

+
✂
✎
🗑

💡
✓
↺
?

No elements selected

Select the elements from the list and add them to the canvas setting the appropriate attributes. Press **TAB** to get to the main menu.

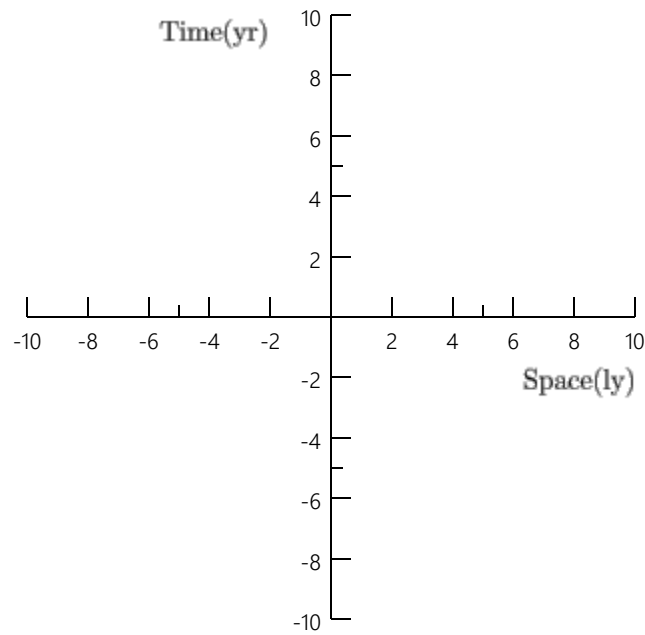
### Part C

Draw a worldline for Angela, who is traveling away from you at a speed of 100,000 km/s .

ANSWER:



No elements selected



Select the elements from the list and add them to the canvas setting the appropriate attributes. Press **TAB** to get to the main menu.

## Problem S3.53

Consider a spacetime diagram on which the vertical time axis is marked in seconds and the horizontal space axis is marked in light-seconds. Assume a worldline with a slope of  $27^\circ$  (from the horizontal).

### Part A

At what speed would an object have to be traveling to have this worldline?

**Express your answer to two significant figures and include the appropriate units.**

ANSWER:

$$v = 5.9 \times 10^8 \frac{\text{m}}{\text{s}}$$

**Correct**

### Part B

Can any object have this worldline?

ANSWER:

- ☒ no  
☐ yes

**Correct**

### Part C

What is the least possible slope of the worldline?

**Express your answer in degrees to two significant figures.**

ANSWER:

$$\phi_{\text{minimal}} = 45^\circ$$

**Correct**

---

### Problem S3.58

The Andromeda Galaxy is about 2.5 million light-years away. Suppose you had a spaceship that could constantly accelerate at  $a = 1.6\,g$ .

How long as the ship is gone from Earth for many years, the amount of time that passes on the spaceship during the trip is approximately:

$$t_{\text{ip}} = \frac{2c}{a} \ln\left(\frac{a \times D}{c^2}\right)$$

where  $D$  is the distance to the destination and  $\ln$  stands for the natural logarithm (which you can calculate with the "ln" key on most scientific calculators). If  $D$  is in light-years,  $g = 9.8\,\text{m/s}^2$ , and  $c = 3 \times 10^8\,\text{m/s}$ , the answer will be in units of seconds.

---

#### Part A

Could you go to the Andromeda Galaxy and come back within your lifetime?

ANSWER:

☐ no☒ yes**Correct**

---

#### Part B

How long would that trip last for you?

**Express your answer in years to two significant figures.**

ANSWER:

$$t_{\text{personal}} = 37 \text{ yr}$$

**Answer Requested**

### Part C

How many time would pass on Earth?

**Express your answer in years to two significant figures.**

ANSWER:

$$t_{\text{Earth}} = 5.0 \times 10^6 \text{ yr}$$

**Answer Requested**

### Problem S3.59

In a relatively weak gravitational field, such as that of a planet or an ordinary star, the following formula tells us the fractional amount of gravitational time dilation at a distance  $r$  from the center of an object of mass  $M_{\text{object}}$ :

$$\frac{1}{c^2} \times \frac{GM_{\text{object}}}{r}$$

$= 6.67 \times 10^{-11} \text{ m}^3/(\text{kg} \times \text{s}^2); c = 3 \times 10^8 \text{ m/s.}$  For example, while 1 hour passes in deep space far from the object, the amount of time that passes at a distance  $r$  is 1 hour minus 1 hour multiplied by the factor above. (This formula does *not* apply to strong gravitational fields, like those near black holes.)

### Part A

Calculate the amount of time that passes on Earth's surface while 3.0 hour passes in deep space.

**Express your answer in seconds to three significant figures.**

ANSWER: