	AV	GC	VC	SE	ED
$R^2$ -score	0.5911	0.6815	0.6978	0.7103	0.5596
$R^2$ -train	0.9456	0.9279	0.9502	0.9241	0.9401
CV:	0.3180 (+/- 0.4977)	0.5423 (+/- 0.4435)	0.5943 (+/- 0.5877)	0.4494 (+/- 0.4608)	0.4755 (+/- 0.4464)
MSE:	0.4407	2491	41608	5284.5403	796956
CV-mean:	0.3076	0.5982	0.6511	0.4150	0.4700

Figure 9: Mg- prediction accuracy results on the Targets; Average Voltage(AV), gravimetric capacity(GV), volumetric capacity(VC), specific energy(SE), and energy density(ED). Each row showes the number representing that type of test, as included in section(REF).

$\frac{Target:\rightarrow}{Accuracy:\downarrow}$	AV	GC	VC	SE	ED
$R^2$ -score	0.3309	0.3867	0.5631	0.3796	0.4027
$R^2$ -train	0.9193	0.9261	0.9286	0.9179	0.9266
CV:	-10.0739 (+/- 7.0309))	0.5009 (+/- 0.1844)	0.6095 (+/- 0.2123)	0.0341 (+/- 1.6924)	0.0298 (+/- 2.0854)
MSE:	0.7683	3318	29971	45911	532777
CV-mean:	-10.4347	0.5200	0.6465	0.4107	0.5093

Figure 10: Li- prediction accuracy results on the Targets; Average Voltage(AV), gravimetric capacity(GV), volumetric capacity(VC), specific energy(SE), and energy density(ED). Each row showes the number representing that type of test, as included in section(REF).

## 5.2.1 Average Voltage

Mg db Charged:

Discharged: Mg db:

Li db:

#### 5.2.2 Capacity

# 5.2.3 Energy Density

#### 5.3 Void fraction

$\frac{Target:\rightarrow}{Accuracy:\downarrow}$	AV	GC	VC	SE	ED
$R^2$ -score	-0.0461	0.3426	0.3784	-0.0011	0.0838
$R^2$ -train	0.8676	0.8799	0.9052	0.8764	0.8786
CV:	-0.7976(+/- 1.3547)	0.1844 (+/- 0.2182)	0.2983 (+/- 0.3636)	-0.3742 (+/- 0.9904)	-0.1623 (+/- 0.7009)
MSE:	1.1457	4521	62785	92593	1613762
CV-mean:	-0.5899	0.1660	0.3166	-0.2962	-0.0398

Figure 11: Mg- prediction accuracy results on the Targets; Average Voltage(AV), gravimetric capacity(GV), volumetric capacity(VC), specific energy(SE), and energy density(ED). Each row showes the number representing that type of test, as included in section(REF).

#### **5.4** AP-RDF

PCA, R2, MSE.

$\frac{Target:\rightarrow}{Accuracy:\downarrow}$	AV	GC	VC	SE	ED
$R^2$ -score	-0.1031	0.0263	0.0159	-0.0857	-0.1346
$R^2$ -train	0.8529	0.8434	0.8530	0.8519	0.8471
CV:	-0.7544 (+/- 1.2666)	-0.0272 (+/- 0.1926)	0.0916 (+/- 0.1639)	-0.4965 (+/- 0.9204))	-0.2823 (+/- 0.6630)
MSE:	1.2888	6426	110679	100803	1775980
CV-mean:	-0.6110	-0.0109	0.0897	-0.4422	-0.1690

Figure 12: Mg- prediction accuracy results on the Targets; Average Voltage(AV), gravimetric capacity(GV), volumetric capacity(VC), specific energy(SE), and energy density(ED). Each row showes the number representing that type of test, as included in section(REF). With the AP-RDF as predictor.

# 5.5 Stability

This is a novel work, the aim is therefor to explore different predictors, by figuring out the different weights of the predictors on different targets, and which predictors that does not favorable for our predictions.

The model is decent at predicting; Gravimetric and Volumetric Capacity (87%), Specific Energy (70%), and Energy density (68%), but has no capability of predicting stability as of now. There is a need for ab initio calculations for several of our predictors, they calculate something that we know most definitely is correlated to the target without any premature calculations. This is something we are trying to move away from. As of now, only using the density fraction, we can get somewhere between 40% to 60% accuracy with our model.

This did not improve when including the void fraction, our predictions actually got worse.

AP-RDF - Still no good results! This is a struggle.

#### 5.6 Geometrical descriptors

These grafs all represent the accuracy of the predictions on the training data and on new data given to the machine, with only the number density as a predictor, and the Average voltage, Gravimetric capacity, Volumetric capacity, energy density, and physical stability for the discharged material, as targets (a-f)??. Most notably the predictions on the Average voltage, Gravimetric capacity, Volumetric capacity, energy density, and specific energy are all showing a decent amount of correlation, with around 60% accuracy. The physical stability for the discharged-,and the physical stability of the charged-materials show that there is no correlation between the number density and the physical stability. It is also shown that there is no correlation between the number density and the void fraction. Or any of the other properties for that matter.

# Part V

# Summary

- 6 Summary and future work
- 6.1 Batteries
- 6.2 future work
- 6.2.1 improving method

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