HIGHLY ACCURATE LINEAR CLASSIFIER WITH APPLICATIONS IN HEALTH INSURANCE COVERAGE

Songkomkrit Chaiyakan

A Dissertation Submitted in Partial Fulfillment of the Requirements

for the Degree of Doctor of Philosophy Program

in Business Analytics and Data Science

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This work proposes a multiclass box classifier both theoretically and empirically

proven to produce the highest training accuracy through the rigorous formulation of 0-1

mixed integer programming problem. It can also determine significant factors. Unlike a

decision tree classifier well-known for simplicity and fast execution, the proposed classifier

has control over a maximal number of features of interest, whether continuous or categorical,

and a number of splitting values on all features. The use of this method is illustrated on

2020 Current Population Survey (CPS) Annual Social and Economic Supplement (ASEC)

health insurance dataset with, as a result of the exponential time complexity of the model,

only three independent variables univariately preselected by the SelectKBest technique.

Compared to decision tree classifiers of different depths, the proposed classification model

can keep a balance between the number of total splitting values and the number of decision

boxes, and it achieves a relatively high training accuracy at the expense of significantly high

computational time and storage usage. Nonetheless, both give the same set of contributing

factors. The fast algorithm of decision box merging is also suggested when the number of

selected features can be further reduced after optimization.

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Nomenclature

$ ilde{d}$	full dimension of given training instances
d	number of both continuous and categorical features of interest
d_{cat}	number of categorical features of interest
$ ilde{\mathcal{C}}_{\mathrm{cont}}$	index set of given continuous features
$ ilde{\mathcal{C}}_{\mathrm{cat}}$	index set of given categorical features
$\mathcal{C}_{\mathrm{cont}}$	index set of new continuous features before optimization
$\mathcal{C}_{\mathrm{cat}}$	index set of intermediate categorical features before optimization
$ ilde{x}^i$	given training instance i
x^i	training instance i as a classifier input of lower continuous and full
	categorical dimensions
x^i_j	value of feature j of instance x^i
y_k^i	whether a given instance \tilde{x}^i is in class k
$c_{j, ilde{j}}$	whether a new continuous feature j comes from an original continuous
	feature \tilde{j}
f_j	whether categorical feature j is selected or, equivalently, significant
p_{j}	number of splitting values on feature j
$b_{j,q}$	q^{th} splitting value on continuous feature j
u_j	new group labels on categorical feature j
v_{j,x^i_j}	new group label of instance \boldsymbol{x}_j^i on categorical feature j
B	number of total decision boxes
S_{eta}	$\beta^{ ext{th}}$ decision box
$lpha^i_{j,q}$	whether x_j^i is in open interval $(b_{j,q}, b_{j,q+1})$
M	sufficiently large positive number
m_{j}	sufficiently small positive number on feature j that can distinguish
	individual feature values of x_j^i
$l^i_{j,q}$	$lpha_{j,q}^i(b_{j,q}+m_j)$
$r^i_{j,q}$	$\alpha_{j,q}^i(b_{j,q+1}-m_j)$
γ^i_eta	whether instance x_j^i is in decision box S_{β}
Θ_{eta}	set of most frequent classes in decision box S_{β}
h_{eta}	negative value of number of correctly classified training instances

CHAPTER I

INTRODUCTION

Social science research heavily relies on the traditional use of logistic regression or structural equation modeling (SEM) to explore or confirm the linkage between multiple factors with the ultimate goal of causal explanation. In addition to the significance test of coefficients, the utilization of mediators, moderators, confounders and covariates provides the convincing magnitude and direction of estimated effects. On the rare occasion of classification with numerous independent variables measured on nominal scales, the excessive number of required dummy variables nevertheless imposes a limitation on these two approaches.

To address this problem, classification algorithms in machine learning are used to identify key characteristics of a separate group despite lack of important statistical tests. For example, a decision tree constructs a set of rules individually formed by minimal attributes to fully describe a training data, and a neural network employs a hidden layer to account for nonlinear interaction between attributes and therefore increases model accuracy. The first maximizes an information gain, whereas the latter minimizes a residual sum of square. Both objective functions are usually smooth and enable real-time data processing.

Despite their advantage, a decision tree and a neural network may provide undesirable inaccuracy. As a result, a linear classifier developed from conventional support vector machine (SVM) through the application of 0-1 mixed integer linear programming (MILP) will be proposed in the dissertation to ensure maximum accuracy without overfitting. In this case, external testing seems redundant unless a training data contains an outlier. As early-stage research, the classifier will serve no purpose of real-time analytics. This modified approach will be adopted for illustrative purposes to examine contributing factors on coverage types of health insurance in the United States in 2019.

1.1 Objectives

- 1. To propose a linear multiclass classifier that yields high training accuracy.
- 2. To apply the proposed classification method to investigate significant factors influencing health insurance coverage.

1.2 Limitations

- 1. A nonlinear classifier is beyond the scope of the study. However, a suitable kernel function may be selected to solve a nonlinear classification problem.
- 2. An entire data is used to train a linear classifier. Hence, only training accuracy is measured.
- 3. The health insurance sample data only includes Americans. It was collected in 2020 to reflect health insurance coverage for entire calendar year 2019.
- 4. Despite its high training accuracy, the proposed classifier requires long training time and large space to store a branch-and-cut tree. Its approximation algorithm is not developed in this dissertation although mitigating both problems to some extent.

CHAPTER II

LITERATURE REVIEW

2.1 Health Insurance Coverage

A variety of statistical tools have long been used to study the factors related to health insurance coverage of multiple subpopulations across different countries. These analytical techniques include linear probability modeling (Cebula, 2006), probit regression analysis (Mulenga et al., 2021) and logistic regression analysis (Jin et al., 2016; Dolinsky and Caputo, 1997; Markowitz et al., 1991).

Generally, health insurance coverage across the U.S. states was positively associated with median family income, female labor force rate, the proportion of population aged 65 and over, and it was negatively linked with the percentages of household with husband absence and Hispanic household (Cebula, 2006). Psychological characteristics also greatly affected the influence of demographic factors among American women (Dolinsky and Caputo, 1997). After controlling for psychological variables, health status and employment were significant determinants only for married and unmarried women respectively. Income and education played important roles in both groups. Americans aged 18 to 24 with permanent, full-time employment were more likely to be insured than those with permanent, part-time employment (Markowitz et al., 1991). This trend became reverse specifically for the students. Low income, less education, rural residence, unmarried status, Hispanic ethnicity and Western residency were indicators of being uninsured in general.

Outside the United States, many research works on health insurance coverage have also been of interest. Income, education, health status and employment correlated with the coverage types among Chinese people aged 45 and over (Jin et al., 2016). Males dominated in both public and private health insurance. Migrants appeared to be covered by both rural and urban public insurance, private insurance or no insurance in comparison to local residents. Rural residents were more inclined to have public insurance coverage. Furthermore, private health insurance in Zambia tended to be purchased by males with service, skilled and unskilled occupations and rural residency as well as women in marital union and clerical duties (Mulenga et al., 2021).

2.2 Feature Selection

2.2.1 Decision Tree

Each parent node partitions a feature space by splitting a specific training variable into two intervals, left and right nodes (Scikit-learn, 2024). A splitting value is chosen to minimize the weighted average of the impurities of both child nodes by their number of training instances. This dissertation uses as an impurity measure the Gini index defined by the probability of a sample at a node being wrongly classified.

2.2.2 SelectKBest

The mutual information (Cover and Thomas, 2005) is a statistic for measuring relationship between two random variables or in practice two datasets.

Definition 2.1. The Kullback-Leibler distance D(f||g) between two densities f and g is defined by

$$D(f||g) = \int f \log \frac{f}{g}.$$

Definition 2.2. The mutual information I(X;Y) between two random variables with joint density f(x,y) is defined as

$$I(X;Y) = D(f(x,y)||f(x)f(y)).$$

Two random variables share no mutual information, i.e. I = 0, only when both are independent. Suppose X is a training variable and Y a discrete target or class. A continuous feature requires an estimation of mutual information, for example by the k-nearest neighbor method (Ross, 2014), because its true probability remains practically unknown. Suppose the k-nearest neighbor of a training instance x^i of the same class has m_i instances of all classes and there are N_i out of N that share the same class with x^i . Compute

$$I_i = \psi(N) - \psi(N_i) + \psi(k) - \psi(m_i)$$

where the digamma function ψ is the logarithmic derivative of the gamma function. The mutual information I(X;Y) is estimated by averaging I_i over all training instances.

Definition 2.3. The gamma function Γ and digamma function ψ are defined on the set of positive real numbers by

$$\Gamma(z) = \int\limits_0^\infty t^{z-1} e^{-t} dt$$

and

$$\psi(z) = \frac{d}{dz} \log \Gamma(z)$$

respectively.

CHAPTER III

RESEARCH METHODS

3.1 Overview

- 1. Propose a multiclass linear classifier which is able to predict continuous contributing factors, produces disconnected decision regions and provides minimum misclassification.
- 2. Extend the classifier when certain features of training data are allowed to be categorical.
 - 3. Illustrate the use of the methods on the health insurance dataset.
 - 4. Compare multiple facets of results with the use of a decision tree.

3.2 SSH Key Generation

The Secure Shell (SSH) protocol is employed for secure connection to a remote compute engine through one-way client authentication by a pair of asymmetric keys: private and public. SSH keys can be generated with the OpenSSH command ssh-keygen by using a native SSL/TLS library provided by an operating system: Secure Channel (Schannel) in Windows or OpenSSL in Linux. The latter keys are very specific to a currently active OpenSSL version especially when an alternative OpenSSL is manually built and installed. In this dissertation, the SSH keys are created on a local computer with the elliptic-curve Ed25519 algorithm (Bernstein et al., 2012), proven to be faster and more efficient than the RSA algorithm (Rivest et al., 1978).

```
cd ~/.ssh
ssh-keygen -f <output_keyfile> -C <comment> -t ed25519
```

A Google Cloud virtual machine requires the comment at the end of a public key file to be a Google username. Since the dissertation results are uploaded to a GitHub repository using SSH, an additional key pair specific to this purpose is suggested to tighten security. A host, a username and their private key must be included in the configuration file ~/.ssh/config in the case of multiple key pairs.

```
Host <hostname>
   User <username>
   IdentityFile <private_keyfile>
```

Unlike Windows, Linux has the .ssh directory hidden, directly by the use of a dot character at the beginning, and partially inheritable POSIX access control list (ACL). A Linux parent directory does not reapply its new ACL to existing descendants, and it simply acts as during path resolution a gate with its execute permission.

The principle of least privilege (PoLP) should be applied to generated keys. Basically, only a key owner can read his/her private key, and the read-only permission on a public key is granted to everyone. In Linux, there are three POSIX permission levels: owner, group and other. Each level is represented by three permission bits: read (r), write(w) and execute (x). They are usually rewritten in base 10, ranging from 0 to 7. The chmod command is used to set all three levels of permission with three numerical digits.

```
chmod 400 <private_key>
chmod 444 <public_key>
```

In Windows, the command icalcs is used, and additional rights can be denied due to more fine-grained permission control as displayed in Table 3.1. An SSH key should be hidden and have no inherited NTFS permission. Its ownership is nontransferable. A SYSTEM account has no access to a private key. An Administrators group can only read, but neither change nor delete, its content, regular and extended attributes, and permissions. This set of access privileges is also applicable to a public key and granted to everyone.

Permission	Description
WD	Write data or add file
AD	Append data or add subdirectory
WA	Write attributes
WEA	Write extended attributes

Write DAC (change permissions)

Write data or add file

Delete

Table 3.1: Example of advanced NTFS permissions in Windows

3.3 Remote Virtual Machine Setup

DE

WDAC

WD

3.3.1 Specifications

All codes are executed on a Google Cloud compute engine with a 64-bit 8-vCPU 4-core CPU, 64 GB RAM and 250 GB SSD persistent disk running on Ubuntu Server 24.04 LTS. The instance locates in region us-central1 (Iowa) and zone us-central1-f. The standard provisioning model, although noticeably more high-priced than the spot counterpart, is chosen to prevent VM preemption primarily because the proposed classifier has exponential time complexity, thereby requiring exceptionally high CPU utilization. The network traffic is routed in a premium tier to provide low latency. A static external IPv4 address is reserved and assigned to the instance for remote connection.

3.3.2 SSH Key-Based Authentication

Password authentication should be disabled by uncommenting the following line in the SSH configuration file /etc/ssh/sshd_config.

PasswordAuthentication no

SSH authentication requires adding a public key of a local computer to the key file /.ssh /authorized_keys.

```
echo <public_keyfile> >> ~/.ssh/authorized_keys
```

3.3.3 Python Installation

Ubuntu Server 24.04 LTS is equipped with outdated Python 3.12.3. The installation of latest Python 3.13.0 at the current stage inevitably requires building from source. As opposed to Python 3.12, Python 3.13 experimentally supports multithreading without global interpreter lock (GIL). However, disabling GIL prevents the successful installation of scikit-learn package which is required to build a decision tree in Chapter 5. In this circumstance, the binary distribution, commonly known as wheel, of scikit-learn is unavailable. Its compilation by Rust and Cargo with the build system requirements specified in pyproject.toml also fails. Therefore, GIL remains as a default mechanism of mutual exclusion lock.

3.3.3.1 Introduction to Compilation in C

All Python source codes are written in C, and they require a C compiler such as GNU Compiler Collection (GCC) and Clang/Low Level Virtual Machine (LLVM). This dissertation chooses the first compiler. GCC 13 can be installed through the APT package manager.

```
sudo apt install build-essential
```

A newer version of GCC, currently GCC 14 release and GCC 15 experimental, can optionally be built from source by its previous version. The C/C++ compiler commands, including versions, and flags can be added to the environment variables CC, CXX, CFLAGS and CXXFLAGS respectively.

GNU Make is used as a build automation tool by reading instructions from Makefile. Parallelism is supported by utilizing multiple CPU threads with the -j or --jobs flag.

```
make -j<N>
make -j<N> install
```

The parameter <N> is the maximum allowable number of jobs executed in parallel which should not exceed the number of available CPU threads.

3.3.3.2 Basic Object Types

Python object structures are declared in the header file Include/object.h. A Python object is stored in memory, it has a C structure named _object, and it can be referenced as a PyObject* pointer. With GIL enabled by default, it declares a reference counter ob_refcnt of type Py_ssize_t and a pointer to the object type *ob_type of type PyTypeObject. When GIL is disabled by configuring Python with the --disable-gil option, a local reference counter is declared by ob_ref_local of type uint32_t is only adjusted by an owner thread, whereas a shared counterpart ob_ref_shared of type Py_ssize_t is adjusted by remaining threads. Its actual reference counter can be computed by merging both. When its reference counter is decremented to zero, it is deleted by a garbage collector (GC). If it only has a cyclic reference, a generational garbage collection is employed. A variable-size Python object can be cast further to PyVarObject* with an additional field ob_size of type Py_ssize_t which holds the number of its items.

```
#ifndef Py_GIL_DISABLED
struct _object {
   #if (defined(__GNUC__) || defined(__clang__)) \
   && !(defined __STDC_VERSION__ && __STDC_VERSION__ >= 201112L)
   // On C99 and older, anonymous union is a GCC and clang extension
   __extension__
   #endif
   #ifdef _MSC_VER
   // Ignore MSC warning C4201: "nonstandard extension used:
   // nameless struct/union"
   __pragma(warning(push))
   __pragma(warning(disable: 4201))
   #endif
   union {
       Py_ssize_t ob_refcnt;
       #if SIZEOF_VOID_P > 4
       PY_UINT32_T ob_refcnt_split[2];
       #endif
   };
   #ifdef _MSC_VER
   __pragma(warning(pop))
   #endif
```

```
PyTypeObject *ob_type;
};
#else
// Objects that are not owned by any thread use a thread id (tid) of
   zero.
// This includes both immortal objects and objects whose reference
   count
// fields have been merged.
#define _Py_UNOWNED_TID 0
// The shared reference count uses the two least-significant bits to
   store
// flags. The remaining bits are used to store the reference count.
#define _Py_REF_SHARED_SHIFT 2
#define _Py_REF_SHARED_FLAG_MASK 0x3
// The shared flags are initialized to zero.
#define _Py_REF_SHARED_INIT 0x0
#define _Py_REF_MAYBE_WEAKREF 0x1
#define _Py_REF_QUEUED 0x2
#define _Py_REF_MERGED 0x3
// Create a shared field from a refcnt and desired flags
#define _Py_REF_SHARED(refcnt, flags) (((refcnt) <<</pre>
   _Py_REF_SHARED_SHIFT) + (flags))
struct _object {
   // ob_tid stores the thread id (or zero). It is also used by the
       GC and the
   // trashcan mechanism as a linked list pointer and by the GC to
       store the
   // computed "gc_refs" refcount.
   uintptr_t ob_tid;
   uint16_t _padding;
   PyMutex ob_mutex; // per-object lock
```

```
uint8_t ob_gc_bits; // gc-related state
uint32_t ob_ref_local; // local reference count
Py_ssize_t ob_ref_shared; // shared (atomic) reference count
PyTypeObject *ob_type;
};
#endif

/* Cast argument to PyObject* type. */
#define _PyObject_CAST(op) _Py_CAST(PyObject*, (op))

typedef struct {
    PyObject ob_base;
    Py_ssize_t ob_size; /* Number of items in variable part */
} PyVarObject;
```

3.3.3.3 String Interning

Python interns strings, which are immutable objects, of the same value mainly through the function _PyUnicode_InternInPlace() defined in the source file Objects/unicodeobject.c by retaining only one copy in memory. This reduces memory usage and speeds up certain operations, for example equality comparison. The reference to all interned strings is stored in the per-interpreter dictionary interned initialized during the first invocation. As opposed to a release build, a debug build denies with an assertion the addition of a process-global interned string into the existing dictionary to prevent the possibility of getting a duplicate.

```
static /* non-null */ PyObject*
intern_static(PyInterpreterState *interp, PyObject *s /* stolen */)
{
    // Note that this steals a reference to `s`, but in many cases
        that
    // stolen ref is returned, requiring no decref/incref.

assert(s != NULL);
assert(_PyUnicode_CHECK(s));
assert(_PyUnicode_CHECK(s).statically_allocated);
assert(!PyUnicode_CHECK_INTERNED(s));
```

```
/* We must not add process-global interned string if there's
       already a
   * per-interpreter interned_dict, which might contain duplicates.
   */
   PyObject *interned = get_interned_dict(interp);
   assert(interned == NULL);
   #endif
   /* Look in the global cache first. */
   PyObject *r = (PyObject *)_Py_hashtable_get(INTERNED_STRINGS, s);
   /* We should only init each string once */
   assert(r == NULL);
   /* but just in case (for the non-debug build), handle this */
   if (r != NULL && r != s) {
       assert(_PyUnicode_STATE(r).interned ==
          SSTATE_INTERNED_IMMORTAL_STATIC);
       assert(_PyUnicode_CHECK(r));
       Py_DECREF(s);
       return Py_NewRef(r);
   }
   if (_Py_hashtable_set(INTERNED_STRINGS, s, s) < -1) {</pre>
       Py_FatalError("failed to intern static string");
   }
   _PyUnicode_STATE(s).interned = SSTATE_INTERNED_IMMORTAL_STATIC;
   return s;
}
```

Soon after Python 3.13.0 had been released, JupyterLab could not be launched in the debug build despite its successful installation. This problem can be fixed by commenting the following assert statement, though discouraged, and rebuilding the Python.

```
//assert(interned == NULL);
```

#ifdef Py_DEBUG

This can also be done by using the sed command.

```
sed -i -e \
   's/assert(interned == NULL);/\/\assert(interned == NULL);/g' \
   Objects/unicodeobject.c
```

However, the source code modification is not required for running the latest JupyterLab.

3.3.3.4 Configuration and Build

It is recommended to have three separate directories: source, build and install. In this dissertation, Python is built against OpenSSL whose runtime library directory rpath is automatically detected, and it respects the OpenSSL crypto policy openssl.cnf by overriding the default Python cipher list.

```
--with-openssl=<openssl_rootdir>
--with-openssl-rpath=auto
--with-ssl-default-suites=openssl
```

As opposed to the built-in Python, a static library (with .a extension) is built from source by default. This dissertation builds a dynamic library (with .so extension) by adding the --enable-shared flag to minimize disk footprint of several programs because Python 3.13.0 will intentionally be built as a new primary version, but inside a home directory without a symbolic link to the system Python binary located in /usr/bin shared by multiple native applications.

Although a release build, default in Python, is more optimized but harder to debug, this dissertation chooses the Python debug build by passing the --with-pydebug flag. The source codes are compiled to intermediate object codes in an attempt to reduce the code size and execution time. A linker produces shared libraries and executables from objects without duplicate definitions. Both compilation and linking are optimized by turning on the --enable-optimizations and --with-lto flags. C assertions are enabled in debug mode by default. Python can be compiled with profiling turned on by using the --enable-profiling flag. The GNU profiler grpof collects data during Python execution and outputs the file gmon.out in a current working directory. Based on this information, the code performance can be analyzed in terms of execution time and memory comsumption, and its bottleneck is identifiable. Nonetheless, this dissertation omits the profiling flag.

Python optimization, if specified, is profile-guided (PGO) based on collected data from sequential test runs. For the PGO generation task, Python by default uses the following arguments assigned to the environment variable PROFILE_TASK.

-m test --pgo --timeout=

The -m flag searches for all files matching a given pattern, in this case test* in the Lib/test subdirectory. The --pgo flag enables PGO training and selects 44 out of 478 test runs. Python 3.13 sets no timeout for an individual test, in contrast to Python 3.12 a default timeout of 20 minutes, and no longer ignores a test failure. Its build time is partly impacted by these test runs and can significantly improve by ignoring through the -i flag time-consuming tests which can be detected, for instance, by setting a custom timeout. This dissertation excludes the test for embedding APIs located at Lib/test/test_embded.py and sets a timeout of 5 minutes.

No timeout error is raised, and all remaining 43 tests pass.

Furthermore, the pyexpat module can be built using an installed expat library by the --with-system-expat flag. DTrace, Valgrind and loadable extensions in the _sqlite extension module are supported by the --with-dtrace, --with-valgrind and --enable -loadable-sqlite-extensions flags. Address sanitizer (ASAN) and memory sanitizer (MSAN) are disabled by default. Certain flags requires additional dependencies. Their environment variables for C compiler and linker flags, required libraries, Python modules to be optionally built, and corresponding APT packages are given in Table 3.2.

Table 3.2: Python options for third-party dependencies

Environment Variables	Library	Module	APT Package
BZIP2_[LIBS CFLAGS]	libbz2	bz2	libbz2-dev
CURSES_[LIBS CFLAGS]	libncurses	curses	libncurses-dev
GDBM_[LIBS CFLAGS]	gdbm		libgdbm-compat-dev
LIBB2_[LIBS CFLAGS]	libb2	hashlib	libb2-dev
LIBEDIT_[LIBS CFLAGS]	libedit	readline	libreadline-dev
LIBFFI_[LIBS CFLAGS]	libffi	ctypes	libffi-dev
LIBMPDEC_[LIBS CFLAGS]	libmpdec	decimal	
LIBLZMA_[LIBS CFLAGS]	liblzma	lzma	liblzma-dev
LIBREADLINE_[LIBS CFLAGS]	libreadline	readline	libreadline-dev
LIBSQLITE3_[LIBS CFLAGS]	libsqlite3	sqlite3	libsqlite3-dev
LIBUUID_[LIBS CFLAGS]	libuuid	uuid	uuid-dev
PANEL_[LIBS CFLAGS]	libpanel	curses.panel	libpanel-dev

Table 3.2: Python options for third-party dependencies (continued)

Environment Variables	Library	Module	APT Package	
TCLTK_[LIBS CFLAGS]	TCLTK		tk-dev	
ZLIB_[LIBS CFLAGS]	libzlib	gzip	zlib1g-dev	

After Python is completely installed in the destination directory, both source and build directories can be removed. The bin directory should be added to the PATH so that the executables are accessible from any location. The system environment variables LD_LIBRARY_PATH and LDFLAGS should include the lib directory so that the library code can be loaded into memory at runtime and compile time respectively. The recently built version must precede the system-wide version.

```
export PATH="<install_dir>/bin:$PATH"
export LD_LIBRARY_PATH="<install_dir>/lib:${LD_LIBRARY_PATH}"
export LDFLAGS="-L<install_dir>/lib $LDFLAGS"
```

This migration should be made to the Bash configuration file ~/.bashrc. Depreciation warnings may be emitted during runtime, but they can be suppressed by setting the Python environment variable PYTHONWARNINGS.

```
export PYTHONWARNINGS="ignore::DeprecationWarning"
```

The changes are not applied until the configuration file is reread.

```
source ~/.bashrc
```

3.3.4 Backup to OCI Object Storage

3.3.4.1 Introduction to OCI

Oracle Cloud Infrastructure (OCI) basically has two logical concepts of organization management: tenancy and compartment. A tenancy is a root container for administering cloud resources. During the signup process, a parent tenancy is provisioned and tied to a specified, unchangeable home region which is ap-singapore-1 in this dissertation. Multiple child tenancies can be created and managed by the parent tenancy. A compartment belongs to a tenancy, controls access to cloud resources, supports up to six levels, and brings clearer separation. It must be specified when a resource is created. A tenancy can be considered as a root compartment.

The OCI command line interface (CLI) can be installed by the oci-cli package in an isolated Python environment to prevent dependency conflicts. The source command is used to activate this environment. After the installation finishes, the executables including oci and its libraries are in the bin and lib directories. Only the first is additionally added to the PATH so that the oci command can be executed in the global environment, not limited to the virtual counterpart.

```
~$ python3 -m venv <env_dir>
~$ source <env_dir>/bin/activate
(env_dir)$ pip3 install oci-cli
(env_dir)$ deactivate
```

Before accessing an OCI resource or service, a basic OCI configuration must be made in an interactive mode from a terminal, for instance.

```
oci setup config
```

This can also be done from a custom configuration file by setting the environment variable OCI_CLI_RC_FILE to its full path. The file has two main components: section and key. A section except the default should be specified via the --profile option in the CLI.

```
[DEFAULT]
user=<user>
fingerprint=<fingerprint>
key_file=<key_file>
tenancy=<tenancy>
region=ap-singapore-1
```

3.3.4.2 OCI Object Storage

An object storage namespace serves as the top-level container for all buckets and objects, it is unique to a tenant, and it spans all compartments within a region. Although region-specific, its name remains the same across all regions. An object is any type of data along with its metadata stored in a logical container called bucket unique in a namespace. Object storage is highly scalable, cost-effective and structurally flat, compared to block and file storage. There are two default tiers. A standard tier has a higher cost and no retention period. In a low-cost archive tier, an object must be retained for at least 90 days, and restoration takes very long time to retrieve all data bytes. OCI Object storage supports auto-tiering, object versioning and multipart uploading which is greatly resilient for a very large object. Uncommitted of failed multipart uploads can be cleaned either manually or through a predefined lifecycle policy rule.

In this dissertation, only a full backup of scripts and results, not only due to its small size but also to avoid the possibility of a corrupted incremental or differential backup, is stored in OCI object storage. A total of 20 GB in all tenancies is always free, and no upgrade to a paid account is required. A bucket is created without auto-tiering and versioning. All buckets in a compartment can be listed along with their namespace.

```
oci os bucket list -c <compartment_id>
```

A backup is performed by a one-way synchronization, and each version is uniquely identified by an object prefix such as a timestamp. An object that exists in a destination but not in a source is deleted.

```
oci os object sync -ns <namespace> -bn <bucket> \
    --prefix <obj_prefix> --src-dir <src_dir> --delete
```

Furthermore, an object can be renamed and deleted where bulk deletion is also permitted.

```
oci os object rename -ns <namespace> -bn <bucket> \
    --name <obj_name> --new-name <obj_new_name>
oci os object delete -ns <namespace> -bn <bucket> \
    --name <obj_name>
oci os object bulk-delete -ns <namespace> -bn <bucket> \
    --prefix <obj_prefix>
```

3.4 GitHub Repository

The template GitHub repository for this dissertation is available at https://github.com/songkomkrit/phd-template. The basic Git commands are included in Table 3.3. The path to the Git global configuration file .gitconfig specific to a user is given by the environment variable GIT_CONFIG_GLOBAL. The username and the email address can be set up either by the git config command with the --global option or by editing the configuration file.

```
git config --global user.name <username>
git config --global user.email <email_address>
```

The following settings should appear in the file.

```
[user]
  name = <username>
  email = <email_address>
```

Table 3.3: Basic Git commands

Command	Description
git clone	Clean copy
git pull	Update with local changes kept
git resethard	Update with local changes discarded
git clean -fdx	Clean with untracked files and directories removed
git push	Remote update with local commits

The JSON-format metadata of both independent and dependent variables are at Data /Original/metadata/meta-indep.json and Data/Original/metadata/meta-dep.json. The health insurance in SAS7BDAT format is omitted, but its feather file of smaller size is already included in the directory Data/Original/feature. This dissertation further limits the number of participants and features to smaller size before fed to a classification model. Since data sampling is random, the sample is put in the directory Samples/cplex.

The box classifier proposed in Chapter 4 is located in the CPLEX Optimization Programming Language (OPL) project Projects/box where its input subdirectory contains a sample data including additional information and its output counterpart all relevant results such as splitting values and predicted class label per decision box. The model can be executed by the oplrun command and logged into file and on console by the tee command.

```
oplrun -p cproject_dir> 2>&1 | tee <log_file>
```

The project_dir> is Projects/box. Thanks to its comparative low-resource consumption,
using the oplrun executable in a terminal is preferred to starting the CPLEX Studio IDE
by executing the oplide command. The manual backup of the CPLEX engine log is stored
in the directory Logs/box. The Python scripts for data preprocessing, decision tree building
and decision box merging can be found in Scripts/Preprocessing/Python, Scripts/ML/
Python and Scripts/Box/Python respectively. The directory and file tree structures can
be printed in terminal by using the tree command, and they are saved to Structures/
directory.txt and Structures/file.txt.

```
tree -d . > Structures/directory.txt
tree -f . > Structures/file.txt
```

There are currently 29 directories and 60 files. The directory structure is displayed in Figure 3.1.

The template repository is very minimal with merely output files generated by a CPLEX optimizer. Its main purpose is to allow users to generate a new repository with the same structure before further Python execution such as exploratory data analysis (EDA). The up-to-date repository based on the template with additional outputs included is available at https://github.com/songkomkrit/phd.

Figure 3.1: Directory tree structure of the template GitHub repository



3.5 Health Insurance Dataset

3.5.1 Background

The 2020 U.S. Census Bureau's Current Population Survey (CPS) Annual Social and Economic Supplement (ASEC) dataset will be used in the dissertation. Questions were asked for the information on a previous calendar year. Therefore, the person-level dataset provides the estimates of individual health insurance coverage for calendar year 2019.

An individual may simultaneously have different coverages. Private health insurance includes an employment-based plan and a direct-purchase plan. Public health insurance comprises Medicare, means-tested coverage (i.e., Medicaid, Peace Church Health Insurance or PCHIP and others), military healthcare (i.e., TRICARE formerly known as Civilian Health and Medical Program of the Uniformed Services or CHAMPUS, Civilian Health and Medical Program of the Department of Veterans Affairs or CHAMPVA and Veterans Affairs or VA) and the combination of Indian Health Service (IHS) and other coverages. Those who only have IHS are considered uninsured.

Since there are in total 10 subtypes of insurance coverage, quantitative data analysis may involve up to $2^{10} + 1 = 1,025$ possible classes. In fact, the maximum number of subtypes of an overall class can be determined by the total sum of the indicator variables of the first ten subtypes. Furthermore, the dataset has at least 150,000 records and 750 attributes which are mostly measured on nominal scales. In addition to their allocation and topcode flags, the dataset variables cover a broad spectrum of characteristics: demographics, work experience, income (i.e., earnings, other income, non-cash benefits and tax), poverty, health insurance (i.e., government, private, employment-based, direct-purchase, subsidized marketplace, unsubsidized marketplace, non-marketplace, Medicaid, other means-tested, PHCIP, Medicare, IHS, TRICARE, CHAMPVA, VA and employer-sponsored), health status and migration. They also include basic CPS items (i.e., labor force and earnings) and medical out-of-pocket (OOP) expenditures.

3.5.2 Scope of Study

Within existing conceptual frameworks, certain independent variables will be preselected in the dissertation before further investigation. A group of infant born after the calendar year is excluded in the analysis. The combination of three following coverages is merely considered: employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB). There are eight possible binary tuples (GRP, DIR, PUB) which are regrouped into five following classes in Table 3.4.

Class	Code	Combination of insurance coverages					
Class	Code	GRP	DIR	PUB			
0	NNN	No	No	No			
1	NNY	No	No	Yes			
2	NY_	No	Yes	Yes			
		No	Yes	No			
3	YNN	Yes	No	No			
4	Y1Y	Yes	No	Yes			
		Yes	Yes	Yes			
		Yes	Yes	No			

Table 3.4: Class codes of insurance coverage combination

3.5.3 Metadata

Metadata 3.1 and 3.2 contain related information on dependent and independent variables in JSON format with a variable symbol as a main key and all of the following as its informative value in dictionary format: label, universe, type (either continuous or categorical), topic, subtopic and possible values including NIU (not in universe).

Metadata 3.1: Dependent variables (data/original/metadata/meta-dep.json)

```
1 {
2    "NOW_COV": {
3         "label": "Currently covered by health insurance coverage",
```

```
4
           "universe": "All Persons",
5
           "type": "Categorical",
           "role": "Dependent",
6
           "topic": "Health insurance",
7
8
           "subtopic": "Any health insurance coverage",
           "values": {
9
               "1": "Yes",
10
               "2": "No"
11
12
           }
       },
13
       "NOW_PUB": {
14
15
           "label": "Current public coverage",
           "universe": "All Persons",
16
           "type": "Categorical",
17
           "role": "Dependent",
18
           "topic": "Health insurance",
19
           "subtopic": "Public coverage",
20
           "values": {
21
               "1": "Yes",
22
               "2": "No"
23
           }
24
25
       },
       "NOW_PRIV": {
26
27
           "label": "Current private coverage",
           "universe": "All Persons",
28
           "type": "Categorical",
29
30
           "role": "Dependent",
           "topic": "Health insurance",
31
32
           "subtopic": "Private coverage",
           "values": {
33
               "1": "Yes",
34
35
               "2": "No"
           }
36
       },
37
       "NOW_GRP": {
38
           "label": "Any current employment-based coverage",
39
```

```
"universe": "All Persons",
40
           "type": "Categorical",
41
42
           "role": "Dependent",
           "topic": "Health insurance",
43
           "subtopic": "Employment-based coverage",
44
           "values": {
45
               "1": "Yes",
46
               "2": "No"
47
           }
48
       },
49
       "NOW_DIR": {
50
51
           "label": "Any current direct-purchase coverage",
           "universe": "All Persons",
52
           "type": "Categorical",
53
           "role": "Dependent",
54
           "topic": "Health insurance",
55
           "subtopic": "Direct-purchase coverage",
56
           "values": {
57
               "1": "Yes",
58
               "2": "No"
59
           }
60
61
       },
       "NOW_MCARE": {
62
63
           "label": "Current Medicare coverage",
           "universe": "All Persons",
64
           "type": "Categorical",
65
           "role": "Dependent",
66
           "topic": "Health insurance",
67
           "subtopic": "Medicare coverage",
68
           "values": {
69
               "1": "Yes",
70
71
               "2": "No"
           }
72
73
       },
       "NOW_MCAID": {
74
75
           "label": "Current Medicaid, PCHIP, or other means-tested coverage",
```

```
76
            "universe": "All Persons",
77
            "type": "Categorical",
78
            "role": "Dependent",
            "topic": "Health insurance",
79
80
            "subtopic": "Medicaid or other means-tested coverage",
            "values": {
81
                "1": "Yes",
82
                "2": "No"
83
            }
84
        },
85
        "NOW_CAID": {
86
87
            "label": "Current Medicaid coverage",
            "universe": "All Persons",
88
            "type": "Categorical",
89
            "role": "Dependent",
90
91
            "topic": "Health insurance",
            "subtopic": "Medicaid coverage",
92
            "values": {
93
                "1": "Yes",
94
                "2": "No"
95
            }
96
97
        },
        "NOW_PCHIP": {
98
99
            "label": "Current PCHIP coverage",
            "universe": "All Persons",
100
101
            "type": "Categorical",
102
            "role": "Dependent",
            "topic": "Health insurance",
103
104
            "subtopic": "PCHIP coverage",
            "values": {
105
                "1": "Yes",
106
107
                "2": "No"
            }
108
109
        },
        "NOW_OTHMT": {
110
            "label": "Current other means-tested coverage",
111
```

```
112
            "universe": "All Persons",
113
            "type": "Categorical",
114
            "role": "Dependent",
            "topic": "Health insurance",
115
116
            "subtopic": "Other means-tested coverage",
            "values": {
117
                "1": "Yes",
118
                "2": "No"
119
120
            }
        },
121
        "NOW_MIL": {
122
123
            "label": "Any current TRICARE coverage",
124
            "universe": "All Persons",
            "type": "Categorical",
125
            "role": "Dependent",
126
127
            "topic": "Health insurance",
            "subtopic": "TRICARE coverage",
128
            "values": {
129
                "1": "Yes",
130
                "2": "No"
131
            }
132
133
        },
        "NOW_CHAMPVA": {
134
135
            "label": "Current CHAMPVA coverage",
            "universe": "All Persons",
136
137
            "type": "Categorical",
138
            "role": "Dependent",
139
            "topic": "Health insurance",
140
            "subtopic": "CHAMPVA coverage",
            "values": {
141
                "1": "Yes",
142
143
                "2": "No"
            }
144
145
        },
        "NOW_VACARE": {
146
147
            "label": "Current VACARE coverage",
```

```
"universe": "All Persons",
148
149
            "type": "Categorical",
            "role": "Dependent",
150
            "topic": "Health insurance",
151
            "subtopic": "VACARE coverage",
152
            "values": {
153
                "1": "Yes",
154
                "2": "No"
155
156
            }
        },
157
        "NOW_IHSFLG": {
158
159
            "label": "Current coverage through the Indian Health Service",
160
            "universe": "All Persons",
            "type": "Categorical",
161
            "role": "Dependent",
162
            "topic": "Health insurance",
163
            "subtopic": "Indian Health Service coverage",
164
            "values": {
165
                "1": "Yes",
166
                "2": "No"
167
            }
168
169
        }
170 }
```

Metadata 3.2: Independent variables (data/original/metadata/meta-indep.json)

```
1 {
2
      "A_AGE": {
          "label": "Age",
3
          "universe": "All Persons",
4
          "type": "Continuous",
5
          "role": "Independent",
6
          "topic": "Demographics",
7
8
          "subtopic": "Individual characteristics",
          "values": {
9
```

```
10
               "00-79": "0-79 years of age",
               "80": "80-84 years of age",
11
               "85": "85+ years of age"
12
           }
13
14
       },
       "A_EXPRRP": {
15
           "label": "Expanded relationship code",
16
           "universe": "All Persons",
17
           "type": "Categorical",
18
           "role": "Independent",
19
           "topic": "Demographics",
20
           "subtopic": "Individual characteristics",
21
           "values": {
22
               "1": "Reference person with relatives",
23
               "2": "Reference person without relatives",
24
               "3": "Husband",
25
               "4": "Wife",
26
               "5": "Own child",
27
               "7": "Grandchild",
28
               "8": "Parent",
29
               "9": "Brother/sister",
30
31
               "10": "Other relative",
32
               "11": "Foster child",
33
               "12": "Nonrelative with relatives",
34
               "13": "Partner/roommate",
               "14": "Nonrelative without relatives"
35
           }
36
       },
37
       "A_FAMTYP": {
38
           "label": "Family type",
39
           "universe": "All Persons",
40
41
           "type": "Categorical",
           "role": "Independent",
42
           "topic": "Demographics",
43
44
           "subtopic": "Individual characteristics",
           "values": {
45
```

```
46
               "1": "Primary family",
               "2": "Nonfamily householder",
47
               "3": "Related subfamily",
48
               "4": "Unrelated subfamily",
49
50
               "5": "Secondary individual"
           }
51
52
       },
       "A_HGA": {
53
           "label": "Educational attainment",
54
           "universe": "All Persons",
55
           "type": "Categorical",
56
57
           "role": "Independent",
           "topic": "Demographics",
58
           "subtopic": "Individual characteristics",
59
           "values": {
60
               "0": "Children",
61
62
               "31": "Less than 1st grade",
               "32": "1st,2nd,3rd,or 4th grade",
63
               "33": "5th or 6th grade",
64
65
               "34": "7th and 8th grade",
               "35": "9th grade",
66
               "36": "10th grade",
67
68
               "37": "11th grade",
               "38": "12th grade no diploma",
69
               "39": "High school graduate - high school diploma or equivalent
70
71
               "40": "Some college but no degree",
               "41": "Associate degree in college - occupation/vocation
72
                  program",
               "42": "Associate degree in college - academic program",
73
               "43": "Bachelor's degree (for example: BA,AB,BS)",
74
75
               "44": "Master's degree (for example: MA, MS, MENG, MED, MSW, MBA)",
76
               "45": "Professional school degree (for example: MD,DDS,DVM,LLB,
                  JD)",
               "46": "Doctorate degree (for example: PHD,EDD)"
77
78
           }
```

```
},
79
        "A_MARITL": {
80
            "label": "Marital status",
81
            "universe": "All Persons",
82
            "type": "Categorical",
83
            "role": "Independent",
84
            "topic": "Demographics",
85
            "subtopic": "Individual characteristics",
86
            "values": {
87
                "1": "Married - civilian spouse present",
88
                "2": "Married - AF spouse present",
89
90
                "3": "Married - spouse absent (exc.separated)",
                "4": "Widowed",
91
                "5": "Divorced",
92
                "6": "Separated",
93
                "7": "Never married"
94
            }
95
96
        },
        "A_PFREL": {
97
98
            "label": "Primary family relationship",
            "universe": "All Persons",
99
100
            "type": "Categorical",
            "role": "Independent",
101
            "topic": "Demographics",
102
            "subtopic": "Individual characteristics",
103
104
            "values": {
                "O": "Not in primary family",
105
106
                "1": "Husband",
                "2": "Wife",
107
108
                "3": "Own child",
109
                "4": "Other relative",
110
                "5": "Unmarried reference person"
            }
111
112
        },
        "A_SEX": {
113
            "label": "Sex",
114
```

```
115
            "universe": "All Persons",
116
            "type": "Categorical",
            "role": "Independent",
117
            "topic": "Demographics",
118
            "subtopic": "Individual characteristics",
119
120
            "values": {
                "1": "Male",
121
                "2": "Female"
122
123
            }
        },
124
        "P_STAT": {
125
126
            "label": "Status of person identifier",
127
            "universe": "All Persons",
            "type": "Categorical",
128
            "role": "Independent",
129
            "topic": "Demographics",
130
            "subtopic": "Individual characteristics",
131
            "values": {
132
                "1": "Civilian 15+",
133
134
                "2": "Armed forces",
                "3": "Children 0-14"
135
136
            }
137
        },
138
        "PEAFEVER": {
139
            "label": "Did you ever serve on active duty in the U.S. Armed
                Forces?",
            "universe": "A_AGE greater than or equal to 17",
140
141
            "type": "Categorical",
142
            "role": "Independent",
143
            "topic": "Demographics",
            "subtopic": "Individual characteristics",
144
145
            "values": {
                "-1": "Not in universe",
146
                "1": "Yes",
147
                "2": "No"
148
149
            }
```

```
},
150
        "PEDISDRS": {
151
            "label": "Does...have difficulty dressing or bathing?",
152
            "universe": "PRPERTYP = 2",
153
            "type": "Categorical",
154
            "role": "Independent",
155
            "topic": "Demographics",
156
            "subtopic": "Individual characteristics",
157
158
            "values": {
                "-1": "Not in universe",
159
                "1": "Yes",
160
                "2": "No"
161
162
            }
163
        },
        "PEDISEAR": {
164
            "label": "Is...deaf or does ...have serious difficulty hearing?",
165
            "universe": "PRPERTYP = 2",
166
            "type": "Categorical",
167
            "role": "Independent",
168
169
            "topic": "Demographics",
170
            "subtopic": "Individual characteristics",
171
            "values": {
                "-1": "Not in universe",
172
                "1": "Yes",
173
                "2": "No"
174
175
            }
176
        },
177
        "PEDISEYE": {
178
            "label": "Is...blind or does...have serious difficulty seeing even
                when wearing glasses?",
179
            "universe": "PRPERTYP = 2",
180
            "type": "Categorical",
            "role": "Independent",
181
            "topic": "Demographics",
182
            "subtopic": "Individual characteristics",
183
184
            "values": {
```

```
185
                "-1": "Not in universe",
186
                "1": "Yes",
                "2": "No"
187
            }
188
189
        },
190
        "PEDISOUT": {
            "label": "Because of a physical, mental, or emotional condition,
191
                does...have difficulty doing errands along such as visiting a
                doctor's office or shopping?",
            "universe": "PRPERTYP = 2",
192
            "type": "Categorical",
193
194
            "role": "Independent",
195
            "topic": "Demographics",
            "subtopic": "Individual characteristics",
196
            "values": {
197
                "-1": "Not in universe",
198
                "1": "Yes",
199
                "2": "No"
200
            }
201
202
        },
203
        "PEDISPHY": {
204
            "label": "Does...have serious difficulty Walking or climbing stairs
                ?",
205
            "universe": "PRPERTYP = 2",
            "type": "Categorical",
206
207
            "role": "Independent",
208
            "topic": "Demographics",
209
            "subtopic": "Individual characteristics",
            "values": {
210
211
                "-1": "Not in universe",
                "1": "Yes",
212
213
                "2": "No"
            }
214
215
        },
        "PEDISREM": {
216
```

```
217
            "label": "Because of a physical, mental, or emotional condition,
                does...have serious difficulty concentrating, remembering, or
               making decisions?",
            "universe": "PRPERTYP = 2",
218
219
            "type": "Categorical",
220
            "role": "Independent",
            "topic": "Demographics",
221
222
            "subtopic": "Individual characteristics",
223
            "values": {
                "-1": "Not in universe",
224
                "1": "Yes",
225
                "2": "No"
226
227
            }
228
        },
        "PRDISFLG": {
229
            "label": "Does this person have any of these disability conditions?
230
            "universe": "PRPERTYP = 2",
231
            "type": "Categorical",
232
233
            "role": "Independent",
            "topic": "Demographics",
234
235
            "subtopic": "Individual characteristics",
236
            "values": {
237
                "-1": "Not in universe",
                "1": "Yes",
238
                "2": "No"
239
240
            }
        },
241
        "PRCITSHP": {
242
243
            "label": "Citizenship group",
            "universe": "All persons",
244
245
            "type": "Categorical",
            "role": "Independent",
246
            "topic": "Demographics",
247
            "subtopic": "Individual characteristics",
248
249
            "values": {
```

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250
                "1": "Native, born in US",
                "2": "Native, born in PR or US outlying area",
251
252
                "3": "Native, born abroad of US parent(s)",
                "4": "Foreign born, US cit by naturalization",
253
254
                "5": "Foreign born, not a US citizen"
            }
255
256
        },
        "PRDTRACE": {
257
            "label": "Race",
258
            "universe": "All persons",
259
            "type": "Categorical",
260
261
            "role": "Independent",
            "topic": "Demographics",
262
            "subtopic": "Individual characteristics",
263
            "values": {
264
                "1": "White only",
265
                "2": "Black only",
266
                "3": "American Indian, Alaskan Native only (AI)",
267
                "4": "Asian only",
268
269
                "5": "Hawaiian/Pacific Islander only (HP)",
                "6": "White-Black",
270
                "7": "White-AI",
271
272
                "8": "White-Asian",
273
                "9": "White-HP",
274
                "10": "Black-AI",
                "11": "Black-Asian",
275
276
                "12": "Black-HP",
                "13": "AI-Asian",
277
278
                "14": "AI-HP",
                "15": "Asian-HP",
279
280
                "16": "White-Black-AI",
281
                "17": "White-Black-Asian",
282
                "18": "White-Black-HP",
283
                "19": "White-AI-Asian",
284
                "20": "White-AI-HP",
285
                "21": "White-Asian-HP",
```

```
286
                "22": "Black-AI-Asian",
                "23": "White-Black-AI-Asian",
287
                "24": "White-AI-Asian-HP",
288
                "25": "Other 3 race comb.",
289
290
                "26": "Other 4 or 5 race comb."
            }
291
292
        },
        "A_MJIND": {
293
            "label": "Major industry code",
294
            "universe": "A_CLSWKR = 1-7",
295
            "type": "Categorical",
296
297
            "role": "Independent",
            "topic": "Basic CPS items",
298
            "subtopic": "Edited labor force items",
299
            "values": {
300
                "0": "Not in universe, or children",
301
302
                "1": "Agriculture, forestry, fishing, and hunting",
                "2": "Mining",
303
                "3": "Construction",
304
305
                "4": "Manufacturing",
                "5": "Wholesale and retail trade",
306
307
                "6": "Transportation and utilities",
                "7": "Information",
308
309
                "8": "Financial activities",
310
                "9": "Professional and business services",
                "10": "Educational and health services",
311
312
                "11": "Leisure and hospitality",
                "12": "Other services",
313
                "13": "Public administration",
314
                "14": "Armed forces"
315
            }
316
317
        },
        "A_MJOCC": {
318
            "label": "Major occupation recode",
319
320
            "universe": "A_CLSWKR = 1-7",
321
            "type": "Categorical",
```

```
322
            "role": "Independent",
323
            "topic": "Basic CPS items",
324
            "subtopic": "Edited labor force items",
            "values": {
325
326
                "0": "Not in universe or children",
                "1": "Management, business, and financial occupations",
327
                "2": "Professional and related occupations",
328
                "3": "Service occupations",
329
                "4": "Sales and related occupations",
330
                "5": "Office and administrative support occupations",
331
                "6": "Farming, fishing, and forestry occupations",
332
                "7": "Construction and extraction occupations",
333
                "8": "Installation, maintenance, and repair occupations",
334
                "9": "Production occupations",
335
                "10": "Transportation and material moving occupations",
336
                "11": "Armed forces"
337
            }
338
339
        },
        "PEIO1COW": {
340
341
            "label": "Individual class of worker on first job",
            "universe": "All persons",
342
343
            "type": "Categorical",
344
            "role": "Independent",
345
            "topic": "Basic CPS items",
346
            "subtopic": "Edited labor force items",
            "values": {
347
                "O": "NIU",
348
                "1": "Government-federal",
349
350
                "2": "Government-state",
                "3": "Government - local",
351
                "4": "Private, for profit",
352
353
                "5": "Private, nonprofit",
354
                "6": "Self-employed, incorporated",
                "7": "Self-employed, unincorporated",
355
                "8": "Without pay"
356
            }
357
```

```
},
358
        "PRDISC": {
359
360
            "label": "Discouraged worker recode",
            "universe": "All persons",
361
            "type": "Categorical",
362
            "role": "Independent",
363
            "topic": "Basic CPS items",
364
            "subtopic": "Edited labor force items",
365
366
            "values": {
                "O": "NIU",
367
                "1": "Discouraged worker",
368
369
                "2": "Conditionally interested",
                "3": "Not available"
370
            }
371
372
        },
        "PRUNTYPE": {
373
            "label": "Individual class of worker on first job",
374
            "universe": "All persons",
375
376
            "type": "Categorical",
377
            "role": "Independent",
            "topic": "Basic CPS items",
378
379
            "subtopic": "Edited labor force items",
            "values": {
380
                "O": "NIU",
381
                "1": "Job loser/on layoff",
382
383
                "2": "Other job loser",
384
                "3": "Temporary job ended",
385
                "4": "Job leaver",
                "5": "Re-entrant",
386
387
                "6": "New-entrant"
            }
388
389
        },
        "A_GRSWK": {
390
```

```
391
            "label": "How much does ... usually earn per week at this job
               before deductions , subject to topcoding, the higher of either
               the amount of item 25a times Item 25c or the actual item 25d
               entry will be present",
            "universe": "PRERELG=1",
392
            "type": "Continuous",
393
            "role": "Independent",
394
395
            "topic": "Basic CPS items",
            "subtopic": "Edited earnings items",
396
            "values": {
397
                "O": "Not in universe or children or armed forces",
398
399
                "0001-2885": "Dollar amount"
            }
400
        },
401
        "A_HRLYWK": {
402
403
            "label": "Is ... paid by the hour on this job?",
            "universe": "PRERELG=1",
404
            "type": "Categorical",
405
            "role": "Independent",
406
407
            "topic": "Basic CPS items",
            "subtopic": "Edited earnings items",
408
409
            "values": {
                "O": "Not in universe or children and armed forces",
410
411
               "1": "Yes",
               "2": "No"
412
413
            }
        },
414
        "A_HRSPAY": {
415
416
            "label": "How much does ... earn per hour?",
            "universe": "A_HRLYWK=1",
417
            "type": "Continuous",
418
419
            "role": "Independent",
420
            "topic": "Basic CPS items",
421
            "subtopic": "Edited earnings items",
422
            "values": {
423
                "O": "Not in universe or children or armed forces",
```

```
424
                "0001-9999": "Entry (2 implied decimal places)"
            }
425
426
        },
        "PRERELG": {
427
428
            "label": "Earnings eligibility flag",
            "universe": "All persons",
429
            "type": "Categorical",
430
            "role": "Independent",
431
            "topic": "Basic CPS items",
432
            "subtopic": "Edited earnings items",
433
            "values": {
434
435
                "0": "Not earnings eligible",
                "1": "Earnings eligible"
436
            }
437
438
        },
        "A_CIVLF": {
439
440
            "label": "Civilian labor force",
            "universe": "All persons",
441
            "type": "Categorical",
442
443
            "role": "Independent",
            "topic": "Basic CPS items",
444
            "subtopic": "Labor force person recodes",
445
446
            "values": {
                "O": "Not in universe or children and Armed Forces",
447
                "1": "In universe"
448
            }
449
        },
450
        "A_CLSWKR": {
451
452
            "label": "Class of worker",
            "universe": "PEMLR=1-3 or (PEMLR=4-7 and person worked in the last
453
                12 months)",
454
            "type": "Categorical",
            "role": "Independent",
455
            "topic": "Basic CPS items",
456
457
            "subtopic": "Labor force person recodes",
            "values": {
458
```

```
459
                "0": "Not in universe or children and armed forces",
460
                "1": "Private",
                "2": "Federal government",
461
                "3": "State government",
462
463
                "4": "Local government",
                "5": "Self-employed-incorporated",
464
465
                "6": "Self-employed-not incorporated",
                "7": "Without pay",
466
                "8": "Never worked"
467
            }
468
        },
469
470
        "A_EXPLF": {
471
            "label": "Experienced labor force employment status",
            "universe": "PEMLR=1-4",
472
            "type": "Categorical",
473
474
            "role": "Independent",
475
            "topic": "Basic CPS items",
            "subtopic": "Labor force person recodes",
476
            "values": {
477
478
                "0": "Not in experienced labor force",
                "1": "Employed",
479
480
                "2": "Unemployed"
            }
481
482
        },
483
        "A_LFSR": {
            "label": "Labor force status recode",
484
            "universe": "All persons",
485
            "type": "Categorical",
486
487
            "role": "Independent",
            "topic": "Basic CPS items",
488
            "subtopic": "Labor force person recodes",
489
490
            "values": {
                "0": "Children or Armed Forces",
491
                "1": "Working",
492
                "2": "With job, not at work",
493
494
                "3": "Unemployed, looking for work",
```

```
495
                "4": "Unemployed, on layoff",
                "7": "Nilf"
496
            }
497
        },
498
        "A_UNCOV": {
499
            "label": "On this job, is ... covered by a union or employee
500
                association contract?",
            "universe": "A_UNMEM=2",
501
502
            "type": "Categorical",
            "role": "Independent",
503
            "topic": "Basic CPS items",
504
            "subtopic": "Labor force person recodes",
505
            "values": {
506
                "O": "Not in universe or children and armed forces",
507
                "1": "Yes",
508
                "2": "No"
509
            }
510
511
        },
        "A_UNMEM": {
512
513
            "label": "On this job, is ... a member of a labor union or of an
                employee association similar to a union?",
514
            "universe": "PRERELG=1",
515
            "type": "Categorical",
            "role": "Independent",
516
            "topic": "Basic CPS items",
517
518
            "subtopic": "Labor force person recodes",
            "values": {
519
520
                "O": "Not in universe or children and armed forces",
                "1": "Yes",
521
                "2": "No"
522
            }
523
524
        },
        "A_UNTYPE": {
525
526
            "label": "Reason for unemployment",
            "universe": "A_LFSR=3 or 4",
527
528
            "type": "Categorical",
```

```
529
            "role": "Independent",
            "topic": "Basic CPS items",
530
531
            "subtopic": "Labor force person recodes",
            "values": {
532
533
                "O": "Not in universe or children and Armed Forces",
                "1": "Job loser - on layoff",
534
                "2": "Other job loser",
535
                "3": "Job leaver",
536
537
                "4": "Re-entrant",
                "5": "New entrant"
538
            }
539
540
        },
        "A_USLHRS": {
541
            "label": "How many hrs per week does ... usually work at this job?"
542
            "universe": "All persons",
543
544
            "type": "Continuous",
            "role": "Independent",
545
            "topic": "Basic CPS items",
546
547
            "subtopic": "Labor force person recodes",
            "values": {
548
                "-4": "Hours vary",
549
550
                "-1": "Not in universe",
551
                "00": "None, no hours",
                "01-99": "Entry"
552
            }
553
        },
554
        "A_WKSCH": {
555
            "label": "Labor force by time worked or lost",
556
            "universe": "All persons",
557
            "type": "Categorical",
558
559
            "role": "Independent",
560
            "topic": "Basic CPS items",
            "subtopic": "Labor force person recodes",
561
            "values": {
562
563
                "0": "Not in universe",
```

```
"1": "At work",
564
565
                "2": "With job, not at work",
566
                "3": "Unemployed, seeks FT",
567
                "4": "Unemployed, seeks PT"
568
            }
569
        },
        "A_WKSLK": {
570
571
            "label": "Duration of unemployment",
572
            "universe": "PEMLR=3 or 4",
            "type": "Continuous",
573
            "role": "Independent",
574
575
            "topic": "Basic CPS items",
            "subtopic": "Labor force person recodes",
576
            "values": {
577
                "000": "NIU, Children or Armed Forces",
578
                "001-999": "Entry"
579
            }
580
581
        },
        "A_WKSTAT": {
582
            "label": "Full/part-time status",
583
            "universe": "All persons",
584
585
            "type": "Categorical",
586
            "role": "Independent",
587
            "topic": "Basic CPS items",
588
            "subtopic": "Labor force person recodes",
            "values": {
589
590
                "0": "Children or Armed Forces",
591
                "1": "Not in labor force",
592
                "2": "Full-time schedules",
593
                "3": "Part-time for economic reasons, usually FT",
594
                "4": "Part-time for non-economic reasons, usually PT",
595
                "5": "Part-time for economic reasons, usually PT",
                "6": "Unemployed FT",
596
                "7": "Unemployed PT"
597
598
            }
599
        },
```

```
600
        "PEHRUSLT": {
601
            "label": "Hours usually worked last week",
            "universe": "All persons",
602
            "type": "Continuous",
603
604
            "role": "Independent",
            "topic": "Basic CPS items",
605
            "subtopic": "Labor force person recodes",
606
            "values": {
607
608
                "-4": "Hours vary",
                "-1": "NIU - adult civilian",
609
                "000": "NIU - children or Armed Forces or no hours",
610
611
                "1-198": "# of hours"
            }
612
613
        },
        "PEMLR": {
614
            "label": "Major labor force recode",
615
616
            "universe": "All persons",
            "type": "Categorical",
617
            "role": "Independent",
618
619
            "topic": "Basic CPS items",
            "subtopic": "Labor force person recodes",
620
621
            "values": {
                "O": "NIU",
622
623
                "1": "Employed - at work",
                "2": "Employed - absent",
624
625
                "3": "Unemployed - on layoff",
626
                "4": "Unemployed - looking",
                "5": "Not in labor force - retired",
627
628
                "6": "Not in labor force - disabled",
629
                "7": "Not in labor force - other"
            }
630
631
        },
        "PRCOW1": {
632
633
            "label": "Class of worker recode-job 1",
634
            "universe": "All persons",
635
            "type": "Categorical",
```

```
636
            "role": "Independent",
            "topic": "Basic CPS items",
637
            "subtopic": "Labor force person recodes",
638
            "values": {
639
                "O": "NIU",
640
                "1": "Federal govt",
641
                "2": "State govt",
642
                "3": "Local govt",
643
                "4": "Private (incl. self-employed incorp.)",
644
                "5": "Self-employed, unincorp.",
645
                "6": "Without pay"
646
647
            }
        },
648
        "PRPTREA": {
649
            "label": "Detailed reason for part-time",
650
651
            "universe": "Part time workers",
652
            "type": "Categorical",
653
            "role": "Independent",
            "topic": "Basic CPS items",
654
655
            "subtopic": "Labor force person recodes",
            "values": {
656
657
                "O": "NIU",
658
                "1": "Usually FT - slack work/business conditions",
               "2": "Usually FT - seasonal work",
659
660
                "3": "Usually FT - job started/ended during week",
                "4": "Usually FT - vacation/personal day",
661
662
                "5": "Usually FT - own illness/injury/medical appt",
                "6": "Usually FT - holiday (religious or legal)",
663
                "7": "Usually FT - child care problems",
664
                "8": "Usually FT - other fam/pers obligations",
665
                "9": "Usually FT - labor dispute",
666
667
                "10": "Usually FT - weather affected job",
                "11": "Usually FT - school/training",
668
669
                "12": "Usually FT - civic/military duty",
670
                "13": "Usually FT - other reason",
                "14": "Usually PT - slack work/business conditions",
671
```

```
672
                "15": "Usually PT - PT could only find PT work",
                "16": "Usually PT - seasonal work",
673
674
                "17": "Usually PT - child care problems",
                "18": "Usually PT - other fam/pers obligations",
675
676
                "19": "Usually PT - health/medical limitations",
                "20": "Usually PT - school/training",
677
678
                "21": "Usually PT - retired/social security limit on earnings",
                "22": "Usually PT - workweek<35 hours",
679
                "23": "Usually PT - other"
680
            }
681
        },
682
683
        "PRWKSTAT": {
            "label": "Full/part-time work status",
684
            "universe": "All persons",
685
            "type": "Categorical",
686
687
            "role": "Independent",
688
            "topic": "Basic CPS items",
            "subtopic": "Labor force person recodes",
689
            "values": {
690
               "O": "NIU",
691
                "1": "Not in labor force",
692
693
               "2": "FT hours (35+), usually FT",
                "3": "PT for economic reasons, usually FT",
694
695
               "4": "PT for non-economic reasons, usually FT",
696
                "5": "Not at work, usually FT",
                "6": "PT hrs, usually PT for economic reasons",
697
                "7": "PT hrs, usually PT for non-economic",
698
                "8": "FT hours, usually PT for economic reasons",
699
700
                "9": "FT hours, usually PT for non-economic reasons",
                "10": "Not at work, usually part-time",
701
                "11": "Unemployed FT",
702
703
                "12": "Unemployed PT"
            }
704
705
        },
        "CLWK": {
706
707
            "label": "Longest job class of worker (recode)",
```

```
708
            "universe": "All persons aged 15+",
709
            "type": "Categorical",
            "role": "Independent",
710
            "topic": "Work experience",
711
            "subtopic": "General",
712
            "values": {
713
                "0": "Niu",
714
                "1": "Private",
715
716
                "2": "Government",
                "3": "Self-employed",
717
718
                "4": "Without pay",
                "5": "Never worked"
719
720
            }
721
        },
        "EARNER": {
722
            "label": "Earner status recode",
723
            "universe": "All persons aged 15+",
724
            "type": "Categorical",
725
            "role": "Independent",
726
727
            "topic": "Work experience",
728
            "subtopic": "General",
729
            "values": {
                "0": "Niu",
730
731
                "1": "Earner",
                "2": "Nonearner"
732
733
            }
734
        },
735
        "HRSWK": {
736
            "label": "In the weeks that ... worked how may hours did ...
                usually work per week?",
            "universe": "WKSWORK > 0",
737
738
            "type": "Continuous",
            "role": "Independent",
739
            "topic": "Work experience",
740
            "subtopic": "General",
741
742
            "values": {
```

```
"0": "Niu",
743
744
                "1": "1 hour",
745
                "2-98": "2-98 hours",
                "99": "99 hours plus"
746
747
            }
        },
748
749
        "LJCW": {
            "label": "Longest job class of worker",
750
751
            "universe": "WKSWORK > 0",
            "type": "Categorical",
752
            "role": "Independent",
753
            "topic": "Work experience",
754
            "subtopic": "General",
755
            "values": {
756
                "O": "Niu",
757
                "1": "Private",
758
                "2": "Federal",
759
                "3": "State",
760
                "4": "Local",
761
762
                "5": "Self employed incorporated, yes",
                "6": "Self employed incorporated, no or farm",
763
764
                "7": "Without pay"
            }
765
766
        },
        "NWLKWK": {
767
            "label": "How may different weeks was ... looking for work or on
768
                layoff?",
769
            "universe": "NWLOOK = 1",
770
            "type": "Continuous",
            "role": "Independent",
771
            "topic": "Work experience",
772
773
            "subtopic": "General",
            "values": {
774
                "0": "Niu",
775
                "1": "1 week",
776
                "2-51": "2-51 weeks",
777
```

```
"52": "52 weeks"
778
            }
779
780
        },
        "NWLOOK": {
781
782
            "label": "Even though ... did not work in 20.. did spend and time
                trying to find a job or on layoff?",
            "universe": "WORKYN = 2",
783
            "type": "Categorical",
784
785
            "role": "Independent",
            "topic": "Work experience",
786
            "subtopic": "General",
787
788
            "values": {
                "0": "Niu",
789
                "1": "Yes",
790
                "2": "No"
791
            }
792
793
        },
        "PHMEMPRS": {
794
795
            "label": "For how many employers did ... work in 20..? if more than
                 one at same time, only count it as one employer",
            "universe": "WKSWORK > 0",
796
797
            "type": "Categorical",
            "role": "Independent",
798
            "topic": "Work experience",
799
            "subtopic": "General",
800
            "values": {
801
802
                "0": "Niu",
                "1": "One employer",
803
                "2": "Two employers",
804
                "3": "3 or more employers"
805
            }
806
807
        },
        "RSNNOTW": {
808
809
            "label": "What was the main reason ... did not work in 20..?",
            "universe": "WORKYN = 2",
810
811
            "type": "Categorical",
```

```
812
            "role": "Independent",
            "topic": "Work experience",
813
            "subtopic": "General",
814
            "values": {
815
                "0": "Niu",
816
                "1": "Ill or disabled",
817
                "2": "Retired",
818
                "3": "Taking care of home",
819
                "4": "Going to school",
820
                "5": "Could not find work",
821
                "6": "Other"
822
            }
823
        },
824
        "WECLW": {
825
            "label": "Longest job class of worker (persons 15+)",
826
            "universe": "All persons aged 15+",
827
828
            "type": "Categorical",
            "role": "Independent",
829
            "topic": "Work experience",
830
831
            "subtopic": "General",
            "values": {
832
833
                "0": "Not in universe",
                "1": "Agriculture (Wage and salary)",
834
835
                "2": "Agriculture (Self-employed)",
                "3": "Agriculture (Unpaid)",
836
                "4": "Nonagriculture (Private household",
837
838
                "5": "Nonagriculture (Other private)",
                "6": "Nonagriculture (Government)",
839
840
                "7": "Nonagriculture (Self-employed)",
                "8": "Nonagriculture (Unpaid)",
841
                "9": "Nonagriculture (Never worked)"
842
843
            }
844
        },
        "WEWKRS": {
845
846
            "label": "Weeks worked recode",
            "universe": "All persons aged 15+",
847
```

```
"type": "Categorical",
848
            "role": "Independent",
849
            "topic": "Work experience",
850
            "subtopic": "General",
851
            "values": {
852
                "O": "Niu",
853
                "1": "Full-year worker (Full time)",
854
                "2": "Full-year worker (Part time)",
855
                "3": "Part-year worker (Full time)",
856
                "4": "Part-year worker (Part time)",
857
                "5": "Part-year worker (Nonworker)"
858
859
            }
        },
860
        "WKSWORK": {
861
            "label": "During 20.. in how many weeks did ... work even for a few
862
                hours? (include paid vacation and sick leave as work)",
863
            "universe": "Persons 15+ with WORKYN = 1",
            "type": "Continuous",
864
            "role": "Independent",
865
866
            "topic": "Work experience",
            "subtopic": "General",
867
868
            "values": {
                "0": "Niu",
869
870
                "1": "1 week",
                "2-51": "2-51 weeks",
871
                "52": "52 weeks"
872
873
            }
        },
874
875
        "WORKYN": {
            "label": "Did ... work at a job or business at any time during
876
                20..?",
877
            "universe": "All persons aged 15+",
            "type": "Categorical",
878
            "role": "Independent",
879
880
            "topic": "Work experience",
881
            "subtopic": "General",
```

```
"values": {
882
                "0": "Niu",
883
884
                "1": "Yes",
                "2": "No"
885
            }
886
        },
887
        "WRK_CK": {
888
            "label": "Worked last year recode, including temporary and part-
889
            "universe": "All persons aged 15+",
890
891
            "type": "Categorical",
            "role": "Independent",
892
            "topic": "Work experience",
893
            "subtopic": "General",
894
            "values": {
895
                "0": "Niu",
896
                "1": "Yes",
897
                "2": "No"
898
            }
899
900
        },
        "WTEMP": {
901
            "label": "Did ... do any temporary, part-time, or seasonal work
902
                even for a few days during 20..?",
903
            "universe": "WORKYN = 2",
904
            "type": "Categorical",
            "role": "Independent",
905
906
            "topic": "Work experience",
            "subtopic": "General",
907
908
            "values": {
                "0": "Niu",
909
                "1": "Yes",
910
911
                "2": "No"
            }
912
913
        },
        "ERN_OTR": {
914
915
            "label": "Wage and salary money earned from other work, Y/N",
```

```
916
            "universe": "All persons aged 15+",
917
            "type": "Categorical",
            "role": "Independent",
918
            "topic": "Income",
919
            "subtopic": "Earnings",
920
            "values": {
921
                "0": "Niu",
922
                "1": "Yes",
923
                "2": "No"
924
            }
925
        },
926
927
        "ERN_SRCE": {
            "label": "Source of earnings from longest job",
928
            "universe": "ERN_YN = 1",
929
            "type": "Categorical",
930
            "role": "Independent",
931
            "topic": "Income",
932
            "subtopic": "Earnings",
933
            "values": {
934
                "0": "Niu",
935
                "1": "Wage and salary",
936
937
                "2": "Self employment",
                "3": "Farm self employment",
938
939
                "4": "Without pay"
            }
940
        },
941
942
        "ERN_VAL": {
943
            "label": "How much did ... earn from this employer before
                deductions in 20..? what was ... net earnings from this
                business/ farm after expenses during 20..?",
            "universe": "ERN_YN = 1",
944
945
            "type": "Continuous",
            "role": "Independent",
946
            "topic": "Income",
947
            "subtopic": "Earnings",
948
949
            "values": {
```

```
"0": "None or Niu",
950
951
                "-9,999 - 9,999,999": "Wages & self-employment"
            }
952
        },
953
        "ERN_YN": {
954
            "label": "Earnings from employer or net earnings from business/
955
                farm after expenses from longest job during 20.. ?",
            "universe": "WORKYN=1 or WTEMP=1",
956
957
            "type": "Categorical",
            "role": "Independent",
958
            "topic": "Income",
959
960
            "subtopic": "Earnings",
            "values": {
961
                "0": "Niu",
962
                "1": "Yes",
963
                "2": "No"
964
            }
965
966
        },
        "FRM_VAL": {
967
            "label": "Amount of farm self-employment earnings from secondary
968
                source",
969
            "universe": "FRMOTR = 1",
970
            "type": "Continuous",
971
            "role": "Independent",
            "topic": "Income",
972
973
            "subtopic": "Earnings",
974
            "values": {
                "0": "None or Niu",
975
976
                "-999999-999999": "Farm self employment"
977
            }
978
        },
979
        "FRMOTR": {
980
            "label": "Receiving farm self-employment from secondary source",
981
            "universe": "ERN_OTR = 1",
            "type": "Categorical",
982
983
            "role": "Independent",
```

```
"topic": "Income",
 984
             "subtopic": "Earnings",
 985
 986
             "values": {
                 "0": "Niu",
 987
                 "1": "Yes",
 988
                 "2": "No"
 989
             }
 990
         },
 991
 992
         "FRSE_VAL": {
             "label": "Total amount of farm self-employment earnings",
 993
             "universe": "ERN_YN=1 or FRMOTR=1",
 994
 995
             "type": "Continuous",
             "role": "Independent",
 996
             "topic": "Income",
 997
             "subtopic": "Earnings",
 998
             "values": {
999
                 "0": "None or Niu;",
1000
                 "-999999-999999": "Farm self employment"
1001
             }
1002
1003
         },
         "FRSE_YN": {
1004
             "label": "Receiving any farm self-employment",
1005
             "universe": "ERN_YN=1 or FRMOTR=1",
1006
1007
             "type": "Categorical",
1008
             "role": "Independent",
1009
             "topic": "Income",
1010
             "subtopic": "Earnings",
1011
             "values": {
1012
                 "0": "Niu",
1013
                 "1": "Yes",
1014
                 "2": "No"
1015
             }
1016
         },
         "PEARNVAL": {
1017
1018
             "label": "Total persons earnings",
1019
             "universe": "All persons aged 15+",
```

```
1020
             "type": "Continuous",
1021
             "role": "Independent",
             "topic": "Income",
1022
1023
             "subtopic": "Earnings",
             "values": {
1024
                 "0": "None;",
1025
                 "negative amt": "Income (loss);",
1026
                 "positive amt": "Income"
1027
1028
             }
         },
1029
         "SE_VAL": {
1030
1031
             "label": "Amount of own business self-employment earnings from
                 secondary source",
             "universe": "SEOTR = 1",
1032
             "type": "Continuous",
1033
             "role": "Independent",
1034
             "topic": "Income",
1035
             "subtopic": "Earnings",
1036
             "values": {
1037
1038
                 "0": "None or niu;",
                 "-99999-99999": "Own business self employment"
1039
1040
             }
1041
         },
1042
         "SEMP_VAL": {
1043
             "label": "Total own business self-employment earnings (combined
                 amounts in ern-val, if ern-srce=2, and se-val)",
1044
             "universe": "ERN_YN=1 or SEOTR=1",
1045
             "type": "Continuous",
1046
             "role": "Independent",
1047
             "topic": "Income",
             "subtopic": "Earnings",
1048
1049
             "values": {
                 "0": "None or niu;",
1050
                 "-99999-99999": "Own business self employment"
1051
1052
             }
1053
         },
```

```
1054
         "SEMP_YN": {
1055
             "label": "Receiving own business self-employment, y/n",
             "universe": "ERN_YN=1 or SEOTR=1",
1056
1057
             "type": "Categorical",
             "role": "Independent",
1058
             "topic": "Income",
1059
             "subtopic": "Earnings",
1060
             "values": {
1061
1062
                 "0": "Niu",
                 "1": "Yes",
1063
                 "2": "No"
1064
             }
1065
         },
1066
         "SEOTR": {
1067
             "label": "Receiving own business self-employment, y/n",
1068
             "universe": "ERN_YN=1 or SEOTR=1",
1069
1070
             "type": "Categorical",
             "role": "Independent",
1071
1072
             "topic": "Income",
1073
             "subtopic": "Earnings",
1074
             "values": {
1075
                 "0": "Niu",
                 "1": "Yes",
1076
                 "2": "No"
1077
             }
1078
1079
         },
1080
         "WAGEOTR": {
1081
             "label": "Receiving wage and salary earnings from other employers,
                 y/n'',
1082
             "universe": "ERN_OTR = 1",
             "type": "Categorical",
1083
1084
             "role": "Independent",
             "topic": "Income",
1085
             "subtopic": "Earnings",
1086
             "values": {
1087
                 "0": "Niu",
1088
```

```
"1": "Yes",
1089
                 "2": "No"
1090
             }
1091
         },
1092
         "WS_VAL": {
1093
             "label": "Amount of wage and salary earnings from other employers",
1094
             "universe": "ERN_OTR = 1",
1095
             "type": "Continuous",
1096
1097
             "role": "Independent",
             "topic": "Income",
1098
             "subtopic": "Earnings",
1099
1100
             "values": {
                 "0": "None or niu;",
1101
                 "1-9999999": "Wage and salary"
1102
             }
1103
1104
         },
1105
         "WSAL_VAL": {
             "label": "Total wage and salary earnings (combined amounts in ern-
1106
                 val, if ern-srce=1, and ws-val)",
1107
             "universe": "ERN_YN=1 or WAGEOTR=1",
             "type": "Continuous",
1108
1109
             "role": "Independent",
             "topic": "Income",
1110
1111
             "subtopic": "Earnings",
1112
             "values": {
                 "0": "None or niu;",
1113
1114
                 "1-9999999": "Wage and salary"
1115
             }
1116
         },
         "WSAL_YN": {
1117
             "label": "Receiving wage and salary earnings",
1118
1119
             "universe": "ERN_YN=1 or WAGEOTR=1",
             "type": "Categorical",
1120
             "role": "Independent",
1121
             "topic": "Income",
1122
1123
             "subtopic": "Earnings",
```

```
"values": {
1124
                 "0": "Niu",
1125
                 "1": "Yes",
1126
                 "2": "No"
1127
             }
1128
         },
1129
         "ANN_VAL": {
1130
1131
             "label": "Retirement income, annuities amount",
1132
             "universe": "ANN_YN = 1",
             "type": "Continuous",
1133
             "role": "Independent",
1134
1135
             "topic": "Income",
             "subtopic": "Other income",
1136
             "values": {
1137
                 "-1": "Niu",
1138
                 "0-999999": "Dollar amount"
1139
             }
1140
         },
1141
         "ANN_YN": {
1142
1143
             "label": "Retirement income, annuities, y/n",
             "universe": "All Persons aged 15+",
1144
1145
             "type": "Categorical",
             "role": "Independent",
1146
1147
             "topic": "Income",
             "subtopic": "Other income",
1148
1149
             "values": {
1150
                 "0": "Niu",
1151
                 "1": "Yes",
                 "2": "No"
1152
1153
             }
1154
         },
1155
         "CAP_VAL": {
             "label": "Capital gains value",
1156
             "universe": "CAP_YN = 1",
1157
             "type": "Continuous",
1158
             "role": "Independent",
1159
```

```
"topic": "Income",
1160
1161
             "subtopic": "Other income",
             "values": {
1162
                 "0": "None or niu",
1163
                 "1-999999": "Captial gains amount"
1164
             }
1165
1166
         },
         "CAP_YN": {
1167
             "label": "Yes/no answer to 'Did you receive capital gain from your
1168
                 shares of stock or mutual fund?'",
             "universe": "DIV_YN = 1",
1169
             "type": "Categorical",
1170
             "role": "Independent",
1171
             "topic": "Income",
1172
             "subtopic": "Other income",
1173
1174
             "values": {
                 "0": "Niu",
1175
                 "1": "Yes",
1176
                 "2": "No"
1177
             }
1178
         },
1179
         "DBTN_VAL": {
1180
1181
             "label": "Total amount of retirement distributions received (
                 dst_val1 + dst_val2)",
             "universe": "DST_VAL1>0 OR DST_VAL2>0",
1182
1183
             "type": "Continuous",
1184
             "role": "Independent",
1185
             "topic": "Income",
1186
             "subtopic": "Other income",
             "values": {
1187
                 "0": "None or niu",
1188
1189
                 "1-9999999": "Dollar amount"
             }
1190
1191
         },
         "DIS_SC1": {
1192
             "label": "What was the source of disability income?",
1193
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"universe": "DIS_YN=1",
1194
1195
             "type": "Categorical",
1196
             "role": "Independent",
             "topic": "Income",
1197
1198
             "subtopic": "Other income",
             "values": {
1199
                 "0": "Niu",
1200
                 "1": "Worker's compensation",
1201
1202
                 "2": "Company or union disability",
                 "3": "Federal government disability",
1203
                 "4": "Us military retirement disability",
1204
                 "5": "State or local gov't employee disability",
1205
                 "6": "Us railroad retirement disability",
1206
                 "7": "Accident or disability insurance",
1207
                 "8": "Blacklung miners disability",
1208
                 "9": "State temporary sickness",
1209
1210
                 "10": "Other or don't know"
             }
1211
         },
1212
1213
         "DIS_SC2": {
1214
             "label": "What was the source of disability income?",
1215
             "universe": "DIS_YN=1",
1216
             "type": "Categorical",
1217
             "role": "Independent",
             "topic": "Income",
1218
1219
             "subtopic": "Other income",
1220
             "values": {
                 "0": "Niu",
1221
1222
                 "1": "Worker's compensation",
                 "2": "Company or union disability",
1223
                 "3": "Federal government disability",
1224
1225
                 "4": "Us military retirement disability",
1226
                 "5": "State or local gov't employee disability",
1227
                 "6": "Us railroad retirement disability",
1228
                 "7": "Accident or disability insurance",
1229
                 "8": "Blacklung miners disability",
```

```
1230
                 "9": "State temporary sickness",
1231
                 "10": "Other or don't know"
             }
1232
         },
1233
1234
         "DIS_VAL1": {
             "label": "How much did ... receive (source type) during 20.. ?",
1235
             "universe": "DIS_SC1>0",
1236
             "type": "Continuous",
1237
             "role": "Independent",
1238
             "topic": "Income",
1239
             "subtopic": "Other income",
1240
1241
             "values": {
                 "0": "None or niu",
1242
                 "1-999999": "Disability income"
1243
             }
1244
1245
         },
1246
         "DIS_VAL2": {
             "label": "How much did ... receive (source type) during 20.. ?",
1247
             "universe": "DIS_SC2>0",
1248
1249
             "type": "Continuous",
             "role": "Independent",
1250
1251
             "topic": "Income",
             "subtopic": "Other income",
1252
1253
             "values": {
1254
                 "0": "None or niu",
                 "1-999999": "Disability income"
1255
1256
         },
1257
         "DIS_YN": {
1258
             "label": "Other than social security did ... receive any income in
1259
                 20.. as a result of health problems?",
1260
             "universe": "All Persons aged 15+",
1261
             "type": "Categorical",
             "role": "Independent",
1262
             "topic": "Income",
1263
1264
             "subtopic": "Other income",
```

```
"values": {
1265
                 "0": "Niu",
1266
                 "1": "Yes",
1267
                 "2": "No"
1268
             }
1269
         },
1270
         "DIV_VAL": {
1271
             "label": "How much did ... receive in dividends from stocks or
1272
                 mutual funds during 20.. ?",
             "universe": "DIV_YN = 1",
1273
             "type": "Continuous",
1274
             "role": "Independent",
1275
             "topic": "Income",
1276
             "subtopic": "Other income",
1277
             "values": {
1278
                 "0": "None or niu",
1279
                 "1-999999": "Dividends"
1280
             }
1281
         },
1282
1283
         "DIV_YN": {
             "label": "Did ... receive dividends?",
1284
1285
             "universe": "All Persons aged 15+",
             "type": "Categorical",
1286
1287
             "role": "Independent",
             "topic": "Income",
1288
             "subtopic": "Other income",
1289
1290
             "values": {
                 "0": "Niu",
1291
                 "1": "Yes",
1292
                 "2": "No"
1293
             }
1294
1295
         },
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1296
1297
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1298
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1300
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1303
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1304
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1305
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1306
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1307
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1308
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1309
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1311
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1312
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1313
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1314
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1317
                 "2": "403b account",
1318
                 "3": "Roth ira",
1319
                 "4": "Regular ira",
1320
1321
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1322
                 "6": "Sep plan (simplified employee pension)",
                 "7": "Other type of retirement account"
1323
1324
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1325
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1327
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1332
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1334
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1335
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1337
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1338
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1339
                 "6": "Sep plan (simplified employee pension)",
1340
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1341
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1342
         },
1343
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1345
1346
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1348
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1349
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1350
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1352
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1353
                 "2": "403b account",
1354
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1355
                 "4": "Regular ira",
1356
1357
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1358
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                 "7": "Other type of retirement account"
1359
1360
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1361
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1365
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1368
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1370
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1374
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1375
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1376
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1377
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1378
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1379
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1380
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1381
1382
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1383
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1384
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1385
             "subtopic": "Other income",
1386
1387
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1388
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1389
             }
1390
         },
1391
1392
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1393
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1394
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1396
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1398
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1399
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1400
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1401
1402
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1403
         },
1404
         "DST_VAL2": {
1405
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1406
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1410
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1412
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1413
             }
1414
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1415
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1416
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1417
1418
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1419
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1420
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1421
1422
             "subtopic": "Other income",
1423
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1424
                 "1- 999,999": "Amount withdrawn or distributed"
1425
             }
1426
         },
1427
1428
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1429
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1430
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1431
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1432
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1433
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1434
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1436
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1437
1438
                 "2": "No"
             }
1439
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1440
1441
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1442
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1445
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1446
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1447
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1449
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1450
                 "2": "No"
1451
             }
1452
         },
1453
1454
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1455
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1456
1457
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1458
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1459
1460
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1461
1462
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                 "1- 99,999": "Dollar amount"
1463
1464
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1465
         },
1466
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1467
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1468
1469
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1470
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1471
1472
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1473
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1474
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1475
                 "2": "No"
1476
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1477
             }
         },
1478
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1479
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1480
                 during 20.. ?",
             "universe": "FIN_YN = 1",
1481
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1482
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1483
             "topic": "Income",
1484
             "subtopic": "Other income",
1485
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1486
1487
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                 "1-999999": "Financial assistance"
1488
             }
1489
         },
1490
1491
         "FIN_YN": {
1492
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             "universe": "All Persons aged 15+",
1493
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1494
1495
             "role": "Independent",
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1496
1497
             "subtopic": "Other income",
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1498
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1499
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1500
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1501
1502
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1503
1504
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1505
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1506
1507
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1508
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1509
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1510
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1511
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1512
1513
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1514
         },
1515
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1516
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1517
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1518
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1519
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1520
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1521
             "subtopic": "Other income",
1522
1523
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1524
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1525
                 "2": "No"
1526
             }
1527
1528
         },
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1529
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1530
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1531
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1532
             "role": "Independent",
1533
1534
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             "subtopic": "Other income",
1535
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1536
1537
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                 "1": "Yes",
1538
                 "2": "No"
1539
             }
1540
1541
         },
1542
         "OED_TYP2": {
             "label": "Source 2 other than gi bill received (OED_TYP2-
1543
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1544
             "type": "Categorical",
1545
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1546
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1547
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1548
             "values": {
1549
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1550
                 "1": "Yes",
1551
                 "2": "No"
1552
             }
1553
         },
1554
         "OED_TYP3": {
1555
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1556
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1557
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1558
             "role": "Independent",
1559
             "topic": "Income",
1560
             "subtopic": "Other income",
1561
             "values": {
1562
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1563
1564
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                 "2": "No"
1565
1566
             }
1567
         },
1568
         "OI_OFF": {
1569
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1570
             "universe": "OI_YN = 1",
1571
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1572
             "role": "Independent",
1573
             "topic": "Income",
             "subtopic": "Other income",
1574
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1575
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1577
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1578
                 "3": "Afdc",
1579
1580
                 "4": "Other public assistance",
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                 "7": "Rents or royalties",
1583
                 "8": "Estates or trusts",
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1585
                 "10": "Disability payments (own insurance)",
1586
                 "11": "Unemployment compensation",
1587
                 "12": "Strike benefits",
1588
                 "13": "Annuities or paid up insurance policies",
1589
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1590
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1591
                 "16": "Wages or salary",
1592
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1593
                 "18": "Farm self-employment",
1594
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1595
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1596
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1597
1598
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1600
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1602
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1603
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1604
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1605
1606
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1607
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                 "1-999999": "Other income"
1608
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1609
1610
         },
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1611
1612
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1613
1614
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1615
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1616
1617
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1618
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1619
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1620
                 "2": "No"
1621
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1622
1623
         },
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1624
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1625
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1626
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1627
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1628
             "topic": "Income",
1629
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1630
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1631
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1632
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1633
                 "2": "Union pension",
1634
                 "3": "Federal government pension",
1635
                 "4": "State government pension",
1636
                 "5": "Local government pension",
1637
1638
                 "6": "Us military pension",
1639
                 "7": "Us railroad retirement",
                 "8": "Other"
1640
1641
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1642
         },
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1643
1644
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             "universe": "PEN_VAL2 > 0",
1645
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1646
1647
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1648
             "subtopic": "Other income",
1649
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1650
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1651
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1652
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                 "2": "Union pension",
1653
1654
                 "3": "Federal government pension",
                 "4": "State government pension",
1655
1656
                 "5": "Local government pension",
                 "6": "Us military pension",
1657
                 "7": "Us railroad retirement",
1658
                 "8": "Other"
1659
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1660
         },
1661
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1662
1663
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1664
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1665
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1666
1667
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1668
             "subtopic": "Other income",
1669
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1670
1671
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             }
1672
1673
         },
1674
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1675
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1676
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1677
1678
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1679
1680
             "subtopic": "Other income",
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1681
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1682
1683
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             }
1684
         },
1685
1686
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1687
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1690
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1691
             "subtopic": "Other income",
1692
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1693
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1694
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1695
                 "2": "No"
1696
             }
1697
         },
1698
1699
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1700
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1701
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1702
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1703
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1704
             "subtopic": "Other income",
1705
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1706
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1707
1708
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1709
1710
         },
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1711
1712
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1713
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1714
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1715
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1716
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             "subtopic": "Other income",
1717
1718
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1719
1720
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                 "positive amt": "Income"
1721
1722
             }
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1723
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1725
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1726
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1727
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1728
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1729
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1730
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1731
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1732
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1733
                 "2": "Disabled (adult or child)",
1734
                 "3": "Widowed",
1735
                 "4": "Spouse",
1736
                 "5": "Surviving child",
1737
                 "6": "Dependent child",
1738
                 "7": "On behalf of surviving, dependent, or disabled child(ren)
1739
                    ш,
1740
                 "8": "Other (adult or child)"
             }
1741
1742
         },
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1743
1744
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1745
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1746
             "type": "Categorical",
1747
             "role": "Independent",
             "topic": "Income",
1748
             "subtopic": "Other income",
1749
             "values": {
1750
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1751
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1752
                 "2": "Disabled (adult or child)",
1753
                 "3": "Widowed",
1754
1755
                 "4": "Spouse",
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1756
                 "6": "Dependent child",
1757
                 "7": "On behalf of surviving, dependent, or disabled child(ren)
1758
                 "8": "Other (adult or child)"
1759
             }
1760
1761
         },
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1762
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1763
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1764
1765
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             "role": "Independent",
1766
             "topic": "Income",
1767
             "subtopic": "Other income",
1768
             "values": {
1769
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1770
                 "1": "Disabled (adult or child)",
1771
                 "2": "Blind (adult or child)",
1772
1773
                 "3": "On behalf of a disabled child",
                 "4": "On behalf of a blind child",
1774
1775
                 "5": "Other (adult or child)"
             }
1776
1777
         },
1778
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1779
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1780
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1781
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             "role": "Independent",
1782
             "topic": "Income",
1783
1784
             "subtopic": "Other income",
             "values": {
1785
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1786
                 "1": "Disabled (adult or child)",
1787
1788
                 "2": "Blind (adult or child)",
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1789
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1790
                 "4": "On behalf of a blind child",
                 "5": "Other (adult or child)"
1791
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1792
1793
         },
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1794
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1795
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1796
1797
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1798
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1799
             "subtopic": "Other income",
1800
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1801
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1802
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1803
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1804
1805
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1806
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1807
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1808
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1809
1810
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             "topic": "Income",
1811
1812
             "subtopic": "Other income",
1813
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1814
1815
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1816
                 "2": "No"
             }
1817
1818
         },
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1820
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1821
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1822
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1823
1824
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1826
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1828
                 "2": "403b account",
1829
                 "3": "Roth ira",
1830
                 "4": "Regular ira",
1831
                 "5": "Keogh plan",
1832
                 "6": "Sep plan (simplified employee pension)",
1833
                 "7": "Other type of retirement account"
1834
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1835
1836
         },
         "RINT_SC2": {
1837
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1838
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1839
1840
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1841
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1842
             "subtopic": "Other income",
1843
             "values": {
1844
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1845
1846
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                 "2": "403b account",
1847
1848
                 "3": "Roth ira",
                 "4": "Regular ira",
1849
                 "5": "Keogh plan",
1850
                 "6": "Sep plan (simplified employee pension)",
1851
                 "7": "Other type of retirement account"
1852
             }
1853
         },
1854
         "RINT_VAL1": {
1855
1856
             "label": "Interest income amt, retirement source 1",
             "universe": "RINT_SC1 > 0",
1857
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1858
             "role": "Independent",
1859
             "topic": "Income",
1860
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"subtopic": "Other income",
1861
1862
             "values": {
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1863
                 "1-999999": "Ret interest income"
1864
1865
             }
1866
         },
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1867
1868
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1869
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1870
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1871
1872
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1873
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1874
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1875
                 "1-999999": "Ret interest income"
1876
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1877
1878
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1879
1880
             "label": "Interest income - retirement, y/n",
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1881
1882
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1883
1884
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1885
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1886
1887
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                 "1": "Yes",
1888
                 "2": "No"
1889
             }
1890
1891
         },
1892
         "RNT_VAL": {
1893
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                 expenses during 20..?",
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1894
             "type": "Continuous",
1895
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1896
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1897
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1898
             "values": {
1899
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1900
                 "-9999-999999": "Rental income"
1901
             }
1902
1903
         },
1904
         "RNT_YN": {
             "label": "Did ... own any land, property, rented to others, or
1905
                 receive income from royalties, roomers or boarders, or from
                 estates or trusts?",
             "universe": "All Persons aged 15+",
1906
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1907
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1908
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1909
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1910
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1911
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1912
                 "1": "Yes",
1913
                 "2": "No"
1914
1915
             }
1916
         },
1917
         "SRVS_VAL": {
1918
             "label": "Total amount of survivor's income received (combined
                 amounts in edited sources sur_val1 and sur_val2 plus the
                 unedited sources 3 & 4 starting in 1995)",
1919
             "universe": "SUR_YN = 1",
1920
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             "role": "Independent",
1921
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1922
1923
             "subtopic": "Other income",
             "values": {
1924
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1925
                 "1-999999": "Income amount"
1926
1927
             }
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},
1928
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1929
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1930
                 during 20.. ?",
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1931
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1932
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1933
             "topic": "Income",
1934
             "subtopic": "Other income",
1935
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1936
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1937
1938
                 "1-99999": "Social security"
             }
1939
         },
1940
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1941
1942
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                 themselves or as combined payments with other family members?",
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1943
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1944
1945
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             "topic": "Income",
1946
1947
             "subtopic": "Other income",
1948
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1949
                 "1": "Yes",
1950
                 "2": "No"
1951
1952
             }
         },
1953
1954
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             "label": "How much did ... receive in supplemental security income
1955
                 during 20..?",
1956
             "universe": "SSI_YN = 1",
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1957
             "role": "Independent",
1958
             "topic": "Income",
1959
             "subtopic": "Other income",
1960
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"values": {
1961
1962
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1963
                 "1-99999": "Supplemental security income"
             }
1964
1965
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1966
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1967
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1968
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1969
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1970
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1971
1972
             "subtopic": "Other income",
             "values": {
1973
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1974
                 "1": "Yes",
1975
                 "2": "No"
1976
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1977
1978
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1979
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1980
                 unemployment or strike benefits?",
1981
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1982
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             "role": "Independent",
1983
             "topic": "Income",
1984
             "subtopic": "Other income",
1985
1986
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1987
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1988
                 "2": "No"
1989
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1990
1991
         },
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1992
1993
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                 unemployment benefits?",
1994
             "universe": "UC_YN = 1",
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1995
1996
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             "topic": "Income",
1997
1998
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1999
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2000
                 "1": "Yes",
2001
                 "2": "No"
2002
2003
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2004
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2005
2006
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                 income?",
             "universe": "SUR_YN = 1",
2007
             "type": "Categorical",
2008
             "role": "Independent",
2009
             "topic": "Income",
2010
             "subtopic": "Other income",
2011
             "values": {
2012
2013
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                 "1": "Company or union survivor pension",
2014
2015
                 "2": "Federal government",
                 "3": "Us military retirement survivor pension",
2016
                 "4": "State or local gov't survivor pension",
2017
                 "5": "Us railroad retirement survivor pension",
2018
2019
                 "6": "Worker compensation survivor",
2020
                 "7": "Black lung",
                 "8": "Regular payments from estates or trusts",
2021
2022
                 "9": "Regular payments from annuities or paid-up life insurance
                    ш,
                 "10": "Other or don't know"
2023
2024
             }
2025
         },
2026
         "SUR_SC2": {
2027
             "label": "What was the source of this other widow or survivor
                 income?",
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"universe": "SUR_YN = 1",
2028
2029
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2030
             "role": "Independent",
             "topic": "Income",
2031
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2032
             "values": {
2033
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2034
                 "1": "Company or union survivor pension",
2035
                 "2": "Federal government",
2036
                 "3": "Us military retirement survivor pension",
2037
                 "4": "State or local gov't survivor pension",
2038
                 "5": "Us railroad retirement survivor pension",
2039
                 "6": "Worker compensation survivor",
2040
                 "7": "Black lung",
2041
                 "8": "Regular payments from estates or trusts",
2042
2043
                 "9": "Regular payments from annuities or paid-up life insurance
                 "10": "Other or don't know"
2044
             }
2045
2046
         },
         "SUR_VAL1": {
2047
2048
             "label": "How much did ... receive (survivor source type) during
                20.. ?",
2049
             "universe": "SUR_YN = 1",
2050
             "type": "Continuous",
             "role": "Independent",
2051
             "topic": "Income",
2052
             "subtopic": "Other income",
2053
             "values": {
2054
                 "0": "None or niu",
2055
                 "1-999,999": "Survivor's income"
2056
2057
             }
2058
         },
2059
         "SUR_VAL2": {
             "label": "How much did ... receive (source type) during 20.. ?",
2060
2061
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2062
2063
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2064
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2065
2066
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                 "O": "None or niu",
2067
                 "1-999,999": "Survivor's income"
2068
             }
2069
2070
         },
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2071
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2072
                  widow's pensions, estates, trusts, insurance annuities, or
                 other survivor's income?",
             "universe": "All Persons aged 15+",
2073
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2074
             "role": "Independent",
2075
             "topic": "Income",
2076
             "subtopic": "Other income",
2077
             "values": {
2078
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2079
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2080
                 "2": "No"
2081
             }
2082
2083
         },
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2084
2085
             "label": "Interest amount, exlcuding retirment account interest",
2086
             "universe": "INT_YN = 1",
             "type": "Continuous",
2087
2088
             "role": "Independent",
             "topic": "Income",
2089
             "subtopic": "Other income",
2090
2091
             "values": {
                 "all": "Dollar value"
2092
2093
             }
2094
         },
2095
         "UC_VAL": {
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2096
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                 20..?",
             "universe": "UC_YN = 1",
2097
             "type": "Continuous",
2098
2099
             "role": "Independent",
             "topic": "Income",
2100
             "subtopic": "Other income",
2101
             "values": {
2102
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2103
                 "1-99999": "Unemployment compensation"
2104
             }
2105
2106
         },
         "UC_YN": {
2107
2108
             "label": "Any type of unemployment compensation? (Combination of
                 subuc, strkuc, and uctot_yn)",
             "universe": "UC_YN = 1",
2109
2110
             "type": "Categorical",
             "role": "Independent",
2111
             "topic": "Income",
2112
2113
             "subtopic": "Other income",
             "values": {
2114
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2115
                 "1": "Yes",
2116
                 "2": "No"
2117
             }
2118
2119
         },
2120
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             "label": "What type of veterans payments did .... receive? (
2121
                 VET_TYP1- disability compensation?)",
2122
             "universe": "VET_YN = 1",
             "type": "Categorical",
2123
2124
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             "topic": "Income",
2125
             "subtopic": "Other income",
2126
             "values": {
2127
2128
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"1": "Yes",
2129
                 "2": "No"
2130
             }
2131
         },
2132
         "VET_TYP2": {
2133
             "label": "What type of veterans payments did .... receive? (
2134
                 VET_TYP2- survivor benefits?)",
             "universe": "VET_YN = 1",
2135
2136
             "type": "Categorical",
             "role": "Independent",
2137
             "topic": "Income",
2138
2139
             "subtopic": "Other income",
             "values": {
2140
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2141
                 "1": "Yes",
2142
                 "2": "No"
2143
             }
2144
2145
         },
         "VET_TYP3": {
2146
2147
             "label": "What type of veterans payments did .... receive? (
                 VET_TYP3- veteran's pension?)",
2148
             "universe": "VET_YN = 1",
2149
             "type": "Categorical",
2150
             "role": "Independent",
             "topic": "Income",
2151
             "subtopic": "Other income",
2152
2153
             "values": {
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2154
                 "1": "Yes",
2155
                 "2": "No"
2156
             }
2157
2158
         },
         "VET_TYP4": {
2159
2160
             "label": "What type of veterans payments did .... receive? (
                 VET_TYP4- education assistance?)",
2161
             "universe": "VET_YN = 1",
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"type": "Categorical",
2162
2163
             "role": "Independent",
             "topic": "Income",
2164
2165
             "subtopic": "Other income",
             "values": {
2166
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2167
                 "1": "Yes",
2168
                 "2": "No"
2169
2170
             }
         },
2171
         "VET_TYP5": {
2172
2173
             "label": "What type of veterans payments did .... receive? (
                 VET_TYP5- other veteran's payments?)",
             "universe": "VET_YN = 1",
2174
             "type": "Categorical",
2175
             "role": "Independent",
2176
             "topic": "Income",
2177
             "subtopic": "Other income",
2178
             "values": {
2179
                 "0": "Niu",
2180
                 "1": "Yes",
2181
                 "2": "No"
2182
             }
2183
2184
         },
2185
         "VET_VAL": {
             "label": "How much did ... receive from veterans' administration
2186
                 during 20..?",
2187
             "universe": "VET_YN = 1",
2188
             "type": "Continuous",
2189
             "role": "Independent",
             "topic": "Income",
2190
2191
             "subtopic": "Other income",
             "values": {
2192
                 "0": "None or niu",
2193
                 "1-999999": "Veterans' payments"
2194
2195
             }
```

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},
2196
         "VET_YN": {
2197
2198
             "label": "Did ... receive veterans' payments?",
2199
             "universe": "All Persons aged 15+",
2200
             "type": "Categorical",
             "role": "Independent",
2201
             "topic": "Income",
2202
             "subtopic": "Other income",
2203
2204
             "values": {
                 "0": "Niu",
2205
                 "1": "Yes",
2206
                 "2": "No"
2207
             }
2208
2209
         },
         "WC_TYPE": {
2210
2211
             "label": "What was source of these payments?",
             "universe": "WC_YN = 1",
2212
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2213
             "role": "Independent",
2214
2215
             "topic": "Income",
             "subtopic": "Other income",
2216
2217
             "values": {
                 "0": "Not in universe",
2218
2219
                 "1": "State worker's compensation",
2220
                 "2": "Employer or employers insurance",
2221
                 "3": "Own insurance",
                 "4": "Other"
2222
2223
             }
2224
         },
         "WC_VAL": {
2225
             "label": "How much compensation did ... receive during 20..?",
2226
2227
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             "type": "Continuous",
2228
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2229
             "topic": "Income",
2230
2231
             "subtopic": "Other income",
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"values": {
2232
2233
                 "0": "None or niu",
                 "1-99999": "Worker's compensation"
2234
             }
2235
2236
         },
         "WC_YN": {
2237
2238
             "label": "During 20.. did ... receive any worker's compensation
                 payments or other payments as a result of a job related injury
                 or illness?",
             "universe": "All Persons aged 15+",
2239
             "type": "Categorical",
2240
             "role": "Independent",
2241
             "topic": "Income",
2242
             "subtopic": "Other income",
2243
             "values": {
2244
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2245
                 "1": "Yes",
2246
                 "2": "No"
2247
             }
2248
2249
         },
         "PAW_TYP": {
2250
2251
             "label": "What type of program did... receive CASH assistance?",
             "universe": "PAW_YN = 1",
2252
2253
             "type": "Categorical",
             "role": "Independent",
2254
2255
             "topic": "Income",
             "subtopic": "Non-cash benefits",
2256
             "values": {
2257
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2258
                 "1": "TANF/AFDC",
2259
                 "2": "Other",
2260
2261
                 "3": "Both"
             }
2262
2263
         },
         "PAW_VAL": {
2264
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2265
             "label": "How much did ... receive in public assistance or welfare
                 during 20..?",
             "universe": "PAW_YN = 1",
2266
             "type": "Continuous",
2267
2268
             "role": "Independent",
             "topic": "Income",
2269
             "subtopic": "Non-cash benefits",
2270
             "values": {
2271
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2272
                 "1-99999": "Public assistance"
2273
             }
2274
2275
         },
         "PAW_YN": {
2276
2277
             "label": "At any time during 20.., even for one month, did...
                 receive an CASH assistance from a state or county welfare
                 program such as (State program name fill)?",
2278
             "universe": "All Persons aged 15+",
             "type": "Categorical",
2279
             "role": "Independent",
2280
2281
             "topic": "Income",
             "subtopic": "Non-cash benefits",
2282
2283
             "values": {
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2284
                 "1": "Yes",
2285
                 "2": "No"
2286
2287
             }
2288
         },
         "PENINCL": {
2289
2290
             "label": "Was ... included in that plan?",
             "universe": "PENPLAN = 1",
2291
             "type": "Categorical",
2292
2293
             "role": "Independent",
             "topic": "Income",
2294
             "subtopic": "Non-cash benefits",
2295
             "values": {
2296
2297
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"1": "Yes",
2298
                 "2": "No"
2299
             }
2300
         },
2301
         "PENPLAN": {
2302
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2303
                  ... worked for in 20.. have a pension or other type of
                 retirement plan?",
2304
             "universe": "WRK_CK = 1",
             "type": "Categorical",
2305
2306
             "role": "Independent",
2307
             "topic": "Income",
             "subtopic": "Non-cash benefits",
2308
             "values": {
2309
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2310
                 "1": "Yes",
2311
                 "2": "No"
2312
             }
2313
         },
2314
         "WICYN": {
2315
             "label": "Who received WIC?",
2316
2317
             "universe": "Adult female",
2318
             "type": "Categorical",
2319
             "role": "Independent",
             "topic": "Income",
2320
2321
             "subtopic": "Non-cash benefits",
             "values": {
2322
2323
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2324
                 "1": "Received WIC",
2325
                 "2": "Did not receive WIC"
             }
2326
2327
         },
         "CHCARE_YN": {
2328
2329
             "label": "Paid child care was needed for this child?",
2330
             "universe": "Persons age 15+ with children",
2331
             "type": "Categorical",
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"role": "Independent",
2332
2333
             "topic": "Income",
2334
             "subtopic": "Supplemental poverty measure",
             "values": {
2335
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2336
                 "1": "Yes",
2337
                 "2": "No"
2338
             }
2339
         },
2340
         "CHELSEW_YN": {
2341
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2342
                 household?",
             "universe": "All persons aged 15+",
2343
             "type": "Categorical",
2344
             "role": "Independent",
2345
             "topic": "Income",
2346
             "subtopic": "Supplemental poverty measure",
2347
             "values": {
2348
                 "0": "Niu",
2349
                 "1": "Yes",
2350
                 "2": "No"
2351
2352
             }
2353
         },
2354
         "CHELSEW_YN": {
2355
             "label": "Does this person have a child living outside the
                 household?",
2356
             "universe": "All persons aged 15+",
             "type": "Categorical",
2357
2358
             "role": "Independent",
             "topic": "Income",
2359
             "subtopic": "Supplemental poverty measure",
2360
2361
             "values": {
                 "0": "Niu",
2362
                 "1": "Yes",
2363
                 "2": "No"
2364
2365
             }
```

