

The effects of a money-financed fiscal stimulus

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JME 2019

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2020.8.14

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Background

- **limits** to conventional countercyclical policies.
 - **decline** of economic activity, through **rapid reductions** in interest rates and **substantial increases** in structural deficits
 - left policymakers out of conventional ammunition
- zero lower bound (ZLB) at a relatively early stage of the crisis
 - rising debt ratios forced widespread fiscal consolidations that likely **delayed the recovery and added to the economic pain.**
- Against that background, need to think of policies that may help stimulate a depressed economy **without relying on lower nominal interest rate** or further rises in the stock of **government debt.**

1. Introduction

How to do ?

- I analyze the effectiveness of an alternative policy: a ***money-financed fiscal stimulus.***
 - neither an increase in the stock of government debt nor higher taxes
- I study separately two types of **money-financed fiscal stimuli**
 - a **reduction** in (lump-sum) **taxes**
 - an **increase** in **government purchases.**

Literature

- Monetary and fiscal framework (*money-financed budget deficits*)
 - *Friedman, (1948); Haberler (1952)*
- Helicopter money (*money-financed fiscal transfers*)
 - *Friedman (1969);*
- A money-financed fiscal stimulus under a binding ZLB
 - *Bernanke (2003); Auerbach and Obstfeld (2005); Buiter (2014); Turner (2013, 2016); Reichlin et al. (2013); Giavazzi and Tabellini (2014)*
- Others
 - *Jung et al. (2005), Eggertsson ,Woodford (2003) and Werning (2011); Christiano et al., (2011); Eggertsson(2011); Bilbiie(2011); Davig and Leeper, (2011)*

Findings:

- In normal times
 - MF fiscal stimulus output multipliers larger than a DF fiscal stimulus.
 - Under DF, tax cut has no effect on activity and an increase in government purchases has a much smaller effect than under MF
 - Under MF, an increase in government purchases has a larger output multiplier, but a smaller consumption multiplier, than a tax cut.
- Under a binding zero lower bound
 - The difference in effectiveness between a MF fiscal stimulus and a DF one persist, though it is smaller in the case of an increase in government spending.
 - Under MF, **the differences between a tax cut and an increase in government spending become smaller.**

3. The fiscal and monetary policy framework

3.1. Government: budget constraints and financing regimes

The government's consolidated budget constraint is given by:

$$P_t G_t + B_{t-1}(1 + i_{t-1}) = P_t T_t + B_t + \Delta M_t \quad (1)$$

$$^1 G_t + B_{t-1} \mathcal{R}_{t-1} = T_t + B_t + \Delta M_t / P_t \quad (2)$$

Equilibria near a steady state with zero inflation, no trend growth.

$$T = G + \rho B \quad (3)$$

the level of seigniorages²

$$(\Delta M_t / P_t)(1/Y) = (\Delta M_t / M_{t-1})(P_{t-1} / P_t)L_{t-1} / Y \simeq \varkappa \Delta m_t \quad (4)$$

¹ G_t : real government purchases

$B_t = B_t / P_t \quad \mathcal{R} = (1 + i_t)(P_t / P_{t+1})$

² $m_t = \log M_t$ and $\varkappa = L/Y$

$L_t \equiv M_t / P_t$ denotes real balances

3. The fiscal and monetary policy framework

3.1. Government: budget constraints

A first order approximation of the consolidated budget constraint³

$$\hat{b}_t = (1 + \rho)\hat{b}_{t-1} + b(1 + \rho)(\hat{i}_{t-1} - \pi_t) + \hat{g}_t - \hat{t}_t - \varkappa \Delta m_t \quad (5)$$

a simple tax rule:

$$\hat{t}_t = \psi_b \hat{b}_{t-1} + \hat{t}_t^* \quad (6)$$

Combining (5) and (6) we obtain

$$\hat{b}_t = (1 + \rho - \psi_b)\hat{b}_{t-1} + b(1 + \rho)(\hat{i}_{t-1} - \pi_t) + \hat{g}_t - \hat{t}_t^* - \varkappa \Delta m_t \quad (7)$$

$$\text{TVC}^4 \quad \lim_{T \rightarrow +\infty} \Lambda_{0,T} \mathcal{B}_T = 0$$

³ $\hat{b}_t = (\mathcal{B}_t - \mathcal{B})/Y$ ⁴ $\psi_b > \rho$ $\hat{g}_t = (G_t - G)/Y$ $\hat{t}_t = (T_t - T)/Y$

3. The fiscal and monetary policy framework

3.1. financing regimes

Experiments⁵

- MF

keep real debt unchanged($\hat{b}_t = 0$)

$$\Delta m_t = (1/\varkappa)[\delta^t + b(1 + \rho)(\hat{i}_{t-1} - \pi_t)] \quad (8)$$