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},
2366
         "CHSP_VAL": {
2367
             "label": "What is the annual amount of child support paid?",
2368
             "universe": "CHSP_YN = 1",
2369
2370
             "type": "Continuous",
             "role": "Independent",
2371
             "topic": "Income",
2372
             "subtopic": "Supplemental poverty measure",
2373
2374
             "values": {
                 "0": "Niu",
2375
                 "1-99999": "Amount paid in child support"
2376
             }
2377
         },
2378
         "CHSP_YN": {
2379
             "label": "Is this person required to pay child support?",
2380
             "universe": "CHELSEW_YN",
2381
2382
             "type": "Categorical",
             "role": "Independent",
2383
             "topic": "Income",
2384
2385
             "subtopic": "Supplemental poverty measure",
             "values": {
2386
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2387
                 "1": "Yes",
2388
                 "2": "No"
2389
             }
2390
2391
         },
2392
         "CSP_VAL": {
             "label": "How much did ... receive in child support payments?",
2393
2394
             "universe": "CHSP_YN = 1",
             "type": "Continuous",
2395
             "role": "Independent",
2396
2397
             "topic": "Income",
             "subtopic": "Supplemental poverty measure",
2398
             "values": {
2399
                 "0": "None or niu",
2400
                 "1-99999": "Child support"
2401
```

```
2402
             }
2403
         },
         "CSP_YN": {
2404
             "label": "Did ... receive child support payments?",
2405
2406
             "universe": "All Persons aged 15+",
             "type": "Categorical",
2407
             "role": "Independent",
2408
             "topic": "Income",
2409
             "subtopic": "Supplemental poverty measure",
2410
             "values": {
2411
                 "0": "Niu",
2412
                 "1": "Yes",
2413
                 "2": "No"
2414
             }
2415
2416
         },
         "ACTC_CRD": {
2417
2418
             "label": "Additional child tax credit",
2419
             "universe": "Tax unit head or dependent filer",
             "type": "Continuous",
2420
2421
             "role": "Independent",
             "topic": "Income",
2422
2423
             "subtopic": "Tax model items",
2424
             "values": {
                 "0": "None",
2425
                 "1-99999": "Dollar amount"
2426
2427
             }
2428
         },
         "AGI": {
2429
2430
             "label": "Adjusted gross income",
2431
             "universe": "Tax unit head or dependent filer",
             "type": "Continuous",
2432
2433
             "role": "Independent",
             "topic": "Income",
2434
             "subtopic": "Tax model items",
2435
             "values": {
2436
                 "0": "None",
2437
```

```
2438
                 "-9999-999999": "Dollar amount"
2439
             }
2440
         },
         "CTC_CRD": {
2441
2442
             "label": "Child tax credit",
2443
             "universe": "Tax unit head or dependent filer",
             "type": "Continuous",
2444
             "role": "Independent",
2445
             "topic": "Income",
2446
             "subtopic": "Tax model items",
2447
             "values": {
2448
2449
                 "0": "None",
                 "1-99999": "Dollar amount"
2450
             }
2451
2452
         },
2453
         "EIT_CRED": {
2454
             "label": "Earn income tax credit",
2455
             "universe": "Tax unit head or dependent filer",
             "type": "Continuous",
2456
2457
             "role": "Independent",
             "topic": "Income",
2458
2459
             "subtopic": "Tax model items",
2460
             "values": {
2461
                 "0": "None",
                 "1-9999": "Dollar amount"
2462
2463
             }
2464
         },
         "FED_RET": {
2465
2466
             "label": "Federal retirement payroll deduction",
2467
             "universe": "Tax unit head or dependent filer",
             "type": "Continuous",
2468
2469
             "role": "Independent",
             "topic": "Income",
2470
             "subtopic": "Tax model items",
2471
             "values": {
2472
                 "0": "None",
2473
```

```
"1-999999": "Dollar amount"
2474
2475
             }
2476
         },
         "FEDTAX_AC": {
2477
2478
             "label": "Federal income tax liability, after all credits",
             "universe": "Tax unit head or dependent filer",
2479
             "type": "Continuous",
2480
             "role": "Independent",
2481
             "topic": "Income",
2482
             "subtopic": "Tax model items",
2483
             "values": {
2484
2485
                 "0": "None",
                 "-9999-999999": "Dollar amount"
2486
             }
2487
2488
         },
         "FEDTAX_BC": {
2489
2490
             "label": "Federal income tax liability, before credits",
             "universe": "Tax unit head or dependent filer",
2491
             "type": "Continuous",
2492
2493
             "role": "Independent",
             "topic": "Income",
2494
2495
             "subtopic": "Tax model items",
2496
             "values": {
2497
                 "0": "None",
                 "-9999-999999": "Dollar amount"
2498
2499
             }
2500
         },
2501
         "FICA": {
2502
             "label": "Social security retirement payroll deduction",
2503
             "universe": "All persons",
             "type": "Continuous",
2504
2505
             "role": "Independent",
             "topic": "Income",
2506
             "subtopic": "Tax model items",
2507
             "values": {
2508
                 "0": "None",
2509
```

```
"1-99999": "Dollar amount"
2510
2511
             }
2512
         },
         "FILESTAT": {
2513
2514
             "label": "Tax filer status",
             "universe": "All persons",
2515
             "type": "Categorical",
2516
             "role": "Independent",
2517
             "topic": "Income",
2518
             "subtopic": "Tax model items",
2519
             "values": {
2520
2521
                 "1": "Joint, both<65",
                 "2": "Joint, one ><65 \& one 65+",
2522
                 "3": "Joint, both 65+",
2523
                 "4": "Head of household",
2524
                 "5": "Single",
2525
                 "6": "Non-filer"
2526
             }
2527
2528
         },
2529
         "MARG_TAX": {
             "label": "Marginal tax rate",
2530
2531
             "universe": "Tax unit head or dependent filer",
2532
             "type": "Continuous",
2533
             "role": "Independent",
             "topic": "Income",
2534
2535
             "subtopic": "Tax model items",
2536
             "values": {
                 "0": "None",
2537
2538
                 "1-99": "Marginal rate"
2539
             }
2540
         },
2541
         "PRSWKXPNS": {
2542
             "label": "Work expenses",
2543
             "universe": "A_AGE > 17 or HHDFMX = 1,2,46, or 47",
2544
             "type": "Continuous",
             "role": "Independent",
2545
```

```
"topic": "Income",
2546
2547
             "subtopic": "Tax model items",
             "values": {
2548
                 "0": "None",
2549
2550
                 "1-1999": "Dollar amount"
             }
2551
2552
         },
         "STATETAX_A": {
2553
             "label": "State income tax liability, after all credits",
2554
2555
             "universe": "Tax unit head or dependent filer",
             "type": "Continuous",
2556
2557
             "role": "Independent",
             "topic": "Income",
2558
             "subtopic": "Tax model items",
2559
             "values": {
2560
                 "0": "None",
2561
2562
                 "-9999-999999": "Dollar amount"
2563
             }
         },
2564
2565
         "STATETAX_B": {
             "label": "State income tax liability, before credits",
2566
2567
             "universe": "Tax unit head or dependent filer",
2568
             "type": "Continuous",
2569
             "role": "Independent",
             "topic": "Income",
2570
             "subtopic": "Tax model items",
2571
             "values": {
2572
                 "0": "None",
2573
2574
                 "-9999-999999": "Dollar amount"
             }
2575
2576
         },
2577
         "TAX_INC": {
             "label": "Taxable income amount",
2578
2579
             "universe": "Tax unit head or dependent filer",
2580
             "type": "Continuous",
             "role": "Independent",
2581
```

```
"topic": "Income",
2582
2583
             "subtopic": "Tax model items",
2584
             "values": {
                 "0": "None",
2585
                 "-9999-999999": "Dollar amount"
2586
             }
2587
2588
         },
         "PERLIS": {
2589
             "label": "Poverty level of persons (Subfamily members have primary
2590
                 family recode)",
             "universe": "All persons",
2591
             "type": "Categorical",
2592
             "role": "Independent",
2593
             "topic": "Poverty",
2594
             "subtopic": "Poverty",
2595
             "values": {
2596
2597
                 "-1": "Not in poverty universe",
                 "1": "Below poverty level",
2598
                 "2": "100 - 124 percent of the poverty level",
2599
                 "3": "125 - 149 percent of the poverty level",
2600
                 "4": "150 and above the poverty level"
2601
2602
             }
2603
         },
2604
         "POV_UNIV": {
2605
             "label": "Poverty universe flag",
2606
             "universe": "All persons",
2607
             "type": "Categorical",
             "role": "Independent",
2608
2609
             "topic": "Poverty",
             "subtopic": "Poverty",
2610
             "values": {
2611
2612
                 "0": "Not in poverty universe",
                 "1": "In poverty universe"
2613
2614
             }
2615
         },
         "HEA": {
2616
```

```
2617
             "label": "Health status",
             "universe": "All persons",
2618
             "type": "Categorical",
2619
             "role": "Independent",
2620
             "topic": "Health insurance",
2621
2622
             "subtopic": "Health status",
             "values": {
2623
                 "1": "Excellent",
2624
                 "2": "Very good",
2625
                 "3": "Good",
2626
                 "4": "Fair",
2627
                 "5": "Poor"
2628
2629
             }
2630
         },
         "SPM_ACTC": {
2631
             "label": "SPM units Additional Child Tax Credit",
2632
             "universe": "All persons",
2633
2634
             "type": "Continuous",
             "role": "Independent",
2635
2636
             "topic": "Supplemental poverty measure",
2637
             "subtopic": "SPM unit characteristics",
             "values": {
2638
                 "0-99999": "Dollar amount"
2639
2640
             }
         }
2641
2642 }
```

3.5.4 Python Modules

The utility module in Code 3.1 is for basic tasks such as creating a directory, backing up existing files before being overwritten, and importing and exporting a dictionary in JSON format. The encoding module in Code 3.2 is used solely during data encoding as its helper, not its main role. The dataset module in Code 3.3 helps importing and exporting dataset in both feather and CSV formats. The first employs LZ4 compression by default to bring a smaller file than the latter. The EDA module in Code 3.4 is primary for cross tabulation analysis. Its result is exported in CSV format, and its chart is saved in SVG, PGF and PDF formats.

Code 3.1: Utility module (module/utility.py)

```
1 import os
  import time
  import json
3
 4
   # Directory
   def create_dir(dir):
 7
       try:
8
          os.makedirs(dir)
9
       except FileExistsError:
10
          pass
11
   # Backup
12
   def backup_duplicate(file_dir, filename, format, backup_dir, info):
13
14
       filepath = f"{file_dir}/{filename}.{format}"
       date = time.strftime("%Y%m%d", time.localtime(time.time()))
15
       if os.path.isfile(filepath):
16
17
           backup_subdir = f"{backup_dir}/{date}/{file_dir.replace('../', '')}
           create_dir(backup_subdir)
18
           filepath_backup = f"{backup_subdir}/{filename}-backup.{format}"
19
           os.replace(filepath, filepath_backup)
20
           if info:
21
               print(f"{filepath} previously exists")
22
```

```
23
              print(f"Back up to {filepath_backup}")
       elif info:
24
           print(f"{filepath} does not previously exists")
25
26
27
   # Import/export dict/JSON
   def import_dict(metadatapath):
28
29
       with open(metadatapath) as myfile:
           indep_contents = myfile.read()
30
       return json.loads(indep_contents)
31
32
   def export_json(dictfile, jsonfile):
33
34
       with open(jsonfile, 'w', encoding='utf-8') as f:
           json.dump(dictfile, f, ensure_ascii=False, indent=4)
35
36
   def export_txt(string, txtfile):
37
       f = open(txtfile, 'w')
38
39
       f.write(string)
       f.close()
40
                   Code 3.2: Encoding module (module/metaencode.py)
1
   import pandas as pd
2
   def extract_dict_cat(indep_dict):
       return {attr: info for (attr, info) in indep_dict.items() if indep_dict
4
           [attr]['type'] == 'Categorical'}
5
   def extract_dict_cont(indep_dict):
       return {attr: info for (attr, info) in indep_dict.items() if indep_dict
7
           [attr]['type'] == 'Continuous'}
8
   def sort_cols(df_indep, indep_dict):
       sorted_cols = sorted(
10
11
           df_indep.head(),
           key=lambda attr: indep_dict[attr]['type'],
12
```

```
13
          reverse=True
14
       )
       return df_indep[sorted_cols]
15
16
17
   def indep_info(df_indep, indep_dict):
18
       df_info = pd.DataFrame({'variable': df_indep.head().columns})
       df_info['type'] = df_info['variable'].apply(lambda attr: indep_dict[
19
           attr]['type'])
20
       minmax = df_indep.agg(['min','max']).values.tolist()
       df_info['min'] = minmax[0]
21
       df_info['max'] = minmax[1]
22
23
       del minmax
24
       return df_info
25
   def count_info(df_info):
26
       df_count = df_info.groupby('type').count().reset_index()[['type','
27
          variable']]
       df_count.rename(columns = {'variable': 'count'}, inplace=True)
28
       df_count.sort_values('type', ascending=False, inplace=True,
29
           ignore_index=True)
       return df_count
30
                     Code 3.3: Dataset module (module/dataset.py)
1 import os
2 import urllib.request
3 import pandas as pd
   import pyarrow
4
5
6
   from module.utility import create_dir, backup_duplicate
7
   # Import
   def import_dataset(dataset_name, feather_dir, sas_dir='', sas_url=''):
       filepath_feather = f"{feather_dir}/{dataset_name}.feather"
10
```

11

```
12
       if os.path.isfile(filepath_feather):
13
           print(f"{filepath_feather} is found")
           print(f"{filepath_feather} was previously preprocessed")
14
           df0 = pd.read_feather(filepath_feather)
15
16
       else:
           print(f"{filepath_feather} is not found")
17
           if sas_dir == '':
18
              raise Exception("SAS data directory is empty")
19
           filepath_sas = f"sas_dir/{dataset_name}.sas7bdat"
20
           if os.path.isfile(filepath_sas):
21
22
              print(f"{filepath_sas} is found")
23
           else:
              print(f"{filepath_sas} is not found")
24
              create_dir('original/data-orig')
25
              print(f"{filepath_sas} will be downloaded")
26
27
              print("Download starts")
28
              try:
                  urllib.request.urlretrieve(sas_url, filepath_sas)
29
                  print("Download finishes")
30
31
              except:
                  raise Exception("Download fails")
32
              print(f"{filepath_sas} is successfully downloaded")
33
34
           df0 = pd.read_sas(filepath_sas)
35
36
       print(f"\nNumber of original data: {len(df0)}")
       df0 = df0[df0['COV']!=0]
37
       print(f"An infant born after calendar year (COV = 0) is excluded")
38
       print(f"Number of training data: {len(df0)}")
39
40
       return df0
41
42 # Export
43
   def export_dataset(df, file_dir, dataset_name, format, info=True,
       backup_dir=''):
44
       create_dir(file_dir)
       if format == 'feather' or format == 'csv':
45
           filepath = f"{file_dir}/{dataset_name}.{format}"
46
```

```
if backup_dir != '':
47
              backup_duplicate(
48
                  file_dir=file_dir, filename=dataset_name,
49
                  format=format,
50
51
                  backup_dir=backup_dir, info=info
              )
52
           if format == 'feather':
53
54
              df.to_feather(filepath)
           else:
55
              df.to_csv(filepath, index=False)
56
           if info:
57
58
              print(f"The dataframe is successfully exported to {filepath}")
       else:
59
           print(f"Input format {format} is unrecognized")
60
                        Code 3.4: EDA module (module/eda.py)
1 import sys
2 import time
3 import pandas as pd
   import matplotlib.pyplot as plt
4
5
   from module.utility import create_dir, backup_duplicate
   from module.dataset import export_dataset
8
9 # Variables
   def describe_var(var_dict, role='independent'):
10
11
       num_cat = 0
       num_cont = 0
12
13
       for key in var_dict:
           if var_dict[key]['type'] == 'Categorical':
14
              num_cat += 1
15
           else:
16
17
              num_cont += 1
```

```
print(f"There are {num_cat + num_cont} {role} variables of interest: {
18
           num_cat} categorical and {num_cont} continuous")
19
20 # Cross Tabulation Analysis
21 def crosstab(df, indep_dict, cont_bins, plot, output_dir, log_filepath,
       backup_dir=''):
       dir_main = f"{output_dir}/tab-cbins-{cont_bins}"
22
23
       for key, val in indep_dict.items():
24
           fname_main = f"{key}-cbins-{cont_bins}"
25
26
27
           if val['type'] == "Categorical":
              crosstb = pd.crosstab(index=df[key].map(lambda x: val['values'
28
                  ][str(x)]), columns=df['code'])
           else:
29
              dat = df[[key, 'code']].copy()
30
31
              dat['bins'] = pd.cut(dat[key], bins=cont_bins)
              crosstb = pd.crosstab(index=dat['bins'],columns=dat['code'])
32
              del dat
33
34
           print(key)
35
36
           print(f"Label: {val['label']}")
           print(f"Universe: {val['universe']}")
37
38
           print(f"Type: {val['type']}")
           print(f"Topic: {val['topic']}")
39
           print(f"Subtopic: {val['subtopic']}")
40
           print("\n")
41
42
           print(f"Code: Employment-based plan (GRP) | Direct-purchase plan (
43
              DIR) | Public health insurance (PUB)")
           print(crosstb)
44
           1.1.1
45
           dir_crosstb = f"{dir_main}/cross-{cont_bins}"
46
           create_dir(dir_crosstb)
47
48
           export_dataset(
              crosstb,
49
```

```
file_dir=f"{dir_crosstb}/feather", dataset_name=f"{fname_main}-
50
                   cross",
               format='feather', info=False,
51
               backup_dir=backup_dir
52
53
           )
           export_dataset(
54
55
               crosstb,
               file_dir=f"{dir_crosstb}/csv", dataset_name=f"{fname_main}-
56
                   cross",
               format='csv', info=False,
57
               backup_dir=backup_dir
58
           )
59
           1 \cdot 1 \cdot 1
60
           print("\n")
61
62
63
           if plot:
64
               barplot = crosstb.plot.bar()
               barplot.legend(title='(GRP,DIR,PUB)',
65
                            bbox_to_anchor=(1,1.02),
66
67
                            loc='upper left')
               plt.title(val['label'])
68
69
               plt.xlabel(key)
               plt.ylabel('Frequency')
70
71
               ls_format = ['svg', 'pgf', 'pdf']
               for format in ls_format:
                   dir_fig = f"{dir_main}/figures/{format}"
73
                   figname = f"{key}-cbins-{cont_bins}"
74
                   figpath = f"{dir_fig}/{figname}.{format}"
75
                   create_dir(dir_fig)
76
                   backup_duplicate(
77
                       file_dir=dir_fig, filename=figname,
78
79
                       format=format,
                       backup_dir=backup_dir, info=False
80
                   )
81
82
                   f = open(log_filepath, 'a')
                   temp = sys.stdout
83
```

```
84
                   sys.stdout = f
                   count, tries = 0, 4
85
                   success = False
86
                   while count < tries:</pre>
87
88
                      try:
                          plt.savefig(figpath, bbox_inches='tight')
89
                          success = True
90
                          break
91
                      except:
92
93
                          pass
                      count += 1
94
95
                   if not success:
                      curtime = time.strftime("%Y-%m-%d %H:%M:%S", time.
96
                          localtime(time.time()))
                      print(f"{curtime} | {key}: {figpath} cannot be saved")
97
98
                   sys.stdout = temp
99
                   f.close()
               #plt.show()
100
101
102
           dftb = crosstb.reset_index().rename_axis(None, axis=1)
           dftb[dftb.columns[1:]] = dftb[dftb.columns[1:]].astype('uint32')
103
104
           export_dataset(
105
               dftb,
106
               file_dir=f"{dir_main}/feather", dataset_name=fname_main,
               format='feather', info=False,
107
108
               backup_dir=backup_dir
109
           export_dataset(
110
111
               dftb,
112
               file_dir=f"{dir_main}/csv", dataset_name=fname_main,
               format='csv', info=False,
113
114
               backup_dir=backup_dir
           )
115
           print("\n----")
116
```

3.5.5 Python Classes

Pandas DataFrame is a two-dimensional columnwise data structure. Each column must have the same data type. Although it provides by default rich functionality for data manipulation, additional namespaces can be added to pandas objects by registering custom accessors to serve specific purposes. Health insurance dataset in SAS7BDAT file format is imported as a Pandas DataFrame. All columns are numerical, either int64 or float64.

With the thesis namespace (Code 3.5), the data type of a column can be of smaller size through the retype method, three dependent variables of interest (GRP, DIR and PUB) can be coded to a string of three character literals, either Y (Yes) or N (No), by the code method, and these eight different codes are regrouped to five with numerical values assigned by the recode method. Since some categorical values do not start from 0 up to a positive integer as required by the box classifier proposed in Chapter 4, they are encoded to be in this format via the data namespace (Code 3.6). Any numerical flags representing a continuous NIU (not in universe) value are converted to zero to become more meaningful. A categorical NIU value is already changed by the previous reordering. The info namespace (Code 3.7) sets the number of splitting values or cuts as given on a feature appropriately, not exceeding the number of all possible values for a categorical feature.

Code 3.5: ThesisExtension class (cls/ThesisExtension.py)

```
1
   import re
   import pandas as pd
3
   @pd.api.extensions.register_dataframe_accessor("thesis")
 5
   class ThesisExtension:
       def __init__(self, pandas_obj):
 6
           #self._validate(pandas_obj, list(indep_dict.keys()) + ['COV'] +
               dep_attrs)
 8
           self.dataset = pandas_obj
9
       1.1.1
10
       Ostaticmethod
11
       def _validate(obj, cols):
12
13
           if any(x not in obj.columns for x in cols):
               raise AttributeError("Some attributes are missing")
14
```

```
15
        1 \cdot 1 \cdot 1
16
17
       def select(self, cols):
           self.dataset.drop(self.dataset.columns.difference(cols), axis=1,
18
               inplace=True)
19
       def show_type(self, option='short'):
20
           if option.lower() == 'full':
21
               with pd.option_context('display.max_rows', None, 'display.
22
                   max_columns', None):
23
                   print(self.dataset.dtypes)
24
           else:
               print(self.dataset.dtypes)
25
26
        Ostaticmethod
27
28
       def retype(ser):
29
           if all(ser.apply(lambda x: isinstance(x, int))):
30
               flag_int = True
           elif all(ser.apply(lambda x: x.is_integer())):
31
32
               flag_int = True
33
           else:
34
               flag_int = False
35
36
           if flag_int:
37
               if all(ser.apply(lambda x: x>=0)):
                   if max(ser) <= 255:</pre>
38
39
                       return ser.astype('uint8')
                   elif max(ser) <= 65535:</pre>
40
                       return ser.astype('uint16')
41
                   else:
42
                       return ser.astype('uint32')
43
44
               else:
                   if min(ser) >= -128 and max(ser) <= 127:
45
                       return ser.astype('int8')
46
                   elif min(ser) \geq -32768 and max(ser) \leq 32767:
47
                       return ser.astype('int16')
48
```

```
49
                  else:
                      return ser.astype('int32')
50
           else:
51
              return ser.astype('float32')
52
53
       def code(self, indep_dict, dep_attrs):
54
           self.select(list(indep_dict.keys()) + ['COV'] + dep_attrs)
55
           for v in indep_dict.keys():
56
              if indep_dict[v]['type'] == 'Categorical':
57
                  self.dataset[v] = self.dataset[v].astype('int8').astype('
58
                      category')
59
              else:
                  self.dataset[v] = self.retype(self.dataset[v])
60
           self.dataset['COV'] = self.dataset['COV'].astype('int8').astype('
61
              category')
           self.dataset[dep_attrs] = self.dataset[dep_attrs].astype('int8')
62
63
           self.dataset['class_orig'] = 0
           self.dataset['code_orig'] = ""
64
           for v in dep_attrs:
65
66
              self.dataset[v] = self.dataset[v].replace([2.0, 1.0], [False,
                  True])
67
              self.dataset['class_orig'] = 2*self.dataset['class_orig'] +
                  self.dataset[v]
68
              self.dataset['code_orig'] = self.dataset['code_orig'] + self.
                  dataset[v].replace([True, False], ['Y', 'N'])
           self.dataset[dep_attrs] = self.dataset[dep_attrs].astype('category'
69
           self.dataset['class_orig'] = self.dataset['class_orig'].astype('
70
              int8').astype('category')
           self.dataset['code_orig'] = self.dataset['code_orig'].astype('
71
              category')
72
       def recode(self):
73
74
           self.dataset['code'] = self.dataset['code_orig'].apply(
              lambda v: 'NY_' if re.match('(NY)', v)
75
```

```
76
              else 'Y1Y' if re.match(r'^Y(?:\w*Y)', v) # Raw string to
                  prevent invalid escape sequence '\w'
77
              else v
           ).astype('category')
78
           self.dataset['class'] = self.dataset[['class_orig', 'code']].apply(
79
              lambda v: 2 if v['code'] == 'NY_'
80
              else 3 if v['code'] == 'YNN'
81
              else 4 if v['code'] == 'Y1Y'
82
              else v['class_orig'],
83
              axis=1
84
           ).astype('int8').astype('category')
85
                           Code 3.6: Data class (cls/Data.py)
1 import re
2 import pandas as pd
3 from sklearn.preprocessing import LabelEncoder
4
   @pd.api.extensions.register_dataframe_accessor("data")
5
   class Data:
       def __init__(self, pandas_obj, indep_dict):
7
8
           self.dataset = pandas_obj
9
           self.metadata = indep_dict
10
       def encodecat(self):
11
           cat_change = ""
12
13
           for attr in self.metadata.keys():
              if self.metadata[attr]['type'] == 'Categorical':
14
                  le = LabelEncoder()
15
                  le.fit(self.dataset[attr])
16
                  self.dataset[attr] = list(le.transform(self.dataset[attr]).
17
                      astype('int8'))
                  newkeys = list()
18
19
                  unseen = 0
                  for strval in self.metadata[attr]['values'].keys():
20
```

```
21
                       try:
22
                          newkeys.append(int(le.transform([int(strval)])))
23
                       except ValueError: # for previously unseen labels
                          unseen -= 1
24
25
                          newkeys.append(unseen)
                   if list(self.metadata[attr]['values'].keys()) != newkeys:
26
                       cat_change += attr+"\n"
27
                   newdict = {key: val for key, val in zip(newkeys, self.
28
                      metadata[attr]['values'].values())}
                   self.metadata[attr]['values'] = newdict
29
           return cat_change[0:-1]
30
31
       def encodecont(self):
32
           pattern = r'(^|[^{w}])(niu|universe)([^{w}]|^{s})' # Raw string to
33
               prevent invalid escape sequence '\w'
34
           pattern = re.compile(pattern, re.IGNORECASE)
           cont_nonpos = ""
35
           for attr in self.metadata.keys():
36
               if self.metadata[attr]['type'] == 'Continuous':
37
38
                   flag = False
                   for strval in self.metadata[attr]['values'].keys():
39
40
                       if not flag:
41
                          try:
42
                              if int(strval) <= 0:</pre>
43
                                  text = self.metadata[attr]['values'][strval]
                                  matches = re.search(pattern, text.replace(',',
44
                                       ' ').lower())
                                  if bool(matches):
45
                                      flag = True
46
                                      cont_nonpos += attr+"\n"
47
                                      self.dataset[attr] = self.dataset[attr].
48
                                          apply(lambda v: 0 \text{ if } v < 0 \text{ else } v)
                                      break
49
50
                           except:
51
                              pass
52
                       if flag:
```

```
53
                          try:
54
                              if int(strval) <= 0:</pre>
                                  self.metadata[attr]['values'].pop(strval,
55
                                     None)
56
                          except:
57
                              pass
58
                  if flag:
                      self.metadata[attr]['values']['0'] = 'NIU'
59
           return cont_nonpos[0:-1]
60
                            Code 3.7: Info class (cls/Info.py)
1 import pandas as pd
2
3 # Delete the accessor to avoid warning
4 try:
       del pd.DataFrame.info
   except AttributeError:
7
       pass
   @pd.api.extensions.register_dataframe_accessor("info")
  class Info:
       def __init__(self, pandas_obj):
11
           self._validate(pandas_obj, ['id', 'variable', 'type', 'min', 'max'
12
              1)
13
           self.dataset = pandas_obj
14
       Ostaticmethod
15
       def _validate(obj, cols):
16
17
           if any(x not in obj.columns for x in cols):
18
              raise AttributeError("Some attributes are missing")
19
       def setcut(self, pcont, pcatmax):
20
           self.dataset['cut'] = 0
21
```

3.5.6 Exploratory Data Analysis (EDA)

This dissertation considers health insurance factors from a range of topics and subtopics as shown in Table 3.5. All infants born after calendar year are excluded in this study because they are not in the scope of health insurance coverage. This results in 157,681 relevant survey participants. Code 3.8 performs exploratory data analysis by using the pandas accessor thesis in Code 3.5 to compute the cross tabulation between a health factor (independent variable) and a combination of categorical insurance coverage types (dependent variable) as illustrated in Table 3.6. All continuous values of an independent variables are segmented into 10 bins. In addition, it can significantly compress the original dataset of size 237.4 MB in SAS7BDAT format into the feather and CSV formats of size 14.2 MB and 68.1 MB respectively.

Table 3.5: Categories of health insurance factors

Topic	Subtopic	List of Variables
Demographics	Individual characteristics	A_AGE, A_EXPRRP, A_FAMTYP, A_HGA, A_MARITL, A_PFREL, A_SEX, P_STAT, PEAFEVER, PEDISDRS, PEDISEAR, PEDISEYE, PEDISOUT, PEDISPHY, PEDISREM, PRDISFLG, PRCITSHP, PRDTRACE
Basic CPS items	Edited labor force items	A_MJIND, A_MJOCC, PEIO1COW, PRDISC, PRUNTYPE
	Edited earnings items	A_GRSWK, A_HRLYWK, A_HRSPAY, PRERELG
	Labor force person recodes	A_CIVLE, A_CLSWKR, A_EXPLF, A_LFSR, A_UNCOV, A_UNMEM, A_UNTYPE, A_USLHRS, A_WKSCH, A_WKSLK, A_WKSTAT, PEHRUSLT, PEMLR, PRCOW1, PRPTREA, PRWKSTAT
Work experience	General	CLWK, EARNER, HRSWK, LJCW, NWLKWK, NWLOOK, PHMEMPRS, RSNNOTW, WECLW, WEWKRS, WKSWORK, WORKYN, WRK_CK, WTEMP

Table 3.5: Categories of health insurance factors (continued)

E	S.:.b4:	Σ [Τ :
Lopic	Subtopic	List of Variables
Income	Earnings	ERN_OTR, ERN_SRCE, ERN_VAL, ERN_YN, FRM_VAL,
		FRMOTR, FRSE_VAL, FRSE_YN, PEARNVAL, SE_VAL,
		SEMP_VAL, SEMP_YN, SEOTR, WAGEOTR, WS_VAL,
		WSAL_VAL, WSAL_YN

Table 3.5: Categories of health insurance factors (continued)

Topic

Subtopic	List of Variables
Other income	ANN_VAL, ANN_YN, CAP_VAL, CAP_YN, DBTN_VAL,
	DIS_SC1, DIS_SC2, DIS_VAL1, DIS_VAL2, DIS_YN, DIV_VAL,
	DIV_YN, DSAB_VAL, DST_SC1, DST_SC1_YNG, DST_SC2,
	DST_SC2_YNG, DST_VAL1, DST_VAL1_YNG, DST_VAL2,
	DST_VAL2_YNG, DST_YN, DST_YN_YNG, ED_VAL,
	ED_YN, FIN_VAL, FIN_YN, INT_VAL, INT_YN, OED_TYP1,
	OED_TYP2, OED_TYP3, OI_OFF, OI_VAL, OI_YN,
	PEN_SC1, PEN_SC2, PEN_VAL1, PEN_VAL2, PEN_YN,
	PNSN_VAL, PTOTVAL, RESNSS1, RESNSS2, RESNSSI1,
	RESNSSI2, RETCB_VAL, RETCB_YN, RINT_SC1, RINT_SC2,
	RINT_VAL1, RINT_VAL2, RINT_YN, RNT_VAL, RNT_YN,
	SRVS_VAL, SS_VAL, SS_YN, SSI_VAL, SSI_YN, STRKUC,
	SUBUC, SUR_SC1, SUR_SC2, SUR_VAL1, SUR_VAL2,
	SUR_YN, TRDINT_VAL, UC_VAL, UC_YN, VET_TYP1,
	VET_TYP2, VET_TYP3, VET_TYP4, VET_TYP5, VET_VAL,
	VET_YN, WC_TYPE, WC_VAL, WC_YN

Table 3.5: Categories of health insurance factors (continued)

Topic	Subtopic	List of Variables
	Non-cash benefits	PAW_TYP, PAW_VAL, PAW_YN, PENINCL, PENPLAN, WICYN
	Supplemental poverty measure	CHCARE_YN, CHELSEW_YN, CHSP_VAL, CHSP_YN, CSP_VAL, CSP_YN
	Tax model items	ACTC_CRD, AGI, CTC_CRD, EIT_CRED, FED_RET, FEDTAX_AC, FEDTAX_BC, FICA, FILESTAT, MARG_TAX, PRSWKXPNS, STATETAX_A, STATETAX_B, TAX_INC
Poverty	Poverty	PERLIS, POV_UNIV
Health insurance	Health status	HEA
Supplemental poverty measure	SPM unit characteristics	SPM_ACTC

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
OTODI TO	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
A_AGE: Age					
Universe: All Persons					
(-0.085, 8.5]	1,407	5,834	789	628	9,795
(8.5, 17.0]	1,557	6,237	1,079	770	11,822
(17.0, 25.5]	2,238	2,475	1,043	414	8,017
(25.5, 34.0]	2,635	2,749	1,082	594	10,611
(34.0, 42.5]	2,271	2,146	926	613	11,509
(42.5, 51.0]	2,109	2,171	1,157	518	12,081
(51.0, 59.5]	1,606	2,403	1,223	471	9,864
(59.5, 68.0]	1,028	4,854	2,313	2,090	260,9
(68.0, 76.5]	105	5,404	2,602	2,044	254
(76.5, 85.0]	62	4,472	1,977	1,353	115
A_EXPRRP: Expanded relationship code					
Universe: All Persons					
Reference person with relatives	3,693	8,822	4,254	3,365	21,403

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY	Y1Y	YNN
Reference person without relatives	1,603	6,102	2,739	1,413	7,066
Husband	1,049	2,196	1,325	1,016	690,2
Wife	1,482	2,898	1,984	1,426	10,471
Own child	4,337	12,355	2,540	1,553	27,291
Grandchild	377	1,621	137	106	940
Parent	335	1,183	305	174	780
Brother/sister	352	636	127	20	089
Other relative	464	1,219	215	106	806
Foster child	2	107	2	44	2
Nonrelative with relatives	305	514	101	73	816
Partner/roommate	803	780	421	149	2,381
Nonrelative without relatives	233	312	91	20	358
A_FAMTYP: Family type					
Primary family	11,310	28,667	10,560	7,564	67,373

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insurar	ıce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
V de Labora	NNN	NNY	NY	Y1Y	YNN
Nonfamily householder	1,603	6,102	2,739	1,413	7,066
Related subfamily	622	2,263	327	232	2,169
Unrelated subfamily	59	175	32	29	223
Secondary individual	1,284	1,538	583	257	3,334
A_HGA: Educational attainment					
Universe: All Persons					
Children	2,431	10,167	1,488	1,160	17,629
Less than 1st grade	92	177	31	19	64
1st,2nd,3rd,or 4th grade	170	390	61	21	115
5th or 6th grade	412	999	105	52	283
7th and 8th grade	418	1,035	222	116	794
9th grade	480	1,208	231	126	1,381
10th grade	459	1,363	252	169	1,694
11th grade	495	1,443	307	172	1,814
12th grade no diploma	339	716	159	94	794

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

$V_{ m emis}$ blo	Insura	Insurance Coverage Type (GRP, DIR, PUB)	age Type (GRP, DIR	, PUB)
Validible	NNN	NNY	NY_	Y1Y	YNN
High school graduate - high school diploma or equivalent	4,267	9,614	3,563	2,174	13,304
Some college but no degree	2,177	4,642	2,282	1,357	10,203
Associate degree in college - occupation/vocation program	465	1,044	589	370	2,681
Associate degree in college - academic program	610	1,260	719	513	3,919
Bachelor's degree (for example: BA,AB,BS)	1,580	3,364	2,738	1,731	15,745
Master's degree (for example: MA,MS,MENG,MED,MSW, MBA)	530	1,221	1,041	1,017	7,264
Professional school degree (for example: MD,DDS,DVM,LLB,JD)	52	189	202	162	1,026
Doctorate degree (for example: PHD,EDD)	74	246	251	242	1,455
A_MARITL: Marital status					
Universe: All Persons					
Married - civilian spouse present	4,911	11,026	6,899	5,333	35,669
Married - AF spouse present	346	11	6	0	98
Married - spouse absent (exc.separated)	261	418	175	26	721
Widowed	282	3,671	1,344	784	741
Divorced	1,186	3,834	1,402	754	4,817

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
Separated	356	723	144	101	758
Never married	7,693	19,062	4,268	2,426	37,373
A_PFREL: Primary family relationship					
Universe: All Persons					
Not in primary family	2,946	7,815	3,354	1,699	10,623
Husband	2,408	5,385	3,324	2,794	16,972
Wife	2,501	4,998	3,382	2,404	17,664
Own child	4,337	12,355	2,540	1,553	27,291
Other relative	1,528	4,659	784	436	3,308
Unmarried reference person	1,315	3,533	857	609	4,307
A_SEX: Sex					
Universe: All Persons					
Male	7,804	17,947	6,658	4,710	39,664
Female	7,231	20,798	7,583	4,785	40,501

P_STAT: Status of person identifier

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Cover	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
	NNN	NNY	NY_	Y1Y	YNN
Universe: All Persons					
Civilian 15+	12,186	28,562	12,747	8,334	62,431
Armed forces	418	16	9	1	105
Children 0-14	2,431	10,167	1,488	1,160	17,629
PEAFEVER: Did you ever serve on active duty in the U.S. Armed Forces?					
Universe: A_AGE greater than or equal to 17					
Not in universe	3,207	11,462	1,745	1,320	20,376
Yes	674	3,025	1,158	1,233	2,498
No	11,154	24,258	11,338	6,942	57,291
PEDISDRS: Doeshave difficulty dressing or bathing?					
Universe: PRPERTYP $= 2$					
Not in universe	2,849	10,183	1,494	1,161	17,734
Yes	86	1,545	299	233	224
No	12,088	27,017	12,448	8,101	62,207

PEDISEAR: Is...deaf or does ...have serious difficulty hearing?

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

$V_{ m ania}$ hle	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR.	PUB)
V CALICADIO.	NNN	NNY	NY_	Y1Y	YNN
${\rm Universe:\ PRPERTYP} = 2$					
Not in universe	2,849	10,183	1,494	1,161	17,734
Yes	153	2,024	808	573	683
No	12,033	26,538	11,938	7,761	61,748
PEDISEYE: Isblind or doeshave serious difficulty seeing even when wearing					
glasses?					
${\rm Universe:\ PRPERTYP} = 2$					
Not in universe	2,849	10,183	1,494	1,161	17,734
Yes	110	1,116	280	202	358
No	12,076	27,446	12,467	8,132	62,073
PEDISOUT: Because of a physical, mental, or emotional condition, doeshave					
difficulty doing errands along such as visiting a doctor's office or shopping?					
Universe: PRPERTYP $= 2$					
Not in universe	2,849	10,183	1,494	1,161	17,734
Yes	223	3,156	638	513	506

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Voring	Insura	unce Cover	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR	, PUB)
, allable	NNN	NNY	NY_	Y1Y	YNN
No	11,963	25,406	12,109	7,821	61,925
PEDISPHY: Doeshave serious difficulty Walking or climbing stairs?					
${\rm Universe}\colon {\rm PRPERTYP} = 2$					
Not in universe	2,849	10,183	1,494	1,161	17,734
Yes	339	4,767	1,210	006	933
No	11,847	23,795	11,537	7,434	61,498
PEDISREM: Because of a physical, mental, or emotional condition, doeshave					
serious difficulty concentrating, remembering, or making decisions?					
${\rm Universe}\colon {\rm PRPERTYP} = 2$					
Not in universe	2,849	10,183	1,494	1,161	17,734
Yes	292	2,489	519	367	762
No	11,894	26,073	12,228	7,967	61,669
PRDISFLG: Does this person have any of these disability conditions?					
Universe: PRPERTYP $= 2$					
Not in universe	2,849	10,183	1,494	1,161	17,734

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
V CALCOOLOG	NNN	NNY	NY_	Y1Y	YNN
Yes	732	7,560	2,124	1,569	2,395
No	11,454	21,002	10,623	6,765	60,036
PRCITSHP: Citizenship group					
Universe: All persons					
Native, born in US	11,006	32,887	12,065	8,403	70,326
Native, born in PR or US outlying area	82	345	09	49	326
Native, born abroad of US parent(s)	153	249	92	92	694
Foreign born, US cit by naturalization	1,004	2,975	1,067	029	4,851
Foreign born, not a US citizen	2,790	2,289	957	317	3,968
PRDTRACE: Race					
Universe: All persons					
White only	11,466	27,682	11,885	7,517	63,366
Black only	1,765	6,815	1,011	1,051	7,484
American Indian, Alaskan Native only (AI)	516	903	26	85	837
Asian only	745	2,010	962	561	5,947

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in

Variahle	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY	Y1Y	YNN
Hawaiian/Pacific Islander only (HP)	68	192	34	41	368
White-Black	150	428	20	28	009
White-AI	131	351	81	96	490
White-Asian	98	111	52	41	613
White-HP	17	20	15	13	112
Black-AI	26	29	ъ	12	28
Black-Asian	2	∞	6	က	45
Black-HP	1	∞	1	4	\vdash
AI-Asian	2	9	1	0	9
AI-HP	0	4	0	0	4
Asian-HP	23	17	12	7	72
White-Black-AI	13	44	2	က	32
White-Black-Asian	12	∞	0	1	34
White-Black-HP	0	1	0	0	ഹ
White-Al-Asian	2	က	0	0	7
White-AI-HP	0	က	0	0	4

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

$V_{ m arrigh}$	Insura	Insurance Coverage Type (GRP, DIR, PUB)	ge Type (C	GRP, DIR,	PUB)
V CLICADIO V	NNN	NNY	NY_	Y1Y	YNN
White-Asian-HP	4	35	1	2	65
Black-AI-Asian	1	0	0	0	1
White-Black-AI-Asian	0	0	2	0	ಬ
Other 3 race comb.	1	0	0	0	က
Other 4 or 5 race comb.	П	0	1	0	9
A_MJIND: Major industry code					
${\rm Universe:~A_CLSWKR} = 1\text{-}7$					
Not in universe, or children	6,704	30,326	8,393	5,873	29,260
Agriculture, forestry, fishing, and hunting	268	241	309	79	536
Mining	44	21	24	18	445
Construction	1,114	029	511	214	2,961
Manufacturing	551	501	331	346	5,528
Wholesale and retail trade	1,124	1,336	270	433	5,857
Transportation and utilities	480	474	276	185	2,865
Information	80	117	93	48	826

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
	NNN	NNY	$^{ m NY}$	Y1Y	YNN
Financial activities	310	336	437	233	3,752
Professional and business services	957	926	813	414	6,036
Educational and health services	1,209	1,607	1,088	957	13,296
Leisure and hospitality	1,346	1,367	629	278	3,561
Other services	589	615	457	185	1,854
Public administration	250	208	110	232	3,236
Armed forces	6	0	0	0	0
A_MJOCC: Major occupation recode					
${\rm Universe}\colon {\rm A_CLSWKR} = 1\text{-}7$					
Not in universe or children	6,704	30,326	8,393	5,873	29,260
Management, business, and financial occupations	998	821	1,144	595	9,953
Professional and related occupations	964	1,023	1,142	951	14,527
Service occupations	2,265	2,597	1,125	547	6,665
Sales and related occupations	791	1,025	289	311	4,343
Office and administrative support occupations	661	797	589	423	5,469

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

$V_{ m aniahle}$	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
V CALLODIO.	NNN	NNY	NY	Y1Y	YNN
Farming, fishing, and forestry occupations	177	123	95	31	246
Construction and extraction occupations	948	536	326	160	2,154
Installation, maintenance, and repair occupations	327	215	129	127	1,622
Production occupations	484	417	228	194	2,728
Transportation and material moving occupations	839	865	383	283	3,198
Armed forces	6	0	0	0	0
PEIO1COW: Individual class of worker on first job					
Universe: All persons					
NIU	6,704	30,326	8,393	5,873	29,260
Government-federal	222	120	22	138	1,708
Government-state	189	237	151	213	3,210
Government - local	219	337	196	296	4,045
Private, for profit	6,214	5,951	3,369	2,233	34,815
Private, nonprofit	274	466	323	343	3,933
Self-employed, incorporated	325	323	756	152	1,484

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
Variable)		
	NNN	NNY	NY_	Y1Y	YNN
Self-employed, unincorporated	880	974	986	246	1,703
Without pay	∞	11	10	П	2
PRDISC: Discouraged worker recode					
Universe: All persons					
NIU	14,880	38,437	14,165	9,452	79,861
Discouraged worker	40	83	18	4	22
Conditionally interested	73	159	34	28	145
Not available	42	99	24	11	102
PRUNTYPE: Individual class of worker on first job					
Universe: All persons					
NIU	14,304	37,763	13,967	9,305	78,459
Job loser/on layoff	252	341	136	72	797
Other job loser	127	130	38	52	329
Temporary job ended	83	26	17	14	93
Job leaver	69	64	14	11	138

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

$V_{ m ania}$ blo	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
	NNN	NNY	$^{-}{ m NY}_{-}$	Y1Y	YNN
Re-entrant	162	266	62	38	275
New-entrant	39	84	7	9	74
A_GRSWK: How much does usually earn per week at this job before					
deductions , subject to topcoding, the higher of either the amount of item 25a					
times Item 25c or the actual item 25d entry will be present					
Universe: PRERELG=1					
(-2.885, 288.5]	14,066	37,929	13,596	9,036	72,547
(288.5, 577.0]	412	407	218	112	1,185
(577.0, 865.5]	285	213	159	122	1,652
(865.5, 1154.0]	111	88	102	92	1,522
(1154.0, 1442.5]	64	47	42	36	626
(1442.5, 1731.0]	34	18	33	27	714
(1731.0, 2019.5]	21	15	20	16	413
(2019.5, 2308.0]	10	6	15	6	314
(2308.0, 2596.5]	13	9	20	6	201

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Cover	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
V CALICADATA	NNN	NNY	NY_	Y1Y	YNN
(2596.5, 2885.0]	19	13	36	36	638
A_HRLYWK: Is paid by the hour on this job?					
Universe: PRERELG=1					
Not in universe or children and armed forces	13,245	37,057	13,165	8,715	67,548
Yes	1,320	1,289	662	468	6,463
No	470	399	414	312	6,154
A_HRSPAY: How much does earn per hour?					
Universe: A_HRLYWK=1					
(-10.901, 989.1]	14,314	38,046	13,813	9,201	76,286
(989.1, 1979.2]	563	582	312	203	2,116
(1979.2, 2969.3]	112	80	69	58	1,059
(2969.3, 3959.4]	28	24	20	19	391
(3959.4, 4949.5]	10	9	12	ಬ	165
(4949.5, 5939.6]	ಬ	4	10	9	92
(5939.6, 6929.7]	33	1	2	2	40

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

$V_{ m arrighle}$	Insura	ınce Covera	Insurance Coverage Type (GRP, DIR, PUB)	3RP, DIR,	PUB)
	NNN	NNY	$^{-}{ m NY}_{-}$	Y1Y	YNN
(6929.7, 7919.8]	0	1	1	1	21
(7919.8, 8909.9]	0	0	0	0	2
(8909.9, 9900.0]	0	T	7	0	4
PRERELG: Earnings eligibility flag					
Universe: All persons					
Not earnings eligible	13,245	37,057	13,165	8,715	67,548
Earnings eligible	1,790	1,688	1,076	780	12,617
A_CIVLF: Civilian labor force					
Universe: All persons					
Not in universe or children and Armed Forces	86,798	30,466	8,496	5,960	29,588
In universe	8,237	8,279	5,745	3,535	50,577
A_CLSWKR: Class of worker					
Universe: PEMLR=1-3 or (PEMLR=4-7 and person worked in the last 12 $$					
months)					
Not in universe or children and armed forces	6,665	30,242	8,386	5,867	29,186

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insure	Insurance Coverage Type (GRP, DIR, PUB)	ege Type (C	GRP, DIR.	PUB)
	NNN	NNY	$^{-}$ NY	Y1Y	YNN
Private	6,488	6,417	3,692	2,576	38,748
Federal government	222	120	22	138	1,708
State government	189	237	151	213	3,210
Local government	219	337	196	296	4,045
Self-employed-incorporated	325	323	756	152	1,484
Self-employed-not incorporated	880	974	986	246	1,703
Without pay	∞	11	10	1	7
Never worked	39	84	7	9	74
A_EXPLF: Experienced labor force employment status Universe: PEMLR=1-4					
Not in experienced labor force	6,837	30,550	8,503	5,966	29,662
Employed	7,506	7,297	5,471	3,342	48,871
Unemployed	692	868	267	187	1,632

A_LFSR: Labor force status recode

Universe: All persons

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	unce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
Children or Armed Forces	2,849	10,183	1,494	1,161	17,734
Working	7,178	6,826	5,136	3,181	46,957
With job, not at work	328	471	335	161	1,914
Unemployed, looking for work	479	641	138	121	606
Unemployed, on layoff	252	341	136	72	797
Nilf	3,949	20,283	7,002	4,799	11,854
A_UNCOV: On this job, is covered by a union or employee association					
contract?					
${\rm Universe:~A_UNMEM=2}$					
Not in universe or children and armed forces	13,962	37,715	13,483	9,016	72,936
Yes	∞	11	∞	10	108
$N_{\rm O}$	1,065	1,019	750	469	7,121

A_UNMEM: On this job, is ... a member of a labor union or of an employee

association similar to a union?

Universe: PRERELG=1

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

$V_{ m smis}$ blo	Insura	ance Cover	Insurance Coverage Type (GRP, DIR, PUB)	3RP, DIR	PUB)
Variable	NNN	NNY	NY_	Y1Y	YNN
Not in universe or children and armed forces	13,909	37,669	13,451	8,957	71,925
Yes	53	46	32	29	1,011
No	1,073	1,030	758	479	7,229
A_UNTYPE: Reason for unemployment					
Universe: A_LFSR=3 or 4					
Not in universe or children and Armed Forces	14,304	37,763	13,967	9,302	78,459
Job loser - on layoff	252	341	136	72	797
Other job loser	209	227	55	99	422
Job leaver	69	64	14	11	138
Re-entrant	162	266	62	38	275
New entrant	39	84	7	9	74
A_USLHRS: How many hrs per week does usually work at this job?					
Universe: All persons					
(-4.103, 6.3]	8,214	32,313	9,452	6,448	33,848
(6.3, 16.6]	279	647	359	198	1,392

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

NNN NNY NY_ Y1 641 1,071 691 2 935 1,099 622 3 4,268 3,105 2,411 1,8 436 291 412 2 186 149 189 45 46 57 7 11 20 6,798 30,466 8,496 5,9 7,178 6,826 5,136 3,1 618 772 197 1 113 260 77	Variable	Insura	Insurance Coverage Type (GRP, DIR, PUB)	ge Type ((3RP, DIR	, PUB)
641 1,071 691 935 1,099 622 4,268 3,105 2,411 436 291 412 186 149 189 189 412 186 149 189 189 57 45 46 57 Abor force by time worked or lost twork t work t work eks FT eks PT eks PT eks PT 113 260 77 114 335 eks PT 115 261 117 47 118 335 eks PT	Valiable	NNN	NNY	NY_	Y1Y	YNN
935 1,099 622 4,268 3,105 2,411 436 291 412 186 149 189 187 141 186 149 189 187 181 188 141 189 189 189 189 189 189 189 189 189 189 189	(16.6, 26.9]	641	1,071	691	288	2,360
4,268 3,105 2,411 436 291 412 186 149 189 45 46 57 24 13 28 abor force by time worked or lost ersons t work t work t work eks FT eks PT eks PT 113 260 775 eks PT e	(26.9, 37.2]	935	1,099	622	362	3,750
436 291 412 186 149 189 45 46 57 24 13 28 25 11 20 abor force by time worked or lost twork twork twork twork eks FT eks PT 13 260 5,136 eks FT eks PT 14 12 20 26 197 eks PT 15 20 27 11 30 28 30,466 8,496 77 11 335 eks FT eks PT 16 20 77	(37.2, 47.5]	4,268	3,105	2,411	1,848	32,501
186 149 189 45 46 57 24 13 28 25 11 20 abor force by time worked or lost ersons t work eks FT eks FT eks PT 113 260 775 129 197 120 121 120 120 121 120 122 120 123 120 124 120 125 127 126 127 127 128 127 128 129 127	(47.5, 57.8]	436	291	412	234	4,378
45 46 57 24 13 28 abor force by time worked or lost ersons twork twork eks FT eks PT 104 13 28 28 28 28 28 28 29 20 20 21 21 20 20 21 20 20 20 20 20 20 20 20 20 20 20 20 20	(57.8, 68.1]	186	149	189	74	1,437
24 13 28 abor force by time worked or lost ersons though the conditions are some as the state of the state	(68.1, 78.4]	45	46	57	22	289
hor force by time worked or lost ersons 6,798 30,466 8,496 7,178 6,826 5,136 t work ersor hor work ersor hor many and a second to the second to the second ersor hor many and a second ersor hor many	(78.4, 88.7]	24	13	28	16	166
abor force by time worked or lost ersons 6,798 30,466 8,496 7,178 6,826 5,136 t work eks FT eks FT eks FT 113 260 77	(88.7, 99.0]	2	11	20	ಬ	44
eks FT 6,798 30,466 8,496 7,178 6,826 5,136 1328 471 335 eks FT 618 722 197 eks PT 113 260 77	A_WKSCH: Labor force by time worked or lost					
t work 6,798 30,466 8,496 7,178 6,826 5,136 8,496 8,496 8,496 9,406 8,496 9,40	Universe: All persons					
7,178 6,826 5,136 3, 328 471 335 618 722 197 113 260 77	Not in universe	6,798	30,466	8,496	5,960	29,588
328 471 335 618 722 197 113 260 77	At work	7,178	6,826	5,136	3,181	46,957
618 722 197 113 260 77	With job, not at work	328	471	335	161	1,914
113 260 77	Unemployed, seeks FT	618	722	197	136	1,316
	Unemployed, seeks PT	113	260	2.2	22	390

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
V CALCODIO.	NNN	NNY	NY_	Y1Y	YNN
A_WKSLK: Duration of unemployment					
Universe: PEMLR=3 or 4					
(-0.099, 9.9]	14,748	38,340	14,142	9,435	79,643
(9.9, 19.8]	118	150	44	27	237
(19.8, 29.7]	49	92	17	12	121
(29.7, 39.6]	26	20	6	7	99
(39.6, 49.5]	10	11	4	4	16
(49.5, 59.4]	45	20	11	20	42
(59.4, 69.3]	6	10	3	0	<u></u>
(69.3, 79.2]	4	2	0	0	1
(79.2, 89.1]	0	0	0	0	1
(89.1, 99.0]	26	26	11	20	31
A_WKSTAT: Full/part-time status					
Universe: All persons					
Children or Armed Forces	2,849	10,183	1,494	1,161	17,734

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	Insurance Coverage Type (GRP, DIR, PUB)	ge Type (C	RP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
Not in labor force	3,949	20,283	7,002	4,799	11,854
Full-time schedules	5,715	4,390	3,714	2,508	42,413
Part-time for economic reasons, usually FT	267	217	153	48	029
Part-time for non-economic reasons, usually PT	1,200	2,313	1,464	718	5,257
Part-time for economic reasons, usually PT	324	377	140	89	531
Unemployed FT	618	722	197	136	1,316
Unemployed PT	113	260	22	22	390
PEHRUSLT: Hours usually worked last week					
Universe: All persons					
(-4.144, 10.4]	8,336	32,561	9,610	6,541	34,614
(10.4, 24.8]	262	1,159	671	330	2,447
(24.8, 39.2]	1,147	1,420	805	444	4,613
(39.2, 53.6]	4,519	3,253	2,721	1,976	35,068
(53.6, 68.0]	333	257	306	147	2,691
(68.0, 82.4]	87	92	102	42	583

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
(82.4, 96.8]	14	2	12	∞	106
(96.8, 111.2]	4	11	13	7	36
(111.2, 125.6]	0	0	1	0	<u></u>
(125.6, 140.0]	0	1	0	0	0
PEMLR: Major labor force recode					
Universe: All persons					
NIU	2,849	10,183	1,494	1,161	17,734
Employed - at work	7,178	6,826	5,136	3,181	46,957
Employed - absent	328	471	335	161	1,914
Unemployed - on layoff	252	341	136	72	797
Unemployed - looking	479	641	138	121	606
Not in labor force - retired	543	11,004	5,087	3,754	1,768
Not in labor force - disabled	437	4,110	405	359	732
Not in labor force - other	2,969	5,169	1,510	989	9,354

PRCOW1: Class of worker recode-job 1

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
VOLUM V	NNN	NNY	$^{-}{ m NY}_{-}$	Y1Y	YNN
Universe: All persons					
NIU	6,704	30,326	8,393	5,873	29,260
Federal govt	222	120	22	138	1,708
State govt	189	237	151	213	3,210
Local govt	219	337	196	296	4,045
Private (incl. self-employed incorp.)	6,813	6,740	4,448	2,728	40,232
Self-employed, unincorp.	880	974	986	246	1,703
Without pay	∞	11	10	1	7
PRPTREA: Detailed reason for part-time					
Universe: Part time workers					
NIU	12,873	35,620	12,343	8,513	71,585
Usually FT - slack work/business conditions	248	202	136	45	634
Usually FT - seasonal work	13	9	14	1	17
Usually FT - job started/ended during week	9	6	3	21	19
Usually FT - vacation/personal day	06	87	09	22	970

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

$V_{ m anighle}$	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
V OILIGIDIA	NNN	NNY	NY_	Y1Y	YNN
Usually FT - own illness/injury/medical appt	109	124	62	22	699
Usually FT - holiday (religious or legal)	ಬ	! -	3	4	40
Usually FT - child care problems	4	Ю	7	7	52
Usually FT - other fam/pers obligations	32	25	20	17	206
Usually FT - labor dispute	2	1	0	0	4
Usually FT - weather affected job	20	30	10	ರ	20
Usually FT - school/training	ಬ	ಬ	1	0	18
Usually FT - civic/military duty	0	1	0	0	4
Usually FT - other reason	119	116	74	44	446
Usually PT - slack work/business conditions	206	223	92	40	345
Usually PT - PT could only find PT work	133	177	61	30	233
Usually PT - seasonal work	12	<u></u>	ಬ	2	12
Usually PT - child care problems	64	116	40	16	236
Usually PT - other fam/pers obligations	271	343	248	111	1,221
Usually PT - health/medical limitations	51	199	54	44	123
Usually PT - school/training	303	450	245	86	1,713

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
V CALCODIC.	NNN	NNY	NY_	Y1Y	YNN
Usually PT - retired/social security limit on earnings	52	440	350	238	228
Usually PT - workweek $<$ 35 hours	260	407	251	106	952
Usually PT - other	107	145	142	55 8	368
PRWKSTAT: Full/part-time work status					
Universe: All persons					
NIU	2,849	10,183	1,494	1,161	17,734
Not in labor force	3,949	20,283	7,002	4,799	11,854
FT hours $(35+)$, usually FT	4,995	3,679	3,226	2,189	38,324
PT for economic reasons, usually FT	267	217	153	48	029
PT for non-economic reasons, usually FT	436	401	254	191	2,479
Not at work, usually FT	227	238	179	105	1,389
PT hrs, usually PT for economic reasons	324	377	140	89	531
PT hrs, usually PT for non-economic	1,099	2,080	1,308	662	4,732
FT hours, usually PT for economic reasons	17	16	12	1	29
FT hours, usually PT for non-economic reasons	40	56	43	22	192

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	Insurance Coverage Type (GRP, DIR, PUB)	ge Type (C	GRP, DIR,	PUB)
V CALICOLUS	NNN	NNY	NY_	Y1Y	YNN
Not at work, usually part-time	101	233	156	56	525
Unemployed FT	618	722	197	136	1,316
Unemployed PT	113	260	2.2	22	390
CLWK: Longest job class of worker (recode)					
Universe: All persons aged $15+$					
Niu	2,431	10,167	1,488	1,160	17,629
Private	6,959	7,099	4,733	3,023	41,294
Government	1,009	747	446	710	9,436
Self-employed	849	992	1,008	253	1,614
Without pay	17	12	15	1	15
Never worked	3,770	19,728	6,551	4,348	10,177
EARNER: Earner status recode					
Universe: All persons aged $15+$					
Niu	2,431	10,167	1,488	1,160	17,629
Earner	8,821	8,842	6,188	3,986	52,346

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY	Y1Y	YNN
Nonearner	3,783	19,736	6,565	4,349	10,190
HRSWK: In the weeks that worked how may hours did usually work per					
week?					
${\rm Universe:\ WKSWORK}>0$					
(-0.099, 9.9]	6,347	30,317	8,296	5,648	28,472
(9.9, 19.8]	354	837	443	259	1,576
(19.8, 29.7]	875	1,550	828	390	2,922
(29.7, 39.6]	1,277	1,534	847	486	4,780
(39.6, 49.5]	5,110	3,719	2,826	2,191	34,221
(49.5, 59.4]	673	461	578	336	5,584
(59.4, 69.3]	276	228	263	122	1,929
(69.3, 79.2]	22	48	74	33	383
(79.2, 89.1]	41	33	33	20	222
(89.1, 99.0]	2	18	23	10	92

LJCW: Longest job class of worker

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	ınce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR.	PUB)
	NNN	NNY	$^{-}$ N $^{-}$	Y1Y	VNN
Niu	6,201	29,895	8,039	5,508	27,806
Private	6,640	6,757	3,950	2,866	40,016
Federal	269	142	63	152	1,842
State	208	249	160	236	3,440
Local	232	356	223	322	4,154
Self employed incorporated, yes	319	342	783	157	1,278
Self employed incorporated, no or farm	849	992	1,008	253	1,614
Without pay	17	12	15	1	15
NWLKWK: How may different weeks was looking for work or on layoff?					
${\rm Universe}\colon {\rm NWLOOK} = 1$					
(-0.052, 5.2]	14,892	38,462	14,188	9,469	79,995
(5.2, 10.4]	15	32	7	9	38
(10.4, 15.6]	13	29	4	0	17
(15.6, 20.8]		17	4	2	6

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
(20.8, 26.0]	14	22	ಬ	4	23
(26.0, 31.2]	က	7	1	0	2
(31.2, 36.4]	က	7	0	0	1
(36.4, 41.6]	9	17	1	П	ಬ
(41.6, 46.8]	4	3	1	0	1
(46.8, 52.0]	78	149	30	13	74
NWLOOK: Even though did not work in 20 did spend and time trying to					
find a job or on layoff?					
${\rm Universe}\colon {\rm WORKYN} = 2$					
Niu	11,265	19,017	7,690	5,147	886,69
Yes	176	340	20	41	236
No	3,594	19,388	6,481	4,307	9,941

PHMEMPRS: For how many employers did \dots work in 20..? if more than one

Universe: WKSWORK > 0

at same time, only count it as one employer

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insur	Insurance Coverage Type (GRP, DIR, PUB)	ge Type ((GRP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY	Y1Y	YNN
Niu	6,201	29,895	8,039	5,508	27,806
One employer	7,684	7,738	5,537	3,439	47,029
Two employers	857	848	535	439	4,433
3 or more employers	293	264	130	109	897
RSNNOTW: What was the main reason did not work in 20?					
${\rm Universe}\colon {\rm WORKYN} = 2$					
Niu	11,265	19,017	7,690	5,147	69,988
Ill or disabled	208	4,721	503	449	681
Retired	477	10,319	4,709	3,378	1,425
Taking care of home	1,331	1,690	562	231	2,816
Going to school	1,043	2,510	829	254	4,901
Could not find work	209	286	39	21	147
Other	202	202	80	15	207

WECLW: Longest job class of worker (persons 15+)

Universe: All persons aged 15+

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	Insurance Coverage Type (GRP, DIR, PUB)	ge Type ((GRP, DIR,	PUB)
V CALCODIO.	NNN	NNY	$^{-}$ NY	Y1Y	YNN
Not in universe	2,431	10,167	1,488	1,160	17,629
Agriculture (Wage and salary)	220	198	181	09	482
Agriculture (Self-employed)	51	28	120	32	106
Agriculture (Unpaid)	7	က	2	0	4
Nonagriculture (Private household	100	138	09	18	133
Nonagriculture (Other private)	6,338	6,452	3,776	2,801	39,483
Nonagriculture (Government)	1,006	742	444	708	9,407
Nonagriculture (Self-employed)	1,102	1,250	1,606	367	2,733
Nonagriculture (Unpaid)	10	6	13	1	11
Nonagriculture (Never worked)	3,770	19,728	6,551	4,348	10,177
WEWKRS: Weeks worked recode					
Universe: All persons aged $15+$					
Niu	2,431	10,167	1,488	1,160	17,629
Full-year worker (Full time)	5,641	3,827	3,519	2,265	41,178
Full-year worker (Part time)	1,027	1,832	1,095	515	3,717

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
V CALTONIAL V	NNN	NNY	NY_	Y1Y	YNN
Part-year worker (Full time)	1,259	1,434	695	716	4,156
Part-year worker (Part time)	206	1,757	893	491	3,308
Part-year worker (Nonworker)	3,770	19,728	6,551	4,348	10,177
WKSWORK: During 20 in how many weeks did work even for a few hours?					
(include paid vacation and sick leave as work)					
Universe: Persons $15+$ with WORKYN $=1$					
(-0.052, 5.2]	6,329	30,179	8,164	5,588	28,130
(5.2, 10.4]	147	315	110	86	626
(10.4, 15.6]	180	343	147	104	716
(15.6, 20.8]	229	363	147	131	748
(20.8, 26.0]	318	518	218	197	926
(26.0, 31.2]	184	242	117	79	493
(31.2, 36.4]	235	266	155	111	733
(36.4, 41.6]	300	342	242	163	1,138
(41.6, 46.8]	267	292	165	126	986

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

$V_{\alpha v_i \alpha b l \alpha}$	Insura	Insurance Coverage Type (GRP, DIR, PUB)	ge Type (C	GRP, DIR,	PUB)
- Valiable	NNN	NNY	NY_	Y1Y	YNN
(46.8, 52.0]	6,846	5,885	4,776	2,898	45,669
WORKYN: Did work at a job or business at any time during 20?					
Universe: All persons aged $15+$					
Niu	2,431	10,167	1,488	1,160	17,629
Yes	8,727	8,684	6,108	3,938	52,062
No	3,877	19,894	6,645	4,397	10,474
WRK_CK: Worked last year recode, including temporary and part-time					
Universe: All persons aged $15+$					
Niu	2,431	10,167	1,488	1,160	17,629
Yes	8,834	8,850	6,202	3,987	52,359
No	3,770	19,728	6,551	4,348	10,177
WTEMP: Did do any temporary, part-time, or seasonal work even for a few					
days during 20?					
${\rm Universe}\colon {\rm WORKYN}=2$					
Niu	11,158	18,851	7,596	5,098	69,691

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insure	Insurance Coverage Type (GRP, DIR, PUB)	ge Type (0	GRP, DIR	PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
Yes	107	166	94	49	297
No	3,770	19,728	6,551	4,348	10,177
ERN_OTR: Wage and salary money earned from other work, $\rm Y/N$					
Universe: All persons aged 15+					
Niu	6,201	29,895	8,039	5,508	27,806
Yes	819	847	635	496	5,174
No	8,015	8,003	5,567	3,491	47,185
ERN_SRCE: Source of earnings from longest job					
${\rm Universe:\ ERN_YN}=1$					
Niu	6,201	29,895	8,039	5,508	27,806
Wage and salary	7,968	7,846	5,179	3,733	50,730
Self employment	808	940	904	224	1,529
Farm self employment	40	52	104	29	82
Without pay	17	12	15	1	15

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	unce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
ERN_VAL: How much did earn from this employer before deductions in					
20? what was net earnings from this business/ farm after expenses during					
20?					
${\rm Universe:\ ERN_YN} = 1$					
(-11108.998, 101000.8]	14,748	38,542	13,748	9,127	72,515
(101000.8, 212000.6]	239	156	378	286	6,274
(212000.6, 323000.4]	22	24	26	54	780
(323000.4, 434000.2]	6	11	18	16	236
(434000.2, 545000.0]	9	9	13	9	114
(545000.0, 655999.8]	က	က	7	0	55
(655999.8, 766999.6]	\vdash	0	4	1	23
(766999.6, 877999.4]	2	0	4	1	28
(877999.4, 988999.2]	П	0	П	1	21
(988999.2, 1099999.0]	4	3	12	3	119

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
ERN_YN: Earnings from employer or net earnings from business/ farm after					
expenses from longest job during 20?					
Universe: WORKYN=1 or WTEMP=1					
Niu	2,431	10,167	1,488	1,160	17,629
Yes	8,817	8,838	6,187	3,986	52,344
No	3,787	19,740	6,566	4,349	10,192
FRM_VAL: Amount of farm self-employment earnings from secondary source					
Universe: $FRMOTR = 1$					
(-10288.999, 19000.9]	15,028	38,744	14,230	9,484	80,131
(19000.9, 48000.8]	3	1	7	က	25
(48000.8, 77000.7]	3	0	0	Ю	
(77000.7, 106000.6]	1	0	4	က	1
(251000.1, 280000.0]	0	0	0	0	1

FRMOTR: Receiving farm self-employment from secondary source

Universe: $ERN_OTR = 1$

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	3RP, DIR,	PUB)
V CALICADIO	NNN	NNY	NY_	Y1Y	YNN
Niu	14,212	37,902	13,606	9,005	75,001
Yes	98	26	73	43	478
No	737	787	292	450	4,686
FRSE_VAL: Total amount of farm self-employment earnings					
Universe: ERN_YN=1 or FRMOTR=1					
(-20767.998, 57001.8]	15,029	38,739	14,206	9,483	80,136
(57001.8, 134001.6]	9	ಬ	29	10	25
(134001.6, 211001.4]	0	1	2	0	3
(211001.4, 288001.2]	0	0	က	1	П
(442000.8, 519000.6]	0	0	0	1	0
(673000.2, 750000.0]	0	0	П	0	0
FRSE_YN: Receiving any farm self-employment					
Universe: ERN_YN=1 or FRMOTR=1					
Niu	2,431	10,167	1,488	1,160	17,629
Yes	122	105	170	20	560

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY	Y1Y	YNN
No	12,482	28,473	12,583	8,265	61,976
PEARNVAL: Total persons earnings					
Universe: All persons aged $15+$					
(-12083.998, 198500.8]	14,962	38,669	14,069	9,370	78,229
(198500.8, 407000.6]	53	62	126	111	1,506
(407000.6, 615500.4]	11	11	22	∞	220
(615500.4, 824000.2]	3	0	10	2	53
(824000.2, 1032500.0]	3	2	ಬ	က	62
(1032500.0, 1240999.8]	ಣ	1	∞	1	93
(1240999.8, 1449499.6]	0	0	1	0	0
(1449499.6, 1657999.4]	0	0	0	0	1
(1866499.2, 2074999.0]	0	0	0	0	1

SE_VAL: Amount of own business self-employment earnings from secondary

source

Universe: SEOTR = 1

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
VOLTOOLI V	NNN	NNY	$^{-}$ N $^{-}$	Y1Y	YNN
(-10558.999, 46000.9]	15,027	38,736	14,220	9,484	80,099
(46000.9, 102000.8]	∞	7	14	9	45
(102000.8, 158000.7]	0	2	rO	2	9
(158000.7,214000.6]	0	0	0	2	4
(214000.6, 270000.5]	0	0	0	1	1
(270000.5, 326000.4]	0	0	23	0	ಬ
(326000.4, 382000.3]	0	0	0	0	က
(382000.3, 438000.2]	0	0	0	0	1
(494000.1,550000.0]	0	0	0	0	П
SEMP_VAL: Total own business self-employment earnings (combined amounts					
in ern-val, if ern-srce=2, and se-val)					
Universe: ERN_YN=1 or SEOTR=1					
(-21117.997, 92001.7]	14,989	38,698	14,106	9,464	79,943
(92001.7, 204001.4]	39	41	111	24	179
(204001.4, 316001.1]	2	3	15	4	20

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

$V_{ m ania}$ has	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
Variably	NNN	NNY	NY	Y1Y	YNN
(316001.1, 428000.8]	0	2	2	2	11
(428000.8, 540000.5]	က	1	2	1	4
(540000.5, 652000.2]	0	0	1	0	2
(652000.2, 763999.9]	0	0	1	0	2
(763999.9, 875999.6]	0	0	1	0	1
(987999.3, 1099999.0]	2	0	2	0	က
SEMP_YN: Receiving own business self-employment, y/n					
Universe: ERN_YN=1 or SEOTR=1					
Niu	2,431	10,167	1,488	1,160	17,629
Yes	942	1,075	1,061	320	2,577
No	11,662	27,503	11,692	8,015	59,959
SEOTR: Receiving own business self-employment, y/n					
Universe: ERN_YN=1 or SEOTR=1					
Niu	14,214	37,904	13,607	9,000	74,996
Yes	148	149	171	101	1,077

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

17	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR	, PUB)
Valiable	NNN	NNY	NY_	Y1Y	YNN
No	673	692	463	394	4,092
WAGEOTR: Receiving wage and salary earnings from other employers, y/n					
Universe: $ERN_OTR = 1$					
Niu	14,218	37,901	13,607	9,002	74,994
Yes	286	807	290	471	4,927
No	31	37	44	22	244
WS_VAL: Amount of wage and salary earnings from other employers					
${\tt Universe:\ ERN_OTR} = 1$					
(-1099.999, 1099999.9]	15,033	38,738	14,235	9,491	80,092
(109999.9, 219999.8]	1	~	ಬ	က	59
(219999.8, 329999.7]	1	0	1	1	က
(329999.7, 439999.6]	0	0	0	0	ಬ
(439999.6, 549999.5]	0	0	0	0	1
(879999.2, 989999.1]	0	0	0	0	က

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
V CALTONIA.	NNN	NNY	$^{-}$ N $^{-}$	Y1Y	YNN
(989999.1, 10999999.0]	0	0	0	0	2
WSAL_VAL: Total wage and salary earnings (combined amounts in ern-val, if					
ern-srce=1, and $ws-val$)					
Universe: ERN_YN=1 or WAGEOTR=1					
(-1999.999, 199999.9]	14,976	38,684	14,113	9,393	78,320
(1999999.9, 3999999.8]	38	44	85	87	1,377
(399999.8, 599999.7]	13	13	25	6	247
[599999.7, 799999.6]	က	1	4	1	26
(799999.6, 999999.5]	က	0	4	23	49
(999999.5, 1199999.4]	2	3	10	က	114
(11999999.4, 13999999.3]	0	0	0	0	1
$(17999999.1,\ 19999999.0]$	0	0	0	0	Н
WSAL_YN: Receiving wage and salary earnings					
Universe: ERN_YN=1 or WAGEOTR=1					
Niu	2,431	10,167	1,488	1,160	17,629

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
Yes	8,025	7,920	5,259	3,764	50,886
No	4,579	20,658	7,494	4,571	11,650
ANN_VAL: Retirement income, annuities amount					
${\rm Universe}\colon {\rm ANN_YN} = 1$					
(-396.0, 39600.0]	15,030	38,705	14,208	9,456	80,136
(39600.0, 79200.0]	4	28	23	34	18
(79200.0, 118800.0]	1	7	9	က	∞
(118800.0, 158400.0]	0	ಣ	2	0	2
(158400.0, 198000.0]	0	2	0	1	0
(356400.0, 396000.0]	0	0	2	1	1
ANN_YN: Retirement income, annuities, y/n					
Universe: All Persons aged 15+					
Niu	2,431	10,167	1,488	1,160	17,629
Yes	26	634	573	422	219

66,843

7,534

11,363

36,074

14,044

Niu

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	3RP, DIR,	PUB)
	NNN	NNY	$^{-}$ N $^{-}$	Y1Y	YNN
No	12,578	27,944	12,180	7,913	62,317
CAP_VAL: Capital gains value					
$\label{eq:cap_var} \text{Universe: CAP_YN} = 1$					
(-999.999, 99999.9]	15,031	38,725	14,211	9,473	80,085
(99999.9, 1999999.8]	2	13	16	16	35
(199999.8, 299999.7]	2	9	9	ಗು	24
(299999.7, 399999.6]	0	1	က	0	6
$(399999.6,\ 4999999.5]$	0	0	1	0	3
$(499999.5,\ 599999.4]$	0	0	1	1	0
(699999.3, 7999999.2]	0	0	1	0	7
(899999.1, 999999.0]	0	0	2	0	2
CAP_YN: Yes/no answer to âDid you receive capital gain from your shares of					
stock or mutual fund?'					
${\rm Universe}\colon {\rm DIV_YN} = 1$					

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY	Y1Y	YNN
Yes	176	734	958	693	3,176
No	815	1,937	1,920	1,268	10,146
DBTN_VAL: Total amount of retirement distributions received (dst_val1 +					
$\operatorname{dst_val2}$)					
Universe: DST_VAL1>0 OR DST_VAL2>0					
[-999.999, 99999.9]	15,033	38,711	14,203	9,460	80,139
(99999.9, 199999.8]	2	32	35	32	23
(199999.8, 299999.7]	0	2	2	1	2
(299999.7, 399999.6]	0	0	0	1	0
(399999.6, 499999.5]	0	0	1	0	1
(899999.1, 999999.0]	0	0	0	П	0
DIS_SC1: What was the source of disability income?					
Universe: DIS_YN=1					
Niu	14,947	38,270	14,130	$9,\!359$	79,707
Worker's compensation	16	32	11	15	96

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY	Y1Y	YNN
Company or union disability	10	48	19	34	123
Federal government disability	9	80	6	10	15
Us military retirement disability	18	45	10	∞	12
State or local gov't employee disability	14	92	21	25	26
Us railroad retirement disability	0	9	7	0	1
Accident or disability insurance	∞	32	16	17	09
Blacklung miners disability	0	0	0	1	0
State temporary sickness	က	1	2	1	6
Other or don't know	13	161	21	25	98
DIS_SC2: What was the source of disability income?					
Universe: DIS_YN=1					
Niu	15,035	38,740	14,240	9,493	80,158
Federal government disability	0	0	1	0	0
Us military retirement disability	0	П	0	0	0
State or local gov't employee disability	0	2	0	1	က

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

$V_{ m ariable}$	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR	PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
Other or don't know	0	2	0	1	4
DIS_VAL1: How much did receive (source type) during 20?					
Universe: DIS_SC1>0					
(-100.0, 10000.0]	14,993	38,533	14,185	9,428	80,005
(10000.0, 20000.0]	26	144	25	31	78
(20000.0, 30000.0]	<u></u>	33	16	23	40
(30000.0, 40000.0]	4	13	4	4	15
(40000.0, 50000.0]	3	10	1	23	11
(50000.0, 60000.0]	1	0	0	1	1
(60000.0, 70000.0]	1	1	1	0	1
(70000.0, 80000.0]	0	1	П	П	4
(80000.0, 90000.0]	0	\vdash	0	П	0
(90000.0, 100000.0]	0	6	∞	4	10

DIS_VAL2: How much did ... receive (source type) during 20.. ?

Universe: DIS_SC2>0

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY	Y1Y	YNN
(-23.672, 2367.2]	15,035	38,740	14,240	9,493	80,158
(4734.4, 7101.6]	0	1	0	0	4
(7101.6, 9468.8]	0	0	0	0	1
(11836.0, 14203.2]	0	0	0	0	1
(14203.2, 16570.4]	0	3	1	2	0
(21304.8, 23672.0]	0	\vdash	0	0	Н
DIS_YN: Other than social security did receive any income in 20 as a					
result of health problems?					
Universe: All Persons aged 15+					
Niu	2,431	10,167	1,488	1,160	17,629
Yes	88	475	111	136	458
No	12,516	28,103	12,642	8,199	62,078

DIV_VAL: How much did ... receive in dividends from stocks or mutual funds

during 20.. ?

Universe: DIV_YN = 1

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR.	PUB)
V CALICADIA	NNN	NNY	NY_	Y1Y	YNN
(-999.999, 99999.9]	15,031	38,730	14,217	9,476	80,108
(99999.9, 1999999.8]	4	10	14	14	36
(199999.8, 299999.7]	0	က	9	က	16
(299999.7, 399999.6]	0	2	2	0	2
(699999.3, 7999999.2]	0	0	0	2	0
(899999.1, 999999.0]	0	0	2	0	33
DIV_YN: Did receive dividends?					
Universe: All Persons aged 15+					
Niu	2,431	10,167	1,488	1,160	17,629
Yes	583	1,873	2,246	1,575	8,875
No	12,021	26,705	10,507	6,760	53,661
DSAB_VAL: Total amount of disability income received, combined amounts in					
edited sources one and two					
Universe: DIS_VAL1>0 OR DIS_VAL2>0					
(-100.0, 10000.0]	14,993	38,529	14,184	9,427	80,002

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

$N_{ m ania}$ hla	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
V CALCADIA	NNN	NNY	NY_	Y1Y	YNN
(10000.0, 20000.0]	26	147	25	32	2.2
(20000.0, 30000.0]	7	33	17	23	44
(30000.0, 40000.0]	4	14	4	က	15
(40000.0, 50000.0]	3	10	1	2	11
(50000.0, 60000.0]	1	0	0	21	1
(60000.0, 70000.0]	1	1	1	0	1
(70000.0, 80000.0]	0	1	1	1	4
(80000.0, 90000.0]	0	1	0	1	0
(90000.0, 100000.0]	0	6	∞	4	10
DST_SC1: Retirement income, distribution source 1					
Universe: DST_VAL1 > 0 and a_age $>= 58$					
Niu	14,982	37,052	12,699	8,267	79,685
401k account	28	684	268	499	249
403b account	0	49	39	48	20
Roth ira	2	114	66	09	24

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insure	ınce Cover	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR.	PUB)
	NNN	NNY	NY_	Y1Y	YNN
Regular ira	17	739	715	499	115
Keogh plan	0	1	3	3	1
Sep plan (simplified employee pension)	1	12	27	18	ಬ
Other type of retirement account	ಬ	94	91	101	99
DST_SC1_YNG: Retriement Distribution source 1, person under age 58					
Universe: DST_YN_YNG = 1 and a_age < 58					
Niu	14,950	38,651	14,163	9,424	79,246
401k account	52	09	45	47	653
403b account	4	ಣ	3	4	41
Roth ira	13	11	ರ	7	99
Regular ira	11	15	20	4	107
Sep plan (simplified employee pension)	0	П	П	0	3
Other type of retirement account	5	4	4	6	49

 $\operatorname{DST_SC2}$ Retirement income, distribution source 2

Universe: DST_VAL2 > 0 and a_age >= 58

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	ance Cover	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR	, PUB)
	NNN	NNY	$^{ m NY}$	Y1Y	YNN
Niu	15,034	38,662	14,160	9,433	80,151
403b account	0	4	ಬ	ಬ	1
Roth ira	1	12	12	9	က
Regular ira	0	51	45	38	6
Keogh plan	0	0	1	0	0
Sep plan (simplified employee pension)	0	3	2	3	0
Other type of retirement account	0	13	16	10	1
DST_SC2_YNG: Retriement Distribution source 2, person under age 58					
Universe: DST_VAL_YNG > 0 and a_age < 58					
Niu	15,031	38,739	14,241	9,494	80,146
403b account	0	0	0	0	1
Roth ira	2	2	0	1	6
Regular ira	2	2	0	0	ಬ
Sep plan (simplified employee pension)	0	2	0	0	ಣ
Other type of retirement account	0	0	0	0	П

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variahla	Insura	ance Cover	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR	, PUB)
V CALICULAI	NNN	NNY	NY_	Y1Y	YNN
DST_VAL1: Retirement income amount, distribution source 1					
${\rm Universe:\ DST_SC1} = 1$					
[-999.999, 99999.9]	15,033	38,711	14,207	9,463	80,139
(99999.9, 1999999.8]	2	32	31	29	23
(199999.8, 2999999.7]	0	2	2	П	2
(299999.7, 399999.6]	0	0	0	П	0
(399999.6, 4999999.5]	0	0	1	0	1
$(899999.1,\ 999999.0]$	0	0	0	П	0
DST_VAL1_YNG: Retriement Distribution amount 1, under age 58					
${\rm Universe:\ DST_SC1_YNG} = 1$					
(-999.999, 99999.9]	15,033	38,743	14,240	9,494	80,137
$(999999.9,\ 1999999.8]$	1	1	0	П	17
(1999999.8, 2999999.7]	0	1	1	0	9
(299999.7, 399999.6]	1	0	0	0	1
(399999.6, 499999.5]	0	0	0	0	က

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	ınce Covera	Insurance Coverage Type (GRP, DIR, PUB)	3RP, DIR	, PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
(899999.1, 999999.0]	0	0	0	0	1
DST_VAL2: Retirement income amount, distribution source 2					
${\rm Universe:\ DST_SC2} = 1$					
(-75.0, 7500.0]	15,034	38,719	14,208	9,469	80,158
(7500.0, 15000.0]	1	20	21	15	4
(15000.0, 22500.0]	0	0	ಣ	2	0
(22500.0, 30000.0]	0	0	1	v	3
(30000.0, 37500.0]	0	1	1	0	0
(37500.0, 45000.0]	0	0	П	1	0
(45000.0, 52500.0]	0	1	0	0	0
(52500.0, 60000.0]	0	1	4	1	0
(60000.0, 67500.0]	0	2	0	0	0
(67500.0, 75000.0]	0	1	2	2	0

DST_VAL2_YNG: Retriement Distribution amount 2, under age 58

Universe: DST_SC2_YNG = 1

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR	PUB)
OT COTTON A	NNN	NNY	$^{-}$ N $^{-}$	Y1Y	YNN
(-43.0, 4300.0]	15,032	38,742	14,241	9,494	80,157
(4300.0, 8600.0]	2	1	0	1	4
(8600.0, 12900.0]	0	1	0	0	П
(21500.0, 25800.0]	0	0	0	0	П
(30100.0, 34400.0]	0	1	0	0	2
(38700.0, 43000.0]	П	0	0	0	0
DST_YN: Retirement income distribution y/n					
Universe: Persons aged 58 and over (a_age $>=58$)					
Niu	13,643	23,641	7,180	3,933	72,508
Yes	53	1,693	1,543	1,228	480
No	1,339	13,411	5,518	4,334	7,177
DST_YN_YNG: Retriement Distribution Recipiency, person under age 58					
Universe: Persons under age $58 (a_a - age < 58)$					
Niu	3,823	25,271	8,549	6,722	25,286
Yes	85	94	78	71	919

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
V CALICODICO	NNN	NNY	NY_	Y1Y	YNN
No	11,127	13,380	5,614	2,702	53,960
ED_VAL: Total amount of educational assistance received (combined amounts					
in pell grant and other educational) assistance during 20 ?					
${\rm Universe}\colon {\rm ED_YN} = 1$					
(-99.999, 9999.9]	14,940	38,640	14,141	9,451	79,622
(9999.9, 19999.8]	62	73	20	21	289
(19999.8, 29999.7]	20	17	26	10	141
$(29999.7,\ 39999.6]$	7	∞	6	6	59
(39999.6, 49999.5]	63	7	2	1	28
$(49999.5,\ 59999.4]$	4	2	ಬ	7	16
(59999.4, 69999.3]	0	1	4	0	33
(69999.3, 79999.2]	0	0	0	0	2
(79999.2, 89999.1]	0	2	2	0	က
(89999.1, 99999.0]	0	0	2	1	2

 $\ensuremath{\mathsf{ED}}\xspace$ YN: Did ... receive educational assistance?

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR.	PUB)
Variable V	NNN	NNY	$^{-}$ N $^{-}$	Y1Y	YNN
Universe: All Persons aged $15+$					
Niu	2,431	10,167	1,488	1,160	17,629
Yes	430	611	303	159	1,946
No	12,174	27,967	12,450	8,176	60,590
FIN_VAL: How much did receive in financial assistance income during 20					
${\rm Universe:\ FIN_YN} = 1$					
(-500.0, 50000.0]	15,033	38,742	14,238	9,491	80,147
(50000.0, 100000.0]	2	သ	က	4	15
(100000.0, 150000.0]	0	0	0	0	2
(450000.0, 500000.0]	0	0	0	0	1
FIN_YN: Did receive financial assistance?					
Universe: All Persons aged $15+$					
Niu	2,431	10,167	1,488	1,160	17,629
Yes	166	321	141	75	406

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

$V_{ m arrighle}$	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
V CALICADATA	NNN	NNY	NY_	Y1Y	YNN
No	12,438	28,257	12,612	8,260	62,130
INT_VAL: Edited total combined interest income					
${\rm Universe}\colon {\rm INT_YN} = 1$					
(-280.0, 28000.0]	14,979	38,527	13,944	9,220	78,544
(28000.0, 56000.0]	31	126	164	145	937
(56000.0, 84000.0]	16	41	09	46	281
(84000.0, 112000.0]	7	45	99	73	354
(112000.0, 140000.0]	1	4	<u></u>	10	35
(140000.0, 168000.0]	1	П	0	0	11
(168000.0, 196000.0]	0	0	0	1	1
(196000.0, 224000.0]	0	П	0	0	1
(252000.0, 280000.0]	0	0	0	0	-
INT_YN: Edited total combined interest income, y/n					
Universe: All Persons aged 15+					
Niu	2,431	10,167	1,488	1,160	17,629

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR.	PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
Yes	3,950	9,847	7,759	5,700	40,283
No	8,654	18,731	4,994	2,635	22,253
OED_TYP1: Source 1 other than gi bill received (OED_TYP1- source of other					
government assistance)					
${\rm Universe}\colon {\rm ED_YN} = 1$					
Niu	14,584	38,089	13,928	9,331	78,173
Yes	102	144	62	44	321
No	349	512	251	120	1,671
OED_TYP2: Source 2 other than gi bill received (OED_TYP2- scholarships,					
grants etc. from the school)					
${\rm Universe}\colon {\rm ED_YN} = 1$					
Niu	14,584	38,089	13,928	9,331	78,173
Yes	146	211	153	61	986
No	305	445	160	103	1,006

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insur	ance Cover	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
OED_TYP3: Source other than gi bill received (OED_TYP3- other assistance					
(employers friends, etc.)					
${\rm Universe}\colon {\rm ED_YN} = 1$					
Niu	14,584	38,089	13,928	9,331	78,173
Yes	51	51	41	26	375
No	400	902	272	138	1,617
Ol_OFF: Other income sources					
Universe: $OI_YN = 1$					
Niu	14,824	38,368	14,077	9,332	79,115
Social security	1	2	1	0	က
Private pensions	0	ಬ	3	က	rO
Afdc	9	9	3	0	13
Other public assistance	0	2	0	1	ಬ
Dividends	0	1	0	0	0
Rents or royalties	2	П	ಣ	0	<u></u>

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variahle	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	3RP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
State disability payments (worker's comp)	1	1	0	1	1
Disability payments (own insurance)	0	1	0	0	4
Annuities or paid up insurance policies	1	1	1	0	7
Anything else	192	330	137	150	696
Alimony	∞	27	16	∞	41
OI_VAL: How much did receive in other incomes					
${\rm Universe}\colon {\rm OI_YN} = 1$					
$(-950.0,\ 95000.0]$	15,033	38,744	14,240	9,488	80,149
(95000.0,190000.0]	2	0	1	ಬ	12
(190000.0, 285000.0]	0	0	0	1	0
(285000.0, 380000.0]	0	1	0	0	1
(380000.0, 475000.0]	0	0	0	П	П
(475000.0, 570000.0]	0	0	0	0	П
(855000.0,950000.0]	0	0	0	0	1

OL_YN: Did ... receive cash income not already covered from any other source?

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
OTGOTTO A	NNN	NNY	$^{-}$ NY	Y1Y	YNN
Universe: All Persons aged 15+					
None or niu	2,431	10,167	1,488	1,160	17,629
Yes	211	377	164	163	1,050
No	12,393	28,201	12,589	8,172	61,486
PEN_SC1: Retirement income, pension source 1					
${\rm Universe:\ PEN_YN} = 1$					
Niu	14,862	36,035	12,394	7,307	79,002
Company pension	48	1,416	1,039	872	419
Union pension	15	264	176	183	94
Federal government pension	22	173	92	262	130
State government pension	21	524	397	643	336
Local government pension	10	162	84	168	129
Us military pension	26	118	15	15	35
Us railroad retirement	0	10	9	∞	7
Other	1	43	54	37	18

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	ınce Cover	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
PEN_SC2: Retirement income, pension source 2					
${\rm Universe:\ PEN_VAL2}>0$					
Niu	15,028	38,634	14,198	9,420	80,137
Union pension	1	21	16	20	4
Federal government pension	0	∞	က	9	1
State government pension	1	17	6	29	∞
Local government pension	0	6	4	9	9
Us military pension	ಬ	49	ಬ	11	7
Us railroad retirement	0	1	0	0	0
Other	0	9	9	3	2
PEN_VAL1: Retirement income amount, pension source 1					
${\rm Universe:\ PEN_SC1} > 0$					
(-999.999, 99999.9]	15,031	38,709	14,220	9,454	80,129
(99999.9, 1999999.8]	4	21	16	33	27
$(1999999.8,\ 2999999.7]$	0	ಣ	П	ಣ	ಣ

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variahla	Insura	ance Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR.	PUB)
A CRITCHOLD V	NNN	NNY	NY_	Y1Y	YNN
(299999.7, 399999.6]	0	3	П	1	1
(399999.6, 499999.5]	0	က	1	0	2
(599999.4, 699999.3]	0	2	0	0	0
(699999.3, 799999.2]	0	1	0	0	0
(899999.1, 999999.0]	0	က	2	4	က
PEN_VAL2: Retirement income amount, pension source 2					
${\rm Universe:\ PEN_SC2} > 0$					
(-360.0, 36000.0]	15,033	38,737	14,239	9,485	80,158
(36000.0, 72000.0]	1	9	1	7	9
(72000.0, 108000.0]	1	1	1	2	1
(108000.0, 144000.0]	0	0	0	1	0
(324000.0, 360000.0]	0	П	0	0	0
PEN_YN: Retirement income, pension y/n					
Universe: All Persons aged 15+					
Niu	2,431	10,167	1,488	1,160	17,629

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY	Y1Y	YNN
Yes	173	2,710	1,847	2,188	1,163
No	12,431	25,868	10,906	6,147	61,373
PNSN_VAL: Total combined amount of pension income received from all					
pension sources					
${\rm Universe:\ PEN_YN} = 1$					
[-999.999, 99999.9]	15,030	38,707	14,219	9,451	80,125
(99999.9, 1999999.8]	ಬ	22	17	36	31
(1999999.8, 2999999.7]	0	3	1	က	3
$(2999999.7,\ 399999.6]$	0	4	1	1	1
$(399999.6,\ 499999.5]$	0	3	1	0	2
(599999.4, 699999.3]	0	2	0	0	0
(699999.3, 799999.2]	0	1	0	0	0
(899999.1, 999999.0]	0	3	2	4	3

PTOTVAL: Total persons income

Universe: All Persons aged 15+

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR.	PUB)
VOLTOOLIA	NNN	NNY	$^{-}$ N $^{-}$	Y1Y	YNN
(-12094.703, 199571.3]	14,933	38,563	13,963	9,239	77,720
(199571.3, 409141.6]	78	150	209	217	1,918
(409141.6, 618711.9]	13	21	35	24	282
(618711.9, 828282.2]	ಬ	ಗು	14	3	74
(828282.2, 1037852.5]	3	4	4	7	09
(1037852.5, 1247422.8]	3	21	13	ស	100
(1247422.8, 1456993.1]	0	0	2	0	∞
(1456993.1, 1666563.4]	0	0	0	0	1
$(1876133.7,\ 2085704.0]$	0	0	1	0	2
RESNSS1: What were the reasons (you/name) (was/were) getting Social					
Security Income last year?					
${\rm Universe:~SS_YN} = 1$					
Niu	14,638	25,268	8,599	5,024	78,937
Retired	195	10,639	5,128	3,924	693
Disabled (adult or child)	138	2,272	280	266	293

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

$V_{ m ania}$ hle	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	R.P. DIR,	PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
Widowed	25	208	93	22	51
Spouse	4	89	39	45	6
Surviving child	16	54	11	18	22
Dependent child	6	59	12	7	36
On behalf of surviving, dependent, or disabled child (ren)	∞	61	9	10	51
Other (adult or child)	2	95	73	144	18
RESNSS2: What were the reasons (you/name) (was/were) getting Social					
Security Income last year?					
${\rm Universe}\colon\thinspace SS_{\rm YN}=1$					
Niu	15,018	38,345	14,129	9,409	80,099
Disabled (adult or child)	2	164	28	20	<u></u>
Widowed	0	103	20	31	က
Spouse	3	20	4	4	က
Surviving child	0	ಬ	2	0	က
Dependent child	0	4	0	0	2

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	ance Cover	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR	PUB)
A CALICADIO	NNN	NNY	NY_	Y1Y	YNN
On behalf of surviving, dependent, or disabled child(ren)	111	89	22	21	47
Other (adult or child)	1	15	9	10	П
RESNSSI1: What were the reasons (you/name) (was/were) getting					
Supplemental Security Income last year?					
${\rm Universe}\colon {\rm SSI}_{\rm YN}=1$					
Niu	14,976	36,504	14,140	9,303	80,055
Disabled (adult or child)	39	1,992	22	159	99
Blind (adult or child)	0	25	2	1	2
On behalf of a disabled child	16	τυ 80	9	10	25
On behalf of a blind child	0	2	0	0	1
Other (adult or child)	4	164	16	22	16
RESNSSI2: What were the reasons (you/name) (was/were) getting					
Supplemental Security Income last year?					
${\rm Universe}\colon {\rm SSI}_{\rm YN}=1$					
Niu	15,031	38,715	14,240	9,493	80,162

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insuran	ce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
Blind (adult or child)	0	2	0	0	0
On behalf of a disabled child	2	14	0	1	1
Other (adult or child)	2	11	1	1	2
RETCB_VAL: Retirement contribution, amount					
${\rm Universe}\colon {\rm RETCB_YN} = 1$					
[-32.0, 3200.0] 14,56	14,564	38,456	13,704	8,916	67,888
(3200.0, 6400.0] 25	256	114	243	252	5,011
(6400.0, 9600.0]	63	09	116	117	2,102
(9600.0, 12800.0]	62	47	52	92	1,625
(12800.0, 16000.0]	31	18	22	30	945
[16000.0, 19200.0]	37	10	20	46	1,617
(19200.0, 22400.0]	10	17	18	23	279
(22400.0, 25600.0]	12	20	32	48	632
(25600.0, 28800.0]	0	0	0	7	22
(28800.0, 32000.0]	0	3	4	ಬ	44

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
V CALLOOLIA	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
RETCB_YN: Retirement contribution, y/n					
Universe: All people 15 years and over					
Niu	13,470	34,901	10,249	6,228	53,437
Yes	1,034	793	1,070	1,247	21,810
No	531	3,051	2,922	2,020	4,918
RINT_SC1: Interest income, retirement source 1					
${\rm Universe}\colon {\rm RINT_YN} = 1$					
Niu	13,470	34,901	10,249	6,228	53,437
401k account	973	1,925	1,791	1,791	19,885
403b account	09	121	118	188	2,112
Roth ira	216	421	583	292	1,465
Regular ira	163	1,063	1,207	711	1,239
Keogh plan	0	ಬ	11	4	23
Sep plan (simplified employee pension)	19	49	86	43	305
Other type of retirement account	134	260	184	238	1,699

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

$V_{ m ania}$ hle	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	3RP, DIR,	PUB)
OTCODI TO	NNN	NNY	$^{-}$ N $^{-}$	Y1Y	YNN
RINT_SC2: Interest income, retirement source 2					
${\rm Universe}\colon {\rm RINT_YN} = 1$					
Niu	14,818	38,284	13,614	8,981	75,781
403b account	10	27	23	34	351
Roth ira	92	113	154	163	2,018
Regular ira	65	255	342	228	1,284
Keogh plan	0	1	9	0	10
Sep plan (simplified employee pension)	7	16	48	18	162
Other type of retirement account	43	49	54	71	559
RINT_VAL1: Interest income amt, retirement source 1					
${\rm Universe:\ RINT_SC1} > 0$					
(-100.0, 10000.0]	14,936	38,372	13,795	9,102	77,436
(10000.0, 20000.0]	51	173	178	147	1,160
(20000.0, 30000.0]	17	09	98	89	496
(30000.0, 40000.0]	6	45	56	40	274

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

$\Lambda_{ m aris}$	Insura	ınce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
VOLIGIDIA V	NNN	NNY	NY_	Y1Y	YNN
(40000.0, 50000.0]	9	28	43	46	287
(50000.0, 60000.0]	က	ಗು	16	7	82
(60000.0, 70000.0]	က	6	12	10	75
(70000.0, 80000.0]	ಬ	13	6	17	71
(80000.0, 90000.0]	0	2	9	4	26
(900000.0, 1000000.0]	ಬ	38	40	54	255
RINT_VAL2: Interest income amt, retirement source 2					
${\rm Universe:\ RINT_SC2} > 0$					
(-100.0, 10000.0]	15,015	38,701	14,182	9,431	79,816
(10000.0, 20000.0]	6	14	22	25	140
(20000.0, 30000.0]	0	13	14	16	44
(30000.0, 40000.0]	2	2	2	4	39
(40000.0, 50000.0]	က	9	<u></u>	က	15
(50000.0, 60000.0]	2	2	1	က	11
(60000.0, 70000.0]	П	0	П	1	14

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variabla	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
V CALICADIO	NNN	NNY	NY_	Y1Y	YNN
(70000.0, 80000.0]	0	2	2	က	12
(80000.0, 90000.0]	0	0	1	0	6
$(90000.0,\ 1000000.0]$	က	ಬ	6	6	65
RINT_YN: Interest income - retirement, y/n					
Universe: All Persons aged 15+					
Niu	2,431	10,167	1,488	1,160	17,629
Yes	1,565	3,844	3,992	3,267	26,728
No	11,039	24,734	8,761	5,068	35,808
RNT_VAL: How much did receive in income from rent after expenses during					
20?					
Universe: $RNT_YN = 1$					
(-11008.998, 91000.8]	15,031	38,718	14,217	9,473	80,117
(91000.8, 192000.6]	23	25	18	20	26
(192000.6, 293000.4]	0	1	1	0	10
(293000.4, 394000.2]	1	1	1	0	9

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
	NNN	NNY	$^{\rm NY}$	Y1Y	VNN
(394000.2, 495000.0]	0	0	П	П	2
(495000.0, 595999.8]	0	0	0	0	1
(595999.8, 696999.6]	1	0	0	0	1
(898999.2,999999.0]	0	0	3	1	7
RNT_YN: Did own any land, property, rented to others, or receive income					
from royalties, roomers or boarders, or from estates or trusts?					
Universe: All Persons aged 15+					
Niu	2,431	10,167	1,488	1,160	17,629
Yes	290	918	1,088	229	2,802
No	12,314	27,660	11,665	7,658	59,734
SRVS_VAL: Total amount of survivor's income received (combined amounts in					
edited sources sur_val1 and sur_val2 plus the unedited sources 3 & 4 starting					
in 1995)					
${\rm Universe:\ SUR_YN} = 1$					
(-200.0, 20000.0]	15,022	38,674	14,181	9,420	80,073

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

$V_{f arriahle}$	Insura	Insurance Coverage Type (GRP, DIR, PUB)	ge Type (C	GRP, DIR,	PUB)
	NNN	NNY	$^{\rm NY}$	Y1Y	YNN
(20000.0, 40000.0]	2	39	39	48	47
(40000.0, 60000.0]	4	18	∞	14	13
(60000.0, 80000.0]	0	1	3	0	∞
(80000.0, 100000.0]	2	11	∞	13	20
(100000.0, 120000.0]	0	1	T	0	1
(120000.0, 140000.0]	0	1	П	0	1
(140000.0, 160000.0]	0	0	0	0	П
(180000.0, 200000.0]	0	0	0	0	1
SS_VAL: How much did receive in social security payments during 20?					
${\rm Universe}\colon\thinspace SS_{\rm YN}=1$					
(-80.0, 8000.0]	14,729	27,315	9,197	5,611	79,192
(8000.0, 16000.0]	185	5,828	1,913	1,388	471
(16000.0, 24000.0]	91	3,923	2,002	1,553	335
(24000.0, 32000.0]	20	1,192	846	695	113
(32000.0, 40000.0]	2	203	146	140	21

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

$V_{f arright la}$	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
Validorio	NNN	NNY	NY_	Y1Y	YNN
(40000.0, 48000.0]	∞	279	136	107	30
(48000.0, 56000.0]	0	က	1	0	0
(56000.0, 64000.0]	0	0	0	1	1
(72000.0, 80000.0]	0	63	0	0	2
SS_YN: Who received social security payments either for themselves or as					
combined payments with other family members?					
Universe: All Persons aged 15+					
Niu	2,431	10,167	1,488	1,160	17,629
Yes	397	13,477	5,642	4,471	1,228
No	12,207	15,101	7,111	3,864	61,308
SSI_VAL: How much did receive in supplemental security income during					
20?					
${\rm Universe}\colon {\rm SSI_YN} = 1$					
(-50.0, 5000.0]	14,990	37,145	14,170	$9,\!351$	80,087
(5000.0, 10000.0]	35	1,032	35	22	47

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
OTCODIO A	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
(10000.0, 15000.0]	က	388	21	44	21
(15000.0, 20000.0]	1	107	7	10	4
(20000.0, 25000.0]	2	41	က	6	3
(25000.0, 30000.0]	အ	31	ಬ	4	က
(45000.0,50000.0]	П	П	0	0	0
SSI_YN: Did received ssi?					
Universe: All Persons aged $15+$					
Niu	2,431	10,167	1,488	1,160	17,629
Yes	29	2,241	101	192	110
No	12,545	26,337	12,652	8,143	62,426
STRKUC: At any time during 20 did receive any union unemployment or					
strike benefits?					
${\rm Universe}\colon {\rm UC_YN} = 1$					
Niu	2,431	10,167	1,488	1,160	17,629
Yes	4	10	က	4	27

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Cover	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
	NNN	NNY	$^{-}$ N $^{-}$	Y1Y	YNN
No	12,600	28,568	12,750	8,331	62,509
SUBUC: At any time during 20 did receive any supplemental unemployment					
benefits?					
${\rm Universe}\colon {\rm UC_YN} = 1$					
Niu	2,431	10,167	1,488	1,160	17,629
Yes	11	28	6	∞	47
No	12,593	28,550	12,744	8,327	62,489
SUR_SC1: What was the source of this other widow or survivor income?					
${\rm Universe:\ SUR_YN} = 1$					
None or niu	14,986	38,246	13,934	9,233	79,856
Company or union survivor pension	10	206	134	106	44
Federal government	7	49	25	41	26
Us military retirement survivor pension	23	48	10	10	6
State or local gov't survivor pension	3	44	34	39	19
Us railroad retirement survivor pension	2	14	9	က	ಬ

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

$V_{ m amig}$ hle	Insura	ance Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
V CALCOSTO	NNN	NNY	NY_	Y1Y	YNN
Worker compensation survivor	0	2	0	3	33
Black lung	0	1	0	0	1
Regular payments from estates or trusts	∞	40	34	17	62
Regular payments from annuities or paid-up life insurance	9	29	30	15	42
Other or don't know	11	99	34	28	81
SUR_SC2: What was the source of this other widow or survivor income?					
${\rm Universe}\colon {\rm SUR}_{\rm YN}=1$					
None or niu	15,034	38,731	14,233	9,490	80,152
Federal government	0	2	0	0	0
Us military retirement survivor pension	1	2	0	1	0
State or local gov't survivor pension	0	2	33	1	7
Worker compensation survivor	0	1	0	0	0
Black lung	0	0	0	1	0
Regular payments from estates or trusts	0	0	1	0	1
Regular payments from annuities or paid-up life insurance	0	ಸರ	1	2	0

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Cover	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	, PUB)
V Ch. LCh.D.I.C.	NNN	NNY	NY_	Y1Y	YNN
Other or don't know	0	2	3	0	5
SUR_VAL1: How much did receive (survivor source type) during 20?					
${\rm Universe}\colon {\rm SUR_YN} = 1$					
(-100.0, 10000.0]	15,009	38,539	14,106	$9,\!366$	80,014
(10000.0, 20000.0]	13	137	78	26	61
(20000.0, 30000.0]	9	35	25	36	32
(30000.0, 40000.0]	1	ಬ	14	11	15
(40000.0, 50000.0]	3	14	ಬ	10	9
(50000.0, 60000.0]	1	က	က	4	∞
(60000.0, 70000.0]	0	0	1	1	7
(70000.0, 80000.0]	0	1	7	0	1
(90000.0, 100000.0]	2	11	2	111	21
SUR_VAL2: How much did receive (source type) during 20?					
${\rm Universe:\ SUR_YN} = 1$					
(-100.0, 10000.0]	15,035	38,741	14,237	9,493	80,160

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

$V_{ m ania}$ hle	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
(10000.0, 20000.0]	0	1	1	1	0
(20000.0, 30000.0]	0	0	0	0	1
(30000.0, 40000.0]	0	1	0	0	0
(60000.0, 70000.0]	0	1	1	1	0
(90000.0, 100000.0]	0	П	2	0	4
SUR_YN: During 20 did receive any survivor benefits such as widow's pensions, estates, trusts, insurance annuities, or other survivor's income?					
Universe: All Persons aged $15+$					
Niu	2,431	10,167	1,488	1,160	17,629
Yes	49	499	307	262	309
No	12,555	28,079	12,446	8,073	62,227
TRDINT_VAL: Interest amount, exlcuding retirment account interest					
${\rm Universe}\colon {\rm INT_YN} = 1$					
(-99.999, 9999.9]	15,018	38,629	14,089	9,398	79,874
(9999.9, 19999.8]	∞	69	87	53	147

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

$V_{ m amig}$ hle	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
$(19999.8,\ 29999.7]$	3	21	23	14	64
(29999.7, 39999.6]	2	∞	16	∞	24
(39999.6, 49999.5]	0	ಬ	4	2	6
$(49999.5,\ 59999.4]$	П	9	9	4	14
(59999.4, 69999.3]	1	1	1	2	11
(69999.3, 79999.2]	П	1	က	4	7
(79999.2, 89999.1]	1	0	1	2	က
(89999.1, 99999.0]	0	5	11	∞	12
UC_VAL: How much did receive in unemployment benefits during 20?					
${\rm Universe}\colon {\rm UC_YN} = 1$					
(-99.999, 9999.9]	15,013	38,710	14,224	9,465	80,074
(9999.9, 19999.8]	21	26	13	26	79
(19999.8, 29999.7]	П	9	0	1	ಬ
(29999.7, 39999.6]	0	1	0	1	0
(39999.6, 499999.5]	0	П	П	0	4

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
OTOTOTO A	NNN	NNY	$^{-}$ N $^{-}$	Y1Y	VNN
(49999.5, 59999.4]	0		က	2	П
(69999.3, 79999.2]	0	0	0	0	1
(89999.1, 999999.0]	0	0	0	0	П
UC_YN: Any type of unemployment compensation? (Combination of subuc,					
strkuc, and uctot_yn)					
${\rm Universe}\colon {\rm UC}_{\rm YN}=1$					
Niu	2,431	10,167	1,488	1,160	17,629
Yes	180	305	119	154	805
m No	12,424	28,273	12,634	8,181	61,731
VET_TYP1: What type of veterans payments did receive? (VET_TYP1-					
disability compensation?)					
${\rm Universe}\colon {\rm VET_YN} = 1$					
Niu	14,764	37,749	14,043	9,176	79,766
Yes	203	675	131	264	322

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

No No VET_TYP2: What type of veterans payments did receive? (VET_TYP2- survivor benefits?) Universe: VET_YN = 1 Niu Yes No VET TYP3: What type of veterans payments did receive? (VET TYP3-	NNY NN			
ivor benefits?) verse: VET_YP2 = 1 TYP2. 14,764 TYP3: What type of veterans payments did receive? (VET_TYP2- 14,764 267		/_ Y1Y		YNN
ivor benefits?) verse: VET_YN = 1 14,764 TYP3: What type of veterans payments did receive? (VET_TYP2- 14,764 267		3 29	55	22
ivor benefits?) verse: $VET_YN = 1$ 14,764 4 267 TYP3: What type of veterans payments did receive? (VET_TYP3-				
verse: VET_YN = 1 $14,764$ 4 267 $TYP3: What type of veterans payments did receive? (VET TYP3-$				
14,764 4 267 2 TYP3: What type of veterans payments did receive? (VET TYP3-				
[TYP3: What type of veterans payments did receive? (VET TYP3-	37,749 14,043	9,176		79,766
	80	16	14	ಬ
VET TYP3: What type of veterans payments did receive? (VET TYP3-	916	182 30	305 3	394
veteran's pension?)				
${\rm Universe}\colon {\rm VET_YN} = 1$				
Niu 14,764 37,	37,749 14,043	9,176		79,766
Yes	245	41	42	48
No 195	751 1	157 277		351

VET_TYP4: What type of veterans payments did receive? (VET_TYP4-

education assistance?)

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
V CALCOOLO V	NNN	NNY	NY_	Y1Y	VNN
${\rm Universe:\ VET_YN} = 1$					
Niu	14,764	37,749	14,043	9,176	99,766
Yes	14	18	က	2	24
m No	257	826	195	312	375
VET_TYP5: What type of veterans payments did receive? (VET_TYP5-					
other veteran's payments?)					
${\rm Universe}\colon {\rm VET_YN} = 1$					
Niu	14,764	37,749	14,043	9,176	79,766
Yes	∞	33	11	_	12
No	263	963	187	312	387
VET_VAL: How much did receive from veterans' administration during					
20?					
${\rm Universe:\ VET_YN} = 1$					
(-100.0, 10000.0]	14,845	38,124	14,132	9,317	79,960
(10000.0, 20000.0]	61	292	49	2.2	86

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
	NNN	NNY	NY_	Y1Y	YNN
(20000.0, 30000.0]	29	121	20	42	59
(30000.0, 40000.0]	23	134	24	34	25
(40000.0, 50000.0]	18	55	6	19	16
(50000.0, 60000.0]	က	∞	7	2	П
(60000.0, 70000.0]	<u></u>	က	1	2	0
(70000.0, 80000.0]	4	0	1	0	0
(80000.0, 90000.0]	4	2	7	0	က
(90000.0, 100000.0]	3	9	1	2	3
VET_YN: Did receive veterans' payments?					
Universe: All Persons aged 15+					
Niu	2,431	10,167	1,488	1,160	17,629
Yes	271	966	198	319	399
No	12,333	27,582	12,555	8,016	62,137

WC_TYPE: What was source of these payments?

Universe: $WC_YN = 1$

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	ance Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR	, PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
Not in universe	14,980	38,653	14,204	9,447	79,891
State worker's compensation	15	40	14	15	74
Employer or employers insurance	39	42	23	30	187
Own insurance	0	1	0	0	ಬ
Other	1	6	0	က	∞
WC_VAL: How much compensation did receive during 20?					
${\rm Universe}\colon {\rm WC_YN} = 1$					
(-99.999, 9999.9]	15,009	38,712	14,227	9,467	80,086
(9999.9, 19999.8]	17	18	9	19	44
(19999.8, 29999.7]	20	∞	2	2	15
(29999.7, 39999.6]	1	9	ಬ	9	12
(39999.6, 49999.5]	0	0	0	0	3
(49999.5, 59999.4]	Π	0	0	1	0
(59999.4, 69999.3]	0	П	0	0	က
(89999.1, 99999.0]	2	0	1	0	2

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	ance Cover	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR.	PUB)
Variable V	NNN	NNY	$^{-}{ m NY}_{-}$	Y1Y	YNN
WC_YN: During 20 did receive any worker's compensation payments or					
other payments as a result of a job related injury or illness?					
Universe: All Persons aged 15+					
Niu	2,431	10,167	1,488	1,160	17,629
Yes	55	92	37	48	274
No	12,549	28,486	12,716	8,287	62,262
PAW_TYP: What type of program did receive CASH assistance?					
$\ {\rm Universe}\colon {\rm PAW_YN} = 1$					
Niu	15,011	38,275	14,214	9,382	80,127
TANF/AFDC	14	327	13	51	16
Other	∞	130	14	09	21
Both	2	13	0	2	1

PAW_VAL: How much did ... receive in public assistance or welfare during

20..?

Universe: $PAW_YN = 1$

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insur	ance Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR	, PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
(-25.0, 2500.0]	15,018	38,508	14,228	9,445	80,143
(2500.0, 5000.0]	9	115	2	28	∞
(5000.0, 7500.0]	v	53	4	ಬ	9
(7500.0, 10000.0]	2	42	1	∞	က
(10000.0, 12500.0]	က	17	0	ಬ	4
(12500.0, 15000.0]	1	9	0	0	0
(15000.0, 17500.0]	0	1	0	1	0
(17500.0, 20000.0]	0	0	0	2	1
(20000.0, 22500.0]	0	2	0	0	0
(22500.0, 25000.0]	0	1	1	1	0
PAW_YN: At any time during 20, even for one month, did receive an CASH	ın CASH				

PAW_YN: At any time during 20.., even for one month, did... receive an CASH assistance from a state or county welfare program such as (State program name fill)?

Universe: All Persons aged 15+

1,160
1,488
10,167
2,431
Niu

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY	Y1Y	YNN
Yes	24	470	27	113	38
No	12,580	28,108	12,726	8,222	62,498
PENINCL: Was included in that plan?					
${\rm Universe}\colon {\rm PENPLAN}=1$					
Niu	12,999	36,775	12,935	7,709	54,529
Yes	1,334	966	775	1,381	21,824
No	702	974	531	405	3,812
PENPLAN: Other than social security did the employer or union that worked					
for in 20 have a pension or other type of retirement plan?					
${\rm Universe}\colon {\rm WRK_CK} = 1$					
Niu	6,201	29,895	8,039	5,508	27,806
Yes	2,036	1,970	1,306	1,786	25,636
No	6,798	6,880	4,896	2,201	26,723

WICYN: Who received WIC?

Universe: Adult female

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insur	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR.	PUB)
	NNN	NNY	$^{ m NY}$	Y1Y	YNN
Niu	10,363	30,214	11,865	8,177	56,383
Received WIC	207	717	59	110	390
Did not receive WIC	4,465	7,814	2,317	1,208	23,392
CHCARE_YN: Paid child care was needed for this child?					
Universe: Persons age $15+$ with children					
Niu	12,604	28,578	12,753	8,335	62,536
Yes	361	1,381	252	233	4,405
No	2,070	8,786	1,236	927	13,224
CHELSEW_YN: Does this person have a child living outside the household?					
Universe: All persons aged 15+					
Niu	2,431	10,167	1,488	1,160	17,629
Yes	386	443	163	129	1,438
No	12,218	28,135	12,590	8,206	61,098
CHSP VAL: What is the annual amount of child support paid?					

CHSP_VAL: What is the annual amount of child support paid?

Universe: $CHSP_YN = 1$

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insuran	ce Covera	Insurance Coverage Type (GRP, DIR, PUB)	3RP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
[-99.999, 9999.9]	15,003	38,723	14,222	9,484	79,970
(9999.9, 19999.8]	26	19	14	7	141
(19999.8, 29999.7]	4	П	1	23	41
(29999.7, 39999.6]	1	П	4	0	က
(39999.6, 49999.5]	1	0	0	1	2
(49999.5, 59999.4]	0	0	0	1	1
(59999.4, 69999.3]	0	П	0	0	1
(69999.3, 79999.2]	0	0	0	0	1
(89999.1, 99999.0]	0	0	0	0	က
CHSP_YN: Is this person required to pay child support?					
Universe: CHELSEW_YN					
Niu	14,649	38,302	14,078	$9,\!366$	78,727
Yes	194	136	70	41	681
No	192	307	93	88	757

CSP_VAL: How much did ... receive in child support payments?

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
V CALCODIO.	NNN	NNY	NY_	Y1Y	YNN
$\label{eq:chisp} \text{Universe: CHSP_YN} = 1$					
(-99.999, 9999.9]	15,010	38,682	14,215	9,484	79,977
(9999.9, 19999.8]	19	48	18	∞	148
(19999.8, 29999.7]	ಬ	10	ಬ	1	23
(29999.7, 39999.6]	0	4	1	1	11
(39999.6, 49999.5]	1	0	1	1	7
(49999.5, 59999.4]	0	0	0	0	1
(69999.3, 79999.2]	0	0	1	0	0
(89999.1, 99999.0]	0	П	0	0	33
CSP_YN: Did receive child support payments?					
Universe: All Persons aged $15+$					
Niu	2,431	10,167	1,488	1,160	17,629
Yes	201	260	112	136	1,080
No	12,403	28,018	12,641	8,199	61,456

ACTC_CRD: Additional child tax credit

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
Universe: Tax unit head or dependent filer					
(-11.1, 1110.0]	13,939	37,125	13,926	9,144	78,392
(1110.0, 2220.0]	534	804	153	168	833
(2220.0, 3330.0]	359	525	102	119	260
(3330.0, 4440.0]	153	215	45	42	256
(4440.0, 5550.0]	27	33	ಬ	12	59
(5550.0, 6660.0]	17	29	∞	∞	41
(6660.0, 7770.0]	3	∞	2	1	15
(7770.0, 8880.0]	2	4	0	0	4
(8880.0, 9990.0]	П	2	0	1	4
(9990.0, 11100.0]	0	0	0	0	П
AGI: Adjusted gross income					
Universe: Tax unit head or dependent filer					
(-12341.073, 224208.3]	14,924	38,542	13,917	9,179	77,141
(224208.3, 458415.6]	88	171	256	278	2,438

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Veriable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
Validolo	NNN	NNY	NY_	Y1Y	YNN
(458415.6, 692622.9]	14	21	33	21	325
(692622.9, 926830.2]	4	ಗು	16	4	86
(926830.2, 1161037.5]	4	ಗು	11	6	87
$(1161037.5,\ 1395244.8]$	0	0	4	2	26
(1395244.8, 1629452.1]	0	1	1	2	7
$(1629452.1,\ 1863659.4]$	0	0	1	0	1
$(1863659.4,\ 2097866.7]$	0	0	1	0	9
(2097866.7, 2332074.0]	0	0	П	0	9
CTC_CRD: Child tax credit					
Universe: Tax unit head or dependent filer					
(-18.0, 1800.0]	13,956	38,047	13,477	8,913	69,728
(1800.0, 3600.0]	646	462	418	331	5,280
(3600.0, 5400.0]	327	186	250	182	3,845
(5400.0, 7200.0]	73	41	78	52	1,015
(7200.0,9000.0]	26	∞	15	15	236

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
	NNN	NNY	NY_{-}	Y1Y	YNN
(9000.0, 10800.0]	ಬ	П	2	2	40
(10800.0, 12600.0]	23	0	0	0	17
(12600.0, 14400.0]	0	0	0	0	2
(14400.0, 16200.0]	0	0	1	0	0
(16200.0, 18000.0]	0	0	0	0	2
EIT_CRED: Earn income tax credit					
Universe: Tax unit head or dependent filer					
(-6.557, 655.7]	13,787	36,710	13,872	9,134	78,356
(655.7, 1311.4]	106	159	45	40	348
(1311.4, 1967.1]	127	149	72	22	330
(1967.1, 2622.8]	153	229	44	46	281
(2622.8, 3278.5]	135	248	45	54	207
(3278.5, 3934.2]	263	420	62	09	266
(3934.2, 4589.9]	92	184	36	24	120
(4589.9, 5245.6]	88	152	20	26	98

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
VOLTOODI V	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
(5245.6, 5901.3]	168	306	28	39	117
(5901.3, 6557.0]	116	188	17	17	54
FED_RET: Federal retirement payroll deduction					
Universe: Tax unit head or dependent filer					
(-16.9, 1690.0]	15,032	38,744	14,241	9,491	80,153
(1690.0, 3380.0]	0	0	0	0	2
(3380.0, 5070.0]	T	1	0	0	2
(5070.0, 6760.0]	2	0	0	1	4
(6760.0, 8450.0]	0	0	0	0	1
(8450.0, 10140.0]	0	0	0	2	2
(10140.0, 11830.0]	0	0	0	0	1
(15210.0, 16900.0]	0	0	0	П	0
FEDTAX_AC: Federal income tax liability, after all credits					
Universe: Tax unit head or dependent filer					
(-10797.046, 69805.6]	15,001	38,684	14,139	9,415	79,276

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	Insurance Coverage Type (GRP, DIR, PUB)	nge Type ((GRP, DIR,	PUB)
VOL ICO OLO	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
(69805.6, 149610.2]	22	49	99	62	605
(149610.2, 229414.8]	∞	ಗು	18	9	94
(229414.8, 309219.4]	2	က	7	4	62
(309219.4, 389024.0]	2	က	7	9	91
(389024.0, 468828.6]	0	1	1	2	23
(468828.6, 548633.2]	0	0	23	0	4
(628437.8, 708242.4]	0	0	1	0	9
(708242.4, 788047.0]	0	0	0	0	4
FEDTAX_BC: Federal income tax liability, before credits					
Universe: Tax unit head or dependent filer					
(-788.047, 78804.7]	15,006	38,696	14,150	9,434	79,411
(78804.7, 157609.4]	18	37	29	43	473
(157609.4, 236414.1]	7	ಬ	14	9	96
(236414.1, 315218.8]	2	ಣ	7	4	62
(315218.8, 394023.5]	2	က	~	9	06

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

$V_{ m emis}$ blo	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
Validatio	NNN	NNY	NY_	Y1Y	YNN
(394023.5, 472828.2]	0	1	1	2	19
(472828.2, 551632.9]	0	0	2	0	4
(630437.6, 709242.3]	0	0	1	0	9
(709242.3, 788047.0]	0	0	0	0	4
FICA: Social security retirement payroll deduction					
Universe: All persons					
(-55.449, 5544.9]	14,080	38,087	12,928	8,678	63,814
(5544.9, 11089.8]	821	521	626	661	14,090
(11089.8, 16634.7]	86	66	209	123	1,751
(16634.7, 22179.6]	23	29	82	19	287
(22179.6, 27724.5]	9	ಬ	21	6	78
(27724.5, 33269.4]	ಗು	4	13	ರ	134
(33269.4, 38814.3]	0	0	4	0	9
(38814.3, 44359.2]	1	0	2	0	1
(44359.2, 49904.1]	П	0	0	0	က

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
(49904.1, 55449.0]	0	0	0	0	1
FILESTAT: Tax filer status					
Universe: All persons					
${\rm Joint,\ both < 65}$	4,721	3,600	2,931	1,621	33,473
Joint, one $><65\ \&$ one $65+$	235	1,045	692	782	1,812
${\bf Joint,\ both\ 65+}$	29	3,661	2,693	2,660	271
Head of household	764	1,485	350	299	3,024
Single	4,246	5,595	3,652	1,956	17,561
Non-filer	5,002	23,359	3,923	2,177	24,024
MARG_TAX: Marginal tax rate					
Universe: Tax unit head or dependent filer					
(-0.037, 3.7]	9,196	31,832	8,644	5,356	45,074
(7.4, 11.1]	1,801	2,645	1,229	717	3,139
(11.1, 14.8]	3,127	2,994	2,557	1,813	14,677
(18.5, 22.2]	289	920	1,267	1,088	11,655

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insur	Insurance Coverage Type (GRP, DIR, PUB)	ige Type (C	3RP, DIR	PUB)
VOLTOOLI V	NNN	NNY	$^{-}$ NY	Y1Y	YNN
(22.2, 25.9]	174	259	404	403	4,335
(29.6, 33.3]	15	39	53	62	523
(33.3, 37.0]	35	26	87	56	762
PRSWKXPNS: Work expenses					
Universe: $A_AGE > 17$ or $HHDFMX = 1,2,46$, or 47					
(-2.065, 206.5]	6,481	30,475	8,279	5,658	29,096
(206.5, 413.0]	131	275	104	94	470
(413.0, 619.5]	175	312	141	101	591
(619.5, 826.0]	210	347	136	124	029
(826.0, 1032.5]	131	225	119	98	416
(1032.5, 1239.0]	352	504	210	178	879
(1239.0, 1445.5]	228	252	155	108	969
(1445.5, 1652.0]	292	336	238	161	1,100
(1652.0, 1858.5]	265	284	167	124	696
(1858.5, 2065.0]	6,770	5,735	4,692	2,861	45,278

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insur	ance Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR.	PUB)
OTTODAY A	NNN	NNY	$^{-}$ N $^{-}$	Y1Y	YNN
STATETAX_A: State income tax liability, after all credits					
Universe: Tax unit head or dependent filer					
(-6490.585, 19727.5]	15,009	38,704	14,157	9,429	79,338
(19727.5, 45686.0]	20	37	63	54	637
(45686.0, 71644.5]	9	က	15	9	113
(71644.5, 97603.0]	0	0	2	9	35
(97603.0, 123561.5]	0	1	4	0	25
(123561.5, 149520.0]	0	0	0	0	10
(149520.0, 175478.5]	0	0	0	0	1
(175478.5, 201437.0]	0	0	0	0	က
(201437.0, 227395.5]	0	0	0	0	7
(227395.5, 253354.0]	0	0	0	0	1
STATETAX_B: State income tax liability, before credits					
Universe: Tax unit head or dependent filer					
$(-253.354,\ 25335.4]$	15,017	38,718	14,185	9,458	79,632

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	RP, DIR,	PUB)
V CLICOTO V	NNN	NNY	NY_	Y1Y	YNN
(25335.4, 50670.8]	12	23	38	28	377
(50670.8, 76006.2]	9	က	12	4	83
(76006.2, 101341.6]	0	0	2	ಬ	39
(101341.6, 126677.0]	0	1	4	0	18
(126677.0, 152012.4]	0	0	0	0	6
$(152012.4,\ 177347.8]$	0	0	0	0	1
(177347.8, 202683.2]	0	0	0	0	က
(202683.2, 228018.6]	0	0	0	0	2
(228018.6, 253354.0]	0	0	0	0	1
TAX_INC: Taxable income amount					
Universe: Tax unit head or dependent filer					
$(-2298.214,\ 229821.4]$	14,968	38,607	14,027	9,280	78,079
(229821.4, 459642.8]	49	112	153	185	1,604
(459642.8, 689464.2]	11	17	34	14	250
(689464.2,919285.6]	ಬ	4	10	4	78

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variahle	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	GRP, DIR,	PUB)
	NNN	NNY	$^{-}$ NY	Y1Y	YNN
(919285.6, 1149107.0]	2	4	11	6	93
(1149107.0, 1378928.4]	0	1	က	က	45
(1378928.4, 1608749.8]	0	0	2	0	4
(1608749.8, 1838571.2]	0	0	0	0	1
(1838571.2, 2068392.6]	0	0	0	0	9
(2068392.6, 2298214.0]	0	0	Н	0	ಬ
PERLIS: Poverty level of persons (Subfamily members have primary family					
recode)					
Universe: All persons					
Not in poverty universe	29	173	6	37	46
Below poverty level	2,650	10,405	1,038	549	1,873
100 - 124 percent of the poverty level	872	3,558	448	302	868
125 - 149 percent of the poverty level	896	3,113	206	303	1,240
150 and above the poverty level	10,516	21,496	12,240	8,304	76,108

POV_UNIV: Poverty universe flag

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

$V_{ m ania}$ blo	Insura	nce Covera	Insurance Coverage Type (GRP, DIR, PUB)	3RP, DIR,	PUB)
Addition	NNN	NNY	NY_	Y1Y	YNN
Universe: All persons					
Not in poverty universe	29	173	6	37	46
In poverty universe	15,006	38,572	14,232	9,458	80,119
HEA: Health status					
Universe: All persons					
Excellent	4,703	8,539	4,173	2,207	32,776
Very good	4,895	9,678	4,540	3,038	29,492
Good	4,164	11,856	3,859	2,899	15,028
Fair	1,039	6,158	1,247	1,007	2,439
Poor	234	2,514	422	344	430
SPM_ACTC: SPM units Additional Child Tax Credit					
Universe: All persons					
(-11.1, 1110.0]	11,509	28,742	13,080	8,266	72,935
(1110.0, 2220.0]	1,538	3,848	513	202	3,105
(2220.0, 3330.0]	1,172	3,423	362	420	2,227

Table 3.6: Number of survey participants by health factors and five insurance coverage combinations of enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) (continued)

Variable	Insura	Insurance Coverage Type (GRP, DIR, PUB)	ge Type (C	GRP, DIR,	PUB)
OTODI TO	NNN	NNY	$^{-}$ NY $^{-}$	Y1Y	YNN
(3330.0, 4440.0]	583	1,834	215	176	1,141
(4440.0, 5550.0]	111	393	26	52	337
(5550.0, 6660.0]	74	314	36	99	233
(6660.0, 7770.0]	25	111	6	2	116
(7770.0, 8880.0]	11	41	0	П	43
(8880.0, 9990.0]	6	32	0	12	15
(9990.0, 11100.0]	ಣ	7	0	0	13

Code 3.8: Exploratory data analysis (describe.py)

```
1 import os
  import pandas as pd
  import warnings
4
  from module.utility import create_dir, import_dict
  from module.eda import *
7 from module.dataset import *
   from cls.ThesisExtension import *
9
   texlive_binpath = '/usr/local/texlive/2024/bin/x86_64-linux'
11
   os.environ['PATH'] += os.pathsep + texlive_binpath
12
13
   pd.set_option('display.max_columns', None)
   pd.set_option('display.width', 1000)
   warnings.filterwarnings('ignore')
16
17 # Given Information
   dataset_name = "pppub20"
18
19
  # Predefined Directories
20
21
   meta_dir = "../../Data/Original/metadata"
   feather_dir = "../../Data/Original/feather"
22
   csv_dir = "../../Data/Original/csv"
23
24
   output_dir = f"../../Outputs/Main/EDA/{dataset_name}"
   log_dir = f"../../Logs/preprocessing"
26
   log_filepath = f"{log_dir}/describe.log"
27
28
   backup_dir = "../../Backups"
29
30
   create_dir(log_dir)
31
32
```

```
33 # Data Preparation
34 indep_dict = import_dict(metadatapath=f"{meta_dir}/meta-indep.json")
35 dep_attrs = ['GRP', 'DIR', 'PUB']
36 print()
37 describe_var(indep_dict)
38 print()
39 df = import_dataset(dataset_name=dataset_name, feather_dir=feather_dir)
40 print()
41 dep_features = ['class_orig', 'code_orig', 'code', 'class']
42 acpt_types = {'category', 'int16', 'int32', 'int8', 'uint16', 'uint32', '
       uint8'}
43 preprocess = True
44
   if all(feat in df.columns for feat in dep_features):
45
       col_types = set()
46
       for col in df.columns:
47
48
           col_types.add(str(df[col].dtype))
49
          if col_types == acpt_types:
50
              preprocess = False
51
   if preprocess:
53
       df.thesis.code(indep_dict, dep_attrs)
54
       df.thesis.recode()
55
   filepath_feather = f"{feather_dir}/{dataset_name}.feather"
   filepath_csv = f"{csv_dir}/{dataset_name}.csv"
57
58
   if not os.path.isfile(filepath_feather):
59
       export_dataset(df, file_dir='data/feather', dataset_name=dataset_name,
60
          format='feather')
61
62
   if not os.path.isfile(filepath_csv):
63
       dfther = pd.read_feather(filepath_feather)
       export_dataset(dfther, file_dir='data/csv', dataset_name=dataset_name,
64
          format='csv')
```

65

```
66
  # Univariate Data Analysis
  df.thesis.show_type(option='full')
68
   print()
   df[['GRP','DIR','PUB','class_orig','code_orig','code','class']].
      drop_duplicates().sort_values('class').reset_index(drop=True)
70 print(f"Code: Employment-based plan (GRP) | Direct-purchase plan (DIR) |
      Public health insurance (PUB)")
   print(df.groupby('code').size())
71
   print('\n'*2)
72
73
74 # Cross Tabulation Analysis
   print("----")
  crosstab(df=df, indep_dict=indep_dict, cont_bins=10, plot=True, output_dir
      =output_dir, log_filepath=log_filepath, backup_dir=backup_dir)
```

3.5.7 Data Encoding

Code 3.9 encodes the input dataset in the correct format, zero for a continuous NIU (not in universe) value and 0 up to a positive integer for a categorical value, by instantiating the Data class defined in Code 3.6. The state of this instance is maintained by two attached attributes dataset, a pandas DataFrame extended by the data accessor, and metadata, a Python list. The nonstatic methods encodecat and encodecont for encoding categorical and continuous features change the object into multiple states. This dissertation excessively uses the shallow copies of attributes by calling the method copy to protect the originals. Unlike a deep copy, a shallow copy inserts reference to an original object to the extent possible.

Code 3.9: Data encoding (convert.py)

```
7 from cls.Data import *
8
  # Given Information
10 dataset_inname = "pppub20"
   dataset_encname = f"{dataset_inname}enc"
   dataset_procname = "proc20"
12
13
14 # Predefined Directories
15 meta_indir = "../../Data/Original/metadata"
16 meta_extra_indir = f"{meta_indir}/extra"
17 feather_indir = "../../Data/Original/feather"
   csv_indir = "../../Data/Original/csv"
19
   meta_encdir = "../../Data/Encoded/metadata"
20
   meta_extra_encdir = f"{meta_encdir}/extra"
   feather_encdir = "../../Data/Encoded/feather"
22
   csv_encdir = "../../Data/Encoded/csv"
   info_encdir = "../../Data/Encoded/info"
25
   csv_procdir = "../../Data/Processed/csv"
27
28 create_dir(meta_extra_indir)
29 create_dir(feather_indir)
30 create_dir(csv_indir)
31 create_dir(meta_extra_encdir)
32 create_dir(feather_encdir)
33 create_dir(csv_encdir)
34 create_dir(info_encdir)
35 create_dir(csv_procdir)
36
37 # Metadata
38 indep_dict = import_dict(metadatapath=f"{meta_indir}/meta-indep.json")
   export_json(extract_dict_cat(indep_dict), f"{meta_extra_indir}/meta-indep-
       cat.json")
40 export_json(extract_dict_cont(indep_dict), f"{meta_extra_indir}/meta-indep-
       cont.json")
```

```
41
42 # Imported Dataset
   if os.path.isfile(f"{feather_indir}/{dataset_inname}.feather"):
       df = pd.read_feather(f"{feather_indir}/{dataset_inname}.feather")
44
45
       if not os.path.isfile(f"{csv_indir}/{dataset_inname}.csv"):
          df.to_csv(f"{csv_indir}/{dataset_inname}.csv", index=False)
46
47
   else:
       df = pd.read_csv(f"{csv_indir}/{dataset_inname}.csv")
48
49
50 # Encoded Dataset and Dictionary
51 data_obj = Data(df.copy(), indep_dict.copy())
52 cat_var_change = data_obj.encodecat()
53 cont_var_nonpos = data_obj.encodecont()
54 df_enc = data_obj.dataset
   indep_dict_enc = data_obj.metadata
55
56
57 # Processed Dataset
58 dep_attrs = ['GRP', 'DIR', 'PUB']
59 class_attrs = ['class_orig','code_orig','code','class']
60 df_proc_enc = df_enc.drop(columns=['COV']+dep_attrs+class_attrs)
61 df_proc_enc = sort_cols(df_proc_enc, indep_dict_enc).join(df_enc['class'])
  df_proc_info = indep_info(df_proc_enc.loc[:, df_proc_enc.columns != 'class
       '], indep_dict_enc)
   df_count_info = count_info(df_proc_info)
64
65 # Exported Results
66 df_enc.to_feather(f"{feather_encdir}/{dataset_encname}.feather")
   df_enc.to_csv(f"{csv_encdir}/{dataset_encname}.csv", index=False)
67
   export_json(
68
69
       indep_dict_enc,
       f"{meta_encdir}/meta-indep-{dataset_encname}.json"
70
71
   export_json(
72
       extract_dict_cat(indep_dict_enc),
73
74
       f"{meta_extra_encdir}/meta-indep-cat-{dataset_encname}.json"
75 )
```

```
76
   df_proc_enc.to_csv(f"{csv_procdir}/{dataset_procname}.csv", header=True,
77
       index=False)
78
79
   df_proc_info.index = df_proc_info.index + 1
   df_proc_info.to_csv(f"{info_encdir}/{dataset_encname}-info.csv",
80
       index_label="id")
   df_count_info.to_csv(f"{info_encdir}/{dataset_encname}-countinfo.csv",
81
       header=True, index=False)
82
   export_txt(cat_var_change, f"{meta_extra_encdir}/catchange-{
83
       dataset_encname}.txt")
  export_txt(cont_var_nonpos, f"{meta_extra_encdir}/contnonpos-{
       dataset_encname}.txt")
```

3.5.8 Sampling using SelectKBest

Because the classifier proposed in Chapter 4 is exponentially expensive, certain features are preselected by evaluating their scores against a target variable. Code 3.10 considers 3, 4 and 8 highest scores based on the mutual information for a discrete target. In addition, 100 out of 157,681 survey participants are sampled of equal class size by calling two methods groupby and sample. Due to its random nature, the sampling result changes in each call. The use of the model is illustrated in Chapter 5 with only three preselected features.

Code 3.10: SelectKBest (selectkbest.py)

```
import pandas as pd
from functools import partial
from sklearn.feature_selection import mutual_info_classif, SelectKBest

from module.utility import create_dir

sel_num_ls = [3, 4, 8]
train_eachclass_num = 20
```

```
10 data_filepath = "../../../Data/Processed/csv/proc20.csv"
  info_filepath = "../.../Data/Encoded/info/pppub20enc-info.csv"
12
13 data_selname = "selproc20"
14 train_name = "seltrain20"
15 test_name = "seltest20"
16
17 # Predefined Directories
18 sample_dir = "../../Samples/random"
   sel_dir = f"{sample_dir}/{data_selname}"
19
20
21 data_dir = f"{sel_dir}/data"
22 info_dir = f"{sel_dir}/info"
23 feat_dir = f"{sel_dir}/features"
24 score_dir = f"{sel_dir}/scores"
25 train_dir = f"{sel_dir}/train"
26 test_dir = f"{sel_dir}/test"
27
28 create_dir(data_dir)
29 create_dir(info_dir)
30 create_dir(feat_dir)
31 create_dir(score_dir)
32 create_dir(train_dir)
33 create_dir(test_dir)
34
35 # Univariate Feature Selection
   def feat_select(df_indata, df_info, sel_num):
36
       discrete_feat_idx = df_info.index[df_info['type']=='Categorical']
37
       score_func = partial(mutual_info_classif, discrete_features=
38
          discrete_feat_idx)
       feat_selector = SelectKBest(score_func, k=sel_num)
39
40
       feat_selector.fit(df_indata.drop('class', axis=1), df_indata['class'])
41
42
       df_scores = pd.DataFrame()
43
       df_scores["Attribute"] = df_indata.drop('class', axis=1).columns
       df_scores['Type'] = df_info['type']
44
```

```
45
       df_scores["Support"] = feat_selector.get_support()
       df_scores["F Score"] = feat_selector.scores_
46
       df_scores["P Value"] = feat_selector.pvalues_
47
48
49
       df_selfeat = df_scores[df_scores['Support']].drop('Support', axis=1).
          reset_index(drop=True)
       df_seldata = df_indata[df_selfeat['Attribute']].join(df_indata['class'
50
          ])
51
       minmax = df_seldata.loc[:, df_seldata.columns != 'class'].agg(['min','
52
          max']).values.tolist()
53
       df_selfeat['Min'] = minmax[0]
       df_selfeat['Max'] = minmax[1]
54
       del minmax
55
56
57
       return df_seldata, df_selfeat, df_scores
58
59 # Implementation
60 df_indata = pd.read_csv(data_filepath)
61 df_info = pd.read_csv(info_filepath)
62
   print(f"\n{df_indata.head()}\n")
64 print(f"{df_info.head()}\n")
65
66 for sel_num in sel_num_ls:
67
68
       # Univariate feature selection
       df_seldata, df_selfeat, df_scores = feat_select(df_indata=df_indata,
69
          df_info=df_info, sel_num=sel_num)
70
       # Display results (selected features)
71
72
       print(f"Select {sel_num} features:\n")
       print(f"{df_selfeat}\n")
73
74
75
       # Train-test split
       df_seltrain = df_seldata.groupby('class', group_keys=False).apply(
76
```

```
77
           lambda x: x.sample(train_eachclass_num)
       )
78
       df_seltest = df_seldata.drop(df_seltrain.index)
79
80
       # Exported results
81
       df_seldata.to_csv(f"{data_dir}/{data_selname}num{sel_num}.csv", header=
82
           True, index=False)
83
       df_selfeat.to_csv(f"{feat_dir}/fnum{sel_num}.csv", header=True, index=
84
           False)
       df_scores.to_csv(f"{score_dir}/snum{sel_num}.csv", header=True, index=
85
           False)
86
       df_selfeat.index = df_selfeat.index + 1
87
       df_selinfo = df_selfeat.drop(['F Score', 'P Value'], axis=1)
88
89
       df_selinfo.columns = ['variable', 'type', 'min', 'max']
90
       df_selinfo.to_csv(f"{info_dir}/{data_selname}num{sel_num}info.csv",
           index_label='id')
91
92
       df_seltrain.to_csv(f"{train_dir}/{train_name}num{sel_num}each{
           train_eachclass_num \rightarrow csv", header=True, index=False)
93
       df_seltest.to_csv(f"{test_dir}/{test_name}num{sel_num}exc{
           train_eachclass_num}.csv", header=True, index=False)
```

3.5.9 Setting Number of Variable Splits

Provided that two and three splits or cuts are of interest, Code 3.11 determines an appropriate number of splits on an individual feature in the health insurance dataset of all noninfant survey participants with full features and previously preselected 3, 4 and 8 features. For example, in the case of three splits, up to two splits are allowed on the feature SS_YN representing the answer, including NIU (not in universe), to the yes/no question regarding social security payments. The column of these numbers is inserted into the DataFrame as an additional information directly through the pandas accessor info in Code 3.7 without explicit class instantiation.

```
1 import pandas as pd
2
   from module.utility import create_dir
4 from cls.Info import *
5
6 # Given Information
7 \text{ pcut_ls} = [2, 3]
   info_ls = []
   info_ls.append({
       'indir': "../../Data/Encoded/info",
10
       'infile': "pppub20enc-info.csv",
11
12
       'outdir': "../../Samples/proc20/cuts"
13 })
   extra_infile_ls = [
14
15
       "selproc20num3info.csv",
16
       "selproc20num4info.csv",
       "selproc20num8info.csv"
17
18
   for file in extra_infile_ls:
20
       info_ls.append({
           'indir': "../../Samples/selproc20/info",
21
22
           'infile': file,
           'outdir': "../../Samples/selproc20/cuts"
23
24
       })
   print(f"\n{info_ls}\n")
25
26
27 # Implementation
   for dc in info_ls:
28
29
       for pcut in pcut_ls:
30
31
           # Import
32
           inpath = f"{dc['indir']}/{dc['infile']}"
           df = pd.read_csv(inpath)
33
34
           # Set cuts
35
36
           pcont, pcatmax = pcut, pcut
```

```
37
           df.info.setcut(pcont, pcatmax)
38
           # Set output path
39
           infilename = dc['infile'].replace('.csv', '').replace('info', '').
40
              replace('-', '')
41
           cutfilename = f"{infilename}co{pcont}ca{pcatmax}cutinfo"
42
           outpath = f"{dc['outdir']}/{cutfilename}.csv"
43
44
           # Display results
           print(f"Input: {inpath}")
45
           print(f"NUmber of features: {len(df)}")
46
47
           print(f"Number of continuous cuts: {pcont}")
           print(f"Number of maximum categorical cuts: {pcatmax}")
48
           print(f"Output: {outpath}\n")
49
           print(f"{df.head()}\n")
50
51
           # Export
52
           create_dir(dc['outdir'])
53
           df.to_csv(outpath, header=True, index=False)
54
```

CHAPTER IV

PROPOSED CLASSIFIER

4.1 Proposed Model for Selecting Continuous Factors

Suppose a training dataset of dimension \tilde{d} excluding its target variable has N instances, and every feature $1 \leq \tilde{j} \leq \tilde{d}$ is continuous. Each training instance $\tilde{x}^i = (\tilde{x}^i_{\tilde{j}})_{1 \leq \tilde{j} \leq \tilde{d}} \in \mathbb{R}^{\tilde{d}}$ where $1 \leq i \leq N$ has an integer class label between 0 and n. Let y^i_k specify whether a training instance \tilde{x}^i is in class k for $0 \leq k \leq n$. Assume that at most $1 \leq d \leq \tilde{d}$ contributing factors are considered. It follows that a reduced instance $x^i = (x^i_j)_{1 \leq j \leq d} \in \mathbb{R}^d$ is a partial selection of the components of the original instance \tilde{x}^i :

$$\begin{aligned} x_j^i &= \sum_{j=1}^d c_{j,\tilde{j}} \tilde{x}_{\tilde{j}}^i \\ \sum_{\tilde{j}=1}^{\tilde{d}} c_{j,\tilde{j}} &\leq 1 \\ \sum_{j=1}^d c_{j,\tilde{j}} &\leq 1 \\ c_{j,\tilde{j}} &\in \{0,1\}. \end{aligned}$$

An original feature \tilde{j} is selected and considered significant when

$$\sum_{j=1}^{d} c_{j,\tilde{j}} = 1$$

and it becomes a new feature j, uniquely, for $c_{j,\tilde{j}} = 1$.

Every selected, rearranged feature $1 \leq j \leq d$ is assumed to have $p_j \geq 0$ splitting values: $b_{j,1} \leq \ldots \leq b_{j,p_j}$. Two endpoints are assumed: $b_{j,0} = -M$ and $b_{j,p_j+1} = M$ for sufficiently large positive M such as $\max\{|x_j^i|\}$. All splitting points along each new axis forms $B = (p_1 + 1) \cdots (p_d + 1)$ decision boxes. A box S_β is defined in the following manner:

$$S_{\beta} = \prod_{j=1}^{d} \sum_{q=0}^{p_j} \beta_{j,q}[b_{j,q}, b_{j,q+1}]$$

where $b_{j,0}$ and b_{j,p_j+1} are sufficiently small negative and large positive,

$$\beta = \sum_{j=1}^{d} \left[\prod_{j_0=0}^{j-1} (p_{j_0} + 1) \right] \left[\sum_{q=0}^{p_j} q \beta_{j,q} \right]$$
$$\sum_{q=0}^{p_j} \beta_{j,q} = 1$$
$$\beta_{j,q} \in \{0,1\}$$

and $p_0 = 1$.

Each $x_j^i \in \mathbb{R}$ is in an open interval $(b_{j,q}, b_{j,q+1})$ for some $0 \le q \le p_j$, and its existence is indicated by a boolean variable $\alpha_{j,q}^i$:

$$\sum_{j=1}^{d} c_{j,\tilde{j}} \tilde{x}_{\tilde{j}}^{i} = x_{j}^{i} \in \sum_{q=0}^{p_{j}} \alpha_{j,q}^{i} [b_{j,q} + m_{j}, b_{j,q+1} - m_{j}] = \sum_{q=0}^{p_{j}} [l_{j,q}^{i}, r_{j,q}^{i}]$$

$$\sum_{q=0}^{p_{j}} \alpha_{j,q}^{i} = 1$$

$$\alpha_{j,q}^{i} \in \{0,1\}$$

for sufficiently small positive m_i such as

$$m_j = \frac{1}{2} \min\{|x_j^{i_1} - x_j^{i_2}| : x_j^{i_1} \neq x_j^{i_2}\}$$

and for some $l_{j,q}^i$ and $r_{j,q}^i$. Both terms are introduced to linearize the nonlinear products $\alpha_{j,q}^i(b_{j,q}+m_j)$ and $\alpha_{j,q}^i(b_{j,q+1}-m_j)$ respectively. Proven constructively, Theorem 4.1 ensures the linearizability.

Theorem 4.1. Two intervals $\alpha_{j,q}^{i}[b_{j,q}+m_{j},b_{j,q+1}-m_{j}]$ and $[l_{j,q}^{i},r_{j,q}^{i}]$ are identical only when

$$l_{j,q}^{i} \in [-M, b_{j,q} + m_{j}] + M(1 - \alpha_{j,q}^{i})$$

$$l_{j,q}^{i} \in [b_{j,q} + m_{j}, M] - M(1 - \alpha_{j,q}^{i})$$

$$r_{j,q}^{i} \in [-M, b_{j,q+1} - m_{j}] + M(1 - \alpha_{j,q}^{i})$$

$$r_{j,q}^{i} \in [b_{j,q+1} - m_{j}, M] - M(1 - \alpha_{j,q}^{i}).$$

Proof. It suffices to show that $l_{j,q}^i = \alpha_{j,q}^i(b_{j,q} + m_j)$ under the given constraints because substitution $b_{j,q}$ and m_j with $b_{j,q+1}$ and $-m_j$ results in the expression for $r_{j,q}^i$. The equivalent condition for the nonlinear product is given by for sufficiently large positive M_1 , M_2 , M_3 and M_4

$$l_{j,q}^{i} = \begin{cases} 0, & \text{for } \alpha_{j,q}^{i} = 0 \\ b_{j,q} + m_{j}, & \text{for } \alpha_{j,q}^{i} = 1 \end{cases}$$

$$\in \begin{cases} [-M_{1}, 0] \cap [0, M_{2}], & \text{for } \alpha_{j,q}^{i} = 0 \\ [b_{j,q} + m_{j}, M_{3}] \cap [-M_{4}, b_{j,q} + m_{j}], & \text{for } \alpha_{j,q}^{i} = 1. \end{cases}$$

Consider how each interval changes when $\alpha_{j,q}^i$ moves from 0 to 1:

$$[b_{j,q} + m_j, M_3] = [-M_1, 0] + [b_{j,q} + m_j + M_1, M_3]$$
$$[-M_4, b_{j,q} + m_j] = [0, M_2] + [-M_4, b_{j,q} + m_j - M_2].$$

Hence the translations are given by $(1 - \alpha_{j,q}^i)[b_{j,q} + m_j + M_1, M_3]$ and $(1 - \alpha_{j,q}^i)[-M_4, b_{j,q} + m_j - M_2]$. To remove all nonlinear terms, choose M_1 and M_2 such that $b_{j,q} + m_j + M_1$ and $b_{j,q} + m_j - M_2$ are constant. One example of such the ordered tuple (M_1, M_2, M_3, M_4) is $(M - b_{j,q} - m_j, M + b_{j,q} + m_j, M, M)$.

Governed by a boolean variable γ^i_{β} , an instance $x^i \in \mathbb{R}^d$ is also located in one of these boxes labeled by $0 \le \beta \le B - 1$:

$$\sum_{j=1}^{d} \left[\prod_{j_0=0}^{j-1} (p_{j_0} + 1) \right] \left[\sum_{q=0}^{p_j} q \alpha_{j,q}^i \right] = \sum_{\beta=0}^{B-1} \beta \gamma_{\beta}^i$$

$$\sum_{\beta=0}^{B-1} \gamma_{\beta}^i = 1$$

$$\gamma_{\beta}^i \in \{0, 1\}.$$

By majority voting, a decision box β therefore predicts exactly one class label from the following set

$$\Theta_{\beta} = \underset{0 \le k \le n}{\operatorname{argmax}} \left\{ \sum_{i=1}^{N} y_k^i \gamma_{\beta}^i \right\}.$$

In total, there are

$$N - \sum_{\beta=0}^{B-1} \max_{0 \le k \le n} \left\{ \sum_{i=1}^{N} y_k^i \gamma_\beta^i \right\} = N + h_\beta$$

misclassified instances where

$$h_{\beta} = \min_{0 \le k \le n} \left\{ -\sum_{i=1}^{N} y_k^i \gamma_{\beta}^i \right\}.$$

Theorem 4.2. The optimal value of the program

minimize
$$\sum_{\beta=0}^{B-1}h_{\beta}$$
 subject to
$$h_{\beta}+\sum_{i=1}^{N}y_{k}^{i}\gamma_{\beta}^{i}+Nz_{\beta,k}\geq0,$$

$$\sum_{k=0}^{n}z_{\beta,k}=n,$$

$$z_{\beta,k}\in\{0,1\}$$

is given by

$$\min_{0 \le k \le n} \left\{ -\sum_{i=1}^N y_k^i \gamma_\beta^i \right\}.$$

Proof. Let \mathcal{P} be the original problem. It can be partitioned into n+1 subproblems, each of which \mathcal{P}_{k_0} for $0 \le k_0 \le n$ has the following restriction:

$$z_{\beta,k} = \begin{cases} 0, & \text{for } k = k_0 \\ 1, & \text{for } k \neq k_0. \end{cases}$$

For each subproblem \mathcal{P}_{k_0} ,

$$h_{\beta} \geq -\sum_{i=1}^{N} y_{k_0}^{i} \gamma_{\beta}^{i} = 0 - \sum_{i=1}^{N} y_{k_0}^{i} \gamma_{\beta}^{i} \geq -\sum_{i=1}^{N} y_{k}^{i} \gamma_{\beta}^{i} - N z_{\beta,k}$$

and this implies

$$\min(\mathcal{P}_{k_0}) = -\sum_{i=1}^N y_{k_0}^i \gamma_{\beta}^i.$$

Hence

$$\min(\mathcal{P}) = \min_{0 \le k_0 \le n} (\min(\mathcal{P}_{k_0})) = \min_{0 \le k_0 \le n} \left\{ -\sum_{i=1}^N y_{k_0}^i \gamma_{\beta}^i \right\}.$$

By Theorems 4.1 and 4.2, the selection model for continuous dataset is given by

minimize
$$\sum_{\beta=0}^{B-1}h_{\beta}$$
 subject to
$$\sum_{\tilde{j}=1}^{\tilde{d}}c_{j,\tilde{j}}\leq 1,$$

$$\sum_{j=1}^{d}c_{j,\tilde{j}}\leq 1,$$

$$\begin{aligned} b_{j,q+1} - b_{j,q} &\geq 0, \\ \sum_{j=1}^{d} \tilde{x}_{j}^{i} c_{j,\tilde{j}} - \sum_{q=0}^{p_{j}} l_{j,q}^{i} &\geq 0, \\ \sum_{j=1}^{d} \tilde{x}_{j}^{i} c_{j,\tilde{j}} - \sum_{q=0}^{p_{j}} l_{j,q}^{i} &\geq 0, \\ \sum_{j=1}^{d} \tilde{x}_{j}^{i} c_{j,\tilde{j}} - \sum_{q=0}^{p_{j}} r_{j,q}^{i} &\leq 0, \\ l_{j,q}^{i} + M\alpha_{j,q}^{i} &\geq 0, \\ l_{j,q}^{i} - M\alpha_{j,q}^{i} &\leq 0, \\ l_{j,q}^{i} - b_{j,q} + M\alpha_{j,q}^{i} &\geq -M + m_{j}, \\ l_{j,q}^{i} - b_{j,q} - M\alpha_{j,q}^{i} &\geq 0, \\ r_{j,q}^{i} - M\alpha_{j,q}^{i} &\geq 0, \\ r_{j,q}^{i} - M\alpha_{j,q}^{i} &\leq 0, \\ r_{j,q}^{i} - b_{j,q+1} + M\alpha_{j,q}^{i} &\leq M - m_{j}, \\ r_{j,q}^{i} - b_{j,q+1} - M\alpha_{j,q}^{i} &\geq -M - m_{j}, \\ \sum_{j=1}^{d} \left[\prod_{j=0}^{j-1} (p_{j_{0}} + 1) \right] \left[\sum_{q=0}^{p_{j}} q\alpha_{j,q}^{i} \right] - \sum_{\beta=0}^{B-1} \beta\gamma_{\beta}^{i} &= 0, \\ \sum_{q=0}^{p_{j}} \alpha_{j,q}^{i} &= 1, \\ \sum_{\beta=0}^{B-1} \gamma_{\beta}^{i} &= 1, \\ \sum_{\beta=0}^{B-1} \gamma_{\beta}^{i} &= 1, \\ k_{\beta} + \sum_{i=1}^{N} y_{k}^{i} \gamma_{\beta}^{i} + Nz_{\beta,k} &\geq 0, \\ \sum_{k=0}^{n} z_{\beta,k} &= n, \\ l_{j,q}^{i}, r_{j,q}^{i}, b_{j,q}, h_{\beta} &\in \mathbb{R}, \\ c_{j,\tilde{j}}, \alpha_{j,q}^{i}, \gamma_{\beta}^{i}, z_{\beta,k} &\in \{0,1\} \end{aligned}$$

where the artificial splitting values $b_{j,0}$ and b_{j,p_j+1} are also treated as decision variables, and it produces a training accuracy of

$$1 + \frac{\sum_{\beta=0}^{B-1} h_{\beta}^*}{N} \le 1.$$

4.2 Selection of Mixed-Type Features

More generally, a training instance $\tilde{x}^i \in \mathbb{R}^{\tilde{d}}$ has a mixed-type component $\tilde{x}^i_{\tilde{j}} \in \mathbb{R}$ in feature \tilde{j} . The index sets of continuous and categorical features are denoted by $\tilde{\mathcal{C}}_{\text{cont}}$ and $\tilde{\mathcal{C}}_{\text{cat}}$ where

$$\tilde{\mathcal{C}}_{\text{cont}} \cup \tilde{\mathcal{C}}_{\text{cat}} = \{1, 2, \dots, \tilde{d}\}.$$

The continuous features are initially selected, whereas all categorical features are kept. The latter will be subsequently selected. The sets C_{cont} and C_{cat} represent new continuous and intermediate categorical components respectively where

$$\begin{aligned} |\mathcal{C}_{\mathrm{cont}}| &\leq |\tilde{\mathcal{C}}_{\mathrm{cont}}| \\ |\mathcal{C}_{\mathrm{cat}}| &= |\tilde{\mathcal{C}}_{\mathrm{cat}}| \\ \\ \mathcal{C}_{\mathrm{cont}} &\cup \mathcal{C}_{\mathrm{cat}} = \{1, 2, \dots, d\}. \end{aligned}$$

These conditions above can be satisfied specifically, as illustrated on the health insurance dataset in Chapter 5, when $\mathcal{C}_{cont} \subseteq \tilde{\mathcal{C}}_{cont}$ and $\mathcal{C}_{cat} = \tilde{\mathcal{C}}_{cat}$, for instance. In the case of continuous data type, the constraints of feature selection become

$$\begin{split} x_j^i &= \sum_{\tilde{j} \in \tilde{\mathcal{C}}_{\text{cont}}} c_{j,\tilde{j}} \tilde{x}_{\tilde{j}}^i, \qquad \qquad j \in \mathcal{C}_{\text{cont}} \\ \sum_{\tilde{j} \in \tilde{\mathcal{C}}_{\text{cont}}} c_{j,\tilde{j}} &\leq 1, \qquad \qquad j \in \mathcal{C}_{\text{cont}} \\ \sum_{j \in \mathcal{C}_{\text{cont}}} c_{j,\tilde{j}} &\leq 1, \qquad \qquad \tilde{j} \in \tilde{\mathcal{C}}_{\text{cont}} \\ c_{j,\tilde{j}} &\in \{0,1\}, \qquad \qquad (j,\tilde{j}) \in \mathcal{C}_{\text{cont}} \times \mathcal{C}_{\text{cont}}. \end{split}$$

Since at most $|C_{cont}|$ out of $|\tilde{C}_{cont}|$ continuous features are selected, the following condition holds:

$$\sum_{(j,\tilde{j}) \in \mathcal{C}_{\text{cont}} \times \tilde{\mathcal{C}}_{\text{cont}}} c_{j,\tilde{j}} \leq |\mathcal{C}_{\text{cont}}|.$$

A selected, rearranged component $x_j^i \in \mathbb{R}$ for a feature $1 \leq j \leq d$ is now either continuous or categorical. A continuous feature $j \in \mathcal{C}_{\text{cont}}$ is similarly assumed to have p_j splitting points, namely $b_{j,q} \in \mathbb{R}$ where $1 \leq q \leq p_j$. Usually, p_j is assumed to be constant across all new continuous features because the new explicit order of this selection is unknown before optimization. A categorical feature $j \in \mathcal{C}_{\text{cat}}$ comprises finite discrete values which are also assumed to form $p_j + 1$ new small groups labeled with $0 \leq u_j \leq p_j$.

A box $0 \le \beta \le B-1$ along a categorical feature, as opposed to a continuous feature, lacks continuity because its entry is simply a singleton. Algebraically, it is represented by a set

$$S_{\beta} = \prod_{j \in \mathcal{C}_{\text{cont}}} \sum_{q=0}^{p_j} \beta_{j,q}[b_{j,q}, b_{j,q+1}] \times \prod_{j \in \mathcal{C}_{\text{cat}}} \{u_j\}$$

where

$$\beta = \sum_{j \in \mathcal{C}_{\text{cont}}} \left[\prod_{0 \le j_0 < j} (p_{j_0} + 1) \right] \left[\sum_{q=0}^{p_j} q \beta_{j,q} \right]$$

$$+ \sum_{j \in \mathcal{C}_{\text{cat}}} \left[\prod_{0 \le j_0 < j} (p_{j_0} + 1) \right] u_j$$

$$\sum_{q=0}^{p_j} \beta_{j,q} = 1, \qquad j \in \mathcal{C}_{\text{cont}}$$

$$\beta_{j,q} \in \{0, 1\}, \qquad j \in \mathcal{C}_{\text{cont}}$$

$$u_j \in \{0, 1, \dots, p_j\}, \qquad j \in \mathcal{C}_{\text{cat}}$$

and $p_0 = 0$. The existence of $b_{j,0}$ and b_{j,p_j+1} where $j \in \mathcal{C}_{\text{cat}}$ is shown in the previous section. Numerically, each box can also be identified by the unique combination of binary $(\beta_{j,q})_{j \in \mathcal{C}_{\text{cont}}}$ and integer $(u_j)_{j \in \mathcal{C}_{\text{cat}}}$.

For a categorical feature $j \in \mathcal{C}_{\text{cat}}$, an original categorical label $x_j^i \in \mathbb{R}$ is reassigned to a new integer group label $0 \le v_{j,x_i^i} \le p_j$. As a result, the following conditions must hold:

$$\sum_{\beta=0}^{B-1} \beta \gamma_{\beta}^{i} = \sum_{j \in \mathcal{C}_{cont}} \left[\prod_{0 \leq j_{0} < j} (p_{j_{0}} + 1) \right] \left[\sum_{q=0}^{p_{j}} q \alpha_{j,q}^{i} \right]$$

$$+ \sum_{j \in \mathcal{C}_{cat}} \left[\prod_{0 \leq j_{0} < j} (p_{j_{0}} + 1) \right] v_{j,x_{j}^{i}}$$

$$\sum_{q=0}^{p_{j}} \alpha_{j,q}^{i} = 1, \qquad j \in \mathcal{C}_{cont}$$

$$\sum_{\beta=0}^{B-1} \gamma_{\beta}^{i} = 1, \qquad j \in \mathcal{C}_{cont}$$

$$\beta_{j,q} \in \{0,1\}, \qquad j \in \mathcal{C}_{cont}$$

$$v_{j,x_{j}^{i}} \in \{0,1,\ldots,p_{j}\}, \qquad j \in \mathcal{C}_{cat}.$$

A boolean variable $f_j \in \{0,1\}$ is defined to determine whether a categorical feature j is significant. All categorical labels of an insignificant feature are grouped together. Its necessary, though insufficient, condition can be obtained:

$$-Mf_j \le v_{j,x_j^i} \le Mf_j.$$

If at most d_{cat} out of $|\mathcal{C}_{\text{cat}}|$ categorical features are of interest, the following condition holds:

$$\sum_{j \in \mathcal{C}_{\text{cat}}} f_j \le d_{\text{cat}}.$$

There are at most $|\mathcal{C}_{\text{cont}}| + d_{\text{cat}} \leq d \leq \tilde{d}$ contributing factors, $|\mathcal{C}_{\text{cont}}| \leq |\tilde{\mathcal{C}}_{\text{cont}}|$ of which are continuous and $d_{\text{cat}} \leq |\mathcal{C}_{\text{cat}}| = |\tilde{\mathcal{C}}_{\text{cat}}|$ categorical:

$$\sum_{(j,\tilde{j}) \in \mathcal{C}_{\text{cont}} \times \tilde{\mathcal{C}}_{\text{cont}}} c_{j,\tilde{j}} + \sum_{j \in \mathcal{C}_{\text{cat}}} f_j \leq d.$$

An original feature $1 \leq \tilde{j} \leq \tilde{d}$ is deemed significant when

$$\sum_{j \in \mathcal{C}_{\text{cont}}} c_{j,\tilde{j}} = 1$$

for a continuous feature $\tilde{j} \in \tilde{\mathcal{C}}_{\operatorname{cont}}$, and a new group label v_{j,x_j^i} is nonconstant across all training instances x^i for a categorical feature $\tilde{j} \in \tilde{\mathcal{C}}_{\operatorname{cat}}$ corresponding to $j \in \mathcal{C}_{\operatorname{cat}}$. The condition $f_j = 0$ can also be used as an initial step to screen out an insignificant categorical feature $j \in \mathcal{C}_{\operatorname{cat}}$.

The final selection model is proposed:

$$\begin{split} & \text{minimize} & \sum_{\beta=0}^{B-1} h_{\beta} \\ & \text{subject to} & \sum_{\tilde{j} \in \tilde{\mathcal{C}}_{\text{cont}}} c_{j,\tilde{j}} \leq 1, \qquad j \in \mathcal{C}_{\text{cont}}, \\ & \sum_{j \in \mathcal{C}_{\text{cont}}} c_{j,\tilde{j}} \leq 1, \qquad j \in \tilde{\mathcal{C}}_{\text{cont}}, \\ & \sum_{j \in \tilde{\mathcal{C}}_{\text{cont}}} \tilde{x}^{i}_{\tilde{j}} c_{j,\tilde{j}} - \sum_{q=0}^{p_{j}} l^{i}_{j,q} \geq 0, \qquad j \in \mathcal{C}_{\text{cont}}, \\ & \sum_{\tilde{j} \in \tilde{\mathcal{C}}_{\text{cont}}} \tilde{x}^{i}_{\tilde{j}} c_{j,\tilde{j}} - \sum_{q=0}^{p_{j}} l^{i}_{j,q} \geq 0, \qquad j \in \mathcal{C}_{\text{cont}}, \\ & \sum_{\tilde{j} \in \tilde{\mathcal{C}}_{\text{cont}}} \tilde{x}^{i}_{\tilde{j}} c_{j,\tilde{j}} - \sum_{q=0}^{p_{j}} r^{i}_{j,q} \leq 0, \qquad j \in \mathcal{C}_{\text{cont}}, \\ & l^{i}_{j,q} + M\alpha^{i}_{j,q} \geq 0, \qquad j \in \mathcal{C}_{\text{cont}}, \\ & l^{i}_{j,q} - M\alpha^{i}_{j,q} \leq 0, \qquad j \in \mathcal{C}_{\text{cont}}, \\ & l^{i}_{j,q} - b_{j,q} + M\alpha^{i}_{j,q} \leq M + m_{j}, \qquad j \in \mathcal{C}_{\text{cont}}, \end{split}$$

 $l_{j,q}^i - b_{j,q} - M\alpha_{j,q}^i \ge -M + m_j, \qquad j \in \mathcal{C}_{\text{cont}},$

 $r_{i,a}^i + M\alpha_{i,a}^i \ge 0,$

 $r_{i,q}^i - M\alpha_{i,q}^i \le 0,$

 $j \in \mathcal{C}_{\mathrm{cont}}$,

 $j \in \mathcal{C}_{cont}$

$$\begin{split} r^i_{j,q} - b_{j,q+1} + M\alpha^i_{j,q} &\leq M - m_j, & j \in \mathcal{C}_{\text{cont}}, \\ r^i_{j,q} - b_{j,q+1} - M\alpha^i_{j,q} &\geq -M - m_j, & j \in \mathcal{C}_{\text{cont}}, \\ \sum_{j \in \mathcal{C}_{\text{cont}}} \left[\prod_{0 \leq j_0 < j} (p_{j_0} + 1) \right] \left[\sum_{q=0}^{p_j} q\alpha^i_{j,q} \right] \\ &+ \sum_{j \in \mathcal{C}_{\text{car}}} \left[\prod_{0 \leq j_0 < j} (p_{j_0} + 1) \right] v_{j,x^i_j} \\ &- \sum_{\beta=0}^{B-1} \beta \gamma^i_{\beta} &= 0, \\ \sum_{q=0}^{p_j} \alpha^i_{j,q} &= 1, & j \in \mathcal{C}_{\text{cont}}, \\ v_{j,x^i_j} + Mf_j &\geq 0, & j \in \mathcal{C}_{\text{cat}}, \\ v_{j,x^i_j} - Mf_j &\leq 0, & j \in \mathcal{C}_{\text{cat}}, \\ \sum_{(j,\bar{j}) \in \mathcal{C}_{\text{cont}} \times \bar{\mathcal{C}}_{\text{cont}}} c_{j,\bar{j}} &+ \sum_{j \in \mathcal{C}_{\text{cat}}} f_j &\leq d, \\ \sum_{j=0}^{D-1} \gamma^i_{\beta} &= 1, & j \in \mathcal{C}_{\text{cat}}, \\ \sum_{k=0}^{D-1} \gamma^i_{\beta} &= 1, & j \in \mathcal{C}_{\text{cont}}, \\ h_{\beta} &+ \sum_{i=1}^{N} y^i_k \gamma^i_{\beta} + Nz_{\beta,k} &\geq 0, \\ \sum_{k=0}^{n} z_{\beta,k} &= n, \\ l^i_{j,q}, r^i_{j,q}, b_{j,q} &\in \mathbb{R}, & j \in \mathcal{C}_{\text{cont}}, \\ h_{\beta} &\in \mathbb{R}, & c_{j,\bar{j}} &\in \{0,1\}, & (j,\bar{j}) \in \mathcal{C}_{\text{cont}} \times \tilde{\mathcal{C}}_{\text{cont}}, \\ \alpha^i_{j,q} &\in \{0,1\}, & j \in \mathcal{C}_{\text{cat}}, \\ v_{j,x^i_j} &\in \{0,1\}, & j \in \mathcal{C}_{\text{cat}}, \\ \alpha^i_{j,q}, \gamma^i_{\beta}, z_{\beta,k} &\in \{0,1\}. & j \in \mathcal{C}_{\text{cat}}, \\ \alpha^i_{j,q}, \gamma^i_{\beta}, z_{\beta,k} &\in \{0,1\}. & j \in \mathcal{C}_{\text{cat}}, \\ \alpha^i_{j,q}, \gamma^i_{\beta}, z_{\beta,k} &\in \{0,1\}. & j \in \mathcal{C}_{\text{cat}}, \\ \end{cases}$$

4.3 CPLEX OPL Modeling

The proposed classifier heavily relies on 0-1 mixed integer programming (MIP). The CPLEX optimizer (version 22.1.1) is used to solve for the classifier including its splitting values and the set of predicted class labels in each decision box. Although achieving higher performance, manual adjustment of internal optimization procedures such as a node selection during branching and a combination of multiple techniques in cut generation is beyond the scope of this dissertation. The MIP problem is very large, and its information is stored in a huge tree data structure. Multiple lock-free nodes can be executed simultaneously in parallel by utilizing all available CPU cores. CPLEX uses in-memory computation.

When a central memory is consumed more than its upper limit which is 2048 MB by default, some nodes are transferred from the in-memory set to node files which are in memory and compressed by default. Optionally, they can be flushed to disk, in either uncompressed or compressed form, where speed is sacrificed for more storage space. As more solutions are explored, the branch-and-cut tree grows larger. When its size exceeds its upper limit, which is set at 10^{75} MB by default, the optimization process terminates. The solver also stops when a memory is exhausted or a disk is fully occupied depending on whether node files are stored in memory or on disk. CPLEX parameters related to this dissertation is included in Table 4.1.

Table 4.1: Relevant CPLEX parameters

Parameter	Description
cplex.intsollim	MIP solution number limit
cplex.tilim	Time limit per optimizer call (in seconds)
cplex.threads	Parallel threads (default: 0 implying up to 32 threads)
cplex.workmem	Working memory before compression and swap (in MB) (default:
	2048)
cplex.trelim	Uncompressed tree limit (in MB) (default: 10^{75})
cplex.nodefileind	Node storage file switch
	0: No node file
	1: Node file in memory and compressed (default)
	2: Node file on disk
	3: Node file on disk and compressed
cplex.status	Solution status code
	1: Optimal for simplex and barrier methods

Table 4.1: Relevant CPLEX parameters (continued)

Parameter	Description
	11: Time limit exceeded
	101: Optimal for MIP model
	102: Optimal within predefined MIP gap tolerance
	104: Limit on mixed integer solutions
	111: Tree memory limit exceeded and integer solution found
	112: Tree memory limit exceeded and no integer solution

Two following classification files are written in Optimization Programming Language (OPL), supported by default. Code 4.1 is the main execution of the classification model in Code 4.2. Two data structures are employed: an array and a tuple. Once the first is declared, its size is unchanged. The latter is used as a secondary option only when a combination of indexes cannot perfectly fit in an array format. As illustrated in Chapter 5, only three features are considered: A AGE, PEMLR and SS YN. Three splits are assumed except two for SS YN representing both whether social security payments are paid and whether a survey participant is in the universe of this question. Two most significant factors are of interest. The cardinality of a new continuous component $|\mathcal{C}_{cont}|$ is assumed to be the minimum of its given counterpart $|\tilde{\mathcal{C}}_{\text{cont}}| = 1$ and an upper bound on the number of significant features d=2. The continuous feature selection can be partially concluded by the condition $c_{i\tilde{i}}^* = 1$. The sufficiently small positive number m_0 is set to be 0.01. The execution time is limited up to 24 hours or one day. Code 4.1 records every MIP solution, feasible but not necessarily optimal, thereby calling a CPLEX solver multiple times. After the working memory exceeds 2 GB, some nodes are transferred to disk in compressed form. The uncompressed tree size is limited to 200 GB.

Code 4.1: Main OPL model

6

```
7 /*******************
   * NOTES
   * pl.bc.solutionValue[thisOplModel.mPairs.find(1,0)]
   10
11
12
  /***************
   * Class Labels
13
14
   * Input file: 0, 1, 2, ..., n
   * Algorithm: 0, 1, 2, ..., n
15
   * Output file: 0, 1, 2, ..., n
16
   17
18
  /****************************
19
   * INPUTS
20
   21
22 int mdimold = 3; // dimension // 4 or 184 or 8 or 4
23 int mdimcontold = 1; // continuous dimension // 2 or 66 or 3 or 2
24 //int mdimcat = 2; // categorical dimension // 2 or 118 or 5 or 2
25 int mN = 100; // number of instances // 8 or 157681 or 100 or 100
  int mn = 4; // the value of n = (number of classes) - 1 // 1 or 4 or 4
27
  int mseltol = 2; // given number of total selected cont/cat dimensions (at
      most)
29
30 // Initialized UB on number of selected continuous dimensions
31 int mselcont = mdimcontold;
32 execute {
     if (mselcont > mseltol)
33
34
        mselcont = mseltol;
35 }
36
37 int mexccont = mdimcontold - mselcont; // computed LB on number of
      excluded continuous dimensions
38 int mdim = mdimold - mexccont;
39 int mdimcont = mselcont;
40
```

```
41 range mDS = 1..mdim;
42 range mDSCONTOLD = 1..mdimcontold; // old continuous
43 range mDSCONT = 1..mselcont; // new continuous
44 range mDSCAT = mdimcont+1..mdim; // shifted categorical
45 \text{ range mIS} = 1..mN;
46 float mxcontold[mIS][mDSCONTOLD]; // x along continuous dimensions
  int mxcat[mIS][mDSCAT]; // x along categorical dimensions
47
48 int my[mIS];
  int mmaxlab[mDSCAT]; // maximum labels for categorical dimensions
49
50 float mM[mDS]; // big-M for all new/shifted dimensions (continuous and
      categorical)
51 float mm[mDSCONT]; // small-m for continuous dimensions
   int mp[mDS]; // number of cuts along axes
   int mcoef[mDS];
53
54
55 /*******************
56
    * TUPLES
    tuple ContPairType { // index for continuous cut
59
      int j;
60
      int q;
61 };
62
   {ContPairType} mContPairs = {<j, q> | j in mDSCONT, q in 0..mp[j]+1};
63
64
   tuple ContTripleType { // index for continuous cut of each individual
65
      instance
66
      int i;
67
      int j;
68
      int q;
69 };
70
   {ContTripleType} mContTriples = {<i, j, q> | i in mIS, j in mDSCONT, q in
      0..mp[j]};
72
73 tuple CatPairType { // index for categorical group
```

```
74
       int j;
75
       int 1;
76 };
77
78
    {CatPairType} mCatPairs = {<j, 1> | j in mDSCAT, 1 in 0..mmaxlab[j]};
79
80
   tuple tuplePred {
       key int b;
81
       sorted {int} label;
82
83 }
84 sorted {tuplePred} mpred;
   {int} memptyset = {};
86
87 /********************
    * OUTSIDE EXECUTION
88
    89
90 execute {
       thisOplModel.settings.run_engineLog = "tmp/current-engine.log"; //
91
          temporary engine log
92 }
93
94 /*************
95
    * MAIN EXECUTION
96
    ************************************
97 main {
       var ftime = Opl.round((new Date()).getTime()/1000) % 100000; // first
98
          timestamp (in seconds)
99
100
       // Input/variable filenames
       var infilename = "input/seltrain20num3each20.csv"; // input filename
101
       var varfilename = "input/selproc20num3co3ca3cutinfo.csv"; // variable
102
          filename (6 columns)
103
104
       // Prefix of all output files
       var prefixout = "output/" + ftime + "-";
105
106
       prefixout += infilename.split("/")[1].split(".")[0] + "-";
```

```
107
108
        // Inputs
        //var MO = 500; // big-M (float)
109
        var m0 = 0.01; // small-m (float)
110
111
        var pcont0 = 3;  // max number of cuts along continuous axis (integer)
112
113
        // Customization
114
        var timelimit = 1; // whether set total time limits (1 = limit / 0 =
115
        var limit = 1; // whether customize performance settings (1 =
           customize / 0 = none)
116
        var perf = 1; // whether set limits (1 = limit / 0 = none)
117
        // Custom time limit parameter
118
        if (timelimit == 1)
119
           var acctimelimmin = 24*60; // accumulated time limit (in minutes)
120
121
122
        // Cplex limit parameters (excluding time limit)
        if (limit == 1) {
123
124
           var intsollim = 1; // MIP solution number limit (in each iteration)
125
        }
126
127
        // Cplex performance parameters
128
        if (perf == 1) {
129
           var threads = 0; // parallel threads (default: 0 = at most 32
               threads)
130
           var workmemgb = 2; // working memory before compression and swap (
               in GB) (default: 2 GB) (only marginally improved efficiency)
           var trelimgb = 200; // uncompressed tree memory limit (in GB) (
131
               default: around 1e+72 GB)
132
133
           /* Node storage file switch
134
            * 0 = No node file
135
            * 1 = Node file in memory and compressed (default)
136
            * 2 = Node file on disk
            * 3 = Node file on disk and compressed
137
```

```
*/
138
139
           var nodefileind = 3;
140
           /* Note on directory for temporary working files
141
142
            * cplex.workdir = ...;
            * CPLEX Error 1422: Could not open file for writing
143
144
            */
145
           // Calculation
146
           var workmem = 1024*workmemgb; // working memory before compression
147
               and swap (in MB) (default: 2048 MB)
148
           var trelim = 1024*trelimgb; // uncompressed tree memory limit (in
               MB) (default: 1e+75 MB)
        }
149
150
151
        // Postfixes
152
        var cpostfixname = "mfullaltseltol-" + thisOplModel.mseltol; // common
           postfix name
        if (timelimit == 1)
153
154
            cpostfixname += "-t-" + acctimelimmin + ".csv";
155
        else
156
            cpostfixname += ".csv";
157
        var postfixerror = "-" + cpostfixname; // postfix of error file
158
        var postfixout = "-pcont-" + pcont0 + "-" + cpostfixname; // postfix of
            all other output files
159
160
        // Output filenames
        var outerrorname = prefixout + "export-error" + postfixerror;
161
162
        var outinstancename = prefixout + "export-predict-instance" +
           postfixout;
        var outcutcontname = prefixout + "export-cutcont-full" + postfixout;
163
164
        var outcutcatname = prefixout + "export-cutcat-full" + postfixout;
165
        // The existence of region is not checked here
166
        // In fact, it can be check through enumeration of certain binary
           representations
167
        var outregionname = prefixout + "export-predict-region" + postfixout;
```

```
168
        var outselvarintname = prefixout + "export-select-var-int" + postfixout
            ; // selected variables (integer)
169
        var outselvarstrname = prefixout + "export-select-var-str" + postfixout
            ; // selected variables (string)
170
        // Engine log (initialized)
171
        var logfilename = "log/" + ftime + "-engine-" + cpostfixname.split(".")
172
            [0] + ".log";
173
        var outlog = new IloOplOutputFile(logfilename);
174
        // OPL
175
176
        var source = new IloOplModelSource("p-mixed-cuts-alt-seltol.mod");
177
        var cplex = new IloCplex();
        var def = new IloOplModelDefinition(source);
178
        var opl = new IloOplModel(def,cplex);
179
180
        var data = new IloOplDataElements();
181
182
        data.dimold = thisOplModel.mdimold;
183
        data.dimcontold = thisOplModel.mdimcontold;
184
        data.dim = thisOplModel.mdim;
185
        data.dimcont = thisOplModel.mdimcont;
186
        //data.dimcat = thisOplModel.mdimcat;
187
        data.N = thisOplModel.mN;
188
        data.n = thisOplModel.mn;
189
        data.xcontold = thisOplModel.mxcontold;
190
        data.xcat = thisOplModel.mxcat;
191
        data.y = thisOplModel.my;
192
193
        var pred = thisOplModel.mpred; // set of predicted labels
194
195
        data.seltol = thisOplModel.mseltol;
196
        data.selcont = thisOplModel.mselcont;
197
        data.exccont = thisOplModel.mexccont;
198
199
        data.m = thisOplModel.mm;
200
        for (var j=1; j<=data.dimcont; j++)</pre>
```

```
201
            data.m[j] = m0;
202
203
        var f = new IloOplInputFile(infilename); // training dataset
204
        f.readline();
                               // skip a header
205
        for (var i=1; i<=data.N; i++) {</pre>
            var myitem = f.readline().split(",");
206
207
            data.y[i] = Opl.intValue(myitem[data.dimold]);
208
            for (var j=1; j<=data.dimcontold; j++)</pre>
                data.xcontold[i][j] = Opl.floatValue(myitem[j-1]);
209
            for (var j=data.dimcontold+1; j<=data.dimold; j++)</pre>
210
                data.xcat[i][j-data.exccont] = Opl.intValue(myitem[j-1]);
211
212
        }
213
        f.close();
214
215
        data.p = thisOplModel.mp;
216
        for (var j=1; j<=data.dimcont; j++)</pre>
217
            data.p[j] = pcont0;
218
219
        data.M = thisOplModel.mM;
220
        data.maxlab = thisOplModel.mmaxlab;
221
        var MOcont = 1;
222
        var f = new IloOplInputFile(varfilename); // variable info
223
        f.readline();
                               // skip a header
224
        for (var j=1; j<=data.dimold; j++) {</pre>
225
            var myitem = f.readline().split(",");
226
            if (j <= data.dimcontold) {</pre>
227
                var curMcont = 1 + Opl.maxl(Opl.abs(Opl.intValue(myitem[3])),
                    Opl.abs(Opl.intValue(myitem[4])));
228
                MOcont = Opl.maxl(MOcont, curMcont);
            }
229
            else {
230
231
                data.p[j-data.exccont] = Opl.intValue(myitem[5]);
232
                data.maxlab[j-data.exccont] = Opl.intValue(myitem[4]);
233
                data.M[j-data.exccont] = 1 + Opl.intValue(myitem[5]);
234
            }
235
        }
```

```
236
        f.close();
237
238
        for (var j=1; j<=data.dimcont; j++)</pre>
            data.M[j] = MOcont;
239
240
        data.coef = thisOplModel.mcoef;
241
242
        data.coef[1] = 1;
        for (var j=2; j<=data.dim; j++)</pre>
243
244
            data.coef[j] = data.coef[j-1]*(data.p[j]+1);
245
        var nump = 0; // total number of cuts
246
247
        for (var j=1; j<=data.dim; j++)</pre>
248
            nump += data.p[j];
249
        opl.addDataSource(data);
250
251
        opl.generate();
252
        opl.settings.mainEndEnabled = true;
253
        // Cplex limits (excluding time limit)
254
255
        if (limit == 1) {
            cplex.intsollim = intsollim; // MIP solution number limit (> 0)
256
257
        }
258
259
        // Cplex performance
260
        if (perf == 1) {
261
            cplex.threads = threads; // parallel threads
262
            cplex.workmem = workmem; // working memory before compression and
                swap (in MB)
263
            cplex.trelim = trelim; // uncompressed tree memory limit (in MB)
            cplex.nodefileind = nodefileind; // node storage file switch
264
        }
265
266
267
        // Initialization
268
        var status = -9; // solution status code (initialized)
269
        var iter = 0; // iteration
        var acctime = 0; // accumulated running time (in seconds)
270
```

```
271
        var texceed = 0; // whether acctime > tilimmin (1 = total time limit
            exceeded / 0 = not)
272
        // Calculation
273
274
        if (timelimit == 1)
            var acctimelim = 60*acctimelimmin; // accumulated time limit (in
275
               seconds)
276
        else
277
            var acctimelim = -1;
278
279
        // Optimization
280
        while (texceed == 0) { // accumulated time limit not exceeded
281
            // Exit status codes
282
            if (status == 1) // 1: CPX_STAT_OPTIMAL
283
284
               break;
285
            else if (status == 101) // 101: CPXMIP_OPTIMAL
286
            else if (status == 102) // 102: CPXMIP_OPTIMAL_TOL
287
288
               break;
            else if (status == 111) // 111: CPXMIP_MEM_LIM_FEAS
289
290
               break;
291
            else if (status == 112) // 112: CPXMIP_MEM_LIM_INFEAS
292
               break;
293
294
            /* Non-exit status codes
295
            * 11: CPX_STAT_ABORT_TIME_LIM
            * 104: CPXMIP_SOL_LIM
296
297
             */
298
299
            // In the case when the previous status is not one of the above
300
            if (timelimit == 1) // time limit for each call to optimizer (in
               seconds)
301
               cplex.tilim = acctimelim - acctime;
302
            var start = new Date(); // begin a timer
303
```

```
304
           pred.clear(); // clear previous set of predicted labels
305
306
           // Solve
            if (cplex.solve()) {
307
308
               var end = new Date(); // end a timer
309
310
               var solvetime = end.getTime() - start.getTime(); // compute
                   solving time
               acctime += solvetime/1000; // accumulated running time (in s)
311
312
               if ((timelimit == 1) && (acctime >= acctimelim)) // total time
313
                   limit exceeded (in seconds)
314
                   texceed = 1;
315
               iter += 1; // update iteration
316
317
318
               var error = data.N + cplex.getObjValue(); // the number of
                   misclassified instances
               var accuracy = (1-error/data.N)*100; // training accuracy
319
320
               status = cplex.status; // solution status code (1 = opt / 11 =
321
                   time limit / ...)
322
               var lberr = data.N + cplex.getBestObjValue(); // LB on minimum
                   (optimal) error
323
               var relgap = cplex.getMIPRelativeGap(); // relative objective
                   gap for MIP
324
               // Open output text files (append = true)
325
               var outerror = new IloOplOutputFile(outerrorname, true);
326
               var outinstance = new IloOplOutputFile(outinstancename, true);
327
328
               var outcutcont = new IloOplOutputFile(outcutcontname, true);
329
               var outcutcat = new IloOplOutputFile(outcutcatname, true);
330
               var outregion = new IloOplOutputFile(outregionname, true);
331
               var outselvarint = new IloOplOutputFile(outselvarintname, true);
```

```
332
               var outselvarstr = new IloOplOutputFile(outselvarstrname, true);
333
               // outerror
334
335
               if (!outerror.exists) {
                   outerror.write("iter,");
336
337
                   for (var j=1; j<=data.dim; j++)</pre>
338
                       outerror.write("p", j, ",");
339
                   outerror.write("error,accuracy,ms,acctmin,status,lberr,
                       relgap");
               }
340
341
               outerror.write("\n", iter, ",");
               for (var j=1; j<=data.dim; j++)</pre>
342
                   outerror.write(data.p[j], ",");
343
               outerror.write(error, ",", accuracy, ",");
344
345
               outerror.write(solvetime, ",", acctime/60, ",");
346
               outerror.write(status, ",", lberr, ",", relgap);
347
348
               // Scripting logs 1
349
               writeln("\n----");
350
               writeln("Iteration ", iter);
               writeln("Bounds on # of cuts = ", nump, " with", data.p);
351
352
               writeln("Error = ", error, " (out of ", data.N, " instances)");
               writeln("Accuracy = ", accuracy);
353
               writeln("Solving time = ", solvetime/60000, " min (minutes)");
354
               writeln("Accumulated time = ", acctime/60, " min (minutes)");
355
               writeln("\nSolution status code = ", status);
356
               writeln("LB on error = ", lberr);
357
               writeln("Relative objective gap = ", relgap);
358
               writeln("\nSelected variables:");
359
360
361
               // Create a set of predicted labels (majority voting)
               for (var b=0; b<opl.B; b++) {</pre>
362
                   var lset = Opl.operatorUNION(thisOplModel.memptyset,
363
                       thisOplModel.memptyset);
                   var maxnum = 0;
364
```

```
365
                    for (var k=0; k<=data.n; k++) {</pre>
366
                        var num = 0;
367
                        for (var i=1; i<=data.N; i++)</pre>
                            num += (data.y[i] == k)*opl.g.solutionValue[i][b];
368
369
                        if (num == maxnum)
370
                            lset.add(k);
371
                        else if (num > maxnum) {
372
                            maxnum = num;
373
                            lset.clear();
                            lset.add(k);
374
375
                        }
                    }
376
                    pred.add(b, lset);
377
                }
378
379
380
                // outinstance
381
                if (!outinstance.exists)
                    outinstance.write("iter,id,class,region,predict");
382
383
                for (var i=1; i<=data.N; i++) {</pre>
                    outinstance.write("\n", iter, ",", i, ",", data.y[i], ",");
384
385
                    for (var b=0; b<opl.B; b++)</pre>
386
                        if (opl.g.solutionValue[i][b] == 1) { // occur only once
387
                            outinstance.write(b, ",");
388
                            outinstance.write(pred.get(b).label);
389
                            break; // terminate the loop
390
                        }
                }
391
392
                // outcutcont
393
                if (!outcutcont.exists)
394
395
                    outcutcont.write("iter,j,q,bc");
                for (var j=1; j<=data.dimcont; j++) {</pre>
396
397
                    for (var q=1; q<=data.p[j]; q++) {</pre>
                        outcutcont.write("\n", iter, ",", j, ",", q, ",");
398
```

```
399
                        outcutcont.write(opl.bc.solutionValue[thisOplModel.
                           mContPairs.find(j,q)]);
400
                    }
                }
401
402
                // outcutcat
403
                if (!outcutcat.exists)
404
                    outcutcat.write("iter,j,1,v");
405
                for (var j=data.dimcont+1; j<=data.dim; j++) {</pre>
406
                    for (var 1=0; 1<=data.maxlab[j]; 1++) {</pre>
407
                        outcutcat.write("\n", iter, ",", j, ",", l, ",");
408
409
                        outcutcat.write(opl.v.solutionValue[thisOplModel.
                           mCatPairs.find(j,1)]);
                    }
410
                }
411
412
413
                // outregion
414
                if (!outregion.exists)
                    outregion.write("iter,region,occupy,predict");
415
416
                for (var b=0; b<opl.B; b++) {</pre>
                    outregion.write("\n", iter, ",", b, ",");
417
418
                    var s = 0; // initialize s (presumably unoccupied)
419
                    for (var i=1; i<=data.N; i++)</pre>
420
                        if (opl.g.solutionValue[i][b] == 1) { // occupied
421
                            s = 1;
422
                           break; // iterminate the loop
423
                        }
                    outregion.write(s, ",");
424
                    outregion.write(pred.get(b).label);
425
                }
426
427
428
                // outselvarint
429
                if (!outselvarint.exists)
430
                    outselvarint.write("iter,j,jold,mselect,type"); // mselect =
                         model select (not actual)
```

```
431
                for (var j=1; j<=data.dimcont; j++) { // selected continuous</pre>
                   features
                   outselvarint.write("\n", iter, ",", j, ",");
432
                   var seljold = -1;
433
434
                   for (var jold=1; jold<=data.dimcontold; jold++)</pre>
                       // Determine which old continuous feature is selected
435
436
                       if (opl.ccont.solutionValue[j][jold] == 1) {
437
                           seljold = jold;
                           break; // terminate the loop
438
                       }
439
                   outselvarint.write(seljold, ",");
440
441
                   outselvarint.write("1,"); // Based on model, all new cont
                       features are selected
                   outselvarint.write("cont");
442
                }
443
444
                for (var j=data.dimcont+1; j<=data.dim; j++) { // categorical</pre>
                   outselvarint.write("\n", iter, ",", j, ",", j+data.exccont,
445
                       ",");
446
                   if (opl.f.solutionValue[j] == 1) // selected categorical
                       feature (model)
447
                       outselvarint.write("1,");
448
                   else // unselected categorical feature (model)
449
                       outselvarint.write("0,");
                   outselvarint.write("cat");
450
                }
451
452
                // outselvarstr
453
                if (!outselvarstr.exists)
454
                   outselvarstr.write("iter,jold,jnew,aselect,type,variable");
455
                       // aselect = actual select
456
                var varinfile = new IloOplInputFile(varfilename); // variable
                   info
                varinfile.readline(); // skip a header
457
458
                var numselcont = 0; // initialized number of actually selected
                   continuous features
```

```
459
                var numselcat = 0; // initialized number of actually selected
                   categorical features
                for (var jold=1; jold<=data.dimcontold; jold++) { // CONTINUOUS</pre>
460
                   outselvarstr.write("\n", iter, ",", jold, ",");
461
462
                   var jnew = -1;
                   var aselect = 0; // initialized to be unselected (continuous
463
                       )
                   for (var j=1; j<=data.dimcont; j++)</pre>
464
                       // Determine whether a current old continuous feature is
465
                            selected
                       if (opl.ccont.solutionValue[j][jold] == 1) { // selected
466
                            (actual 1/2)
467
                           jnew = j;
                           break; // terminate the loop
468
                       }
469
470
                   outselvarstr.write(jnew, ",");
471
                   var myitem = varinfile.readline().split(",");
                   if (jnew > 0) { // selected continuous feature (actual 1/2)
472
                       aselect = 1; // seem to be selected (initialization for
473
                           actual 2/2)
                       for (var q=0; q<=data.p[jnew]; q++) {</pre>
474
475
                           var bcleft = opl.bc.solutionValue[thisOplModel.
                               mContPairs.find(jnew,q)];
476
                           var bcright = opl.bc.solutionValue[thisOplModel.
                               mContPairs.find(jnew,q+1)];
                           var minxjnew = Opl.intValue(myitem[3]);
477
                           var maxxjnew = Opl.intValue(myitem[4]);
478
                           if ((bcleft <= minxjnew) && (bcright >= maxxjnew)) {
479
                               // cover [min,max]
                               aselect = 0; // unselected (actual 2/2)
480
481
                               break;
482
                           }
                       }
483
484
                   }
485
                   outselvarstr.write(aselect, ",");
                   if (aselect == 1) { // actually selected continuous feature
486
```

```
487
                       // Scripting logs 2 (continuous)
                       write("\t", myitem[1], " (Continuous)\n");
488
                       numselcont += 1;
489
                   }
490
491
                   outselvarstr.write("cont,");
                   outselvarstr.write(myitem[1]); // variable name
492
                }
493
                for (var jold=data.dimcontold+1; jold<=data.dimold; jold++) { //</pre>
494
                    CATEGORICAL
                   var jnew = jold-data.exccont;
495
                   outselvarstr.write("\n", iter, ",", jold, ",", jnew, ",");
496
497
                   var aselect = 0; // initialized to be unselected (
                       categorical)
                   var myitem = varinfile.readline().split(",");
498
                   if (opl.f.solutionValue[jnew] == 1) { // selected
499
                       categorical feature (actual 1/2)
500
                       var vat0 = opl.v.solutionValue[thisOplModel.mCatPairs.
                           find(jnew,0)];
                       for (var l=1; l<=data.maxlab[jnew]; l++) {</pre>
501
502
                           var vcur = opl.v.solutionValue[thisOplModel.mCatPairs
                               .find(jnew,1)];
503
                           if (vcur != vat0) { // distinct new groups are
                               detected
504
                               aselect = 1; // selected categorical feature (
                                   actual 2/2)
                               break;
505
506
                           }
                       }
507
                   }
508
                   outselvarstr.write(aselect, ",");
509
                   if (aselect == 1) { // actually selected categorical feature
510
511
                       // Scripting logs 2 (categorical)
                       write("\t", myitem[1], " (Categorical)\n");
512
513
                       numselcat += 1;
                   }
514
                   outselvarstr.write("cat,");
515
```

```
516
                   outselvarstr.write(myitem[1]);
               }
517
               varinfile.close();
518
519
520
               // Scripting logs 3
521
               var numselall = numselcont + numselcat;
               writeln("\nNumber of selected variables = ", numselall, " (",
522
                   numselcont, " continuous + ", numselcat, " categorical)");
523
               writeln("----");
524
               // Closing output text files
525
526
               outerror.close();
527
               outinstance.close();
               outcutcont.close();
528
               outcutcat.close();
529
530
               outregion.close();
531
               outselvarint.close();
532
               outselvarstr.close();
           }
533
534
           else
               writeln("No solution");
535
536
        }
537
538
        opl.end();
539
        data.end();
        def.end();
540
        cplex.end();
541
        source.end();
542
543
        // Engine log (exported)
544
        var inlog = new IloOplInputFile("tmp/current-engine.log");
545
546
        while (!inlog.eof) {
           outlog.writeln(inlog.readline());
547
548
        }
549
        inlog.close();
550
        outlog.close();
```

Code 4.2: Box classifier OPL model

```
1 /**************
   * OPL 22.1.1.0 Model
  * Author: songkomkrit
   * Creation Date: Nov 4, 2024 at 1:15:57 AM
  *****************
5
6
7 /*******************
  * DATA INFORMATION (INPUTS)
  10 int dimold = ...; // old dimension
  int dimcontold = ...; // old continuous dimension
12 int dim = ...; // new dimension
13 int dimcont = ...; // new continuous dimension
14 //int dimcat = ...; // categorical dimension
  int N = ...; // number of instances
  int n = ...; // number of classes
16
17
18 /********************
  * FEATURE SELECTION (INPUTS)
  21 int seltol = ...; // given number of total selected cont/cat dimensions (
     at most)
  int selcont = ...; // UB on number of selected continuous dimensions
  int exccont = ...; // computed LB on number of excluded continuous
     dimensions
24
25 /**************
26
  * INDEX RANGES 1
28 range DS = 1..dim; // for dimensions
29 range DSCONTOLD = 1..dimcontold; // for old continuous dimensions
```

```
30 range DSCONT = 1..dimcont; // for new continuous dimensions
31 range DSCAT = dimcont+1..dim; // for shifted categorical dimensions
32 range IS = 1..N; // for instances
33 range KS = 0..n; // for classes
34
35 /******************
36 * INITIAL PARAMETERS (INPUTS)
38 float M[DS] = ...; // big-M for all new/shifted dimensions (continuous
     and categorical)
  float m[DSCONT] = ...; // small-m for new continuous dimensions
40
41 /*********************
42 * DATA EXTRACTION (INPUTS)
44 float xcontold[IS][DSCONTOLD] = ...; // instances along old continuous
     dimensions
45 int xcat[IS][DSCAT] = ...; // instances along shifted categorical
     dimensions
  int y[IS] = ...; // targets
  int maxlab[DSCAT] = ...; // maximum labels for new categorical dimensions
  int p[DS] = ...; // number of cuts along axes
  int coef[DS] = ...; // product coefficients
50
51 /**************
* NUMBER OF BOXES
  *********************************
54 int B = 1; // initialize the number of boxes
55 execute {
     for (var j in DS)
56
57
        B = B*(p[j]+1); // compute the number of boxes
58 }
59
60 /************
* INDEX RANGES 2
  62
```

```
63 range BS = 0..B-1; // for regions
64
65 /*******************
   * TUPLES
66
67
   68 tuple ContPairType { // index for continuous cut
69
      int j;
70
     int q;
71 };
72
  {ContPairType} ContPairs = {<j, q> | j in DSCONT, q in 0..p[j]+1};
73
74
75 tuple ContTripleType { // index for continuous cut of each individual
      instance
76
     int i;
77
     int j;
78
     int q;
79 };
80
   {ContTripleType} ContTriples = {<i, j, q> | i in IS, j in DSCONT, q in 0...
     p[j]};
82
83 tuple CatPairType { // index for categorical group
84
      int j;
85
     int 1;
86 };
87
   {CatPairType} CatPairs = {<j, 1> | j in DSCAT, 1 in 0..maxlab[j]};
88
89
  /***************
  * DECISION VARIABLES
91
  93 dvar float 1[ContTriples];
94 dvar float r[ContTriples];
95 dvar float bc[ContPairs]; // bc is in R (c = cut)
96 // Note that b is used for beta indexing
```

```
97 dvar float h[BS]; // h
98 dvar boolean a[ContTriples]; // alpha
99 dvar int+ v[CatPairs]; // v (categorical features)
100 dvar boolean g[IS][BS]; // gamma
101 dvar boolean z[BS][KS]; //
102 // Feature selection
103 dvar boolean ccont[DSCONT][DSCONTOLD]; // select continuous dimensions
104 dvar boolean f[DSCAT];
                           // select categorical dimensions
105
106 /***********************
    * OBJECTIVE FUNCTION
107
108
    109 minimize sum(b in BS) h[b]; // min total number of misclassifed
       instances
110
111 /**************************
112
    * CONSTRAINTS
113
    **********************************
114 subject to {
115
116
       forall(j in DSCONT)
117
          getnewcont:
118
              sum(jold in DSCONTOLD) ccont[j][jold] <= 1;</pre>
119
120
       forall(jold in DSCONTOLD)
121
           seloldcont:
122
              sum(j in DSCONT) ccont[j][jold] <= 1;</pre>
123
       forall(j in DSCONT, q in 0..p[j])
124
           bc[<j,q+1>] - bc[<j,q>] >= 0;
125
126
127
       forall(i in IS, j in DSCONT) {
128
           lbound:
              (sum(jold in DSCONTOLD) xcontold[i][jold]*ccont[j][jold]) - (
129
                 sum(q in 0..p[j]) 1[\langle i, j, q \rangle]) >= 0;
130
          rbound:
```

```
(sum(jold in DSCONTOLD) xcontold[i][jold]*ccont[j][jold]) - (
131
                         sum(q in 0..p[j]) r[\langle i, j, q \rangle]) <= 0;
          }
132
133
134
          forall(i in IS, j in DSCONT, q in 0..p[j]) {
               1[\langle i, j, q \rangle] + M[j]*a[\langle i, j, q \rangle] >= 0;
135
136
               1[\langle i,j,q \rangle] - M[j]*a[\langle i,j,q \rangle] <= 0;
137
               1[\langle i,j,q \rangle] - bc[\langle j,q \rangle] + M[j]*a[\langle i,j,q \rangle] <= M[j] + m[j];
138
               1[\langle i,j,q \rangle] - bc[\langle j,q \rangle] - M[j]*a[\langle i,j,q \rangle] >= -M[j] + m[j];
               r[\langle i, j, q \rangle] + M[j]*a[\langle i, j, q \rangle] >= 0;
139
               r[\langle i, j, q \rangle] - M[j]*a[\langle i, j, q \rangle] \le 0;
140
141
               r[\langle i,j,q \rangle] - bc[\langle j,q+1 \rangle] + M[j]*a[\langle i,j,q \rangle] <= M[j] - m[j];
               r[\langle i,j,q \rangle] - bc[\langle j,q+1 \rangle] - M[j]*a[\langle i,j,q \rangle] >= -M[j] - m[j];
142
          }
143
144
          forall(i in IS)
145
146
               (sum(j in DSCONT) coef[j]*(sum(q in 0..p[j]) q*a[<i,j,q>])) + (sum(
                    j in DSCAT) coef[j]*v[<j,xcat[i][j]>]) - (sum(b in BS) b*g[i][b
                    ]) == 0;
147
          forall(i in IS, j in DSCONT)
148
149
               pregion:
150
                    sum(q in 0..p[j]) a[\langle i,j,q \rangle] == 1;
151
152
          forall(i in IS) {
153
               bregion:
                    sum(b in BS) g[i][b] == 1;
154
          }
155
156
          forall(b in BS, k in KS)
157
158
               error1:
159
                    h[b] + (sum(i in IS) (y[i] == k)*g[i][b]) + N*z[b][k] >= 0;
160
          forall(b in BS)
161
162
               error2:
                    sum(k in KS) z[b][k] == n;
163
```

```
164
        forall(j in DSCAT, l in 0..maxlab[j])
165
            v[<j,1>] <= p[j];
166
167
168
        forall(i in IS, j in DSCAT) {
            selcat1:
169
                v[<j,xcat[i][j]>] + M[j]*f[j] >= 0;
170
            selcat2:
171
                v[<j,xcat[i][j]>] - M[j]*f[j] <= 0;
172
        }
173
174
175
        seltolnum:
            (sum(j in DSCONT, jold in DSCONTOLD) ccont[j][jold]) + (sum(j in
176
                DSCAT) f[j]) <= seltol;
177 }
```

4.4 Recalculation of Decision Boxes

Some of selected d features may be trivial; therefore, they cannot be contributing factors. This occurs when two consecutive splitting values along a continuous feature covers an entire dataset or all categorical values are reallocated to the same group. Moreover, no continuous feature may be actually selected $(c_{j,\tilde{j}}^*=0)$, but the proposed classification model usually assumes that there are up to d new continuous features ($|\mathcal{C}_{\text{cont}}| \leq d$). All of these circumstances lead to excessive number of decision boxes. A close examination of optimal splitting values $b_{j,q}^*$ and $v_{j,x_j^*}^*$ can further provide which feature is actually important and should be finally selected, thereby reducing number of boxes. To determine which two distinct boxes can be merged, all numerical decision box labels are recalculated through a transformation q to new labels in a final feature space.

Suppose only d' out of d features are finally selected. The feature map σ : $\{0,1,\ldots,d\}\to\{-1\}\cup\{0,1,\ldots,d'\}$ is defined by

$$\sigma(j) = \begin{cases} \text{feature in new space,} & \text{for finally selected feature } j \\ -1, & \text{for finally unselected feature } j \\ 0, & \text{if } j = 0. \end{cases}$$

There is a one-to-one corresponding between j and $\sigma(j) \geq 0$, and the image of σ includes $0, 1, \ldots, d'$. Consider a decision box $1 \leq \beta \leq B$. Define its position along a feature j by

$$q_j = \begin{cases} \sum_{q=0}^{p_j} q \beta_{j,q}, & \text{for continuous feature } j \\ u_j, & \text{for categorical feature } j. \end{cases}$$

Let $w = \min\{j : q_j \neq 0\}$. If w = 1, then both positions of the current box β and the previous counterpart $\beta - 1$ along the first feature differ by 1. For w > 1, the previous box $\beta - 1$ locates at position p_j along every feature j < w, and the position of both boxes at feature w differs by 1. Based on this observation, the following recurrence relation of new box labels can be obtained:

$$g(\beta) - g(\beta - 1) = -\sum_{j=1}^{w-1} p_j \prod_{j' \in \Sigma_j} (p_{j'} + 1) + 1 \cdot \prod_{j' \in \Sigma_w} (p_{j'} + 1)$$

where $\Sigma_j = \{j' : 0 \le \sigma(j') < \sigma(j)\}.$

The utility module in Code 4.3 includes file copying, floating point number rounding, retrieving all keys of maximum dictionary value, finding an interval containing a given number, and exporting DataFrame with nonduplicate entries. The typecasting module in Code 4.4 can convert a set in string format to a Python set and vice versa, and also express an immutable interval object in string format. The recalculation module in Code 4.5 computes a full list of final numerical decision regions $g(\beta)$. Modules 4.6 and 4.7 returns the dictionaries of selected features and their splitting values respectively. True decision regions including their predicted class labels are computed by Module 4.8. Similar results generated by Module 4.9 is based solely on numerical decision regions, possibly redundant before merging, and their predicted class labels directly reported by CPLEX optimizer. As shown in Chapter 5, CPLEX solutions are inconsistent and therefore infeasible during first few iterations. Module 4.10 calculates the number of correctly classified instances based on the true decision region from Module 4.8 and the CPLEX counterpart from Module 4.9. Clearly, the first is more accurate than the latter. Code 4.11 is the main execution file. A DataFrame iterator initially constructed by the method itertuples is utilized only when a DataFrame, an iterable, can be iterated row by row using the method next during an informational query; nonetheless, its usage is not recommended when a query answer is scattered over rows.

Code 4.3: Basic utility for recalculation of region (module/operation/xutil.py)

```
2 import shutil
3 import json
4 import math
   import numpy as np
   import pandas as pd
7
   # Create directory (if not exist)
   def create_dir(dir):
       1.1.1
10
           Usage: create directory (if not exist)
11
12
           Required arguments:
13
               dir: directory name
       1 \cdot 1 \cdot 1
14
15
       try: os.makedirs(dir)
16
17
       except FileExistsError: pass
18
19
   # Copy single file
20
   def copy(srcpath, destpath):
       1.1.1
22
23
           Usage: copy single file
24
           Required arguments:
25
               srcpath: source pathname
26
               destpath: destination pathname
       1.1.1
27
28
       # Split path into directory and file
29
       srcdir, srcfile = os.path.split(srcpath) # source
30
       destdir, destfile = os.path.split(destpath) # destination
31
32
33
       # Create destination directory (if not exist)
       create_dir(destdir)
34
35
       # Copy source file into destination folder (filename unchanged)
36
37
       shutil.copy2(srcpath, destdir) # preserve file metadata
```

```
38
       # Rename copied file to correct destination filename
39
       os.rename(f"{destdir}/{srcfile}", destpath)
40
41
42
   # Round up or down number to decimal places
43
44
   def round_num(number, decimals, direction):
       1.1.1
45
           Usage: round up or down number to decimal places
46
           Required arguments:
47
               number: number to be rounded
48
               decimals: number of decimal places to round to
49
               direction: either up or down ('up', 'down')
50
           Outputs:
51
               rounded number to specified decimal places
52
       1.1.1
53
54
       if isinstance(decimals, int) or isinstance(decimals, np.integer):
55
           if decimals >= 0:
56
57
               if direction == 'up':
                  return math.ceil(number*10**decimals)/10**decimals
58
59
               elif direction == 'down':
60
                  return math.floor(number*10**decimals)/10**decimals
61
               else:
                  raise TypeError("Direction can be either up or down")
           else:
63
               raise TypeError("Number of decimal places to round to must be
64
                  nonnegative")
65
       else:
           raise TypeError("Number of decimal places must be an integer")
66
67
68
69 # Find maximum value of dictionary and key set
  def max_dictval(dc):
70
       1.1.1
71
```

```
72
            Usage: find maximum value of dictionary and all of its
                corresponding keys
73
            Required arguments:
74
                dc: dictionary
75
            Outputs:
                kmax: set of all keys of maximum value
76
77
                vmax: maximum value
         \mathbf{I}^{-1},\mathbf{I}^{-1}
78
79
        kmax = set()
80
        vmax = dc[next(iter(dc))] # value of first key
81
82
        for k, v in dc.items():
            if v > vmax:
83
                vmax = v
84
                kmax = \{k\}
85
            elif v == vmax:
86
                kmax.add(k)
87
88
89
        return kmax, vmax
90
91
    # Find interval index of specific value from list of real-line splits
93
    def itvpos(x, splits, closed='neither'):
94
95
            Usage: find interval index of specific value from array of real-
                line splits
96
            Required arguments:
97
                x: specific value of interest
                splits: list of real line splits
98
                closed: whether intervals are closed on left-side, right-side
99
                    or neither ('left', 'right', 'neither')
100
            Outputs:
101
                interval index of specific input value
        1 \cdot 1 \cdot 1
102
103
104
        if closed == 'left': # [_, s), [s, _)
```

```
105
            for i, s in enumerate(splits):
106
                if x < s: return i</pre>
107
        elif closed == 'neither': # (_, s), (s, _)
108
            for s in splits:
109
                if x == s:
110
                   raise Exception(f"Open intervals are chosen but input value
                       {x} is at split value {s}")
            closed = 'right' # now safe to be extended to (_, s], (s, _]
111
112
        if closed == 'right': # (_, s], (s, _]
113
114
            for i, s in enumerate(splits):
                if x <= s:
115
116
                   return i
117
        # Last interval
118
        return i + 1
119
120
121
    # Return left and right endpoints of rounded interval
122
    def itvtopts(itv, decimals=2, extend=True):
        1.1.1
124
125
            Usage: return left and right endpoints of rounded interval
126
            Required arguments:
127
                ity: Pandas interval to be rounded
128
            Optional arguments:
129
                decimals: number of decimal places to round to (default: 2)
130
                extend: whether extend (true) or shrink (default) interval (
                    default: True)
131
            Outputs:
132
                lpt: left endpoint of rounded interval
133
                rpt: right endpoint of rounded interval
134
        1 \cdot 1 \cdot 1
135
136
        if isinstance(itv, pd._libs.interval.Interval):
137
            if extend:
138
                ldirect, rdirect = 'down', 'up'
```

```
139
            else:
140
                ldirect, rdirect = 'up', 'down'
141
            if np.isinf(itv.left):
142
143
                lpt = itv.left
144
            else:
                lpt = round_num(itv.left, decimals, ldirect)
145
146
147
            if np.isinf(itv.right):
                rpt = itv.right
148
            else:
149
150
                rpt = round_num(itv.right, decimals, rdirect)
151
152
            return lpt, rpt
153
154
        else:
155
            raise TypeError("Only Pandas intervals are allowed")
156
157
    # Import dictionary from JSON file
    def import_dict(jsonpath):
        1.1.1
160
161
            Usage: parse JSON data into dictionary
162
            Required arguments:
163
                jsonpath: JSON filepath (usually metadata filepath)
164
            Outputs:
165
                dictionary
        1 \cdot 1 \cdot 1
166
167
168
        with open(jsonpath) as file:
169
            contents = file.read()
170
171
        # JSON data is parsed into dictionary
172
        return json.loads(contents)
173
174
```

```
# Export dataframe with nonduplicate entries
    def nondup(df, ndcols, intcols=list(), intdtype='Int16'):
        1.1.1
177
178
            Usage: export dataframe with nonduplicate entries
179
            Required arguments:
180
               df: dataframe
181
               ndcols: two-dimensional multilevel column lists with
                   nonduplicate entries
182
            Optional arguments:
183
               intcols: integer columns (default: empty list)
184
               intdtype: Pandas integer data type (default: 'Int16' or pd.
                   Int16Dtype())
185
            Outputs: same dataframe but without duplicate entries
        1.1.1
186
187
188
        dfn = df.copy(deep=True)
189
        for i in range(len(ndcols),0,-1): # iterate over multilevel column
            lists with nonduplicate entries
            ccols = [f for cols in ndcols[0:i] for f in cols]
190
191
            dfn.loc[dfn[ccols].duplicated(), ccols] = pd.NA
        for col in intcols:
192
193
            dfn[col] = pd.array(dfn[col], dtype=intdtype)
194
195
        return dfn
                   Code 4.4: Typecasting (module/operation/typecast.py)
 1 import numpy as np
    import pandas as pd
 2
```

```
import numpy as np
import pandas as pd

from module.operation.xutil import itvtopts

# Convert set/number in string format to Python set

def strtoset(setstr):
```

```
9
        \mathbf{1}\cdot\mathbf{1}\cdot\mathbf{1}
10
           Usage: convert set/number in string format to Python set
           Required arguments:
11
                setstr: set/number in string format
12
13
            Outputs: corresponding set
        1 \cdot 1 \cdot 1
14
15
        strset = set(setstr.strip().strip('{ }'))
16
17
        try: strset.remove(' ') # for set of more than two elements
        except: pass
18
       numset = set(map(int, strset))
19
20
21
       return numset
22
23
24
   # Convert set to string
   def settostr(st, sep=',', left='{', right='}'):
26
27
           Usage: convert set to string
28
            Required arguments:
                st: set
29
30
           Optional arguments:
                sep: separator (default: ',')
31
32
                left: left symbol (default: '{')
                right: right symbol (default: '}')
33
            Outputs: string representing given set
34
        1.1.1
35
36
37
        stre = sep.join([str(e) for e in st])
38
       return f"{left}{stre}{right}"
39
40
41
42 # Convert Pandas interval to string
43
   def itvtostr(itv, decimals=2, extend=True):
        1.1.1
44
```

```
45
           Usage: convert Pandas interval to string
           Required arguments:
46
               itv: Pandas interval
47
           Optional arguments:
48
49
               decimals: number of decimal places to round to (default: 2)
               extend: whether extend (true) or shrink (default) interval (
50
                  default: True)
51
           Outputs: string interval
       1.1.1
52
53
       lpt, rpt = itvtopts(itv, decimals, extend)
54
55
       1 = f"{lpt:.{decimals}f}"
       r = f"{rpt:.{decimals}f}"
56
57
       if itv.closed == 'neither': return f"({1}, {r})"
58
       elif itv.closed == 'left': return f"[{1}, {r})"
59
       elif itv.closed == 'right': return f"({1}, {r}]"
60
       else: return f"[{1}, {r}]"
61
62
63
64 # Describe Pandas interval in text format
   def itvtodesc(itv, decimals=2, extend=True):
       1.1.1
66
67
           Usage: describe Pandas interval in text format
           Required arguments:
68
               itv: Pandas interval
69
           Optional arguments:
70
               decimals: number of decimal places to round to (default: 2)
71
72
               extend: whether extend (true) or shrink (default) interval (
                  default: True)
           Outputs: description of interval in text format
73
       1.1.1
74
75
76
       lpt, rpt = itvtopts(itv, decimals, extend)
       1 = f"{lpt:.{decimals}f}"
77
       r = f"{rpt:.{decimals}f}"
78
```

```
79
       esum = itv.left + itv.right
80
       if np.isnan(esum): # -np.inf, np.inf
81
           return "any number"
82
83
       elif not np.isinf(esum): # num, num
           return f"between {1} and {r}"
84
       elif esum < 0: # -np.inf, num</pre>
85
           return f"below {r}"
86
       else: # num, np.inf
87
           return f"above {1}"
88
              Code 4.5: Recalculation of regions (module/operation/calregs.py)
1 import numpy as np
2
3
   # Calculate new corresponding region label (helper)
   def hcalbn(bo, bnprev, idxn, pcuto, pocum, pncumx):
       111
           Usage: calculate new corresponding region label (helper)
 7
           Required arguments:
8
9
               bo: region label for old features (nonzero)
               bnprev: previous region label for new features
10
               idxn: new feature indexes
11
12
               pcuto: old cut numbers
               pocum: cumulative number of box regions across old features
13
14
               pncumx: cumulative number of extrended box regions across new
                  features
15
           Outputs: corresponding region label
       1.1.1
16
17
       # bo must be between 1 and np.prod(pcuto+1)-1
18
19
       bn = bnprev
20
       for jmax in range(len(pcuto)-1,-1,-1):
```

```
21
           # bo (incremented by 1) in base representation has the last nonzero
                at digit jmax
           if bo%pocum[jmax] == 0:
22
               for j in range(jmax):
23
24
                  bn -= pcuto[j]*pncumx[idxn[j]]
               bn += pncumx[idxn[jmax]]
25
26
               break
27
       return bn
28
29
30
31
   # Calculate corresponding decision regions (helper)
   def hcalregs(BO, idxn, pcuto, pocum, pncumx):
32
       1.1.1
33
           Usage: calculate corresponding decision regions (helper)
34
35
           Required arguments:
36
               BO: total number of old box regions
37
               idxn: new feature indexes
38
               pcuto: old cut numbers
39
               pocum: cumulative number of box regions across old features
               pncumx: cumulative number of extrended box regions across new
40
                  features
41
           Outputs: corresponding region label
       111
42
43
       bns = [0] # list of corresponding box regions (region 0)
44
       for bo in range(1, BO):
45
           bnprev = bns[-1]
46
47
           bn = hcalbn(bo, bnprev, idxn, pcuto, pocum, pncumx)
           bns.append(bn)
48
49
50
       return bns
51
52
53 # Calculate new corresponding decision regions (main)
```

```
54 def calregs(pcuto, sidx, pdtype=np.int16, idtype=np.int16, rdtype=np.int16
       ):
       111
55
           Usage: calculate new corresponding decision regions (main)
56
57
           Required arguments:
              pcuto: old cut numbers
58
59
              sidx: selected feature indexes (in order)
60
           Optional arguments:
              pdtype: NumPy data type of cut number (default: np.int16)
61
              idtype: NumPy data type of index (default: np.int16)
62
              rdtype: NumPy data type of region number (default: np.int16)
63
64
           Outputs: new correspoding regions
       1.1.1
65
66
       # Typecasting
67
       pcuto = np.array(pcuto, dtype=pdtype)
68
69
       sidx = np.array(sidx, dtype=idtype)
70
       # Basic calculation
71
72
       dimo = pcuto.size # old dimension
73
       dimn = sidx.size # new dimension
74
       pcutn = pcuto[sidx] # new cut numbers
75
       BO = np.prod(pcuto+1).astype(rdtype) # number of old regions
       BN = np.prod(pcutn+1).astype(rdtype) # number of new regions
76
77
       # New feature indexes
78
       idxn = np.full(dimo, -1, dtype=idtype)
79
       idxn[sidx] = np.arange(dimn, dtype=idtype)
80
       idxn[idxn < 0] = np.arange(dimn, dimo, dtype=idtype)</pre>
81
82
83
       # Cumulative number of box regions
84
       pocum = np.cumprod(np.append([1], pcuto[0:-1]+1), dtype=rdtype) # old
       pncum = np.cumprod(np.append([1], pcutn[0:-1]+1), dtype=rdtype) # new
85
       pncumx = np.concatenate((pncum, np.zeros(dimo-dimn, dtype=rdtype))) #
86
           new and extended
```

```
88
        # New correspoding regions (helper function called)
        bns = np.array(hcalregs(BO, idxn, pcuto, pocum, pncumx), dtype=rdtype)
89
90
        # Output
91
92
        return bns
93
94
95 # Illustration
96
97 print('pcuto: {0}\nsidx: {1}\nbns: {2}\n'.format(pcuto:=[3, 4], sidx:=[0],
         calregs(pcuto, sidx)))
98 print('pcuto: {0}\nsidx: {1}\nbns: {2}\n'.format(pcuto:=[3, 4], sidx:=[1],
         calregs(pcuto, sidx)))
99 print('pcuto: {0}\nsidx: {1}\nbns: {2}\n'.format(pcuto:=[3, 4], sidx:=[0,
        1], calregs(pcuto, sidx)))
100 print('pcuto: {0}\nsidx: {1}\nbns: {2}\n'.format(pcuto:=[3, 4], sidx:=[1,
        0], calregs(pcuto, sidx)))
101
                   Code 4.6: Feature selection (module/model/findsels.py)
 1 # Find feature selection
   def findsels(itsel, pcuto):
        1.1.1
 3
           Usage: find feature selection (per file)
 4
 5
           Required arguments:
               itsel: selected string variables (DataFrame iterator)
 6
               pcuto: old cut numbers
 7
 8
            Outputs:
 9
               tsels: dictionary of selected variables and given number of
                   cuts
        1 \cdot 1 \cdot 1
10
11
12
        csrow = next(itsel) # iterator of selected string variables across all
```

iterations

```
13
       tsels = dict() # selected variables and given number of cuts
14
       citer = -1 # current iteration
15
       while True:
16
17
           try:
               if csrow.aselect == 1: # for selected variable
18
19
                  if csrow.iter != citer:
                      citer = csrow.iter
20
                      tsels[citer] = {
21
                          'variables': list(), # selected feature
22
23
                          'types': list(), # type of selected feature
24
                          'js': list(), # selected index
                          'ps': list() # given cut number
25
                      }
26
                  tsels[citer]['variables'].append(csrow.variable)
27
                  tsels[citer]['types'].append(csrow.type)
28
                  tsels[citer]['js'].append(csrow.jnew)
29
                  tsels[citer]['ps'].append(pcuto[csrow.jnew-1])
30
               csrow = next(itsel) # update DataFrame iterator
31
32
           except StopIteration:
               break
33
34
35
       return tsels
                 Code 4.7: Cuts or split values (module/model/findcuts.py)
1 import numpy as np
   import pandas as pd
3
4 # Find cuts and groups
5 def findcuts(tsels, itcont, itcat, intvclosed='neither', intvsubtype='
       float32'):
       1.1.1
6
7
           Usage: find cuts and groups (per file)
```

8

Required arguments:

```
9
               tsels: dictionary of selected variables and given number of
                  cuts
               itcont: full continuous cuts (DataFrame iterator)
10
               itcat: full categiorical cuts (DataFrame iterator)
11
12
           Optional arguments:
               intvclosed: types of Pandas interval sides (values: 'left', '
13
                  right', 'both', 'neither')
               intvsubtype: types of Pandas interval bounds (subtype of pandas.
14
                  IntervalDtype)
           Outputs:
15
               tcuts: dictionary of cuts and groups along all selected
16
                  features
       1 \cdot 1 \cdot 1
17
18
       ccontrow = next(itcont) # iterator of full continuous cuts across all
19
           iterations
20
       ccatrow = next(itcat) # iterator of full categorical cuts across all
           iterations
       tcuts = dict() # cuts and groups along all selected features
21
22
       for citer, sel in tsels.items(): # cuts across all selected features
23
24
           tcuts[citer] = dict()
           for ind, j in enumerate(sel['js']):
25
26
               tcuts[citer][j] = {
                   'variable': tsels[citer]['variables'][ind],
27
                   'type': tsels[citer]['types'][ind],
28
                   'cuts': list(),
29
                   'groups': dict()
30
31
               }
32
           # Cuts
33
34
           while ccontrow.iter < citer: # previous iteration may select no</pre>
               continuous feature
35
               ccontrow = next(itcont)
36
           while ccatrow.iter < citer: # previous iteration may select no</pre>
               categorical feature
```

```
37
              ccatrow = next(itcat)
           for jcur in sorted(sel['js']): # numerically sorted features
38
              selected
              cuts = tcuts[citer][jcur]['cuts'] # list of cuts along specific
39
                   selected feature
              try: # iterate over full continuous cuts
40
                  while ccontrow.iter == citer:
41
42
                      if ccontrow.j > jcur: # seek no more than current
                         feature
                          break
43
                      else:
44
45
                          if ccontrow.j == jcur: # at current selected feature
                             cuts.append(ccontrow.bc) # continuous feature
46
                                 seen
                          ccontrow = next(itcont) # update DataFrame iterator
47
48
              except StopIteration:
49
                  pass
              try: # iterate over full categorical cuts
50
51
                  while ccatrow.iter == citer:
52
                      if ccatrow.j > jcur: # seek no more than current feature
53
                         break
                      else:
54
55
                          if ccatrow.j == jcur: # at current selected feature
                             cuts.append(ccatrow.v) # categorical feature seen
56
                          ccatrow = next(itcat) # update DataFrame iterator
57
              except StopIteration:
58
59
                  pass
60
           # Groups
61
           pcutdc = dict(zip(tsels[citer]['js'], tsels[citer]['ps'])) # cut
62
              numbers along selected features
63
           for j, info in tcuts[citer].items():
              pnum = pcutdc[j] # number of cuts on current selected feature
64
              cuts = info['cuts']
65
              if info['type'] == 'cont': # continuous feature
66
                  excuts = [-np.inf] + cuts + [np.inf]
67
```

```
68
                  intvs = pd.arrays.IntervalArray.from_breaks(
                      breaks=excuts,
69
70
                      copy=False, # default: False
                      closed=intvclosed, # types of Pandas interval sides
71
72
                      dtype=pd.IntervalDtype(subtype=intvsubtype) # types of
                         Pandas interval bounds
                  )
73
                  info['groups'] = {gr: intvs[gr] for gr in range(pnum+1)}
74
              else: # categorical feature
75
                  info['groups'] = {gr: set() for gr in range(pnum+1)}
76
77
                  for val, gr in enumerate(cuts):
78
                      info['groups'][gr].add(val) # categorical value in cut/
                         group
79
       return tcuts
80
               Code 4.8: True decision regions (module/model/findtregs.py)
1 import numpy as np
   import pandas as pd
2
3
4 from module.operation.xutil import max_dictval, itvpos
5
   # Calculate new true decision regions and predictions (truly correct)
   def findtregs(tsels, tcuts, df, pdtype=np.int16):
9
10
           Usage: calculate new true decision regions and predictions (per
              file)
11
           Required arguments:
              tsels: dictionary of selected variables and given number of
12
                  cuts
13
              tcuts: dictionary of cuts and groups along all selected
```

features

```
14
              df: training dataset including target variable (DataFrame, not
                  iterator)
           Optional arguments:
15
              pdtype: NumPy data type of cut number (default: np.int16)
16
17
           Outputs:
              ttregs: dictionary of new true decision regions and their
18
                  predicted classes
       1.1.1
19
20
       ttregs = dict() # new true regions with predicted classes (truly
21
           correct)
       classes = df['class'].unique() # all possible classes
22
23
       for citer in tsels.keys():
24
           regs = pd.Series([0]*len(df))
25
26
           js = tsels[citer]['js']
27
           pcutn = np.array(tsels[citer]['ps'], dtype=pdtype) # new cut
           pncum = np.cumprod(np.append([1], pcutn[0:-1]+1), dtype=pdtype) #
28
              cumulative number of new box regions
           BN = np.prod(pcutn+1) # number of new regions
29
30
31
           # Convert base representation of decision region to base 10
32
           for ind, j in enumerate(js):
              info = tcuts[citer][j]
33
              attr = info['variable']
34
              cuts = info['cuts']
35
              if info['type'] == 'cont': # continuous feature
36
                  regs = regs + pncum[ind]*df[attr].apply(lambda x: itvpos(x,
37
                      cuts))
              else: # categorical feature
38
39
                  regs = regs + pncum[ind]*pd.Series([cuts[x] for x in df[attr
                      ]])
40
41
           # Find predicted classes in decision regions
           ttregs[citer] = {
42
```

```
'classes': set(), # true predicted class set
44
                  'correct': 0, # number of instances correctly predicted
45
                  'ninst': 0, # number of training instances (total)
46
47
                  'ncinst': {n: 0 for n in range(len(classes))} # number of
                      training instances in targets
              } for b in range(BN)
48
           }
49
           for i in range(len(df)):
50
              ttregs[citer][regs[i]]['ninst'] += 1 # instance in region
51
              ttregs[citer][regs[i]]['ncinst'][df['class'][i]] += 1 #
52
                  instance of specific target in region
           for b in range(BN):
53
              kmax, vmax = max_dictval(ttregs[citer][b]['ncinst']) # true
54
                  majority voting
55
              ttregs[citer][b]['classes'] = kmax # all classes that have
                  maximum number of instances
              ttregs[citer][b]['correct'] = vmax # maximum number of
56
                  instances
57
58
       return ttregs
              Code 4.9: CPLEX decision regions (module/model/findcregs.py)
1 import numpy as np
2
  from module.operation.typecast import strtoset
   from module.operation.calregs import calregs
5
6
   # Calculate new cplex decision regions and predictions (partially correct)
   def findcregs(tsels, itpred, pcuto, idtype=np.int16, pdtype=np.int16):
       1.1.1
9
10
           Usage: calculate new cplex decision regions and predictions (per
              file)
```

b: {

43

```
11
           Required arguments:
12
              tsels: dictionary of selected variables and given number of
                  cuts
              itpred: individual result of cplex prediction (DataFrame
13
                  iterator)
              pcuto: old cut numbers
14
15
           Optional arguments:
              pdtype: NumPy data type of cut number (default: np.int16)
16
17
              idtype: NumPy data type of index (default: np.int16)
           Outputs:
18
              tcregs: dictionary of new cplex decision regions and their
19
                  predicted classes
       1.1.1
20
21
22
       cprow = next(itpred) # iterator of instance predictions across all
           iterations
23
       tcregs = dict() # new cplex regions with predicted classes (partially
       classes = set() # set all possible classes (collected from training
24
           dataset)
25
26
       citer = -1 # current iteration
27
28
       while True: # reported by cplex as occupied region
29
          try:
              if cprow.iter != citer: # new iteration
30
                  citer = cprow.iter
31
                  if citer in tsels.keys(): # current iteration actually
32
                      selects at least one feature
                      keep = True # keep doing in this while loop
33
                      pcutn = np.array(tsels[citer]['ps'], dtype=pdtype)
34
35
                      sidx = np.array(tsels[citer]['js'], dtype=idtype) - 1 #
                         index starts at 0
36
                      BN = np.prod(pcutn+1) # number of new regions
37
                      bns = calregs(pcuto, sidx) # new correspoding regions
                      tcregs[citer] = {
38
```

```
b: {
39
                             'lclasses': list(), # list of cplex predicted
40
                                 class set
                             'nlcinst': list() # list of instance number in
41
                                 corresponding cplex class set
                          } for b in range(BN)
42
                      }
43
44
                  else: # current iteration selects no feature
                      keep = False # update iterator and go to the next while
45
                         loop
              if keep and cprow.iter == citer: # every record in iteration
46
                  that selects feature
                  creg = tcregs[citer][bns[cprow.region]] # new cplex region
47
                  pset = strtoset(cprow.predict) # current set of classes
48
                      predicted by cplex
49
                  classes = classes.union(pset) # add to set of all possible
                      classes
                  try: # current set of predicted classes already exists
50
                      creg['nlcinst'][creg['lclasses'].index(pset)] += 1
51
52
                  except ValueError: # new set of predicted classes
                      creg['lclasses'].append(pset)
53
54
                      creg['nlcinst'].append(1)
              cprow = next(itpred) # update DataFrame iterator
55
           except StopIteration:
56
              break
57
58
       for cregs in tcregs.values(): # reported by cplex as unoccupied region
59
           for creg in cregs.values():
60
              if not creg['lclasses']:
61
                  creg['lclasses'] = [classes] # predict only one of the
62
                      entire set
63
                  nlcinst = [0] # no instance reported by cplex in the rest of
                       new regions
64
65
       return tcregs
```

Code 4.10: Classification correctness (module/model/findcorr.py)

```
1 # Find both true and recalculated cplex correctness
   def findcorr(ttregs, tcregs):
3
4
           Usage: find both true and recalculated cplex correctness (per file)
           Required arguments:
5
              ttregs: dictionary of new true decision regions and their
 6
                  predicted classes
              tcregs: dictionary of new cplex decision regions and their
                  predicted classes
8
           Outputs:
9
              tcorr: true number of correctly classified instances per region
10
              ccorr: recalculated cplex number of correctly classified
                  instances per region
       1.1.1
11
12
13
       tcorr = dict() # true correctness
14
       ccorr = dict() # cplex correctness
       for citer, tregs in ttregs.items(): # true classification
15
16
           tcorr[citer] = {
17
               'correct': 0,
               'detail': {b: tregs[b]['correct'] for b in tregs.keys()}
18
19
           tcorr[citer]['correct'] = sum(tcorr[citer]['detail'].values())
20
21
       for citer, cregs in tcregs.items(): # cplex classification
           ccorr[citer] = {
22
23
               'correct': 0,
               'detail': {b: 0 for b in cregs.keys()}
24
           }
25
           for b in cregs.keys():
26
              for soc in tcregs[citer][b]['lclasses']:
27
                  ccorr[citer]['detail'][b] = max([ttregs[citer][b]['ncinst'][
28
                      c] for c in soc])
           ccorr[citer]['correct'] = sum(ccorr[citer]['detail'].values())
29
30
```

Code 4.11: Final mixed box classifier (finalbox.py)

```
1 import csv
  import re
3 import pandas as pd
 4
5 from module.operation.xutil import *
  from module.operation.typecast import settostr, itvtostr, itvtodesc
  from module.operation.calregs import calregs
8 from module.model.findsels import findsels
  from module.model.findcuts import findcuts
  from module.model.findtregs import findtregs
11 from module.model.findcregs import findcregs
12 from module.model.findcorr import findcorr
13
14
15 # Parameters
16 pcuto = [3,3,2] # original cut numbers across all given features
  isexample = True # whether example is shown
  issreport = True # whether reports of feature selection are written
19 isrreport = True # whether reports of detailed decision regions are
       written
20
21 # Informational prefixes/postfixes
22 ts = "75305" # last digits of timestamp
23 data = "seltrain20num3each20" # data name (no file extension)
   inprefix = f"{ts}-{data}-export-" # input filename prefix
   inpostfix = "-mfullaltseltol-2-t-1440" # input filename postfix
25
26
27 # Required inputs
28 datdir = "../../Projects/Box Classifiers/alternative/input" # directory
        of training instances (cplex inputs)
```

```
29 indir = "../../Projects/Box Classifiers/alternative/output" # main
       input directory (cplex results)
30 datfile = f"{data}.csv" # training dataset with target variable
31 datpredfile = f"{inprefix}predict-instance-pcont-3{inpostfix}.csv" #
       individual result of cplex prediction
32 inerrfile = f"{inprefix}error{inpostfix}.csv" # classification errors and
       performance metrics
33 inselfile = f"{inprefix}select-var-str-pcont-3{inpostfix}.csv" # selected
       string variables
34 incutcontfile = f"{inprefix}cutcont-full-pcont-3{inpostfix}.csv" #
       continuous cuts
35 incutcatfile = f"{inprefix}cutcat-full-pcont-3{inpostfix}.csv" #
       categorical cuts
36
  # Optional inputs
38
   if issreport: # reports of feature selection must be written
39
       metadir = "../../Data/Encoded/metadata" # metadata directory
       metafile = "meta-indep-pppub20enc.json" # metadata (after encoding)
40
          file
41
       # Relabel case-insensitive NIU values for all selected categorical
          features
42
       niudc = {'SS_YN': "NIU (aged below 15)", 'PEMLR': "NIU"}
   if isrreport: # reports of detailed decision regions must be written
44
       clabels = {0: 'NNN', 1: 'NNY', 2: 'NY_', 3: 'YNN', 4: 'Y1Y'}
45
46 # Required outputs
47 outdir = f"../../../Outputs/Main/Box/{data}" # main output directory
48 outeperffile = f"{ts}-eperf.csv" # classification performances (accuracy/
       error/time)
49 outselfile = f"{ts}-selvarfin.csv" # selected string variables, cuts and
       groups
  outregfile = f"{ts}-predregfin.csv" # full decision regions
51
52 # Optional outputs
53 outcutcontfile = f"{ts}-cutcont.csv" # continuous cuts
54 outcutcatfile = f"{ts}-cutcat.csv" # categorical cuts
```

```
55
  if issreport: # reports of feature selection must be written
       outsrepwdfile = f"{ts}-report-sel-dup.csv" # with duplicate entries
56
57
       outsrepndfile = f"{ts}-report-sel-nondup.csv" # with nonduplicate
          entries
   if isrreport: # reports of detailed decision regions
58
       outrrepwdfile = f"{ts}-report-reg-dup.csv" # with duplicate entries
59
       outrrepndfile = f"{ts}-report-reg-nondup.csv" # with nonduplicate
60
          entries
61
62 # Create main output directory (if not exist)
63 create_dir(outdir)
64
65 # Import datasets
66 dfe = pd.read_csv(f"{indir}/{inerrfile}") # cplex classification errors
       and performance metrics
67 dfs = pd.read_csv(f"{indir}/{inselfile}") # selected string variables
68 dfcont = pd.read_csv(f"{indir}/{incutcontfile}") # full continuous cuts
69 dfcat = pd.read_csv(f"{indir}/{incutcatfile}") # full categorical cuts
70 df = pd.read_csv(f"{datdir}/{datfile}") # training dataset including
       target variable
71 dfp = pd.read_csv(f"{indir}/{datpredfile}") # individual result of cplex
       prediction
72
73 # Initialize DataFrame iterators
74 itsel = dfs.itertuples() # selected string variables
75 itcont = dfcont.itertuples() # full continuous cuts
76 itcat = dfcat.itertuples() # full categorical cuts
77 itpred = dfp.itertuples() # individual result of cplex prediction
78
79 # Main execution
80 tsels = findsels(itsel, pcuto) # selected variables
81 tcuts = findcuts(tsels, itcont, itcat) # cuts along all selected features
82 ttregs = findtregs(tsels, tcuts, df) # new true regions and predicted
83 tcregs = findcregs(tsels, itpred, pcuto) # new cplex regions and predicted
        classes
```

```
84 tcorr, ccorr = findcorr(ttregs, tcregs) # true/cplex correctness
85
    # Calculate performance results
86
    dfen = pd.DataFrame({
87
88
        'iter': tcorr.keys(), # iteration that selects feature
        'taccuracy': [info['correct']*100/len(df) for info in tcorr.values()],
89
           # true accuracies
        'caccuracy': [info['correct']*100/len(df) for info in ccorr.values()],
90
           # recalculated cplex accuracies
        'terror': [len(df) - info['correct'] for info in tcorr.values()], #
91
           true errors
92
        'cerror': [len(df) - info['correct'] for info in ccorr.values()] #
           recalculated cplex errors
93 })
94 dfen = pd.merge(dfen, dfe, how='outer')
   dfen.rename(columns = {
96
        'error': 'rerror', # reported cplex errors
        'accuracy': 'raccuracy' # reported cplex accuracies
97
98 }, inplace=True)
99 cols = dfen.columns.tolist()
100 new_cols = cols[0:1] + cols[5:5+len(pcuto)] + cols[1:3] + cols[-6:-5] +
        cols[3:5] + cols[-7:-6] + cols[-5:]
101 dfen = dfen[new_cols] # rearranged columns
102 dfen['ms'] = dfen['ms']/60000 # convert milliseconds to minutes
103 dfen = dfen.rename(columns={'ms':'minute'})
104
105 # Display performance results
106 print(f"\n{dfen}\n")
107
108 # Examples
109
   if isexample:
110
        iters = [1, 2, 15]
        for citer in iters:
111
112
           try:
113
               print(f"Selected features (iteration {citer})\n{tsels[citer]}\n
                   ")
```

```
print(f"Cuts (iteration {citer})\n{tcuts[citer]}\n")
114
               print(f"True decision regions (iteration {citer})\n{ttregs[
115
                   citer]}\n")
               print(f"Cplex decision regions (iteration {citer})\n{tcregs[
116
                   citer]}\n")
               print(f"True correctness (iteration {citer})\n{tcorr[citer]}\n")
117
               print(f"Cplex correctness (iteration {citer})\n{ccorr[citer]}\n
118
                   ")
           except KeyError:
119
               print(f"Iteration {citer} selects no features\n")
120
121
122 # Export non-edited information
123 copy(f"{indir}/{incutcontfile}", f"{outdir}/{outcutcontfile}") #
        continuous cuts
124 copy(f"{indir}/{incutcatfile}", f"{outdir}/{outcutcatfile}") # categorical
         cuts
125
126 # Export performance results (accuracy/error/time)
127 dfen.to_csv(f"{outdir}/{outeperffile}", float_format="%.2f", header=True,
        index=False)
128
    # Export selected variables, cuts and groups
    with open(f"{outdir}/{outselfile}", 'w', newline='') as file:
        writer = csv.DictWriter(
131
132
           file.
           fieldnames = [
133
               'iter', 'jfin', 'j', 'var', 'type',
134
               'p', 'cuts', 'groups'
135
           ]
136
137
        )
138
        writer.writeheader()
139 for citer, info in tsels.items():
        cuts = [[round(cut, 2) for cut in tcuts[citer][j]['cuts']] for j in
140
           info['js']]
        groups = list()
141
```

```
142
        for ind, j in enumerate(info['js']):
            if info['types'][ind] == 'cont': # continuous feature
143
               jgrs = dict()
144
               for gr, member in tcuts[citer][j]['groups'].items():
145
146
                   jgrs[gr] = itvtostr(member)
147
               groups.append(jgrs)
148
            else: # categorical feature
               groups.append(tcuts[citer][j]['groups'])
149
150
        dfstmp = pd.DataFrame({
            'iter': citer,
151
            'jfin': range(1, len(info['js'])+1), # 1, 2, ...
152
153
            'j': info['js'], # j in cplex model
            'variable': info['variables'],
154
            'type': info['types'],
155
            'p': info['ps'],
156
157
            'cuts': cuts,
158
            'groups': groups
159
        })
        dfstmp.to_csv(f"{outdir}/{outselfile}", mode='a', header=False, index=
160
            False)
    del dfstmp
162
    # Export predicted classes and number of instances in all decision regions
    with open(f"{outdir}/{outregfile}", 'w', newline='') as file:
        writer = csv.DictWriter(
165
166
            file.
167
            fieldnames = ['iter', 'reg', 'ninst', 'tpred', 'cpred',
                         'tcorr', 'ccorr', 'ncinst']
168
169
        )
        writer.writeheader()
170
171
        for citer, tregs in ttregs.items():
172
            for b, treg in tregs.items():
               writer.writerow({
173
                   'iter': citer,
174
175
                   'reg': b,
176
                   'ninst': treg['ninst'], # number of instances
```

```
177
                   'tpred': settostr(treg['classes']), # true predicted class
                   'cpred': ','.join([settostr(st) for st in tcregs[citer][b]['
178
                       lclasses']]), # cplex predicted class
                   'tcorr': tcorr[citer]['detail'][b], # true correctness
179
180
                   'ccorr': ccorr[citer]['detail'][b], # cplex correctness
                   'ncinst': treg['ncinst'] # targets and number of member
181
                       instances
               })
182
183
184
    # Export final reports of feature selection (with duplicate/nonduplicate
185
        entries) (if specified)
186
    if issreport: # reports of feature selection must be written
187
188
189
        # New labels of selected categorical features (catvdc)
190
        metadc = import_dict(jsonpath=f"{metadir}/{metafile}") # metadata after
            encoding
        catvars = set() # all selected categorical features (initialized)
191
192
        pattern = r'(^|[^\w])(niu)([^\w]|^*) # regex to search for niu
        pattern = re.compile(pattern, re.IGNORECASE)
193
194
        for info in tsels.values():
195
           for ind, attr in enumerate(info['variables']):
196
               if info['types'][ind] == 'cat':
197
                   catvars.add(attr)
        catvdc = {attr: metadc[attr]['values'] for attr in catvars} # labels of
198
             selected categorical features
        for attr, valdc in catvdc.items():
199
200
           for val, desc in valdc.items():
               matches = re.search(pattern, desc.replace(',', ''))
201
202
               if bool(matches): # case-insensitive value label containing niu
203
                   try:
204
                       catvdc[attr][val] = niudc[attr] # relabel
205
                   except KeyError: # new NIU label of current feature is
                      missing
206
                       pass
```

```
207
208
        # True classification accuracies and performance metrics
        efields = ['iter', 'taccuracy', 'minute', 'acctmin', 'status']
209
210
211
        # Groups
        grls = list() # list of all member groups across all features and
212
            iterations
213
        for citer, scuts in tcuts.items():
214
            for j, info in scuts.items(): # cuts along all selected feature
               vartype = 'Continuous' if info['type'] == 'cat' else 'Categorical
215
216
               if info['type'] == 'cont': # continuous feature (groups not
                   displayed for convenience)
                   for gr, member in info['groups'].items():
217
                       dc = {
218
                           'iter': citer,
219
220
                           'j': j, 'variable': info['variable'],
                           'type': 'Continuous',
221
222
                           'label': metadc[info['variable']]['label'],
223
                           'group': gr,
                           'member': itvtostr(member),
224
225
                           'desc': itvtodesc(member, decimals=0, extend=False).
                              capitalize()
226
                       }
227
                       grls.append(dc)
               else: # categorical feature (groups displayed)
228
229
                   for gr, member in info['groups'].items():
                       for elem in member: # all elements in group member
230
231
                           desc = catvdc[info['variable']][str(elem)]
232
                           dc = {
                               'iter': citer,
233
234
                               'j': j, 'variable': info['variable'],
235
                               'type': 'Categorical',
236
                               'label': metadc[info['variable']]['label'],
237
                               'group': gr,
238
                               'member': elem,
```

```
'desc': desc
239
                           }
240
241
                           grls.append(dc)
242
        dfg = pd.DataFrame(grls) # group dataframe
243
244
        # Report dataframe of feature selection with duplicate entries (dfrp)
        dfsrp = pd.merge(dfen[efields], dfg) # merge two dataframes: error/
245
            metric and group
246
247
        # Report dataframe of feature selection with nonduplicate entries (dfn)
248
        dfsrpn = nondup(
249
            dfsrp,
250
            ndcols=[
                ['iter', 'taccuracy', 'minute', 'acctmin', 'status'],
251
                ['j', 'variable', 'type', 'label'],
252
253
                ['group']
254
            ],
            intcols=['iter', 'status', 'j', 'group'] # integer columns
255
        )
256
257
        # Export final reports of feature selection
258
        dfsrp.to_csv( # with duplicate entries
259
            f"{outdir}/{outsrepwdfile}",
260
261
            float_format="%.2f",
            header=True, index=False
262
263
264
        dfsrpn.to_csv( # with nonduplicate entries
265
            f"{outdir}/{outsrepndfile}",
266
            sep=',', na_rep='',
267
            float_format="%.2f",
            header=True, index=False
268
269
        )
270
271 print(f"{dfsrp.head()}\n") # feature selection (with duplicate entries)
272 print(f"{dfsrpn.head()}\n") # feature selection (with nonduplicate entries
        )
```

```
273
274
    # Export final reports of detailed decision regions (with duplicate/
        nonduplicate entries) (if specified)
276
    if isrreport: # reports of detailed decision regions must be written
277
278
279
        # Export final reports of detailed regions (with duplicate entries)
280
        with open(f"{outdir}/{outrrepwdfile}", 'w', newline='') as file:
            writer = csv.DictWriter(
281
282
                file,
283
                fieldnames = [
                    'iter',
284
                    'ordvars', 'strvars',
285
                    'reg', 'ordreg', 'crossreg',
286
                    'tpreds', 'strtpreds',
287
                    'ninst'
288
               1)
289
            writer.writeheader()
290
291
            for citer, tregs in ttregs.items():
                strvars = ', '.join(tsels[citer]['variables'])
292
293
                ps = tsels[citer]['ps']
                qs = [0]*len(ps) # base representation of numerical decision
294
                   region
                js = tsels[citer]['js']
295
296
                for b, treg in tregs.items():
297
                   grls = list() # list of group members
298
                   for ind in range(len(ps)):
299
                       member = tcuts[citer][js[ind]]['groups'][qs[ind]]
300
                       if isinstance(member, pd._libs.interval.Interval): #
                           Pandas interval
301
                           grls.append(itvtostr(member))
302
                       elif isinstance(member, set): # set
303
                           grls.append(settostr(member))
304
                       else:
```

```
305
                          raise TypeError("Cut intervals can be either Pandas
                              intervals or sets")
306
                   writer.writerow({
307
                       'iter': citer,
                       'ordvars': f"({','.join([str(j) for j in js])})", #
308
                          ordered pair of selected features
                       'strvars': strvars, # string of selected features
309
310
                       'reg': b,
311
                       'ordreg': f"({','.join([str(q) for q in qs])})", #
                           ordered pair of numerical region
312
                       'crossreg': 'x'.join(grls), # cross product of
                          features in string format
313
                       'tpreds': ','.join([str(v) for v in treg['classes']]), #
                           true predicted classes
                       'strtpreds': ', '.join([clabels[v] for v in treg['
314
                           classes']]), # true predicted classes
315
                       'ninst': treg['ninst'] # number of training instances in
                           region
                   })
316
317
                   for ind in range(len(ps)): # increment base representation
                       of region for next for loop
                       qs[ind] += 1 # increment by 1
318
319
                       if qs[ind] > ps[ind]: qs[ind] = 0 # new leading one
320
                       else: break # same leading one
321
322
        # Export final reports of detailed regions (with nonduplicate entries)
323
        dfrrp = pd.read_csv(f"{outdir}/{outrrepwdfile}")
324
        dfrrpn = nondup(dfrrp, ndcols=[['iter', 'ordvars', 'strvars']], intcols
           =['iter'])
325
        dfrrpn.to_csv( # with nonduplicate entries
            f"{outdir}/{outrrepndfile}",
326
327
            sep=',', na_rep='',
           header=True, index=False
328
329
        )
330
```

```
331 print(f"{dfrrp.head()}\n") # detailed decision regions (with duplicate
        entries)
332 print(f"{dfrrpn.head()}\n") # detailed decision regions (with nonduplicate
         entries)
333
334
335
    # Reexamination of CPLEX Results
336
337 # Additional output files
338 outexffile = f"{ts}-exam-full.csv" # full cplex reexamination
339 outexdfile = f"{ts}-exam-diff.csv" # difference in new decision regions
340 outexnfile = f"{ts}-exam-diffnum.csv" # number of difference
341
    # Convert full coordinate to position in new feature space
342
    def tonpos(citer, coord):
343
        ls = list()
344
345
        for j in tsels[citer]['js']:
            if tcuts[citer][j]['type'] == 'cont':
346
               ls.append(itvpos(coord[j-1], tcuts[citer][j]['cuts']))
347
348
            else:
               ls.append(tcuts[citer][j]['cuts'][coord[j-1]])
349
350
        return tuple(ls)
351
    # Compute new numerical region from given position to new feature space
352
    def tonreg(citer, pos):
353
        pcutn = np.array(tsels[citer]['ps'], dtype=np.int16)
354
        pncum = np.cumprod(np.append([1], pcutn[0:-1]+1), dtype=np.int16)
355
        return np.dot(pncum, pos)
356
357
    dfpn = dfp.copy() # copy of individual result of cplex prediction
358
359
    dfpn = dfpn[dfpn['iter'].isin(tsels.keys())] # exclude iterations of no
        feature selection
360
    nregdc = dict() # new numerical regions in all iterations
361
362 for citer, info in tsels.items():
363
        nregdc[citer] = calregs(pcuto=pcuto,sidx=np.array(info['js'])-1)
```

```
364 dfpn['creg'] = dfpn.apply(lambda x: nregdc[x.iter][x.region], axis=1) #
        new region based on cplex result
365 dfpn['tpred'] = dfpn.apply(lambda x: ttregs[x.iter][x.creg]['classes'],
        axis=1) # true predicted class
366
367 dfc = pd.merge(df, dfpn, how='right', left_on=df.index+1, right_on='id',
        suffixes=('', '_pn')) # include instance
368 del dfc['class_pn']
369 cols = dfc.columns.tolist()
370 new_cols = cols[len(pcuto)+1:len(pcuto)+3] + cols[0:len(pcuto)+1] + cols
        [-4:]
371 dfc = dfc[new_cols]
372 dfc = dfc.rename(columns={'region': 'rreg', 'predict': 'rpred'})
373
374 dfc['coord'] = dfc.iloc[:,2:len(pcuto)+2].apply(lambda x: tuple(x), axis
        =1) # full original coordinate
375 dfc['tpos'] = dfc.apply(lambda x: tonpos(x.iter, x.coord), axis=1) # true
        position in new feature space
376 dfc['treg'] = dfc.apply(lambda x: tonreg(x.iter, x.tpos), axis=1) # true
        decision region
377
378
379 dfcd = dfc[dfc['creg'] != dfc['treg']] # new cplex region differs from new
         true region
380 dfcn = dfcd.groupby('iter').size().reset_index(name='dnum') # number of
        difference
381
    print(f"{dfcn}\n") # display number of difference in region recalculation
382
    print(f"{dfcd}\n") # display difference in new regions
383
384
385 # Export cplex reexamination results
386 dfc.to_csv(f"{outdir}/{outexffile}", header=True, index=False) # full
        cplex reexamination
387 dfcd.to_csv(f"{outdir}/{outexdfile}", header=True, index=False) #
        difference in new decision regions
```

CHAPTER V

RESULTS ON HEALTH INSURANCE

5.1 Training Data

The box classifier proposed in Chapter 4 is illustrated on the sample of size 100 (25 per class) and three preselected features: A_AGE, PEMLR and SS_YN. The variable description and cross tabulation analysis with five bins on a continuous feature is displayed in Table 5.1. Each bin covers at least two different insurance coverage types. Although survey participants are unique, some sample records can be the same in feature and even in target due to initial preselection of features and resultant partial loss of personal information. The sampling result can be seen during Iteration 7 in Table 5.7. This chapter investigates two contributing factors out of three based solely on highest training accuracy.

Table 5.1: Cross tabulation of sample data by preselected variables and health insurance coverage types

Dracalantad Variahla	Insurar	ice Covera	ge Type (Insurance Coverage Type (GRP, DIR, PUB)	PUB)
Valtable	NNN	NNY	NY_	Y1Y	YNN
A_AGE: Age					
Universe: All persons					
(1.917, 18.6]	4	∞	2	0	ಗು
(18.6, 35.2]	10	2	П	4	∞
(35.2, 51.8]	ಬ	\vdash	ಬ	2	ರ
(51.8, 68.4]	1	4	∞	9	2
(68.4, 85.0]	0	ಬ	4	∞	0
PEMLR: Major labor force recode					
Universe: All persons					
0: NIU	4	ಬ	2	0	4
1: Employed - at work	∞	က	7	6	12
2: Employed - absent	0	0	က	1	0
3: Unemployed - on layoff	1	\vdash	0	0	0
4: Unemployed - looking	1	П	1	0	2
5: Not in labor force - retired	0	ಬ	ಬ	6	0
6: Not in labor force - disabled	0	2	П	0	0

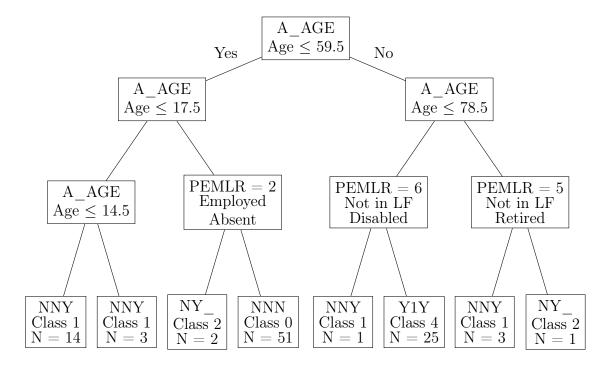
Table 5.1: Cross tabulation of sample data by preselected variables and health insurance coverage types (continued)

NNN NNN 7: Not in labor force - other 6 3	NNY NY_ 3 1			
7: Not in labor force - other 6 3	က		Y1Y	YNN
		1	1	2
SS_YN: Who received social security payments either for themselves or as				
combined payments with other family members?				
Universe: All persons aged 15+				
0: NIU 3 5	ಬ	2	0	4
1: Yes 0 9	6	7 10	0	\vdash
2: No 6	6	11 10	0	15

5.2 Decision Tree

The goal is to find up to two significant determinants of health insurance coverage out of three features namely A_AGE, PEMLR and SS_YN. The first is continuous whereas the last two are categorical. Three splits are assumed in Code 4.1 on an individual feature. Since SS_YN has only three possible values, this feature can have up to two splits. In total, there should be at most (3+1)(3+1)=16 decision boxes. As a result, decision trees of at least depth 3 and at most 16 leaf nodes are considered. Code 5.1 computes the trees of depths 3, 4 and 5 built by the Gini impurity within 5 seconds each as displayed in Figures 5.1, 5.2 and 5.3 respectively. They give training accuracies of 45%, 50% and 54% with 7, 11 and 15 splitting values in total and 8, 12 and 16 decision boxes. The two splits A_AGE = 70.5 and A_AGE = 75 in Figures 5.2 and 5.3 are redundant because both cannot distinguish the classes of training instances in left and right nodes by predicting the same class label 4.

Figure 5.1: Gini-based decision tree with depth 3, 7 non-leaf nodes and 8 leaf nodes giving a training accuracy of 45%



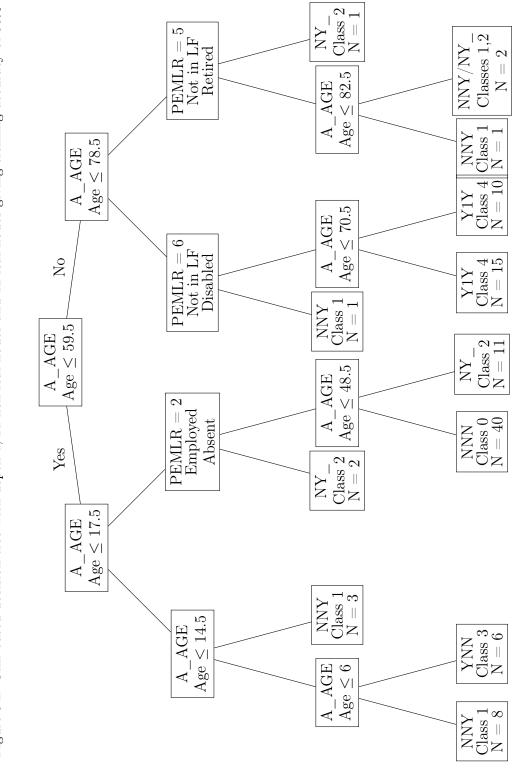


Figure 5.2: Gini-based decision tree with depth 4, 11 non-leaf nodes and 12 leaf nodes giving training accuracy of 50%

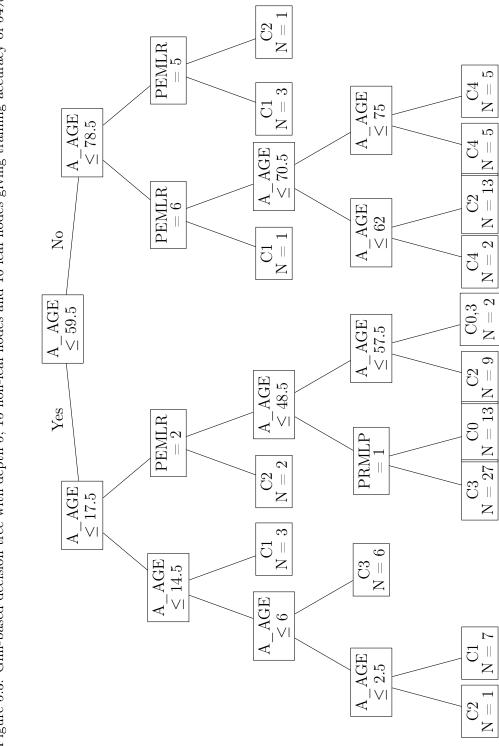


Figure 5.3: Gini-based decision tree with depth 5, 15 non-leaf nodes and 16 leaf nodes giving training accuracy of 54%

Code 5.1: Gini-based decision tree classifier

```
1 import matplotlib.pyplot as plt
2 import pandas as pd
3 import numpy as np
4 import csv
5 import os
  from sklearn.tree import DecisionTreeClassifier, export_text, plot_tree
   def create_dir(dir):
9
       try:
10
          os.makedirs(dir)
11
       except FileExistsError:
12
         pass
13
14 # Given Information
15 data_ls = []
   data_ls.append({
17
       'data': "../../Samples/cplex/seltrain20num3each20.csv",
       'info': "../../Samples/cplex/selproc20num3co3ca3cutinfo.csv",
18
       'configs': [
19
          {'max_depth': 3, 'max_leaves': 16},
20
          {'max_depth': 4, 'max_leaves': 16},
21
          {'max_depth': 5, 'max_leaves': 16}
22
       ],
23
       'outdir': "../../Outputs/Main/Tree"
24
25 })
26 print(f"{data_ls}\n")
27
28 # Decision Tree
29 def dtree(df_data, df_info, max_depth, max_leaves, data_path='', info_path
       =''):
30
31
       # One-hot encoding
```

```
feat_cat = list(df_info[df_info['type'] == 'Categorical']['variable'])
32
       for v in feat_cat:
33
           df_data[v] = df_data[v].astype('category')
34
       one_hot_data = pd.get_dummies(df_data[feat_cat], drop_first=True)
35
36
       X = df_data.iloc[:,0:-(len(feat_cat)+1)].join(one_hot_data)
       y = df_data['class']
37
38
       # Build decision tree
39
       clf = DecisionTreeClassifier(
40
           max_depth=max_depth,
41
42
           max_leaf_nodes=max_leaves,
43
           random_state=0
       )
44
       clf.fit(X, y)
45
46
47
       # Performance
48
       score = clf.score(X, y)
       y_pred = clf.predict(X)
49
       err_ind = (y_pred != y.to_numpy().flatten()).astype(int)
50
51
       error = np.count_nonzero(err_ind)
       accuracy = (1-error/len(y_pred))*100
52
53
54
       # Tree structure
55
       depth = clf.tree_.max_depth
56
       nodes = clf.tree_.node_count
       leaves = clf.tree_.n_leaves
57
       splits = nodes - leaves
58
59
60
       # Decision tree summary
       summary = {
61
           'error': error, 'accuracy': accuracy, 'score': score,
62
63
           'depth': depth,
           'nodes': nodes, 'leaves': leaves, 'splits': splits
64
65
       }
66
       # Decision rules
67
```

```
rules = export_text(clf, feature_names=list(X.columns))
68
69
        # Predicted values
70
        df_pred = pd.DataFrame({
71
            'y_true': df_data['class'],
72.
            'y_pred': y_pred,
73
            'e': err_ind
74
        })
75
76
        # Display results
77
        if data_path != '':
78
79
            print(f"Data: {data_path}")
        if info_path != '':
80
           print(f"Info: {info_path}")
81
        print(f"Maximum depth: {max_depth}")
82
        print(f"Maximum number of leaves: {max_leaves}\n")
83
        print(f"Categorical features: {feat_cat}")
84
        print(f"X: {X.columns.values}\n")
85
        print(f"Summary:")
86
        print(f"\tDepth = {depth} | Leaves = {leaves}")
87
        print(f"\tError = {error} | Accuracy = {accuracy} | Score = {score}")
88
89
        print(f"\tNodes = {nodes} | Splits = {splits}\n")
        print(f"Decision rules:\n{rules}\n")
90
91
92
        # Return statement
93
        return clf, summary, rules, df_pred
94
    # Implementation
95
96 for dc in data_ls:
97
        # Export information
98
99
        datname = os.path.splitext(os.path.basename(dc['data']))[0] # without
           file extension
        outdatdir = f"{dc['outdir']}/{datname}"
100
101
        outprefix = datname
102
        outsumfile = f"{outdatdir}/{outprefix}-summary.csv"
```

```
103
        outruledir = f"{outdatdir}/rules"
104
        outpreddir = f"{outdatdir}/prediction"
105
        outfigdir = f"{outdatdir}/figures"
106
107
        # Import
108
        df_data = pd.read_csv(dc['data'])
        df_info = pd.read_csv(dc['info'])
109
110
111
        # Exported figure formats
        fig_formats = ['svg', 'pgf', 'pdf']
112
113
114
        # Create directories
        create_dir(f"{outdatdir}/rules")
115
        create_dir(f"{outdatdir}/prediction")
116
117
        for format in fig_formats:
            create_dir(f"{outdatdir}/figures/{format}")
118
119
        # Export summary file in CSV format
120
        with open(outsumfile, 'w') as sumfile:
121
122
123
            sumheader = [
124
                'mdepth', 'mleaves', 'depth', 'leaves',
                'error', 'accuracy', 'score',
125
126
                'nodes', 'splits'
127
128
            writer = csv.DictWriter(sumfile, fieldnames=sumheader)
129
            writer.writeheader()
130
131
            for config in dc['configs']:
132
               # Tree configuration
133
134
               mdepth = config['max_depth'] # depth
               mleaves = config['max_leaves'] # number of leaves
135
136
137
               # Postfix of exported files with specific depth and number of
                   leaves
```

```
138
               outpostfix = f"mdepth-{mdepth}-mleaves-{mleaves}"
139
140
               # Decision tree
               clf, summary, rules, df_pred = dtree(
141
142
                   df_data, df_info, mdepth, mleaves,
                   data_path=dc['data'], info_path=dc['info']
143
               )
144
145
146
               # Export summary result to CSV file
               summary['mdepth'] = mdepth
147
               summary['mleaves'] = mleaves
148
149
               writer.writerow(summary)
150
               # Decision rules
151
               with open(f"{outruledir}/{outprefix}-rule-{outpostfix}.txt", 'w
152
                   ') as rulefile:
                   rulefile.write(rules)
153
154
               # Prediction
155
156
               outpredfile = f"{outpreddir}/{outprefix}-pred-{outpostfix}.csv"
               df_pred.index = df_pred.index + 1
157
158
               df_pred.to_csv(outpredfile, index_label='id')
159
160
               # Tree plots
161
               plot_tree(clf)
162
               #plot_tree(clf, label='none', impurity=False)
163
               for format in fig_formats:
164
                   outfigfile = f"{outfigdir}/{format}/{outprefix}-fig-{
                       outpostfix}.{format}"
165
                   plt.savefig(outfigfile, bbox_inches='tight')
               #plt.show()
166
167
               # Newline
168
169
               print()
```

5.3 Proposed Model

A record of an MIP solution returned by a CPLEX solver is counted as an iteration. The proposed box classifier is given within 15 iterations as reported by the solver, or 13 iterations by careful reexamination, before all CPLEX node files fully occupy the reserved disk space of 200 GB where the optimal solution status is inconclusive. As shown in Tables 5.2 and 5.3, the box classifier gives six splitting values in total, three per each contributing factor, whereas all three decision trees at least seven. It achieves a high training accuracy of 51%, compared to the trees of 12 and 16 boxes at 50% and 54%. Although the first requires a significantly longer building time of at least 78.88 minutes (iteration 13) or up to 209.93 minutes (last iteration 15), the latter two output superfluous 11 and 15 total splits. Interestingly, the box classifier and all three decision trees consider A_AGE and PEMLR significant features, and they have consistent, though nonidentical, categorical splitting values on PEMLR. Based on the box classifier, PEMLR = 3, 4, 5 and 7 share similar characteristics, and they are grouped together as a new single unit or splitting value. Another group of PEMLR = 0 and 6 is also generated. Nonetheless, all decision trees lack the capability to bundle similar categorical values.

The training accuracy, the execution time and the minimum storage size of a box classifier per iteration are reported in Table 5.4. Feature selection occurs as of iteration 2. The training accuracy directly reported by a CPLEX solver as the negative of the objective value differs from the true accuracy produced and recomputed by the proposed box classifier based solely on the splitting values during the first 13 iterations. Decision regions predicted by a CPLEX solver is inconsistent with those recomputed until iteration 10. The acceptable box classifier of training accuracy 51% is given since iteration 13 within 78.88 minutes, taking up at least 5.92 GB of disk space but no more than 7 GB, and with a relative MIP gap of 6.35 defined by the relative difference between the best integer objective and the objective of the best CPLEX tree node remaining. The CPLEX engine log can be examined in an appendix.

Groups of values on selected features and their resultant box regions including predicted class labels are shown in Tables 5.5 and 5.6 respectively. Some bins as a result of feature splits may be empty, and their corresponding decision boxes are therefore nonexistent. The dimension of new continuous features in Code 4.1 is one, but iterations 2 to 9 select only categorical features. As a result, splits on the continuous feature A_AGE is redundant, and the number of decision boxes is overly reported by a CPLEX solver. After recalculating numerical decision regions and merging boxes, the difference between CPLEX and true decision regions occurs as illustrated on a per-instance basis in Table 5.7. This is possibly due to the insufficiently small CPLEX feasibility tolerance of 10^{-6} by default. At least 41 training instances suffer from this inconsistency, and all especially in iteration 7. No difference can be detected as of iteration 10.

Table 5.2: Comparison between multiple decision tree of depths 3 to 5 and proposed classifier in iterations 13 to 15 based on number of splitting values, number of decision boxes, training accuracy and execution time

Classification Model	n Model	N	um of Split	Num of Splitting Values		Num of Boxes	Num of Boxes Training Accuracy (%) Execution Time (min)	Execution Time (min)
Model	Specification A_AGE PEMLR SS_YN Total	A_AGE	PEMLR	SS_YN	Total			
Decision tree	Depth of 3	4	က	0	7	∞	45	0.08
	Depth of 4	∞	က	0	11	12	50	
	Depth of 5	12	3	0	15	16	54	
Proposed classifier	Iteration 13	က	3	0	9	16	51	78.88
	Iteration 14	3	က	0	9	16	51	82.02
	Iteration 15	ಣ	က	0	9	16	51	209.93

Table 5.3: Splitting values on features of multiple decision tree of depths 3 to 5 and proposed classifier in iterations 13 to 15

Classification Model	Š	Splitting Values		
Specification	A_AGE	PEMLR	SS_YN	Training Accuracy (%)
	14.5, 17.5, 59.5, 78.5	2, 5, 6	1	45
	6, 14.5, 17.5, 48.5, 59.5, 70.5, 78.5, 82.5	2, 5, 6	I	50
1	2.5, 6, 14.5, 17.5, 48.5, 57.5, 59.5, 62, 70.5, 75, 78.5	2, 5, 6	I	54
1	24.99, 55.99, 64.99	{2}, {1}, {3, 4, 5, 7}, {0, 6}	ı	51
Iterations 14 to 15	24.01, 55.99, 64.99	$\{2\}, \{1\}, \{3,4,5,7\}, \{0,6\}$	I	51

Table 5.4: Training accuracy, execution time, minimum storage usage, relative MIP gap and number of inconsistent data across all iterations

1 0		Accuracy (%)		Execution	Execution Time (min)	Mi	Min Storage (GB)	B)	Rel Gan	Inconsistent
1 6	True	CPLEX	Reported	Each	Accum	Tree	Nodes	Comp	3	
c			20	0	0				279	
71	38	35	28	0.03	0.03				27.57	41
3	38	35	31	0.01	0.04				22.14	41
4	38	35	36	0.01	90.0				17.25	41
ಗು	38	35	38	0.03	0.09				15.5	41
9	40	36	39	13.3	13.39	0.99	0	0	8.67	41
7	40	30	40	5.27	18.66	1.24	0	0	8.42	100
∞	43	40	43	4.64	23.3	2.74	0.49	0.45	7.75	41
6	44	42	44	2.67	30.97	3.68	1.3	1.18	7.54	41
10	47	47	46	37.23	68.2	3.35	1.34	1.19	7.01	
11	48	48	48	1.18	69.38	3.46	1.5	1.32	29.9	
12	20	20	49	7.17	76.55	4.11	1.64	1.45	6.51	
13	51	51	20	2.33	78.88	8.13	5.93	5.17	6.35	
14	51	51	51	3.14	82.02	9.06	7	6.13	6.2	
15	51	51	51	127.91	209.93	192.68	190.58	167.06	80.9	

Table 5.5: Selected variables and groups of values across all iterations

[teration		Selected Variable	iable	Choire.		Member
1001001	Index	Symbol	Type	daga	Index	Label
2	2	PEMLR	Categorical	0	1	Employed - at work
					က	Unemployed - on layoff
					2	Not in labor force - other
				2	ις	Not in labor force - retired
				3	0	NIU
					2	Employed - absent
					4	Unemployed - looking
					9	Not in labor force - disabled
	3	SS_YN	Categorical	0	2	No
				1	1	Yes
				2	0	NIU (aged below 15)
3	2	PEMLR	Categorical	0	1	Employed - at work
					3	Unemployed - on layoff
					7	Not in labor force - other
				2	ಬ	Not in labor force - retired
				3	0	NIU

Table 5.5: Selected variables and groups of values across all iterations (continued)

Iteration		Selected Variable	iable	Crono		Member
	Index	Symbol	Type	drogo	Index	Label
					2	Employed - absent
					4	Unemployed - looking
					9	Not in labor force - disabled
	က	SS_YN	Categorical	0	2	ON
				1	1	Yes
				2	0	NIU (aged below 15)
4	2	PEMLR	Categorical	0	1	Employed - at work
					3	Unemployed - on layoff
					2	Not in labor force - other
				2	വ	Not in labor force - retired
				3	0	NIU
					2	Employed - absent
					4	Unemployed - looking
					9	Not in labor force - disabled
	33	SS_YN	Categorical	0	2	No
				П	1	Yes

Table 5.5: Selected variables and groups of values across all iterations (continued)

			-			
Iteration		Selected Variable	riable	Group		Member
	Index	Symbol	Type	T	Index	Label
				2	0	NIU (aged below 15)
5	2	PEMLR	Categorical	0	1	Employed - at work
					3	Unemployed - on layoff
					7	Not in labor force - other
				2	v	Not in labor force - retired
				က	0	NIU
					2	Employed - absent
					4	Unemployed - looking
					9	Not in labor force - disabled
	3	SS_YN	Categorical	0	2	O'N
				Н	1	Yes
				2	0	NIU (aged below 15)
9	2	PEMLR	Categorical	0	1	Employed - at work
					3	Unemployed - on layoff
					2	Not in labor force - other
					2	Employed - absent

Table 5.5: Selected variables and groups of values across all iterations (continued)

Iteration		Selected Variable	iable	(Froit)	$ m M\epsilon$	Member
	Index	Symbol	Type	J. C.	Index	Label
				2	ಗು	Not in labor force - retired
				3	0	NIU
					4	Unemployed - looking
					9	Not in labor force - disabled
	3	SS_YN	Categorical	0	2	$ m N_{0}$
				1	1	Yes
				2	0	NIU (aged below 15)
2	2	PEMLR	Categorical	0	1	Employed - at work
					2	Employed - absent
					4	Unemployed - looking
				2	0	NIU
					3	Unemployed - on layoff
					9	Not in labor force - disabled
					-1	Not in labor force - other
				3	22	Not in labor force - retired
	က	$^{ m SS}$	Categorical	1	0	NIU (aged below 15)

Table 5.5: Selected variables and groups of values across all iterations (continued)

Iteration		Selected Variable	riable	Group		Member
	Index	Symbol	Type	dron	Index	Label
					2	m No
				2	1	Yes
∞	2	PEMLR	Categorical	0	2	Employed - absent
				1	1	Employed - at work
					9	Not in labor force - disabled
				2	0	NIU
					3	Unemployed - on layoff
					4	Unemployed - looking
					7	Not in labor force - other
				3	ಬ	Not in labor force - retired
	3	SS_YN	Categorical	0	2	No
				2	0	NIU (aged below 15)
					1	Yes
6	2	PEMLR	Categorical	0	2	Employed - absent
				1	П	Employed - at work
				2	0	NIU

Table 5.5: Selected variables and groups of values across all iterations (continued)

Iteration		Selected Variable	iable	ano.		Member
	Index	Symbol	Type	droin	Index	Label
					က	Unemployed - on layoff
					4	Unemployed - looking
					9	Not in labor force - disabled
					2	Not in labor force - other
				က	က	Not in labor force - retired
	က	SS_YN	Categorical	0	2	No
				2	0	NIU (aged below 15)
					1	Yes
10	1	A_AGE	Continuous	0	$(-\infty, 24.01)$	Below 24
				1	(24.01, 40.99)	Between 25 and 40
				2	(40.99, 65.99)	Between 41 and 65
				3	$(65.99,\infty)$	Above 66
	23	PEMLR	Categorical	0	2	Employed - absent
				П	1	Employed - at work
					1-	Not in labor force - other
				2	4	Unemployed - looking

Table 5.5: Selected variables and groups of values across all iterations (continued)

 [teration		Selected Variable	iable	Group		Member
	Index	Symbol	Type	J _S	Index	Label
					ಗು	Not in labor force - retired
				3	0	NIU
					3	Unemployed - on layoff
					9	Not in labor force - disabled
11	1	A_AGE	Continuous	0	$(-\infty, 24.01)$	Below 24
				П	(24.01, 40.99)	Between 25 and 40
				2	(40.99, 64.99)	Between 41 and 64
				3	$(64.99,\infty)$	Above 65
	7	PEMLR	Categorical	0	2	Employed - absent
				1	1	Employed - at work
					1-	Not in labor force - other
				2	4	Unemployed - looking
					ာင္	Not in labor force - retired
				3	0	NIU
					9	Unemployed - on layoff
					9	Not in labor force - disabled

Table 5.5: Selected variables and groups of values across all iterations (continued)

Iteration		Selected Variable	iable	d.roin		Member
	Index	Symbol	Type		Index	Label
12	1	A_AGE	Continuous	0	$(-\infty, 24.99)$	Below 24
				1	(24.99, 40.01)	Between 25 and 40
				2	(40.00, 64.01)	Between 41 and 64
				က	$(64.01,\infty)$	Above 65
	2	PEMLR	Categorical	0	2	Employed - absent
				1	1	Employed - at work
				2	4	Unemployed - looking
					က	Not in labor force - retired
					2	Not in labor force - other
				က	0	NIU
					3	Unemployed - on layoff
					9	Not in labor force - disabled
13	1	A_AGE	Continuous	0	$(-\infty, 24.99)$	Below 24
				1	(24.99, 55.99)	Between 25 and 55
				2	(55.99, 64.99)	Between 56 and 64
				က	$(64.99,\infty)$	Above 65

Table 5.5: Selected variables and groups of values across all iterations (continued)

T+ cuc +1		Selected Variable	iable			Member
iver actori	Index	Symbol	Type	diono	Index	Label
	2	PEMLR	Categorical	0	2	Employed - absent
				1	1	Employed - at work
				2	က	Unemployed - on layoff
					4	Unemployed - looking
					ιO	Not in labor force - retired
					7	Not in labor force - other
				8	0	NIU
					9	Not in labor force - disabled
14	1	A_AGE	Continuous	0	$(-\infty, 24.01)$	Below 24
				1	(24.01, 55.99)	Between 25 and 55
				2	(55.99, 64.99)	Between 56 and 64
				က	$(64.99,\infty)$	Above 65
	2	PEMLR	Categorical	0	2	Employed - absent
				1	1	Employed - at work
				2	3	Unemployed - on layoff
					4	Unemployed - looking

Table 5.5: Selected variables and groups of values across all iterations (continued)

Iteration		Selected Variable	iable	Group		Member
	Index	Symbol	Type	5	Index	Label
					ಗು	Not in labor force - retired
					1~	Not in labor force - other
				3	0	NIU
					9	Not in labor force - disabled
15	1	A_AGE	Continuous	0	$(-\infty, 24.01)$	Below 24
				П	(24.01, 55.99)	Between 25 and 55
				2	(55.99, 64.99)	Between 56 and 64
				33	$(64.99,\infty)$	Above 65
	2	PEMLR	Categorical	0	2	Employed - absent
				1	1	Employed - at work
				2	3	Unemployed - on layoff
					4	Unemployed - looking
					rĊ	Not in labor force - retired
					!~	Not in labor force - other
				33	0	NIU
					9	Not in labor force - disabled

Table 5.6: Decision regions and predicted class labels across all iterations

Iter	Sele	Selected Variables		Deci	Decision Region		Predicted Classes	ai
Tool	Tuple	Symbol	Ind	Tuple	Cross Product	lnd	Label	Main
2	(2,3)	PEMLR, SS_YN	0	(0,0)	$\{1, 3, 7\} \times \{2\}$	0	NNN	48
			1	(1,0)	$\emptyset \times \{2\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			2	(2,0)	$\{5\} \times \{2\}$	2	$^{\rm NY}$	3
			3	(3,0)	$\{0,2,4,6\}\times\{2\}$	2	$^{\rm NY}$	∞
			4	(0,1)	$\{1,3,7\} \times \{1\}$	2,4	$NY_{-}, Y1Y$	9
			ಬ	(1,1)	$\emptyset \times \{1\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			9	(2,1)	$\{5\} \times \{1\}$	4	Y1Y	16
			7	(3,1)	$\{0,2,4,6\}\times\{1\}$	1	NNY	ಬ
			∞	(0,2)	$\{1,3,7\} \times \{0\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			6	(1,2)	$\emptyset \times \{0\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			10	(2,2)	$\{5\} \times \{0\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			11	(3,2)	$\{0,2,4,6\}\times\{0\}$	1	NNY	14
က	(2,3)	$PEMLR, SS_YN$	0	(0,0)	$\{1, 3, 7\} \times \{2\}$	0	NNN	48
				(1,0)	$\emptyset \times \{2\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			2	(2,0)	$\{5\} \times \{2\}$	2	$^{\rm NY}$	က
			င	(3,0)	$\{0,2,4,6\}\times\{2\}$	2	$^{ m NY}$	∞

Table 5.6: Decision regions and predicted class labels across all iterations (continued)

	Sele	Selected Variables		Decis	Decision Region		Predicted Classes	
	Tuple	Symbol	Ind	Tuple	Cross Product	lnd	Label	Num
1			4	(0,1)	$\{1,3,7\} \times \{1\}$	2,4	NY_, Y1Y	9
			ಬ	(1,1)	$\emptyset \times \{1\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			9	(2,1)	$\{5\} \times \{1\}$	4	Y1Y	16
			7	(3,1)	$\{0,2,4,6\}\times\{1\}$	1	NNY	ರ
			∞	(0,2)	$\{1,3,7\} \times \{0\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			6	(1,2)	$\emptyset \times \{0\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			10	(2,2)	$\{5\} \times \{0\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			11	(3,2)	$\{0,2,4,6\}\times\{0\}$	П	NNY	14
	(2,3)	PEMLR, SS_YN	0	(0,0)	$\{1, 3, 7\} \times \{2\}$	0	NNN	48
			\vdash	(1,0)	$\emptyset \times \{2\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			2	(2,0)	$\{5\} \times \{2\}$	2	$^{\rm NY}$	3
			က	(3,0)	$\{0, 2, 4, 6\} \times \{2\}$	2	$^{\rm NY}_{-}$	∞
			4	(0,1)	$\{1,3,7\} \times \{1\}$	2,4	NY, Y1Y	9
			ಬ	(1,1)	$\emptyset \times \{1\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			9	(2,1)	$\{5\}\times\{1\}$	4	Y1Y	16
			7	(3,1)	$\{0,2,4,6\}\times\{1\}$	1	NNY	ಬ

Table 5.6: Decision regions and predicted class labels across all iterations (continued)

140	Sel	Selected Variables		Deci	Decision Region		Predicted Classes	N.:.N
1991	Tuple	Symbol	Ind	Tuple	Cross Product	lnd	Label	TACITI
			∞	(0,2)	$\{1,3,7\} \times \{0\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			6	(1,2)	$\emptyset \times \{0\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			10	(2,2)	$\{5\} \times \{0\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			11	(3,2)	$\{0,2,4,6\}\times\{0\}$	1	NNY	14
ಬ	(2,3)	PEMLR, SS_YN	0	(0,0)	$\{1,3,7\} \times \{2\}$	0	NNN	48
			\vdash	(1,0)	$\emptyset \times \{2\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			2	(2,0)	$\{5\} \times \{2\}$	2	$^{\rm NY}$	က
			က	(3,0)	$\{0,2,4,6\}\times\{2\}$	2	$^{\rm NY}$	∞
			4	(0,1)	$\{1,3,7\} \times \{1\}$	2,4	$NY_{-}, Y1Y$	9
			ಬ	(1,1)	$\emptyset imes \{1\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			9	(2,1)	$\{5\} \times \{1\}$	4	Y1Y	16
			7	(3,1)	$\{0,2,4,6\}\times\{1\}$	П	NNY	20
			∞	(0,2)	$\{1,3,7\} \times \{0\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			6	(1,2)	$\emptyset \times \{0\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			10	(2,2)	$\{5\} \times \{0\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			11	(3,2)	$\{0, 2, 4, 6\} \times \{0\}$	1	NNY	14

Table 5.6: Decision regions and predicted class labels across all iterations (continued)

Iter	Sel_{ϵ}	Selected Variables		Decis	Decision Region		Predicted Classes	Nım
1001	Tuple	Symbol	Ind	Tuple	Cross Product	lnd	Label	
9	(2,3)	PEMLR, SS_YN	0	(0,0)	$\{1,3,7\} \times \{2\}$	0	NNN	48
			1	(1,0)	$\{2\} \times \{2\}$	2	$^{\rm NY}_{-}$	က
			2	(2,0)	$\{5\} \times \{2\}$	2	$^{\rm NY}$	3
			3	(3,0)	$\{0,4,6\} \times \{2\}$	0,3	NNN, YNN	ಬ
			4	(0,1)	$\{1,3,7\} \times \{1\}$	2,4	NY, Y1Y	9
			ಬ	(1,1)	$\{2\} \times \{1\}$	2	$^{\rm NY}$	\Box
			9	(2,1)	$\{5\}\times\{1\}$	4	Y1Y	16
			7	(3,1)	$\{0,4,6\} \times \{1\}$	1	NNY	4
			∞	(0,2)	$\{1,3,7\} \times \{0\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			6	(1,2)	$\{2\} \times \{0\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			10	(2,2)	$\{5\} \times \{0\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			11	(3,2)	$\{0,4,6\} \times \{0\}$	1	NNY	14
2	(2,3)	$PEMLR, SS_YN$	0	(0,0)	$\{1,2,4\}\times\emptyset$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			П	(1,0)	$\emptyset \times \emptyset$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			2	(2,0)	$\{0,3,6,7\}\times\emptyset$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			က	(3,0)	$\{5\}\times\emptyset$	0,1,2,3,4	NNN , NNY , NY_{-} , YNN , $Y1Y$	0

Table 5.6: Decision regions and predicted class labels across all iterations (continued)

Tter	Sele	Selected Variables		Deci	Decision Region		Predicted Classes	Niin
	Tuple	Symbol	Ind	Tuple	Cross Product	Ind	Label	
			4	(0,1)	$\{1,2,4\}\times\{0,2\}$	က	YNN	42
			ಬ	(1,1)	$\emptyset \times \{0,2\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			9	(2,1)	$\{0,3,6,7\}\times\{0,2\}$	0	NNN	28
			7	(3,1)	$\{5\}\times\{0,2\}$	2	$^{\rm NY}_{-}$	3
			∞	(0,2)	$\{1,2,4\} \times \{1\}$	2	$^{\rm NY}$	9
			6	(1,2)	$\emptyset \times \{1\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			10	(2,2)	$\{0,3,6,7\}\times\{1\}$	1	NNY	ഹ
			11	(3,2)	$\{5\} \times \{1\}$	4	Y1Y	16
∞	(2,3)	PEMLR, SS_YN	0	(0,0)	$\{2\} \times \{2\}$	2	$^{-}\mathrm{NY}^{-}$	3
			1	(1,0)	$\{1,6\}\times\{2\}$	3	YNN	35
			2	(2,0)	$\{0,3,4,7\} \times \{2\}$	0	NNN	18
			3	(3,0)	$\{5\} \times \{2\}$	2	NY	3
			4	(0,1)	$\{2\}\times\emptyset$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			ರ	(1,1)	$\{1,6\}\times\emptyset$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			9	(2,1)	$\{0,3,4,7\}\times\emptyset$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			_	(3,1)	$\{5\} \times \emptyset$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0

Table 5.6: Decision regions and predicted class labels across all iterations (continued)

1+01	Sele	Selected Variables		Dec	Decision Region		Predicted Classes	N.i.m
1001	Tuple	Symbol	Ind	Tuple	Cross Product	Ind	Label	III
			∞	(0,2)	$\{2\} \times \{0,1\}$	2	NY_{-}	1
			6	(1,2)	$\{1,6\} imes \{0,1\}$	7	$^{\rm NY}$	7
			10	(2,2)	$\{0,3,4,7\}\times\{0,1\}$	1	NNY	17
			11	(3,2)	$\{5\}\times\{0,1\}$	4	Y1Y	16
6	(2,3)	PEMLR, SS_YN	0	(0,0)	$\{2\} \times \{2\}$	2	NY_{-}	က
			\vdash	(1,0)	$\{1\} \times \{2\}$	က	YNN	35
			2	(2,0)	$\{0,3,4,6,7\} \times \{2\}$	0	NNN	18
			3	(3,0)	$\{5\} \times \{2\}$	7	$^{\rm NY}$	3
			4	(0,1)	$\{2\} \times \emptyset$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			ಬ	(1,1)	$\{1\} \times \emptyset$	0,1,2,3,4	NNN , NNY , NY_{-} , YNN , $Y1Y$	0
			9	(2,1)	$\{0,3,4,6,7\}\times\emptyset$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			7	(3,1)	$\{5\} \times \emptyset$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			∞	(0,2)	$\{2\} \times \{0,1\}$	7	$^{\rm NY}$	П
			6	(1,2)	$\{1\} \times \{0,1\}$	7	$^{\rm NY}$	4
			10	(2,2)	$\{0,3,4,6,7\}\times\{0,1\}$	1	NNY	20
			11	(3,2)	$\{5\}\times\{0,1\}$	4	Y1Y	16

Table 5.6: Decision regions and predicted class labels across all iterations (continued)

Tuple Symbol Ind Tuple Cross Product $(1,2) A_{-}AGE, PEMLR 0 (0,0) (-\infty, 24.01) \times \{2\} \\ 1 (1,0) (24.01, 40.99) \times \{2\} \\ 2 (2,0) (40.99, 65.99) \times \{2\} \\ 3 (3,0) (65.99, \infty) \times \{2\} \\ 4 (0,1) (-\infty, 24.01) \times \{1,7\} \\ 5 (1,1) (24.01, 40.99) \times \{1,7\} \\ 6 (2,1) (40.99, 65.99) \times \{1,7\} \\ 7 (3,1) (65.99, \infty) \times \{1,7\} \\ 8 (0,2) (-\infty, 24.01) \times \{4,5\} \\ 9 (1,2) (24.01, 40.99) \times \{4,5\} \\ 10 (2,2) (40.99, 65.99) \times \{4,5\} \\ 11 (3,2) (65.99, \infty) \times \{4,5\} \\ 12 (0,3) (-\infty, 24.01) \times \{0,3,6\} \\ 13 (1,3) (24.01, 40.99) \times \{0,3,6\} \\ 14 (2,3) (65.99, \infty) \times \{0,3,6\} \\ 15 (3,3) (65.99, \infty) \times \{0,3,6\} \\ 15 (3,3) (65.99, \infty) \times \{0,3,6\} \\ 15 (3,3) (65.99, \infty) \times \{0,3,6\} \\ 16 (3,3) (65.99, \infty) \times \{0,3,6\} \\ 17 (3,3) (65.99, \infty) \times \{0,3,6\} \\ 18 (1,3) (24.01, 40.99) \times \{0,3,6\} \\ 19 (1,2) (24.01, 40.99) \times \{0,3,6\} \\ 11 (2,3) (40.99, 65.99) \times \{0,3,6\} \\ 12 (3,3) (65.99, \infty) \times \{0,3,6\} \\ 13 (1,3) (65.99, \infty) \times \{0,3,6\} \\ 14 (2,3) (65.99, \infty) \times \{0,3,6\} \\ 15 (3,3) (65.99, \infty) \times \{0,3,6\} \\ 16 (3,3) (65.99, \infty) \times \{0,3,6\} \\ 17 (3,3) (65.99, \infty) \times \{0,3,6\} \\ 18 (1,3) (24.01, 40.99) \times \{0,3,6\} \\ 19 (1,2) (24.01, 40.99) \times \{0,3,6\} \\ 10 (25.90, \infty) \times \{0,3,6\} \\ 11 (25.90, \infty) \times \{0,3,6\} \\ 12 (25.90, \infty) \times \{0,3,6\} \\ 13 (24.01, 40.99) \times \{0,3,6\} \\ 14 (25.90, \infty) \times \{0,3,6\} \\ 15 (3.30, \infty) (65.99, \infty) \times \{0,3,6\} \\ 16 (3.30, \infty) (65.99, \infty) \times \{0,3,6\} \\ 17 (3.30, \infty) (65.99, \infty) \times \{0,3,6\} \\ 18 (1,3) (24.01, 40.99) \times \{0,3,6\} \\ 19 (1,3) (24.01, 40.99) \times \{0,3,6\} \\ 19 (1,3) (24.01, 40.99) \times \{0,3,6\} \\ 19 (1,3,0) (24.01, 40.99) \times \{0,3,6\} \\ 11 (24.01, 40.99, 65.99) \times \{0,3,6\} \\ 12 (34.01, 40.99, 65.99) \times \{0,3,6\} \\ 13 (1,3) (24.01, 40.99, 60.3,6\} \\ 14 (24.01, 40.99, 60.3,6\} \\ 15 (24.01, 40.99, 60.3,6\} \\ 16 (24.01, 40.99, 60.3,6\} \\ 17 (24.01, 40.99, 60.3,6\} \\ 18 (24.01, 40.99, 60.3,6\} \\ 18 (24.01, 40.99, 60.3,6) \\ 18 (24.01, 40.99, 60.3,6) \\ 18 (24.01, 40.99, 60.3,6) \\ 18 (24.01, 40.99, 60.3,6) \\ 18 (24.01, 40.99, 60.3,6) \\ 18 (24.01,$		Sele	Selected Variables		De	Decision Region		Predicted Classes	%::N
(1,2) $A_{-}AGE, PEMLR$ 0 (0,0) $(-\infty, 24.01) \times \{2\}$ 1 (1,0) $(24.01, 40.99) \times \{2\}$ 2 (2,0) $(40.99, 65.99) \times \{2\}$ 3 (3,0) $(65.99, \infty) \times \{2\}$ 4 (0,1) $(-\infty, 24.01) \times \{1,7\}$ 5 (1,1) $(24.01, 40.99) \times \{1,7\}$ 6 (2,1) $(40.99, 65.99) \times \{1,7\}$ 7 (3,1) $(65.99, \infty) \times \{1,7\}$ 8 (0,2) $(-\infty, 24.01) \times \{4,5\}$ 9 (1,2) $(24.01, 40.99) \times \{4,5\}$ 10 (2,2) $(40.99, 65.99) \times \{4,5\}$ 11 (3,2) $(65.99, \infty) \times \{4,5\}$ 12 (0,3) $(-\infty, 24.01) \times \{0,3,6\}$ 13 (1,3) $(24.01, 40.99) \times \{0,3,6\}$ 14 (2,3) $(65.99, \infty) \times \{0,3,6\}$ 15 (3,3) $(65.99, \infty) \times \{0,3,6\}$	Ieu	Tuple	Symbol	Ind	Tuple	Cross Product	puI	Label	IIIIII
$(1,0) \qquad (24.01, 40.99) \times \{2\}$ $(2,0) \qquad (40.99, 65.99) \times \{2\}$ $(3,0) \qquad (65.99, \infty) \times \{2\}$ $(0,1) \qquad (-\infty, 24.01) \times \{1, 7\}$ $(1,1) \qquad (24.01, 40.99) \times \{1, 7\}$ $(2,1) \qquad (40.99, 65.99) \times \{1, 7\}$ $(0,2) \qquad (-\infty, 24.01) \times \{4, 5\}$ $(1,2) \qquad (24.01, 40.99) \times \{4, 5\}$ $(2,2) \qquad (40.99, 65.99) \times \{4, 5\}$ $(2,2) \qquad (40.99, 65.99) \times \{4, 5\}$ $(3,2) \qquad (65.99, \infty) \times \{4, 5\}$ $(0,3) \qquad (-\infty, 24.01) \times \{0, 3, 6\}$ $(1,3) \qquad (24.01, 40.99) \times \{0, 3, 6\}$ $(1,3) \qquad (24.01, 40.99) \times \{0, 3, 6\}$ $(2,3) \qquad (65.99, \infty) \times \{0, 3, 6\}$ $(3,3) \qquad (65.99, \infty) \times \{0, 3, 6\}$	10	(1,2)	A_AGE, PEMLR	0	(0,0)	$(-\infty,24.01)\times\{2\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
$(2,0) \qquad (40.99, 65.99) \times \{2\}$ $(3,0) \qquad (65.99, \infty) \times \{2\}$ $(0,1) \qquad (-\infty, 24.01) \times \{1,7\}$ $(1,1) \qquad (24.01, 40.99) \times \{1,7\}$ $(2,1) \qquad (40.99, 65.99) \times \{1,7\}$ $(3,1) \qquad (65.99, \infty) \times \{1,7\}$ $(1,2) \qquad (-\infty, 24.01) \times \{4,5\}$ $(1,2) \qquad (24.01, 40.99) \times \{4,5\}$ $(2,2) \qquad (40.99, 65.99) \times \{4,5\}$ $(3,2) \qquad (65.99, \infty) \times \{4,5\}$ $(0,3) \qquad (-\infty, 24.01) \times \{0,3,6\}$ $(1,3) \qquad (24.01, 40.99) \times \{0,3,6\}$ $(2,3) \qquad (40.99, 65.99) \times \{0,3,6\}$ $(3,3) \qquad (65.99, \infty) \times \{0,3,6\}$				П	(1,0)	$(24.01, 40.99) \times \{2\}$	2	$^{ m NY}$	2
$(3,0) \qquad (65.99,\infty) \times \{2\}$ $(0,1) \qquad (-\infty, 24.01) \times \{1,7\}$ $(1,1) \qquad (24.01, 40.99) \times \{1,7\}$ $(2,1) \qquad (40.99, 65.99) \times \{1,7\}$ $(3,1) \qquad (65.99,\infty) \times \{1,7\}$ $(0,2) \qquad (-\infty, 24.01) \times \{4,5\}$ $(1,2) \qquad (24.01, 40.99) \times \{4,5\}$ $(2,2) \qquad (40.99, 65.99) \times \{4,5\}$ $(3,2) \qquad (65.99,\infty) \times \{4,5\}$ $(0,3) \qquad (-\infty, 24.01) \times \{0,3,6\}$ $(1,3) \qquad (24.01, 40.99) \times \{0,3,6\}$ $(1,3) \qquad (24.01, 40.99) \times \{0,3,6\}$ $(2,3) \qquad (65.99,\infty) \times \{0,3,6\}$ $(3,3) \qquad (65.99,\infty) \times \{0,3,6\}$				2	(2,0)	$(40.99, 65.99) \times \{2\}$	4	Y1Y	П
$(0,1) \qquad (-\infty, 24.01) \times \{1,7\}$ $(1,1) \qquad (24.01, 40.99) \times \{1,7\}$ $(2,1) \qquad (40.99, 65.99) \times \{1,7\}$ $(3,1) \qquad (65.99, \infty) \times \{1,7\}$ $(0,2) \qquad (-\infty, 24.01) \times \{4,5\}$ $(1,2) \qquad (24.01, 40.99) \times \{4,5\}$ $(2,2) \qquad (40.99, 65.99) \times \{4,5\}$ $(3,2) \qquad (65.99, \infty) \times \{4,5\}$ $(0,3) \qquad (-\infty, 24.01) \times \{0,3,6\}$ $(1,3) \qquad (24.01, 40.99) \times \{0,3,6\}$ $(2,3) \qquad (40.99, 65.99) \times \{0,3,6\}$ $(3,3) \qquad (65.99, \infty) \times \{0,3,6\}$				3	(3,0)	$(65.99,\infty)\times\{2\}$	2	$^{ m NY}$	1
$(1,1) \qquad (24.01, 40.99) \times \{1, 7\}$ $(2,1) \qquad (40.99, 65.99) \times \{1, 7\}$ $(3,1) \qquad (65.99, \infty) \times \{1, 7\}$ $(0,2) \qquad (-\infty, 24.01) \times \{4, 5\}$ $(1,2) \qquad (24.01, 40.99) \times \{4, 5\}$ $(2,2) \qquad (40.99, 65.99) \times \{4, 5\}$ $(3,2) \qquad (65.99, \infty) \times \{4, 5\}$ $(0,3) \qquad (-\infty, 24.01) \times \{0, 3, 6\}$ $(1,3) \qquad (24.01, 40.99) \times \{0, 3, 6\}$ $(2,3) \qquad (40.99, 65.99) \times \{0, 3, 6\}$ $(2,3) \qquad (65.99, \infty) \times \{0, 3, 6\}$ $(3,3) \qquad (65.99, \infty) \times \{0, 3, 6\}$				4	(0,1)	$(-\infty, 24.01) \times \{1, 7\}$	0	NNN	11
$(2,1) \qquad (40.99, 65.99) \times \{1, 7\}$ $(3,1) \qquad (65.99, \infty) \times \{1, 7\}$ $(0,2) \qquad (-\infty, 24.01) \times \{4, 5\}$ $(1,2) \qquad (24.01, 40.99) \times \{4, 5\}$ $(2,2) \qquad (40.99, 65.99) \times \{4, 5\}$ $(3,2) \qquad (65.99, \infty) \times \{4, 5\}$ $(0,3) \qquad (-\infty, 24.01) \times \{0, 3, 6\}$ $(1,3) \qquad (24.01, 40.99) \times \{0, 3, 6\}$ $(2,3) \qquad (40.99, 65.99) \times \{0, 3, 6\}$ $(3,3) \qquad (65.99, \infty) \times \{0, 3, 6\}$				\mathcal{D}	(1,1)	$(24.01, 40.99) \times \{1, 7\}$	33	YNN	17
$(3,1)$ $(65.99,\infty) \times \{1,7\}$ $(0,2)$ $(-\infty,24.01) \times \{4,5\}$ $(1,2)$ $(24.01,40.99) \times \{4,5\}$ $(2,2)$ $(40.99,65.99) \times \{4,5\}$ $(3,2)$ $(65.99,\infty) \times \{4,5\}$ $(0,3)$ $(-\infty,24.01) \times \{0,3,6\}$ $(1,3)$ $(24.01,40.99) \times \{0,3,6\}$ $(2,3)$ $(65.99,\infty) \times \{0,3,6\}$ $(3,3)$ $(65.99,\infty) \times \{0,3,6\}$				9	(2,1)	$(40.99, 65.99) \times \{1, 7\}$	3	YNN	20
$(0,2) \qquad (-\infty, 24.01) \times \{4, 5\}$ $(1,2) \qquad (24.01, 40.99) \times \{4, 5\}$ $(2,2) \qquad (40.99, 65.99) \times \{4, 5\}$ $(3,2) \qquad (65.99, \infty) \times \{4, 5\}$ $(0,3) \qquad (-\infty, 24.01) \times \{0, 3, 6\}$ $(1,3) \qquad (24.01, 40.99) \times \{0, 3, 6\}$ $(2,3) \qquad (40.99, 65.99) \times \{0, 3, 6\}$ $(3,3) \qquad (65.99, \infty) \times \{0, 3, 6\}$				7	(3,1)	$(65.99,\infty)\times\{1,7\}$	2,4	NY, Y1Y	4
$(1,2)$ $(24.01, 40.99) \times \{4, 5\}$ $(2,2)$ $(40.99, 65.99) \times \{4, 5\}$ $(3,2)$ $(65.99, \infty) \times \{4, 5\}$ $(0,3)$ $(-\infty, 24.01) \times \{0, 3, 6\}$ $(1,3)$ $(24.01, 40.99) \times \{0, 3, 6\}$ $(2,3)$ $(40.99, 65.99) \times \{0, 3, 6\}$ $(3,3)$ $(65.99, \infty) \times \{0, 3, 6\}$				∞	(0,2)	$(-\infty, 24.01) \times \{4, 5\}$	1,3	NNY, YNN	2
$(2,2) \qquad (40.99, 65.99) \times \{4, 5\}$ $(3,2) \qquad (65.99, \infty) \times \{4, 5\}$ $(0,3) \qquad (-\infty, 24.01) \times \{0, 3, 6\}$ $(1,3) \qquad (24.01, 40.99) \times \{0, 3, 6\}$ $(2,3) \qquad (40.99, 65.99) \times \{0, 3, 6\}$ $(3,3) \qquad (65.99, \infty) \times \{0, 3, 6\}$				6	(1,2)	$(24.01, 40.99) \times \{4, 5\}$	0,3	NNN, YNN	2
(3,2) (0,3) (1,3) (2,3) (3,3)				10	(2,2)	$(40.99,65.99)\times\{4,5\}$	2	$^{ m NY}$	4
(0,3) (1,3) (2,3) (3,3)				111	(3,2)	$(65.99,\infty)\times\{4,5\}$	4	Y1Y	16
(1,3) (2,3) (3,3)				12	(0,3)	$(-\infty, 24.01) \times \{0, 3, 6\}$	\vdash	NNY	15
(2,3)				13	(1,3)	$(24.01, 40.99) \times \{0, 3, 6\}$	0	NNN	1
(3,3)				14	(2,3)	$(40.99,65.99)\times\{0,3,6\}$	\vdash	NNY	က
(-/-)				15	(3,3)	$(65.99,\infty) \times \{0,3,6\}$	1	NNY	1

Table 5.6: Decision regions and predicted class labels across all iterations (continued)

Iter	Sel	Selected Variables		De	Decision Region		Predicted Classes	Nim
	Tuple	Symbol	Ind	Tuple	Cross Product	puI	Label	
11	(1,2)	A_AGE, PEMLR	0	(0,0)	$(-\infty, 24.01) \times \{2\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			\vdash	(1,0)	$(24.01, 40.99) \times \{2\}$	23	$^{\rm NY}$	2
			2	(2,0)	$(40.99, 64.99) \times \{2\}$	4	Y1Y	П
			3	(3,0)	$(64.99,\infty)\times\{2\}$	23	NY	П
			4	(0,1)	$(-\infty, 24.01) \times \{1, 7\}$	0	NNN	11
			5	(1,1)	$(24.01, 40.99) \times \{1, 7\}$	က	γ NN	17
			9	(2,1)	$(40.99, 64.99) \times \{1, 7\}$	33	γ NN	18
			2	(3,1)	$(64.99,\infty)\times\{1,7\}$	2,4	NY, Y1Y	9
			∞	(0,2)	$(-\infty, 24.01) \times \{4, 5\}$	1,3	NNY, YNN	2
			6	(1,2)	$(24.01, 40.99) \times \{4, 5\}$	0,3	NNN, YNN	2
			10	(2,2)	$(40.99, 64.99) \times \{4, 5\}$	2	$^{ m NY}$	4
			11	(3,2)	$(64.99,\infty)\times\{4,5\}$	4	Y1Y	16
			12	(0,3)	$(-\infty, 24.01) \times \{0, 3, 6\}$	1	NNY	15
			13	(1,3)	$(24.01, 40.99) \times \{0, 3, 6\}$	0	NNN	П
			14	(2,3)	$(40.99,64.99)\times\{0,3,6\}$	1	NNY	33
			15	(3,3)	$(64.99, \infty) \times \{0, 3, 6\}$	П	NNY	1

Table 5.6: Decision regions and predicted class labels across all iterations (continued)

Nim		0	2	\leftarrow	\vdash	7	14	13	ಬ	9	ಬ	6	17	15	\vdash	က	-
Predicted Classes	Label	NNN, NNY, NY_, YNN, Y1Y	$^{\rm NY}$	Y1Y	$^{\rm NY}$	NNN	YNN	YNN	$^{ m NY}$	NNY	NNN	$^{ m NY}_{-}$	Y1Y	NNY	NNN	NNY	NNY
	Ind	0,1,2,3,4	2	4	2	0	လ	33	7	1	0	7	4	1	0	1	H
Decision Region	Cross Product	$(-\infty, 24.99) \times \{2\}$	$(24.99, 40.01) \times \{2\}$	$(40.00, 64.01) \times \{2\}$	$(64.01,\infty)\times\{2\}$	$(-\infty, 24.99) \times \{1\}$	$(24.99,40.01)\times\{1\}$	$(40.00, 64.01) \times \{1\}$	$(64.01,\infty)\times\{1\}$	$(-\infty, 24.99) \times \{4, 5, 7\}$	$(24.99, 40.01) \times \{4, 5, 7\}$	$(40.00, 64.01) \times \{4, 5, 7\}$	$(64.01,\infty) \times \{4,5,7\}$	$(-\infty, 24.99) \times \{0, 3, 6\}$	$(24.99, 40.01) \times \{0, 3, 6\}$	$(40.00,64.01)\times\{0,3,6\}$	$(64.01, \infty) \times \{0, 3, 6\}$
De	Tuple	(0,0)	(1,0)	(2,0)	(3,0)	(0,1)	(1,1)	(2,1)	(3,1)	(0,2)	(1,2)	(2,2)	(3,2)	(0,3)	(1,3)	(2,3)	(3,3)
	Ind	0	\vdash	2	33	4	25	9	7	∞	6	10	11	12	13	14	15
Selected Variables	Symbol	A_AGE, PEMLR															
Sele	Tuple	(1,2)															
14.01		12															

Table 5.6: Decision regions and predicted class labels across all iterations (continued)

Selected Variables			De	Decision Region		Predicted Classes	Min
Tuple Symbol		Ind	Tuple	Cross Product	Ind	Label	IIIIIII
A_AGE, PEMLR		0	(0,0)	$(-\infty,24.99)\times\{2\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
		П	(1,0)	$(24.99, 55.99) \times \{2\}$	7	$^{\rm NY}$	2
		2	(2,0)	$(55.99,64.99)\times\{2\}$	4	Y1Y	\vdash
		3	(3,0)	$(64.99,\infty)\times\{2\}$	2	$^{\rm NY}$	\vdash
		4	(0,1)	$(-\infty, 24.99) \times \{1\}$	0	NNN	2
		ಬ	(1,1)	$(24.99, 55.99) \times \{1\}$	33	YNN	23
		9	(2,1)	$(55.99,64.99)\times\{1\}$	33	YNN	4
		7	(3,1)	$(64.99,\infty)\times\{1\}$	7	$^{ m NY}$	ಬ
		∞	(0,2)	$(-\infty, 24.99) \times \{3, 4, 5, 7\}$	1	NNY	9
		6	(1,2)	$(24.99, 55.99) \times \{3, 4, 5, 7\}$	0	NNN	6
		10	(2,2)	$(55.99,64.99)\times\{3,4,5,7\}$	2	$^{ m NY}_{-}$	7
		11	(3,2)	$(64.99, \infty) \times \{3, 4, 5, 7\}$	4	Y1Y	17
		12	(0,3)	$(-\infty, 24.99) \times \{0, 6\}$	Н	NNY	15
		13	(1,3)	$(24.99, 55.99) \times \{0, 6\}$	П	NNY	1
		14	(2,3)	$(55.99, 64.99) \times \{0, 6\}$	2	$^{ m NY}$	1
		15	(3,3)	$(64.99,\infty)\times\{0,6\}$	П	NNY	П
	l						

Table 5.6: Decision regions and predicted class labels across all iterations (continued)

Tuple 3							Nıım
(1,2)	Symbol	Ind	Tuple	Cross Product	Ind	Label	
	A_AGE, PEMLR	0	(0,0)	$(-\infty, 24.01) \times \{2\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
		П	(1,0)	$(24.01, 55.99) \times \{2\}$	23	$^{\rm NY}$	2
		2	(2,0)	$(55.99, 64.99) \times \{2\}$	4	Y1Y	П
		3	(3,0)	$(64.99,\infty)\times\{2\}$	73	$^{\rm NY}$	П
		4	(0,1)	$(-\infty, 24.01) \times \{1\}$	0	NNN	7
		\mathcal{D}	(1,1)	$(24.01, 55.99) \times \{1\}$	33	YNN	23
		9	(2,1)	$(55.99,64.99)\times\{1\}$	3	YNN	4
		7	(3,1)	$(64.99,\infty)\times\{1\}$	2	$^{ m NY}$	ಬ
		∞	(0,2)	$(-\infty, 24.01) \times \{3, 4, 5, 7\}$	П	NNY	9
		6	(1,2)	$(24.01, 55.99) \times \{3, 4, 5, 7\}$	0	NNN	6
		10	(2,2)	$(55.99,64.99)\times\{3,4,5,7\}$	2	$^{ m NY}$	7
		11	(3,2)	$(64.99, \infty) \times \{3, 4, 5, 7\}$	4	Y1Y	17
		12	(0,3)	$(-\infty, 24.01) \times \{0, 6\}$	П	NNY	15
		13	(1,3)	$(24.01, 55.99) \times \{0, 6\}$	П	NNY	1
		14	(2,3)	$(55.99,64.99)\times\{0,6\}$	2	$^{ m NY}_{-}$	1
		15	(3,3)	$(64.99,\infty)\times\{0,6\}$	1	NNY	1

Table 5.6: Decision regions and predicted class labels across all iterations (continued)

Iter	$Sel\epsilon$	Selected Variables		De	Decision Region		Predicted Classes	2
	Tuple	Symbol	Ind	Tuple	Cross Product	Ind	Label	
15	(1,2)	A_AGE , PEMLR	0	(0,0)	$(-\infty, 24.01) \times \{2\}$	0,1,2,3,4	NNN, NNY, NY_, YNN, Y1Y	0
			\vdash	(1,0)	$(24.01, 55.99) \times \{2\}$	73	$^{\rm NY}$	2
			2	(2,0)	$(55.99, 64.99) \times \{2\}$	4	Y1Y	П
			33	(3,0)	$(64.99,\infty)\times\{2\}$	7	$^{\rm NY}$	П
			4	(0,1)	$(-\infty, 24.01) \times \{1\}$	0	NNN	7
			ಬ	(1,1)	$(24.01, 55.99) \times \{1\}$	လ	YNN	23
			9	(2,1)	$(55.99, 64.99) \times \{1\}$	33	YNN	4
			7	(3,1)	$(64.99,\infty)\times\{1\}$	2	$^{ m NY}$	\mathcal{D}
			∞	(0,2)	$(-\infty, 24.01) \times \{3, 4, 5, 7\}$	1	NNY	9
			6	(1,2)	$(24.01, 55.99) \times \{3, 4, 5, 7\}$	0	NNN	6
			10	(2,2)	$(55.99, 64.99) \times \{3, 4, 5, 7\}$	2	$^{ m NY}$	7
			11	(3,2)	$(64.99, \infty) \times \{3, 4, 5, 7\}$	4	Y1Y	17
			12	(0,3)	$(-\infty,24.01)\times\{0,6\}$	П	NNY	15
			13	(1,3)	$(24.01, 55.99) \times \{0, 6\}$	П	NNY	П
			14	(2,3)	$(55.99,64.99)\times\{0,6\}$	2	$^{\rm NY}$	1
			15	(3,3)	$(64.99,\infty)\times\{0,6\}$	1	NNY	1

Table 5.7: Inconsistency between numerical CPLEX and true decision regions

Iter		Tra	Training Instance	ıce		Reported	rted	CPLEX		True	
	ID	A_AGE	PEMLR	NASS	Target	Region	Predict	Region	Position	Region	Predict
2	∞	4	0	0	0	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	10	12	0	0	0	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	20	10	0	0	0	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	21	82	ಬ	1	1	22	4	Ю	(2, 1)	9	0, 1, 2, 3, 4
	22	74	ರ	1	1	22	4	Ю	(2, 1)	9	0, 1, 2, 3, 4
	23	64	ರ	1	1	22	4	ıΩ	(2, 1)	9	0, 1, 2, 3, 4
	24	73	ಬ	1	1	22	4	Ю	(2, 1)	9	0, 1, 2, 3, 4
	26	ಬ	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	27	4	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	28	10	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	29	54	9	1	1	26	1	9	(3, 1)	7	4
	30	33	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	33	17	4	1	1	26	1	9	(3, 1)	7	4
	35	77	9	1	1	26	1	9	(3, 1)	7	4
	36	ಬ	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	37	80	ಬ	1	1	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4

Table 5.7: Inconsistency between numerical CPLEX and true decision regions (continued)

Iter		$- \Gamma \epsilon$	Training Instance	ıce		Reported	orted	CPLEX		True	
;	ID	A_AAGE	PEMLR	SSYN	Target	Region	Predict	Region	Position	Region	Predict
	40	21	2	1	1	14	2	3	(0, 1)	4	2
	44	62	1	1	2	14	2	က	(0, 1)	4	2
	47	Ю	0	0	2	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	48	92	ಬ	1	23	22	4	ಗು	(2, 1)	9	0, 1, 2, 3, 4
	51	2	0	0	2	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	53	29	1	1	2	14	2	ಣ	(0, 1)	4	2
	54	29	ಬ	1	2	22	4	Ю	(2, 1)	9	0, 1, 2, 3, 4
	26	85	ಬ	1	2	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	28	70	2	1	2	26	П	9	(3, 1)	7	4
	09	56	9	1	2	26	1	9	(3, 1)	7	4
	64	63	1	1	3	14	7	3	(0, 1)	4	7
	65	14	0	0	က	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	74	4	0	0	33	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	75	12	0	0	33	38	П	6	(3, 2)	11	0, 1, 2, 3, 4
	78	2	0	0	33	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	87	73	ಬ	П	4	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	06	92	ರ	П	4	22	4	ಗು	(2, 1)	9	0, 1, 2, 3, 4

Table 5.7: Inconsistency between numerical CPLEX and true decision regions (continued)

Iter		Tre	Training Instance	ıce		Reported	orted	CPLEX		True	
	ID	A_AGE	PEMLR	NASS	Target	Region	Predict	Region	Position	Region	Predict
	91	22	5	1	4	22	4	5	(2, 1)	9	0, 1, 2, 3, 4
	93	71	1	П	4	14	2	3	(0, 1)	4	2
	94	70	ಬ	П	4	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	95	28	ಬ	П	4	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	96	29	<u></u>	1	4	14	2	3	(0, 1)	4	2
	26	71	ಬ	П	4	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	86	99	ಬ	П	4	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	66	29	ರ	\vdash	4	22	4	ಒ	(2, 1)	9	0, 1, 2, 3, 4
3	8	4	0	0	0	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	10	12	0	0	0	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	20	10	0	0	0	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	21	85	ಬ	П	1	22	4	25	(2, 1)	9	0, 1, 2, 3, 4
	22	74	ಬ	1	1	22	4	2	(2, 1)	9	0, 1, 2, 3, 4
	23	64	ಬ	1	1	22	4	2	(2, 1)	9	0, 1, 2, 3, 4
	24	73	ಬ	1	1	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	26	ಬ	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4

Table 5.7: Inconsistency between numerical CPLEX and true decision regions (continued)

Tter		${ m Tr} \epsilon$	Training Instance	1ce		Repo	Reported	CPLEX		True	
5	ID	A_AGE	PEMLR	SSYN	Target	Region	Predict	Region	Position	Region	Predict
	27	4	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	28	10	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	29	54	9	П	1	26	1	9	(3, 1)	<u>~</u>	4
	30	က	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	33	17	4	П	1	26	1	9	(3, 1)	! ~	4
	35	22	9	П	1	26	1	9	(3, 1)	! ~	4
	36	Ю	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	37	80	ಬ	1	П	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	40	21	7	1	1	14	7	33	(0, 1)	4	2
	44	62	1	1	23	14	23	က	(0, 1)	4	2
	47	ಬ	0	0	73	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	48	92	ಬ	1	7	22	4	ಸಂ	(2, 1)	9	0, 1, 2, 3, 4
	51	2	0	0	2	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	53	29	1	1	2	14	7	3	(0, 1)	4	2
	54	29	ಬ	1	2	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	26	82	ಬ	1	2	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	28	20	2	П	2	26	1	9	(3, 1)		4

Table 5.7: Inconsistency between numerical CPLEX and true decision regions (continued)

Iter		Tr	Training Instance	лсе		Reported	rted	CPLEX		True	
	П	A_AAGE	PEMLR	SSYN	Target	Region	Predict	Region	Position	Region	Predict
	09	56	9	1	2	26	1	9	(3, 1)	7	4
	64	63	1	П	33	14	2	3	(0, 1)	4	2
	65	14	0	0	3	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	74	4	0	0	33	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	75	12	0	0	33	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	28	<u></u>	0	0	33	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	87	73	ಬ	1	4	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	06	92	ಬ	П	4	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	91	22	ಬ	П	4	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	93	71	1	1	4	14	2	3	(0, 1)	4	2
	94	20	ಬ	П	4	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	92	78	ಬ	П	4	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	96	29	7	П	4	14	2	က	(0, 1)	4	2
	26	71	ಬ	П	4	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	86	99	ಸಂ		4	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	66	29	2	1	4	22	4	2	(2, 1)	9	0, 1, 2, 3, 4

Table 5.7: Inconsistency between numerical CPLEX and true decision regions (continued)

Ter.		Tre	Training Instance	ce		Reported	rted	CPLEX		True	
1001	ID	A_AGE	PEMLR	SSYN	Target	Region	Predict	Region	Position	Region	Predict
4	∞	4	0	0	0	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	10	12	0	0	0	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	20	10	0	0	0	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	21	85	ಬ	1	1	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	22	74	ಬ	1	1	22	4	Ю	(2, 1)	9	0, 1, 2, 3, 4
	23	64	ಬ	1	1	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	24	73	ಬ	1	1	22	4	ъ	(2, 1)	9	0, 1, 2, 3, 4
	26	ಬ	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	27	4	0	0	П	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	28	10	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	29	54	9	1	П	26	1	9	(3, 1)	7	4
	30	33	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	33	17	4	1	П	26	1	9	(3, 1)	7	4
	35	22	9	1	П	26	1	9	(3, 1)	7	4
	36	ಬ	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	37	80	ಬ	1	1	22	4	ರ	(2, 1)	9	0, 1, 2, 3, 4

Table 5.7: Inconsistency between numerical CPLEX and true decision regions (continued)

Itor		${ m Tr}_{ m E}$	Training Instance	ıce		Repo	Reported	CPLEX		True	
	II III	A_AGE	PEMLR	SSYN	Target	Region	Predict	Region	Position	Region	Predict
	40	21	7	1	1	14	2	8	(0, 1)	4	2
	44	62	1	П	2	14	2	က	(0, 1)	4	2
	47	ъ	0	0	7	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	48	92	ಬ	П	7	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	51	7	0	0	7	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	53	29	П	П	2	14	2	က	(0, 1)	4	2
	54	29	ಬ	П	2	22	4	ಗು	(2, 1)	9	0, 1, 2, 3, 4
	26	85	ಬ	П	7	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	28	70	2	П	7	26	1	9	(3, 1)	7	4
	09	56	9	1	2	26	1	9	(3, 1)	7	4
	64	63	1	1	33	14	2	3	(0, 1)	4	2
	65	14	0	0	33	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	74	4	0	0	3	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	75	12	0	0	33	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	78	7	0	0	က	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	87	73	ಬ	П	4	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	06	92	ಬ	П	4	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4

Table 5.7: Inconsistency between numerical CPLEX and true decision regions (continued)

		E						35 100		E	
Iter		Tr	Training Instance	ıce		Kepc	Keported	CPLEA		True	
	П	A_AAGE	PEMLR	SSYN	Target	Region	Predict	Region	Position	Region	Predict
	91	22	5	1	4	22	4	5	(2, 1)	9	0, 1, 2, 3, 4
	93	71	1	1	4	14	2	က	(0, 1)	4	2
	94	20	ಬ	П	4	22	4	Ю	(2, 1)	9	0, 1, 2, 3, 4
	92	78	ಬ	1	4	22	4	ъ	(2, 1)	9	0, 1, 2, 3, 4
	96	29	7	1	4	14	2	က	(0, 1)	4	2
	26	71	ಬ	1	4	22	4	ъ	(2, 1)	9	0, 1, 2, 3, 4
	86	99	ಬ	1	4	22	4	ъ	(2, 1)	9	0, 1, 2, 3, 4
	66	29	rc	П	4	22	4	ಒ	(2, 1)	9	0, 1, 2, 3, 4
2	8	4	0	0	0	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	10	12	0	0	0	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	20	10	0	0	0	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	21	85	ಬ	1	1	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	22	74	ಬ	1	1	22	4	ъ	(2, 1)	9	0, 1, 2, 3, 4
	23	64	ಬ	1	1	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	24	73	ಬ	1	1	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	26	ಬ	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4

Table 5.7: Inconsistency between numerical CPLEX and true decision regions (continued)

Ter		${ m Tr} \delta$	Training Instance	ıce		Reported	orted	CPLEX		True	
	ID	A_AGE	PEMLR	SSYN	Target	Region	Predict	Region	Position	Region	Predict
	27	4	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	28	10	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	29	54	9	1	1	26	1	9	(3, 1)	7	4
	30	3	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	33	17	4	П	1	26	1	9	(3, 1)	2	4
	35	2.2	9	П	1	26	1	9	(3, 1)	7	4
	36	ъ	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	37	80	ಬ	П	1	22	4	ъ	(2, 1)	9	0, 1, 2, 3, 4
	40	21	7	1	1	14	2	က	(0, 1)	4	2
	44	79	1	1	23	14	2	3	(0, 1)	4	2
	47	ಬ	0	0	7	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	48	92	20	1	7	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	51	2	0	0	7	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	53	29	1	1	7	14	2	33	(0, 1)	4	2
	54	29	ಬ	1	7	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	26	85	20	1	7	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	28	70	2	1	2	26	1	9	(3, 1)	7	4

Table 5.7: Inconsistency between numerical CPLEX and true decision regions (continued)

Iter		${ m Tr}_{ m E}$	Training Instance	ıce		Reported	rted	CPLEX		True	
	П	A_AAGE	PEMLR	SSYN	Target	Region	Predict	Region	Position	Region	Predict
	09	56	9	1	2	26	1	9	(3, 1)	7	4
	64	63	1	1	3	14	2	3	(0, 1)	4	2
	65	14	0	0	3	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	74	4	0	0	3	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	75	12	0	0	3	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	78	<u></u>	0	0	3	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	87	73	ಬ	1	4	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	06	92	ಬ	1	4	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	91	22	ಬ	1	4	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	93	71	П	1	4	14	2	33	(0, 1)	4	2
	94	70	ರ	1	4	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	92	78	ಬ	1	4	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	96	29	7	1	4	14	2	3	(0, 1)	4	2
	26	71	ಬ	П	4	22	4	ಸಂ	(2, 1)	9	0, 1, 2, 3, 4
	86	99	ಬ	1	4	22	4	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	66	29	22	1	4	22	4	ıΩ	(2, 1)	9	0, 1, 2, 3, 4

Table 5.7: Inconsistency between numerical CPLEX and true decision regions (continued)

Iter		Tre	Training Instance	ıce		Reported	orted	CPLEX		True	
	ID	A_AGE	PEMLR	SSYN	Target	Region	Predict	Region	Position	Region	Predict
9	∞	4	0	0	0	38	П	6	(3, 2)	11	0, 1, 2, 3, 4
	10	12	0	0	0	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	20	10	0	0	0	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	21	82	ರ	1	1	22	4	rO	(2, 1)	9	2
	22	74	ಬ	П	1	22	4	ಬ	(2, 1)	9	2
	23	64	ರ	1	1	22	4	rO	(2, 1)	9	2
	24	73	ಬ	П	1	22	4	ъ	(2, 1)	9	2
	26	ಬ	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	27	4	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	28	10	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	29	54	9	1	1	26	1	9	(3, 1)	7	4
	30	3	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	33	17	4	1	1	26	1	9	(3, 1)	7	4
	35	2.2	9	1	1	26	1	9	(3, 1)	7	4
	36	ಬ	0	0	1	38	1	6	(3, 2)	11	0, 1, 2, 3, 4
	37	80	ಬ	П	1	22	4	ъ	(2, 1)	9	2

Table 5.7: Inconsistency between numerical CPLEX and true decision regions (continued)

Iter		Tre	Training Instance	ıce		Repo	Reported	CPLEX		True	
	ID	A_AGE	PEMLR	SSYN	Target	Region	Predict	Region	Position	Region	Predict
	40	21	2	1	1	14	2,3	3	(0, 1)	4	0, 3
	44	62	П	1	23	14	2,3	က	(0, 1)	4	0, 3
	47	ಬ	0	0	2	38	1	6	(3, 2)	111	0, 1, 2, 3, 4
	48	92	ಬ	1	21	22	4	ಗು	(2, 1)	9	2
	51	2	0	0	2	38	1	6	(3, 2)	111	0, 1, 2, 3, 4
	53	29	П	1	2	14	2,3	33	(0, 1)	4	0, 3
	54	29	ಬ	1	2	22	4	ಬ	(2, 1)	9	2
	26	85	ಬ	1	2	22	4	ಗು	(2, 1)	9	2
	28	70	2	1	2	18	7	4	(1, 1)	ಬ	2, 4
	09	26	9	1	23	26	1	9	(3, 1)	_	4
	64	63	П	1	က	14	2,3	33	(0, 1)	4	0, 3
	65	14	0	0	က	38	1	6	(3, 2)	111	0, 1, 2, 3, 4
	74	4	0	0	က	38	1	6	(3, 2)	111	0, 1, 2, 3, 4
	75	12	0	0	33	38	П	6	(3, 2)	111	0, 1, 2, 3, 4
	78	7	0	0	3	38	П	6	(3, 2)	111	0, 1, 2, 3, 4
	87	73	ಬ	П	4	22	4	ಬ	(2, 1)	9	2
	06	92	ಬ	П	4	22	4	ಗು	(2, 1)	9	2

Table 5.7: Inconsistency between numerical CPLEX and true decision regions (continued)

Ther		${ m Tr}_{ m E}$	Training Instance	ıce		Repo	Reported	CPLEX		True	
	ID	A_AAGE	PEMLR	SSYN	Target	Region	Predict	Region	Position	Region	Predict
	91	22	5	1	4	22	4	5	(2, 1)	9	2
	93	71	1	1	4	14	2,3	3	(0, 1)	4	0, 3
	94	20	ಬ	1	4	22	4	ಬ	(2, 1)	9	2
	95	78	ಬ	1	4	22	4	20	(2, 1)	9	2
	96	29	7	1	4	14	2,3	3	(0, 1)	4	0, 3
	26	71	ಬ	1	4	22	4	ಬ	(2, 1)	9	2
	86	99	ಬ	1	4	22	4	ಬ	(2, 1)	9	2
	66	29	5	1	4	22	4	5	(2, 1)	9	2
7	1	24	1	2	0	14	က	က	(0, 1)	4	0, 1, 2, 3, 4
	2	28	_	2	0	22	0	25	(2, 1)	9	0, 1, 2, 3, 4
	3	24	1	2	0	14	3	3	(0, 1)	4	0, 1, 2, 3, 4
	4	40	_	2	0	22	0	22	(2, 1)	9	0, 1, 2, 3, 4
	κ	24	1	7	0	14	3	3	(0, 1)	4	0, 1, 2, 3, 4
	9	26	1	2	0	14	3	3	(0, 1)	4	0, 1, 2, 3, 4
	7	18	7	2	0	22	0	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	∞	4	0	0	0	22	0	2	(2, 1)	9	0, 1, 2, 3, 4

Table 5.7: Inconsistency between numerical CPLEX and true decision regions (continued)

Tter _		Tre	Training Instance	ıce		Reported	orted	CPLEX		True	
	Π	A_AGE	PEMLR	SSYN	Target	Region	Predict	Region	Position	Region	Predict
	6	38	လ	2	0	22	0	ಸು	(2, 1)	9	0, 1, 2, 3, 4
	10	12	0	0	0	22	0	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	11	46	<u>~</u>	2	0	22	0	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	12	26	1	2	0	14	က	ಣ	(0, 1)	4	0, 1, 2, 3, 4
	13	35	<u>~</u>	2	0	22	0	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	14	19	<u></u>	2	0	22	0	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	15	29	4	2	0	14	က	ಣ	(0, 1)	4	0, 1, 2, 3, 4
	16	24	0	2	0	22	0	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	17	35	1	2	0	14	33	င	(0, 1)	4	0, 1, 2, 3, 4
	18	48	1	2	0	14	33	33	(0, 1)	4	0, 1, 2, 3, 4
	19	41	1	2	0	14	33	33	(0, 1)	4	0, 1, 2, 3, 4
	20	10	0	0	0	22	0	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	21	82	ಬ	1	1	38	4	6	(3, 2)	11	0, 1, 2, 3, 4
	22	74	ಬ	1	П	38	4	6	(3, 2)	11	0, 1, 2, 3, 4
	23	64	ಬ	П	П	38	4	6	(3, 2)	11	0, 1, 2, 3, 4
	24	73	ಬ	\vdash	Н	38	4	6	(3, 2)	11	0, 1, 2, 3, 4
	25	15	_	2	1	22	0	ಬ	(2, 1)	9	0, 1, 2, 3, 4

Table 5.7: Inconsistency between numerical CPLEX and true decision regions (continued)

Ter		$\operatorname{Tr} arepsilon$	Training Instance	1Ce		Reported	rted	CPLEX		True	
	ID	A_AGE	PEMLR	NASS	Target	Region	Predict	Region	Position	Region	Predict
	26	ಬ	0	0	1	22	0	ಬ	(2,1)	9	0, 1, 2, 3, 4
	27	4	0	0	1	22	0	ъ	(2, 1)	9	0, 1, 2, 3, 4
	28	10	0	0	1	22	0	Ю	(2, 1)	9	0, 1, 2, 3, 4
	59	54	9	1	1	34	1	∞	(2, 2)	10	2
	30	က	0	0	1	22	0	Ю	(2, 1)	9	0, 1, 2, 3, 4
	31	45	3	2	1	22	0	ıΩ	(2, 1)	9	0, 1, 2, 3, 4
	32	28	П	2	1	14	က	က	(0, 1)	4	0, 1, 2, 3, 4
	33	17	4	1	1	26	2	9	(0, 2)	∞	0
	34	22	1	2	1	14	က	က	(0, 1)	4	0, 1, 2, 3, 4
	35	77	9	1	1	34	1	∞	(2, 2)	10	2
	36	ಬ	0	0	1	22	0	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	37	80	ಬ	1	1	38	4	6	(3, 2)	11	0, 1, 2, 3, 4
	38	16	1	2	1	14	3	3	(0, 1)	4	0, 1, 2, 3, 4
	39	22	7	2	1	22	0	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	40	21	7	1	1	34	1	∞	(2, 2)	10	2
	41	26	4	7	2	14	3	33	(0, 1)	4	0, 1, 2, 3, 4
	42	64	ಬ	7	2	26	2	9	(3, 1)	7	0

Table 5.7: Inconsistency between numerical CPLEX and true decision regions (continued)

			Training Instance	lce		Reported	rted	CPLEX		True	
Iter	П	A_AGE	PEMLR	SSYN	Target	Region	Predict	Region	Position	Region	Predict
	43	38	2	2	2	14	8	က	(0, 1)	4	0, 1, 2, 3, 4
	44	62	1	1	2	26	2	9	(0, 2)	∞	0
	45	22	2	2	2	22	0	τc	(2, 1)	9	0, 1, 2, 3, 4
	46	65	П	2	2	14	က	က	(0, 1)	4	0, 1, 2, 3, 4
	47	ಬ	0	0	2	22	0	ъ	(2, 1)	9	0, 1, 2, 3, 4
	48	92	ಬ	1	2	38	4	6	(3, 2)	11	0, 1, 2, 3, 4
	49	49	П	2	2	14	က	က	(0, 1)	4	0, 1, 2, 3, 4
	20	37	2	2	2	14	က	က	(0, 1)	4	0, 1, 2, 3, 4
	51	2	0	0	2	22	0	Ю	(2, 1)	9	0, 1, 2, 3, 4
	52	41	П	2	23	14	3	3	(0, 1)	4	0, 1, 2, 3, 4
	53	29	П	1	2	26	2	9	(0, 2)	∞	0
	54	29	ಬ	1	2	38	4	6	(3, 2)	11	0, 1, 2, 3, 4
	55	63	ಬ	2	2	26	2	9	(3, 1)	2	0
	26	82	ಬ	1	2	38	4	6	(3, 2)	11	0, 1, 2, 3, 4
	22	19	1	7	2	14	3	က	(0, 1)	4	0, 1, 2, 3, 4
	28	70	2	1	2	26	2	9	(0, 2)	∞	0
	29	38	1	7	2	14	3	က	(0, 1)	4	0, 1, 2, 3, 4

Table 5.7: Inconsistency between numerical CPLEX and true decision regions (continued)

Iter		Tre	Training Instance	ıce		Repo	Reported	CPLEX		True	
1001	ID	A_AGE	PEMLR	SSYN	Target	Region	Predict	Region	Position	Region	Predict
	09	26	9	1	2	34	1	∞	(2, 2)	10	2
	61	29	1	2	3	14	3	3	(0, 1)	4	0, 1, 2, 3, 4
	62	26	1	2	3	14	3	3	(0, 1)	4	0, 1, 2, 3, 4
	63	59	1	2	33	14	3	33	(0, 1)	4	0, 1, 2, 3, 4
	64	63	1	1	3	26	2	9	(0, 2)	∞	0
	92	14	0	0	3	22	0	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	99	22	4	2	3	14	3	3	(0, 1)	4	0, 1, 2, 3, 4
	29	25	<u></u>	2	3	22	0	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	89	18	1	2	3	14	33	33	(0, 1)	4	0, 1, 2, 3, 4
	69	25	1	2	3	14	33	3	(0, 1)	4	0, 1, 2, 3, 4
	20	46	1	2	3	14	3	3	(0, 1)	4	0, 1, 2, 3, 4
	71	40	1	2	3	14	33	33	(0, 1)	4	0, 1, 2, 3, 4
	73	29	4	2	3	14	33	3	(0, 1)	4	0, 1, 2, 3, 4
	73	33	1	2	3	14	3	3	(0, 1)	4	0, 1, 2, 3, 4
	74	4	0	0	3	22	0	ಬ	(2, 1)	9	0, 1, 2, 3, 4
	75	12	0	0	3	22	0	v	(2, 1)	9	0, 1, 2, 3, 4
	92	51	7	2	3	22	0	ಬ	(2, 1)	9	0, 1, 2, 3, 4

Table 5.7: Inconsistency between numerical CPLEX and true decision regions (continued)

Iter		${ m Tr} s$	Training Instance). (Ce		Reported	rted	CPLEX		True	
	ID	A_AAGE	PEMLR	SSYN	Target	Region	Predict	Region	Position	Region	Predict
	22	29	1	2	3	14	3	3	(0, 1)	4	0, 1, 2, 3, 4
	78	1 -	0	0	3	22	0	Ю	(2, 1)	9	0, 1, 2, 3, 4
	62	51	П	7	3	14	33	က	(0, 1)	4	0, 1, 2, 3, 4
	80	41	1	2	က	14	က	က	(0, 1)	4	0, 1, 2, 3, 4
	81	78	ಬ	2	4	26	23	9	(3, 1)	_	0
	82	09	2	2	4	14	က	က	(0, 1)	4	0, 1, 2, 3, 4
	83	27	1	2	4	14	က	က	(0, 1)	4	0, 1, 2, 3, 4
	84	65	П	2	4	14	က	က	(0, 1)	4	0, 1, 2, 3, 4
	82	22	1	7	4	14	က	က	(0, 1)	4	0, 1, 2, 3, 4
	98	42	1	7	4	14	3	3	(0, 1)	4	0, 1, 2, 3, 4
	87	73	70	1	4	38	4	6	(3, 2)	111	0, 1, 2, 3, 4
	88	45	1	7	4	14	က	က	(0, 1)	4	0, 1, 2, 3, 4
	88	26	1	7	4	14	3	3	(0, 1)	4	0, 1, 2, 3, 4
	06	92	70	1	4	38	4	6	(3, 2)	111	0, 1, 2, 3, 4
	91	27	ಬ	1	4	38	4	6	(3, 2)	111	0, 1, 2, 3, 4
	92	27	П	7	4	14	3	က	(0, 1)	4	0, 1, 2, 3, 4
	93	71	1	1	4	26	2	9	(0, 2)	∞	0

Table 5.7: Inconsistency between numerical CPLEX and true decision regions (continued)

		 Tr	Training Instance	1ce		Reported	orted	CPLEX		True	
1001	ID	A_AGE	PEMLR	SSYN	Target	Region	Predict	Region	Position	Region	Predict
	94	70	ಒ	1	4	38	4	6	(3, 2)	11	0, 1, 2, 3, 4
	95	78	ъ	1	4	38	4	6	(3, 2)	11	0, 1, 2, 3, 4
	96	29	1-	1	4	34	1	∞	(2, 2)	10	2
	26	71	Ю	1	4	38	4	6	(3, 2)	11	0, 1, 2, 3, 4
	86	99	ಬ	1	4	38	4	6	(3, 2)	11	0, 1, 2, 3, 4
	66	29	Ю	1	4	38	4	6	(3, 2)	11	0, 1, 2, 3, 4
	100	61	1	2	4	14	3	3	(0, 1)	4	0, 1, 2, 3, 4
∞	8	4	0	0	0	34	1	∞	(2, 2)	10	2
	10	12	0	0	0	34	1	œ	(2, 2)	10	2
	20	10	0	0	0	34	1	∞	(2,2)	10	2
	21	85	ಬ	1	П	38	4	6	(3, 2)	11	7
	22	74	ಬ	1	П	38	4	6	(3, 2)	11	7
	23	64	ಬ	1	1	38	4	6	(3, 2)	11	7
	24	73	ಬ	П	1	38	4	6	(3, 2)	11	7
	26	ಬ	0	0	1	34	1	∞	(2, 2)	10	7
	27	4	0	0	П	34	П	∞	(2, 2)	10	2

Table 5.7: Inconsistency between numerical CPLEX and true decision regions (continued)

			<u> </u>			6		אם זתט		E	
Iter		TĽ	raining instance	ıce		Kepc	Reported	CFLEA		Irue	
	ID	A_AAGE	PEMLR	SSYN	Target	Region	Predict	Region	Position	Region	Predict
	28	10	0	0	1	34	1	∞	(2, 2)	10	2
	59	54	9	1	1	30	2		(1, 2)	6	0, 1, 2, 3, 4
	30	က	0	0	1	34	1	∞	(2, 2)	10	2
	33	17	4	1	1	34	1	∞	(2, 2)	10	2
	35	22	9	1	1	30	2		(1, 2)	6	0, 1, 2, 3, 4
	36	ъ	0	0	1	34	1	∞	(2, 2)	10	2
	37	80	ಬ	1	1	38	4	6	(3, 2)	11	2
	40	21	7	1	1	34	1	∞	(2, 2)	10	2
	44	79	1	1	23	30	73		(1, 2)	6	0, 1, 2, 3, 4
	47	ಬ	0	0	23	34	П	∞	(2, 2)	10	73
	48	92	70	1	23	38	4	6	(3, 2)	11	73
	51	2	0	0	2	34	1	∞	(2, 2)	10	73
	53	29	1	1	23	30	23	<u></u>	(1, 2)	6	0, 1, 2, 3, 4
	54	29	ಸರ	1	2	38	4	6	(3, 2)	11	2
	26	82	70	1	23	38	4	6	(3, 2)	11	73
	28	70	2	1	23	26	73	9	(0, 2)	∞	0, 1, 2, 3, 4
	09	26	9	1	23	30	7	7	(1, 2)	6	0, 1, 2, 3, 4

Table 5.7: Inconsistency between numerical CPLEX and true decision regions (continued)

1 10+1		${ m Tr}_{ m E}$	Training Instance	ıce		Reported	rted	CPLEX		True	
	ID	A_AGE	PEMLR	SSYN	Target	Region	Predict	Region	Position	Region	Predict
	64	63	1	1	3	30	2	2	(1, 2)	6	0, 1, 2, 3, 4
	65	14	0	0	ಣ	34	1	∞	(2, 2)	10	2
	74	4	0	0	ಣ	34	П	∞	(2, 2)	10	2
	72	12	0	0	က	34	1	∞	(2, 2)	10	2
	28	<u> </u>	0	0	ಣ	34	1	∞	(2, 2)	10	2
	87	73	ಬ	1	4	38	4	6	(3, 2)	11	2
	06	92	ಸಂ	1	4	38	4	6	(3, 2)	11	2
	91	22	ಬ	1	4	38	4	6	(3, 2)	11	2
	93	71	1	1	4	30	2	7	(1, 2)	6	0, 1, 2, 3, 4
	94	70	ಬ	1	4	38	4	6	(3, 2)	11	2
	92	78	ಬ	1	4	38	4	6	(3, 2)	11	2
	96	29	7	1	4	34	1	∞	(2, 2)	10	2
	26	71	ಬ	1	4	38	4	6	(3, 2)	11	2
	86	99	ಬ	Н	4	38	4	6	(3, 2)	11	2
	66	29	22	1	4	38	4	6	(3, 2)	11	2
6	∞	4	0	0	0	34	1	∞	(2, 2)	10	2

Table 5.7: Inconsistency between numerical CPLEX and true decision regions (continued)

Iter		Tra	Training Instance	ıce		Reported	rted	CPLEX		True	
	ID	A_AGE	PEMLR	SSYN	Target	Region	Predict	Region	Position	Region	Predict
	10	12	0	0	0	34	1	∞	(2, 2)	10	2
	20	10	0	0	0	34	1	∞	(2, 2)	10	2
	21	82	ಬ	1	П	38	4	6	(3, 2)	11	2
	22	74	ಬ	1	1	38	4	6	(3, 2)	11	2
	23	64	ಬ	1	1	38	4	6	(3, 2)	11	2
	24	73	ಬ	1	П	38	4	6	(3, 2)	11	2
	26	ಬ	0	0	1	34	П	∞	(2, 2)	10	2
	27	4	0	0	1	34	1	∞	(2,2)	10	2
	28	10	0	0	1	34	1	∞	(2, 2)	10	2
	29	54	9	1	1	34	1	∞	(2, 2)	10	2
	30	3	0	0	1	34	П	∞	(2, 2)	10	2
	33	17	4	1	1	34	1	∞	(2, 2)	10	2
	35	2.2	9	1	1	34	1	∞	(2, 2)	10	2
	36	ಬ	0	0	1	34	1	∞	(2, 2)	10	2
	37	80	ಬ	1	1	38	4	6	(3, 2)	11	2
	40	21	2	П	П	34	Н	∞	(2, 2)	10	2
	44	79	П	1	2	30	2		(1, 2)	6	0, 1, 2, 3, 4

Table 5.7: Inconsistency between numerical CPLEX and true decision regions (continued)

Iter		Tra	Training Instance	1ce		Repo	Reported	CPLEX		True	
	ID	A_AGE	PEMLR	NASS	Target	Region	Predict	Region	Position	Region	Predict
	47	5	0	0	2	34	1	∞	(2, 2)	10	2
	48	92	ಬ	1	2	38	4	6	(3, 2)	11	2
	51	2	0	0	2	34	1	∞	(2, 2)	10	2
	53	29	П	1	2	30	2	2	(1, 2)	6	0, 1, 2, 3, 4
	54	29	ಬ	1	2	38	4	6	(3, 2)	11	2
	26	85	ಬ	1	2	38	4	6	(3, 2)	11	2
	28	20	2	1	2	26	2	9	(0, 2)	∞	0, 1, 2, 3, 4
	09	26	9	1	2	34	П	∞	(2, 2)	10	2
	64	63	1	1	က	30	2	7	(1, 2)	6	0, 1, 2, 3, 4
	65	14	0	0	3	34	1	∞	(2, 2)	10	7
	74	4	0	0	က	34	1	∞	(2, 2)	10	2
	72	12	0	0	က	34	1	∞	(2,2)	10	2
	28	<u></u>	0	0	3	34	1	∞	(2, 2)	10	7
	87	73	70	1	4	38	4	6	(3, 2)	11	73
	06	92	ಬ	1	4	38	4	6	(3, 2)	11	73
	91	22	ಬ	1	4	38	4	6	(3, 2)	11	7
	93	71	П	П	4	30	2		(1, 2)	6	0, 1, 2, 3, 4

Table 5.7: Inconsistency between numerical CPLEX and true decision regions (continued)

Ther		Tra	Training Instance	ce		Reported	rted	CPLEX		True	
	ID	A_AGE PEMLR	PEMLR	SSYN	Target	Region	Region Predict	${ m Region}$	Position	Region	Predict
	94	20	ಗು	1	4	38	4	6	(3, 2)	11	2
	92	78	ಬ	1	4	38	4	6	(3, 2)	11	2
	96	29	_	1	4	34	1	∞	(2, 2)	10	2
	26	71	ಬ	1	4	38	4	6	(3, 2)	11	2
	86	99	ಬ	1	4	38	4	6	(3, 2)	11	2
	66	29	က	1	4	38	4	6	(3, 2)	11	2

CHAPTER VI

CONCLUDING REMARKS

Throughout this dissertation, the 2020 person-level CPS ASEC health insurance dataset in SAS7BDAT format is converted to feather and CSV formats. The file sizes markedly reduce by 94.02% and 71.31% respectively. Five combinations of health insurance enrollment in employment-based plan (GRP), direct-purchase plan (DIR) and public health insurance (PUB) are considered, leading to five possible classes. All codes are written in Python, well-known for data analysis, except the proposed box classifier in OPL embedded in CPLEX Optimization Studio. A Python class and a pandas DataFrame accessor are introduced so that a method can be called on a DataFrame at any time. All classification models, a Gini-based decision tree and the proposed classifier, are tested on a remote virtual machine to prevent the intervention in local computing resources and also to flexibly configure hardware and operating system. Python 3.13 with the global interpreter lock (GIL) still enabled is built from source. The GitHub repository is also available at https://github.com/songkomkrit/phd.

The proposed box classifier is heavily based on the rigorous formulation of 0-1 MILP problem, and it is very large-scale. Only 100 out of 157,681 noninfant survey participants are randomly selected as a sample of equal class size. Prior to the investigation of 2 contributing factors, 3 out of 184 independent variables are preselected by the SelectKBest using mutual information from a mixture of continuous and categorical features. Compared to the decision tree of multiple depths, the proposed model achieves a high training accuracy and low number of total splits within an hour and a half, though optimality not guaranteed, it constructs the branch-and-cut tree of large size between 6 GB and 7 GB, and it can group together similar categorical values to provide better insight into a selected categorical feature. A limitation of this study includes the lack of high-performance computing (HPC) technology of aggregating multiple computer clusters to efficiently serve massive computation required by the proposed model in the nature of 0-1 MILP. Therefore, further investigation into its approximation algorithm with theoretically derived bound on training accuracy compared to the exact 0-1 MILP model is suggested.

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CPLEX Engine Log

<<< setup

Version identifier: 22.1.1.0 | 2022-11-28 | 9160aff4d CPXPARAM_MIP_Strategy_File CPXPARAM_MIP_Limits_Solutions 1 CPXPARAM_TimeLimit 86400 ${\tt CPXPARAM_MIP_Limits_TreeMemory}$ 204800 Tried aggregator 1 time. MIP Presolve eliminated 402 rows and 800 columns. MIP Presolve modified 200 coefficients. Reduced MIP has 4004 rows, 5507 columns, and 22553 nonzeros. Reduced MIP has 4643 binaries, 11 generals, 0 SOSs, and 0 indicators. Presolve time = 0.01 sec. (17.75 ticks) Found incumbent of value -20.000000 after 0.02 sec. (24.01 ticks) Root node processing (before b&c): Real time 0.02 sec. (24.25 ticks) Parallel b&c, 8 threads: 0.00 sec. (0.00 ticks) Real time Sync time (average) = 0.00 sec. Wait time (average) = 0.00 sec. Total (root+branch&cut) = 0.02 sec. (24.25 ticks) Iteration 1 Bounds on # of cuts = 8 with [3 3 2] Error = 80 (out of 100 instances) Accuracy = 20Solving time = 0.0003894 min (minutes) Accumulated time = 0.0003894 min (minutes) Solution status code = 104

Selected variables:

LB on error = -5500

Relative objective gap = 278.999999999

Number of selected variables = 0 (0 continuous + 0 categorical)

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CPXPARAM_MIP_Strategy_File 3

CPXPARAM_MIP_Limits_Solutions 1

CPXPARAM_TimeLimit 86399.976635986328

CPXPARAM_MIP_Limits_TreeMemory 204800

Probing time = 0.01 sec. (4.62 ticks)

Cover probing fixed 8 vars, tightened 40 bounds.

Clique table members: 11812.

MIP emphasis: balance optimality and feasibility.

MIP search method: dynamic search.

Parallel mode: deterministic, using up to 8 threads.

Root relaxation solution time = 0.03 sec. (35.79 ticks)

Nodes Cuts/

Node Left Objective IInf Best Integer Best Bound ItCnt Gap

0+ -20.0000 -5600.0000 -800.0000 -800.0000 -20.0000 0 0 472 1209 0 -800.0000 346 -20.0000 Cuts: 512 1987 0 0 -800.0000 651 -20.0000 Cuts: 874 3508 0+ 0 -28.0000 -800.0000

GUB cover cuts applied: 29
Clique cuts applied: 10
Cover cuts applied: 51

Implied bound cuts applied: 242

Flow cuts applied: 6

Mixed integer rounding cuts applied: 186

Zero-half cuts applied: 77

Lift and project cuts applied: 7
Gomory fractional cuts applied: 16

Root node processing (before b&c):

Real time = 1.78 sec. (1803.05 ticks)

Parallel b&c, 8 threads:

Real time = 0.00 sec. (0.00 ticks)

```
Sync time (average)
                   = 0.00 \text{ sec.}
Wait time (average)
                         0.00 sec.
_____
Total (root+branch&cut) = 1.78 sec. (1803.05 ticks)
_____
Iteration 2
Bounds on # of cuts = 8 with [3 3 2]
Error = 72 (out of 100 instances)
Accuracy = 28
Solving time = 0.029740967 min (minutes)
Accumulated time = 0.030130367 min (minutes)
Solution status code = 104
LB on error = -700
Relative objective gap = 27.571428571
Selected variables:
PEMLR (Categorical)
SS_YN (Categorical)
Number of selected variables = 2 (0 continuous + 2 categorical)
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Version identifier: 22.1.1.0 | 2022-11-28 | 9160aff4d
CPXPARAM_MIP_Strategy_File
CPXPARAM_MIP_Limits_Solutions
                                              1
CPXPARAM_TimeLimit
                                              86398.192177978519
CPXPARAM_MIP_Limits_TreeMemory
                                              204800
MIP emphasis: balance optimality and feasibility.
MIP search method: dynamic search.
Parallel mode: deterministic, using up to 8 threads.
Nodes
                                           Cuts/
              Objective IInf Best Integer
Node Left
                                             Best Bound ItCnt
                                                                    Gap
     0+
           0
                                     -31.0000
                                                -717.7485
                                                                       ___
GUB cover cuts applied: 41
```

Clique cuts applied: 73

```
Cover cuts applied: 433
Implied bound cuts applied: 315
Flow cuts applied: 8
Mixed integer rounding cuts applied: 447
Zero-half cuts applied: 145
Lift and project cuts applied: 13
Gomory fractional cuts applied: 57
Root node processing (before b&c):
                         0.74 sec. (861.25 ticks)
Real time
Parallel b&c, 8 threads:
Real time
                         0.00 sec. (0.00 ticks)
Sync time (average) = 0.00 sec.
Wait time (average) = 0.00 sec.
_____
Total (root+branch&cut) = 0.74 sec. (861.25 ticks)
_____
Iteration 3
Bounds on # of cuts = 8 with [3 3 2]
Error = 69 (out of 100 instances)
Accuracy = 31
Solving time = 0.01229578 min (minutes)
Accumulated time = 0.042426147 min (minutes)
Solution status code = 104
LB on error = -617.482727096
Relative objective gap = 22.1446041
Selected variables:
PEMLR (Categorical)
SS_YN (Categorical)
Number of selected variables = 2 (0 continuous + 2 categorical)
Version identifier: 22.1.1.0 | 2022-11-28 | 9160aff4d
CPXPARAM_MIP_Strategy_File
CPXPARAM_MIP_Limits_Solutions
                                               1
CPXPARAM_TimeLimit
                                               86397.45443115235
```

CPXPARAM_MIP_Limits_TreeMemory

MIP emphasis: balance optimality and feasibility.

MIP search method: dynamic search.

Parallel mode: deterministic, using up to 8 threads.

Nodes Cuts/

Node Left Objective IInf Best Integer Best Bound ItCnt Gap

204800

* 0+ 0 -36.0000 -657.1275 ---

GUB cover cuts applied: 41
Clique cuts applied: 73
Cover cuts applied: 623

Implied bound cuts applied: 329

Flow cuts applied: 12

Mixed integer rounding cuts applied: 562

Zero-half cuts applied: 191

Lift and project cuts applied: 22 Gomory fractional cuts applied: 108

Root node processing (before b&c):

Real time = 0.82 sec. (913.50 ticks)

Parallel b&c, 8 threads:

Real time = 0.00 sec. (0.00 ticks)

Sync time (average) = 0.00 sec.Wait time (average) = 0.00 sec.

Total (root+branch&cut) = 0.82 sec. (913.50 ticks)

Iteration 4

Bounds on # of cuts = 8 with [3 3 2]

Error = 64 (out of 100 instances)

Accuracy = 36

Solving time = 0.013641048 min (minutes)

Accumulated time = 0.056067196 min (minutes)

Solution status code = 104

LB on error = -557.127521455

Relative objective gap = 17.253542263

Selected variables:

PEMLR (Categorical)

SS_YN (Categorical)

Number of selected variables = 2 (0 continuous + 2 categorical)

 $\label{tension} \mbox{Version identifier: } 22.1.1.0 \ | \ 2022-11-28 \ | \ 9160aff4d$

CPXPARAM_MIP_Strategy_File

CPXPARAM_MIP_Limits_Solutions 1

CPXPARAM_TimeLimit 86396.635968261719

CPXPARAM_MIP_Limits_TreeMemory 204800

MIP emphasis: balance optimality and feasibility.

MIP search method: dynamic search.

Parallel mode: deterministic, using up to 8 threads.

Nodes Cuts/

Node Left Objective IInf Best Integer Best Bound ItCnt Gap

* 0+ 0 -38.0000 -626.9345 ---

GUB cover cuts applied: 82

Clique cuts applied: 73

Cover cuts applied: 1063

Implied bound cuts applied: 407

Flow cuts applied: 35

Mixed integer rounding cuts applied: 819

Zero-half cuts applied: 258

Lift and project cuts applied: 22

Gomory fractional cuts applied: 160

Root node processing (before b&c):

Real time = 1.96 sec. (1928.89 ticks)

Parallel b&c, 8 threads:

Real time = 0.00 sec. (0.00 ticks)

Sync time (average) = 0.00 sec.Wait time (average) = 0.00 sec.

Total (root+branch&cut) = 1.96 sec. (1928.89 ticks)

Iteration 5

Bounds on # of cuts = 8 with [3 3 2]

Error = 62 (out of 100 instances)

Accuracy = 38

Solving time = 0.032725952 min (minutes)

Accumulated time = 0.088793148 min (minutes)

Solution status code = 104

LB on error = -526.934511415

Relative objective gap = 15.498276616

Selected variables:

PEMLR (Categorical)

SS_YN (Categorical)

Number of selected variables = 2 (0 continuous + 2 categorical)

Version identifier: 22.1.1.0 | 2022-11-28 | 9160aff4d

CPXPARAM_MIP_Strategy_File 3

CPXPARAM_MIP_Limits_Solutions 1

CPXPARAM_TimeLimit 86394.672411132808

CPXPARAM_MIP_Limits_TreeMemory 204800

MIP emphasis: balance optimality and feasibility.

 $\ensuremath{\mathsf{MIP}}$ search method: dynamic search.

Parallel mode: deterministic, using up to 8 threads.

Nodes						Cuts/				
	Node	Left	Objective	IInf	Best Integer	Best Bound	ItCnt	Gap		
	0	0	-577.3658	659	-38.0000	Cuts: 836	28237			
	0	0	-558.5105	640	-38.0000	Cuts: 955	31741			
	0	0	-540.9147	613	-38.0000	Cuts: 870	34307			
	0	0	-539.0391	710	-38.0000	Cuts: 924	36234			
	0	0	-538.9354	762	-38.0000	Cuts: 989	37794			
	Detecting symmetries									
	0	0	-538.8822	778	-38.0000	Cuts: 830	39029			

0	0	-538.8578	826	-38.0000	Cuts: 708	40186	
0	0	-538.8409	806	-38.0000	Cuts: 266	40928	
0	0	-538.8265	840	-38.0000	Cuts: 601	41623	
0	2	-538.8265	827	-38.0000	-538.8265	41623	
Elapse	ed time	e = 5.26 sec	. (5435.47	ticks, tree	= 0.02 MB, so	olutions =	5)
2	4	-532.4711	622	-38.0000	-538.8264	44441	
9	9	-530.6872	643	-38.0000	-538.8264	47088	
27	20	-521.8493	667	-38.0000	-538.6068	60887	
46	20	-531.9657	614	-38.0000	-538.6066	60999	
80	68	-509.9472	575	-38.0000	-538.6066	103610	
118	57	-528.6696	612	-38.0000	-538.6066	98680	
156	138	-490.7266	504	-38.0000	-538.6066	147852	
194	169	-486.6126	511	-38.0000	-538.6066	164110	
248	209	-484.0715	570	-38.0000	-538.6066	181896	
625	468	-387.6828	467	-38.0000	-538.6066	243471	
Elapse	ed time	e = 8.32 sec	. (8694.74	ticks, tree	= 6.06 MB, so	olutions =	5)
1551	1044	infeasible	Э	-38.0000	-538.6066	323452	

Performing restart 1

Repeating presolve.

Tried aggregator 1 time.

MIP Presolve eliminated 447 rows and 48 columns.

MIP Presolve modified 2098 coefficients.

Reduced MIP has 3557 rows, 5459 columns, and 21635 nonzeros.

Reduced MIP has 4603 binaries, 51 generals, 0 SOSs, and 0 indicators.

Presolve time = 0.01 sec. (20.08 ticks)

Tried aggregator 1 time.

MIP Presolve eliminated 1 rows and 0 columns.

MIP Presolve modified 300 coefficients.

Reduced MIP has 3556 rows, 5459 columns, and 21533 nonzeros.

Reduced MIP has 4603 binaries, 51 generals, 0 SOSs, and 0 indicators.

Presolve time = 0.02 sec. (21.21 ticks)

Represolve time = 0.18 sec. (172.19 ticks)

1603	0	-531.3154	530	-38.0000	Cuts: 989	388606	
1603	0	-507.2228	677	-38.0000	Cuts: 989	394828	
1603	0	-483.0125	703	-38.0000	Cuts: 989	399749	
1603	0	-460.7636	713	-38.0000	Cuts: 989	407166	
1603	0	-451.8578	687	-38.0000	Cuts: 989	412425	

1603	0	-450.6323	805	-38.0000	Cuts: 989	415841	
1603	0	-432.3823	759	-38.0000	Cuts: 989	423001	
1603	0	-431.4684	871	-38.0000	Cuts: 989	426280	
1603	0	-418.8128	830	-38.0000	Cuts: 989	433824	
1603	0	-417.3207	854	-38.0000	Cuts: 989	437138	998.21%
1603	0	-412.4347	847	-38.0000	Cuts: 989	442602	985.35%
1603	0	-412.0400	919	-38.0000	Cuts: 989	445973	984.32%
1603	0	-411.2439	902	-38.0000	Cuts: 989	449769	980.32%
1603	0	-405.6804	852	-38.0000	Cuts: 989	458674	967.58%
1603	0	-405.2740	821	-38.0000	Cuts: 989	461351	962.76%
1603	0	-400.9631	855	-38.0000	Cuts: 989	468469	952.28%
1603	0	-400.5521	861	-38.0000	Cuts: 989	472372	952.28%
1603	0	-399.9329	893	-38.0000	Cuts: 989	475615	952.28%
1603	0	-397.2191	915	-38.0000	Cuts: 989	483998	944.52%
1603	0	-397.1061	974	-38.0000	Cuts: 989	487153	944.52%
1603	0	-396.3444	963	-38.0000	Cuts: 989	492117	943.01%
1603	0	-395.8637	958	-38.0000	Cuts: 989	496720	939.08%
1603	0	-395.7821	987	-38.0000	Cuts: 989	498869	938.39%
1603	0	-393.1402	932	-38.0000	Cuts: 989	506111	934.58%
1603	0	-393.0317	970	-38.0000	Cuts: 989	508897	934.29%
1603	0	-392.7950	1024	-38.0000	Cuts: 989	513782	933.67%
1603	0	-391.5060	909	-38.0000	Cuts: 989	518934	930.28%
1603	0	-391.4094	932	-38.0000	Cuts: 989	523923	930.02%
1603	0	-390.7816	965	-38.0000	Cuts: 989	530008	928.37%
1603	0	-390.4502	996	-38.0000	Cuts: 989	535960	927.50%
1603	0	-389.7746	975	-38.0000	Cuts: 964	544136	925.72%
1603	0	-389.7179	1028	-38.0000	Cuts: 989	548551	925.57%
1603	0	-389.2127	1004	-38.0000	Cuts: 779	559361	924.24%
1603	0	-389.1541	1044	-38.0000	Cuts: 989	563246	924.09%
1603	0	-388.9571	1041	-38.0000	Cuts: 550	570153	923.57%
1603	0	-388.9327	1102	-38.0000	Cuts: 989	573533	923.51%
1603	0	-388.7011	1102	-38.0000	Cuts: 689	580181	922.90%
1603	0	-388.6569	1153	-38.0000	Cuts: 989	583864	922.78%
1603	2	-388.6569	1138	-38.0000	-388.6569	583864	922.78%
1604	3	-388.2777	1073	-38.0000	-388.2776	587877	921.78%
1605	4	-387.6984	1112	-38.0000	-387.6983	589040	920.26%
1606	5	-387.2199	1098	-38.0000	-387.2194	590656	919.00%
1607	6	-386.8095	1049	-38.0000	-387.0084	594070	918.44%
1609	4	-386.1028	771	-38.0000	-387.0084	595848	918.44%

1610	5	-384.6422	738	-38.0000	-387.0084	598389	918.44%
1612	8	-382.0306	768	-38.0000	-387.0084	613444	918.44%
1615	9	-383.3599	777	-38.0000	-386.9557	622553	918.30%
Elapsed	time =	129.55 sec.	(136	324.17 ticks,	tree = 0.02 MB,	solution	ns = 5)
1616	9	-375.8867	788	-38.0000	-386.9557	626524	918.30%
1618	12	-381.5367	781	-38.0000	-386.9557	649547	918.30%
1620	11	-384.0428	927	-38.0000	-386.9557	645526	918.30%
1621	7	-385.0541	787	-38.0000	-386.9557	604066	918.30%
1624	17	-380.8858	736	-38.0000	-386.8091	710376	917.92%
1626	18	-380.7050	773	-38.0000	-386.8091	720185	917.92%
1628	20	-383.5446	949	-38.0000	-386.8091	752988	917.92%
1629	23	-382.1894	814	-38.0000	-386.1685	802390	916.23%
1633	19	-379.8805	765	-38.0000	-386.1685	724806	916.23%
1636	21	-382.9042	965	-38.0000	-386.1685	754400	916.23%
Elapsed	time =	144.26 sec.	(150	551.65 ticks,	tree = 0.16 MB,	solution	ns = 5)
1638	23	-380.8078	875	-38.0000	-386.1685	784761	916.23%
1640	30	-378.6604	789	-38.0000	-386.1685	871097	916.23%
1642	33	-382.5092	979	-38.0000	-386.1685	905127	916.23%
1644	28	-369.0237	733	-38.0000	-386.1685	859325	916.23%
1645	37	-371.9556	867	-38.0000	-386.1685	939036	916.23%
1648	39	-371.2651	710	-38.0000	-386.1685	956044	916.23%
1650	41	-372.1191	850	-38.0000	-386.1685	974080	916.23%
1653	42	-379.9721	743	-38.0000	-386.1685	985124	916.23%
1658	49	-377.9725	784	-38.0000	-386.1685	1012953	916.23%
1660	42	-368.8209	739	-38.0000	-386.1685	980397	916.23%
Elapsed	time =	158.38 sec.	(165	820.30 ticks,	tree = 0.22 MB,	solution	ns = 5)
1662	46	-371.9569	788	-38.0000	-386.1685	996170	916.23%
1664	45	-378.6304	890	-38.0000	-386.1685	993788	916.23%
1666	48	-362.4336	921	-38.0000	-386.1685	1004351	916.23%
1669	57	-375.2631	783	-38.0000	-386.1685	1054343	916.23%
1672	65	-377.0938	785	-38.0000	-386.1685	1077462	916.23%
1676	56	-370.4028	811	-38.0000	-386.1685	1048798	916.23%
1677	58	-377.8983	718	-38.0000	-386.1685	1057061	916.23%
1680	69	-377.3027	879	-38.0000	-386.1685	1098444	916.23%
1682	73	-377.2401	751	-38.0000	-386.1685	1119275	916.23%
1687	64	-366.9964	711	-38.0000	-386.1685	1081207	916.23%
Elapsed	time =	170.66 sec.	(179	644.29 ticks,	tree = 0.33 MB,	solution	ns = 5)
1689	80	-376.0566	805	-38.0000	-386.1685	1152637	916.23%
1692	81	-364.2601	795	-38.0000	-386.1685	1158452	916.23%

1698	86	-375.6997	713	-38.0000	-386.1685	1176524	916.23%
1702	78	-367.0278	782	-38.0000	-386.1685	1148330	916.23%
1705	87	-362.6076	808	-38.0000	-386.1685	1186831	916.23%
1709	87	-372.5778	688	-38.0000	-386.1685	1182617	916.23%
1715	91	-361.2418	775	-38.0000	-386.1685	1198439	916.23%
1718	96	-364.3288	787	-38.0000	-386.1685	1229751	916.23%
1722	97	-361.7048	671	-38.0000	-386.1685	1223041	916.23%
1731	101	-371.0484	819	-38.0000	-386.1685	1241877	916.23%
Elapse	ed time =	181.55 sec.	(190	828.34 ticks,	tree = 0.48 MB	, solutio	ons = 5)
1738	101	-352.9145	701	-38.0000	-386.1685	1224916	916.23%
1747	105	-348.2397	651	-38.0000	-386.1685	1226350	916.23%
1751	92	-355.5354	732	-38.0000	-386.1685	1201408	916.23%
1753	98	-363.3957	800	-38.0000	-386.1685	1236017	916.23%
1760	109	-360.8998	699	-38.0000	-386.1685	1258257	916.23%
1766	106	-362.0373	768	-38.0000	-386.1685	1251129	916.23%
1770	138	-369.8963	847	-38.0000	-386.1685	1315878	916.23%
1776	157	-359.2809	751	-38.0000	-386.1685	1371681	916.23%
1780	143	-372.8468	866	-38.0000	-386.1685	1336188	916.23%
1788	159	-357.3907	752	-38.0000	-386.1685	1376458	916.23%
Elapse	ed time =	192.07 sec.	(201	.530.64 ticks,	tree = 1.48 MB	, solutio	ons = 5)
1793	165	-351.1548	720	-38.0000	-386.1685	1382812	916.23%
1800	146	-330.0804	647	-38.0000	-386.1685	1313355	916.23%
1809	168	-354.1876	662	-38.0000	-386.1685	1388199	916.23%
1819	169	-347.8706	660	-38.0000	-386.1685	1390338	916.23%
1827	171	-347.0562	700	-38.0000	-386.1685	1392341	916.23%
1838	198	-359.3410	735	-38.0000	-386.1685	1468649	916.23%
1844	189	-316.1421	609	-38.0000	-386.1685	1413172	916.23%
1856	184	-366.0754	822	-38.0000	-386.1685	1431628	916.23%
1862	177	-342.0989	643	-38.0000	-386.1685	1401987	916.23%
1872	185	-368.7856	775	-38.0000	-386.1685	1433055	916.23%
Elapse	ed time =	202.84 sec.	(212	2543.16 ticks,	tree = 2.11 MB	, solutio	ns = 5)
1886	204	-348.5624	768	-38.0000	-386.1685	1470065	916.23%
1896	187	-367.8768	775	-38.0000	-386.1685	1439100	916.23%
1910	263	-366.6514	725	-38.0000	-386.1685	1563807	916.23%
1917	226	-366.2143	745	-38.0000	-386.1685	1526100	916.23%
1936	223	-329.7481	750	-38.0000	-386.1685	1508197	916.23%
1943	280	-352.0908	798	-38.0000	-386.1685	1611855	916.23%
1954	306	-346.5994	704	-38.0000	-386.1685	1668764	916.23%
1963	266	-359.3957	727	-38.0000	-386.1685	1578568	916.23%

1976	227	-330.0316	709	-38.0000	-386.1685	1517288 916.23%
1996	304	-332.9077	756	-38.0000		
Elapse	ed time =	212.95 sec.	(223101.	71 ticks,	tree = 5.77 MB	, solutions = 5)
2005	237	-359.0799	637	-38.0000		
2023	289	-351.0669	792	-38.0000		1631819 916.23%
2045	312	-332.4457	739	-38.0000	-386.1685	1662091 916.23%
2068	366	-350.4486	785	-38.0000	-386.1685	1774184 916.23%
2081	393	-327.5920	631	-38.0000	-386.1685	1810141 916.23%
2099	326	-322.0228	695	-38.0000	-386.1685	1696440 916.23%
2119	349	-325.3107	627	-38.0000	-386.1685	1722349 916.23%
2140	448	-321.3074	722	-38.0000	-386.1685	1913614 916.23%
2160	460	-315.9675	684	-38.0000	-386.1685	1927645 916.23%
2227	375	-329.5555	813	-38.0000	-386.1685	1801495 916.23%
Elapse	ed time =	225.67 sec.	(235995.	28 ticks,	tree = 6.47 MB	, solutions = 5)
2329	554	-274.9106	575	-38.0000	-386.1685	2020145 916.23%
2462	603	-208.4551	608	-38.0000	-386.1685	2106858 916.23%
2643	662	-287.5155	621	-38.0000	-386.1685	2198449 916.23%
2816	632	-274.9940	683	-38.0000	-386.1685	2159172 916.23%
2986	735	-213.5904	523	-38.0000	-386.1685	2277454 916.23%
3306	787	-211.7584	632	-38.0000	-385.3111	2315535 913.98%
3607	1286	-201.8962	558	-38.0000	-385.3111	2674488 913.98%
3977	1303	-183.7525	692	-38.0000	-385.3111	2693379 913.98%
4008	1540	-376.5161	957	-38.0000	-385.3111	2835562 913.98%
4055	1700	-376.8232	922	-38.0000	-385.3111	2930975 913.98%
Elapse	ed time =	265.35 sec.	(274668.	79 ticks,	tree = 65.53 M	B, solutions = 5)
4113	1703	-375.8357	891	-38.0000	-385.3111	2941519 913.98%
4283	2263	-129.2319	583	-38.0000	-384.4635	3322625 911.75%
4472	2267	-374.2307	1055	-38.0000	-384.4635	3388151 911.75%
4510	2280	-365.4293	795	-38.0000	-384.4635	3426661 911.75%
4538	2416	-346.9335	718	-38.0000	-381.9426	3507655 905.11%
4576	2480	-361.8407	815	-38.0000	-381.9426	3618609 905.11%
4615	2528	-373.4181	888	-38.0000	-381.9426	3742100 905.11%
4658	2532	-342.0634	836	-38.0000	-381.9426	3734502 905.11%
4699	2533	-365.4533	944	-38.0000	-381.9426	3763000 905.11%
4747	2657	-310.5418	677	-38.0000	-381.9426	4014791 905.11%
Elapse	ed time =	303.11 sec.	(313289.	88 ticks,	tree = 111.76	MB, solutions = 5)
4802	2620	-349.3655	890	-38.0000	-381.9426	3957330 905.11%
4871	2755	-323.3668	697	-38.0000	-381.9426	4199276 905.11%
4946	2741	-290.9565	601	-38.0000	-381.9426	4189091 905.11%

5043	2816	-273.6839	761	-38.0000	-381.9426	4291508	905.11%
5155	2962	-201.2710	658	-38.0000	-381.9426	4460142	905.11%
5291	2981	-169.8593	604	-38.0000	-381.9426	4478921	905.11%
5466	3076	-203.9541	682	-38.0000	-381.9426	4584024	905.11%
5694	3180	-135.7850	678	-38.0000	-381.9426	4698677	905.11%
6097	3555	-75.2412	434	-38.0000	-381.9426	4847836	905.11%
6335	3538	-100.6562	464	-38.0000	-381.9426	4949312	905.11%
Elaps	ed time =	342.63 sec.	(351762.	11 ticks,	tree = 158.31	MB, solut	ions = 5)
6614	4051	-82.9797	391	-38.0000	-381.9426	5198382	905.11%
7157	4043	-93.9551	441	-38.0000	-381.9426	5261948	905.11%
7752	4029	-193.8106	526	-38.0000	-381.9426	5254080	905.11%
7876	4590	-83.9348	406	-38.0000	-381.8931	5514496	904.98%
7902	4881	-379.3565	919	-38.0000	-381.8926	5595047	904.98%
7940	5145	-286.1287	658	-38.0000	-380.8071	5682204	902.12%
8002	4691	-379.3689	774	-38.0000	-380.6354	5544630	901.67%
8035	5148	-364.5840	753	-38.0000	-380.6354	5716992	901.67%
8098	5346	-324.6925	717	-38.0000	-379.9667	5809066	899.91%
8209	5380	-263.0652	689	-38.0000	-379.9667	5827011	899.91%
Elaps	ed time =	383.55 sec.	(391445.	00 ticks,	tree = 250.41	MB, solut	ions = 5)
8407	5393	-359.8021	721	-38.0000	-379.9667	5914698	899.91%
8481	5521	-262.1683	689	-38.0000	-379.9667	6008749	899.91%
8682	5483	-357.5335	722	-38.0000	-379.9667	6039212	899.91%
8840	5744	-352.5118	627	-38.0000	-379.9667	6188503	899.91%
9256	5975	-93.5178	383	-38.0000	-379.9667	6283362	899.91%
9630	6102	-222.7763	518	-38.0000	-379.9667	6388913	899.91%
9957	6395	-332.9427	599	-38.0000	-379.9667	6566131	899.91%
10206	6704	-102.7602	493	-38.0000	-379.9667	6620570	899.91%
10687	6744	-356.8449	804	-38.0000	-379.9667	6676558	899.91%
10892	7279	-141.4255	485	-38.0000	-379.9667	6824257	899.91%
Elaps	ed time =	424.74 sec.	(430070.	66 ticks,	tree = 348.74	MB, solut	ions = 5)
11285	7549	-266.8955	713	-38.0000	-379.9667	6935942	899.91%
11952	8078	-81.0221	475	-38.0000	-379.9667	7048892	899.91%
12136	8219	-376.5899	831	-38.0000	-379.7943	7146826	899.46%
12316	8696	-376.1854	831	-38.0000	-379.5824	7253016	898.90%
12762	9331	-109.6829	395	-38.0000	-379.5824	7366582	898.90%
13127	9413	-307.3537	678	-38.0000	-379.4554	7421367	898.57%
13190	9725	-370.0417	752	-38.0000	-379.4554	7491216	898.57%
13369	10087	-365.0055	759	-38.0000	-379.4554	7647384	898.57%
13522	9992	-149.8716	574	-38.0000	-379.3906	7584555	898.40%

13675 10455	-169.6634	556	-38.0000	-379.3906	7707912	898.40%
<pre>Elapsed time =</pre>	472.46 sec.	(4684	53.20 ticks, tree	= 464.06 1	MB, soluti	ons = 5)
13959 10554	-275.5156	638	-38.0000	-379.3906	7826355	898.40%
14081 10676	-330.6031	587	-38.0000	-379.3841	7853249	898.38%
14380 10903	-299.8063	554	-38.0000	-379.2996	7908540	898.16%
14811 10991	-84.2419	244	-38.0000	-379.2886	7914970	898.13%
15473 11856	-43.7849	209	-38.0000	-379.2886	8097559	898.13%
15621 11659	-375.0829	765	-38.0000	-379.2886	8079509	898.13%
15745 12045	-279.4488	234	-38.0000	-379.2886	8159239	898.13%
16259 12480	-122.9856	334	-38.0000	-379.2886	8247673	898.13%
16560 12619	-150.5545	539	-38.0000	-379.2386	8302917	898.00%
16678 12987	-260.3273	396	-38.0000	-378.8563	8406230	896.99%
Elapsed time =	525.90 sec.	(5066	88.39 ticks, tree	= 537.86 1	MB, soluti	ons = 5)
16832 13408	-360.3564	681	-38.0000	-378.8563	8512516	896.99%
17110 13421	-347.1104	577	-38.0000	-378.7315	8526769	896.66%
17190 13641	-337.1913	715	-38.0000	-378.5983	8577198	896.31%
17403 13718	-266.2754	489	-38.0000	-378.5983	8642161	896.31%
17723 13869	-246.2897	615	-38.0000	-378.5983	8701973	896.31%
17846 14453	-147.7591	476	-38.0000	-378.5983	8901628	896.31%
18013 14743	-257.4287	619	-38.0000	-378.5983	9008331	896.31%
18451 14774	-193.0102	557	-38.0000	-378.5983	9013834	896.31%
18659 14808	-112.1777	501	-38.0000	-378.5983	9017455	896.31%
18954 15194	-365.5685	865	-38.0000	-378.5983	9123572	896.31%
Elapsed time =	577.52 sec.	(5464	29.72 ticks, tree	= 545.80 1	MB, soluti	ons = 5)
18993 14989	-304.6462	216	-38.0000	-378.5190	9079117	896.10%
19220 15840	-359.2220	537	-38.0000	-378.5190	9298493	896.10%
19362 15500	-367.9160	862	-38.0000	-378.3778	9199784	895.73%
19647 16099	-337.1348	625	-38.0000	-378.2779	9416366	895.47%
19967 16207	-348.9415	288	-38.0000	-378.2779	9475112	895.47%
20375 16345	-375.7467	838	-38.0000	-378.2215	9569876	895.32%
20568 16421	-210.0809	171	-38.0000	-378.2029	9586501	895.27%
20898 16905	-48.9183	177	-38.0000	-378.1858	9664318	895.23%
21209 17362	-43.6742	267	-38.0000	-378.1858	9772573	895.23%
21460 17380	-195.1753	181	-38.0000	-378.1382	9776799	895.10%
Elapsed time =	628.76 sec.	(5850	05.60 ticks, tree	= 564.44 1	MB, soluti	ons = 5)
21731 17569	-176.2266	368	-38.0000	-378.1382	9846289	895.10%
22006 18252	-234.4369	589	-38.0000	-378.1353	10008342	895.09%
22183 18306	-306.6087	349	-38.0000	-378.1353	9991426	895.09%
22423 18469	-121.7009	505	-38.0000	-378.1353	10072247	895.09%

22692 18987	-121.6388	336	-38.0000	-378.1353	10213880	895.09%
22850 19137	-56.8695	394	-38.0000	-378.1353	10254885	895.09%
22918 19013	-364.3899	709	-38.0000	-378.0981	10236729	894.99%
23147 19464	-325.3539	713	-38.0000	-377.9287	10374695	894.55%
23527 19550	-169.3183	533	-38.0000	-377.9287	10393813	894.55%
24049 19625	-364.2002	903	-38.0000	-377.8836	10371003	894.43%
Elapsed time =	682.61 sec.	(6237	23.92 ticks, tree	= 682.22 N	MB, soluti	ons = 5)
24686 20421	-368.3340	750	-38.0000	-377.8294	10657403	894.29%
25245 19621	-341.1563	713	-38.0000	-377.8294	10466998	894.29%
25810 20807	-353.1728	676	-38.0000	-377.8294	10767293	894.29%
26049 21383	-358.5244	487	-38.0000	-377.8294	10845444	894.29%
26370 21135	-277.1734	655	-38.0000	-377.7041	10818422	893.96%
26824 21172	-182.8045	538	-38.0000	-377.6195	10821038	893.74%
27218 22670	-296.3888	360	-38.0000	-377.6195	11004288	893.74%
27628 22783	-189.3246	127	-38.0000	-377.6147	11054059	893.72%
28136 22825	-270.7104	612	-38.0000	-377.6147	11112939	893.72%
28294 24138	-209.7610	529	-38.0000	-377.6147	11307267	893.72%
Elapsed time =	734.91 sec.	(6620	90.80 ticks, tree	= 797.77 N	MB, soluti	ons = 5)
28605 23711	-234.1514	552	-38.0000	-377.6147	11253825	893.72%
28840 24553	-268.2504	475	-38.0000	-377.5816	11391896	893.64%
29426 24982	-166.5687	513	-38.0000	-377.5816	11485504	893.64%
29687 25483	-371.1550	894	-38.0000	-377.5816	11577943	893.64%
30202 25692	-274.5559	499	-38.0000	-377.4552	11622202	893.30%
30909 25657	-63.7559	371	-38.0000	-377.4257	11604346	893.23%
31597 25853	-118.5099	565	-38.0000	-377.4257	11717188	893.23%
32092 26336	-181.8973	511	-38.0000	-377.4257	11767598	893.23%
33050 26745	-46.3389	148	-38.0000	-377.4257	11832881	893.23%
33558 27309	-53.9421	87	-38.0000	-377.3971	11887058	893.15%
<pre>Elapsed time =</pre>	781.18 sec.	(7003	63.36 ticks, tree	= 1010.72	MB, solut	ions = 5)
33666 27434	-282.0341	190	-38.0000	-377.2214	11958972	892.69%
* 33853+29275			-39.0000	-377.143	35	867.03%
33922 29276	-367.3141	816	-39.0000	-377.1435	12240781	867.03%
33978 29609	-373.9386	762	-39.0000	-377.1435	12286072	867.03%
33978 29609 34107 29321	-373.9386 -272.3192	762 625	-39.0000 -39.0000	-377.1435 -377.1435		

GUB cover cuts applied: 745 Clique cuts applied: 45

Cover cuts applied: 3303

Implied bound cuts applied: 47

```
Flow cuts applied: 81
Mixed integer rounding cuts applied: 882
Zero-half cuts applied: 110
Lift and project cuts applied: 6
Gomory fractional cuts applied: 196
Root node processing (before b&c):
Real time
                    = 5.07 sec. (5253.09 ticks)
Parallel b&c, 8 threads:
                    = 792.79 sec. (713089.45 ticks)
Real time
Sync time (average) = 91.30 sec.
Wait time (average) = 0.07 sec.
_____
Total (root+branch&cut) = 797.86 sec. (718342.54 ticks)
_____
Iteration 6
Bounds on # of cuts = 8 with [3 3 2]
Error = 61 (out of 100 instances)
Accuracy = 39
Solving time = 13.297700484 min (minutes)
Accumulated time = 13.386493632 min (minutes)
Solution status code = 104
LB on error = -277.143152611
Relative objective gap = 8.670337246
Selected variables:
PEMLR (Categorical)
SS_YN (Categorical)
Number of selected variables = 2 (0 continuous + 2 categorical)
_____
Version identifier: 22.1.1.0 | 2022-11-28 | 9160aff4d
CPXPARAM_MIP_Strategy_File
CPXPARAM_MIP_Limits_Solutions
                                              1
CPXPARAM_TimeLimit
                                              85596.810382080075
CPXPARAM_MIP_Limits_TreeMemory
                                              204800
```

Nodes Cuts/ Node Left Objective IInf Best Integer ItCnt Best Bound Gap 34184 30011 infeasible -39.0000 -377.1432 12462046 867.03% Elapsed time = 0.56 sec. (7.69 ticks, tree = 1131.55 MB, solutions = 6) 34185 30011 infeasible -39.0000 -377.1432 12463576 867.03% 34186 30012 -353.1274 307 -39.0000 -377.1432 12467117 867.03% 34230 30050 -240.2890 140 -39.0000 -377.1432 12469248 867.03% 34284 30101 -96.2412 68 -39.0000 -377.1432 12469654 867.03% -310.4203 34322 30026 254 -39.0000 -377.1432 12474494 867.03% 34358 30062 -208.3211 -39.0000 -377.1432 12474783 168 867.03% 34418 30117 -39.0000 -377.1432 12474986 -61.5243 49 867.03% 34429 30013 -375.1626 -377.1432 12465551 767 -39.0000 867.03% 34430 30013 -368.5689 712 -39.0000 -377.1432 12480749 867.03% 34467 30044 -274.8883 182 -39.0000 -377.1369 12485663 867.02% Elapsed time = 4.67 sec. (3790.87 ticks, tree = 1118.48 MB, solutions = 6) 34559 30016 -375.0799 850 -39.0000 -377.1369 12488423 867.02% 34566 30025 -347.9018 -39.0000 -376.9781 12489041 626 866.61% 34577 30032 -332.5967 607 -39.0000 -376.9781 12490820 866.61% 34601 30027 -337.4018 605 -39.0000 -376.9781 12498141 866.61% 34627 30041 -305.9294 -39.0000 -376.9781 12501938 499 866.61% 34686 30147 -296.6126 -39.0000 -376.9781 12501312 233 866.61% -376.9781 12506723 34810 30028 -351.9984 446 -39.0000 866.61% 34871 30070 -210.9115 477 -39.0000 -376.9781 12496496 866.61% 34894 30030 -376.9781 12516063 -347.0129 721 -39.0000 866.61% 34921 30128 -340.5311 403 -39.0000 -376.9781 12501487 866.61% Elapsed time = 18.01 sec. (13637.71 ticks, tree = 1129.36 MB, solutions = 6) 35000 30164 -376.9781 12503763 -248.6996 190 -39.0000 866.61% 35127 30084 -205.3721 505 -39.0000 -376.9781 12522308 866.61% -376.9781 12523058 35293 30114 -133.2772 471 -39.0000 866.61% 35359 30236 -342.9975 706 -39.0000 -376.9781 12518300 866.61% 35553 30295 -154.2894 -39.0000 -376.9781 12510201 866.61% 114 -66.1665 -39.0000 -376.9781 12512438 35761 30483 53 866.61% 35798 30258 -297.3622 651 -39.0000 -376.9781 12521841 866.61% 35816 30266 -281.3269 625 -39.0000 -376.9781 12523129 866.61% 35843 30276 -256.0856 595 -39.0000 -376.9744 12523344 866.60% 35885 30140 -302.2962 240 -39.0000 -376.9744 12517050 866.60%

Elapsed time = 30.67 sec. (23289.65 ticks, tree = 1133.67 MB, solutions = 6)

-39.0000

-376.9744 12529649

866.60%

36002 30180

-252.7491

441

36062 30299	-206.5953	589	-39.0000	-376.9744 12527129 866	.60%
36101 30230	-57.4126	281	-39.0000	-376.9744 12532623 866	.60%
36126 30319	-159.6736	546	-39.0000	-376.9744 12528123 866	.60%
36145 30340	-344.3312	457	-39.0000	-376.9744 12533604 866	.60%
36233 30409	-163.6412	356	-39.0000	-376.9744 12535025 866	.60%
36303 30347	-91.1935	479	-39.0000	-376.9744 12529582 866	.60%
36329 30235	-375.3955	857	-39.0000	-376.9744 12539899 866	.60%
36545 30368	cutoff		-39.0000	-376.9744 12531654 866	.60%
36575 30265	-348.5818	255	-39.0000	-376.9744 12541452 866	.60%
Elapsed time =	42.20 sec.	(33038.41	ticks, tree =	= 1127.58 MB, solutions =	6)
36709 30470	-351.3221	624	-39.0000	-376.9744 12544142 866	.60%
36729 30559	-215.9049	649	-39.0000	-376.9744 12544298 866	.60%
36812 30436	-161.8911	120	-39.0000	-376.9744 12548856 866	.60%
36944 30486	-328.9821	597	-39.0000	-376.9744 12550670 866	.60%
37174 30492	-322.6494	608	-39.0000	-376.9744 12552363 866	.60%
37271 30718	-149.7022	112	-39.0000	-376.9744 12556065 866	.60%
37335 30604	-117.6572	523	-39.0000	-376.9744 12548367 866	.60%
37361 30612	-97.8061	497	-39.0000	-376.9744 12549204 866	.60%
37508 30622	-74.8865	483	-39.0000	-376.9744 12549545 866	.60%
37547 30284	-269.1983	676	-39.0000	-376.9744 12570795 866	.60%
Elapsed time =	56.00 sec.	(42712.64	ticks, tree =	= 1132.84 MB, solutions =	6)
37587 30639	-46.6761	404	-39.0000	-376.9744 12551100 866	.60%
37639 30414	-311.7083	637	-39.0000	-376.9744 12561840 866	.60%
37916 30226	-75.1134	38	-39.0000	-376.9744 12586701 866	.60%
37975 30522	-298.5992	190	-39.0000	-376.9744 12567952 866	.60%
38358 30734	-49.6809	34	-39.0000	-376.9744 12573259 866	.60%
38425 30896	-312.8846	395	-39.0000	-376.9744 12576993 866	.60%
38560 30651	-351.1738	707	-39.0000	-376.9744 12567726 866	.60%
38703 30659	-338.3736	682	-39.0000	-376.9744 12569044 866	.60%
38722 30923	-251.4943	422	-39.0000	-376.9744 12578618 866	.60%
38807 30678	-300.9916	641	-39.0000	-376.9744 12570330 866	.60%
Elapsed time =	69.11 sec.	(52474.66	ticks, tree =	= 1168.75 MB, solutions =	6)
38865 30114	-364.9152	785	-39.0000	-376.9744 12605868 866	.60%
39094 30118	-364.5336	776	-39.0000	-376.9744 12608499 866	.60%
39163 30390	-290.9313	188	-39.0000	-376.9744 12593666 866	.60%
39318 30330	-128.7170	102	-39.0000	-376.9744 12608320 866	.60%
39378 30824	-371.6508	666	-39.0000	-376.9744 12583385 866	.60%
39448 30859	-235.6664	169	-39.0000	-376.9744 12587080 866	.60%
39572 30207	-115.2196	106	-39.0000	-376.9744 12620071 866	.60%

39664 30963 -184.5348	344	-39.0000	-376.9744 12600785 866.60%
39767 30781 -243.6394	154	-39.0000	-376.9744 12609310 866.60%
39849 30937 -367.9700	804	-39.0000	-376.9744 12597338 866.60%
Elapsed time = 80.41 sec.	(62223.15	ticks, tree =	= 1187.62 MB, solutions = 6)
39854 30851 -372.7405	686	-39.0000	-376.9744 12613720 866.60%
39993 30935 -102.8985	77	-39.0000	-376.9744 12616877 866.60%
40140 30982 -256.2504	319	-39.0000	-376.9744 12605444 866.60%
40214 31050 -74.6662	160	-39.0000	-376.9744 12606445 866.60%
40237 30486 -373.3192	818	-39.0000	-376.9744 12620511 866.60%
40365 30487 -371.8640	807	-39.0000	-376.9744 12623950 866.60%
40369 31131 -374.6936	763	-39.0000	-376.9744 12621218 866.60%
40456 31135 -198.9005	131	-39.0000	-376.9744 12617239 866.60%
40555 30500 -355.6002	607	-39.0000	-376.9744 12631140 866.60%
40570 30508 -331.8984	543	-39.0000	-376.9744 12632773 866.60%
Elapsed time = 92.34 sec.	(72321.10	ticks, tree =	= 1149.15 MB, solutions = 6)
40596 30518 -328.9640	539	-39.0000	-376.9744 12633058 866.60%
40632 30271 -259.0082	190	-39.0000	-376.9744 12650779 866.60%
40800 31223 -90.5794	81	-39.0000	-376.9744 12635395 866.60%
41073 31344 -64.5276	40	-39.0000	-376.9744 12637685 866.60%
41160 30618 -133.3406	487	-39.0000	-376.9744 12643767 866.60%
41210 31110 -356.1415	734	-39.0000	-376.9744 12623652 866.60%
41230 30356 -355.0434	236	-39.0000	-376.9744 12664838 866.60%
41364 31124 -323.7738	674	-39.0000	-376.9744 12626631 866.60%
41379 31356 -369.4440	735	-39.0000	-376.9744 12647780 866.60%
41481 30734 -138.1924	86	-39.0000	-376.9744 12656975 866.60%
Elapsed time = 104.01 sec	. (81980.9	ticks, tree	= 1160.34 MB, solutions = 6)
41544 30398 -298.4723	615	-39.0000	-376.9744 12669908 866.60%
41678 31417 -241.3441	167	-39.0000	-376.9744 12654919 866.60%
41866 31505 -61.6078	64	-39.0000	-376.9744 12655794 866.60%
41914 31163 -244.9421	559	-39.0000	-376.9744 12639460 866.60%
42050 31172 -220.4289	522	-39.0000	-376.9744 12640470 866.60%
42082 30440 -203.7039	545	-39.0000	-376.9744 12674888 866.60%
42117 30505 -307.1978	643	-39.0000	-376.9744 12694878 866.60%
42157 30458 -162.6077	487	-39.0000	-376.9744 12676762 866.60%
42257 31346 -321.7987	248	-39.0000	-376.9744 12666744 866.60%
42771 31228 -124.3631	93	-39.0000	-376.9744 12686599 866.60%
Elapsed time = 119.11 sec	. (94489.24	1 ticks, tree	= 1192.42 MB, solutions = 6)
43224 31270 -374.6367	958	-39.0000	-376.9744 12694136 866.60%
43751 33045 -161.2916	114	-39.0000	-376.9744 12987648 866.60%

30774	-150.7804	111	-39.0000	-376.9744	12718084	866.60%
30814	-374.2969	1033	-39.0000	-376.9744	12725929	866.60%
30671	cutoff		-39.0000	-376.9744	12724888	866.60%
31494	-360.9840	699	-39.0000	-376.9744	12709907	866.60%
31897	-85.7831	53	-39.0000	-376.9744	12902866	866.60%
35065	-111.8791	76	-39.0000	-376.9744	13253046	866.60%
31053	-356.1008	650	-39.0000	-376.9744	12774822	866.60%
31958	-274.4820	382	-39.0000	-376.9744	12935080	866.60%
d time =	164.80 sec.	(133139.	60 ticks, tree	= 1235.78	MB, soluti	ions = 6)
31337	-291.1340	219	-39.0000	-376.9744	12792486	866.60%
31430	-374.7112	1029	-39.0000	-376.9744	12799082	866.60%
32033	-116.6233	179	-39.0000	-376.9194	12782627	866.46%
32202	-357.4841	370	-39.0000	-376.9194	12958830	866.46%
32432	-103.9418	68	-39.0000	-376.9194	12967930	866.46%
31080	-370.9851	885	-39.0000	-376.9194	12828929	866.46%
1+31549			-40.0000	-376.919	94	842.30%
32626	-160.4344	119	-40.0000	-376.9194	12988233	842.30%
33736	-344.6369	244	-40.0000	-376.9194	13106949	842.30%
37235	-345.6706	331	-40.0000	-376.9194	13626666	842.30%
31438	-349.4261	701	-40.0000	-376.9194	12876494	842.30%
d time =	209.24 sec.	(171662.	93 ticks, tree	= 1199.03	MB, solut	ions = 7)
37432	-201.6757	314	-40.0000	-376.9194	13648219	842.30%
35758	-365.5130	684	-40.0000	-376.9194	13371629	842.30%
37682	-130.6639	94	-40.0000	-376.9194	13667768	842.30%
34391	-222.5263	261	-40.0000	-376.9194	13156341	842.30%
34575	-118.8445	76	-40.0000	-376.9194	13161634	842.30%
32867	-274.5121	285	-40.0000	-376.9194	13066188	842.30%
36351	-126.9557	87	-40.0000	-376.9194	13427861	842.30%
36429	-261.6947	186	-40.0000	-376.9194	13441222	842.30%
34630	-361.6861	651	-40.0000	-376.9194	13188259	842.30%
31799	-294.4002	652	-40.0000	-376.9194	12963851	842.30%
d time =	253.04 sec.	(209922.	64 ticks, tree	= 1190.36	MB, solut	ions = 7)
31813	-374.9630	885	-40.0000	-376.9194	12984867	842.30%
36555	-349.2594	626	-40.0000	-376.9194	13480838	842.30%
31966	-342.6780	723	-40.0000	-376.9194	13006011	842.30%
32052	-133.2492	96	-40.0000	-376.9194	13020291	842.30%
36670	-319.4597	209	-40.0000	-376.9194	13512903	842.30%
38194	infeasible		-40.0000	-376.9194	13776794	842.30%
36778	-351.9628	635	-40.0000	-376.9194	13531178	842.30%
	30814 30671 31494 31897 35065 31053 31958 31 time = 31337 31430 32033 32202 32432 31080 1+31549 32626 33736 37235 31438 31 time = 37432 35758 37432 35758 37432 35758 37432 35758 37432 35758 37432 3	30814 -374.2969 30671 cutoff 31494 -360.9840 31897 -85.7831 35065 -111.8791 31053 -356.1008 31958 -274.4820 31 time = 164.80 sec. 31337 -291.1340 31430 -374.7112 32033 -116.6233 32202 -357.4841 32432 -103.9418 31080 -370.9851 31+31549 32626 -160.4344 33736 -344.6369 37235 -345.6706 31438 -349.4261 31 time = 209.24 sec. 37432 -201.6757 35758 -365.5130 37682 -130.6639 34391 -222.5263 34575 -118.8445 32867 -274.5121 36351 -126.9557 36429 -261.6947 34630 -361.6861 31799 -294.4002 31 time = 253.04 sec. 31813 -374.9630 36555 -349.2594 31966 -342.6780 319.4597 38194 infeasible	30814 -374.2969 1033 30671 cutoff 31494 -360.9840 699 31897 -85.7831 53 35065 -111.8791 76 31053 -356.1008 650 31958 -274.4820 382 31437 -291.1340 219 31430 -374.7112 1029 31430 -374.7112 1029 32033 -116.6233 179 32202 -357.4841 370 32432 -103.9418 68 31080 -370.9851 885 31438 -344.6369 244 37235 -345.6706 331 31438 -349.4261 701 31 time = 209.24 sec. (171662.37432 -201.6757 314 35758 -365.5130 684 37682 -130.6639 94 34391 -222.5263 261 34575 -118.8445 76 32867 -274.5121 285 36351 -126.9557 87 36429 -261.6947 186 384575 -118.8445 76 38267 -274.5121 285 36351 -126.9557 87 36429 -261.6947 186 384630 -361.6861 651 381799 -294.4002 652 381813 -374.9630 885 386555 -349.2594 626 381966 -342.6780 723 38194 infeasible	30814 -374.2969 1033 -39.0000 30671 cutoff -39.0000 31494 -360.9840 699 -39.0000 315065 -111.8791 76 -39.0000 315065 -111.8791 76 -39.0000 31958 -274.4820 382 -39.0000 31958 -274.4820 382 -39.0000 314 time = 164.80 sec. (133139.60 ticks, tree 31337 -291.1340 219 -39.0000 31430 -374.7112 1029 -39.0000 32202 -357.4841 370 -39.0000 32432 -103.9418 68 -39.0000 31431549 -40.0000 31431549 -40.0000 31438 -344.6369 244 -40.0000 31438 -344.6369 244 -40.0000 31438 -349.4261 701 -40.0000 31438 -349.4261 701 -40.0000 315758 -365.5130 684 -40.0000 316168 -222.5263 261 -40.0000 31617 -222.5263 261 -40.0000 31617 -222.5263 261 -40.0000 31617 -222.5263 261 -40.0000 31617 -222.5263 261 -40.0000 31617 -222.5263 261 -40.0000 31799 -294.4002 652 -40.0000	38814 -374.2969 1033 -39.0000 -376.9744 380671 cutoff -39.0000 -376.9744 31494 -360.9840 699 -39.0000 -376.9744 31897 -85.7831 53 -39.0000 -376.9744 35065 -111.8791 76 -39.0000 -376.9744 31958 -274.4820 382 -39.0000 -376.9744 31430 -374.7112 1029 -39.0000 -376.9744 31430 -374.7112 1029 -39.0000 -376.9744 32033 -116.6233 179 -39.0000 -376.9194 32432 -103.9418 68 -39.0000 -376.9194 31430 -370.9851 885 -39.0000 -376.9194 31431549 -40.0000 -376.9194 3143549 -40.0000 -376.9194 31438 -344.6369 244 -40.0000 -376.9194 31438 -349.4261 701 -40.0000 -376.9194	30814 -374.2969 1033 -39.0000 -376.9744 12728929 30671 cutoff -39.0000 -376.9744 12724888 31494 -360.9840 699 -39.0000 -376.9744 12709907 31897 -85.7831 53 -39.0000 -376.9744 13253046 31053 -356.1008 650 -39.0000 -376.9744 12253046 31958 -274.4820 382 -39.0000 -376.9744 12935080 31430 -347.7112 1029 -39.0000 -376.9744 12792486 31430 -374.7112 1029 -39.0000 -376.9744 12792486 32023 -116.6233 179 -39.0000 -376.9194 12782627 32202 -357.4841 370 -39.0000 -376.9194 12958830 31080 -370.9851 885 -39.0000 -376.9194 1298283 31366 -160.4344 119 -40.0000 -376.9194 12982823 37376

```
59775 33722
              -371.4617
                        918
                                  -40.0000
                                              -376.9194 13181426 842.30%
                                  -40.0000
59948 36900
              -366.2275 661
                                              -376.9194 13549234 842.30%
60447 32460
                                  -40.0000
                                              -376.9194 13080118 842.30%
              -335.7909
                        735
Elapsed time = 296.23 sec. (248581.39 ticks, tree = 1274.28 MB, solutions = 7)
60791 37101
              -185.5764
                         181
                                  -40.0000
                                              -376.9194 13570876 842.30%
61392 34217
              -374.0933
                        734
                                  -40.0000
                                              -376.9194 13219253 842.30%
              -363.2180
62039 36439
                                 -40.0000
                                              -376.9194 13336882 842.30%
                        698
62196 36566
              -46.5830
                          229
                                  -40.0000
                                              -376.9194 13345567 842.30%
62482 34472
              -340.0144
                        758
                                  -40.0000
                                              -376.9194 13248238 842.30%
```

Began writing nodes to disk (directory ./cpxhGkJOU created)

GUB cover cuts applied: 872

Clique cuts applied: 53 Cover cuts applied: 3794

Implied bound cuts applied: 59

Flow cuts applied: 95

Mixed integer rounding cuts applied: 1264

Zero-half cuts applied: 118

Lift and project cuts applied: 8

Gomory fractional cuts applied: 197

Root node processing (before b&c):

Real time = 0.00 sec. (0.68 ticks)

Parallel b&c, 8 threads:

Real time = 316.13 sec. (270209.62 ticks)

Sync time (average) = 21.13 sec. Wait time (average) = 0.00 sec.

Total (root+branch&cut) = 316.14 sec. (270210.30 ticks)

Iteration 7

Bounds on # of cuts = 8 with [3 3 2]

Error = 60 (out of 100 instances)

Accuracy = 40

Solving time = 5.268966785 min (minutes)

Accumulated time = 18.655460417 min (minutes)

Solution status code = 104

LB on error = -276.833555011
Relative objective gap = 8.420838875

Selected variables:

PEMLR (Categorical)

SS_YN (Categorical)

62722 56376

62904 56365

62969 56414

63094 56358

-285.1413

-320.2108

-207.5316

-361.8225

212

319

159

455

Number of selected variables = 2 (0 continuous + 2 categorical)

Version identifier: 22.1.1.0 | 2022-11-28 | 9160aff4d

CPXPARAM_MIP_Strategy_File 3

CPXPARAM_MIP_Limits_Solutions 1

CPXPARAM_TimeLimit 85280.672374999995

CPXPARAM_MIP_Limits_TreeMemory 204800

Cuts/ Nodes Node Left Objective IInf Best Integer Best Bound ItCnt Gap 62493 56328 -371.5512 -40.0000 -376.8336 16793405 842.08% 875 Elapsed time = 1.28 sec. (381.47 ticks, tree = 2553.13 MB, solutions = 7) Nodefile size = 505.19 MB (457.73 MB after compression) 62494 56329 -371.1453 802 -40.0000 -376.8336 16795022 842.08% 62497 56331 -371.0317 -40.0000 -376.8336 16796271 842.08% 798 62498 56328 -40.0000 -376.8336 16797169 842.08% -368.1504 812 62512 56334 -374.4435 -40.0000 -376.8336 16798167 842.08% 690 62525 56343 -367.3256 732 -40.0000 -376.8336 16801668 842.08% 62532 56335 -369.7631 729 -40.0000 -376.8336 16799811 842.08% 62542 56346 -40.0000 -376.8336 16803611 842.08% infeasible 62547 56350 -365.8593 652 -40.0000 -376.8336 16804496 842.08% 62560 56356 -364.8589 634 -40.0000 -376.8336 16805402 842.08% 62618 56340 705 -40.0000 -376.8336 16804652 842.08% -373.4930 Elapsed time = 5.50 sec. (4460.10 ticks, tree = 2546.50 MB, solutions = 7) Nodefile size = 505.19 MB (457.73 MB after compression) 62639 56342 -376.2051 -40.0000 -376.8205 16808904 842.05% 828 62665 56385 -373.6476 -40.0000 439 -376.8205 16811958 842.05%

-40.0000

-40.0000

-40.0000

-40.0000

-376.8205 16814049 842.05%

-376.8205 16832674 842.05%

-376.8205 16836614 842.05%

-376.8205 16829520 842.05%

63139 56390	-350.5564	411	-40.0000	-376.8205 16833177	842.05%
63164 56347	-366.7584	820	-40.0000	-376.8205 16827937	842.05%
63232 56547	-261.9177	265	-40.0000	-376.8205 16828650	842.05%
63383 56506	-372.3550	659	-40.0000	-376.8205 16845155	842.05%
Elapsed time =	17.85 sec.	(15002.70	ticks, tree =	2538.21 MB, solutio	ns = 7)
Nodefile size =	505.19 MB	(457.73 MB	after compre	ssion)	
63431 56370	-361.1593	662	-40.0000	-376.8205 16836599	842.05%
63518 56528	-366.3616	580	-40.0000	-376.8205 16851365	842.05%
63551 56668	-372.7898	614	-40.0000	-376.8205 16838522	842.05%
63617 56356	infeasible		-40.0000	-376.8205 16847550	842.05%
63657 56433	-373.2525	857	-40.0000	-376.5778 16842129	841.44%
63720 56584	infeasible		-40.0000	-376.5778 16866006	841.44%
63742 56708	-347.8130	343	-40.0000	-376.5778 16851562	841.44%
63817 56407	-372.9694	713	-40.0000	-376.5778 16853277	841.44%
63875 56438	-336.4001	379	-40.0000	-376.5778 16856671	841.44%
63937 56457	-370.4856	719	-40.0000	-376.5778 16855716	841.44%
Elapsed time =	29.24 sec.	(24884.76	ticks, tree =	2542.06 MB, solutio	ns = 7)
Nodefile size =	505.19 MB	(457.73 MB	after compre	ssion)	
63986 56760	-361.2265	352	-40.0000	-376.5778 16863808	841.44%
* 64088+56788			-42.0000	-376.5778	796.61%
64161 56427	-308.4527	287	-42.0000	-376.5778 16861750	796.61%
64305 56426	-364.4031	448	-42.0000	-376.5778 16867050	796.61%
64344 56429	cutoff		-42.0000	-376.5778 16870294	796.61%
64408 56433	-361.1858	402	-42.0000	-376.5778 16864366	796.61%
64514 56592	-369.9594	867	-42.0000	-376.5778 16880737	796.61%
64661 56555	-117.7107	86	-42.0000	-376.5778 16881851	796.61%
64713 56603	-366.8417	779	-42.0000	-376.5778 16886930	796.61%
64780 56605	-366.4698	401	-42.0000	-376.5778 16885487	796.61%
64920 56444	-257.3129	304	-42.0000	-376.5778 16880818	796.61%
<pre>Elapsed time =</pre>	40.45 sec.	(34952.40	ticks, tree =	2527.61 MB, solutio	ns = 8)
Nodefile size =	= 505.19 MB	(457.73 MB	after compre	ssion)	
65008 56483	-373.2735	748	-42.0000	-376.5778 16879719	796.61%
65038 56496	-371.2082	756	-42.0000	-376.5778 16884054	796.61%
65110 56516	-350.0730	368	-42.0000	-376.5778 16888980	796.61%
65158 56558	-235.2681	191	-42.0000	-376.5778 16892346	796.61%
65285 56665	-371.7312	780	-42.0000	-376.5778 16902786	796.61%
65319 56612	-366.8891	1013	-42.0000	-376.5778 16899193	796.61%
65328 56515	-369.2649	813	-42.0000	-376.5778 16898243	796.61%
65349 56619	-365.9130	961	-42.0000	-376.5778 16903443	796.61%

```
65377 56656
               -374.9636
                          869
                                    -42.0000
                                                 -376.5778 16903553 796.61%
65461 56566
               -354.8815
                           435
                                    -42.0000
                                                 -376.5778 16906832 796.61%
Elapsed time = 51.75 sec. (45094.74 ticks, tree = 2537.59 MB, solutions = 8)
Nodefile size = 505.19 MB (457.73 MB after compression)
65538 56652
               -352.6881
                                     -42.0000
                                                 -376.5778 16912258 796.61%
                           414
65579 56663
               -373.6537
                           807
                                    -42.0000
                                                 -376.5778 16911756 796.61%
65603 56591
               -375.1709
                           881
                                    -42.0000
                                                 -376.5778 16912590 796.61%
65614 56685
               -368.6663
                           587
                                    -42.0000
                                                 -376.5778 16926075 796.61%
65654 56606
               -326.8965
                           270
                                    -42.0000
                                                 -376.5778 16919118 796.61%
65840 56689
               -344.0531
                           352
                                    -42.0000
                                                 -376.5778 16932035 796.61%
                                                 -376.5778 16935329 796.61%
65863 56702
               -353.1667
                           420
                                    -42.0000
                                                 -376.5778 16938567 796.61%
65889 56719
               -319.7314
                           372
                                    -42.0000
65911 56725
               -322.5031
                                    -42.0000
                                                 -376.5778 16941732 796.61%
                           341
65958 56694
                -373.2894 1005
                                     -42.0000
                                                  -376.5778 16931254 796.61%
Elapsed time = 62.90 sec. (55166.59 ticks, tree = 2544.63 MB, solutions = 8)
Nodefile size = 505.19 MB (457.73 MB after compression)
65997 56768
               -253.7349
                           280
                                     -42.0000
                                                  -376.5778 16947850 796.61%
66033 56799
               -200.2774
                           224
                                    -42.0000
                                                 -376.5778 16951162 796.61%
66088 56579
               -363.1327
                           912
                                    -42.0000
                                                  -376.5778 16939742 796.61%
66104 56529
               -366.7705
                           832
                                    -42.0000
                                                 -376.5778 16919965 796.61%
               -363.5003
                                    -42.0000
                                                 -376.5778 16923506 796.61%
66121 56540
                           629
66256 56603
               -333.1568
                                    -42.0000
                                                 -376.5778 16927307 796.61%
                           482
                                                 -376.5778 16950761 796.61%
66353 56781
               -358.3175
                           407
                                    -42.0000
66420 56807
               -333.2784
                           378
                                    -42.0000
                                                 -376.5778 16954452 796.61%
66540 56939
               -273.2919
                           280
                                     -42.0000
                                                 -376.5778 16973671 796.61%
66663 56741
               -346.7942
                            445
                                     -42.0000
                                                 -376.5778 16960552 796.61%
Elapsed time = 74.45 sec. (65498.15 ticks, tree = 2558.25 MB, solutions = 8)
Nodefile size = 505.19 MB (457.73 MB after compression)
66746 56738
               -367.2268
                           477
                                     -42.0000
                                                  -376.5778 16960134 796.61%
67127 56776
                                                 -376.5778 16968251 796.61%
               -342.2970
                           517
                                    -42.0000
                                                 -376.5778 16983874 796.61%
67238 56999
               -371.4690
                           752
                                    -42.0000
67266 57021
               -333.9642
                           341
                                    -42.0000
                                                 -376.5778 16987177
                                                                     796.61%
67424 56898
                -76.4479
                                    -42.0000
                                                 -376.5778 16978530 796.61%
                           160
                                                 -376.5778 16993918 796.61%
67530 57053
               -373.1439
                           621
                                    -42.0000
67784 57039
                -91.9323
                            75
                                    -42.0000
                                                 -376.5778 16976965
                                                                     796.61%
67923 57209
               -374.6908
                           824
                                    -42.0000
                                                 -376.5778 17000708 796.61%
67941 56855
               -372.2216
                            428
                                     -42.0000
                                                 -376.5778 16977830 796.61%
68103 56928
               -331.4462
                            469
                                     -42.0000
                                                 -376.5778 16990292 796.61%
Elapsed time = 85.79 sec. (75199.50 ticks, tree = 2566.21 MB, solutions = 8)
```

Nodefile size = 505.19 MB	(457.73 MB afte	r compression)	
68294 56955 -247.9800	326 -42.	0000 -376.5778	16984262 796.61%
68361 56926 infeasible	-42.	0000 -376.5778	16995251 796.61%
68454 56941 -342.9196	259 -42.	0000 -376.5778	16998376 796.61%
68580 56992 -249.5999	176 -42.	0000 -376.5778	17002343 796.61%
68785 57111 -334.3761	321 -42.	0000 -376.5778	16998461 796.61%
68946 56636 -370.2219	1051 -42.	0000 -376.5778	16959597 796.61%
68960 57248 infeasible	-42.	0000 -376.5778	17004796 796.61%
69028 57254 infeasible	-42.	0000 -376.5778	17007632 796.61%
69137 57046 cutoff	-42.	0000 -376.5778	17011825 796.61%
69146 57258 -374.6623	732 -42.	0000 -376.5778	17013586 796.61%
Elapsed time = 96.76 sec.	(84893.06 ticks	, tree = 2553.89 M	B, solutions = 8)
Nodefile size = 505.19 MB	(457.73 MB afte	r compression)	
69174 57079 -374.6247	714 -42.	0000 -376.5778	17010021 796.61%
69379 57535 -154.2234	96 -42.	0000 -376.5778	17040415 796.61%
69542 57048 -351.2630	495 -42.	0000 -376.5778	17024459 796.61%
69611 57092 -249.8471	236 -42.	0000 -376.5778	17027482 796.61%
69791 57123 -266.5293	180 -42.	0000 -376.5778	17021100 796.61%
69896 57588 infeasible	-42.	0000 -376.5778	17051599 796.61%
69900 57201 -372.7224	744 -42.	0000 -376.5778	17026463 796.61%
69921 57253 -355.6185	324 -42.	0000 -376.5778	17037474 796.61%
70000 57290 -294.2659	218 -42.	0000 -376.5778	17038577 796.61%
70742 57498 -268.3576	172 -42.	0000 -376.5778	17052046 796.61%
Elapsed time = 111.68 sec	. (97530.70 tick	s, tree = 2556.97	MB, solutions = 9)
Nodefile size = 505.19 MB	(457.73 MB afte	r compression)	
71350 57728 -348.3798	248 -42.	0000 -376.5778	17063553 796.61%
71743 57460 -373.4932	966 -42.	0000 -376.5778	17049682 796.61%
71755 57653 -370.4464	636 -42.	0000 -376.5778	17078692 796.61%
72187 57551 -215.6947	184 -42.	0000 -376.5778	17066389 796.61%
72276 57850 -367.7073	661 -42.	0000 -376.5778	17096223 796.61%
72618 57937 -157.8367	118 -42.	0000 -376.5778	17107344 796.61%
73589 58103 -366.4535	645 -42.	0000 -376.5778	17117318 796.61%
74114 58372 -220.1499	157 -42.	0000 -376.5778	17127622 796.61%
74271 57688 -366.0440	1022 -42.	0000 -376.5778	17107476 796.61%
74330 58468 -278.5357	406 -42.	0000 -376.5778	17158803 796.61%
Elapsed time = 151.49 sec	. (136817.80 tic	ks, tree = 2572.25	MB, solutions = 9)
Nodefile size = 505.19 MB	(457.73 MB afte	r compression)	
74466 57137 -373.4744	786 -42.	0000 -376.5778	17075738 796.61%
74579 57229 -125.4892	163 -42.	0000 -376.5778	17083210 796.61%

74997 58823	-124.1569	77	-42.0000	-376.5778 17191261 796.6	1%
75138 57699	-351.9220	642	-42.0000	-376.5778 17150191 796.6	1%
75183 57727	-312.4915	310	-42.0000	-376.5778 17159655 796.6	1%
75598 57528	cutoff		-42.0000	-376.5778 17113472 796.6	1%
75757 57645	-372.7641	917	-42.0000	-376.5778 17123059 796.6	1%
75781 57652	-363.8514	654	-42.0000	-376.5778 17133198 796.6	1%
75914 57770	-368.0621	641	-42.0000	-376.5778 17141831 796.6	1%
76307 57888	-367.1160	710	-42.0000	-376.5778 17151066 796.6	1%
Elapsed time =	182.24 sec.	(17663	2.97 ticks, tre	e = 2640.89 MB, solutions =	10)
Nodefile size	= 505.19 MB	(457.73	MB after compre	ession)	
76625 58372	-276.7328	275	-42.0000	-376.5778 17215778 796.6	1%
76896 58881	-363.3072	789	-42.0000	-376.5778 17266359 796.6	1%
77088 58341	-205.9310	178	-42.0000	-376.5778 17178206 796.6	1%
77452 58913	-289.3936	190	-42.0000	-376.5778 17282930 796.6	1%
77896 58805	-59.1187	71	-42.0000	-376.5778 17249555 796.6	1%
78198 58777	-104.5215	100	-42.0000	-376.5778 17202653 796.6	1%
78213 58926	-368.4008	652	-42.0000	-376.5778 17267554 796.6	1%
78401 58786	-372.5803	1028	-42.0000	-376.5778 17218675 796.6	1%
78547 59186	-304.1862	222	-42.0000	-376.5778 17287687 796.6	1%
78819 59304	-355.0582	246	-42.0000	-376.5778 17297787 796.6	1%
				010.0110 11201101 100.0	
Elapsed time =				e = 2715.45 MB, solutions =	
-	213.20 sec.	(21619		e = 2715.45 MB, solutions =	
-	213.20 sec.	(21619	3.23 ticks, tre	e = 2715.45 MB, solutions = ession)	
Nodefile size	213.20 sec.	(21619	3.23 ticks, tree	e = 2715.45 MB, solutions = ession)	11) .76%
Nodefile size * 78861+59332	213.20 sec. = 505.19 MB	(216193) (457.73) 923	3.23 ticks, tree MB after compre -43.0000 -43.0000	e = 2715.45 MB, solutions = ession) -376.5778 775	11) .76%
Nodefile size : * 78861+59332 78863 58919	213.20 sec. = 505.19 MB -372.1730 -362.0419	(216193 (457.73 923 695	3.23 ticks, tree MB after compre -43.0000 -43.0000	e = 2715.45 MB, solutions = ession) -376.5778 775 -376.5778 17245546 775.76 -376.5778 17262028 775.76	11) .76% 6%
* 78861+59332 * 78863 58919 78865 58921	213.20 sec. = 505.19 MB -372.1730 -362.0419 -287.4919	(216193 (457.73 923 695 224	3.23 ticks, tree MB after compre -43.0000 -43.0000 -43.0000 -43.0000	e = 2715.45 MB, solutions = ession) -376.5778 775 -376.5778 17245546 775.76 -376.5778 17262028 775.76 -376.5778 17274297 775.76	11) .76% 6% 6%
* 78861+59332 * 78863 58919 78865 58921 78908 58961	213.20 sec. = 505.19 MB -372.1730 -362.0419 -287.4919 -351.1997	(216193 (457.73) 923 695 224 373	3.23 ticks, tree MB after compre -43.0000 -43.0000 -43.0000 -43.0000	e = 2715.45 MB, solutions = ession) -376.5778	11) .76% 6% 6% 6%
* 78861+59332 * 78863 58919 78865 58921 78908 58961 79046 59079	213.20 sec. = 505.19 MB -372.1730 -362.0419 -287.4919 -351.1997 -136.6352	(216193 (457.73) 923 695 224 373 93	3.23 ticks, tree MB after compre -43.0000 -43.0000 -43.0000 -43.0000 -43.0000	e = 2715.45 MB, solutions = ession) -376.5778	11) .76% 6% 6% 6% 6%
* 78861+59332 * 78863 58919 78865 58921 78908 58961 79046 59079 79251 59269	213.20 sec. = 505.19 MB -372.1730 -362.0419 -287.4919 -351.1997 -136.6352 -331.8259	(216193 (457.73) 923 695 224 373 93 277	3.23 ticks, tree MB after compre -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000	e = 2715.45 MB, solutions = ession) -376.5778	11) .76% 6% 6% 6% 6%
* 78861+59332 * 78863 58919 78865 58921 78908 58961 79046 59079 79251 59269 79485 59473	213.20 sec. = 505.19 MB -372.1730 -362.0419 -287.4919 -351.1997 -136.6352 -331.8259 -368.4471	(216193 (457.73) 923 695 224 373 93 277 613	3.23 ticks, tree MB after compre -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000	e = 2715.45 MB, solutions = ession) -376.5778	11) .76% 6% 6% 6% 6% 6% 6%
* 78861+59332 * 78863 58919 78863 58921 78865 58921 78908 58961 79046 59079 79251 59269 79485 59473 79610 59575	213.20 sec. = 505.19 MB -372.1730 -362.0419 -287.4919 -351.1997 -136.6352 -331.8259 -368.4471 -235.4136	(216193 (457.73) 923 695 224 373 93 277 613 155	3.23 ticks, tree MB after compre -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000	e = 2715.45 MB, solutions = ession) -376.5778	11) .76% 6% 6% 6% 6% 6% 6%
* 78861+59332 * 78863 58919 78863 58919 78865 58921 78908 58961 79046 59079 79251 59269 79485 59473 79610 59575 79779 59736 79874 59817	213.20 sec. = 505.19 MB -372.1730 -362.0419 -287.4919 -351.1997 -136.6352 -331.8259 -368.4471 -235.4136 infeasible	(216193 (457.73) 923 695 224 373 93 277 613 155	3.23 ticks, tree MB after compre -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000	e = 2715.45 MB, solutions = ession) -376.5778	11) .76% 6% 6% 6% 6% 6% 6% 6%
* 78861+59332 * 78861+59332 78863 58919 78865 58921 78908 58961 79046 59079 79251 59269 79485 59473 79610 59575 79779 59736 79874 59817 79976 59913	213.20 sec. = 505.19 MB -372.1730 -362.0419 -287.4919 -351.1997 -136.6352 -331.8259 -368.4471 -235.4136 infeasible -352.6447	(216193 (457.73) 923 695 224 373 93 277 613 155	3.23 ticks, tree MB after compre -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000	e = 2715.45 MB, solutions = ession) -376.5778	11) .76% 6% 6% 6% 6% 6% 6% 6% 6%
Nodefile size : * 78861+59332 78863 58919 78865 58921 78908 58961 79046 59079 79251 59269 79485 59473 79610 59575 79779 59736 79874 59817 79976 59913 Elapsed time =	213.20 sec. = 505.19 MB -372.1730 -362.0419 -287.4919 -351.1997 -136.6352 -331.8259 -368.4471 -235.4136 infeasible -352.6447 240.73 sec.	(216193 (457.73) 923 695 224 373 93 277 613 155	3.23 ticks, tree MB after compre -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000	e = 2715.45 MB, solutions = ession) -376.5778	11) .76% 6% 6% 6% 6% 6% 6% 6% 6%
Nodefile size : * 78861+59332 78863 58919 78865 58921 78908 58961 79046 59079 79251 59269 79485 59473 79610 59575 79779 59736 79874 59817 79976 59913 Elapsed time =	213.20 sec. = 505.19 MB -372.1730 -362.0419 -287.4919 -351.1997 -136.6352 -331.8259 -368.4471 -235.4136 infeasible -352.6447 240.73 sec. = 505.19 MB	(216193 (457.73) 923 695 224 373 93 277 613 155 359 (260469 (457.73)	3.23 ticks, tree MB after compre -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000	e = 2715.45 MB, solutions = ession) -376.5778	11) .76% 6% 6% 6% 6% 6% 6% 6% 6% 12)
* 78861+59332 * 78861+59332 78863 58919 78865 58921 78908 58961 79046 59079 79251 59269 79485 59473 79610 59575 79779 59736 79874 59817 79976 59913 Elapsed time = Nodefile size = 80225 60135	213.20 sec. = 505.19 MB -372.1730 -362.0419 -287.4919 -351.1997 -136.6352 -331.8259 -368.4471 -235.4136 infeasible -352.6447 240.73 sec. = 505.19 MB -351.0370	(216193 (457.73) 923 695 224 373 93 277 613 155 359 (260463 (457.73) 334	MB after compre-43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000	e = 2715.45 MB, solutions = ession) -376.5778	11) .76% 6% 6% 6% 6% 6% 6% 6% 6% 6%
* 78861+59332 * 78861+59332 78863 58919 78865 58921 78908 58961 79046 59079 79251 59269 79485 59473 79610 59575 79779 59736 79874 59817 79976 59913 Elapsed time = Nodefile size = 80225 60135 80482 60367	213.20 sec. = 505.19 MB -372.1730 -362.0419 -287.4919 -351.1997 -136.6352 -331.8259 -368.4471 -235.4136 infeasible -352.6447 240.73 sec. = 505.19 MB -351.0370 -372.6844	(216193 (457.73) 923 695 224 373 93 277 613 155 359 (260463 (457.73) 334 1128	3.23 ticks, tree MB after compre -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 9.65 ticks, tree MB after compre -43.0000 -43.0000	e = 2715.45 MB, solutions = ession) -376.5778	11) .76% 6% 6% 6% 6% 6% 6% 6% 6% 6% 6%
* 78861+59332 * 78861+59332 78863 58919 78865 58921 78908 58961 79046 59079 79251 59269 79485 59473 79610 59575 79779 59736 79874 59817 79976 59913 Elapsed time = Nodefile size = 80225 60135 80482 60367	213.20 sec. = 505.19 MB -372.1730 -362.0419 -287.4919 -351.1997 -136.6352 -331.8259 -368.4471 -235.4136 infeasible -352.6447 240.73 sec. = 505.19 MB -351.0370 -372.6844 -370.6348	(216193 (457.73) 923 695 224 373 93 277 613 155 359 (260463 (457.73) 334 1128 854	3.23 ticks, tree MB after compre -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000 -43.0000	e = 2715.45 MB, solutions = ession) -376.5778	11) .76% 6% 6% 6% 6% 6% 6% 6% 6% 6% 6% 6%

8	30618	60496	-366.6781	671	-43.0000	-376.5778	17414997	775.76%
8	80896	60756	cutoff		-43.0000	-376.5778	17426348	775.76%
8	31024	60865	-368.8018	769	-43.0000	-376.5778	17439191	775.76%
8	31161	60978	infeasible		-43.0000	-376.5778	17452029	775.76%
8	31372	61172	-368.2417	708	-43.0000	-376.5778	17463161	775.76%

GUB cover cuts applied: 916
Clique cuts applied: 53

Cover cuts applied: 3875

Implied bound cuts applied: 59

Flow cuts applied: 100

Mixed integer rounding cuts applied: 1398

Zero-half cuts applied: 121

Lift and project cuts applied: 9
Gomory fractional cuts applied: 198

Root node processing (before b&c):

Real time = 0.00 sec. (0.97 ticks)

Parallel b&c, 8 threads:

Real time = 278.62 sec. (311816.15 ticks)

Sync time (average) = 11.93 sec.

Wait time (average) = 0.00 sec.

Total (root+branch&cut) = 278.62 sec. (311817.12 ticks)

 ${\tt Iteration} \ {\tt 8}$

Bounds on # of cuts = 8 with [3 3 2]

Error = 57 (out of 100 instances)

Accuracy = 43

Solving time = 4.643691231 min (minutes)

Accumulated time = 23.299151648 min (minutes)

Solution status code = 104

LB on error = -276.380316895

Relative objective gap = 7.753030625

Selected variables:

PEMLR (Categorical)

SS_YN (Categorical)

Number of selected variables = 2 (0 continuous + 2 categorical)

Version identifier: 22.1.1.0 | 2022-11-28 | 9160aff4d CPXPARAM_MIP_Strategy_File 3 CPXPARAM_MIP_Limits_Solutions 1

CPXPARAM_TimeLimit 85002.050901123046

CPXPARAM_MIP_Limits_TreeMemory 204800

Nodes				Cuts/		
Node Left	Objective	IInf Best	Integer	Best Bound	ItCnt	Gap
81435 71926	-369.0867	475	-43.0000	-376.3803	19472128	775.30%
Elapsed time =	3.10 sec. (2384.36 ti	cks, tree	= 3375.96 MB,	solutions	= 13)
Nodefile size	= 1328.84 MB	(1208.58	MB after c	ompression)		
81438 71929	-351.7855	242	-43.0000	-376.3803	19472768	775.30%
81471 71961	-270.8111	173	-43.0000	-376.3803	19473216	775.30%
81515 72001	-157.5837	98	-43.0000	-376.3803	19473641	775.30%
81563 71926	-374.3382	753	-43.0000	-376.3803	19473609	775.30%
81564 71928	-372.4402	715	-43.0000	-376.3803	19481748	775.30%
81567 71930	-371.4346	663	-43.0000	-376.3803	19482880	775.30%
81571 71933	-371.2108	644	-43.0000	-376.3803	19483675	775.30%
81572 71934	-370.7107	636	-43.0000	-376.3803	19484433	775.30%
81576 71931	-360.4175	763	-43.0000	-376.3803	19502020	775.30%
81661 72012	-144.5408	107	-43.0000	-376.3803	19488685	775.30%
Elapsed time =	9.37 sec. (7373.28 ti	cks, tree	= 3370.21 MB,	solutions	= 13)
Nodefile size	= 1328.84 MB	(1208.58	MB after c	ompression)		
81706 72044	-358.3163	625	-43.0000	-376.3803	19488229	775.30%
81757 72071	-303.3940	260	-43.0000	-376.3803	19492258	775.30%
82046 72027	-154.9862	247	-43.0000	-376.3803	19515571	775.30%
82190 72089	-266.6773	179	-43.0000	-376.3803	19502642	775.30%
82339 72085	-249.3634	162	-43.0000	-376.3803	19503964	775.30%
82548 71934	-359.2701	768	-43.0000	-376.3803	19543860	775.30%
82551 71937	-357.5116	530	-43.0000	-376.3803	19547438	775.30%
82574 71952	-339.6193	324	-43.0000	-376.3803	19550709	775.30%
82657 72026	-155.4003	164	-43.0000	-376.3803	19552766	775.30%
82707 72064	-355.4909	247	-43.0000	-376.3803	19555144	775.30%
Elapsed time =	23.10 sec.	(18322.56	ticks, tre	e = 3345.19 M	B, solution	ns = 13)

Nodefile size =	: 1328.84 MB (1208	3.58 MB after com	nression)	
82804 72154	-136.7153 96	-43.0000	-376.3527 19557777	775.24%
82850 72307	-360.9410 741	-43.0000	-376.3527 19521065	775.24%
82855 72311	-342.6034 249	-43.0000	-376.1368 19523927	774.74%
82983 71936	-362.8146 626	-43.0000	-376.1368 19553992	774.74%
82985 72161	-371.0562 970	-43.0000	-376.1368 19520957	774.74%
82987 72193	-374.9001 951	-43.0000	-376.1368 19562191	774.74%
82993 71941	-358.9686 430	-43.0000	-376.1368 19567870	774.74%
82999 71946	-348.8783 255	-43.0000	-376.1368 19572436	774.74%
83050 71987	-258.2577 225	-43.0000	-376.1368 19574685	774.74%
83115 72047	-106.9395 149	-43.0000	-376.1368 19575766	774.74%
Elapsed time =	35.85 sec. (2897	7.15 ticks, tree =	= 3351.66 MB, solutio	ns = 13)
Nodefile size =	1328.84 MB (1208	3.58 MB after com	pression)	
83146 72066	infeasible	-43.0000	-376.1368 19578155	774.74%
83150 72197	-355.5337 338	-43.0000	-376.1368 19576926	774.74%
83255 72221	-222.3896 129	-43.0000	-376.1368 19540293	774.74%
83429 72318	cutoff	-43.0000	-376.1368 19579829	774.74%
83434 72191	-359.3736 818	-43.0000	-376.1368 19542416	774.74%
83449 72287	-371.6337 619	-43.0000	-376.1368 19550427	774.74%
83487 72317	-265.8980 174	-43.0000	-376.1368 19553782	774.74%
83744 72447	-333.6008 253	-43.0000	-376.1368 19553268	774.74%
83839 72511	-194.0038 122	-43.0000	-376.1368 19554512	774.74%
83950 72252	-192.8584 143	-43.0000	-376.1368 19555244	774.74%
Elapsed time =	48.25 sec. (3935	4.87 ticks, tree	= 3364.70 MB, solutio	ns = 13)
Nodefile size =	1328.84 MB (1208	3.58 MB after comp	pression)	
84017 72081	-354.4707 699	-43.0000	-376.1368 19578452	774.74%
84023 72069	-366.0459 957	-43.0000	-376.1368 19597048	774.74%
84036 71956	-348.2522 252	-43.0000	-376.1368 19588460	774.74%
84184 72414	-333.2872 216	-43.0000	-376.1368 19572926	774.74%
84316 72094	-351.1716 513	-43.0000	-376.1368 19591693	774.74%
84492 72137	-253.3089 162	-43.0000	-376.1368 19595305	774.74%
84589 72520	-372.8630 619	-43.0000	-376.1368 19581721	774.74%
84631 72559	-273.3236 176	-43.0000	-376.1368 19584387	774.74%
84755 72337	-342.0960 228	-43.0000	-376.1368 19606229	774.74%
84999 72657	-350.7128 344	-43.0000	-376.1368 19589927	774.74%
Elapsed time =	59.71 sec. (4948)	3.74 ticks, tree	= 3372.85 MB, solutio	ns = 13)
Nodefile size =	1328.84 MB (1208	3.58 MB after comp	pression)	
85177 72284	-200.4956 128	-43.0000	-376.1368 19608089	774.74%
85252 72564	-366.6790 841	-43.0000	-376.1368 19577339	774.74%

85269 72536	infeasible	-43.0000	-376.1368 19591276 774.74	
85318 72802		79 -43.0000	-376.1368 19598160 774.74	
85458 72106		04 -43.0000	-376.1368 19630436 774.74	
85583 72343		35 -43.0000	-376.1368 19620884 774.74	1%
85753 72537	-368.2100 8	67 -43.0000	-376.1368 19598411 774.74	1%
85869 72101	-319.9908 2	-43.0000	-376.1368 19628379 774.74	1%
86144 72573	-271.7490 1	96 -43.0000	-376.1368 19604341 774.74	1%
86291 72116	-306.6315 3	-43.0000	-376.1368 19628397 774.74	1%
Elapsed time =	72.00 sec. (59	610.39 ticks, tre	ee = 3339.28 MB, solutions = 13	3)
Nodefile size	= 1328.84 MB (1	208.58 MB after o	compression)	
86447 72541	-125.2543	-43.0000	-376.1368 19631988 774.74	1%
86788 72227	-46.0606 1	74 -43.0000	-376.1368 19635812 774.74	1 %
86904 72855	-90.1545	-43.0000	-376.1368 19614400 774.74	1%
86987 72371	-183.6352 1	-43.0000	-376.1368 19641703 774.74	1%
87059 72230	-371.5048 6	94 -43.0000	-376.1368 19641837 774.74	1 %
87140 72762	-210.2776 1	-43.0000	-376.1368 19616474 774.74	1%
87328 72220	-366.7426 6	-43.0000	-376.1368 19654622 774.74	1%
87338 72227	-342.5130 2	-43.0000	-376.1368 19658216 774.74	1%
87497 73022	-331.2281 3	15 -43.0000	-376.1368 19630982 774.74	1%
87569 73080	-184.5925 1	-43.0000	-376.1368 19631567 774.74	1%
Elapsed time =	83.56 sec. (69	415.07 ticks, tre	ee = 3374.71 MB, solutions = 13	3)
Nodefile size	= 1328.84 MB (1	208.58 MB after o	compression)	
87722 72426	-196.0292 3	-43.0000	-376.1368 19658817 774.74	1%
87813 72470	-313.7015 2	24 -43.0000	-376.1368 19657117 774.74	1%
88010 73139	-332.3763 2	-43.0000	-376.1368 19638071 774.74	1%
88193 72344	-369.2216 68	-43.0000	-376.1368 19671787 774.74	1%
88226 72439	-344.1819 3	06 -43.0000	-376.1368 19663453 774.74	1%
88382 73331	-108.0697	65 -43.0000	-376.1368 19645596 774.74	1%
88585 72524	-154.1781 1	03 -43.0000	-376.1368 19666440 774.74	1%
88643 72580	-341.4974 3	85 -43.0000	-376.1368 19679295 774.74	1%
88686 72613	-276.5086 2	21 -43.0000	-376.1368 19683720 774.74	1%
88853 73404	-204.9500 1	46 -43.0000	-376.1368 19657466 774.74	1%
Elapsed time =	96.42 sec. (79	164.76 ticks, tre	ee = 3376.03 MB, solutions = 13	3)
Nodefile size	= 1328.84 MB (1	208.58 MB after (compression)	
88930 72572		28 -43.0000	-	1%
88947 72490		94 -43.0000		1%
89059 72630		37 -43.0000		
89353 73556		16 -43.0000		
89437 72881		80 -43.0000		
				.•

```
89803 72768
               -138.0596
                            89
                                     -43.0000
                                                 -376.1368 19686828 774.74%
90099 73621
               -369.2874
                            668
                                     -43.0000
                                                 -376.1368 19676578 774.74%
90187 72870
                                     -43.0000
                                                 -376.1368 19692884 774.74%
               -145.8195
                            96
90391 72907
                                     -43.0000
                                                  -376.1368 19696002 774.74%
               -350.2219
                            270
90568 72953
                                     -43.0000
                                                  -376.1368 19699570 774.74%
               -260.3118
                            162
Elapsed time = 107.23 sec. (88918.59 ticks, tree = 3355.42 MB, solutions = 13)
Nodefile size = 1328.84 MB (1208.58 MB after compression)
90747 73000
                                                  -376.1368 19670487 774.74%
               -232.2603
                                     -43.0000
                            144
90865 73685
               -212.0829
                            144
                                     -43.0000
                                                  -376.1368 19685798 774.74%
91021 73711
               -147.6431
                            128
                                     -43.0000
                                                  -376.1368 19686698 774.74%
91106 73041
                                                 -376.1368 19662197 774.74%
               -279.0274
                            184
                                     -43.0000
91217 72694
                                                 -376.1368 19714979 774.74%
               -367.0982
                            639
                                     -43.0000
91226 72696
                                                 -376.1368 19718381 774.74%
               -364.1187
                            634
                                     -43.0000
91279 73087
               -334.1832
                            285
                                     -43.0000
                                                  -376.1368 19684478 774.74%
91581 72886
               -239.2958
                            177
                                     -43.0000
                                                 -376.1368 19731529 774.74%
                                                  -376.1368 19724728 774.74%
91880 72773
               -172.1287
                            147
                                     -43.0000
92103 72979
               -318.1041
                                     -43.0000
                                                  -376.1368 19741671 774.74%
                            204
Elapsed time = 122.50 sec. (101620.07 ticks, tree = 3349.38 MB, solutions = 13)
Nodefile size = 1328.84 MB (1208.58 MB after compression)
92488 73193
               -370.3096
                            645
                                     -43.0000
                                                  -376.1368 19705612 774.74%
92693 73253
                                     -43.0000
                                                  -376.1368 19716357 774.74%
               -263.1795
                            257
93074 72883
               -356.9105
                                     -43.0000
                                                 -376.1368 19744324 774.74%
                            851
93449 72909
                                                 -376.1368 19753841 774.74%
               -298.8729
                            213
                                     -43.0000
94224 73670
               -245.3925
                            164
                                     -43.0000
                                                  -376.1368 19727039 774.74%
95151 73027
               -142.9352
                            102
                                     -43.0000
                                                 -376.1368 19773585 774.74%
96004 73918
                            168
                                     -43.0000
                                                 -376.1368 19744955 774.74%
               -234.3377
96537 75077
                -76.1794
                                     -43.0000
                                                 -376.1368 19787753 774.74%
                            41
97188 73361
               -339.1905
                            244
                                     -43.0000
                                                  -376.1368 19803446 774.74%
97957 73408
                 -98.3815
                             50
                                     -43.0000
                                                  -376.1368 19811535 774.74%
Elapsed time = 169.17 sec. (140231.77 ticks, tree = 3363.58 MB, solutions = 13)
Nodefile size = 1328.84 MB (1208.58 MB after compression)
98359 73123
               -368.1863
                            739
                                     -43.0000
                                                  -376.1368 19803156 774.74%
                                     -43.0000
99166 73425
               -362.4546
                                                  -376.1368 19828990 774.74%
                            512
                                                  -376.1368 19832253 774.74%
99573 74050
                -348.9752
                            262
                                     -43.0000
*100206+75506
                                       -44.0000
                                                    -376.1368
                                                                        754.86%
100260 74255
                                      -44.0000
                                                  -376.1368 19841225 754.86%
                -187.1122
                            111
100755 73923
                -141.6525
                              76
                                      -44.0000
                                                  -376.1368 19855053 754.86%
101360 74183
                                      -44.0000
                                                  -376.1368 19869790 754.86%
                -254.1317
                             165
101983 74396
                                                  -376.1368 19880718 754.86%
                 -365.9683
                             679
                                      -44.0000
```

102256 73251	-358.7644	844	-44.0000	-376.1368 19850813	754.86%
102534 74551	-369.3515	969	-44.0000	-376.1368 19886540	754.86%
102636 74685	-201.0157	189	-44.0000	-376.1368 19906540	754.86%
Elapsed time = 1	213.97 sec.	(178886	3.70 ticks, tree	= 3369.28 MB, soluti	ons = 14)
Nodefile size =	1328.84 MB	(1208.5	88 MB after compr	ression)	
103075 74690	-137.0039	86	-44.0000	-376.1368 19858793	754.86%
103324 74781	-259.5830	176	-44.0000	-376.1368 19870758	754.86%
103868 73707	-357.3355	710	-44.0000	-376.1368 19916863	754.86%
104488 74966	-156.8062	105	-44.0000	-376.1368 19935045	754.86%
104840 73993	-298.3118	195	-44.0000	-376.1368 19937028	754.86%
105230 74463	-370.2003	680	-44.0000	-376.1368 19945863	754.86%
106185 75111	-328.7164	230	-44.0000	-376.1368 19921098	754.86%
106948 74994	-64.9639	51	-44.0000	-376.1368 19976173	754.86%
107545 75108	-275.3044	179	-44.0000	-376.1368 19985828	754.86%
108190 74573	-122.1881	75	-44.0000	-376.1368 19949611	754.86%
Elapsed time = 2	255.53 sec.	(217150	0.33 ticks, tree	= 3470.33 MB, soluti	ons = 15)
Nodefile size =	1328.84 MB	(1208.5	8 MB after compr	ression)	
108890 74604	-302.1580	203	-44.0000	-376.1368 19988782	754.86%
109683 74939	-72.1704	42	-44.0000	-376.1368 19996434	754.86%
110213 75844	-152.6764	113	-44.0000	-376.1368 20025497	754.86%
110687 74738	-372.4462	654	-44.0000	-376.1368 19979491	754.86%
111104 75218	-255.9594	181	-44.0000	-376.1368 20021953	754.86%
111226 75914	-280.6563	210	-44.0000	-376.1368 20052210	754.86%
111818 75067	-108.0074	75	-44.0000	-376.1368 20004989	754.86%
112086 74183	-175.7369	112	-44.0000	-376.1368 20000307	754.86%
112565 76266	-241.4723	169	-44.0000	-376.1368 20079748	754.86%
113030 76439	-164.3090	212	-44.0000	-376.1368 20090558	754.86%
Elapsed time = 3	300.62 sec.	(255370	0.86 ticks, tree	= 3493.07 MB, soluti	ons = 16)
Nodefile size =	1328.84 MB	(1208.5	8 MB after compr	ression)	
113440 75423	-356.3437	390	-44.0000	-376.1368 20066747	754.86%
113846 75655	-329.7125	232	-44.0000	-376.1368 20074973	754.86%
114376 76956	-372.7014	765	-44.0000	-376.1368 20119752	754.86%
114992 75269	-357.7460	861	-44.0000	-376.1368 20084688	754.86%
115064 75899	-244.1868	170	-44.0000	-376.1368 20104973	754.86%
115422 75281	-356.3431	761	-44.0000	-376.1368 20099647	754.86%
115659 77257	-354.9574	229	-44.0000	-376.1368 20156509	754.86%
116481 77486	-350.4063	259	-44.0000	-376.1368 20166270	754.86%
117012 74851	-338.6518	338	-44.0000	-376.1368 20099673	754.86%
117672 76593	-73.3108	55	-44.0000	-376.1368 20139708	754.86%

```
Elapsed time = 340.22 sec. (294342.29 ticks, tree = 3590.75 MB, solutions = 16)
Nodefile size = 1328.84 MB (1208.58 MB after compression)
                                                   -376.1368 20149430 754.86%
118392 76837
                -340.1003
                             223
                                      -44.0000
118661 76951
                 -338.5554
                             252
                                      -44.0000
                                                   -376.1368 20159026 754.86%
119232 78202
                -370.3891
                             879
                                      -44.0000
                                                   -376.1368 20206881 754.86%
119504 78208
                 -365.8875
                             675
                                      -44.0000
                                                   -376.1368 20215279 754.86%
120370 78339
                -294.4108
                             228
                                     -44.0000
                                                   -376.1368 20224887 754.86%
120736 77663
                 -371.1597
                             751
                                      -44.0000
                                                   -376.1368 20197661 754.86%
121137 78468
                 -263.1958
                             171
                                      -44.0000
                                                   -376.1368 20240044
                                                                       754.86%
                                      -44.0000
121380 76760
                 -361.0483
                             578
                                                   -376.1368 20206996 754.86%
                                      -44.0000
121504 78546
                 -372.0299
                                                   -376.1368 20254287 754.86%
                             951
121709 77052
                                      -44.0000
                                                   -376.1368 20224660 754.86%
                 -189.2273
                             149
Elapsed time = 369.68 sec. (333296.33 ticks, tree = 3591.38 MB, solutions = 17)
Nodefile size = 1328.84 MB (1208.58 MB after compression)
121787 77894
                -347.8439
                             314
                                      -44.0000
                                                   -376.1368 20232409 754.86%
121944 78563
                             674
                -362.8561
                                      -44.0000
                                                   -376.1368 20281358 754.86%
122228 78030
                 -369.6159
                             952
                                      -44.0000
                                                   -376.1368 20251103 754.86%
122239 78035
                -365.2604
                                     -44.0000
                                                   -376.1368 20260623 754.86%
                             668
122604 79033
                 -116.1095
                              76
                                      -44.0000
                                                   -376.1368 20304884
                                                                       754.86%
122641 77112
                -360.7584
                             740
                                      -44.0000
                                                   -376.1368 20264111 754.86%
122909 79061
                                      -44.0000
                                                   -376.1368 20328240 754.86%
                 -359.0364
                             761
122912 79064
                                      -44.0000
                                                   -376.1368 20339694 754.86%
                -345.4132
                             728
123088 79214
                                                   -376.1368 20349332 754.86%
                -340.4910
                             331
                                      -44.0000
123335 79434
                 -366.9963
                             736
                                      -44.0000
                                                   -376.1368 20359227 754.86%
Elapsed time = 386.93 sec. (378266.74 ticks, tree = 3689.23 MB, solutions = 18)
Nodefile size = 1328.84 MB (1208.58 MB after compression)
123606 77360
                -367.9078
                             813
                                      -44.0000
                                                   -376.1368 20304015 754.86%
123789 77402
                                                   -376.1368 20313171 754.86%
                -270.6668
                             213
                                     -44.0000
124252 77565
                 -147.9091
                             111
                                      -44.0000
                                                   -376.1368 20322273 754.86%
                                      -44.0000
                                                   -376.1368 20399552 754.86%
124710 80275
                 -339.1575
                             259
                                                   -376.1368 20407189 754.86%
125071 80455
                 -130.4602
                              96
                                      -44.0000
125120 80488
                 -364.5023
                             979
                                      -44.0000
                                                   -376.1368 20414180
                                                                       754.86%
125393 78074
                                     -44.0000
                                                   -376.1368 20356949
                 -67.5268
                              51
                                                                       754.86%
125548 78206
                  -61.4737
                              25
                                      -44.0000
                                                   -376.1368 20365875
                                                                       754.86%
125824 80617
                 -365.8242
                             646
                                      -44.0000
                                                   -376.1368 20434361 754.86%
126311 80820
                 -149.0581
                             106
                                      -44.0000
                                                   -376.1368 20445898 754.86%
Elapsed time = 402.92 sec. (417930.32 ticks, tree = 3750.55 MB, solutions = 18)
Nodefile size = 1328.84 MB (1208.58 MB after compression)
126818 78688
                -359.1233
                            621
                                      -44.0000
                                                   -376.1368 20397046 754.86%
```

127130 78818	-361.6743	326	-44.0000	-376.1368 20405785	754.86%
127645 81464	infeasible		-44.0000	-376.1368 20480980	754.86%
127773 79050	-370.5096	967	-44.0000	-376.1368 20420424	754.86%
128047 79052	-369.8842	919	-44.0000	-376.1368 20426470	754.86%
128292 82017	-100.5857	62	-44.0000	-376.1368 20513017	754.86%
128338 82042	-364.7610	328	-44.0000	-376.1368 20523898	754.86%
128527 79071	-360.6063	650	-44.0000	-376.1368 20446426	754.86%
128837 82360	-201.0485	146	-44.0000	-376.1368 20543286	754.86%
129157 82638	-369.1021	836	-44.0000	-376.1368 20553236	754.86%
Elapsed time =	= 433.80 sec.	(46066	7.96 ticks, tre	e = 3767.71 MB, solution	ons = 19)
Nodefile size	= 1328.84 MB	(1208.	58 MB after com	pression)	
129298 82771	-49.6236	49	-44.0000	-376.1368 20560041	754.86%
129563 83000	-360.7373	441	-44.0000	-376.1368 20569164	754.86%
129908 83292	-150.2737	107	-44.0000	-376.1368 20580126	754.86%
130141 83494	-240.2222	141	-44.0000	-376.1368 20590944	754.86%
130362 83680	-370.2243	736	-44.0000	-376.1368 20601487	754.86%
130505 83814	-359.7878	388	-44.0000	-376.1368 20614667	754.86%
130871 84128	-128.4628	80	-44.0000	-376.1368 20623685	754.86%

GUB cover cuts applied: 1043

Clique cuts applied: 57
Cover cuts applied: 4277

Implied bound cuts applied: 68

Flow cuts applied: 118

Mixed integer rounding cuts applied: 1735

Zero-half cuts applied: 125

Lift and project cuts applied: 9
Gomory fractional cuts applied: 199

Root node processing (before b&c):

Real time = 0.00 sec. (1.39 ticks)

Parallel b&c, 8 threads:

Real time = 460.44 sec. (493387.72 ticks)

Sync time (average) = 9.29 sec. Wait time (average) = 0.00 sec.

Total (root+branch&cut) = 460.44 sec. (493389.11 ticks)

Iteration 9

Bounds on # of cuts = 8 with [3 3 2]

Error = 56 (out of 100 instances)

Accuracy = 44

Solving time = 7.674096716 min (minutes)

Accumulated time = 30.973248364 min (minutes)

Solution status code = 104

LB on error = -275.942710447

Relative objective gap = 7.54415251

Selected variables:

PEMLR (Categorical)

SS_YN (Categorical)

Number of selected variables = 2 (0 continuous + 2 categorical)

Version identifier: 22.1.1.0 | 2022-11-28 | 9160aff4d

CPXPARAM_MIP_Strategy_File 3

CPXPARAM_MIP_Limits_Solutions 1

CPXPARAM_TimeLimit 84541.60509814453

CPXPARAM_MIP_Limits_TreeMemory 204800

Nodes Cuts/

Node Left Objective IInf Best Integer Best Bound ItCnt Gap

130908 115417 infeasible -44.0000 -375.9427 24852547 754.42%

Elapsed time = 0.21 sec. (11.76 ticks, tree = 4875.97 MB, solutions = 20)

Nodefile size = 2828.82 MB (2551.19 MB after compression)

Nodefile size	= 2828.82 MB (2	551.19 MB	after compre	ssion)	
130946 115453	-75.7118	39	-44.0000	-375.9427 24852830	754.42%
130960 115461	infeasible		-44.0000	-375.9427 24854245	754.42%
130961 115417	infeasible		-44.0000	-375.9427 24855273	754.42%
130962 115419	-375.5477	854	-44.0000	-375.9427 24854727	754.42%
130963 115462	-374.5850	952	-44.0000	-375.9427 24856324	754.42%
130964 115419	-374.8863	762	-44.0000	-375.9239 24859471	754.37%
130966 115420	-370.7308	599	-44.0000	-375.9239 24861461	754.37%
130970 115420	-365.1263	677	-44.0000	-375.9239 24865366	754.37%
130974 115425	-353.5129	272	-44.0000	-375.9239 24863328	754.37%
131072 115431	-318.7079	260	-44.0000	-375.9239 24868843	754.37%

```
Elapsed time = 6.88 sec. (4499.63 ticks, tree = 4853.98 MB, solutions = 20)
Nodefile size = 2828.82 MB (2551.19 MB after compression)
131222 115489
                  -186.2469
                              144
                                       -44.0000
                                                    -375.9239 24869233 754.37%
131419 115588
                  -227.5296
                                       -44.0000
                                                    -375.9064 24867646
                              151
                                                                        754.33%
131578 115473
                  -365.3839
                              660
                                       -44.0000
                                                    -375.9064 24885085
                                                                        754.33%
131721 115419
                  -364.6390
                              889
                                       -44.0000
                                                    -375.9064 24870560
                                                                        754.33%
131724 115420
                  -363.4877
                              908
                                       -44.0000
                                                    -375.9064 24872570
                                                                        754.33%
131728 115601
                                                    -375.9064 24886633
                  -368.4619
                              691
                                       -44.0000
                                                                        754.33%
131749 115614
                  -344.4963
                              237
                                       -44.0000
                                                    -375.9064 24889538
                                                                        754.33%
131877 115538
                                       -44.0000
                  -365.3678
                              477
                                                    -375.9064 24884596
                                                                        754.33%
131914 115567
                  -282.2076
                              191
                                       -44.0000
                                                    -375.9064 24887643
                                                                        754.33%
132035 115773
                                       -44.0000
                                                    -375.9064 24887689 754.33%
                  -357.5782
                              691
Elapsed time = 20.65 sec. (15475.37 ticks, tree = 4891.62 MB, solutions = 20)
Nodefile size = 2828.82 MB (2551.19 MB after compression)
132298 115478
                  -363.3619
                              938
                                       -44.0000
                                                    -375.9064 24905374 754.33%
                                       -44.0000
132305 115885
                              666
                                                    -375.9064 24893668 754.33%
                  -365.9278
132438 115476
                  -371.2272
                              830
                                       -44.0000
                                                    -375.9064 24902926
                                                                        754.33%
132450 115660
                  -367.9299
                              777
                                       -44.0000
                                                    -375.6031 24899669
                                                                        753.64%
132461 115721
                  -365.2211
                              688
                                       -44.0000
                                                    -375.6031 24906865
                                                                        753.64%
132632 115757
                  -133.2122
                               81
                                       -44.0000
                                                    -375.6031 24904356
                                                                        753.64%
132765 115485
                  -337.9961
                              301
                                       -44.0000
                                                    -375.6031 24920324
                                                                        753.64%
132903 115483
                  -354.2930
                                       -44.0000
                                                    -375.6031 24918321
                              485
                                                                        753.64%
132974 115524
                                       -44.0000
                                                    -375.6031 24920543
                  -276.5625
                              264
                                                                        753.64%
                                       -44.0000
                                                    -375.6031 24912566 753.64%
133138 116022
                  -319.0843
                              203
Elapsed time = 33.13 sec. (25766.01 ticks, tree = 4914.84 MB, solutions = 20)
Nodefile size = 2828.82 MB (2551.19 MB after compression)
133451 115867
                  -144.2583
                                       -44.0000
                                                    -375.6031 24916493 753.64%
133606 116211
                                       -44.0000
                                                    -375.6031 24916465
                  -45.0030
                               24
                                                                        753.64%
133745 115906
                  -235.1235
                              148
                                       -44.0000
                                                    -375.6031 24924857
                                                                        753.64%
134004 115642
                                       -44.0000
                                                    -375.6031 24933906
                  -254.9202
                              165
                                                                        753.64%
134329 115597
                                       -44.0000
                                                    -375.6031 24927955
                  -79.8389
                               61
                                                                        753.64%
134423 116045
                  -141.1138
                              100
                                       -44.0000
                                                    -375.6031 24933151
                                                                        753.64%
134467 115718
                              866
                                       -44.0000
                                                    -375.6031 24938524
                  -373.6129
                                                                        753.64%
134536 115666
                                       -44.0000
                                                    -375.6031 24932904
                  -199.6527
                              129
                                                                        753.64%
                                       -44.0000
                                                    -375.6031 24943712
134612 115721
                  -354.9792
                              377
                                                                        753.64%
134717 116230
                  -335.6979
                              239
                                       -44.0000
                                                    -375.6031 24937404 753.64%
Elapsed time = 44.97 sec. (35418.05 ticks, tree = 4934.31 MB, solutions = 20)
Nodefile size = 2828.82 MB (2551.19 MB after compression)
135026 115538
                  -238.0279
                              154
                                       -44.0000
                                                    -375.6031 24941038 753.64%
```

```
135204 115612
                  -369.4843
                              771
                                       -44.0000
                                                    -375.6031 24941848 753.64%
135514 116263
                  -248.8541
                              173
                                       -44.0000
                                                    -375.6031 24945872 753.64%
135735 115696
                  -158.7882
                              110
                                       -44.0000
                                                    -375.6031 24946026
                                                                        753.64%
135885 116414
                  -164.6318
                                       -44.0000
                                                    -375.6031 24949736
                              107
                                                                        753.64%
136157 115950
                   -98.4789
                                       -44.0000
                                                    -375.6031 24954128
                               83
                                                                        753.64%
136177 116049
                  -371.4216
                              844
                                       -44.0000
                                                    -375.6031 24942096
                                                                        753.64%
                                                    -375.6031 24956224
136184 115729
                  -359.2447
                              647
                                       -44.0000
                                                                        753.64%
136316 116080
                                                    -375.6031 24961109
                   -98.6373
                               67
                                       -44.0000
                                                                        753.64%
136393 116100
                  -349.1181
                              249
                                       -44.0000
                                                    -375.6031 24963534
                                                                        753.64%
Elapsed time = 57.63 sec. (45651.53 ticks, tree = 4905.68 MB, solutions = 20)
Nodefile size = 2828.82 MB (2551.19 MB after compression)
136849 115888
                                                    -375.6031 24959565 753.64%
                  -253.3435
                              164
                                       -44.0000
137050 116213
                                       -44.0000
                                                    -375.6031 24967308
                  -367.0710
                              403
                                                                        753.64%
137303 115892
                  -370.9447
                              739
                                       -44.0000
                                                    -375.6031 24969401
                                                                        753.64%
137389 116655
                  -171.9714
                              119
                                       -44.0000
                                                    -375.6031 24969048
                                                                        753.64%
137495 115924
                                       -44.0000
                                                    -375.6031 24973699
                  -298.0111
                              212
                                                                        753.64%
137631 115998
                  -263.0363
                                       -44.0000
                                                    -375.6031 24969968
                              183
                                                                         753.64%
137795 116758
                  -248.3035
                                       -44.0000
                                                    -375.6031 24976581
                                                                        753.64%
                              154
137891 116269
                  -369.5074
                              798
                                       -44.0000
                                                    -375.6031 24966502
                                                                        753.64%
137901 115848
                  -360.4711
                              938
                                       -44.0000
                                                    -375.5768 24990340
                                                                        753.58%
137906 116274
                  -365.3659
                              725
                                       -44.0000
                                                    -375.5768 24971064 753.58%
Elapsed time = 70.87 sec. (56061.54 ticks, tree = 4932.76 MB, solutions = 20)
Nodefile size = 2828.82 MB (2551.19 MB after compression)
137960 116487
                                       -44.0000
                                                    -375.5768 24985812 753.58%
                  -316.4243
                              288
138142 116067
                                                    -375.5768 24985266 753.58%
                  -228.0601
                              154
                                       -44.0000
138227 115731
                  -362.3989
                              865
                                       -44.0000
                                                    -375.5768 24979413 753.58%
138244 116283
                  -344.5858
                              239
                                       -44.0000
                                                    -375.5768 24983061
                                                                         753.58%
138307 115736
                                       -44.0000
                                                    -375.5768 24983469
                  -359.8629
                              779
                                                                        753.58%
138489 115938
                  -175.9894
                              129
                                       -44.0000
                                                    -375.5768 25004586
                                                                        753.58%
138590 115775
                                       -44.0000
                                                    -375.5768 24988921
                  -255.4406
                              180
                                                                         753.58%
138814 116345
                              760
                                       -44.0000
                                                    -375.5768 24995243
                  -359.1724
                                                                        753.58%
139074 115974
                  -105.0916
                               65
                                       -44.0000
                                                    -375.5768 24992675
                                                                        753.58%
139113 116128
                  -374.1367
                              970
                                       -44.0000
                                                    -375.5768 24991767 753.58%
Elapsed time = 82.98 sec. (65890.40 ticks, tree = 4914.26 MB, solutions = 20)
Nodefile size = 2828.82 MB (2551.19 MB after compression)
139288 116450
                     cutoff
                                       -44.0000
                                                    -375.5768 25002072 753.58%
139503 116586
                  -365.1134
                              478
                                       -44.0000
                                                    -375.5768 25000336 753.58%
139743 116674
                  -294.4688
                              225
                                       -44.0000
                                                    -375.5768 24997586
                                                                        753.58%
139909 116748
                  -108.7938
                                       -44.0000
                                                    -375.5768 24997959
                                                                        753.58%
                               89
```

139971 116095	-335.3009	237	-44.0000	-375.5768	25004249	753.58%
140220 116203	-69.1186	46	-44.0000	-375.5768	25004973	753.58%
140240 116121	-362.5128	582	-44.0000	-375.5768	25007014	753.58%
140401 116148	-303.0626	212	-44.0000	-375.5768	25009101	753.58%
140517 116574	-348.2827	284	-44.0000	-375.5768	25019146	753.58%
140699 116276	-258.9445	196	-44.0000	-375.5768	25012673	753.58%
Elapsed time = 94	.85 sec. (75	581.51 tid	cks, tree = 49	917.26 MB,	solutions	= 20)
Nodefile size = 28	328.82 MB (2	551.19 MB	after compres	ssion)		
140877 116078	-121.0623	82	-44.0000	-375.5768	25036048	753.58%
140925 116350	-343.0377	230	-44.0000	-375.5768	25017733	753.58%
141100 116151	-232.2341	177	-44.0000	-375.5768	25039954	753.58%
141253 117269	-234.1615	167	-44.0000	-375.5768	25034933	753.58%
141416 116174	-281.4930	181	-44.0000	-375.5768	25019843	753.58%
141745 116720	-364.4253	455	-44.0000	-375.5768	25034074	753.58%
141861 116802	-175.3061	289	-44.0000	-375.5768	25036560	753.58%
142147 116886	-280.5945	190	-44.0000	-375.5768	25034867	753.58%
142406 117437	-150.9468	103	-44.0000	-375.5768	25044378	753.58%
142489 116212	-373.2448	888	-44.0000	-375.5768	25048786	753.58%
Elapsed time = 106	6.60 sec. (8	5221.60 ti	icks, tree = 4	1909.58 MB	, solutions	s = 20)
Nodefile size = 28	328.82 MB (2	551.19 MB	after compres	ssion)		
142508 117488	-336.2286	214	-44.0000	-375.5768	25048940	753.58%
142640 116225	-363.3862	631	-44.0000	-375.5768	25033233	753.58%
142775 116458	-157.0598	131	-44.0000	-375.5768	25036898	753.58%
142949 117590	-353.3226	361	-44.0000	-375.5768	25056638	753.58%
143076 116219	-361.4628	313	-44.0000	-375.5768	25060174	753.58%
143254 118022	-345.2241	249	-44.0000	-375.5297	25176661	753.48%
143691 116631	-45.6814	55	-44.0000	-375.5297	25047642	753.48%
143831 116896	-258.8147	156	-44.0000	-375.5297	25056621	753.48%
143932 117151	-370.4339	702	-44.0000	-375.5297	25050563	753.48%
144503 116351	-361.2385	431	-44.0000	-375.5297	25058610	753.48%
Elapsed time = 124	1.41 sec. (9	8029.26 ti	icks, tree = 4	1935.34 MB	, solutions	s = 20)
Nodefile size = 28	328.82 MB (2	551.19 MB	after compres	ssion)		
145598 118282	-84.7192	45	-44.0000	-375.5297	25200709	753.48%
146286 116663	-146.1327	110	-44.0000	-375.5297	25086583	753.48%
146983 118364	-196.2860	147	-44.0000	-375.5297	25217258	753.48%
147695 116842	-288.8602	173	-44.0000	-375.5297	25106005	753.48%
148179 118682	-364.6394	681	-44.0000	-375.5297	25235746	753.48%
148895 118808	-45.9513	35	-44.0000	-375.5297	25239563	753.48%
149564 117128	-102.2161	125	-44.0000	-375.5297	25113787	753.48%

150155 117500	-250.4974	176	-44.0000	-375.5297 25113826	753.48%
151053 117401	-133.1193	72	-44.0000	-375.5297 25149498	753.48%
152268 117266	-74.6968	45	-44.0000	-375.5297 25133951	753.48%
Elapsed time =	171.10 sec. (1	136215	.45 ticks, tree =	5020.68 MB, soluti	ons = 20)
Nodefile size =	2828.82 MB (2	2551.1	9 MB after compre	ssion)	
153265 117421	-131.6317	86	-44.0000	-375.5297 25148312	753.48%
153651 123366	-204.8835	135	-44.0000	-375.5297 25710075	753.48%
154291 127032	-273.1402	193	-44.0000	-375.4562 26185133	753.31%
154685 132699	-230.5562	138	-44.0000	-375.4562 26809062	753.31%
155410 135455	-86.7902	48	-44.0000	-375.0224 27113648	752.32%
156010 135713	-353.6035	369	-44.0000	-374.9424 27159569	752.14%
156428 136562	-373.1474	752	-44.0000	-374.9424 27240959	752.14%
156856 136991	-207.2019	119	-44.0000	-374.9424 27278840	752.14%
157325 137622	-282.8151	202	-44.0000	-374.6467 27376398	751.47%
157554 137746	-361.1068	365	-44.0000	-374.6467 27400626	751.47%
Elapsed time =	229.01 sec. (1	174835	.59 ticks, tree =	6750.00 MB, soluti	ons = 20)
Nodefile size =	4694.67 MB (4	4271.7	9 MB after compre	ssion)	
158142 137958	-121.8675	82	-44.0000	-374.6467 27423219	751.47%
158452 138468	-76.5513	58	-44.0000	-374.3973 27479789	750.90%
158893 138456	-347.6235	270	-44.0000	-374.3973 27513832	750.90%
159308 139453	-83.8846	50	-44.0000	-374.3973 27639581	750.90%
159480 139089	-351.9897	348	-44.0000	-374.2840 27601366	750.65%
159932 140136	-288.8156	190	-44.0000	-374.2840 27773711	750.65%
160342 139970	-351.9906	293	-44.0000	-374.2840 27751169	750.65%
161057 140601	-366.0149	640	-44.0000	-374.2840 27867684	750.65%
162160 140791	-223.6580	127	-44.0000	-374.2101 27879510	750.48%
163097 142224	-222.4034	148	-44.0000	-374.1965 28026597	750.45%
Elapsed time =	278.81 sec. (2	213139	.08 ticks, tree =	6770.20 MB, soluti	ons = 20)
Nodefile size =	4714.67 MB (4	4281.1	1 MB after compre	ssion)	
163912 142512	infeasible		-44.0000	-374.1965 28049351	750.45%
164581 143728	-93.8205	59	-44.0000	-374.0908 28152876	750.21%
165350 144119	-79.5072	47	-44.0000	-374.0698 28225664	750.16%
165945 144892	-229.1467	130	-44.0000	-374.0698 28296508	750.16%
166536 145100	-279.1562	190	-44.0000	-374.0698 28313847	750.16%
167263 145224	-248.0966	153	-44.0000	-374.0500 28324091	750.11%
167930 146403	-350.6970	275	-44.0000	-373.9883 28442310	749.97%
168968 146615	-100.5712	70	-44.0000	-373.9312 28450581	749.84%
169395 147938	-355.1343	366	-44.0000	-373.9312 28581082	749.84%
170326 148098	-257.4100	169	-44.0000	-373.9312 28588582	749.84%

```
Elapsed time = 328.74 sec. (251329.20 ticks, tree = 6859.09 MB, solutions = 20)
Nodefile size = 4790.43 MB (4339.89 MB after compression)
170842 148288
                  -349.1396
                              362
                                       -44.0000
                                                    -373.9124 28607750 749.80%
171150 149503
                  -320.2788
                                       -44.0000
                                                    -373.9124 28727565
                              218
                                                                        749.80%
171832 149966
                  -350.6827
                              359
                                       -44.0000
                                                    -373.8929 28794113
                                                                        749.76%
172192 150174
                  -170.2027
                              122
                                       -44.0000
                                                    -373.8929 28843720
                                                                        749.76%
172580 149983
                  -359.4415
                              786
                                       -44.0000
                                                    -373.8929 28820435
                                                                        749.76%
                                                    -373.8929 28944854
172880 151136
                  -335.9286
                              284
                                       -44.0000
                                                                        749.76%
173494 151420
                  -241.2605
                              162
                                       -44.0000
                                                    -373.8929 28978189
                                                                        749.76%
173961 151599
                                       -44.0000
                   -79.5849
                               38
                                                    -373.8929 29002456
                                                                        749.76%
174586 152338
                  -361.9703
                              801
                                       -44.0000
                                                    -373.8929 29088367
                                                                        749.76%
175313 152491
                  -326.2307
                                       -44.0000
                                                    -373.8929 29085315 749.76%
                              218
Elapsed time = 380.88 sec. (289676.74 ticks, tree = 7073.81 MB, solutions = 20)
Nodefile size = 4990.52 MB (4516.97 MB after compression)
176015 152689
                  -289.1985
                              182
                                       -44.0000
                                                    -373.8929 29144336 749.76%
                                       -44.0000
176855 154160
                  -77.4398
                               37
                                                    -373.8929 29266758 749.76%
177448 154194
                  -290.7869
                              193
                                       -44.0000
                                                    -373.8929 29274335
                                                                        749.76%
177800 155086
                  -352.6978
                              552
                                       -44.0000
                                                    -373.8929 29417626
                                                                        749.76%
178144 155126
                  -277.9166
                              175
                                       -44.0000
                                                    -373.8929 29427343
                                                                        749.76%
178488 155853
                  -325.1799
                              217
                                       -44.0000
                                                    -373.6771 29539764
                                                                        749.27%
178978 155690
                  -227.7448
                              269
                                       -44.0000
                                                    -373.6771 29534376 749.27%
179678 156294
                  -172.5863
                                       -44.0000
                                                    -373.6130 29606670
                               99
                                                                        749.12%
180144 157102
                                       -44.0000
                                                    -373.6099 29747844 749.11%
                  -355.1944
                              657
180869 157097
                                       -44.0000
                                                    -373.5628 29743077 749.01%
                  -338.7220
                              212
Elapsed time = 433.30 sec. (328264.55 ticks, tree = 7285.22 MB, solutions = 20)
Nodefile size = 5230.30 MB (4731.06 MB after compression)
181719 157876
                  -303.7777
                              268
                                       -44.0000
                                                    -373.5628 29865351 749.01%
182794 159272
                                                    -373.5628 29984307 749.01%
                  -237.1395
                              147
                                       -44.0000
183348 159346
                  -351.1395
                              663
                                       -44.0000
                                                    -373.5628 30006348 749.01%
184056 160314
                              687
                                       -44.0000
                                                    -373.4833 30086392
                  -367.6314
                                                                        748.83%
184762 160989
                                       -44.0000
                                                    -373.4409 30149317 748.73%
                  -99.2792
                               65
185495 161553
                  -357.1583
                              641
                                       -44.0000
                                                    -373.4409 30227053
                                                                        748.73%
                  -156.6030
186459 162127
                                       -44.0000
                                                    -373.4409 30284992
                               90
                                                                        748.73%
187261 161936
                   -61.7549
                               32
                                       -44.0000
                                                    -373.3481 30259262
                                                                        748.52%
188114 162740
                   -73.0164
                               36
                                       -44.0000
                                                    -373.3443 30325642
                                                                        748.51%
189070 163956
                  -152.9141
                               96
                                       -44.0000
                                                    -373.3443 30438865 748.51%
Elapsed time = 486.25 sec. (367163.04 ticks, tree = 7512.82 MB, solutions = 20)
Nodefile size = 5447.40 MB (4922.11 MB after compression)
189644 164386
                  -367.8376
                              887
                                       -44.0000
                                                    -373.3443 30477271 748.51%
```

```
190685 164981
                  -87.2124
                               61
                                       -44.0000
                                                     -373.3443 30514247 748.51%
191184 166418
                  -333.6920
                              221
                                       -44.0000
                                                     -373.3443 30646990
                                                                        748.51%
192458 166950
                  -208.3170
                              120
                                       -44.0000
                                                     -373.3443 30699405
                                                                        748.51%
193547 167529
                  -198.3154
                                       -44.0000
                                                     -373.3443 30739547
                              118
                                                                         748.51%
194774 168011
                  -168.6088
                                       -44.0000
                                                     -373.2787 30794964
                              199
                                                                         748.36%
195925 168908
                  -142.5090
                              148
                                       -44.0000
                                                     -373.2427 30835364
                                                                         748.28%
196620 171308
                  -224.7571
                              158
                                       -44.0000
                                                     -373.2408 30997697
                                                                         748.27%
197264 171376
                  -371.6623
                              716
                                       -44.0000
                                                     -373.2408 31005841
                                                                         748.27%
198034 171635
                  -208.1538
                              134
                                       -44.0000
                                                     -373.2055 31055553 748.19%
Elapsed time = 539.69 sec. (405452.81 ticks, tree = 7961.62 MB, solutions = 20)
Nodefile size = 5907.38 MB (5338.30 MB after compression)
198412 172029
                  -289.5103
                                                     -373.2055 31095374 748.19%
                              235
                                       -44.0000
198962 172723
                                                     -373.2055 31160733 748.19%
                  -143.3916
                               95
                                       -44.0000
199414 172871
                  -308.1767
                              199
                                       -44.0000
                                                     -373.2055 31188479 748.19%
200445 174277
                   -67.7922
                               28
                                       -44.0000
                                                     -373.1191 31301581
                                                                         748.00%
201225 174685
                              671
                                                     -373.1191 31351164 748.00%
                  -365.1012
                                       -44.0000
201850 175086
                                       -44.0000
                                                     -373.1191 31384774
                  -310.6747
                              205
                                                                        748.00%
202420 176028
                              228
                                       -44.0000
                                                     -373.1191 31500120 748.00%
                  -299.8808
202989 176150
                  -356.5293
                              345
                                       -44.0000
                                                     -373.1191 31508469
                                                                         748.00%
203966 177277
                  -349.3249
                              252
                                       -44.0000
                                                     -373.1191 31616486
                                                                         748.00%
204804 177320
                              257
                                       -44.0000
                                                     -373.0455 31638301 747.83%
                  -351.0572
Elapsed time = 590.71 sec. (444013.14 ticks, tree = 8114.88 MB, solutions = 20)
Nodefile size = 6058.27 MB (5468.92 MB after compression)
                                       -44.0000
205628 178179
                                                     -373.0143 31717251 747.76%
                  -111.3682
                               81
206144 178259
                  -197.6408
                              123
                                       -44.0000
                                                     -373.0143 31727454 747.76%
206619 178812
                  -178.9469
                              189
                                       -44.0000
                                                     -372.9949 31789311 747.72%
207249 179762
                  -363.1710
                                       -44.0000
                                                     -372.9899 31871857 747.70%
                              818
207745 180890
                                                     -372.9899 32040405 747.70%
                  -212.8827
                              131
                                       -44.0000
208953 181296
                   -86.9530
                               56
                                       -44.0000
                                                     -372.9899 32078113 747.70%
209931 181837
                                                     -372.9480 32163706
                   -93.0117
                              192
                                       -44.0000
                                                                         747.61%
210844 182022
                                                     -372.9480 32157809 747.61%
                  -195.7135
                              130
                                       -44.0000
211479 182394
                  -336.0640
                              243
                                       -44.0000
                                                     -372.8824 32214463
                                                                        747.46%
211879 183270
                  -333.1627
                                       -44.0000
                                                     -372.8748 32262683 747.44%
                              209
Elapsed time = 646.29 sec. (482797.42 ticks, tree = 8350.07 MB, solutions = 20)
Nodefile size = 6294.05 MB (5672.22 MB after compression)
212147 184598
                  -363.4645 1062
                                       -44.0000
                                                     -372.8748 32370505 747.44%
212919 185068
                  -288.2498
                              184
                                       -44.0000
                                                     -372.8748 32431657 747.44%
214028 185646
                  -210.1929
                              142
                                       -44.0000
                                                     -372.8748 32487431 747.44%
214899 185756
                  -200.4004
                                       -44.0000
                                                    -372.8600 32475142 747.41%
                              137
```

215323 186568	-146.7879	101	-44.0000	-372.8563 32572067	747.40%
215585 186646	-265.0594	174	-44.0000	-372.8430 32582774	747.37%
215930 186866	-296.3604	233	-44.0000	-372.8430 32646715	747.37%
216342 188005	-368.3260	1030	-44.0000	-372.8430 32726916	747.37%
216864 188736	-183.1399	110	-44.0000	-372.8430 32848795	747.37%
217090 189090	-331.5462	245	-44.0000	-372.8430 32903193	747.37%
Elapsed time = 6	897.47 sec. (521071.	74 ticks, tree =	= 8599.97 MB, solution	ns = 20)
Nodefile size =	6544.44 MB (5890.61	MB after compre	ession)	
217790 188686	-323.9812	247	-44.0000	-372.8014 32870258	747.28%
218356 189541	-133.4137	76	-44.0000	-372.7773 32936831	747.22%
219174 190551	-351.0221	300	-44.0000	-372.7773 33038249	747.22%
219578 190300	-368.7349	934	-44.0000	-372.7684 33027649	747.20%
219598 190825	-355.7343	627	-44.0000	-372.7631 33100093	747.19%
219718 191769	-139.0102	86	-44.0000	-372.7377 33251637	747.13%
220184 191764	-131.8059	121	-44.0000	-372.7377 33230928	747.13%
221011 192191	-217.5934	136	-44.0000	-372.7272 33365455	747.11%
221677 192658	-312.0576	207	-44.0000	-372.7272 33417939	747.11%
222408 192605	-131.1298	82	-44.0000	-372.6994 33406887	747.04%
Elapsed time = 7	751.00 sec. (560245.	75 ticks, tree =	8875.72 MB, solution	ns = 20)
Nodefile size =	6819.28 MB (6143.16	MB after compre	ession)	
222807 193252	-351.8520	359	-44.0000	-372.6994 33474914	747.04%
223697 193819	-368.2402	1014	-44.0000	-372.6705 33555864	746.98%
224291 194508	-168.4572	113	-44.0000	-372.6705 33597439	746.98%
224688 194980	-328.9159	330	-44.0000	-372.6705 33680048	746.98%
225604 195221	-350.0778	362	-44.0000	-372.6431 33710002	746.92%
226659 196294	-277.8216	183	-44.0000	-372.6029 33779087	746.82%
227209 195824	-306.6847	195	-44.0000	-372.6029 33766707	746.82%
228433 197223	-367.8317	689	-44.0000	-372.5677 33854373	746.74%
229269 199080	-361.1116	655	-44.0000	-372.5534 34022057	746.71%
230336 199294	-175.2973	112	-44.0000	-372.5531 34046870	746.71%
Elapsed time = 8	304.93 sec. (599059.	75 ticks, tree =	9113.38 MB, solution	ns = 20)
Nodefile size =	7058.01 MB (6351.40	MB after compre	ession)	
231216 200588	-358.3446	489	-44.0000	-372.5531 34129659	746.71%
231583 200216	-268.3678	255	-44.0000	-372.5531 34115070	746.71%
232305 201798	-46.5832	26	-44.0000	-372.5531 34219507	746.71%
233137 202370	-185.0193	120	-44.0000	-372.5031 34307455	746.60%
234418 201984	-225.0413	192	-44.0000	-372.4962 34280003	746.58%
235315 203798	-343.5671	300	-44.0000	-372.4823 34427805	746.55%
235540 203201	-194.1673	132	-44.0000	-372.4823 34396450	746.55%

236303 204300	-90.3678	54	-44.0000	-372.4732 34472118	746.53%
236745 204491	-353.6942	922	-44.0000	-372.4732 34519696	746.53%
237725 205433	-362.9104	718	-44.0000	-372.4587 34591948	746.50%
Elapsed time = 858	8.28 sec. (637821.53	ticks, tree =	9338.06 MB, solutio	ns = 20)
Nodefile size = 7	269.93 MB (6536.27 MB	after compre	ssion)	
238274 205925	-85.8155	50	-44.0000	-372.4587 34647302	746.50%
238981 207487	-231.9881	149	-44.0000	-372.3994 34779028	746.36%
239878 207765	-93.4593	61	-44.0000	-372.3994 34786500	746.36%
240120 207756	-365.9616	411	-44.0000	-372.3994 34822268	746.36%
240478 209365	-199.8041	130	-44.0000	-372.3584 34940305	746.27%
240821 209539	-360.1367	638	-44.0000	-372.3584 34972410	746.27%
241271 209541	-363.1588	1122	-44.0000	-372.3584 34983161	746.27%
241424 210053	-361.2374	950	-44.0000	-372.3584 35084084	746.27%
241576 210292	-347.5688	297	-44.0000	-372.3584 35112261	746.27%
241997 210422	-368.2257	1017	-44.0000	-372.3584 35145629	746.27%
Elapsed time = 91	2.88 sec. (676882.31	ticks, tree =	9709.04 MB, solutio	ns = 20)
Nodefile size = 70	655.42 MB (6	6887.57 MB	after compre	ssion)	
242245 210584	-240.9517	157	-44.0000	-372.3584 35171767	746.27%
242570 210687	-338.0566	350	-44.0000	-372.3584 35275535	746.27%
243231 210809	-332.0380	238	-44.0000	-372.2883 35284325	746.11%
243525 211377	-366.4540	682	-44.0000	-372.2883 35363030	746.11%
243864 211549	-332.6650	319	-44.0000	-372.2883 35413331	746.11%
244343 212034	-284.4207	206	-44.0000	-372.2542 35461002	746.03%
244916 211665	-371.1470	1019	-44.0000	-372.2542 35425781	746.03%
245241 213063	-339.6566	564	-44.0000	-372.2542 35635322	746.03%
245969 213431	-346.9792	377	-44.0000	-372.2542 35676293	746.03%
246514 214170	-356.2338	419	-44.0000	-372.2542 35731859	746.03%
Elapsed time = 960	6.08 sec. (716168.10	ticks, tree =	9727.48 MB, solutio	ns = 20)
Nodefile size = 7	670.55 MB (6	6894.27 MB	after compre	ssion)	
247304 214362	-248.7154	181	-44.0000	-372.1984 35793183	745.91%
247544 214195	-368.2592	1074	-44.0000	-372.1984 35773514	745.91%
248320 215215	-339.6080	224	-44.0000	-372.1984 35912774	745.91%
248943 215127	-219.3915	150	-44.0000	-372.1939 35887771	745.90%
249564 215696	-329.7974	226	-44.0000	-372.1939 35961847	745.90%
250132 216976	-264.5542	167	-44.0000	-372.1916 36040514	745.89%
250395 216722	-370.6489	959	-44.0000	-372.1916 36031786	745.89%

Repeating presolve.

Tried aggregator 1 time.

Reduced MIP has 3556 rows, 5459 columns, and 23781 nonzeros.

Reduced MIP has 4603 binaries, 51 generals, 0 SOSs, and 0 indicators.

Presolve time = 0.01 sec. (12.05 ticks)

Tried aggregator 1 time.

Reduced MIP has 3556 rows, 5459 columns, and 23781 nonzeros.

Reduced MIP has 4603 binaries, 51 generals, 0 SOSs, and 0 indicators.

Presolve time = 0.02 sec. (16.72 ticks)

Represolve time = 1.99 sec. (423.12 ticks)

250594	0	-385.6923	1361	-44.0000	Cuts: 281	36368218	745.89%
250594	0	-385.5894	1250	-44.0000	Cuts: 88	36373095	745.89%
250594	0	-385.5320	1275	-44.0000	Cuts: 631	36377740	745.89%
250594	0	-385.4713	1249	-44.0000	Cuts: 545	36381282	745.89%
250594	0	-385.4204	1259	-44.0000	Cuts: 957	36387163	745.89%
250594	0	-385.3847	1222	-44.0000	Cuts: 654	36390902	745.89%
250594	0	-385.3577	1237	-44.0000	Cuts: 790	36394642	745.89%
250594	0	-385.3485	1245	-44.0000	Cuts: 703	36396546	745.89%
250594	0	-385.3400	1274	-44.0000	Cuts: 658	36398676	745.89%
250594	2	-385.3400	1250	-44.0000	-372.1916	36398676	745.89%
250597	5	-382.4444	787	-44.0000	-372.1916	36411834	745.89%
250602	9	-380.3559	797	-44.0000	-372.1916	36423958	745.89%
Elapsed	time =	1108.28 sec.	(8556	83.12 ticks, tree	= 0.02 MB	, solution	ıs = 20)
250611	6	-378.8050	657	-44.0000	-372.1916	36417553	745.89%
250635	35	-376.0446	672	-44.0000	-372.1916	36531095	745.89%
250672	68	-370.5626	763	-44.0000	-372.1916	36616128	745.89%
250694	92	-371.9434	943	-44.0000	-372.1916	36701820	745.89%
250721	118	-362.8932	629	-44.0000	-372.1916	36801968	745.89%
250761	125	-361.9080	779	-44.0000	-372.1916	36885878	745.89%
250789	184	-368.8459	821	-44.0000	-372.1916	37004980	745.89%
250841	217	-339.4235	586	-44.0000	-372.1916	37066500	745.89%
251153	486	-210.0063	143	-44.0000	-372.1916	37133536	745.89%
251322	495	-364.4991	902	-44.0000	-372.1916	37206131	745.89%
Elapsed	time =	1152.80 sec.	(8952	88.35 ticks, tree	= 14.88 M	B, solutio	ons = 20)
251351	672	-367.3628	827	-44.0000	-372.1916	37251757	745.89%
251394	715	-364.1056	761	-44.0000	-372.1916	37328615	745.89%
251440	744	-268.2901	507	-44.0000	-372.1916	37368491	745.89%
251521	826	-318.6446	749	-44.0000	-372.1916	37511071	745.89%
251833	831	-324.7711	304	-44.0000	-372.1916	37519578	745.89%

252407	1017	-289.7608	602	-44.0000	-372.1916	37636368	745.89%
252474	1569	-230.7063	364	-44.0000	-372.1916	37760627	745.89%
252551	1641	-175.7780	280	-44.0000	-372.1916	37815845	745.89%
252648	1761	-350.1193	690	-44.0000	-372.1916	37915832	745.89%
252770	1798	-297.9704	428	-44.0000	-372.1916	37931390	745.89%
Elapsed time = 1202.91 sec. (933976.92 ticks, tree = 72.71 MB, solutions = 20)							
252957	1879	-365.0530	907	-44.0000	-372.1916	38019591	745.89%
253190	1961	-374.1327	746	-44.0000	-372.1916	38105061	745.89%
253209	2081	-366.6955	727	-44.0000	-372.1916	38154827	745.89%
253245	2107	-349.4859	750	-44.0000	-372.1916	38232352	745.89%
253296	2321	-323.2255	719	-44.0000	-372.1916	38306497	745.89%
253335	2350	-338.7238	810	-44.0000	-372.1916	38399274	745.89%
253431	2430	-223.8642	266	-44.0000	-372.1916	38441630	745.89%
253627	2511	-375.7077	894	-44.0000	-372.1916	38536324	745.89%
253710	2600	-267.8143	648	-44.0000	-372.1916	38634838	745.89%
253859	2807	-130.4952	121	-44.0000	-372.1916	38706683	745.89%
Elapsed	time =	1250.04 sec.	(972969	.48 ticks,	tree = 103.61 N	MB, soluti	ons = 20)
253990	2793	-354.1329	866	-44.0000	-372.1916	38772365	745.89%
254125	2847	-378.1667	932	-44.0000	-372.1916	38821293	745.89%
254160	3057	-345.8537	710	-44.0000	-372.1916	38991676	745.89%
254272	3174	-338.3096	397	-44.0000	-372.1916	39057856	745.89%
254829	3402	-355.6737	381	-44.0000	-372.1916	39162730	745.89%
255039	3352	-378.1796	878	-44.0000	-372.1916	39140890	745.89%
255759	3966	-377.3962	848	-44.0000	-372.1916	39289058	745.89%
256132	4683	-376.0871	913	-44.0000	-372.1916	39411724	745.89%
256571	4897	-110.1847	135	-44.0000	-372.1916	39448784	745.89%
256899	5006	-264.7572	206	-44.0000	-372.1916	39493263	745.89%
Elapsed	time =	1299.80 sec.	(101192	3.48 ticks,	tree = 185.99	MB, solut	ions = 20)
257633	5503	-108.6815	304	-44.0000	-372.1916	39551337	745.89%
257704	5875	-357.2719	386	-44.0000	-372.1916	39627575	745.89%
258222	6596	-269.8295	197	-44.0000	-372.1916	39752633	745.89%
258860	6676	-377.5047	795	-44.0000	-372.1916	39771980	745.89%
259177	6867	-342.8244	368	-44.0000	-372.1916	39847164	745.89%
259604	7816	-126.7714	273	-44.0000	-372.1916	39962898	745.89%
259992	8066	-346.3133	285	-44.0000	-372.1916	40043650	745.89%
260634	8324	-250.4738	183	-44.0000	-372.1916	40101264	745.89%
261423	8587	-117.3785	72	-44.0000	-372.1916	40156633	745.89%
261811	8623	cutoff		-44.0000	-372.1916	40168545	745.89%
Elapsed	time =	1345.55 sec.	(105017	4.00 ticks,	tree = 360.71	MB, solut	ions = 20)

262463 9727	-346.0636	360	-44.0000	-372.1916	40305990	745.89%
262827 10015	-53.0047	53	-44.0000	-372.1916	40336812	745.89%
263497 10204	-291.6292	329	-44.0000	-372.1916	40409727	745.89%
263810 10834	-368.7024	900	-44.0000	-372.1916	40508382	745.89%
264034 11380	-299.6250	270	-44.0000	-372.1916	40589629	745.89%
264353 11408	-333.6570	364	-44.0000	-372.1916	40631990	745.89%
265209 11627	-127.5949	81	-44.0000	-372.1916	40690974	745.89%
265375 12058	-373.9214	775	-44.0000	-372.1916	40825316	745.89%
265683 12067	-374.6869	871	-44.0000	-372.1916	40813199	745.89%
266145 12871	-108.7038	66	-44.0000	-372.1916	40958008	745.89%
Elapsed time =	1392.76 sec.	(1089	307.50 ticks,	tree = 376.25	MB, solut	ions = 20)
267009 13160	-339.9349	292	-44.0000	-372.1916	41042304	745.89%
267684 13451	-235.2024	155	-44.0000	-372.1916	41068056	745.89%
268135 14202	-301.8026	239	-44.0000	-372.1916	41179259	745.89%
269063 14802	-332.9360	201	-44.0000	-372.1916	41233945	745.89%
269908 15031	-151.4007	185	-44.0000	-372.1916	41298728	745.89%
270417 15902	-355.9540	424	-44.0000	-372.1916	41379785	745.89%
271179 15998	-182.1055	124	-44.0000	-372.1916	41374578	745.89%
271618 16779	-343.4644	297	-44.0000	-372.1916	41483634	745.89%
272154 17272	-266.0548	154	-44.0000	-372.1916	41561427	745.89%
272757 17853	-107.8635	54	-44.0000	-372.1916	41620379	745.89%
Elapsed time =	1441.86 sec.	(1127	546.03 ticks,	tree = 531.02	MB, solut	ions = 20)
273371 18302	-282.6906	198	-44.0000	-372.1916	41702255	745.89%
274130 18595	-244.6982	252	-44.0000	-372.1916	41749235	745.89%
274538 18916	-352.0270	368	-44.0000	-372.1916	41810597	745.89%
275533 19350	-242.7152	146	-44.0000	-372.1916	41846033	745.89%
276032 19990	-54.5599	49	-44.0000	-372.1916	41908637	745.89%
276526 20374	-115.2920	72	-44.0000	-372.1916	41972219	745.89%
277076 21354	-362.0541	532	-44.0000	-372.1916	42106109	745.89%
277609 20404	-368.4605	1077	-44.0000	-372.1916	41979761	745.89%
278059 22108	-337.7553	273	-44.0000	-372.1916	42232415	745.89%
278647 22119	-320.3121	220	-44.0000	-372.1916	42214941	745.89%
Elapsed time =	1491.47 sec.	(1166	019.37 ticks,	tree = 615.31	MB, solut	ions = 20)
279632 23591	-334.9430	280	-44.0000	-372.1916	42392818	745.89%
280126 23804	-128.5027	69	-44.0000	-372.1916	42401404	745.89%
280920 23955	-138.4359	120	-44.0000	-372.1916	42477580	745.89%
281437 24950	-129.1561	99	-44.0000	-372.1916	42575431	745.89%
281989 25082	-134.7455	71	-44.0000	-372.1916	42585611	745.89%
282711 25369	-371.6460	532	-44.0000	-372.1916	42618193	745.89%

283322 26147	-343.3787	304	-44.0000	-372.1916 42729297 745.89%	
284664 26732	-334.3227	329	-44.0000	-372.1916 42818857 745.89%	
285866 26665	-363.2964	860	-44.0000	-372.1916 42775391 745.89%	
286482 28580	-247.8636	167	-44.0000	-372.1916 42941939 745.89%	
Elapsed time =	1539.98 sec.	(1204	311.03 ticks,	tree = 860.28 MB, solutions = 20))
287505 28813	-299.1811	243	-44.0000	-372.0951 42963649 745.67%	
288523 29633	-250.3703	162	-44.0000	-372.0110 43033224 745.48%	
289106 30046	-295.2430	201	-44.0000	-372.0110 43069346 745.48%	
289455 30190	-192.9309	112	-44.0000	-372.0040 43074509 745.46%	
289993 31045	-141.5293	173	-44.0000	-372.0040 43163423 745.46%	
290206 31157	-348.8130	419	-44.0000	-371.9483 43202763 745.34%	
290699 31651	-341.1091	335	-44.0000	-371.9469 43228780 745.33%	
291317 32466	-341.1582	315	-44.0000	-371.9469 43373635 745.33%	
291837 32743	-352.7835	540	-44.0000	-371.6923 43438115 744.76%	
292068 32468	-351.9463	516	-44.0000	-371.6923 43398040 744.76%	
Elapsed time =	1589.93 sec.	(1242	794.09 ticks,	tree = 1076.94 MB, solutions = 20))
292671 33486	-239.0993	208	-44.0000	-371.6923 43533295 744.76%	
292992 33266	-363.6098	582	-44.0000	-371.6923 43504347 744.76%	
293493 33938	-118.9946	101	-44.0000	-371.5623 43606836 744.46%	
293974 34166	-353.3337	727	-44.0000	-371.5062 43668357 744.33%	
294519 34909	-280.2416	186	-44.0000	-371.5062 43776237 744.33%	
295353 35538	-189.7857	111	-44.0000	-371.2609 43849416 743.77%	
295790 35885	-52.6185	40	-44.0000	-371.2083 43882368 743.66%	
296289 35883	-314.7165	258	-44.0000	-371.2083 43920204 743.66%	
296578 35201	-354.8640	645	-44.0000	-371.2083 43857528 743.66%	
296765 36460	-354.9554	528	-44.0000	-371.2083 44019420 743.66%	
Elapsed time =	1642.27 sec.	(1284	198.61 ticks,	tree = 1170.56 MB, solutions = 20))
296907 36344	-353.1478	725	-44.0000	-371.2083 44017102 743.66%	
297436 37190	-175.1358	102	-44.0000	-371.2083 44086601 743.66%	
297836 37240	-360.3308	492	-44.0000	-371.0292 44096222 743.25%	
298225 37776	-368.8773	710	-44.0000	-371.0292 44237544 743.25%	
298876 37904	-76.2539	71	-44.0000	-371.0292 44259745 743.25%	
299088 38497	-366.8987	596	-44.0000	-371.0292 44375456 743.25%	
299492 38089	-358.5517	265	-44.0000	-370.9771 44293705 743.13%	
300346 38897	-311.8971	282	-44.0000	-370.9771 44428265 743.13%	
300919 39134	-357.5479	819	-44.0000	-370.9771 44454488 743.13%	
301172 39614	-319.6664	202	-44.0000	-370.8041 44571989 742.74%	
Elapsed time =	1691.83 sec.	(1323	114.08 ticks,	tree = 1204.52 MB, solutions = 20))
301646 39448	-344.0955	491	-44.0000	-370.8041 44557156 742.74%	

301836	40335	-103.6051	83	-44.0000	-370.8041 4	14707703	742.74%
302225	40202	-358.3735	487	-44.0000	-370.8041 4	14704677	742.74%
302610	40600	-355.9007	952	-44.0000	-370.8041 4	14777613	742.74%
302988	41309	-298.4826	193	-44.0000	-370.6520 4	14872708	742.39%
303374	40766	-283.5381	167	-44.0000	-370.6520 4	14825751	742.39%
303891	41485	-304.3835	215	-44.0000	-370.6520 4	14908146	742.39%
304356	41571	-74.9176	60	-44.0000	-370.6109 4	14934370	742.30%
304928	42264	-364.8487	443	-44.0000	-370.4962 4	15035283	742.04%
305462	42397	-359.8320	501	-44.0000	-370.4951 4	15041146	742.03%
Elapse	d time =	1741.50 sec.	(1361	578.50 ticks,	tree = 1299.40	MB, solu	tions = 20)
305990	43081	-87.9339	46	-44.0000	-370.4951 4	15139238	742.03%
306368	43162	-215.9043	149	-44.0000	-370.4950 4	15145034	742.03%
307093	43334	-343.6828	419	-44.0000	-370.3971 4	15170187	741.81%
307363	44228	-335.0437	293	-44.0000	-370.3971 4	15262113	741.81%
307994	44774	-209.7137	119	-44.0000	-370.3477 4	15337005	741.70%
308082	44372	-360.5717	1018	-44.0000	-370.3477 4	15292973	741.70%
308313	44758	-359.0325	970	-44.0000	-370.3477 4	15372677	741.70%
308796	45146	-329.1411	285	-44.0000	-370.2988 4	15421832	741.59%
309247	45738	-85.4863	51	-44.0000	-370.2988 4	15556907	741.59%
309734	46020	-367.5729	426	-44.0000	-370.2988 4	15588630	741.59%
Elapse	d time =	1792.12 sec.	(1401	098.88 ticks,	tree = 1498.55	MB, solu	tions = 20)
310298	46140	-357.3188	1014	-44.0000	-370.1730 4	15686049	741.30%
310880	46723	-313.9365	262	-44.0000	-370.0978 4	15733688	741.13%
311618	47314	-351.6886	376	-44.0000	-370.0978 4	15815752	741.13%
312071	47781	-268.8162	238	-44.0000	-370.0978 4	15873219	741.13%
312444	47505	-244.1141	152	-44.0000	-370.0978 4	15846117	741.13%
313037	48077	-223.3538	252	-44.0000	-370.0978 4	15934014	741.13%
313489	48766	-231.3842	174	-44.0000	-370.0978 4	15982195	741.13%
314106	49110	-286.7892	161	-44.0000	-369.8680 4	16027720	740.61%
314277	49227	-352.6875	410	-44.0000	-369.7946 4	16049462	740.44%
315052	49499	-356.5130	502	-44.0000	-369.7890 4	16093606	740.43%
Elapse	d time =	1844.27 sec.	(1439	867.53 ticks,	tree = 1727.94	MB, solu	tions = 20)
315430	50490	infeasible		-44.0000	-369.7665 4	16227867	740.38%
315633	50873	-116.4103	66	-44.0000	-369.7325 4	16279007	740.30%
316395	50950	-319.2967	221	-44.0000	-369.7325 4	16305582	740.30%
317079	51065	-360.8404	415	-44.0000	-369.6889 4	16312413	740.20%
317677	51183	-365.7037	1061	-44.0000	-369.6668 4	16348889	740.15%
318344	51962	-125.6950	92	-44.0000	-369.6668 4	16450552	740.15%
318572	51990	-368.0280	694	-44.0000	-369.6179 4	16457249	740.04%

```
318765 52695
                -357.1016 1077
                                     -44.0000
                                                  -369.5690 46541748 739.93%
319126 52963
                -352.8065
                             686
                                     -44.0000
                                                  -369.5690 46586748 739.93%
319440 53430
                -260.1408
                                     -44.0000
                                                  -369.5690 46663375 739.93%
                             161
Elapsed time = 1896.37 sec. (1479194.25 ticks, tree = 1951.39 MB, solutions = 20)
320144 53982
                                     -44.0000
                                                  -369.5411 46755129 739.87%
                -234.4145
                             165
320530 53857
                -207.5893
                             175
                                     -44.0000
                                                  -369.5411 46726581 739.87%
320617 53926
                -344.9031
                             756
                                     -44.0000
                                                  -369.5411 46789304 739.87%
                                                  -369.5411 46876025 739.87%
321019 54333
                 -331.2943
                             278
                                     -44.0000
321384 54728
                 -330.9338
                             393
                                      -44.0000
                                                   -369.4818 46956127 739.73%
Began writing nodes to disk (directory ./cpx6hXQcQ created)
321929 55231
                 -205.4632
                                     -44.0000
                                                  -369.4596 47068125 739.68%
                             119
322419 55580
                -324.8614
                             213
                                     -44.0000
                                                  -369.4596 47114860 739.68%
322789 55897
                                                  -369.3454 47171636 739.42%
                -364.3820
                             405
                                     -44.0000
323522 56158
                 -364.5998
                             889
                                      -44.0000
                                                   -369.3454 47201561 739.42%
323533 56166
                 -341.7744
                             430
                                      -44.0000
                                                  -369.3454 47208791 739.42%
Elapsed time = 1948.33 sec. (1518462.54 ticks, tree = 2111.35 MB, solutions = 20)
Nodefile size = 58.62 MB (51.63 MB after compression)
323942 57003
                                     -44.0000
                                                  -369.3155 47332465 739.35%
                 -96.3349
                             92
324164 57093
                 -340.3201
                             295
                                     -44.0000
                                                   -369.3155 47380106 739.35%
324358 57091
                -342.8492
                             664
                                     -44.0000
                                                   -369.3155 47399665 739.35%
                                     -44.0000
                                                  -369.3155 47485341 739.35%
324721 57452
                 -332.6673
                             256
325593 57417
                 -80.5629
                                     -44.0000
                                                  -369.2700 47458323 739.25%
                             105
                                                  -369.2662 47566012 739.24%
325870 57756
                -344.9406
                             339
                                     -44.0000
326635 58368
                 -235.1431
                             177
                                      -44.0000
                                                  -369.2522 47647462 739.21%
326735 58498
                -310.1259
                             223
                                     -44.0000
                                                  -369.2522 47686593 739.21%
327241 58889
                 -332.4587
                             307
                                     -44.0000
                                                  -369.2522 47744689 739.21%
328157 58732
                 -348.2701
                             337
                                      -44.0000
                                                  -369.2483 47714755 739.20%
Elapsed time = 2000.08 sec. (1556813.49 ticks, tree = 2191.10 MB, solutions = 20)
Nodefile size = 138.10 MB (121.57 MB after compression)
                                                  -369.2483 47866301 739.20%
328696 59366
                 -349.9339
                             591
                                      -44.0000
                                                  -369.2483 47903916 739.20%
329258 59928
                 -200.9429
                                     -44.0000
                             112
330085 59816
                 -360.8325
                             274
                                      -44.0000
                                                   -369.2169 47888319 739.13%
330696 60569
                                     -44.0000
                                                  -369.1513 47944891 738.98%
                 -251.8809
                             167
331215 61510
                 -350.2743
                             253
                                     -44.0000
                                                   -369.1513 48067414 738.98%
331643 61684
                 -252.4282
                             148
                                     -44.0000
                                                   -369.1169 48074972 738.90%
332328 62542
                 -300.0368
                             269
                                     -44.0000
                                                   -369.1169 48153942 738.90%
333052 62613
                 -172.4415
                             137
                                     -44.0000
                                                   -369.1169 48170227 738.90%
333503 63456
                -273.7816
                             225
                                     -44.0000
                                                  -369.0920 48254726 738.85%
334319 64313
                 -129.4382
                             75
                                                  -369.0066 48319508 738.65%
                                      -44.0000
```

```
Elapsed time = 2053.05 sec. (1595009.26 ticks, tree = 2609.90 MB, solutions = 20)
Nodefile size = 546.80 MB (482.47 MB after compression)
334526 64366
                -353.2900
                             430
                                      -44.0000
                                                   -369.0066 48353456 738.65%
335096 64236
                 -348.8633
                             383
                                      -44.0000
                                                   -369.0066 48342110 738.65%
335482 64995
                -357.2174
                             248
                                      -44.0000
                                                   -369.0066 48410627 738.65%
335751 65112
                -108.3985
                              85
                                      -44.0000
                                                   -369.0066 48422213 738.65%
336342 65566
                -342.3519
                             298
                                     -44.0000
                                                   -369.0066 48508876 738.65%
336872 65367
                -278.6137
                             218
                                      -44.0000
                                                   -369.0030 48496547 738.64%
337666 66284
                 -241.4814
                             163
                                      -44.0000
                                                   -369.0030 48624088
                                                                       738.64%
                                      -44.0000
338557 67101
                 -71.7748
                              33
                                                   -368.7571 48737948 738.08%
                 -280.2961
                             200
                                      -44.0000
                                                   -368.7571 48788027 738.08%
339421 67550
340094 67778
                  -72.4334
                                      -44.0000
                                                   -368.7571 48792340 738.08%
                              62
Elapsed time = 2105.71 sec. (1633306.25 ticks, tree = 2773.62 MB, solutions = 20)
Nodefile size = 694.67 MB (612.65 MB after compression)
340708 68252
                 -89.3731
                              41
                                      -44.0000
                                                   -368.7571 48849031 738.08%
341145 68828
                -235.1402
                             140
                                      -44.0000
                                                   -368.7364 48907267 738.04%
342133 69534
                -227.6095
                             155
                                      -44.0000
                                                   -368.6620 49008465 737.87%
343080 69560
                                      -44.0000
                                                   -368.6620 48981554 737.87%
                    cutoff
343436 70905
                 -359.4257
                             669
                                      -44.0000
                                                   -368.6480 49119605
                                                                       737.84%
344064 69862
                -316.9504
                             228
                                      -44.0000
                                                   -368.6321 49055558 737.80%
344917 71337
                -358.6754
                             317
                                     -44.0000
                                                   -368.6321 49158258 737.80%
345459 71450
                -241.4689
                                      -44.0000
                                                   -368.5854 49178803
                             183
                                                                       737.69%
345806 72770
                                                   -368.5854 49313002 737.69%
                -350.6402
                             414
                                      -44.0000
346180 72776
                 -344.2606
                             682
                                      -44.0000
                                                   -368.5854 49334729 737.69%
Elapsed time = 2158.28 sec. (1671605.97 ticks, tree = 3247.77 MB, solutions = 20)
Nodefile size = 1193.67 MB (1058.69 MB after compression)
346629 73045
                -306.0790
                             188
                                      -44.0000
                                                   -368.5714 49381248 737.66%
346989 73311
                -326.8352
                             274
                                     -44.0000
                                                   -368.5714 49410860 737.66%
347251 73656
                 -159.0263
                             107
                                      -44.0000
                                                   -368.5025 49428784 737.51%
                                                   -368.4952 49535435 737.49%
347944 74202
                -186.4601
                             103
                                      -44.0000
348859 74293
                -334.4883
                             288
                                      -44.0000
                                                   -368.4952 49557222 737.49%
349336 74834
                 -85.2232
                             153
                                      -44.0000
                                                   -368.4952 49628825 737.49%
                -246.7459
349792 75367
                                     -44.0000
                                                   -368.4952 49673306 737.49%
                             197
350409 75634
                 -214.3057
                             148
                                      -44.0000
                                                   -368.4689 49693562 737.43%
351125 76103
                  -65.2717
                              23
                                      -44.0000
                                                   -368.4689 49729789
                                                                       737.43%
351528 76502
                 -121.4386
                              73
                                      -44.0000
                                                   -368.4689 49803180 737.43%
Elapsed time = 2212.26 sec. (1709831.49 ticks, tree = 3429.06 MB, solutions = 20)
Nodefile size = 1374.50 MB (1216.81 MB after compression)
351877 76695
                -210.5933
                                      -44.0000
                                                   -368.3886 49818966 737.25%
                            124
```

GUB cover cuts applied: 1479

Clique cuts applied: 53 Cover cuts applied: 4469

Implied bound cuts applied: 115

Flow cuts applied: 171

Mixed integer rounding cuts applied: 2859

Zero-half cuts applied: 135

Lift and project cuts applied: 20 Gomory fractional cuts applied: 182

Root node processing (before b&c):

Real time = 0.00 sec. (2.63 ticks)

Parallel b&c, 8 threads:

Real time = 2233.60 sec. (1733502.38 ticks)

Sync time (average) = 300.51 sec. Wait time (average) = 0.08 sec.

Total (root+branch&cut) = 2233.60 sec. (1733505.01 ticks)

Iteration 10

Bounds on # of cuts = 8 with [3 3 2]

Error = 54 (out of 100 instances)

Accuracy = 46

Solving time = 37.2267415 min (minutes)

Accumulated time = 68.199989864 min (minutes)

Solution status code = 104

LB on error = -268.366653275

Relative objective gap = 7.007970723

Selected variables:

A_AGE (Continuous)

PEMLR (Categorical)

```
Number of selected variables = 2 (1 continuous + 1 categorical)
Version identifier: 22.1.1.0 | 2022-11-28 | 9160aff4d
CPXPARAM_MIP_Strategy_File
CPXPARAM_MIP_Limits_Solutions
                                                 1
CPXPARAM_TimeLimit
                                                 82308.000608154296
CPXPARAM_MIP_Limits_TreeMemory
                                                 204800
Nodes
                                              Cuts/
Node Left
               Objective IInf Best Integer
                                                Best Bound
                                                              ItCnt
                                                                        Gap
352957 78439
                infeasible
                                      -46.0000
                                                   -368.3667 50058943 700.80%
Elapsed time = 0.58 sec. (13.44 ticks, tree = 3578.62 MB, solutions = 21)
Nodefile size = 1531.15 MB (1354.94 MB after compression)
352959 78441
                 -355.0696
                             622
                                      -46.0000
                                                   -368.3667 50059517 700.80%
352960 78442
                 -354.9621
                                      -46.0000
                                                   -368.3667 50059978 700.80%
                             614
352961 78441
                 -368.1422
                             467
                                      -46.0000
                                                   -368.3667 50059688 700.80%
352963 78442
                 -366.8929
                             459
                                      -46.0000
                                                   -368.3667 50061062 700.80%
                                                   -368.3667 50063349 700.80%
352970 78443
                 -364.4998
                             478
                                      -46.0000
352991 78459
                 -359.1808
                             287
                                      -46.0000
                                                   -368.3667 50061782 700.80%
353012 78471
                 -341.2399
                             250
                                      -46.0000
                                                   -368.3667 50062182 700.80%
353032 78481
                 -314.3891
                             241
                                      -46.0000
                                                   -368.3667 50062713 700.80%
353075 78464
                                      -46.0000
                                                   -368.3667 50065349 700.80%
                 -352.9182
                             243
353290 78522
                                      -46.0000
                                                   -368.3667 50066815 700.80%
                 -216.3510
                             139
Elapsed time = 5.58 sec. (3453.73 ticks, tree = 3574.72 MB, solutions = 21)
Nodefile size = 1531.15 MB (1354.94 MB after compression)
353412 78478
                 -313.4469
                             240
                                      -46.0000
                                                   -368.3065 50067622 700.67%
353582 78573
                -120.4601
                                      -46.0000
                                                   -368.3065 50068969 700.67%
                              54
353756 78583
                 -366.5572
                             569
                                      -46.0000
                                                   -368.3065 50069592 700.67%
353915 78593
                 -350.4133
                                      -46.0000
                                                   -368.3065 50071762 700.67%
                             356
354013 78638
                 -255.5095
                             182
                                      -46.0000
                                                   -368.3065 50073098 700.67%
354172 78670
                 -225.7101
                             139
                                      -46.0000
                                                   -368.3065 50075904 700.67%
354385 78504
                 -226.4890
                                      -46.0000
                                                   -368.2929 50093543 700.64%
                             127
354717 78838
                                      -46.0000
                                                   -368.2929 50076924 700.64%
                  -68.3427
                              35
354895 78735
                 -366.5307
                                      -46.0000
                             385
                                                   -368.2929 50081410 700.64%
355013 78725
                 -358.3571
                             260
                                      -46.0000
                                                   -368.2929 50081358 700.64%
Elapsed time = 18.04 sec. (13079.83 ticks, tree = 3596.11 MB, solutions = 21)
Nodefile size = 1531.15 MB (1354.94 MB after compression)
```

355350 78840

-106.1301

61

-46.0000

-368.2929 50082313 700.64%

355421 78637	-265.3412	275	-46.0000	-368.2929 50101647	700.64%
355525 78674	-185.2515	141	-46.0000	-368.2802 50103370	700.61%
*355558+78900			-47.0000	-368.2802	683.57%
355620 78594	-339.7121	378	-47.0000	-368.2802 50098468	683.57%
355766 78770	-294.4367	166	-47.0000	-368.2802 50106522	683.57%
356139 78635	-175.6360	123	-47.0000	-368.2802 50098267	683.57%
356248 78595	-327.9391	290	-47.0000	-368.2802 50116071	683.57%
356341 78649	-216.7224	142	-47.0000	-368.2802 50118193	683.57%
356578 78816	-170.0356	106	-47.0000	-368.2802 50108680	683.57%
356638 78453	-344.8623	449	-47.0000	-368.2802 50116537	683.57%
Elapsed time = 2	9.93 sec. (23092.66	S ticks, tree =	3533.95 MB, solution	s = 24)
Nodefile size =	1531.15 MB	(1354.94	l MB after comp	ression)	
356671 78466	-341.4183	357	-47.0000	-368.2802 50117958	683.57%
356751 78750	-256.5897	150	-47.0000	-368.2802 50111786	683.57%
356870 78469	-366.3548	433	-47.0000	-368.2802 50121648	683.57%
356949 78525	-255.7729	163	-47.0000	-368.2802 50124119	683.57%
357102 78851	-349.7279	232	-47.0000	-368.2802 50117120	683.57%
*357191+78873			-48.0000	-368.2802	667.25%
357191 78711	-367.6334	1100	-48.0000	-368.2802 50124118	667.25%
357194 78714	-367.6270	1104	-48.0000	-368.2802 50124781	667.25%
357195 78609	-342.4514	413	-48.0000	-368.2802 50139710	667.25%
357262 78665	-248.5754	138	-48.0000	-368.2802 50141684	667.25%
357380 78718	-354.8980	803	-48.0000	-368.2802 50142887	667.25%
Elapsed time = 4	4.43 sec. (43023.32	2 ticks, tree =	3542.02 MB, solution	s = 27)
Nodefile size =	1531.15 MB	(1354.94	MB after comp	ression)	
357385 78720	-354.1313	745	-48.0000	-368.2802 50144502	667.25%
357389 78723	-352.5103	493	-48.0000	-368.2802 50146723	667.25%
357394 78727	-339.5890	283	-48.0000	-368.2802 50148761	667.25%
357420 78744	-332.3197	331	-48.0000	-368.2802 50149654	667.25%
357451 78769	-280.8813	168	-48.0000	-368.2802 50150722	667.25%
357488 78795	-215.9856	158	-48.0000	-368.2802 50151746	667.25%
357527 78746	-354.7789	1031	-48.0000	-368.2802 50162814	667.25%
357530 78749	-354.6699	1031	-48.0000	-368.2802 50163649	667.25%
357531 78750	-346.2256	653	-48.0000	-368.2802 50170449	667.25%
357533 78752	-344.5490	744	-48.0000	-368.2802 50171923	667.25%
Elapsed time = 5	5.57 sec. (57967.17	ticks, tree =	3535.25 MB, solution	s = 27)
Nodefile size =	1531.15 MB	(1354.94	1 MB after comp	ression)	
357536 78821	-366.0749	1161	-48.0000	-368.2802 50157991	667.25%
357540 78823	-366.0599	1158	-48.0000	-368.2802 50158619	667.25%

357556	78769	-325.5245	302	-48.0000	-368.2802 50177346	667.25%
357590	78792	-291.4648	232	-48.0000	-368.2802 50178499	667.25%
357621	78817	-233.7738	198	-48.0000	-368.2802 50179962	667.25%
357636	78824	-365.1710	595	-48.0000	-368.2802 50183101	667.25%
357669	78849	-340.1584	284	-48.0000	-368.2802 50185185	667.25%
357722	78826	-361.9055	1039	-48.0000	-368.2802 50168111	667.25%
357723	78827	-354.3601	752	-48.0000	-368.2802 50176673	667.25%
357725	78829	-352.8350	745	-48.0000	-368.2802 50178651	667.25%
Elapsed	time = 63	3.73 sec.	(73838.94	ticks, tree =	3542.48 MB, solution	s = 28)
Nodefil	e size = 1	1531.15 MB	(1354.94	MB after compr	ession)	
357727	78831	-351.3868	663	-48.0000	-368.2802 50180601	667.25%
357729	78833	-349.5185	509	-48.0000	-368.2802 50182598	667.25%
357733	78835	-339.0805	430	-48.0000	-368.2802 50184554	667.25%
357757	78857	-321.4356	295	-48.0000	-368.2802 50185975	667.25%
357781	78864	-367.4109	559	-48.0000	-368.2802 50189238	667.25%
357788	78868	-362.7362	469	-48.0000	-368.2802 50191101	667.25%
357803	78879	-356.6581	374	-48.0000	-368.2802 50192864	667.25%

GUB cover cuts applied: 1515

Clique cuts applied: 53 Cover cuts applied: 4487

Implied bound cuts applied: 116

Flow cuts applied: 171

Mixed integer rounding cuts applied: 3009

Zero-half cuts applied: 135

Lift and project cuts applied: 20 Gomory fractional cuts applied: 183

Root node processing (before b&c):

Real time = 0.00 sec. (1.95 ticks)

Parallel b&c, 8 threads:

Real time = 70.85 sec. (82977.94 ticks)

Sync time (average) = 1.52 sec.Wait time (average) = 0.00 sec.

Total (root+branch&cut) = 70.85 sec. (82979.89 ticks)

Iteration 11

Bounds on # of cuts = 8 with [3 3 2] Error = 52 (out of 100 instances)

Accuracy = 48

Solving time = 1.180936951 min (minutes)

Accumulated time = 69.380926815 min (minutes)

Solution status code = 104 LB on error = -268.191364056

Relative objective gap = 6.670653418

Selected variables:

A_AGE (Continuous)

PEMLR (Categorical)

Number of selected variables = 2 (1 continuous + 1 categorical)

Version identifier: 22.1.1.0 | 2022-11-28 | 9160aff4d

CPXPARAM_MIP_Strategy_File 3

CPXPARAM_MIP_Limits_Solutions

CPXPARAM_TimeLimit 82237.144391113281

204800 CPXPARAM_MIP_Limits_TreeMemory

Nodes Cuts/

Node Left Objective IInf Best Integer Best Bound ItCnt Gap

357813 81848 infeasible -48.0000 -368.1914 50513898 667.07%

Elapsed time = 0.66 sec. (292.33 ticks, tree = 3726.48 MB, solutions = 29)

Nodefile size = 1679.11 MB (1484.78 MB after compression) 357826 81861 -292.1446 183 -48.0000 -368.1914 50513559 667.07% 357851 81885 -234.4599 151 -48.0000 -368.1914 50514204 667.07% 357887 81913 -152.0224 89 -48.0000 -368.1909 50514540 667.06% 357920 81854 -357.2824 437 -48.0000 -368.1909 50516152 667.06% 357957 81858 -352.0901 310 -48.0000 -368.1909 50519329 667.06% 358005 81876 -328.8730 208 -48.0000 -368.1909 50519839 667.06% 358061 81952 -365.6237 549 -48.0000 -368.1909 50516426 667.06% 358123 81944 -173.5007 110 -48.0000 -368.1909 50520624 667.06% 358187 81986 -63.5680 31 -48.0000 -368.1909 50520867 667.06% -368.1843 50525639 667.05% 358404 81869 -356.0177 335 -48.0000

Elapsed time = 4.90 sec. (3429.12 ticks, tree = 3706.40 MB, solutions = 29)

Nodefile size =	1679.11 MB ((1484.78	B MB after comp	ression)	
358736 81977	-104.3151	66	-48.0000	-368.1843 50527782	667.05%
359077 81930	-213.6064	155	-48.0000	-368.1843 50539357	667.05%
359402 81958	-126.7440	131	-48.0000	-368.1843 50534882	667.05%
359558 82114	-323.8779	203	-48.0000	-368.1843 50527920	667.05%
360011 82123	-110.9767	62	-48.0000	-368.1843 50534255	667.05%
360279 82251	-303.4537	198	-48.0000	-368.1843 50531448	667.05%
360674 82270	-333.9872	256	-48.0000	-368.1843 50533165	667.05%
360773 82324	-216.5179	149	-48.0000	-368.1433 50535459	666.97%
360935 81876	-334.8739	394	-48.0000	-368.1433 50554007	666.97%
361126 82233	-126.4382	85	-48.0000	-368.1433 50538997	666.97%
Elapsed time =	16.84 sec. (1	13063.54	ł ticks, tree =	3721.75 MB, solution	s = 29)
Nodefile size =	1679.11 MB ((1484.78	B MB after comp	ression)	
361224 82365	-356.3953	443	-48.0000	-368.1433 50542559	666.97%
361281 82131	-357.4859	303	-48.0000	-368.1433 50550840	666.97%
361426 82156	-326.2501	224	-48.0000	-368.1433 50553536	666.97%
361646 82220	-176.9277	120	-48.0000	-368.1433 50556001	666.97%
361770 82452	-180.0865	199	-48.0000	-368.1433 50554805	666.97%
361955 82503	-57.9050	56	-48.0000	-368.1433 50556571	666.97%
362344 82097	-142.5888	80	-48.0000	-368.1433 50569144	666.97%
362616 82168	-298.4494	201	-48.0000	-368.1433 50555327	666.97%
362791 82238	-120.0840	76	-48.0000	-368.1433 50557846	666.97%
363008 82410	-348.3597	333	-48.0000	-368.1433 50568317	666.97%
Elapsed time =	29.19 sec. (2	22675.86	S ticks, tree =	3702.14 MB, solution	s = 29)
Nodefile size =	1679.11 MB ((1484.78	B MB after comp	ression)	
363419 82370	-120.3047	72	-48.0000	-368.1433 50561564	666.97%
363578 82189	-249.4025	251	-48.0000	-368.1433 50581892	666.97%
363716 82216	-192.8838	220	-48.0000	-368.1433 50583993	666.97%
364045 82643	-113.9610	77	-48.0000	-368.1433 50563974	666.97%
364090 82681	-358.5332	390	-48.0000	-368.1433 50576810	666.97%
364122 82699	-341.6880	311	-48.0000	-368.1433 50578930	666.97%
364284 82291	-317.6356	231	-48.0000	-368.1433 50591814	666.97%
364631 82674	-357.5447	338	-48.0000	-368.1433 50572614	666.97%
364749 82708	-296.0979	196	-48.0000	-368.1433 50574904	666.97%
364984 82786	-87.9932	99	-48.0000	-368.1433 50575721	666.97%
Elapsed time =	41.83 sec. (3	32254.33	3 ticks, tree =	3717.44 MB, solution	s = 29)
Nodefile size =	1679.11 MB ((1484.78	B MB after comp	ression)	
365223 82504	-191.5209	217	-48.0000	-368.1433 50591049	666.97%
365504 82549	-331.3050	208	-48.0000	-368.1433 50601365	666.97%

```
365992 82893
                -127.0245
                             73
                                     -48.0000
                                                  -368.1433 50588165 666.97%
366170 82544
                -366.6969
                            623
                                     -48.0000
                                                  -368.1433 50597281 666.97%
366176 82548
                -355.5594
                            469
                                     -48.0000
                                                  -368.1433 50601349 666.97%
366189 82559
                                     -48.0000
                                                  -368.1433 50603729
                -351.7782
                            427
                                                                      666.97%
366204 82569
                                     -48.0000
                                                  -368.1433 50607134
                -339.4731
                            368
                                                                      666.97%
366249 82599
                -272.1125
                            282
                                     -48.0000
                                                  -368.1433 50608232
                                                                      666.97%
366396 82671
                -114.3516
                             71
                                     -48.0000
                                                  -368.1433 50609897
                                                                      666.97%
366634 82736
                -309.9270
                            209
                                     -48.0000
                                                  -368.1433 50611201 666.97%
Elapsed time = 54.67 sec. (42460.70 ticks, tree = 3710.17 MB, solutions = 29)
Nodefile size = 1679.11 MB (1484.78 MB after compression)
366756 82821
                -111.5596
                                     -48.0000
                                                  -368.1433 50612395 666.97%
                             54
366807 82858
                                                  -368.1433 50613675 666.97%
                -343.9349
                            258
                                     -48.0000
366896 82914
                                                  -368.1433 50615760 666.97%
                -211.1564
                            174
                                     -48.0000
366985 82971
                -366.4920
                            430
                                     -48.0000
                                                  -368.1433 50617063 666.97%
367034 82400
                -351.3165
                            559
                                     -48.0000
                                                  -368.1433 50587667
                                                                      666.97%
367120 83037
                -244.8728
                            179
                                     -48.0000
                                                  -368.1433 50620481
                                                                      666.97%
367337 82703
                -334.1119
                            233
                                     -48.0000
                                                  -368.1433 50628475
                                                                      666.97%
367706 82986
                                     -48.0000
                                                  -368.1433 50617616
                -316.4094
                            188
                                                                      666.97%
367821 83126
                -356.0752
                            340
                                     -48.0000
                                                  -368.1433 50627458
                                                                      666.97%
368044 82503
                -135.1360
                            111
                                     -48.0000
                                                  -368.1433 50593666 666.97%
Elapsed time = 67.00 sec. (52139.75 ticks, tree = 3695.91 MB, solutions = 29)
Nodefile size = 1679.11 MB (1484.78 MB after compression)
368238 82922
                                                  -368.1433 50634114 666.97%
                -164.7335
                             92
                                     -48.0000
368430 83224
                -123.8483
                            141
                                     -48.0000
                                                  -368.1433 50637485 666.97%
368773 83201
                -128.9948
                             87
                                     -48.0000
                                                  -368.1433 50629760 666.97%
368913 83264
                -357.5110
                                     -48.0000
                                                  -368.1433 50641918 666.97%
                            311
369098 83112
                -324.3748
                                     -48.0000
                                                  -368.1433 50639612 666.97%
                            198
369400 83329
                                                  -368.1433 50645762 666.97%
                -191.7452
                            204
                                     -48.0000
369572 83433
                -223.7018
                             132
                                     -48.0000
                                                  -368.1433 50636921 666.97%
369806 82380
                -287.5304
                            169
                                     -48.0000
                                                  -368.1433 50648326
                                                                      666.97%
370042 83155
                -230.0538
                            152
                                     -48.0000
                                                  -368.1433 50627192 666.97%
370296 83206
                -105.6802
                             84
                                     -48.0000
                                                  -368.1433 50627997
                                                                      666.97%
Elapsed time = 79.67 sec. (61734.30 ticks, tree = 3719.22 MB, solutions = 29)
Nodefile size = 1679.11 MB (1484.78 MB after compression)
370473 83648
                -363.5100
                            330
                                     -48.0000
                                                  -368.1433 50644687 666.97%
370572 83690
                -301.8013
                            207
                                     -48.0000
                                                  -368.1433 50648101 666.97%
370729 83483
                -197.3347
                            130
                                     -48.0000
                                                  -368.1387 50658662 666.96%
370929 83541
                -365.7080
                            488
                                     -48.0000
                                                  -368.1387 50660523 666.96%
371088 83221
                -351.9229
                            387
                                     -48.0000
                                                  -368.1387 50653084 666.96%
```

371487 83670	-73.6233	44	-48.0000	-368.1387 50663896 66	6.96%
371836 83297	-205.4547	120	-48.0000	-368.1387 50656731 66	6.96%
371955 84037	-363.3737	398	-48.0000	-368.1387 50658794 66	6.96%
372245 84150	-104.1935	62	-48.0000	-368.1387 50660639 66	6.96%
372599 84174	-356.4815	416	-48.0000	-368.1387 50662713 66	6.96%
<pre>Elapsed time =</pre>	91.72 sec. (71418.2	7 ticks, tree =	3710.01 MB, solutions =	29)
Nodefile size =	1679.11 MB	(1484.7	8 MB after compr	ression)	
372758 83830	-350.2123	218	-48.0000	-368.1387 50673011 66	6.96%
372917 83910	-185.9764	100	-48.0000	-368.1337 50675434 66	6.95%
373114 82774	-318.4387	220	-48.0000	-368.1337 50678770 66	6.95%
373417 84320	-338.0692	224	-48.0000	-368.1337 50669801 66	6.95%
373666 83414	-320.7274	235	-48.0000	-368.1337 50655149 66	6.95%
374022 83475	-168.1748	126	-48.0000	-368.1337 50656810 66	6.95%
374273 84491	-280.5796	200	-48.0000	-368.1337 50676353 66	6.95%
374608 84074	-110.7467	74	-48.0000	-368.1337 50687542 66	6.95%
374870 83955	-200.9511	127	-48.0000	-368.1337 50773859 66	6.95%
375060 84635	-264.2193	176	-48.0000	-368.1337 50681732 66	6.95%
Elapsed time =	104.63 sec.	(80997.	62 ticks, tree =	3712.07 MB, solutions	= 29)
Nodefile size =	1679.11 MB	(1484.7	8 MB after compr	ression)	
375289 83674	-313.4418	201	-48.0000	-368.1337 50666202 66	6.95%
375652 83029	-311.7428	205	-48.0000	-368.1337 50695634 66	6.95%
375861 83121	-243.7553	181	-48.0000	-368.1337 50707677 66	6.95%
376042 83812	-322.3605	225	-48.0000	-368.1337 50672426 66	6.95%
376328 83907	-76.8829	55	-48.0000	-368.1337 50673938 66	6.95%
376562 84043	-315.9558	248	-48.0000	-368.1337 50786727 66	6.95%
376701 84097	-203.0215	121	-48.0000	-368.1337 50788420 66	6.95%
376892 83281	-94.0053	88	-48.0000	-368.1337 50707850 66	6.95%
376963 84416	-300.0476	169	-48.0000	-368.1337 50708399 66	6.95%
377680 83473	-295.0804	190	-48.0000	-368.1337 50717425 66	6.95%
Elapsed time =	120.42 sec.	(93442.	31 ticks, tree =	3693.86 MB, solutions	= 29)
Nodefile size =	1679.11 MB	(1484.7	8 MB after compr	ression)	
378589 84784	-62.4796	50	-48.0000	-368.1337 50723926 66	6.95%
379167 84588	-357.1111	256	-48.0000	-368.1295 50809279 66	6.94%
379898 84778	-210.9325	156	-48.0000	-368.1295 50814162 66	6.94%
381019 83619	-115.1233	68	-48.0000	-368.1295 50707029 66	6.94%
382720 83365	-140.2585	105	-48.0000	-368.1295 50688807 66	6.94%
384080 83309	-101.5742	51	-48.0000	-368.1295 50766747 66	6.94%
384963 83446	-105.2105	49	-48.0000	-368.1295 50774019 66	6.94%
386015 84519	-346.9758	297	-48.0000	-368.1265 50783476 66	6.93%

386910 85693	-155.1845	151	-48.0000	-368.1265 50775095	666.93%
387595 84934	-333.2850	217	-48.0000	-368.1265 50794129	666.93%
Elapsed time =	167.93 sec.	(131619.	11 ticks, tree	= 3741.29 MB, soluti	ons = 29)
Nodefile size =	1679.11 MB	(1484.78	MB after comp	ression)	
388775 86007	-55.9050	38	-48.0000	-368.1265 50790936	666.93%
389667 89849	-58.8835	63	-48.0000	-368.1265 51217466	666.93%
390428 84259	-235.6584	138	-48.0000	-368.1265 50820389	666.93%
391907 85686	-200.5898	122	-48.0000	-368.1265 50817259	666.93%
393428 86618	-190.2522	146	-48.0000	-368.1265 51023481	666.93%
394894 85686	-338.0291	262	-48.0000	-368.1265 50892802	666.93%
396235 86317	-283.0987	189	-48.0000	-368.1265 50835383	666.93%
397505 86197	-70.7395	64	-48.0000	-368.1265 50901768	666.93%
398333 86550	-347.5027	457	-48.0000	-368.1265 50846264	666.93%
399245 86427	-177.6206	95	-48.0000	-368.1265 50911461	666.93%
Elapsed time =	217.63 sec.	(169797.	21 ticks, tree	= 3979.15 MB, soluti	ons = 29)
Nodefile size =	1679.11 MB	(1484.78	MB after comp	ression)	
400219 86967	-365.8791	488	-48.0000	-368.1265 50855776	666.93%
401660 91267	-243.3707	155	-48.0000	-368.1265 51274192	666.93%
403296 87512	-341.1402	231	-48.0000	-368.1265 50866250	666.93%
404989 84983	-140.2182	86	-48.0000	-368.0929 50859564	666.86%
406525 88101	-184.9819	105	-48.0000	-368.0929 50876062	666.86%
407805 92086	-259.9844	159	-48.0000	-368.0929 51296163	666.86%
409441 86511	-258.7671	146	-48.0000	-368.0929 50913194	666.86%
411560 92832	-360.5152	318	-48.0000	-368.0929 51306048	666.86%
413551 93075	-71.0918	41	-48.0000	-368.0929 51311387	666.86%
415320 93351	-366.3324	416	-48.0000	-368.0856 51316812	666.84%
Elapsed time =	280.95 sec.	(207992.	61 ticks, tree	= 4136.27 MB, soluti	ons = 29)
Nodefile size =	1679.11 MB	(1484.78	MB after comp	ression)	
416761 93635	-356.6959	307	-48.0000	-368.0856 51321961	666.84%
417641 103611	-333.272	7 267	-48.0000	-368.0856 52115151	666.84%
418995 86717	-91.4659	93	-48.0000	-368.0856 50923115	666.84%
420375 95010	-345.7725	227	-48.0000	-368.0856 51592947	666.84%
422388 97745	-208.8593	113	-48.0000	-368.0856 51806281	666.84%
*424820+95327			-49.0000	-368.0856	651.20%
424875 86974	-117.5452	83	-49.0000	-368.0856 50941301	651.20%
426829 88296	-141.1596	108	-49.0000	-368.0856 51174273	651.20%
428842 87107	-81.6216	48	-49.0000	-368.0856 50956823	651.20%
430040 88694	-143.4552	113	-49.0000	-368.0856 51183846	651.20%
431654 88993	-56.4649	57	-49.0000	-368.0856 51187570	651.20%

Elapsed time = 330.56 sec. (246162.32 ticks, tree = 3912.30 MB, solutions = 30) Nodefile size = 1679.11 MB (1484.78 MB after compression) -368.0856 51192129 651.20% 432487 89155 -309.7494 252 -49.0000 433820 98871 -248.0751 169 -49.0000 -368.0856 51844744 651.20% 434923 89508 -95.4429 54 -49.0000 -368.0856 50996457 651.20% 436455 90671 -329.4717 245 -49.0000 -368.0856 51072363 651.20% -49.0000 438281 90148 -118.6082 102 -368.0856 51006030 651.20% 439742 90497 167 -207.3705 -49.0000 -368.0856 51216254 651.20% 441567 90674 -173.8533 102 -49.0000 -368.0856 51016082 651.20% -303.3454 443828 91216 206 -49.0000 -368.0856 51223635 651.20% 445236 87736 -175.7545 94 -49.0000 -368.0856 51043195 651.20% 447049 91633 -313.8024 195 -49.0000 -368.0856 51113941 651.20% Elapsed time = 373.44 sec. (284339.53 ticks, tree = 4204.39 MB, solutions = 30) Nodefile size = 1679.11 MB (1484.78 MB after compression) 447980 100629 -348.9983 289 -49.0000 -368.0856 51894673 651.20% 449086 92335 75 -49.0000 -368.0856 51244067 651.20% -127.1360 449528 92362 -357.3279 1052 -49.0000 -368.0856 51255961 651.20%

GUB cover cuts applied: 1587

Clique cuts applied: 53 Cover cuts applied: 4561

Implied bound cuts applied: 116

Flow cuts applied: 178

Mixed integer rounding cuts applied: 3530

Zero-half cuts applied: 136

Lift and project cuts applied: 20 Gomory fractional cuts applied: 183

Root node processing (before b&c):

Real time = 0.00 sec. (2.15 ticks)

Parallel b&c, 8 threads:

Real time = 430.29 sec. (305295.57 ticks)

Sync time (average) = 41.19 sec.
Wait time (average) = 0.00 sec.

Total (root+branch&cut) = 430.29 sec. (305297.72 ticks)

Iteration 12

```
Bounds on # of cuts = 8 with [3 3 2]

Error = 51 (out of 100 instances)
```

Accuracy = 49

Solving time = 7.171601351 min (minutes)

Accumulated time = 76.552528166 min (minutes)

Solution status code = 104LB on error = -267.975324274

Relative objective gap = 6.509700495

Selected variables:

A_AGE (Continuous)

PEMLR (Categorical)

Number of selected variables = 2 (1 continuous + 1 categorical)

Version identifier: $22.1.1.0 \mid 2022-11-28 \mid 9160aff4d$

CPXPARAM_MIP_Strategy_File 3

CPXPARAM_MIP_Limits_Solutions

CPXPARAM_TimeLimit 81806.848310058587

CPXPARAM_MIP_Limits_TreeMemory 204800

Nodes Cuts/

Node Left Objective IInf Best Integer Best Bound ItCnt Gap

449529 148551 infeasible -49.0000 -367.9753 54370598 650.97%

Elapsed time = 0.47 sec. (14.98 ticks, tree = 8107.53 MB, solutions = 30)

Nodefile size = 6060.88 MB (5290.89 MB after compression)

449531 148553 -359.5659 442 -49.0000 -367.9753 54371140 650.97% 449538 148551 -49.0000 -367.9753 54371316 650.97% infeasible 449555 148565 -356.7244 318 -49.0000 -367.9753 54371964 650.97% 449593 148577 -332.7352 218 -49.0000 -367.9753 54373247 650.97% 650.97% 449639 148602 -280.7380 198 -49.0000 -367.9753 54373435 449702 148606 -260.2627 157 -49.0000 -367.9753 54373161 650.97% 449786 148649 -166.4203 107 -49.0000 -367.9753 54373940 650.97% 449880 148675 -94.9784 61 -49.0000 -367.9753 54374029 650.97% 449971 148638 -203.4032 129 -49.0000 -367.9753 54375734 650.97% -367.9753 54375106 650.97% 450059 148698 -49.0000 -366.2099 443

Elapsed time = 5.04 sec. (3168.00 ticks, tree = 8124.01 MB, solutions = 30)

Nodefile size = 6	060.88 MB (5	290.89	MB after compre	ession)		
450236 148594	-295.4153	184	-49.0000	-367.9753	54382327	650.97%
450577 148682	-63.8978	27	-49.0000	-367.9753	54385978	650.97%
450591 148559	-360.5034	415	-49.0000	-367.8207	54398193	650.65%
450738 148908	-173.4438	111	-49.0000	-367.8207	54383205	650.65%
450900 148662	-146.4658	101	-49.0000	-367.8207	54401032	650.65%
451012 148976	-333.3717	213	-49.0000	-367.8207	54385969	650.65%
451296 148560	-363.7896	978	-49.0000	-367.6854	54392980	650.38%
451342 149129	-304.8566	181	-49.0000	-367.6854	54388385	650.38%
451481 148830	-361.6500	361	-49.0000	-367.6854	54396382	650.38%
451603 148878	-283.0614	180	-49.0000	-367.6854	54397899	650.38%
Elapsed time = 17	.82 sec. (12	954.41	ticks, tree = 8	3108.39 MB,	solutions	= 30)
Nodefile size = 6	060.88 MB (5	290.89	MB after compre	ession)		
451826 148953	-82.9050	50	-49.0000	-367.6854	54398543	650.38%
451879 148704	-340.0657	313	-49.0000	-367.6854	54393842	650.38%
451961 149414	-296.1621	239	-49.0000	-367.6854	54395518	650.38%
452167 148607	-276.8603	214	-49.0000	-367.6854	54403955	650.38%
452428 149031	-219.7767	147	-49.0000	-367.6854	54406146	650.38%
452701 148652	-365.3107	433	-49.0000	-367.6854	54406178	650.38%
453008 148875	-265.3827	181	-49.0000	-367.6854	54403380	650.38%
453289 149184	-154.6563	92	-49.0000	-367.6854	54411487	650.38%
453348 148960	-360.0414	372	-49.0000	-367.6854	54406637	650.38%
453502 149046	-148.5781	74	-49.0000	-367.6854	54407919	650.38%
Elapsed time = 30	.74 sec. (22	572.71	ticks, tree = 8	3146.19 MB,	solutions	= 30)
Nodefile size = 6	060.88 MB (5	290.89	MB after compre	ession)		
453759 148853	-256.7948	204	-49.0000	-367.6854	54415433	650.38%
453922 148937	-60.9847	87	-49.0000	-367.6854	54416165	650.38%
454060 149366	-363.9560	517	-49.0000	-367.6854	54420697	650.38%
*454067+148947			-50.0000	-367.6854	1	635.37%
454103 149399	-314.6991	203	-50.0000	-367.6854	54422606	635.37%
454237 149500	-56.4004	29	-50.0000	-367.6854	54423429	635.37%
454247 148825	-356.6694	887	-50.0000	-367.6854	54420679	635.37%
454277 148835	-290.6358	185	-50.0000	-367.6854	54422588	635.37%
454414 148923	-67.9049	38	-50.0000	-367.6854	54423303	635.37%
454472 148930	-363.1861	506	-50.0000	-367.6854	54424890	635.37%
454545 149615	-91.8766	82	-50.0000	-367.6854	54431081	635.37%
Elapsed time = 43	.16 sec. (32	219.69	ticks, tree = 8	3192.55 MB,	solutions	= 31)
Nodefile size = 6	060.88 MB (5	290.89	MB after compre	ession)		
454566 149628	-364.7786	412	-50.0000	-367.6854	54432926	635.37%

```
454641 149685
                  -257.6134
                              147
                                       -50.0000
                                                     -367.6854 54434532
                                                                         635.37%
454765 149232
                  -338.9140
                              319
                                       -50.0000
                                                     -367.6854 54425621
                                                                         635.37%
454818 149263
                  -264.9478
                              165
                                       -50.0000
                                                     -367.6854 54427210
                                                                         635.37%
455006 148623
                  -232.9872
                                       -50.0000
                                                     -367.6854 54453546
                              171
                                                                         635.37%
455113 148698
                                       -50.0000
                                                     -367.6854 54454977
                  -365.3190
                              406
                                                                         635.37%
455205 148741
                  -298.9809
                              232
                                       -50.0000
                                                     -367.6854 54456259
                                                                         635.37%
455387 149424
                  -232.1075
                              128
                                       -50.0000
                                                     -367.6854 54435736
                                                                         635.37%
455507 148735
                                                     -367.6854 54427522
                  -264.2029
                              170
                                       -50.0000
                                                                         635.37%
455726 149833
                  -203.7847
                              140
                                       -50.0000
                                                     -367.6854 54447876
                                                                         635.37%
Elapsed time = 54.10 sec. (41946.00 ticks, tree = 8217.64 MB, solutions = 32)
Nodefile size = 6060.88 MB (5290.89 MB after compression)
455921 149884
                                                     -367.6854 54452377 635.37%
                 infeasible
                                       -50.0000
455956 149909
                              221
                                                     -367.6854 54453965
                  -340.9434
                                       -50.0000
                                                                         635.37%
456118 148703
                  -322.7887
                              332
                                       -50.0000
                                                     -367.6854 54448276
                                                                         635.37%
456211 150028
                  -361.5807
                              311
                                       -50.0000
                                                     -367.6854 54457854
                                                                         635.37%
456551 150147
                                                     -367.6854 54458849
                  -90.9050
                               48
                                       -50.0000
                                                                         635.37%
456710 150218
                  -244.2240
                                       -50.0000
                                                     -367.6854 54460397
                              146
                                                                         635.37%
456937 150290
                  -365.6604
                              620
                                       -50.0000
                                                     -367.6854 54461963
                                                                         635.37%
457104 150332
                  -301.2754
                              178
                                       -50.0000
                                                     -367.6854 54463828
                                                                         635.37%
457325 149253
                  -317.2975
                              220
                                       -50.0000
                                                     -367.6854 54475276
                                                                         635.37%
457456 149351
                   -66.9050
                                       -50.0000
                                                     -367.6854 54475951
                               55
                                                                         635.37%
Elapsed time = 68.03 sec. (53360.20 ticks, tree = 8134.99 MB, solutions = 33)
Nodefile size = 6060.88 MB (5290.89 MB after compression)
                                       -50.0000
457550 149392
                                                     -367.6854 54477445
                  -299.9797
                              180
                                                                         635.37%
457686 148828
                  -349.3764
                              432
                                       -50.0000
                                                     -367.6854 54460618
                                                                         635.37%
457810 148869
                  -286.1150
                              166
                                       -50.0000
                                                     -367.6854 54462183
                                                                         635.37%
458021 148956
                  -366.7730
                                       -50.0000
                                                     -367.6854 54465966
                             1041
                                                                         635.37%
458023 148958
                                                     -367.6854 54471615
                  -365.0671
                              968
                                       -50.0000
                                                                         635.37%
458024 148959
                  -363.9372 1032
                                       -50.0000
                                                     -367.6854 54476003
                                                                         635.37%
458026 148959
                                                     -367.6854 54482253
                 infeasible
                                       -50.0000
                                                                         635.37%
458028 149619
                  -355.0212
                              967
                                       -50.0000
                                                     -367.6854 54505490
                                                                         635.37%
458029 149620
                  -354.8428
                              952
                                       -50.0000
                                                     -367.6854 54509299
                                                                         635.37%
458031 148960
                  -361.1371 1077
                                       -50.0000
                                                     -367.6854 54490873
                                                                         635.37%
Elapsed time = 75.01 sec. (76144.16 ticks, tree = 8099.72 MB, solutions = 33)
Nodefile size = 6060.88 MB (5290.89 MB after compression)
                                                     -367.6854 54515789 635.37%
458035 149623
                  -338.0811
                              587
                                       -50.0000
458072 149654
                  -292.3925
                              206
                                       -50.0000
                                                     -367.6854 54517524
                                                                         635.37%
458195 149745
                  -366.2947
                              371
                                       -50.0000
                                                     -367.6854 54518192 635.37%
458268 149801
                  -265.0918
                              206
                                       -50.0000
                                                     -367.6854 54519721 635.37%
```

458362 148969	-339.0310	358	-50.0000	-367.6854 54499208 635.37%
458394 148993	-294.8755	208	-50.0000	-367.6854 54501358 635.37%
458507 149871	-352.6250	646	-50.0000	-367.6854 54535166 635.37%
458509 149873	-348.5649	612	-50.0000	-367.6854 54536702 635.37%
458514 149878	-344.9235	428	-50.0000	-367.6854 54539075 635.37%
458536 149895	-297.6408	238	-50.0000	-367.6854 54541041 635.37%
Elapsed time = 8	8.09 sec. (94	1500.64 t	icks, tree = 8	8197.13 MB, solutions = 33)
Nodefile size =	6060.88 MB (5	5290.89 M	B after compre	ession)
458680 149994	-364.9267	362	-50.0000	-367.6854 54542471 635.37%
458801 149115	-328.4475	206	-50.0000	-367.6854 54526877 635.37%
459008 150143	-344.6698	288	-50.0000	-367.6854 54544620 635.37%
459201 150256	-366.0108	502	-50.0000	-367.6854 54545677 635.37%
459262 150301	-288.3912	191	-50.0000	-367.6854 54547706 635.37%
459384 149217	cutoff		-50.0000	-367.6854 54536299 635.37%
459407 150400	-355.7017	347	-50.0000	-367.6854 54550553 635.37%
459462 150443	-285.5415	194	-50.0000	-367.6854 54552575 635.37%
459552 150512	-80.8691	63	-50.0000	-367.6854 54553583 635.37%
459612 150559	-306.0035	185	-50.0000	-367.6854 54555246 635.37%
Elapsed time = 9	5.25 sec. (10)4655.04	ticks, tree =	8273.17 MB, solutions = 33)
Nodefile size =	6060.88 MB (5	5290.89 M	B after compre	ession)
459757 150659	-364.0543	363	-50.0000	-367.6854 54556163 635.37%
460012 150786	-365.0957	367	-50.0000	-367.6854 54557236 635.37%
460166 150852	-257.4208	157	-50.0000	-367.6854 54558763 635.37%
460271 150928	-364.7451	440	-50.0000	-367.6854 54559507 635.37%
460315 150961	-322.3830	231	-50.0000	-367.6854 54560849 635.37%
460444 151056	-365.3064	533	-50.0000	-367.6854 54562520 635.37%
460460 151063	-349.8631	236	-50.0000	-367.6854 54564641 635.37%
460548 151134	-168.2526	125	-50.0000	-367.6854 54565692 635.37%
460596 149345	-353.9889	773	-50.0000	-367.6854 54557078 635.37%
460634 149374	-285.4250	215	-50.0000	-367.6854 54563745 635.37%
Elapsed time = 1	04.38 sec. (1	17804.09	ticks, tree =	= 8133.27 MB, solutions = 33)
Nodefile size =	6060.88 MB (5	5290.89 M	B after compre	ession)
460972 151200	-309.7938	276	-50.0000	-367.6854 54579043 635.37%
460986 149605	-354.4270	858	-50.0000	-367.6854 54576765 635.37%
461156 149721	-353.2440	644	-50.0000	-367.6854 54594267 635.37%
461200 149747	-319.7503	298	-50.0000	-367.6854 54601578 635.37%
461459 149970	-140.8536	83	-50.0000	-367.6854 54607404 635.37%
461869 150271	-362.2076	370	-50.0000	-367.6854 54611721 635.37%
462205 150520	-348.8006	380	-50.0000	-367.6854 54618159 635.37%

462684 150874 -141.8029 82 -50.0000 -367.6854 54623422 635.37% 462904 151045 -365.6643 568 -50.0000 -367.6854 54630449 635.37% 463109 151192 -349.4642 263 -50.0000 -367.6854 54638262 635.37% Elapsed time = 136.21 sec. (163970.28 ticks, tree = 8327.89 MB, solutions = 34) Nodefile size = 6060.88 MB (5290.89 MB after compression)

GUB cover cuts applied: 1636

Clique cuts applied: 53 Cover cuts applied: 4620

Implied bound cuts applied: 117

Flow cuts applied: 182

Mixed integer rounding cuts applied: 3798

Zero-half cuts applied: 137

Lift and project cuts applied: 21 Gomory fractional cuts applied: 183

Root node processing (before b&c):

Real time = 0.00 sec. (2.40 ticks)

Parallel b&c, 8 threads:

Real time = 139.89 sec. (165844.88 ticks)

Sync time (average) = 3.07 sec.Wait time (average) = 0.00 sec.

Total (root+branch&cut) = 139.89 sec. (165847.28 ticks)

Iteration 13

Bounds on # of cuts = 8 with [3 3 2]

Error = 50 (out of 100 instances)

Accuracy = 50

Solving time = 2.331538167 min (minutes)

Accumulated time = 78.884066333 min (minutes)

Solution status code = 104

LB on error = -267.498135184

Relative objective gap = 6.349962704

Selected variables:

A_AGE (Continuous)

PEMLR (Categorical)

Number of selected variables = 2 (1 continuous + 1 categorical) Version identifier: 22.1.1.0 | 2022-11-28 | 9160aff4d CPXPARAM_MIP_Strategy_File CPXPARAM_MIP_Limits_Solutions 1 81666.956020019526 CPXPARAM_TimeLimit CPXPARAM_MIP_Limits_TreeMemory 204800 Nodes Cuts/ Node Left Objective IInf Best Integer Best Bound ItCnt Gap 463135 158775 infeasible -50.0000 -367.4981 55198048 635.00% Elapsed time = 0.72 sec. (15.17 ticks, tree = 9214.61 MB, solutions = 35) Nodefile size = 7167.73 MB (6279.59 MB after compression) 463136 158777 -366.5895 490 -50.0000 -367.4981 55198583 635.00% 463140 158777 -366.5176 642 -50.0000 -367.4981 55198925 635.00% 463162 158789 -348.1658 230 -50.0000 -367.4981 55199716 635.00% 463191 158808 -305.6908 217 -50.0000 -367.4981 55200151 635.00% 463231 158839 125 -50.0000 -367.4981 55200362 -228.0707 635.00% 463277 158868 87 -50.0000 -367.4981 55200885 -155.1797 635.00% 463346 158903 -50.0000 -367.4981 55201169 -73.9050 40 635.00% 463386 158807 -332.2260 227 -50.0000 -367.4981 55203386 635.00% 463443 158821 -50.0000 -309.8742 204 -367.4981 55202374 635.00% 463885 158912 -57.9050 30 -50.0000 -367.4981 55206450 635.00% Elapsed time = 4.78 sec. (3333.40 ticks, tree = 9185.11 MB, solutions = 35) Nodefile size = 7167.73 MB (6279.59 MB after compression) 463977 158951 -311.4922 247 -50.0000 -367.4981 55207360 635.00% 464319 159014 74 -50.0000 -129.0656 -367.4981 55211007 635.00% 464400 159039 556 -367.4981 55214011 -365.9692 -50.0000 635.00% 464435 158914 -363.0478 611 -50.0000 -367.4981 55217781 635.00% -332.7367 464654 158929 352 -50.0000 -367.4981 55213624 635.00% 464900 158970 -238.0384 158 -50.0000 -367.3236 55215938 634.65% 465154 159315 -57.9050 43 -50.0000 -367.3236 55221298 634.65% 465181 159068 -320.7091 311 -50.0000 -367.3236 55222588 634.65% 465201 158920 -354.1757 744 -50.0000 -367.3236 55218060 634.65% 465256 159111 -246.3611 193 -50.0000 -367.3236 55228446 634.65%

Elapsed time = 18.42 sec. (13757.59 ticks, tree = 9195.97 MB, solutions = 35)

```
Nodefile size = 7167.73 MB (6279.59 MB after compression)
465358 159084
                  -314.4182
                              271
                                        -50.0000
                                                     -367.3236 55226164
                                                                         634.65%
465456 159131
                  -187.6688
                              114
                                        -50.0000
                                                     -367.3236 55228695
                                                                         634.65%
465661 158957
                  -277.9212
                                        -50.0000
                                                     -367.3236 55224025
                              163
                                                                         634.65%
466060 159341
                              208
                                        -50.0000
                                                     -367.3236 55231554
                  -322.8122
                                                                         634.65%
466373 159214
                  -320.7883
                              207
                                        -50.0000
                                                     -367.3236 55238808
                                                                         634.65%
466710 159450
                  -363.6421
                              406
                                        -50.0000
                                                     -367.3236 55235082
                                                                         634.65%
467092 159174
                                                     -367.2274 55234189
                   -82.9050
                               46
                                        -50.0000
                                                                         634.45%
467517 159450
                   -80.0285
                               38
                                        -50.0000
                                                     -367.2274 55243721
                                                                         634.45%
467643 159181
                  -361.5120
                              332
                                        -50.0000
                                                     -367.2274 55237667
                                                                         634.45%
467857 159282
                                        -50.0000
                                                     -367.2274 55239206
                  -137.5505
                               86
                                                                         634.45%
Elapsed time = 30.58 sec. (23322.97 ticks, tree = 9206.18 MB, solutions = 35)
Nodefile size = 7167.73 MB (6279.59 MB after compression)
468131 159579
                   -98.6959
                               54
                                        -50.0000
                                                     -367.2274 55248828
                                                                         634.45%
                  -138.5116
468495 159424
                               92
                                        -50.0000
                                                     -367.2274 55251419
                                                                         634.45%
468860 159757
                                                     -367.2274 55249968
                  -299.5947
                              187
                                        -50.0000
                                                                         634.45%
469263 159717
                  -102.4586
                                        -50.0000
                                                     -367.2274 55254216
                               55
                                                                         634.45%
469473 159677
                  -150.4201
                                        -50.0000
                                                     -367.2274 55251829
                               83
                                                                         634.45%
469748 159820
                  -174.4052
                              108
                                        -50.0000
                                                     -367.2274 55257568
                                                                         634.45%
                  -323.6713
470173 159481
                              253
                                        -50.0000
                                                     -367.2274 55252810
                                                                         634.45%
470415 158856
                  -199.7805
                              124
                                        -50.0000
                                                     -367.2274 55276184
                                                                         634.45%
470751 159959
                  -175.7107
                                        -50.0000
                                                     -367.2274 55263101
                               99
                                                                         634.45%
471015 159827
                                        -50.0000
                                                     -367.2274 55267815 634.45%
                  -151.8560
                               89
Elapsed time = 42.21 sec. (32903.35 ticks, tree = 9179.86 MB, solutions = 35)
Nodefile size = 7167.73 MB (6279.59 MB after compression)
471249 160104
                  -129.7341
                               76
                                       -50.0000
                                                     -367.2274 55266272 634.45%
471728 159717
                                        -50.0000
                                                     -367.2274 55262790
                     cutoff
                                                                         634.45%
472043 158873
                                                     -367.2274 55269576
                  -146.7093
                               92
                                        -50.0000
                                                                         634.45%
472112 159045
                  -359.1444
                              299
                                        -50.0000
                                                     -367.2274 55288895
                                                                         634.45%
472255 159107
                  -255.2068
                                        -50.0000
                                                     -367.2274 55290947
                              161
                                                                         634.45%
472607 160018
                                                     -367.2274 55279581
                  -340.2480
                              214
                                        -50.0000
                                                                         634.45%
473049 160115
                  -107.4381
                               59
                                        -50.0000
                                                     -367.2274 55281245
                                                                         634.45%
473256 160127
                  -327.8756
                                        -50.0000
                                                     -367.2274 55275796
                              214
                                                                         634.45%
473588 159992
                                        -50.0000
                   -67.9050
                               32
                                                     -367.2274 55278335
                                                                         634.45%
                                        -50.0000
                                                     -367.2274 55276168
473847 159971
                  -349.1251
                              284
                                                                         634.45%
Elapsed time = 53.92 sec. (42468.69 ticks, tree = 9219.60 MB, solutions = 35)
Nodefile size = 7167.73 MB (6279.59 MB after compression)
*473936+160266
                                         -51.0000
                                                      -367.2274
                                                                          620.05%
474206 160073
                  -106.9895
                               61
                                       -51.0000
                                                    -367.2274 55277413 620.05%
```

```
474463 160635
                  -153.2612
                               94
                                        -51.0000
                                                     -367.2274 55286212 620.05%
474720 160190
                  -231.7403
                              139
                                        -51.0000
                                                     -367.2274 55285078
                                                                         620.05%
474998 160214
                  -188.9340
                                        -51.0000
                                                     -367.2274 55293399
                              119
                                                                         620.05%
475115 158909
                  -351.2163
                                        -51.0000
                                                     -367.2274 55286348
                              434
                                                                         620.05%
475182 160297
                  -322.9094
                              208
                                        -51.0000
                                                     -367.2274 55297449
                                                                         620.05%
475430 159398
                  -178.7548
                              109
                                        -51.0000
                                                     -367.2274 55314927
                                                                         620.05%
475645 160241
                  -343.1800
                              338
                                        -51.0000
                                                     -367.2274 55290066
                                                                         620.05%
475689 159453
                                                     -367.2274 55318299
                  -352.9342
                              244
                                        -51.0000
                                                                         620.05%
475854 159546
                  -132.8329
                               74
                                        -51.0000
                                                     -367.2274 55319648
                                                                         620.05%
Elapsed time = 65.35 sec. (52182.49 ticks, tree = 9149.24 MB, solutions = 37)
Nodefile size = 7167.73 MB (6279.59 MB after compression)
476031 160718
                  -240.2005
                                                     -367.2274 55306433 620.05%
                              152
                                        -51.0000
476142 159580
                              332
                                                     -367.2274 55324358
                  -362.2827
                                        -51.0000
                                                                         620.05%
476249 160829
                  -310.6718
                              209
                                        -51.0000
                                                     -367.2274 55309938
                                                                         620.05%
476542 159639
                  -255.0189
                              186
                                        -51.0000
                                                     -367.2274 55330168
                                                                         620.05%
476682 159724
                                                     -367.2274 55332953
                  -364.8578
                              329
                                        -51.0000
                                                                         620.05%
476863 159830
                  -123.2319
                                        -51.0000
                                                     -367.2274 55334306
                               72
                                                                         620.05%
477115 159915
                              167
                                        -51.0000
                                                     -367.2274 55335820
                  -264.5046
                                                                         620.05%
477332 159993
                  -363.7070
                              330
                                        -51.0000
                                                     -367.2274 55337385
                                                                         620.05%
477539 160005
                  -346.0468
                              269
                                        -51.0000
                                                     -367.2274 55340473
                                                                         620.05%
477743 160033
                  -289.9295
                              263
                                        -51.0000
                                                     -367.2274 55343355
                                                                         620.05%
Elapsed time = 76.10 sec. (61944.06 ticks, tree = 9151.21 MB, solutions = 37)
Nodefile size = 7167.73 MB (6279.59 MB after compression)
                                        -51.0000
478067 160528
                   -58.4099
                               23
                                                     -367.2274 55320438
                                                                         620.05%
478272 161231
                  -353.4015
                              234
                                        -51.0000
                                                     -367.2274 55327993
                                                                         620.05%
478528 161319
                  -127.3948
                               80
                                        -51.0000
                                                     -367.2274 55330121
                                                                         620.05%
478842 160780
                  -107.5241
                                        -51.0000
                                                     -367.2274 55324854
                                                                         620.05%
                               73
479065 160251
                                                     -367.2274 55353325
                  -364.3253
                              339
                                        -51.0000
                                                                         620.05%
479151 160321
                  -214.6277
                               139
                                        -51.0000
                                                     -367.2274 55354988
                                                                         620.05%
479262 160382
                              407
                                                     -367.2274 55356639
                  -363.8436
                                        -51.0000
                                                                         620.05%
479450 159282
                   -67.9050
                                                     -367.2274 55326580
                               30
                                        -51.0000
                                                                         620.05%
479573 160516
                   -80.8811
                               56
                                        -51.0000
                                                     -367.2274 55359174
                                                                         620.05%
479698 159343
                  -257.4662
                              179
                                        -51.0000
                                                     -367.2274 55329998
                                                                         620.05%
Elapsed time = 87.26 sec. (71569.74 ticks, tree = 9167.39 MB, solutions = 37)
Nodefile size = 7167.73 MB (6279.59 MB after compression)
479968 159410
                                                     -367.2274 55331365 620.05%
                   -78.9050
                               42
                                        -51.0000
480111 160658
                  -364.4200
                              444
                                        -51.0000
                                                     -367.2274 55364600
                                                                         620.05%
480282 159204
                  -331.5965
                              250
                                       -51.0000
                                                     -367.2274 55319373
                                                                         620.05%
480731 161741
                  -101.9345
                                        -51.0000
                                                     -367.2274 55352367
                                                                         620.05%
                               64
```

480977	160912	-99.4795	61	-51.0000	-367.2274	55369544	620.05%
481190	161873	-98.8474	60	-51.0000	-367.2274	55355666	620.05%
481381	159573	-347.1083	234	-51.0000	-367.2274	55341855	620.05%
481707	160908	-133.3562	68	-51.0000	-367.2274	55346119	620.05%
481897	160938	-363.3551	308	-51.0000	-367.2274	55348000	620.05%
481964	162036	-343.0073	212	-51.0000	-367.2274	55364517	620.05%
Elapsed	l time = 98.	33 sec. (81	154.62 tic	ks, tree = 92	209.33 MB,	solutions	= 37)
Nodefil	e size = 71.	.67.73 MB (6	279.59 MB	after compres	ssion)		
482104	162103	-209.0701	120	-51.0000	-367.2274	55366952	620.05%
482251	161057	-106.7135	99	-51.0000	-367.2274	55353243	620.05%
482354	162205	-281.0030	193	-51.0000	-367.2274	55370235	620.05%
482515	161109	-330.1069	237	-51.0000	-367.2274	55357746	620.05%
482708	162411	-81.9050	43	-51.0000	-367.2274	55372148	620.05%
482820	162458	-269.5278	203	-51.0000	-367.2274	55374343	620.05%
482988	161088	-309.6921	433	-51.0000	-367.2274	55399414	620.05%
483039	162556	-348.2095	215	-51.0000	-367.2274	55378317	620.05%
483226	162656	-89.9044	79	-51.0000	-367.2274	55379615	620.05%
483938	161562	-209.0311	125	-51.0000	-367.2274	55374982	620.05%
Elapsed	l time = 113	3.95 sec. (9	3675.38 ti	.cks, tree = 9	9187.73 MB	, solutions	s = 37)
Nodefil	.e size = 71	.67.73 MB (6	279.59 MB	after compres	ssion)		
484586	159413	-172.3045	113	-51.0000	-367.2274	55359518	620.05%
485529	161722	-101.4604	54	-51.0000	-367.2274	55433697	620.05%
486131	161941	-232.0853	139	-51.0000	-367.2274	55443663	620.05%
486946	162526	-81.6550	59	-51.0000	-367.2274	55404513	620.05%
487527	162760	-156.1149	92	-51.0000	-367.2274	55412036	620.05%
488098	162756	-160.2393	94	-51.0000	-367.2274	55463473	620.05%
488873	163196	-364.3675	591	-51.0000	-367.2274	55428823	620.05%
489167	163437	-131.5328	86	-51.0000	-367.2274	55437245	620.05%
489499	163605	-353.8026	297	-51.0000	-367.2274	55443068	620.05%
490304	163909	-255.8353	167	-51.0000	-367.2274	55449013	620.05%
Elapsed	l time = 143	3.38 sec. (1	.32189.37 t	cicks, tree =	9198.49 M	B, solution	ns = 37)
Nodefil	.e size = 71	.67.73 MB (6	279.59 MB	after compres	ssion)		
490905	160344	-153.9110	84	-51.0000	-367.2274	55422663	620.05%
491333	160512	-362.6557	903	-51.0000	-367.2274	55435036	620.05%
491496	164109	-56.2383	27	-51.0000	-367.2274	55478391	620.05%
492194	160785	-95.2200	49	-51.0000	-367.2274	55448138	620.05%
492741	160943	-352.7760	226	-51.0000	-367.2274	55453097	620.05%
493057	164745	-364.0406	1032	-51.0000	-367.2274	55509590	620.05%
493058	164746	-359.9377	895	-51.0000	-367.2274	55516078	620.05%

493120 164797 -239.5931 151 -51.0000 -367.2274 55522135 620.05% 493562 165115 -101.7102 52 -51.0000 -367.2274 55526531 620.05% 493915 165390 -364.7521 472 -51.0000 -367.2274 55531114 620.05% Elapsed time = 181.06 sec. (181989.34 ticks, tree = 9277.64 MB, solutions = 37) Nodefile size = 7167.73 MB (6279.59 MB after compression) 494186 165607 -206.6682 119 -51.0000 -367.2274 55535763 620.05%

GUB cover cuts applied: 1670

Clique cuts applied: 55 Cover cuts applied: 4658

Implied bound cuts applied: 117

Flow cuts applied: 184

Mixed integer rounding cuts applied: 4034

Zero-half cuts applied: 137

Lift and project cuts applied: 21 Gomory fractional cuts applied: 185

Root node processing (before b&c):

Real time = 0.00 sec. (2.58 ticks)

Parallel b&c, 8 threads:

Real time = 188.35 sec. (189207.47 ticks)

Sync time (average) = 8.78 sec.Wait time (average) = 0.00 sec.

Total (root+branch&cut) = 188.35 sec. (189210.06 ticks)

Iteration 14

Bounds on # of cuts = 8 with [3 3 2]

Error = 49 (out of 100 instances)

Accuracy = 51

Solving time = 3.139274398 min (minutes)

Accumulated time = 82.023340731 min (minutes)

Solution status code = 104

LB on error = -267.006174534

Relative objective gap = 6.196199501

Selected variables:

```
A_AGE (Continuous)
```

PEMLR (Categorical)

495298 182342

Number of selected variables = 2 (1 continuous + 1 categorical)

Version identifier: 22.1.1.0 | 2022-11-28 | 9160aff4d

CPXPARAM_MIP_Strategy_File 3

CPXPARAM_MIP_Limits_Solutions 1

CPXPARAM_TimeLimit 81478.599556152345

CPXPARAM_MIP_Limits_TreeMemory 204800

Nodes Cuts/

Node Left Objective IInf Best Integer Best Bound ItCnt Gap

494456 182201 infeasible -51.0000 -367.0062 56675674 619.62%

Elapsed time = 0.24 sec. (15.33 ticks, tree = 9524.00 MB, solutions = 37)

Nodefile size = 7477.22 MB (6520.03 MB after compression)

494475 182210 -351.9932 224 -51.0000 -367.0062 56676084 619.62% 494530 182230 -312.2393 195 -51.0000 -367.0062 56676456 619.62% 494589 182255 -259.6874 171 -51.0000 -367.0062 56676687 619.62% 494665 182282 -180.5270 126 -51.0000 -367.0062 56676863 619.62% 494755 182309 -122.6764 100 -51.0000 -367.0062 56677062 619.62% 494863 182335 -51.0000 -367.0062 56677152 619.62% cutoff 494937 182324 -367.0062 56678670 619.62% -78.8158 40 -51.0000

494991 182280 -211.8674 166 -51.0000 -367.0062 56678002 619.62%

495064 182323 -88.9050 60 -51.0000 -367.0062 56678696 619.62%

-51.0000

-367.0062 56679876 619.62%

Elapsed time = 4.70 sec. (3143.89 ticks, tree = 9530.75 MB, solutions = 37)

Nodefile size = 7477.22 MB (6520.03 MB after compression)

400

-361.4826

495594 182388 -251.8648 214 -51.0000 -367.0062 56683074 619.62% 495860 182577 -108.7543 80 -51.0000 -366.9523 56694950 619.51% 496088 182540 -189.7373 134 -51.0000 -366.9144 56684616 619.44% 496320 182525 -286.3870 178 -51.0000 -366.8762 56685783 619.37% 496537 182580 -366.8762 56706383 -340.4613 383 -51.0000 619.37% -366.8762 56689431 496821 182691 -147.6478 81 -51.0000 619.37% 497372 182733 -88.9050 52 -51.0000 -366.8762 56690879 619.37% 497664 182720 -358.8124 331 -51.0000 -366.8762 56710686 619.37% 498118 182764 -237.3959 195 -51.0000 -366.8762 56719970 619.37% 498480 182825 -73.9050 -51.0000 -366.8762 56720555 619.37% 56

```
Elapsed time = 17.54 sec. (12704.97 ticks, tree = 9531.09 MB, solutions = 37)
Nodefile size = 7477.22 MB (6520.03 MB after compression)
498995 182744
                   -91.4849
                              132
                                       -51.0000
                                                     -366.8762 56695063 619.37%
499164 182989
                  -359.6095
                              298
                                       -51.0000
                                                     -366.8762 56716539
                                                                         619.37%
499601 182253
                  -244.0278
                                       -51.0000
                                                     -366.8762 56701358
                              167
                                                                         619.37%
500209 183036
                  -344.9522
                              226
                                       -51.0000
                                                     -366.8762 56700971
                                                                         619.37%
                                                     -366.8762 56701706
500569 183145
                     cutoff
                                       -51.0000
                                                                         619.37%
500875 183215
                  -223.8724
                              139
                                       -51.0000
                                                     -366.8681 56703419
                                                                         619.35%
501515 183296
                  -345.3847
                              265
                                       -51.0000
                                                     -366.8681 56704825
                                                                         619.35%
502158 182831
                   -92.9050
                               50
                                       -51.0000
                                                     -366.8681 56713383
                                                                         619.35%
502527 183166
                  -226.7766
                              170
                                       -51.0000
                                                     -366.8681 56734624
                                                                         619.35%
502909 182911
                  -262.1243
                                       -51.0000
                                                     -366.8681 56716455 619.35%
                              189
Elapsed time = 31.50 sec. (22253.24 ticks, tree = 9560.30 MB, solutions = 37)
Nodefile size = 7477.22 MB (6520.03 MB after compression)
503332 183801
                  -327.4005
                              260
                                       -51.0000
                                                     -366.8681 56775885 619.35%
503678 183393
                                       -51.0000
                                                     -366.8681 56750272 619.35%
                  -63.9050
                               28
503992 183427
                  -231.5535
                              138
                                       -51.0000
                                                     -366.8681 56739737
                                                                         619.35%
504587 183223
                  -69.9050
                               35
                                       -51.0000
                                                     -366.8681 56721762
                                                                         619.35%
504948 183535
                  -301.0740
                              190
                                       -51.0000
                                                     -366.8681 56742532
                                                                         619.35%
505495 184109
                  -189.3199
                              149
                                       -51.0000
                                                     -366.8681 56735249
                                                                         619.35%
505823 184172
                              255
                                       -51.0000
                                                     -366.8681 56736378
                  -347.1391
                                                                         619.35%
506089 184248
                  -152.5782
                                       -51.0000
                                                     -366.8681 56737407
                               92
                                                                         619.35%
506643 185098
                                                     -366.8681 56816717
                  -102.4718
                               45
                                       -51.0000
                                                                         619.35%
507163 183514
                   -94.8596
                               38
                                       -51.0000
                                                     -366.8681 56762693
                                                                        619.35%
Elapsed time = 46.09 sec. (31831.63 ticks, tree = 9612.19 MB, solutions = 37)
Nodefile size = 7507.91 MB (6546.68 MB after compression)
507847 183617
                  -150.3053
                               85
                                       -51.0000
                                                     -366.8681 56764277 619.35%
508280 183802
                  -328.5517
                              206
                                       -51.0000
                                                     -366.8681 56736660 619.35%
508940 182769
                  -294.7658
                              190
                                       -51.0000
                                                     -366.8681 56727257
                                                                         619.35%
509517 183778
                   -95.4761
                                       -51.0000
                                                     -366.8681 56769219
                               51
                                                                         619.35%
509986 183838
                              199
                                       -51.0000
                                                     -366.8681 56771014
                  -290.1692
                                                                         619.35%
510665 185497
                  -128.6918
                               82
                                       -51.0000
                                                     -366.8681 56826754
                                                                         619.35%
511065 184321
                              177
                                       -51.0000
                                                     -366.8681 56758291
                  -310.4287
                                                                         619.35%
511453 184748
                  -323.7543
                              217
                                       -51.0000
                                                     -366.8681 56799934
                                                                         619.35%
511733 185661
                  -352.0178
                              342
                                       -51.0000
                                                     -366.8681 56831520
                                                                         619.35%
512296 184878
                  -331.4491
                              218
                                       -51.0000
                                                     -366.8681 56802445
                                                                         619.35%
Elapsed time = 57.78 sec. (41390.10 ticks, tree = 9769.69 MB, solutions = 37)
Nodefile size = 7582.35 MB (6611.74 MB after compression)
512740 183738
                  -354.3047
                              315
                                       -51.0000
                                                    -366.8681 56746494 619.35%
```

```
513064 183797
                  -218.5924
                              179
                                       -51.0000
                                                    -366.8681 56747822 619.35%
513481 184788
                   -81.0717
                               42
                                       -51.0000
                                                    -366.8681 56759505
                                                                        619.35%
513901 185908
                   -76.0885
                               72
                                       -51.0000
                                                    -366.8681 56837494
                                                                        619.35%
514340 185153
                  -329.4190
                              291
                                       -51.0000
                                                    -366.8681 56808466
                                                                         619.35%
514728 186009
                  -167.6558
                                       -51.0000
                                                    -366.8681 56840056
                              111
                                                                         619.35%
515145 186083
                  -313.4338
                              183
                                       -51.0000
                                                    -366.8681 56841160
                                                                         619.35%
515566 186176
                  -351.2108
                              233
                                       -51.0000
                                                    -366.8681 56842573
                                                                         619.35%
516099 183458
                  -234.0999
                              156
                                       -51.0000
                                                    -366.8681 56749879
                                                                         619.35%
516357 184213
                  -145.4731
                               71
                                       -51.0000
                                                    -366.8681 56758558
                                                                         619.35%
Elapsed time = 70.16 sec. (50950.48 ticks, tree = 9712.96 MB, solutions = 37)
Nodefile size = 7477.22 MB (6520.03 MB after compression)
516670 183638
                   -94.4050
                                                    -366.8681 56751485 619.35%
                                       -51.0000
516864 185539
                                                    -366.8681 56816763 619.35%
                  -353.3629
                              464
                                       -51.0000
517026 184475
                  -139.9466
                               79
                                       -51.0000
                                                    -366.8681 56762655
                                                                         619.35%
                  -107.6787
517314 183765
                               60
                                       -51.0000
                                                    -366.8681 56756087
                                                                         619.35%
517555 183845
                                                    -366.8681 56757069
                  -229.9116
                              137
                                       -51.0000
                                                                         619.35%
517758 185685
                  -338.3882
                                       -51.0000
                                                    -366.8681 56822383
                              320
                                                                         619.35%
517891 186354
                                       -51.0000
                                                    -366.8681 56852885
                  -219.8397
                              132
                                                                         619.35%
518073 184508
                  -358.8005
                              571
                                       -51.0000
                                                    -366.8681 56769302
                                                                         619.35%
518144 186464
                  -294.3353
                              217
                                       -51.0000
                                                    -366.8681 56855343
                                                                         619.35%
                  -338.0686
518452 184522
                              327
                                       -51.0000
                                                    -366.8681 56773560
                                                                        619.35%
Elapsed time = 82.11 sec. (60586.41 ticks, tree = 9748.86 MB, solutions = 37)
Nodefile size = 7477.22 MB (6520.03 MB after compression)
518550 186598
                                                    -366.8681 56857731 619.35%
                  -301.8589
                              186
                                       -51.0000
518811 184586
                  -223.8810
                              142
                                       -51.0000
                                                    -366.8681 56777456
                                                                        619.35%
519155 186711
                  -339.9077
                              213
                                       -51.0000
                                                    -366.8681 56860244
                                                                        619.35%
519520 184342
                  -334.0798
                                       -51.0000
                                                    -366.8681 56774326 619.35%
                              215
520022 184788
                                                    -366.8681 56781028 619.35%
                  -364.9442
                              404
                                       -51.0000
520231 184896
                  -112.3531
                               60
                                       -51.0000
                                                    -366.8681 56782057
                                                                         619.35%
520511 186342
                                                    -366.8681 56836938
                   -61.9044
                               48
                                       -51.0000
                                                                         619.35%
520730 185006
                                                    -366.8681 56821850
                  -324.4910
                              234
                                       -51.0000
                                                                         619.35%
521264 186394
                  -278.5470
                              174
                                       -51.0000
                                                    -366.8681 56840495
                                                                         619.35%
521704 187004
                                       -51.0000
                                                    -366.8681 56869988 619.35%
                 infeasible
Elapsed time = 94.06 sec. (70165.35 ticks, tree = 10016.79 MB, solutions = 37)
Nodefile size = 7722.86 MB (6734.35 MB after compression)
522368 185197
                  -202.6451
                              126
                                       -51.0000
                                                    -366.8681 56827042 619.35%
523238 186645
                  -324.7403
                              228
                                       -51.0000
                                                    -366.8681 56843991 619.35%
523980 184871
                  -232.7469
                                       -51.0000
                                                    -366.8681 56807304 619.35%
                              163
524708 185358
                              125
                                       -51.0000
                                                    -366.8681 56831143 619.35%
                  -157.1693
```

525280 185365	-269.3653	153	-51.0000	-366.8681 56795954	619.35%
526076 187442	-206.7137	130	-51.0000	-366.8681 56875020	619.35%
526790 187097	-172.2746	99	-51.0000	-366.8681 56849651	619.35%
527291 187608	-120.3658	68	-51.0000	-366.8681 56877135	619.35%
527767 187253	-100.7237	59	-51.0000	-366.8681 56851707	619.35%
528154 185854	-221.2637	143	-51.0000	-366.8681 56837647	619.35%
Elapsed time = 1	05.04 sec. (7	9721.7	78 ticks, tree =	9885.67 MB, solutions	s = 37)
Nodefile size =	7507.91 MB (6	546.68	B MB after compre	ession)	
528448 185109	-360.5449	304	-51.0000	-366.8681 56798386	619.35%
528973 187895	-53.9050	24	-51.0000	-366.8681 56882736	619.35%
529424 187460	-214.0870	144	-51.0000	-366.8681 56857690	619.35%
529852 185284	-258.7113	179	-51.0000	-366.8681 56801753	619.35%
530303 185125	-310.7185	195	-51.0000	-366.8681 56801060	619.35%
530717 186242	-282.9556	190	-51.0000	-366.8681 56845048	619.35%
531229 188181	-355.5929	249	-51.0000	-366.8681 56888841	619.35%
531749 185561	-244.8323	151	-51.0000	-366.8681 56806389	619.35%
532217 187856	-154.1270	103	-51.0000	-366.8681 56865472	619.35%
534491 186745	-336.7932	237	-51.0000	-366.8681 56853455	619.35%
Elapsed time = 1	19.93 sec. (9	2134.2	22 ticks, tree =	9989.67 MB, solutions	s = 37)
Nodefile size =	7507.91 MB (6	546.68	B MB after compre	ession)	
537173 186121	-92.9050	64	-51.0000	-366.8681 56817216	619.35%
539433 186104	-360.0615	320	-51.0000	-366.8681 56829949	619.35%
541783 189363	-350.7550	227	-51.0000	-366.8681 56911498	619.35%
544525 189732	-354.4750	399	-51.0000	-366.8681 56916526	619.35%
547325 187207	-180.8447	112	-51.0000	-366.8681 56852153	619.35%
549534 187269	-359.7960	299	-51.0000	-366.8681 56841886	619.35%
552483 188561	-76.0000	37	-51.0000	-366.8681 56890908	619.35%
555018 187941	-292.0210	169	-51.0000	-366.8681 56850235	619.35%
557686 188231	-248.4755	165	-51.0000	-366.8681 56855537	619.35%
560583 190787	-328.4668	210	-51.0000	-366.8681 56924690	619.35%
Elapsed time = 1	65.90 sec. (1	.30289.	67 ticks, tree =	= 10459.45 MB, solutio	ons = 37)
Nodefile size =	7582.35 MB (6	611.74	MB after compre	ession)	
563125 189628	-59.9050	34	-51.0000	-366.8681 56911187	619.35%
565396 189136	-263.8448	164	-51.0000	-366.8681 56885160	619.35%
568071 190242	-138.8590	81	-51.0000	-366.8209 56920270	619.26%
570320 189734	-104.5327	70	-51.0000	-366.8209 56893599	619.26%
573161 191852	-256.3504	179	-51.0000	-366.8209 57017459	619.26%
575843 191145	-210.8755	128	-51.0000	-366.8209 56934904	619.26%
578475 190142	-345.4650	248	-51.0000	-366.8209 56896990	619.26%

	581192	192533	-166.7373	98	-51.0000	-366.8209 57036295	619.26%
	583459	192174	-248.0752	140	-51.0000	-366.8209 56949279	619.26%
	585497	192912	-207.3005	124	-51.0000	-366.8209 57048453	619.26%
	Elapsed	time = 227	.81 sec. (1	68444.95 t	cicks, tree =	10705.98 MB, solution	ons = 37)
	Nodefil	e size = 84	70.98 MB (7	389.34 MB	after compres	ssion)	
	587923	194446	-219.1194	128	-51.0000	-366.8209 57002407	619.26%
	590344	193814	-191.1955	108	-51.0000	-366.8209 56985418	619.26%
	592510	191113	-132.6357	88	-51.0000	-366.8209 56935710	619.26%
	594613	193928	-278.0600	157	-51.0000	-366.8209 57069018	619.26%
	596034	194250	-121.5324	72	-51.0000	-366.8209 57074094	619.26%
	597396	191764	-298.5444	188	-51.0000	-366.8209 56955753	619.26%
	598784	192141	-156.6665	97	-51.0000	-366.8209 56955666	619.26%
	599769	192343	-327.9550	264	-51.0000	-366.8209 56962010	619.26%
	600940	192582	-61.4004	30	-51.0000	-366.8209 56968128	619.26%
	602947	191282	-360.3925	339	-51.0000	-366.8209 56966375	619.26%
	Elapsed	time = 273	.41 sec. (2	06606.47 t	cicks, tree =	10538.83 MB, solution	ons = 37)
	Nodefil	e size = 74	77.22 MB (6	520.03 MB	after compres	ssion)	
	604824	195159	-209.5223	165	-51.0000	-366.8209 57110082	619.26%
	606991	194686	-228.1652	141	-51.0000	-366.8209 57033764	619.26%
	609377	196058	-89.4794	40	-51.0000	-366.8209 57072395	619.26%
	611483	196054	-210.2735	128	-51.0000	-366.8209 57126646	619.26%
	612145	196417	-241.6389	147	-51.0000	-366.8209 57130810	619.26%
	612256	195015	-359.0492	1034	-51.0000	-366.8125 57046859	619.24%
	612368	217470	-320.2838	211	-51.0000	-366.7797 57738968	619.18%
	612887	228501	-284.2145	276	-51.0000	-366.7797 58010282	619.18%
	613500	239780	-358.5293	274	-51.0000	-366.7797 58330379	619.18%
	613861	251538	-360.7471	397	-51.0000	-366.7514 58625105	619.12%
	Elapsed	time = 387	.78 sec. (2	45504.90 t	cicks, tree =	17529.07 MB, solution	ons = 37)
Nodefile size = 15466.73 MB (13518.12 MB after compression)							
	615353	239610	-359.5604	1040	-51.0000	-366.7514 58326157	619.12%
	616586	263789	-273.0794	174	-51.0000	-366.7514 58939204	619.12%
	617658	274839	-355.0167	266	-51.0000	-366.3450 59284748	618.32%
	618974	275150	-281.4216	230	-51.0000	-366.3450 59302104	618.32%
	620336	276782	-209.2482	130	-51.0000	-366.3450 59362700	618.32%
	621684	277961	-214.6874	119	-51.0000	-366.3450 59441273	618.32%
	622900	278715	-298.6923	213	-51.0000	-366.3450 59465451	618.32%
	624291	279922	-315.4854	231	-51.0000	-366.3450 59533597	618.32%
	625218	281037	-120.8353	63	-51.0000	-366.3450 59570495	618.32%
	625993	281792	-361.4253	347	-51.0000	-366.3450 59617364	618.32%

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Elapsed time = 469.11 sec. (283897.44 ticks, tree = 21071.25 MB, solutions = 37)
Nodefile size = 18993.43 MB (16609.64 MB after compression)
626629 282086
                  -355.1436
                              393
                                       -51.0000
                                                    -366.3450 59634771 618.32%
627551 282737
                  -161.8955
                                       -51.0000
                                                    -366.3450 59683802 618.32%
                              100
628412 283151
                  -358.0560
                                                    -366.3450 59702143
                              333
                                       -51.0000
                                                                         618.32%
629606 283908
                  -223.1311
                              128
                                       -51.0000
                                                    -366.3358 59768358
                                                                        618.31%
630987 285351
                  -186.6854
                              131
                                       -51.0000
                                                    -365.9983 59853631
                                                                         617.64%
631970 286256
                  -60.4004
                               37
                                       -51.0000
                                                    -365.9983 59881553
                                                                        617.64%
632808 286815
                  -190.7839
                              136
                                       -51.0000
                                                    -365.9983 59919228
                                                                         617.64%
634294 287409
                  -119.7052
                               96
                                       -51.0000
                                                    -365.9983 59983074
                                                                         617.64%
635715 288834
                              320
                                       -51.0000
                                                    -365.8797 60038286
                  -355.2322
                                                                        617.41%
636500 289526
                  -336.6266
                                                    -365.8797 60093169 617.41%
                              237
                                       -51.0000
Elapsed time = 527.49 sec. (322134.89 ticks, tree = 22006.45 MB, solutions = 37)
Nodefile size = 19922.83 MB (17427.82 MB after compression)
637899 289868
                  -261.2537
                              170
                                       -51.0000
                                                    -365.8532 60117036 617.36%
639303 291156
                  -357.4336
                              362
                                       -51.0000
                                                    -365.8468 60164756 617.35%
640364 292296
                  -357.0002
                              225
                                       -51.0000
                                                    -365.8468 60205310
                                                                         617.35%
641826 293296
                                       -51.0000
                                                    -365.8468 60231289
                  -129.2980
                               67
                                                                         617.35%
643710 294344
                  -324.7103
                              219
                                       -51.0000
                                                    -365.8468 60275209
                                                                         617.35%
645087 295929
                  -357.5296
                              251
                                       -51.0000
                                                    -365.8468 60347341
                                                                         617.35%
647574 297096
                              347
                                       -51.0000
                                                    -365.8468 60403205
                  -361.3072
                                                                         617.35%
650132 298525
                                       -51.0000
                                                    -365.8468 60437070
                  -157.9824
                               91
                                                                         617.35%
652370 300285
                                                    -365.8468 60481233 617.35%
                  -215.2495
                              130
                                       -51.0000
653642 302565
                  -225.2487
                              127
                                       -51.0000
                                                    -365.8468 60540176 617.35%
Elapsed time = 588.75 sec. (360318.24 ticks, tree = 23214.25 MB, solutions = 37)
Nodefile size = 21147.62 MB (18482.80 MB after compression)
655359 303578
                  -241.1639
                              143
                                       -51.0000
                                                    -365.8468 60576128 617.35%
656778 304539
                                                    -365.7387 60611664 617.13%
                  -233.3815
                              133
                                       -51.0000
658460 305910
                  -334.7923
                              278
                                       -51.0000
                                                    -365.6873 60683628 617.03%
661036 307178
                                                    -365.6873 60721530
                  -306.5428
                              187
                                       -51.0000
                                                                         617.03%
662791 308542
                  -360.1018
                              349
                                       -51.0000
                                                    -365.6873 60767056
                                                                        617.03%
664931 310615
                   -73.4004
                               33
                                       -51.0000
                                                    -365.6873 60843282
                                                                         617.03%
666181 311479
                   -80.9050
                                                    -365.5489 60873920
                               38
                                       -51.0000
                                                                         616.76%
667712 313460
                  -341.7799
                              221
                                       -51.0000
                                                    -365.4342 60942375
                                                                         616.54%
668738 314033
                  -250.3615
                              164
                                       -51.0000
                                                    -365.4342 60969439
                                                                         616.54%
670378 314777
                  -340.3181
                              254
                                       -51.0000
                                                    -365.4342 61007417 616.54%
Elapsed time = 648.51 sec. (398512.68 ticks, tree = 24220.43 MB, solutions = 37)
Nodefile size = 22149.07 MB (19347.63 MB after compression)
671660 316624
                  -190.6028
                              117
                                       -51.0000
                                                    -365.4342 61082628 616.54%
```

673339 316740	-255.8649	201	-51.0000	-365.4342 61117104	616.54%		
675296 318619	-119.2922	64	-51.0000	-365.4342 61162844	616.54%		
677401 320444	-231.1208	167	-51.0000	-365.4342 61223447	616.54%		
679864 321923	-307.6958	207	-51.0000	-365.4342 61254347	616.54%		
681222 323429	-355.7521	293	-51.0000	-365.4342 61293481	616.54%		
682604 324985	-164.2641	90	-51.0000	-365.3694 61405616	616.41%		
684015 325743	-179.6358	117	-51.0000	-365.3555 61458609	616.38%		
685518 327413	-250.6560	141	-51.0000	-365.3071 61539485	616.29%		
687434 328626	-146.6897	95	-51.0000	-365.3062 61584384	616.29%		
Elapsed time = 708.04 sec. (436685.01 ticks, tree = 25451.98 MB, solutions = 37)							
Nodefile size =	23372.09 MB ((20413.	94 MB after comp	ression)			
689399 329467	-99.3480	36	-51.0000	-365.2479 61635355	616.17%		
691000 331344	-346.8231	238	-51.0000	-365.2050 61692904	616.09%		
692237 332230	-329.2119	241	-51.0000	-365.2050 61733192	616.09%		
693523 332898	-86.5479	42	-51.0000	-365.2050 61759830	616.09%		
694552 333849	-187.8206	113	-51.0000	-365.1849 61826192	616.05%		
696545 334946	-64.0000	28	-51.0000	-365.1849 61889587	616.05%		
698225 336435	-223.7746	142	-51.0000	-365.1395 61969519	615.96%		
700385 337181	-141.2558	76	-51.0000	-365.1393 61999411	615.96%		
701942 339213	-228.3630	129	-51.0000	-365.1151 62061295	615.91%		
703039 340138	-336.6943	518	-51.0000	-365.1074 62106040	615.90%		
Elapsed time = 7	'69.48 sec. (4	174868.	46 ticks, tree =	26523.33 MB, soluti	ons = 37)		
Nodefile size =	24455.97 MB ((21345.	49 MB after comp	ression)			
703806 340972	-154.5474	96	-51.0000	-365.1074 62151674	615.90%		
704648 342280	-338.7462	252	-51.0000	-365.1031 62231946	615.89%		
705803 342510	-349.4838	328	-51.0000	-365.0948 62264654	615.87%		
706909 343736	-348.7916	269	-51.0000	-365.0948 62339333	615.87%		
708639 344121	-208.9617	132	-51.0000	-365.0948 62361186	615.87%		
710029 345547	-179.6985	112	-51.0000	-365.0948 62447113	615.87%		
711771 346626	-185.8141	108	-51.0000	-365.0912 62486059	615.87%		
712627 348066	-362.4201	343	-51.0000	-365.0912 62582067	615.87%		
713715 348780	-80.0606	43	-51.0000	-365.0912 62624224	615.87%		
715391 349314	-306.6991	235	-51.0000	-365.0912 62666144	615.87%		
Elapsed time = 824.55 sec. (513173.77 ticks, tree = 26881.08 MB, solutions = 37)							
Nodefile size = 24808.87 MB (21640.42 MB after compression)							
717378 350702	-353.4336	324	-51.0000	-365.0912 62715620	615.87%		
719540 351649	-316.9172	222	-51.0000	-365.0912 62746033	615.87%		
721322 353579	-162.3109	86	-51.0000	-365.0912 62799262	615.87%		
723113 355134	-63.9143	35	-51.0000	-365.0289 62843640	615.74%		

724802 356270	-143.9895	81	-51.0000	-365.0169 62884338 615.72%		
726441 357146	-175.7427	100	-51.0000	-365.0169 62911220 615.72%		
728427 358874	-343.8456	331	-51.0000	-365.0169 63006867 615.72%		
731003 361195	-342.7434	262	-51.0000	-365.0169 63074158 615.72%		
733427 361941	-268.4267	171	-51.0000	-364.9677 63090909 615.62%		
735290 363459	cutoff		-51.0000	-364.9677 63130298 615.62%		
Elapsed time = 8	85.78 sec. (5	51330.	14 ticks, tree	= 28246.52 MB, solutions = 37)		
Nodefile size =	26162.99 MB (22819.	78 MB after com	pression)		
737115 365594	-144.9050	89	-51.0000	-364.9635 63178021 615.61%		
738541 366505	-117.0880	69	-51.0000	-364.9446 63192669 615.58%		
739326 367895	-338.1909	310	-51.0000	-364.9446 63273313 615.58%		
740151 368444	-354.4144	323	-51.0000	-364.9446 63300507 615.58%		
742291 369430	-258.6669	164	-51.0000	-364.9336 63409029 615.56%		
745357 370124	-133.1314	67	-51.0000	-364.9268 63420455 615.54%		
747378 373306	-70.4004	24	-51.0000	-364.9221 63486694 615.53%		
749580 374547	-60.0000	43	-51.0000	-364.9158 63533026 615.52%		
752396 376503	-224.8379	132	-51.0000	-364.9158 63590702 615.52%		
753817 377198	-110.4004	59	-51.0000	-364.9158 63601596 615.52%		
Elapsed time = 9	47.27 sec. (5	89510.	67 ticks, tree	= 29838.63 MB, solutions = 37)		
Nodefile size =	27723.94 MB (24182.	95 MB after com	pression)		
754664 378350	-313.3719	241	-51.0000	-364.9158 63637522 615.52%		
755945 380009	-132.6635	77	-51.0000	-364.8896 63692159 615.47%		
756996 381032	-114.4004	55	-51.0000	-364.8721 63750087 615.44%		
758046 382017	-353.4691	330	-51.0000	-364.8721 63794359 615.44%		
758657 382456	-354.2886	246	-51.0000	-364.8721 63843088 615.44%		
759881 382519	-240.3827	153	-51.0000	-364.8710 63859500 615.43%		
761113 384017	-109.7342	57	-51.0000	-364.8710 63946364 615.43%		
762231 384489	-201.7776	137	-51.0000	-364.8699 63967543 615.43%		
763687 385146	-167.7341	97	-51.0000	-364.8699 64005961 615.43%		
764990 386464	-360.0574	326	-51.0000	-364.8699 64058084 615.43%		
Elapsed time = 1	005.19 sec. (627814	1.24 ticks, tree	= 30794.27 MB, solutions = 37)		
Nodefile size = 28692.51 MB (25023.74 MB after compression)						
765714 386900	-139.3959	80	-51.0000	-364.8697 64109034 615.43%		
766817 387531	-295.4339	190	-51.0000	-364.8697 64159777 615.43%		
767913 388740	-70.4004	29	-51.0000	-364.8697 64211795 615.43%		
768975 390150	-137.9050	71	-51.0000	-364.8697 64307062 615.43%		
771045 390586	-353.6152	274	-51.0000	-364.8488 64348089 615.39%		
773557 392244	-62.7203	32	-51.0000	-364.8292 64409874 615.35%		
775988 394237	cutoff		-51.0000	-364.8095 64462634 615.31%		

	777702 396139	-166.8143	88	-51.0000	-364.8095	64503623	615.31%
	779614 396520	-122.6436	68	-51.0000	-364.7910	64539613	615.28%
	782146 398855	-312.5603	192	-51.0000	-364.7910	64610935	615.28%
	Elapsed time = :	1065.82 sec.	(665982	2.42 ticks, tree	= 32000.35	MB, solut	ions = 37)
	Nodefile size =	29928.83 MB	(26098.	.76 MB after comp	oression)		
	784000 399838	-224.3325	136	-51.0000	-364.7910	64651290	615.28%
	785883 401786	-194.0282	115	-51.0000	-364.7910	64740881	615.28%
	787276 402494	-236.2952	187	-51.0000	-364.7910	64773173	615.28%
	788203 403332	-208.3501	132	-51.0000	-364.7626	64821019	615.22%
	789654 404080	-274.5377	173	-51.0000	-364.7626	64871019	615.22%
	791185 405717	-136.7522	74	-51.0000	-364.7626	64928476	615.22%
	792944 407063	-143.8552	81	-51.0000	-364.7489	65009012	615.19%
	794449 407935	-60.4004	35	-51.0000	-364.7489	65055525	615.19%
	796012 408937	-244.0269	148	-51.0000	-364.7489	65090206	615.19%
	797658 410676	-108.4004	65	-51.0000	-364.7316	65157440	615.16%
	Elapsed time = :	1123.50 sec.	(704203	3.36 ticks, tree	= 32906.29	MB, solut	ions = 37)
	Nodefile size =	30835.32 MB	(26886.41 MB after compression)				
	799447 411601	-334.4220	270	-51.0000	-364.7302	65214712	615.16%
	800825 412665	-327.5934	259	-51.0000	-364.7141	65259056	615.13%
	801941 413971	-339.3653	241	-51.0000	-364.7058	65332119	615.11%
	803933 414717	-68.2934	28	-51.0000	-364.7058	65352630	615.11%
	806553 416163	-182.9371	105	-51.0000	-364.7058	65420516	615.11%
	808329 417827	-92.0000	46	-51.0000	-364.6968	65446803	615.09%
	809926 419512	-324.4454	225	-51.0000	-364.6968	65503730	615.09%
	811015 420726	-346.9501	222	-51.0000	-364.6855	65546728	615.07%
	812351 421285	-332.8297	220	-51.0000	-364.6809	65576229	615.06%
	813635 422486	-188.0082	108	-51.0000	-364.6809	65605887	615.06%
	<pre>Elapsed time = 3</pre>	1183.30 sec.	(742384	1.03 ticks, tree	= 34000.77	MB, solut	ions = 37)
Nodefile size = 31911.50 MB		(27825.	.65 MB after comp	oression)			
	815552 423494	-73.9775	32	-51.0000	-364.6777	65663571	615.05%
	817134 424794	-341.0814	263	-51.0000	-364.6777	65690837	615.05%
	818641 426281	-180.3990	110	-51.0000	-364.6777	65757727	615.05%
	820682 426974	-165.8716	91	-51.0000	-364.6777	65800359	615.05%
	822833 428289	-84.4004	53	-51.0000	-364.6777	65824189	615.05%
	824603 430176	-322.1515	209	-51.0000	-364.6777	65871864	615.05%
	826717 432281	-222.8604	118	-51.0000	-364.6777	65938161	615.05%
	828986 432669	-221.0570	168	-51.0000	-364.6777	65943629	615.05%
	830980 435000	-274.5929	162	-51.0000	-364.6777	66001113	615.05%
	833801 436907	-324.0902	213	-51.0000	-364.6475	66128348	615.00%

```
Elapsed time = 1245.90 sec. (780552.64 ticks, tree = 35882.93 MB, solutions = 37)
Nodefile size = 33776.48 MB (29467.99 MB after compression)
835709 439181
                  -133.2156
                               72
                                       -51.0000
                                                    -364.6475 66178885 615.00%
837674 439908
                  -175.4624
                                       -51.0000
                                                    -364.6475 66189714
                              114
                                                                        615.00%
839601 441162
                  -250.9862
                              176
                                       -51.0000
                                                    -364.6475 66240455
                                                                         615.00%
841355 442464
                  -300.2932
                              199
                                       -51.0000
                                                    -364.5726 66291801
                                                                         614.85%
842695 444227
                  -317.4591
                              246
                                       -51.0000
                                                    -364.5726 66361667
                                                                         614.85%
844185 445795
                  -174.4656
                               98
                                       -51.0000
                                                    -364.5726 66440393
                                                                        614.85%
845686 446846
                  -285.6416
                              179
                                       -51.0000
                                                    -364.5718 66500594
                                                                         614.85%
                  -114.7342
847592 448069
                               59
                                       -51.0000
                                                    -364.5542 66550404
                                                                        614.81%
849312 448835
                                       -51.0000
                                                    -364.5542 66582371
                  -257.9658
                              167
                                                                        614.81%
851394 450013
                                       -51.0000
                                                    -364.5542 66633782 614.81%
                  -314.9399
                              211
Elapsed time = 1307.35 sec. (818726.26 ticks, tree = 37244.89 MB, solutions = 37)
Nodefile size = 35133.82 MB (30656.34 MB after compression)
853084 452324
                  -312.0660
                              196
                                       -51.0000
                                                    -364.5542 66693652 614.81%
854812 453846
                  -356.9786
                              261
                                       -51.0000
                                                    -364.5542 66761242 614.81%
855968 454651
                  -63.4004
                                       -51.0000
                                                    -364.5542 66802143
                               24
                                                                        614.81%
857129 455667
                                       -51.0000
                                                    -364.5490 66843806
                  -171.9293
                               96
                                                                        614.80%
858381 456135
                  -163.1172
                               96
                                       -51.0000
                                                    -364.5490 66892873
                                                                        614.80%
860461 456922
                   -61.1046
                               29
                                       -51.0000
                                                    -364.5490 66953083
                                                                         614.80%
862972 458277
                                       -51.0000
                                                    -364.5200 66982830
                  -214.0353
                              124
                                                                        614.75%
865304 460473
                  -180.0223
                                       -51.0000
                                                    -364.5200 67059361
                              111
                                                                         614.75%
867660 461169
                                                    -364.4985 67072536
                  -321.5716
                              208
                                       -51.0000
                                                                        614.70%
870293 463316
                  -340.5852
                              217
                                       -51.0000
                                                    -364.4819 67128946 614.67%
Elapsed time = 1368.78 sec. (856888.40 ticks, tree = 38648.48 MB, solutions = 37)
Nodefile size = 36539.17 MB (31877.98 MB after compression)
873538 467608
                  -217.7467
                              139
                                       -51.0000
                                                    -364.4664 67233746 614.64%
876593 467125
                  -244.4728
                              135
                                       -51.0000
                                                    -364.4574 67228464 614.62%
879178 470882
                  -154.9824
                              104
                                       -51.0000
                                                    -364.4499 67296718 614.61%
881958 472445
                                                    -364.4351 67334944
                  -284.8297
                              214
                                       -51.0000
                                                                         614.58%
884732 474861
                                                    -364.4351 67377191
                  -279.1491
                              156
                                       -51.0000
                                                                        614.58%
887617 477416
                  -315.0698
                              194
                                       -51.0000
                                                    -364.4211 67435378
                                                                         614.55%
890379 478124
                                                    -364.4195 67448458
                  -214.2439
                              123
                                       -51.0000
                                                                         614.55%
892245 480785
                  -325.1725
                              248
                                       -51.0000
                                                    -364.4066 67510545
                                                                        614.52%
894557 482750
                  -324.9394
                              205
                                       -51.0000
                                                    -364.4066 67569546
                                                                        614.52%
896840 483406
                  -343.9195
                              287
                                       -51.0000
                                                    -364.3964 67595487 614.50%
Elapsed time = 1434.42 sec. (895055.27 ticks, tree = 41047.78 MB, solutions = 37)
Nodefile size = 38972.02 MB (34000.81 MB after compression)
898846 485804
                  -362.7281
                              405
                                       -51.0000
                                                    -364.3964 67685395 614.50%
```

```
900772 486739
                  -93.3809
                               45
                                        -51.0000
                                                     -364.3964 67709447 614.50%
902306 488326
                  -249.0641
                              223
                                        -51.0000
                                                     -364.3780 67756185
                                                                         614.47%
904443 489887
                              107
                                        -51.0000
                                                     -364.3780 67817292 614.47%
                  -182.8472
906206 491028
                  -234.4828
                                        -51.0000
                                                     -364.3780 67848657
                              133
                                                                         614.47%
907466 491892
                                                     -364.3676 67899357
                  -312.0740
                              182
                                        -51.0000
                                                                         614.45%
908931 493915
                  -326.9604
                              233
                                        -51.0000
                                                     -364.3676 67959190
                                                                         614.45%
910191 494806
                  -275.8860
                              191
                                        -51.0000
                                                     -364.3676 68017211
                                                                         614.45%
911432 496455
                   -70.3965
                               32
                                        -51.0000
                                                     -364.3676 68085484
                                                                         614.45%
912334 496717
                   -64.4004
                               28
                                        -51.0000
                                                     -364.3676 68095822
                                                                         614.45%
Elapsed time = 1492.98 sec. (933225.40 ticks, tree = 41910.78 MB, solutions = 37)
Nodefile size = 39834.84 MB (34729.80 MB after compression)
913439 497838
                                                     -364.3676 68177102 614.45%
                  -194.3815
                              105
                                        -51.0000
914980 498261
                                                     -364.3676 68196338 614.45%
                  -152.9293
                               86
                                        -51.0000
915804 499766
                  -323.8244
                              224
                                        -51.0000
                                                     -364.3575 68290289
                                                                         614.43%
916628 500079
                  -302.3960
                              211
                                        -51.0000
                                                     -364.3575 68305529
                                                                         614.43%
918039 500368
                  -343.3726
                              228
                                        -51.0000
                                                     -364.3403 68340234
                                                                         614.39%
920007 501929
                                                     -364.3317 68419509
                  -275.8006
                              198
                                        -51.0000
                                                                         614.38%
922741 503623
                                                     -364.3275 68467641
                  -362.6283
                              406
                                        -51.0000
                                                                         614.37%
925606 505643
                  -142.1086
                               79
                                        -51.0000
                                                     -364.3179 68521503
                                                                         614.35%
928546 508163
                  -217.8474
                              137
                                        -51.0000
                                                     -364.3103 68580599
                                                                         614.33%
930886 509848
                                        -51.0000
                                                     -364.2995 68622180
                  -158.5826
                               87
                                                                         614.31%
Elapsed time = 1554.53 sec. (971382.80 ticks, tree = 43251.15 MB, solutions = 37)
Nodefile size = 41149.86 MB (35884.09 MB after compression)
932899 511986
                  -119.3072
                               74
                                        -51.0000
                                                     -364.2902 68685278 614.29%
934637 512936
                  -269.4526
                              187
                                        -51.0000
                                                     -364.2902 68703163
                                                                         614.29%
936749 513505
                  -198.9682
                              162
                                        -51.0000
                                                     -364.2805 68733415
                                                                        614.28%
939019 516384
                  -100.4004
                                        -51.0000
                                                     -364.2805 68830529
                               61
                                                                         614.28%
940965 516910
                                                     -364.2729 68840204
                  -213.4897
                              124
                                        -51.0000
                                                                         614.26%
943366 518019
                  -329.1310
                              247
                                        -51.0000
                                                     -364.2674 68885751
                                                                         614.25%
946119 520442
                  -350.7558
                              252
                                        -51.0000
                                                     -364.2625 68944343
                                                                         614.24%
949262 523916
                  -170.8749
                               94
                                        -51.0000
                                                     -364.2478 69045300
                                                                         614.21%
951577 525662
                  -284.4097
                              170
                                        -51.0000
                                                     -364.2457 69087488
                                                                         614.21%
953822 526036
                  -343.7839
                              272
                                        -51.0000
                                                     -364.2457 69097886
                                                                         614.21%
Elapsed time = 1618.93 sec. (1009540.36 ticks, tree = 44976.81 MB, solutions = 37)
Nodefile size = 42900.58 MB (37403.42 MB after compression)
956067 528253
                  -114.9327
                                       -51.0000
                                                     -364.2457 69141165 614.21%
                               57
958128 529673
                  -203.9004
                              114
                                       -51.0000
                                                     -364.2349 69171360
                                                                         614.19%
960075 531911
                  -80.4004
                                       -51.0000
                                                     -364.2178 69250399
                               39
                                                                         614.15%
961383 532901
                              122
                                                     -364.2178 69269827
                  -192.4865
                                       -51,0000
                                                                         614.15%
```

963351 534290	-331.6833	237	-51.0000	-364.2171 69334703 614.15%
964998 535026	-292.4749	209	-51.0000	-364.2171 69368474 614.15%
966596 537588	-233.1557	129	-51.0000	-364.2171 69455104 614.15%
968783 537908	infeasible		-51.0000	-364.1968 69462106 614.11%
970664 538749	-158.7677	91	-51.0000	-364.1944 69525096 614.11%
971877 540717	-303.3489	187	-51.0000	-364.1830 69565557 614.08%
Elapsed time = 3	1681.97 sec. (1	04770	5.63 ticks, tree	= 46825.36 MB, solutions = 37)
Nodefile size =	44749.88 MB (3	9030.	34 MB after comp	ression)
972591 541449	-360.6409	389	-51.0000	-364.1830 69614316 614.08%
973284 542393	-346.1220	219	-51.0000	-364.1810 69668081 614.08%
974504 543255	-356.6271	308	-51.0000	-364.1748 69742147 614.07%
975615 544122	-82.3339	49	-51.0000	-364.1721 69809177 614.06%
976405 544162	-359.4143	328	-51.0000	-364.1721 69815975 614.06%
978363 545748	-101.4004	57	-51.0000	-364.1668 69906213 614.05%
979846 546197	-351.0579	406	-51.0000	-364.1654 69950306 614.05%
981386 547870	-81.4004	39	-51.0000	-364.1654 69980541 614.05%
982550 549015	-333.7721	202	-51.0000	-364.1654 70056096 614.05%
983567 549656	-147.8308	79	-51.0000	-364.1654 70073713 614.05%
Elapsed time = 3	1742.23 sec. (1	08591	2.50 ticks, tree	= 47716.70 MB, solutions = 37)
Nodefile size =	45612.43 MB (3	9779.	51 MB after comp	ression)
984554 551413	cutoff		-51.0000	-364.1654 70161318 614.05%
985491 551428	-150.5823	93	-51.0000	-364.1654 70191726 614.05%
986750 552700	-282.6257	188	-51.0000	-364.1467 70255403 614.01%
988694 553598	-362.4581	443	-51.0000	-364.1387 70317096 614.00%
990679 555384	-217.3788	127	-51.0000	-364.1311 70394011 613.98%
992846 556974	-362.6461	391	-51.0000	-364.1311 70465635 613.98%
994875 556704	-249.0947	144	-51.0000	-364.1311 70449904 613.98%
996495 558587	-56.8487	28	-51.0000	-364.1193 70519524 613.96%
998699 558897	-98.4589	53	-51.0000	-364.1120 70551356 613.95%
1000118 561480	-343.5201	231	-51.0000	-364.1120 70621249 613.95%
Elapsed time = 3	1798.66 sec. (1	12408	39.14 ticks, tree	= 48342.35 MB, solutions = 37)
Nodefile size =	46248.91 MB (4	0321.	99 MB after comp	ression)
1002022 563411	-277.8063	195	-51.0000	-364.1120 70676416 613.95%
1003930 564748	-65.4004	19	-51.0000	-364.1120 70710284 613.95%
1006162 565013	-362.5691	336	-51.0000	-364.1120 70739515 613.95%
1008681 566024	-125.8004	73	-51.0000	-364.1120 70757009 613.95%
1010748 569646	-67.4004	33	-51.0000	-364.1120 70829790 613.95%
1012267 569841	-291.9516	204	-51.0000	-364.1120 70837248 613.95%
1013891 572086	-161.2518	85	-51.0000	-364.1120 70909039 613.95%

1015221 573589	-211.6472	122	-51.0000	-364.1120	70967323	613.95%
1016223 573677	-312.2773	198	-51.0000	-364.1120	70974601	613.95%
1018064 575321	-64.4004	27	-51.0000	-364.0706	71125303	613.86%
Elapsed time = 1	1860.88 sec. (11	6226	8.08 ticks, tree	= 49744.02	MB, solut	ions = 37)
Nodefile size =	47631.36 MB (41	523.	58 MB after compr	ession)		
1019166 576465	-115.9403	63	-51.0000	-364.0706	71178541	613.86%
1020846 576679	-64.4004	35	-51.0000	-364.0568	71195308	613.84%
1022213 578055	-173.5622	90	-51.0000	-364.0568	71266779	613.84%
1023857 578647	-65.4004	29	-51.0000	-364.0531	71297045	613.83%
1026303 581678	-234.5717	164	-51.0000	-364.0414	71391239	613.81%
1029153 583567	-158.5802	93	-51.0000	-364.0414	71445861	613.81%
1032346 585534	-348.8949	248	-51.0000	-364.0236	71475979	613.77%
1035328 585926	-347.8431	215	-51.0000	-364.0196	71480905	613.76%
1037744 587920	-211.7419	131	-51.0000	-364.0029	71521216	613.73%
1040441 591033	-303.7881	176	-51.0000	-363.9979	71589175	613.72%
Elapsed time = 1	1926.76 sec. (12	0042	8.91 ticks, tree	= 51781.74	MB, solut	ions = 37)
Nodefile size =	49671.30 MB (43	311.	39 MB after compr	ession)		
1042352 593264	-71.9796	30	-51.0000	-363.9963	71626550	613.72%
1043678 593042	-324.0286	219	-51.0000	-363.9963	71627371	613.72%
1045587 595732	-200.1915	114	-51.0000	-363.9832	71708209	613.69%
1047688 596461	-254.6115	163	-51.0000	-363.9832	71730582	613.69%
1049872 597740	-287.0454	175	-51.0000	-363.9832	71785578	613.69%
1051704 600386	-91.4004	47	-51.0000	-363.9832	71849627	613.69%
1053617 602054	-261.5171	153	-51.0000	-363.9772	71927071	613.68%
1055976 603674	-132.4849	72	-51.0000	-363.9772	71965461	613.68%
1058607 604897	-255.3902	153	-51.0000	-363.9635	72011301	613.65%
1060413 605986	-354.7212	330	-51.0000	-363.9578	72031929	613.64%
Elapsed time = 1	1988.67 sec. (12	3860	9.25 ticks, tree	= 53778.28	MB, solut	ions = 37)
Nodefile size =	51644.80 MB (45	060.	90 MB after compr	ession)		
1061914 607317	cutoff		-51.0000	-363.9507	72074436	613.63%
1063680 609340	-360.3288	326	-51.0000	-363.9390	72148771	613.61%
1065328 610155	-124.4046	63	-51.0000	-363.9390	72161179	613.61%
1066797 611383	-59.0000	29	-51.0000	-363.9390	72237860	613.61%
1068142 612237	-224.3689	137	-51.0000	-363.9354	72271213	613.60%
1070142 614705	-76.4004	67	-51.0000	-363.9267	72406469	613.58%
1071992 614979	-246.9402	155	-51.0000	-363.9267	72398235	613.58%
1073903 617010	-228.2843	137	-51.0000	-363.9267	72494327	613.58%
1075706 617392	-204.5836	114	-51.0000	-363.9267	72507148	613.58%
1077501 619338	-86.0025	40	-51.0000	-363.9267	72547889	613.58%

```
Elapsed time = 2046.66 sec. (1276770.39 ticks, tree = 54677.74 MB, solutions = 37)
Nodefile size = 52565.31 MB (45853.57 MB after compression)
1079161 620410
                   -209.3248
                                        -51.0000
                                                     -363.9135 72608861 613.56%
                               118
1081649 622851
                   -300.1106
                                        -51.0000
                                                     -363.8983 72686256 613.53%
                               181
1083926 623234
                               202
                                        -51.0000
                   -323.1341
                                                     -363.8983 72691650 613.53%
1086076 625246
                  -193.9602
                               117
                                        -51.0000
                                                     -363.8939 72732098 613.52%
1088179 627756
                  -283.5262
                               204
                                        -51.0000
                                                     -363.8939 72790211 613.52%
                                                     -363.8939 72814198 613.52%
1091190 628092
                  -287.6054
                               202
                                        -51.0000
1093431 629524
                   -254.8223
                               146
                                        -51.0000
                                                     -363.8939 72854966 613.52%
1095986 632197
                   -346.0530
                               225
                                        -51.0000
                                                     -363.8939 72931006 613.52%
1098500 634277
                                        -51.0000
                                                     -363.8939 72978948 613.52%
                   -179.1473
                               104
1100539 636794
                   -187.8855
                                        -51.0000
                                                     -363.8939 73044618 613.52%
                               109
Elapsed time = 2112.64 sec. (1314938.67 ticks, tree = 56546.65 MB, solutions = 37)
Nodefile size = 54466.62 MB (47506.30 MB after compression)
                   -312.4463
1103600 637668
                               201
                                        -51.0000
                                                     -363.8939 73072583 613.52%
1106082 638900
                                        -51.0000
                   -267.2381
                               173
                                                     -363.8939 73105694 613.52%
1108007 641241
                  -209.4077
                              120
                                        -51.0000
                                                     -363.8939 73190173 613.52%
1109950 644769
                   -99.5139
                                        -51.0000
                                                     -363.8939 73272081 613.52%
                               51
1111945 645280
                   -92.0000
                               48
                                        -51.0000
                                                     -363.8939 73287605 613.52%
1113936 646411
                   -228.3004
                                        -51.0000
                                                     -363.8939 73319493 613.52%
                               131
1116470 648988
                                        -51.0000
                                                     -363.8939 73413311 613.52%
                  -229.0410
                               145
1119248 649821
                  -191.2266
                                        -51.0000
                                                     -363.8939 73426213 613.52%
                              109
1121744 651852
                                                     -363.8939 73474305 613.52%
                   -229.0925
                               141
                                        -51.0000
                                                     -363.8939 73494935 613.52%
1124550 652993
                   -117.5139
                                51
                                        -51.0000
Elapsed time = 2177.62 sec. (1353097.69 ticks, tree = 58255.81 MB, solutions = 37)
Nodefile size = 56118.36 MB (48944.37 MB after compression)
1127139 655456
                    -90.7754
                               40
                                        -51.0000
                                                     -363.8939 73547001 613.52%
1130118 657939
                                                     -363.8281 73617943 613.39%
                   -351.8666
                               276
                                        -51.0000
1132460 659122
                   -340.0214
                               322
                                        -51.0000
                                                     -363.8281 73638023 613.39%
1135268 661999
                   -350.3458
                                        -51.0000
                                                     -363.8281 73703788 613.39%
                               253
1138155 663270
                                                     -363.7914 73727031 613.32%
                   -349.7733
                               221
                                        -51.0000
1141315 666997
                   -109.6681
                                        -51.0000
                                                     -363.7801 73803719 613.29%
                               61
                               197
1143035 667300
                   -319.7683
                                        -51.0000
                                                     -363.7685 73809554 613.27%
1144567 670776
                   -253.0387
                               158
                                        -51.0000
                                                     -363.7537 73913216 613.24%
1146521 670545
                   -259.3532
                               152
                                        -51.0000
                                                     -363.7537 73901076 613.24%
1149449 672203
                   -348.4441
                               219
                                        -51.0000
                                                     -363.7500 73968135 613.24%
Elapsed time = 2242.11 sec. (1391262.97 ticks, tree = 60633.18 MB, solutions = 37)
Nodefile size = 58549.92 MB (51084.18 MB after compression)
1152049 673941
                   -272.6028
                                        -51.0000
                                                     -363.7500 74029925 613.24%
                               196
```

```
1154335 675960
                  -232.3749
                               144
                                        -51.0000
                                                    -363.7346 74096293 613.21%
1156256 677959
                  -342.2852
                              228
                                        -51.0000
                                                    -363.7346 74162994 613.21%
1158262 679301
                  -283.8515
                                        -51.0000
                                                    -363.7346 74213670 613.21%
                               185
1160659 681152
                  -329.8099
                                        -51.0000
                                                     -363.7346 74291318 613.21%
                               233
1163080 682052
                                        -51.0000
                                                     -363.7346 74302383 613.21%
                  -356.6172
                               229
1164962 684898
                  -239.2677
                               149
                                        -51.0000
                                                     -363.7346 74363108 613.21%
1166859 686253
                  -215.5065
                              147
                                        -51.0000
                                                    -363.7035 74429048 613.14%
1169268 687434
                  -137.5978
                               79
                                        -51.0000
                                                    -363.7026 74462687 613.14%
1171545 689622
                   -209.2428
                               119
                                        -51.0000
                                                     -363.7026 74521715 613.14%
Elapsed time = 2302.32 sec. (1429431.71 ticks, tree = 61810.58 MB, solutions = 37)
Nodefile size = 59703.04 MB (52075.58 MB after compression)
1173411 692218
                  -356.7395
                                                     -363.7002 74586749 613.14%
                              294
                                        -51.0000
1175378 692552
                  -168.7210
                                        -51.0000
                                                     -363.6861 74594723 613.11%
                               87
1177260 694405
                   -353.1794
                              310
                                        -51.0000
                                                     -363.6861 74666144 613.11%
1178498 695421
                  -323.5001
                              196
                                        -51.0000
                                                    -363.6825 74706969 613.10%
1180148 696748
                                                     -363.6825 74757697 613.10%
                  -157.0337
                               90
                                        -51.0000
1181894 698492
                  -174.7770
                                        -51.0000
                                                    -363.6749 74851125 613.09%
                             102
1183386 700062
                                        -51.0000
                                                    -363.6749 74931587 613.09%
                   -74.6611
                               40
1185302 699922
                   -80.6800
                               35
                                        -51.0000
                                                     -363.6678 74926413 613.07%
1186617 701400
                   -271.7142
                               167
                                        -51.0000
                                                     -363.6671 74988295
                                                                        613.07%
1189228 702436
                                                     -363.6556 75016408 613.05%
                   -317.6486
                               188
                                        -51.0000
Elapsed time = 2360.98 sec. (1467594.59 ticks, tree = 62502.87 MB, solutions = 37)
Nodefile size = 60366.86 MB (52639.96 MB after compression)
                                                     -363.6524 75108073 613.04%
1191792 705430
                   -255.5873
                               151
                                        -51.0000
1194437 706237
                  -124.2892
                               69
                                        -51.0000
                                                     -363.6470 75131286 613.03%
1197089 707759
                  -307.1593
                              218
                                        -51.0000
                                                    -363.6470 75162684 613.03%
1199984 710769
                  -130.2921
                                        -51.0000
                                                    -363.6466 75226744 613.03%
                               67
1202782 713542
                                                    -363.6466 75289008 613.03%
                  infeasible
                                        -51.0000
1205543 714868
                  -250.1788
                               148
                                        -51.0000
                                                     -363.6466 75306792 613.03%
1207640 716798
                  -324.8750
                              197
                                        -51.0000
                                                    -363.6272 75347915 612.99%
1209905 717923
                                                    -363.6272 75381128 612.99%
                  -274.8872
                              173
                                        -51.0000
1211507 720196
                  -128.8731
                               68
                                        -51.0000
                                                     -363.6147 75451092
                                                                        612.97%
1212988 721254
                   -185.9255
                                                     -363.6147 75476208 612.97%
                               105
                                        -51.0000
Elapsed time = 2430.66 sec. (1505753.18 ticks, tree = 65025.03 MB, solutions = 37)
Nodefile size = 62942.95 MB (54909.80 MB after compression)
                                                     -363.6147 75481562 612.97%
1214464 721679
                  -114.8208
                               59
                                        -51.0000
1216487 723625
                  -345.3600
                              243
                                        -51.0000
                                                     -363.6147 75547226 612.97%
1218075 723995
                  -323.9574
                                        -51.0000
                                                    -363.6134 75552962 612.97%
                             195
1219748 725238
                  -302.7574
                                        -51.0000
                                                    -363.6134 75612915 612.97%
                              216
```

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1221521 726612
                  -361.9645
                              476
                                       -51.0000
                                                    -363.5945 75637366 612.93%
1222967 728865
                  -342.9362
                              292
                                       -51.0000
                                                    -363.5945 75726583 612.93%
1224384 730826
                  -247.8571
                                       -51.0000
                                                    -363.5945 75797131 612.93%
                              152
1225757 731044
                  -330.0338
                                       -51.0000
                                                    -363.5945 75791560 612.93%
                              261
1226952 732586
                                                    -363.5845 75882721 612.91%
                  -258.1447
                              163
                                       -51.0000
1228618 732872
                  -321.9352
                              194
                                       -51.0000
                                                    -363.5839 75927746 612.91%
Elapsed time = 2489.07 sec. (1543964.51 ticks, tree = 66176.85 MB, solutions = 37)
Nodefile size = 64093.97 MB (55912.45 MB after compression)
1230703 733149
                  -351.7396
                              436
                                       -51.0000
                                                    -363.5839 75968280 612.91%
1233278 735609
                  -131.9364
                               71
                                       -51.0000
                                                    -363.5839 76043170 612.91%
1234652 737416
                                                    -363.5839 76127813 612.91%
                  -235.5213
                              139
                                       -51.0000
1236454 738419
                                                    -363.5549 76156762 612.85%
                  -181.1871
                             107
                                       -51.0000
1237699 740772
                  -129.0000
                                                    -363.5549 76254593 612.85%
                               66
                                       -51.0000
1239535 740626
                  -147.0000
                               76
                                       -51.0000
                                                    -363.5501 76250246 612.84%
                                       -51.0000
1241284 742271
                  -246.1793
                              138
                                                    -363.5421 76335355 612.83%
1243215 744506
                                                    -363.5421 76435943 612.83%
                  -336.5570
                              217
                                       -51.0000
1245194 745177
                  -297.8112
                                       -51.0000
                                                    -363.5421 76453687 612.83%
                              177
1247711 747555
                  -348.0724
                                       -51.0000
                                                    -363.5421 76533897 612.83%
                              218
Elapsed time = 2544.68 sec. (1582125.76 ticks, tree = 66528.97 MB, solutions = 37)
Nodefile size = 64413.10 MB (56160.38 MB after compression)
1250771 749319
                  -339.8761
                                       -51.0000
                                                    -363.5421 76568677 612.83%
                              240
1253428 749875
                  -124.3338
                                       -51.0000
                                                    -363.5421 76582998 612.83%
                               66
1255484 752046
                                                    -363.5421 76616090 612.83%
                  -313.9867
                              199
                                       -51.0000
1257505 755090
                  -350.9171
                              242
                                       -51.0000
                                                    -363.5421 76681612 612.83%
                                                    -363.5421 76709254 612.83%
1260061 756810
                  -221.2307
                              125
                                       -51.0000
1262802 758964
                  -239.4641
                                       -51.0000
                                                    -363.5421 76823900 612.83%
                              151
1266020 760556
                   -67.0000
                                       -51.0000
                                                    -363.5421 76853753 612.83%
                               27
1268615 762001
                                                    -363.5421 76882255 612.83%
                  -360.4381
                              313
                                       -51.0000
1270717 764173
                  -272.7824
                              204
                                       -51.0000
                                                    -363.5421 76921149 612.83%
                                                    -363.5421 76934663 612.83%
1273013 764966
                  -349.1395
                              221
                                        -51.0000
Elapsed time = 2612.51 sec. (1620287.49 ticks, tree = 68888.14 MB, solutions = 37)
Nodefile size = 66752.03 MB (58218.78 MB after compression)
1274910 766152
                  -207.9977
                                                    -363.5421 76966938 612.83%
                              119
                                       -51.0000
1276895 767806
                                                    -363.5421 77002202 612.83%
                  -303.6618
                              187
                                       -51.0000
                                                    -363.5421 77074936 612.83%
1279341 770025
                   -65.0000
                               32
                                       -51.0000
1281908 771422
                  -347.6908
                              259
                                       -51.0000
                                                    -363.5421 77108674 612.83%
1284101 773070
                  -177.3216
                               96
                                       -51.0000
                                                    -363.5421 77190936 612.83%
1286070 776897
                  -256.3404
                                       -51.0000
                                                    -363.5421 77312454 612.83%
                              143
1287980 777168
                  -310.7619
                                       -51.0000
                                                    -363.5421 77318855 612.83%
                              207
```

1290484 778922	-188.5016	112	-51.0000	-363.5421	77387526	612.83%
1293069 781489	-349.1820	220	-51.0000	-363.5421	77460748	612.83%
1296398 783285	-98.9651	55	-51.0000	-363.4446		612.64%
Elapsed time = 26	369.17 sec. (10	65844	2.71 ticks, tree	= 70071.06	MB, solut	ions = 37)
Nodefile size = 6			-		·	·
1299543 786097	-336.3001	223	-51.0000	-363.4300	77552721	612.61%
1303025 787564	-273.5397	156	-51.0000	-363.4226	77573312	612.59%
1306367 789080	-165.2899	99	-51.0000	-363.4165	77602295	612.58%
1309683 790823	-118.8209	58	-51.0000	-363.4165	77631755	612.58%
1312927 792605	-219.8976	134	-51.0000	-363.4015	77657849	612.55%
1315995 795803	-116.3636	55	-51.0000	-363.3930	77719274	612.54%
1318964 798022	-189.8624	104	-51.0000	-363.3865	77756398	612.52%
1322287 801721	-105.9631	46	-51.0000	-363.3788	77824176	612.51%
1325904 803857	-200.5226	112	-51.0000	-363.3710	77862574	612.49%
1328164 806865	-213.8837	137	-51.0000	-363.3676	77911316	612.49%
Elapsed time = 27	740.62 sec. (10	69660	1.21 ticks, tree	= 73281.65	MB, solut	ions = 37)
Nodefile size = 7	71175.40 MB (6	2084.	28 MB after comp	ression)		
1330725 808432	-253.4076	158	-51.0000	-363.3637	77946512	612.48%
1333424 811368	-83.0000	38	-51.0000	-363.3566	77996494	612.46%
1335998 812588	-207.2111	132	-51.0000	-363.3501	78032150	612.45%
1338136 815838	-262.3210	156	-51.0000	-363.3501	78120654	612.45%
1340355 816178	-79.0000	32	-51.0000	-363.3501	78126079	612.45%
1342750 818717	-179.9456	121	-51.0000	-363.3501	78197929	612.45%
1344977 819655	-64.0000	23	-51.0000	-363.3495	78246621	612.45%
1347424 820968	-220.0034	147	-51.0000	-363.3341	78263692	612.42%
1350340 824500	-337.0347	270	-51.0000	-363.3323	78361658	612.42%
1353068 826086	-218.3378	126	-51.0000	-363.3240	78392139	612.40%
Elapsed time = 28	308.76 sec. (1°	73476	9.59 ticks, tree	= 75570.94	MB, solut	ions = 37)
Nodefile size = 7	73464.03 MB (64	4075.	14 MB after comp	ression)		
1354929 828737	-249.5033	167	-51.0000	-363.3240	78453276	612.40%
1357188 828878	-58.0000	31	-51.0000	-363.3240	78474265	612.40%
1360989 829429	-120.5256	54	-51.0000	-363.3071	78489831	612.37%
1363767 832535	-233.8816	139	-51.0000	-363.3009	78554923	612.35%
1366058 836220	-353.4513	283	-51.0000	-363.3009	78615429	612.35%
1368168 836811	-168.0117	96	-51.0000	-363.2916	78636188	612.34%
1370621 838448	-150.5858	71	-51.0000	-363.2852	78668575	612.32%
1373310 840832	-192.6639	118	-51.0000	-363.2852	78723896	612.32%
1376021 842744	-116.0000	61	-51.0000	-363.2846	78755757	612.32%
1378544 843891	-303.4139	177	-51.0000	-363.2846	78798222	612.32%

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Elapsed time = 2876.38 sec. (1772947.12 ticks, tree = 78009.93 MB, solutions = 37)
Nodefile size = 75864.31 MB (66187.42 MB after compression)
1380852 844714
                   -104.8889
                               54
                                        -51.0000
                                                     -363.2846 78805091 612.32%
1382951 849567
                   -266.2673
                                        -51.0000
                                                     -363.2846 78916286 612.32%
                               184
                  -354.9558
                                        -51.0000
                                                     -363.2591 78921259 612.27%
1385337 849918
                               288
1387121 850980
                  -220.9833
                               127
                                        -51.0000
                                                     -363.2554 78943781 612.27%
1388896 853784
                  -311.5685
                               191
                                        -51.0000
                                                     -363.2506 79021815 612.26%
1390673 854058
                  -319.6543
                                        -51.0000
                                                     -363.2506 79027093 612.26%
                               213
1392561 856415
                   -215.9617
                               135
                                        -51.0000
                                                     -363.2506 79109073 612.26%
1394362 856773
                   -336.7539
                               231
                                        -51.0000
                                                     -363.2487 79114447 612.25%
1396269 858330
                               196
                                                     -363.2487 79170234 612.25%
                   -314.7448
                                        -51.0000
1398329 859496
                                        -51.0000
                                                     -363.2457 79188574 612.25%
                   -278.4522
                               165
Elapsed time = 2939.17 sec. (1811109.90 ticks, tree = 80161.14 MB, solutions = 37)
Nodefile size = 77996.90 MB (68060.51 MB after compression)
1400362 861629
                    -94.8928
                               60
                                        -51.0000
                                                     -363.2457 79278236 612.25%
1402182 863414
                                        -51.0000
                   -210.8249
                               123
                                                     -363.2457 79322997 612.25%
1403647 864988
                  -356.3679
                               277
                                        -51.0000
                                                     -363.2134 79365317 612.18%
1405435 865338
                  -146.7865
                               78
                                        -51.0000
                                                     -363.2088 79370410 612.17%
1406589 867010
                   -359.7785
                               358
                                        -51.0000
                                                     -363.2088 79449597 612.17%
1407357 867801
                   -175.8509
                               103
                                        -51.0000
                                                     -363.2088 79473735 612.17%
1408480 869141
                                        -51.0000
                                                     -363.2060 79559155 612.17%
                   -357.7632
                               286
1409072 869005
                                        -51.0000
                                                     -363.2030 79576725
                  -292.4575
                               185
                                                                         612.16%
1409931 870613
                                                     -363.2030 79678668 612.16%
                   -317.9388
                               207
                                        -51.0000
1410846 871221
                   -300.5855
                               191
                                        -51.0000
                                                     -363.2030 79725732 612.16%
Elapsed time = 3001.29 sec. (1849268.80 ticks, tree = 81426.69 MB, solutions = 37)
Nodefile size = 79340.13 MB (69235.09 MB after compression)
1412565 871839
                   -198.5468
                               146
                                        -51.0000
                                                     -363.1993 79794879 612.16%
1414222 872610
                  -355.1605
                               245
                                        -51.0000
                                                     -363.1976 79824561 612.15%
1416451 873746
                   -136.8493
                               75
                                        -51.0000
                                                     -363.1940 79887929 612.15%
1418802 875876
                                        -51.0000
                                                     -363.1940 79985747 612.15%
                   -262.7594
                               150
1420667 877986
                                                     -363.1940 80044684 612.15%
                   -120.8353
                               67
                                        -51.0000
1422897 879153
                   -68.0000
                               29
                                        -51.0000
                                                     -363.1912 80105755 612.14%
1424675 880527
                   -102.5792
                                        -51.0000
                                                     -363.1912 80124655 612.14%
                               49
1426442 881127
                   -214.1609
                               129
                                        -51.0000
                                                     -363.1912 80157146 612.14%
1428467 883401
                   -182.3962
                               109
                                        -51.0000
                                                     -363.1707 80225126 612.10%
1430584 885240
                   -157.4481
                               95
                                        -51.0000
                                                     -363.1701 80286129 612.10%
Elapsed time = 3060.58 sec. (1887439.56 ticks, tree = 82485.78 MB, solutions = 37)
Nodefile size = 80396.88 MB (70146.52 MB after compression)
1431870 886774
                   -284.1700
                                        -51.0000
                                                     -363.1701 80338190 612.10%
                               176
```

```
1433655 887329
                  -192.0080
                               106
                                        -51.0000
                                                    -363.1701 80363893 612.10%
1435683 887996
                  -221.9601
                              130
                                        -51.0000
                                                    -363.1701 80378007
                                                                        612.10%
1437806 890614
                  -173.4306
                                        -51.0000
                                                    -363.1701 80521614 612.10%
                               90
1439772 890705
                  -346.6358
                                        -51.0000
                                                     -363.1634 80541956 612.09%
                              222
1441413 894088
                                        -51.0000
                                                    -363.1634 80639579 612.09%
                  -326.9882
                              225
1443300 893400
                   -70.0000
                               28
                                        -51.0000
                                                     -363.1542 80610357 612.07%
1445035 896243
                  -208.7591
                              119
                                        -51.0000
                                                    -363.1453 80712144 612.05%
1446281 897127
                   -197.6167
                                        -51.0000
                                                    -363.1419 80754887 612.04%
                               112
1447762 898657
                    -91.8217
                                40
                                        -51.0000
                                                     -363.1419 80807489 612.04%
Elapsed time = 3123.21 sec. (1925598.32 ticks, tree = 83544.11 MB, solutions = 37)
Nodefile size = 81452.99 MB (71050.24 MB after compression)
1449076 899736
                   -322.1691
                                                     -363.1419 80869707 612.04%
                              203
                                        -51.0000
1450689 899823
                  -232.5075
                                                     -363.1318 80862276 612.02%
                               136
                                        -51.0000
1452809 901413
                   -225.7858
                               139
                                        -51.0000
                                                     -363.1314 80941867 612.02%
                                                    -363.1282 81042552 612.02%
1454893 903274
                  -358.8973
                              388
                                        -51.0000
1457193 905392
                  -173.3702
                               95
                                        -51.0000
                                                     -363.1282 81100657 612.02%
1459630 905749
                  -248.7621
                                                     -363.1229 81106133 612.01%
                              160
                                        -51.0000
1462412 908405
                  -327.4000
                                        -51.0000
                                                    -363.1193 81191230 612.00%
                              317
1465284 910018
                   -269.0734
                               163
                                        -51.0000
                                                     -363.1193 81234773 612.00%
1467995 911192
                   -127.3125
                               68
                                        -51.0000
                                                     -363.1193 81272725 612.00%
1470171 915051
                                                     -363.1193 81338792 612.00%
                   -214.2308
                               131
                                        -51.0000
Elapsed time = 3185.87 sec. (1963768.00 ticks, tree = 85097.25 MB, solutions = 37)
Nodefile size = 82996.73 MB (72399.07 MB after compression)
                                                     -363.0963 81359705 611.95%
1472123 915840
                    -61.2873
                               25
                                        -51.0000
1474944 917352
                  -150.6935
                              103
                                        -51.0000
                                                     -363.0963 81406102 611.95%
1477413 918699
                  -206.5598
                                        -51.0000
                                                    -363.0963 81437361 611.95%
                              113
1480258 921424
                  -164.2992
                                        -51.0000
                                                    -363.0819 81482776 611.93%
                              111
1482580 921768
                                        -51.0000
                                                    -363.0819 81488923 611.93%
                  -268.5418
                               165
1485060 924969
                   -143.3574
                               86
                                        -51.0000
                                                     -363.0736 81569087 611.91%
1487196 925334
                                                     -363.0736 81574482 611.91%
                  -228.5638
                               136
                                        -51.0000
1488705 927554
                                                    -363.0736 81634624 611.91%
                  -163.6258
                              104
                                        -51.0000
1490312 928638
                   -309.5214
                               190
                                        -51.0000
                                                     -363.0642 81673852 611.89%
1491785 929380
                   -358.3981
                                                     -363.0642 81684293 611.89%
                               270
                                        -51.0000
Elapsed time = 3251.39 sec. (2001939.32 ticks, tree = 87079.65 MB, solutions = 37)
Nodefile size = 84914.94 MB (74090.46 MB after compression)
1493123 932100
                  -361.1607
                                        -51.0000
                                                     -363.0642 81782395 611.89%
                              431
1494409 933384
                  -226.9344
                              133
                                        -51.0000
                                                     -363.0459 81815947 611.85%
1495695 934332
                  -340.4590
                              462
                                        -51.0000
                                                   -363.0412 81876672 611.85%
1496875 935790
                                                    -363.0360 81930955 611.84%
                   -83.4127
                               43
                                        -51.0000
```

```
1498611 936080
                  -340.2493
                              219
                                       -51.0000
                                                    -363.0359 81938184 611.84%
1500352 938166
                  -344.8650
                              243
                                       -51.0000
                                                    -363.0359 82058846 611.84%
1501886 939423
                  -214.2697
                                       -51.0000
                                                    -363.0359 82133186 611.84%
                              147
1504021 940301
                  -358.9608
                                       -51.0000
                                                    -363.0299 82162519 611.82%
                              298
1505915 940547
                                                    -363.0219 82169070 611.81%
                  -111.5071
                               60
                                       -51.0000
1508308 942596
                  -290.0645
                              164
                                       -51.0000
                                                    -363.0181 82259386 611.80%
Elapsed time = 3310.11 sec. (2040140.88 ticks, tree = 87780.04 MB, solutions = 37)
Nodefile size = 85628.88 MB (74705.56 MB after compression)
1509877 943462
                  -362.1250
                              345
                                       -51.0000
                                                    -363.0181 82279281 611.80%
1511487 944392
                  -250.2819
                              153
                                       -51.0000
                                                    -363.0181 82311234 611.80%
1513253 946218
                                                    -363.0181 82347204 611.80%
                  -108.1399
                               52
                                       -51.0000
1515387 948834
                                                    -363.0181 82452582 611.80%
                  -189.7285
                              105
                                       -51.0000
                   -75.4540
                                                    -363.0181 82477198 611.80%
1517182 949556
                               32
                                       -51.0000
1519399 949444
                 infeasible
                                       -51.0000
                                                    -363.0181 82514269 611.80%
1521136 952636
                  -323.2530
                              196
                                       -51.0000
                                                    -363.0181 82576083 611.80%
1522540 953923
                                                    -363.0181 82642685 611.80%
                  -233.5832
                              139
                                       -51.0000
1524673 955141
                  -324.2844
                                       -51.0000
                                                    -363.0181 82669446 611.80%
                              195
1527134 957400
                  -270.0783
                                       -51.0000
                                                    -363.0181 82761101 611.80%
                              153
Elapsed time = 3375.30 sec. (2078300.10 ticks, tree = 89832.75 MB, solutions = 37)
Nodefile size = 87735.09 MB (76556.10 MB after compression)
1529246 958614
                                       -51.0000
                                                    -362.9817 82793638 611.73%
                  -201.0558
                              130
1531688 958996
                  -161.7118
                                       -51.0000
                                                    -362.9817 82798680 611.73%
                              88
                                                    -362.9680 82872188 611.70%
1533866 961145
                  -311.7875
                              206
                                       -51.0000
1536179 963907
                  -186.8495
                              106
                                       -51.0000
                                                    -362.9665 82919347 611.70%
                                                    -362.9639 82919358 611.69%
1538696 963676
                  -352.0906
                              262
                                       -51.0000
1541291 967962
                  -352.4511
                              278
                                       -51.0000
                                                    -362.9596 83060386 611.69%
1543733 968242
                  -357.3868
                                       -51.0000
                                                    -362.9596 83066483 611.69%
                              235
1546056 969753
                  -131.0000
                              70
                                       -51.0000
                                                    -362.9596 83094379 611.69%
1548313 973663
                  -358.5955
                              292
                                       -51.0000
                                                    -362.9596 83188282 611.69%
                                                    -362.9596 83193612 611.69%
1550146 974076
                  -337.6329
                              235
                                       -51.0000
Elapsed time = 3438.78 sec. (2116458.32 ticks, tree = 91621.92 MB, solutions = 37)
Nodefile size = 89472.03 MB (78071.33 MB after compression)
1552066 975198
                  -257.4841
                                                    -362.9596 83217109 611.69%
                              153
                                       -51.0000
1554054 978192
                  -362.7689
                              413
                                       -51.0000
                                                    -362.9596 83329259 611.69%
1555755 978851
                  -143.0000
                               75
                                       -51.0000
                                                    -362.9596 83355737 611.69%
1557601 980081
                  -111.0000
                               62
                                       -51.0000
                                                    -362.9596 83402580 611.69%
1559461 980883
                   -65.5000
                               31
                                       -51.0000
                                                    -362.9596 83416493 611.69%
1561060 981959
                   -95.2712
                                       -51.0000
                                                    -362.9596 83457941 611.69%
                               54
1563252 984242
                  -362.0169
                                                    -362.9596 83525920 611.69%
                              413
                                       -51.0000
```

1565359 98	5051 -35	7.4587 294	-51.0000 -	362.9233	83550747	611.61%
1567576 98	6032 -14	9.0000 85	-51.0000 -	362.9233	83574660	611.61%
1569513 98	7717 -27	9.5274 163	-51.0000 -	362.9233	83634697	611.61%
Elapsed ti	me = 3504.02	sec. (2154615.60	ticks, tree =	93479.99	MB, soluti	ons = 37)
Nodefile s	ize = 91371.	26 MB (79754.57 MB	after compres	sion)		
1571974 99	0722 -36	2.4365 380	-51.0000 -	362.9233	83694670	611.61%
1573897 99	2646 -6	8.4032 28	-51.0000 -	362.9114	83746398	611.59%
1575392 99	2729 -33	0.2044 206	-51.0000 -	362.9114	83779146	611.59%
1577047 99	3978 -35	8.7650 359	-51.0000 -	362.9057	83809952	611.58%
1578890 99	5730 -12	7.0000 61	-51.0000 -	362.8989	83877449	611.57%
1580686 99	8467 -28	7.4760 169	-51.0000 -	362.8989	83985755	611.57%
1582486 99	8774 -18	4.8990 96	-51.0000 -	362.8989	83990762	611.57%
1584991 99	8842 -35	6.8110 390	-51.0000 -	362.8859	84005528	611.54%
1587493 99	9579 -7	7.0000 35	-51.0000 -	362.8859	84044828	611.54%
1589567 10	02790 -1	31.3414 85	-51.0000	-362.8732	84134590	611.52%
Elapsed ti	me = 3565.26	sec. (2192780.39	ticks, tree =	94791.64	MB, soluti	ons = 37)
Nodefile s	ize = 92672.	34 MB (80888.26 MB	after compres	sion)		
1592670 10	04787 -2	97.9113 190	-51.0000	-362.8725	84180248	611.51%
1595731 10	05466 -	95.7042 50	-51.0000	-362.8672	84210720	611.50%
1599386 10	06137 -2	55.3546 166	-51.0000	-362.8664	84220217	611.50%
1602374 10	11809 -2	58.4069 167	-51.0000	-362.8652	84331862	611.50%
1604997 10	10524 -3	60.4317 388	-51.0000	-362.8581	84307783	611.49%
1607859 10	15041 -2	90.6650 167	-51.0000	-362.8530	84391761	611.48%
1610787 10	17262 -3	48.8495 243	-51.0000	-362.8508	84436563	611.47%
1613632 10	21191 -1	35.1203 72	-51.0000	-362.8508	84518537	611.47%
1615516 10	20433 -2	16.2144 140	-51.0000	-362.8410	84504224	611.45%
1617251 10	22386 -2	70.4581 162	-51.0000	-362.8333	84547261	611.44%
Elapsed ti	me = 3635.70	sec. (2230941.04	ticks, tree =	97508.37	MB, soluti	ons = 37)
Nodefile s	ize = 95355.	95 MB (83241.89 MB	after compres	sion)		
1619480 10	26326 -1	06.0000 53	-51.0000	-362.8282	84646400	611.43%
1621653 10	26348 -3	55.3272 241	-51.0000	-362.8246	84638448	611.42%
1624106 10	28420 -1	65.5907 118	-51.0000	-362.8246	84737509	611.42%
1626046 10	31119 -1	97.2253 111	-51.0000	-362.8246	84803674	611.42%
1628354 10	31483 -2	72.8441 187	-51.0000	-362.8182	84808486	611.41%
1630900 10	33785 -1	36.0000 74	-51.0000	-362.8149	84879529	611.40%
1633280 10	35225 -1	78.0256 106	-51.0000	-362.8095	84897759	611.39%
1635519 10	36730 -3	52.3538 246	-51.0000	-362.8073	84951001	611.39%
1637650 10	37407 -1	27.6583 75	-51.0000	-362.8062	84968280	611.38%
1640581 10	37971 -3	53.0674 237	-51.0000	-362.8062	84995175	611.38%

```
Elapsed time = 3699.91 sec. (2269105.18 ticks, tree = 99299.35 MB, solutions = 37)
Nodefile size = 97165.67 MB (84826.35 MB after compression)
1643113 1042917
                   -123.0000
                                 65
                                         -51.0000
                                                      -362.7964 85104583 611.37%
1645682 1045072
                    -98.0000
                                         -51.0000
                                                      -362.7915 85155504 611.36%
                                 43
                   -247.7274
1647968 1044321
                                144
                                         -51.0000
                                                      -362.7915 85146785 611.36%
1649894 1048126
                   -262.8989
                                152
                                         -51.0000
                                                      -362.7845 85227817 611.34%
1651814 1049151
                   -186.8173
                                101
                                        -51.0000
                                                      -362.7845 85253195
                                                                          611.34%
1653327 1049473
                   -356.1169
                                318
                                         -51.0000
                                                      -362.7795 85258164
                                                                         611.33%
1655002 1053056
                    -355.6073
                                278
                                         -51.0000
                                                      -362.7795 85359222
                                                                          611.33%
                                         -51.0000
                                                                         611.33%
1656520 1053373
                   -135.0000
                                 67
                                                      -362.7795 85407938
                                         -51.0000
1658361 1054656
                                                      -362.7795 85449771 611.33%
                    -101.0000
                                 57
1659888 1055695
                                         -51.0000
                                                      -362.7795 85516761 611.33%
                    -256.1699
                                146
Elapsed time = 3765.79 sec. (2307266.26 ticks, tree = 101441.55 MB, solutions = 37)
Nodefile size = 99318.60 MB (86720.36 MB after compression)
1661149 1056024
                    -127.0000
                                 72
                                         -51.0000
                                                      -362.7795 85521668 611.33%
                                265
1662587 1057258
                    -353.0349
                                         -51.0000
                                                      -362.7795 85568921 611.33%
1663677 1059201
                    -312.0521
                                192
                                         -51.0000
                                                      -362.7795 85649252 611.33%
1665018 1060718
                                253
                                        -51.0000
                                                      -362.7795 85699888 611.33%
                   -346.8945
1667093 1061145
                    -233.1731
                                124
                                         -51.0000
                                                      -362.7795 85762078 611.33%
1668662 1063518
                   -185.8541
                                 99
                                         -51.0000
                                                      -362.7540 85814491
                                                                          611.28%
1670566 1063921
                    -292.5807
                                         -51.0000
                                                      -362.7471 85869834
                                179
                                                                          611.27%
1673003 1064269
                    -93.0000
                                 51
                                         -51.0000
                                                      -362.7471 85876458
                                                                          611.27%
1674618 1066561
                                                      -362.7460 85962658 611.27%
                    -318.0390
                                230
                                         -51.0000
                                                      -362.7419 85956170 611.26%
1676422 1066460
                    -355.5526
                                277
                                         -51.0000
Elapsed time = 3822.33 sec. (2345444.75 ticks, tree = 102413.17 MB, solutions = 37)
Nodefile size = 100313.89 MB (87590.71 MB after compression)
1678428 1069357
                    -120.0000
                                         -51.0000
                                                      -362.7356 86082885 611.25%
1680900 1070444
                                 79
                   -127.0000
                                         -51.0000
                                                      -362.7356 86127269 611.25%
1684018 1072004
                    -195.2310
                                115
                                         -51.0000
                                                      -362.7356 86162816 611.25%
1686950 1074672
                                         -51.0000
                                                      -362.7213 86217540
                   -198.9341
                                121
                                                                          611.22%
1688817 1075569
                                                      -362.7205 86234976 611.22%
                   -344.0144
                                261
                                         -51.0000
1690232 1077618
                    -349.8671
                                358
                                         -51.0000
                                                      -362.7205 86267376
                                                                          611.22%
                   -230.6096
                                        -51.0000
1692562 1078890
                                                      -362.7201 86305304
                                136
                                                                         611.22%
                    -93.0000
1694242 1081904
                                 43
                                         -51.0000
                                                      -362.7066 86455402 611.19%
1695461 1080671
                    -211.5977
                                136
                                         -51.0000
                                                      -362.7044 86405574
                                                                          611.19%
1697499 1082638
                    -347.2280
                                227
                                         -51.0000
                                                      -362.7018 86477065 611.18%
Elapsed time = 3887.72 sec. (2383611.26 ticks, tree = 103831.56 MB, solutions = 37)
Nodefile size = 101675.30 MB (88760.66 MB after compression)
1699409 1083919
                   -347.0445
                                252
                                         -51.0000
                                                      -362.7018 86523820 611.18%
```

```
1701903 1087178
                   -164.0000
                                86
                                        -51.0000
                                                     -362.6903 86637076 611.16%
1705244 1087473
                   -111.0000
                                54
                                        -51.0000
                                                     -362.6903 86641463 611.16%
1708528 1091154
                   -351.8627
                               327
                                        -51.0000
                                                     -362.6816 86710675 611.14%
1711345 1091455
                   -305.5254
                                        -51.0000
                                                     -362.6810 86716115 611.14%
                               226
1714058 1093531
                   -125.0000
                                        -51.0000
                                                     -362.6810 86742733 611.14%
                                68
1716044 1093882
                   -270.4370
                               177
                                        -51.0000
                                                     -362.6810 86747997
                                                                         611.14%
                                                     -362.6732 86820470
1717546 1096977
                   -165.0000
                                85
                                        -51.0000
                                                                         611.12%
                                                     -362.6672 86862102 611.11%
1718830 1098665
                   -355.7772
                               430
                                        -51.0000
1720069 1100901
                   -135.0000
                                80
                                        -51.0000
                                                     -362.6656 86925829
                                                                         611.11%
Elapsed time = 3953.78 sec. (2421784.63 ticks, tree = 106417.14 MB, solutions = 37)
Nodefile size = 104319.82 MB (91096.33 MB after compression)
1721339 1101680
                   -117.0000
                                                     -362.6656 86974958 611.11%
                                56
                                        -51.0000
1722319 1102272
                                                     -362.6596 87030638 611.10%
                   -218.3016
                               136
                                        -51.0000
1723245 1103269
                   -275.9999
                               162
                                        -51.0000
                                                     -362.6596 87056591 611.10%
1724223 1103312
                    -96.0000
                                46
                                        -51.0000
                                                     -362.6596 87073826 611.10%
1725584 1104731
                                                     -362.6596 87136461 611.10%
                   -177.3169
                               117
                                        -51.0000
1726911 1106217
                   -188.3971
                                        -51.0000
                                                     -362.6574 87241554 611.09%
                               143
1728561 1106444
                   -176.0748
                                        -51.0000
                                                     -362.6574 87287791 611.09%
                                89
1730521 1108181
                   -327.5582
                               201
                                        -51.0000
                                                     -362.6574 87316342 611.09%
1732599 1108551
                    -74.0000
                                35
                                        -51.0000
                                                     -362.6574 87322004
                                                                         611.09%
1734632 1110364
                   -337.1043
                               250
                                        -51.0000
                                                     -362.6574 87399542 611.09%
Elapsed time = 4014.37 sec. (2459957.65 ticks, tree = 107224.35 MB, solutions = 37)
Nodefile size = 105067.96 MB (91749.43 MB after compression)
1737166 1112205
                   -193.2310
                                                     -362.6459 87446556 611.07%
                               114
                                        -51.0000
                                                     -362.6459 87486378 611.07%
1739419 1112996
                   -173.7686
                                92
                                        -51.0000
1741249 1114769
                   -347.1913
                               214
                                        -51.0000
                                                     -362.6401 87522106 611.06%
1743358 1115064
                   -192.2962
                               107
                                        -51.0000
                                                     -362.6384 87515063 611.06%
1744968 1118074
                                                     -362.6359 87592968 611.05%
                   -328.4236
                               210
                                        -51.0000
1746865 1119076
                   -191.1902
                               112
                                        -51.0000
                                                     -362.6287 87643898 611.04%
                    -81.0000
                                37
                                                     -362.6225 87699408
1748365 1121241
                                        -51.0000
                                                                         611.02%
1750085 1121481
                                                     -362.6225 87705667
                   -324.0813
                               201
                                        -51.0000
                                                                         611.02%
1752508 1124145
                     -60.0000
                                19
                                        -51.0000
                                                     -362.6205 87805130
                                                                         611.02%
1755390 1123880
                                        -51.0000
                                                     -362.6205 87785448 611.02%
                  infeasible
Elapsed time = 4081.48 sec. (2498117.32 ticks, tree = 109186.03 MB, solutions = 37)
Nodefile size = 107010.45 MB (93469.83 MB after compression)
                                                     -362.6205 87862964 611.02%
1757833 1127056
                   -215.2144
                               120
                                        -51.0000
1759906 1130330
                   -126.6583
                                64
                                        -51.0000
                                                     -362.6205 87942162 611.02%
1761605 1131195
                   -158.9016
                                        -51.0000
                                                     -362.6205 87952404 611.02%
                                98
```

1763935 1132655

-353.8302

251

-51.0000

-362.6059 88000738 610.99%

1766383	1135120	-358.4267	298	-51.0000	-362.5995	88069117	610.98%
1769340	1134674	-351.0958	290	-51.0000	-362.5959	88065237	610.97%
1770949	1137435	-354.5922	298	-51.0000	-362.5959	88133999	610.97%
1772901	1138195	-317.6154	230	-51.0000	-362.5891	88152987	610.96%
1774852	1138989	-319.6824	186	-51.0000	-362.5858	88197180	610.95%
1777181	1141667	-228.0794	142	-51.0000	-362.5778	88238065	610.94%
Elapsed	time = 4149	.17 sec. (25	36284.58 1	ticks, tree =	111606.07	MB, solut	ions = 37)
Nodefile	e size = 1094	464.13 MB (9	5628.95 MI	B after compre	ession)		
1779471	1142822	-356.9082	300	-51.0000	-362.5778	88301076	610.94%
1781560	1145486	-345.4786	300	-51.0000	-362.5709	88354961	610.92%
1783964	1146383	-142.0000	75	-51.0000	-362.5683	88384760	610.92%
1786599	1149409	-156.9016	93	-51.0000	-362.5632	88449409	610.91%
1788528	1150674	-286.3848	175	-51.0000	-362.5575	88476984	610.90%
1790262	1152003	-152.8889	82	-51.0000	-362.5554	88530369	610.89%
1792157	1154316	-312.5151	205	-51.0000	-362.5519	88608998	610.89%
1794239	1155329	-81.4111	38	-51.0000	-362.5519	88632851	610.89%
1796795	1155687	-226.8191	121	-51.0000	-362.5490	88638195	610.88%
1798889	1157971	-242.5105	141	-51.0000	-362.5490	88695455	610.88%
Elapsed	time = 4216	.83 sec. (25	74439.80 1	ticks, tree =	113971.04	MB, solut	ions = 37)
Nodefile	e size = 1118	320.30 MB (9	7713.78 MI	B after compre	ession)		
1801257	1160786	-326.2609	217	-51.0000	-362.5476	88785387	610.88%
1803904	1160584	-197.5598	116	-51.0000	-362.5476	88778037	610.88%
1806916	1163684	-112.0000	59	-51.0000	-362.5476	88855097	610.88%
1809860	1164061	-164.0000	89	-51.0000	-362.5359	88860117	610.85%
1812427	1167790	-353.8110	266	-51.0000	-362.5338	88946081	610.85%
1813938	1169137	-355.4961	313	-51.0000	-362.5313	88984565	610.85%
1815156	1169515	-95.0000	50	-51.0000	-362.5280	88989276	610.84%
1816884	1172293	-109.0000	56	-51.0000	-362.5280	89054712	610.84%
1819029	1172222	-359.4854	274	-51.0000	-362.5165	89088292	610.82%
1820702	1175341	-101.0000	59	-51.0000	-362.5139	89172352	610.81%
Elapsed	time = 4283	.62 sec. (26	12607.16	ticks, tree =	116452.58	MB, solut	ions = 37)
Nodefile	e size = 1143	352.58 MB (9	9959.10 MI	B after compre	ession)		
1821717	1175520	-316.6016	211	-51.0000	-362.5105	89178976	610.80%
1822802	1175743	-356.9446	302	-51.0000	-362.5105	89208707	610.80%
1825186	1177728	-359.8573	307	-51.0000	-362.5019	89292196	610.79%
1828466	1178524	-311.3564	177	-51.0000	-362.4955	89352642	610.78%
1831697	1179704	-254.7012	147	-51.0000	-362.4947	89383091	610.77%
1833684	1185363	-346.5593	242	-51.0000	-362.4913	89494458	610.77%
1835958	1185747	-65.0000	35	-51.0000	-362.4905	89499237	610.77%

1838222 1187800	-349.6080	333	-51.0000	-362.4905	89556219	610.77%
1840349 1189274	-190.9810	106	-51.0000	-362.4891	89593726	610.76%
1842574 1190077	-131.0000	66	-51.0000	-362.4891	89607149	610.76%
Elapsed time = 434	8.73 sec. (26	50771.96	S ticks, tree =	118254.77	MB, solut	ions = 37)
Nodefile size = 11	6123.16 MB (1	01513.80) MB after comp	ression)		
1844137 1190950	-337.9764	239	-51.0000	-362.4773	89621043	610.74%
1845868 1194067	-163.0000	91	-51.0000	-362.4773	89702644	610.74%
1847428 1194442	infeasible		-51.0000	-362.4773	89707519	610.74%
1848545 1195399	-338.9939	269	-51.0000	-362.4715	89749797	610.73%
1849976 1197189	-312.5297	186	-51.0000	-362.4715	89842164	610.73%
1852539 1197765	-172.7495	102	-51.0000	-362.4715	89864964	610.73%
1855071 1199117	-174.5109	95	-51.0000	-362.4673	89907349	610.72%
1857581 1199427	-79.0000	33	-51.0000	-362.4673	89912585	610.72%
1860128 1204628	-139.0000	78	-51.0000	-362.4673	90040175	610.72%
1862424 1204806	-92.0000	38	-51.0000	-362.4673	90046923	610.72%
Elapsed time = 441	2.31 sec. (26	88942.58	3 ticks, tree =	119835.92	MB, solut	ions = 37)
Nodefile size = 11	7703.76 MB (1	02891.72	2 MB after comp	ression)		
1864012 1205110	-334.7566	231	-51.0000	-362.4673	90052032	610.72%
1865715 1206430	-248.0777	143	-51.0000	-362.4673	90089209	610.72%
1867880 1208849	-360.7170	315	-51.0000	-362.4673	90124930	610.72%
1869710 1210002	-253.9861	148	-51.0000	-362.4461	90184073	610.68%
1871605 1212587	-271.6025	172	-51.0000	-362.4461	90320048	610.68%
1873471 1213584	-156.0000	98	-51.0000	-362.4461	90347220	610.68%
1875249 1215234	-346.3866	246	-51.0000	-362.4461	90387853	610.68%
1876789 1216880	-136.0000	70	-51.0000	-362.4317	90467261	610.65%
1878428 1216583	-360.9537	396	-51.0000	-362.4300	90462464	610.65%
1879496 1218118	-271.7228	172	-51.0000	-362.4300	90528095	610.65%
Elapsed time = 447	5.52 sec. (27	27125.87	ticks, tree =	121765.60	MB, solut	ions = 37)
Nodefile size = 11	9662.56 MB (1	04632.68	B MB after comp	ression)		
1879927 1219133	-331.2837	228	-51.0000	-362.4208	90557727	610.63%
1881200 1219700	-354.6783	283	-51.0000	-362.4206	90586562	610.63%
1882723 1221442	-339.9416	253	-51.0000	-362.4201	90642101	610.63%
1883876 1222681	-353.1613	241	-51.0000	-362.4167	90733610	610.62%
1884976 1222419	-356.8062	237	-51.0000	-362.4167	90727814	610.62%
1885808 1224246	-174.6478	96	-51.0000	-362.4148	90820647	610.62%
1887127 1224675	-96.0000	47	-51.0000	-362.4143	90824870	610.62%
1888119 1226301	-354.7976	297	-51.0000	-362.4143	90942207	610.62%
1889542 1227449	-292.9870	200	-51.0000	-362.4143	90980258	610.62%
1891491 1227878	-201.0640	120	-51.0000	-362.4065	90984614	610.60%

```
Elapsed time = 4533.80 sec. (2765317.84 ticks, tree = 122538.28 MB, solutions = 37)
Nodefile size = 120337.04 MB (105215.91 MB after compression)
1893792 1227996
                   -162.0000
                                 91
                                         -51.0000
                                                      -362.4065 91035314 610.60%
1896328 1230354
                    -246.3380
                                         -51.0000
                                                      -362.4053 91099099
                                142
                                                                          610.60%
1898667 1232386
                   -348.0567
                                224
                                         -51.0000
                                                      -362.4034 91151758
                                                                          610.59%
1900424 1234216
                   -202.3876
                                116
                                         -51.0000
                                                      -362.3982 91202203
                                                                          610.58%
1902409 1235516
                   -146.0000
                                 82
                                         -51.0000
                                                      -362.3963 91228751 610.58%
1904297 1236559
                   -294.4467
                                221
                                         -51.0000
                                                      -362.3939 91256879
                                                                          610.58%
1905946 1237273
                    -169.0000
                                 91
                                         -51.0000
                                                      -362.3926 91297562
                                                                          610.57%
                                                                          610.57%
1908247 1238212
                   -359.1546
                                327
                                         -51.0000
                                                      -362.3923 91327857
                                         -51.0000
1910238 1241889
                                                      -362.3840 91454153 610.56%
                     -93.0000
                                 43
1912123 1242108
                                                      -362.3840 91443338 610.56%
                    -253.7352
                                161
                                         -51.0000
Elapsed time = 4597.07 sec. (2803482.88 ticks, tree = 124122.99 MB, solutions = 37)
Nodefile size = 121915.48 MB (106601.21 MB after compression)
1913823 1244810
                    -293.5904
                                165
                                         -51.0000
                                                      -362.3840 91560056 610.56%
1915261 1242831
                                224
                    -348.9132
                                         -51.0000
                                                      -362.3840 91487721 610.56%
1917087 1245691
                    -357.7825
                                398
                                         -51.0000
                                                      -362.3736 91596278 610.54%
1919377 1247859
                   -350.8520
                                301
                                         -51.0000
                                                      -362.3727 91640207
                                                                          610.53%
1920957 1249365
                    -349.1644
                                264
                                         -51.0000
                                                      -362.3727 91704716 610.53%
1922448 1251919
                   -241.0255
                                135
                                         -51.0000
                                                      -362.3727 91787046
                                                                          610.53%
1924299 1251385
                   -139.0000
                                                      -362.3727 91745691
                                 89
                                         -51.0000
                                                                          610.53%
1925928 1254633
                   -335.5796
                                         -51.0000
                                                      -362.3727 91864879
                                212
                                                                          610.53%
1927733 1253942
                                                      -362.3727 91863422 610.53%
                   -248.7582
                                148
                                         -51.0000
1929800 1254954
                    -161.5000
                                 98
                                         -51.0000
                                                      -362.3727 91914276 610.53%
Elapsed time = 4665.96 sec. (2841657.11 ticks, tree = 125876.31 MB, solutions = 37)
Nodefile size = 123736.62 MB (108198.02 MB after compression)
1932915 1257567
                    -356.6930
                                308
                                         -51.0000
                                                      -362.3727 91971230 610.53%
1935557 1257895
                   -235.1592
                                138
                                         -51.0000
                                                      -362.3485 91975728 610.49%
1937930 1259507
                    -133.0000
                                 76
                                         -51.0000
                                                      -362.3470 92043433 610.48%
1939112 1262952
                   -268.7837
                                146
                                         -51.0000
                                                      -362.3423 92119640
                                                                          610.48%
1941120 1263559
                                228
                   -336.0770
                                         -51.0000
                                                      -362.3380 92141033
                                                                          610.47%
1943317 1266134
                    -78.0000
                                 38
                                         -51.0000
                                                      -362.3380 92201328
                                                                          610.47%
                    -81.0000
                                         -51.0000
1945343 1266470
                                                      -362.3380 92230682
                                 35
                                                                          610.47%
1947101 1268368
                    -140.3414
                                 74
                                         -51.0000
                                                      -362.3309 92291980
                                                                          610.45%
1948917 1269242
                    -223.0782
                                125
                                         -51.0000
                                                      -362.3309 92327936
                                                                          610.45%
1950788 1269706
                     -57.0000
                                 25
                                         -51.0000
                                                      -362.3309 92331814 610.45%
Elapsed time = 4731.66 sec. (2879825.80 ticks, tree = 127608.51 MB, solutions = 37)
Nodefile size = 125386.48 MB (109656.60 MB after compression)
1952593 1272828
                   -163.0000
                                         -51.0000
                                                      -362.3309 92422770 610.45%
                                 86
```

```
1955188 1273992
                   -348.8436
                               266
                                        -51.0000
                                                     -362.3309 92476904 610.45%
1957494 1273935
                   -179.5526
                                97
                                        -51.0000
                                                     -362.3309 92458164 610.45%
1958998 1275371
                   -357.5784
                               362
                                        -51.0000
                                                     -362.3309 92499131 610.45%
1960528 1278994
                   -183.2555
                                        -51.0000
                                                     -362.3309 92595513
                               100
                                                                         610.45%
1962501 1279390
                   -143.0000
                                79
                                        -51.0000
                                                     -362.3309 92614185
                                                                         610.45%
1963753 1279515
                   -181.5109
                               103
                                        -51.0000
                                                     -362.3309 92622257
                                                                         610.45%
1965266 1282516
                   -101.0000
                                45
                                        -51.0000
                                                     -362.3309 92718093
                                                                         610.45%
1966607 1283982
                   -337.5188
                               281
                                        -51.0000
                                                     -362.3309 92799904
                                                                         610.45%
1968190 1282938
                   -315.7303
                               204
                                        -51.0000
                                                     -362.3309 92761351
                                                                         610.45%
Elapsed time = 4795.38 sec. (2917991.21 ticks, tree = 129154.59 MB, solutions = 37)
Nodefile size = 127050.39 MB (111116.43 MB after compression)
1970548 1286382
                                                     -362.3309 92905255 610.45%
                   -334.5310
                               206
                                        -51.0000
1972793 1287538
                                                     -362.3309 92945474 610.45%
                   -249.0323
                               140
                                        -51.0000
1974081 1286958
                   -223.8645
                               140
                                        -51.0000
                                                     -362.3309 92914229 610.45%
1975090 1289465
                   -301.1046
                               172
                                        -51.0000
                                                     -362.3309 93018059
                                                                         610.45%
1976045 1288874
                   -355.0767
                               231
                                        -51.0000
                                                     -362.3309 92974520
                                                                         610.45%
1977011 1292121
                   -361.9902
                               290
                                        -51.0000
                                                     -362.3309 93088426
                                                                         610.45%
1978501 1293014
                   -358.8972
                               302
                                        -51.0000
                                                     -362.3309 93119372 610.45%
1980427 1292664
                   -196.8761
                               136
                                        -51.0000
                                                     -362.3074 93113119
                                                                         610.41%
1981659 1294107
                    -96.5679
                                44
                                        -51.0000
                                                     -362.3074 93290304
                                                                         610.41%
1982761 1295504
                   -257.0260
                                        -51.0000
                                                     -362.3074 93318116 610.41%
                               157
Elapsed time = 4857.33 sec. (2956165.23 ticks, tree = 130261.01 MB, solutions = 37)
Nodefile size = 128107.74 MB (112032.73 MB after compression)
                                                     -362.3074 93336345 610.41%
1984197 1296305
                   -228.6609
                               123
                                        -51.0000
1985492 1296197
                   -177.2575
                               101
                                        -51.0000
                                                     -362.3074 93393577 610.41%
1986946 1298745
                   -119.0000
                                59
                                        -51.0000
                                                     -362.3074 93460887 610.41%
1988715 1298777
                   -360.0183
                               343
                                        -51.0000
                                                     -362.3074 93496963
                                                                         610.41%
1990344 1301907
                                                     -362.3074 93607408 610.41%
                   -355.9441
                               253
                                        -51.0000
1992706 1302258
                   -120.0000
                                62
                                        -51.0000
                                                     -362.2874 93612558 610.37%
1995018 1304182
                   -225.4859
                               128
                                        -51.0000
                                                     -362.2874 93683921
                                                                         610.37%
1997601 1303431
                                                     -362.2874 93659824
                   -155.8836
                                85
                                        -51.0000
                                                                         610.37%
1999960 1306782
                   -179.7059
                               100
                                        -51.0000
                                                     -362.2874 93741768
                                                                         610.37%
2001806 1307133
                   -277.2162
                                                     -362.2534 93746417 610.30%
                               157
                                        -51.0000
Elapsed time = 4924.31 sec. (2994343.65 ticks, tree = 131623.21 MB, solutions = 37)
Nodefile size = 129402.80 MB (113165.07 MB after compression)
2003608 1310011
                      cutoff
                                        -51.0000
                                                     -362.2505 93852745 610.30%
2005876 1311929
                   -360.7152
                               340
                                        -51.0000
                                                     -362.2420 93872511 610.28%
2007520 1314349
                   -361.2690
                               324
                                        -51.0000
                                                     -362.2401 93949400 610.27%
2010050 1315474
                   -358.1109
                               347
                                        -51.0000
                                                     -362.2348 93980261 610.26%
```

2012141 1314837	-121.0000	78	-51.0000	-362.2319	93967126	610.26%
2014117 1316900	-210.4484	137	-51.0000	-362.2319	94047490	610.26%
2016539 1320203	-301.7363	185	-51.0000	-362.2225	94177706	610.24%
2018363 1319559	-90.0000	35	-51.0000	-362.2210	94148369	610.24%
2019749 1322440	-109.2500	66	-51.0000	-362.2210	94261607	610.24%
2021774 1322860	-353.5627	239	-51.0000	-362.2210	94250994	610.24%
Elapsed time = 4	1990.11 sec. (3	032511.	21 ticks, tree =	133163.44	MB, solut	ions = 37)
Nodefile size =	130977.97 MB (114541.	34 MB after comp	ression)		
2023532 1324766	-201.9114	114	-51.0000	-362.2210	94318165	610.24%
2025242 1327799	-353.9849	299	-51.0000	-362.2100	94439879	610.22%
2026170 1326401	-158.0000	94	-51.0000	-362.2098	94361700	610.22%
2026901 1329537	-287.7297	180	-51.0000	-362.2078	94472233	610.21%
2028133 1330094	-58.4032	26	-51.0000	-362.2078	94513762	610.21%
2029923 1331143	-65.4032	29	-51.0000	-362.2065	94618610	610.21%
2031440 1331107	-318.8100	196	-51.0000	-362.2065	94607266	610.21%
2032934 1332754	-265.4758	167	-51.0000	-362.2058	94669472	610.21%
2034589 1334098	-153.0000	81	-51.0000	-362.2021	94746572	610.20%
2036138 1334328	-243.3282	168	-51.0000	-362.2021	94751540	610.20%
Elapsed time = 5	053.58 sec. (3	070737.	59 ticks, tree =	134474.79	MB, solut	ions = 37)
Nodefile size =	132323.41 MB (115713.	57 MB after comp	ression)		
2038712 1333925	-78.5139	50	-51.0000	-362.2021	94744505	610.20%
2040376 1337795	infeasible		-51.0000	-362.1926	94873080	610.18%
2042249 1338711	-95.0000	53	-51.0000	-362.1918	94889167	610.18%
2043289 1339688	-196.9467	171	-51.0000	-362.1918	94930297	610.18%
2044354 1340831	-339.2202	210	-51.0000	-362.1918	94959160	610.18%
2045538 1341759	-316.6392	222	-51.0000	-362.1891	94978591	610.17%
2047212 1344458	-298.5127	183	-51.0000	-362.1891	95116161	610.17%
2048192 1343500	-315.8810	205	-51.0000	-362.1891	95075051	610.17%
2050162 1346617	-258.7810	146	-51.0000	-362.1891	95248518	610.17%
2052107 1347065	-209.5024	121	-51.0000	-362.1834	95285696	610.16%
Elapsed time = 5	5113.04 sec. (3	108900.	99 ticks, tree =	135743.20	MB, solut	ions = 37)
Nodefile size =	133587.80 MB (116827.	78 MB after comp	ression)		
2054327 1347767	-179.1118	105	-51.0000	-362.1834	95328232	610.16%
2056734 1350306	-355.7437	324	-51.0000	-362.1701	95403631	610.14%
2057895 1349123	-285.9940	159	-51.0000	-362.1701	95387785	610.14%
2059298 1353824	177 0050	104	-51.0000	-362.1701	95512857	610.14%
2009290 1000024	-177.2253	104			00012001	
2061571 1354213		137	-51.0000	-362.1701		610.14%
	-235.3818				95517218	

2066171 1357304	-216.6867	128	-51.0000	-362.1588	95666338	610.12%
2068842 1358733	-338.9059	219	-51.0000	-362.1540	95690539	610.11%
2071197 1359079	-151.0000	86	-51.0000	-362.1505	95694410	610.10%
Elapsed time =	5183.43 sec. (3	3147063.	12 ticks, tree =	137247.59	MB, solut	ions = 37)
Nodefile size =	= 135065.62 MB (118120.	50 MB after comp	oression)		
2073960 1362024	l infeasible		-51.0000	-362.1492	95770534	610.10%
2076419 1362562	-356.2101	269	-51.0000	-362.1458	95796757	610.09%
2078532 1365651	-229.5769	161	-51.0000	-362.1441	95842208	610.09%
2080519 1367251	-81.0000	42	-51.0000	-362.1406	95880610	610.08%
2082831 1367594	-215.7704	129	-51.0000	-362.1361	95886294	610.07%
2085431 1371304	-165.5000	93	-51.0000	-362.1349	95986118	610.07%
2087706 1371516	-311.5010	186	-51.0000	-362.1292	95993806	610.06%
2090838 1372474	-196.4747	136	-51.0000	-362.1266	96028276	610.05%
2093888 1376175	-268.9368	163	-51.0000	-362.1222	96150851	610.04%
2097037 1376513	-93.0000	48	-51.0000	-362.1195	96156174	610.04%
Elapsed time =	5252.06 sec. (3	3185223.	84 ticks, tree =	= 139227.82	MB, solut	ions = 37)
Nodefile size =	= 137044.02 MB (119868.	56 MB after comp	oression)		
2099977 1377822	-309.5230	191	-51.0000	-362.1194	96195538	610.04%
2102737 1383997	-216.9528	122	-51.0000	-362.1141	96313606	610.03%
2105386 1382784	-357.4801	259	-51.0000	-362.1109	96296349	610.02%
2107072 1384958	-243.3201	190	-51.0000	-362.1080	96353624	610.02%
2109715 1389908	-91.0000	41	-51.0000	-362.1018	96431278	610.00%
2112892 1389386	-237.2620	142	-51.0000	-362.1014	96428949	610.00%
2116344 1392877	-76.0000	37	-51.0000	-362.0952	96518047	609.99%
2119601 1396055	-239.8675	163	-51.0000	-362.0902	96571138	609.98%
2122701 1397588	-162.0000	92	-51.0000	-362.0878	96597500	609.98%
2125585 1399419	-107.0000	56	-51.0000	-362.0837	96623631	609.97%
Elapsed time =	5323.57 sec. (3	3223386.	22 ticks, tree =	= 142291.72	MB, solut	ions = 37)
Nodefile size =	= 140136.28 MB (122587.	56 MB after comp	oression)		
2127637 1401788	-98.9772	55	-51.0000	-362.0837	96673819	609.97%
2129462 1403019	-101.0000	53	-51.0000	-362.0777	96689106	609.96%
2130967 1403384	-180.0312	103	-51.0000	-362.0736	96694336	609.95%
2132398 1407650	-249.8456	150	-51.0000	-362.0716	96832474	609.94%
2134190 1407911	-259.4266	153	-51.0000	-362.0716	96840144	609.94%
2136287 1409592	2 -347.6216	223	-51.0000	-362.0716	96926465	609.94%
2138800 1410407	-107.4540	54	-51.0000	-362.0673	96963154	609.94%
2140533 1410269	-356.8189	314	-51.0000	-362.0623	96948737	609.93%
2141817 1413348		205	-51.0000	-362.0608	97027902	609.92%
2143712 1415198			-51.0000	-362.0608		609.92%
						-

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Elapsed time = 5387.73 sec. (3261572.73 ticks, tree = 144059.10 MB, solutions = 37)
Nodefile size = 141929.99 MB (124151.38 MB after compression)
2145303 1415470
                    -243.6396
                                140
                                         -51.0000
                                                      -362.0548 97110721 609.91%
2147224 1415864
                    -346.9044
                                         -51.0000
                                                      -362.0548 97087785
                                241
                                                                          609.91%
2149106 1420398
                   -353.5467
                                272
                                         -51.0000
                                                      -362.0502 97254799
                                                                          609.90%
2151211 1420743
                    -195.9210
                                100
                                         -51.0000
                                                      -362.0502 97260086
                                                                          609.90%
2153737 1421083
                    -290.3449
                                215
                                         -51.0000
                                                      -362.0502 97264392
                                                                          609.90%
2155994 1424276
                    -173.5964
                                 95
                                         -51.0000
                                                      -362.0502 97359502
                                                                          609.90%
2157424 1423832
                    -188.4168
                                116
                                         -51.0000
                                                      -362.0502 97352625
                                                                          609.90%
2158038 1425742
                    -231.6470
                                143
                                         -51.0000
                                                      -362.0502 97404097
                                                                          609.90%
                                         -51.0000
2159500 1428123
                    -166.8025
                                                      -362.0502 97507292 609.90%
                                112
2161270 1427691
                                                      -362.0502 97484141 609.90%
                    -233.3973
                                129
                                         -51.0000
Elapsed time = 5455.78 sec. (3299734.67 ticks, tree = 145843.98 MB, solutions = 37)
Nodefile size = 143666.89 MB (125689.91 MB after compression)
2163098 1428744
                    -310.5486
                                196
                                         -51.0000
                                                      -362.0502 97518331 609.90%
2164625 1429691
                                                      -362.0502 97530450 609.90%
                    -72.0000
                                 29
                                         -51.0000
2166592 1430389
                    -262.9791
                                183
                                         -51.0000
                                                      -362.0502 97612273
                                                                          609.90%
2168915 1431725
                    -356.9467
                                343
                                         -51.0000
                                                      -362.0502 97621871
                                                                          609.90%
2170713 1434358
                    -258.5424
                                166
                                         -51.0000
                                                      -362.0502 97704062
                                                                          609.90%
2172463 1434714
                    -357.2590
                                274
                                         -51.0000
                                                      -362.0502 97708705
                                                                          609.90%
2174588 1437891
                                227
                                                      -362.0284 97794992
                    -344.3184
                                         -51.0000
                                                                          609.86%
2176317 1438251
                    -145.9176
                                         -51.0000
                                                      -362.0284 97800479
                                 80
                                                                          609.86%
2177202 1438198
                                                      -362.0284 97815908
                    -333.6357
                                210
                                         -51.0000
                                                                          609.86%
2179165 1439916
                    -353.4805
                                424
                                         -51.0000
                                                      -362.0284 97872104 609.86%
Elapsed time = 5521.06 sec. (3337907.15 ticks, tree = 147605.70 MB, solutions = 37)
Nodefile size = 145495.21 MB (127311.62 MB after compression)
2181324 1440866
                    -283.2540
                                         -51.0000
                                                      -362.0284 97891679 609.86%
                                176
2182556 1442766
                    -158.4380
                                 82
                                         -51.0000
                                                      -362.0284 97941562 609.86%
2184500 1444493
                    -314.4764
                                222
                                         -51.0000
                                                      -362.0284 97994623
                                                                          609.86%
2186406 1444801
                    -224.1898
                                124
                                         -51.0000
                                                      -362.0284 98013376
                                                                          609.86%
2188871 1447973
                    -339.4077
                                214
                                         -51.0000
                                                      -362.0284 98109830
                                                                          609.86%
2190940 1449999
                    -290.2922
                                199
                                         -51.0000
                                                      -361.9977 98233021
                                                                          609.80%
                                         -51.0000
2193520 1449073
                    -361.5637
                                                      -361.9977 98128061
                                435
                                                                          609.80%
                                                      -361.9971 98276855
2196434 1451931
                    -314.6463
                                224
                                         -51.0000
                                                                          609.80%
2199381 1453652
                    -185.5070
                                 97
                                         -51.0000
                                                      -361.9971 98315726
                                                                          609.80%
2201426 1454807
                    -117.0000
                                         -51.0000
                                                      -361.9971 98362893
                                                                          609.80%
                                 60
Elapsed time = 5587.16 sec. (3376070.73 ticks, tree = 149537.40 MB, solutions = 37)
Nodefile size = 147385.66 MB (128968.65 MB after compression)
2204276 1456451
                   -225.5052
                                         -51.0000
                                                      -361.9971 98391992 609.80%
                                131
```

```
2206451 1460380
                   -271.7723
                                166
                                        -51.0000
                                                      -361.9904 98473773 609.79%
                                                                          609.79%
2209077 1462514
                   -361.1800
                               374
                                         -51.0000
                                                      -361.9904 98527678
2212458 1462879
                                                      -361.9809 98522461
                   -197.8400
                                113
                                        -51.0000
                                                                          609.77%
2215420 1467461
                    -259.2272
                                         -51.0000
                                                      -361.9735 98624285
                                145
                                                                          609.75%
2218387 1468647
                   -123.6583
                                         -51.0000
                                                      -361.9723 98654373
                                67
                                                                          609.75%
2221372 1471853
                    -350.9130
                                263
                                         -51.0000
                                                      -361.9667 98702789
                                                                          609.74%
2225070 1470218
                   -121.0000
                                64
                                         -51.0000
                                                      -361.9636 98673690
                                                                          609.73%
2228119 1471931
                    -201.6745
                                126
                                         -51.0000
                                                      -361.9572 98699736
                                                                          609.72%
2230869 1478734
                    -305.8009
                                190
                                         -51.0000
                                                      -361.9524 98808636
                                                                          609.71%
Elapsed time = 5661.26 sec. (3414225.98 ticks, tree = 153064.91 MB, solutions = 37)
Nodefile size = 150931.10 MB (132094.45 MB after compression)
2232763 1478343
                    -189.2024
                                                      -361.9492 98802610 609.70%
                                111
                                         -51.0000
2234988 1480112
                                                      -361.9440 98828947
                    -312.4234
                                187
                                         -51.0000
                                                                          609.69%
2237925 1484751
                    -313.7701
                                180
                                         -51.0000
                                                      -361.9388 98937741
                                                                          609.68%
2240558 1486010
                    -87.0000
                                43
                                         -51.0000
                                                      -361.9364 98964759
                                                                          609.68%
2242539 1487781
                   -275.2400
                                187
                                         -51.0000
                                                      -361.9309 99031246
                                                                          609.67%
2245035 1487728
                   -219.6291
                                                      -361.9281 99003844
                                122
                                         -51.0000
                                                                          609.66%
2246529 1491934
                                         -51.0000
                                                      -361.9255 99095848
                   -179.1228
                                94
                                                                          609.66%
2247954 1491580
                    -351.5553
                                243
                                         -51.0000
                                                      -361.9245 99089066
                                                                          609.66%
2249384 1491991
                    -291.4054
                                198
                                         -51.0000
                                                      -361.9245 99093972
                                                                          609.66%
                    -344.8796
2250277 1494816
                                224
                                                      -361.9245 99189716
                                         -51.0000
                                                                          609.66%
Elapsed time = 5727.78 sec. (3452393.37 ticks, tree = 155438.60 MB, solutions = 37)
Nodefile size = 153292.60 MB (134181.29 MB after compression)
2251810 1495637
                    -112.0000
                                58
                                         -51.0000
                                                      -361.9219 99235307 609.65%
2252985 1496849
                   -242.5733
                               165
                                         -51.0000
                                                      -361.9219 99290827
                                                                          609.65%
2253778 1497620
                   -345.1575
                                         -51.0000
                                                      -361.9219 99333352 609.65%
                                417
2254166 1498135
                   -355.5885
                                         -51.0000
                                                      -361.9157 99318850
                                                                          609.64%
                               305
                                                      -361.9157 99344381
2254590 1497715
                   -156.6532
                                90
                                         -51.0000
                                                                          609.64%
2255374 1499614
                    -341.7492
                                301
                                         -51.0000
                                                      -361.9143 99483056
                                                                          609.64%
                                                      -361.9143 99461630
2256612 1499695
                   -256.9245
                                148
                                         -51.0000
                                                                          609.64%
2258131 1500600
                    -112.0000
                                59
                                         -51.0000
                                                      -361.9143 99521815
                                                                          609.64%
2259968 1502063
                    -74.0000
                                31
                                         -51.0000
                                                      -361.9143 99596909
                                                                          609.64%
2261589 1501021
                    -217.7357
                                                      -361.9143 99544139
                                145
                                         -51.0000
                                                                          609.64%
Elapsed time = 5789.89 sec. (3490642.38 ticks, tree = 156097.56 MB, solutions = 37)
Nodefile size = 153881.77 MB (134701.90 MB after compression)
2263540 1503689
                    -351.0484
                               271
                                         -51.0000
                                                      -361.9143 99662117 609.64%
2265593 1505294
                   -257.5113
                                150
                                         -51.0000
                                                      -361.9143 99690177 609.64%
2267732 1505621
                    -77.0000
                                         -51.0000
                                                     -361.9143 99694602 609.64%
                                31
2269137 1508711
                                                      -361.9071 99827984 609.62%
                    -65.5679
                                35
                                         -51,0000
```

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2270876 1509033
                   -240.1320
                               134
                                        -51.0000
                                                     -361.9071 99832992 609.62%
2272906 1509090
                   -314.8264
                               233
                                        -51.0000
                                                     -361.9071 99822254 609.62%
2274629 1511601
                   -189.8173
                                                     -361.9002 99916173 609.61%
                               101
                                        -51.0000
2275232 1511926
                   -147.0000
                                        -51.0000
                                                     -361.9002 99933267
                                73
                                                                         609.61%
2276649 1513432
                                        -51.0000
                                                     -361.9002 99961904
                  infeasible
                                                                         609.61%
2284484 1518423
                   -347.9256
                               237
                                        -51.0000
                                                     -361.8881 1.00e+08 609.58%
Elapsed time = 5869.03 sec. (3540255.65 ticks, tree = 158053.08 MB, solutions = 37)
Nodefile size = 155868.06 MB (136448.34 MB after compression)
2293888 1523878
                   -359.4920
                               234
                                        -51.0000
                                                     -361.8779 1.00e+08
                                                                         609.56%
                                77
2300244 1531155
                   -143.7059
                                        -51.0000
                                                     -361.8641 1.01e+08 609.54%
2305495 1533878
                                                     -361.8641 1.01e+08 609.54%
                   -312.1851
                               184
                                        -51.0000
2310737 1538466
                                                     -361.8504 1.01e+08 609.51%
                   -359.9087
                               375
                                        -51.0000
2319427 1544696
                                                     -361.8504 1.01e+08 609.51%
                   -187.5489
                               104
                                        -51.0000
2329798 1548090
                   -351.7499
                               300
                                        -51.0000
                                                     -361.8348 1.01e+08 609.48%
                                        -51.0000
2340901 1560129
                   -303.0342
                               183
                                                     -361.8223 1.01e+08
                                                                         609.46%
2352039 1567246
                   -183.5988
                               116
                                        -51.0000
                                                     -361.8057 1.02e+08
                                                                         609.42%
2362020 1573455
                                        -51.0000
                                                     -361.7982 1.02e+08
                  infeasible
                                                                         609.41%
2374073 1581038
                   -228.1897
                               133
                                        -51.0000
                                                     -361.7858 1.02e+08 609.38%
Elapsed time = 6146.10 sec. (3692873.43 ticks, tree = 166163.23 MB, solutions = 37)
Nodefile size = 163955.13 MB (143560.66 MB after compression)
2383552 1588797
                                                     -361.7788 1.02e+08 609.37%
                   -311.2394
                               181
                                        -51.0000
2391426 1596592
                   -100.0000
                                        -51.0000
                                                     -361.7660 1.02e+08
                                67
                                                                         609.35%
                                                     -361.7523 1.03e+08 609.32%
2399501 1604465
                   -353.4838
                               253
                                        -51.0000
2406212 1609092
                   -187.2150
                               110
                                        -51.0000
                                                     -361.7359 1.03e+08 609.29%
2414023 1613458
                    -99.6122
                                48
                                        -51.0000
                                                     -361.7213 1.03e+08
                                                                         609.26%
2423894 1621187
                   -346.7928
                               202
                                        -51.0000
                                                     -361.7141 1.03e+08 609.24%
2432402 1623753
                   -181.7823
                                        -51.0000
                                                     -361.7031 1.03e+08
                                93
                                                                         609.22%
                                                     -361.6890 1.03e+08
2441756 1636254
                   -339.1537
                               432
                                        -51.0000
                                                                         609.19%
2448558 1638942
                   -357.1295
                               284
                                        -51.0000
                                                     -361.6797 1.03e+08 609.18%
                                        -51.0000
                                                     -361.6752 1.04e+08
2454329 1646493
                   -207.1387
                               147
                                                                         609.17%
Elapsed time = 6408.01 sec. (3845475.54 ticks, tree = 173640.02 MB, solutions = 37)
Nodefile size = 171517.61 MB (150199.52 MB after compression)
2458581 1647298
                                                     -361.6752 1.04e+08 609.17%
                   -162.0000
                                89
                                        -51.0000
2466444 1654276
                   -315.4581
                               198
                                        -51.0000
                                                     -361.6752 1.04e+08 609.17%
2470355 1658826
                   -353.0127
                               356
                                        -51.0000
                                                     -361.6752 1.04e+08
                                                                         609.17%
2473616 1660657
                   -169.0000
                                93
                                        -51.0000
                                                     -361.6752 1.04e+08 609.17%
2477627 1664097
                   -293.9190
                               163
                                        -51.0000
                                                     -361.6752 1.05e+08
                                                                         609.17%
2482952 1664957
                   -317.8915
                               228
                                        -51.0000
                                                     -361.6626 1.05e+08
                                                                         609.14%
2490159 1670626
                   -299.0124
                                                     -361.6626 1.05e+08 609.14%
                               185
                                        -51.0000
```

```
2496441 1674807
                   -179.6537
                               100
                                        -51.0000
                                                     -361.6489 1.05e+08 609.12%
2499857 1680158
                   -360.0926
                               333
                                        -51.0000
                                                     -361.6489 1.05e+08 609.12%
2503644 1682909
                   -223.7228
                                        -51.0000
                                                     -361.6489 1.05e+08 609.12%
                                137
Elapsed time = 6660.25 sec. (3998105.33 ticks, tree = 177713.50 MB, solutions = 37)
Nodefile size = 175582.00 MB (153769.34 MB after compression)
2508133 1685701
                    -351.1965
                                242
                                        -51.0000
                                                      -361.6489 1.05e+08 609.12%
2513566 1689957
                   -315.2063
                               204
                                        -51.0000
                                                      -361.6489 1.06e+08
                                                                         609.12%
                                                                         609.03%
2522621 1692554
                   -159.2441
                                        -51.0000
                                                      -361.6054 1.06e+08
                                88
2531222 1701571
                    -351.4425
                                327
                                        -51.0000
                                                      -361.6054 1.06e+08
                                                                         609.03%
2537166 1707313
                   -344.7554
                               276
                                        -51.0000
                                                      -361.6054 1.06e+08
                                                                         609.03%
2543854 1710306
                                                      -361.6054 1.06e+08
                    -288.1213
                                179
                                        -51.0000
                                                                         609.03%
                                                      -361.6054 1.06e+08
2548956 1715402
                   -352.9752
                                266
                                        -51.0000
                                                                         609.03%
                                                      -361.6054 1.07e+08
2556366 1719215
                    -90.8929
                                53
                                        -51.0000
                                                                         609.03%
2563936 1724929
                    -348.9798
                                269
                                         -51.0000
                                                      -361.5820 1.07e+08
                                                                         608.98%
2572853 1730095
                    -143.0000
                                96
                                         -51.0000
                                                      -361.5413 1.07e+08 608.90%
Elapsed time = 6920.25 sec. (4150726.32 ticks, tree = 184835.85 MB, solutions = 37)
Nodefile size = 182651.48 MB (160032.23 MB after compression)
2580724 1735982
                                                      -361.5161 1.07e+08 608.86%
                    -348.7664
                               273
                                        -51.0000
2585129 1742238
                    -340.2640
                                247
                                        -51.0000
                                                      -361.5073 1.07e+08 608.84%
2592516 1746730
                   -357.0770
                                344
                                        -51.0000
                                                      -361.4975 1.07e+08
                                                                         608.82%
2598719 1750962
                                                      -361.4916 1.08e+08
                   -323.6565
                                219
                                        -51.0000
                                                                         608.81%
2606882 1756673
                   -120.0000
                                        -51.0000
                                                      -361.4748 1.08e+08
                                64
                                                                         608.77%
                                                      -361.4690 1.08e+08
2611677 1761982
                   -164.3744
                                85
                                        -51.0000
                                                                         608.76%
2619177 1766883
                    -178.8411
                                97
                                         -51.0000
                                                      -361.4666 1.08e+08
                                                                         608.76%
2627954 1770167
                   -107.0000
                                47
                                         -51.0000
                                                      -361.4526 1.08e+08
                                                                         608.73%
2635043 1780029
                    -123.1203
                                        -51.0000
                                                      -361.4435 1.09e+08 608.71%
                                62
2639585 1781709
                    -314.0933
                                         -51.0000
                                                      -361.4365 1.09e+08 608.70%
                                199
Elapsed time = 7185.81 sec. (4303333.35 ticks, tree = 191557.34 MB, solutions = 37)
Nodefile size = 189428.39 MB (166019.78 MB after compression)
                                                      -361.4335 1.09e+08 608.69%
2647726 1786498
                    -104.0000
                                54
                                         -51.0000
2653388 1791883
                    -89.0000
                                45
                                        -51.0000
                                                      -361.4254 1.09e+08
                                                                         608.68%
2659559 1796095
                    -248.7363
                                        -51.0000
                                                      -361.4195 1.09e+08
                                                                         608.67%
                                154
2664920 1800003
                                                      -361.4124 1.09e+08
                   -208.3245
                                115
                                        -51.0000
                                                                         608.65%
2671339 1803572
                    -242.4922
                                143
                                        -51.0000
                                                      -361.4098 1.09e+08
                                                                         608.65%
                                                                         608.65%
2679485 1809454
                    -163.4830
                                93
                                         -51.0000
                                                      -361.4098 1.10e+08
2687816 1818604
                    -161.0000
                                        -51.0000
                                                      -361.4098 1.10e+08
                                82
                                                                         608.65%
2692818 1820449
                    -106.8889
                                48
                                         -51.0000
                                                      -361.3861 1.10e+08
                                                                         608.60%
2698954 1825943
                   -120.0000
                                        -51.0000
                                                      -361.3847 1.10e+08
                                69
                                                                         608.60%
2705641 1829933
                   -340.4938
                                                      -361.3663 1.10e+08 608.56%
                                220
                                        -51.0000
```

```
Elapsed time = 7443.22 sec. (4455943.64 ticks, tree = 197301.95 MB, solutions = 37)
Nodefile size = 195152.26 MB (171064.80 MB after compression)
2716311 1836247
                                                    -361.3485 1.11e+08 608.53%
                   -164.0000
                                97
                                       -51.0000
2724612 1841495
                   -209.1877
                               122
                                       -51.0000
                                                    -361.3366 1.11e+08 608.50%
2736277 1851272
                   -354.5079
                              276
                                       -51.0000
                                                    -361.3239 1.11e+08 608.48%
2746256 1859680
                                                    -361.3177 1.11e+08 608.47%
                   -304.4639
                               194
                                       -51.0000
2752715 1865169
                                       -51.0000
                                                    -361.3065 1.11e+08 608.44%
                   -314.2210
                              188
2760747 1868729
                               236
                                                    -361.2981 1.11e+08 608.43%
                   -334.1027
                                       -51.0000
2767824 1874686
                   -358.6653
                              314
                                       -51.0000
                                                    -361.2860 1.12e+08 608.40%
2776708 1879875
                   -108.5139
                               58
                                       -51.0000
                                                    -361.2798 1.12e+08 608.39%
2780036 1883524
                                                    -361.2798 1.12e+08 608.39%
```

-51.0000

728

GUB cover cuts applied: 2067

Clique cuts applied: 60 Cover cuts applied: 5679

Implied bound cuts applied: 140

Flow cuts applied: 220

Mixed integer rounding cuts applied: 7001

-346.3044

Zero-half cuts applied: 147

Lift and project cuts applied: 28 Gomory fractional cuts applied: 187

Root node processing (before b&c):

Real time 0.01 sec. (4.06 ticks)

Parallel b&c, 8 threads:

Real time = 7674.31 sec. (4597796.80 ticks)

Sync time (average) = 2890.35 sec. Wait time (average) = 0.00 sec.

Total (root+branch&cut) = 7674.31 sec. (4597800.86 ticks)

Iteration 15

Bounds on # of cuts = 8 with [3 3 2]

Error = 49 (out of 100 instances)

Accuracy = 51

Solving time = 127.905276652 min (minutes)

Accumulated time = 209.928617383 min (minutes)

<<< done

Biography

Songkomkrit Chaiyakan was born in Hatyai, Thailand, on August 12, 1991. He had been studying Mathematics and Applied Mathematics-Economics at Brown University, United States of America, from 2011 to 2013. In 2014, he transferred to a university in Thailand and received the Bachelor of Science (B.Sc.) degree in Mathematics from Prince of Songkla University, Thailand, in 2017. The Master of Science (M.Sc.) degree in Applied Mathematics and Computational Science was conferred by Chulalongkorn University, Thailand, in 2020. Currently, he is pursuing the Doctor of Philosophy (Ph.D.) program in Business Analytics and Data Science at National Institute of Development Administration (NIDA), Thailand.

Regarding work experience, he served as a homework grader for two undergraduate-level courses in calculus and microeconomics at Brown University from September 2012 to May 2013. He also worked as an academic officer at Learn Corporation from June 2019 to November 2019. At Chulalongkorn University, he served as a teaching assistant for two graduate-level courses in mathematical programming and real analysis in addition to three undergraduate-level courses in calculus and stochastic processes from January 2018 to April 2020. At National Institute of Development Administration, he assisted professors with their graduate classes in basic programming and database management, applied machine learning, and data streaming and real-time analytics from August 2022 to May 2024.

His research interest is to develop quantitative tools and achieve a breakthrough in finance, optimization, statistics and artificial intelligence (AI). In his spare time, he enjoys tackling unsolvable problems and also proving or providing interesting insights into commonly used, yet partially theoretically substantiated, statements.