- DF

the monetary authority conducts policy so that $\pi_t = 0$ for all t

Code:

(i2-1)*dp + (i2-2)*bh = 0 ;

⁵ $\hat{t}_t^* = -\delta^t < 0$ $\hat{g}^t = \delta^t > 0$

4. Non-policy blocks

4.1 Households

$$\text{Max: } E_0 \sum_{t=0}^{\infty} \beta^t U(C_t, L_t, N_t; Z_t) \quad (9)$$

$$\text{s.t. } P_t C_t + B_t + M_t = B_{t-1}(1 + i_{t-1}) + M_{t-1} + W_t N_t + D_t - P_t T_t$$

$${}^6 \lim_{T \rightarrow +\infty} \Lambda_{0,T} \mathcal{A}_T \geq 0 \quad (10)$$

$$U(C, L, N; Z) = (U(C, L) - V(N))Z$$

$$U_{c,t} = \beta(1 + i_t)(P_t/P_{t-1})U_{c,t+1} \quad (11)$$

$$W_t/P_t = V_{n,t}/U_{c,t} \quad (12)$$

$$h(L_t/C_t) = i_t/(1 + i_{t1}) \quad (13)$$

⁶ $\mathcal{A}_T = [B_{t-1}(1 + i_{t-1}) + M_{t-1}]/P_t$

4. Non-policy blocks

4.1 Firms

- A representative firm

$$Y_t = \left(\int_0^1 Y_t(i)^{1-\frac{1}{\epsilon}} di \right)^{\frac{\epsilon}{\epsilon-1}}$$

- The set of demand conditions

$$Y_t(i) = (P_t(i)/P_t)^{-\epsilon} Y_t \quad \text{all } i \in [0, 1] \quad (14)$$

- Each firm produces a differentiated intermediate good with a technology

$$Y_t(i) = N_t(i)^{1-\alpha}$$

- NKPC

$$\pi_t = \beta \pi_{t+1} - \lambda(\mu_t - \mu)$$

$$\mu_t = \log \frac{(1-\alpha)P_t}{W_t N_t^\alpha} \quad \lambda = \frac{(1-\theta)(1-\beta\theta)(1-\alpha)}{\theta(1-\alpha+\alpha\epsilon)}$$

5. Steady state and equilibrium

$$\widehat{y}_t \equiv \log(Y_t/Y), \widehat{c}_t \equiv \log(C_t/C), \widehat{l}_t \equiv \log(L_t/L), \widehat{\xi}_t \equiv \log(U_{c,t}/U_c), \widehat{i}_t \equiv \log((1+i_t)/(1+\rho)), \text{ and } \widehat{\rho}_t \equiv -\log(Z_{t+1}/Z_t), \widehat{g}_t = G_t/Y$$

$$\widehat{y}_t = \widehat{c}_t + \widehat{g}_t \quad (15)$$

$$\widehat{\xi}_t = \widehat{\xi}_{t+1} + (\widehat{i}_t - \pi_{t+1} - \widehat{\rho}_t) \quad (16)$$

$$\widehat{\xi}_t = -\sigma \widehat{c}_t + \nu \widehat{l}_t \quad (17)$$

$$\pi_t = \beta \pi_{t+1} - \lambda \widehat{\mu}_t \quad (18)$$

$$\widehat{\mu}_t = \widehat{\xi}_t - \left(\frac{\alpha + \varphi}{1 - \alpha} \right) \widehat{y}_t \quad (19)$$

$$\widehat{l}_t = \widehat{c}_t - \eta \widehat{i}_t \quad (20)$$

$$\widehat{l}_{t-1} = \widehat{l}_t + \pi_t - \Delta m_t \quad (21)$$

$$\widehat{b}_t = (1 + \rho - \psi_b) \widehat{b}_{t-1} + b(1 + \rho)(\widehat{i}_{t-1} - \pi_t) + \widehat{g}_t - \widehat{t}_t^* - \kappa \Delta m_t, \quad (22)$$

$$\text{MF: } \Delta m_t = (1/\kappa) (\delta^t + b(1 + \rho)(\widehat{i}_{t-1} - \pi_t)) \quad (23)$$

$$\text{DF: } \pi_t = 0 \quad (24)$$

5.1 Calibration

Value	Describe
$\beta = 0.995$	discount factor
$\phi = 5$	inverse labor supply elasticity
$\alpha = 0.25$	capital share in production
$\epsilon = 9$	price markup
$\theta = 3/4$	price rigidity
$\varkappa = 1/3$	inverse velocity of money
$\eta = 7$	interest semi-elasticity of money demand
$\nu = 0$	separability of real balance
$\psi_b = 0.02$	tax adjustment parameter
$b = 2.4$	target debt ratio
$\delta = 0.5$	persistence parameter
$\sigma = 1$	coefficient of risk aversion

6.1. A money-financed tax cut

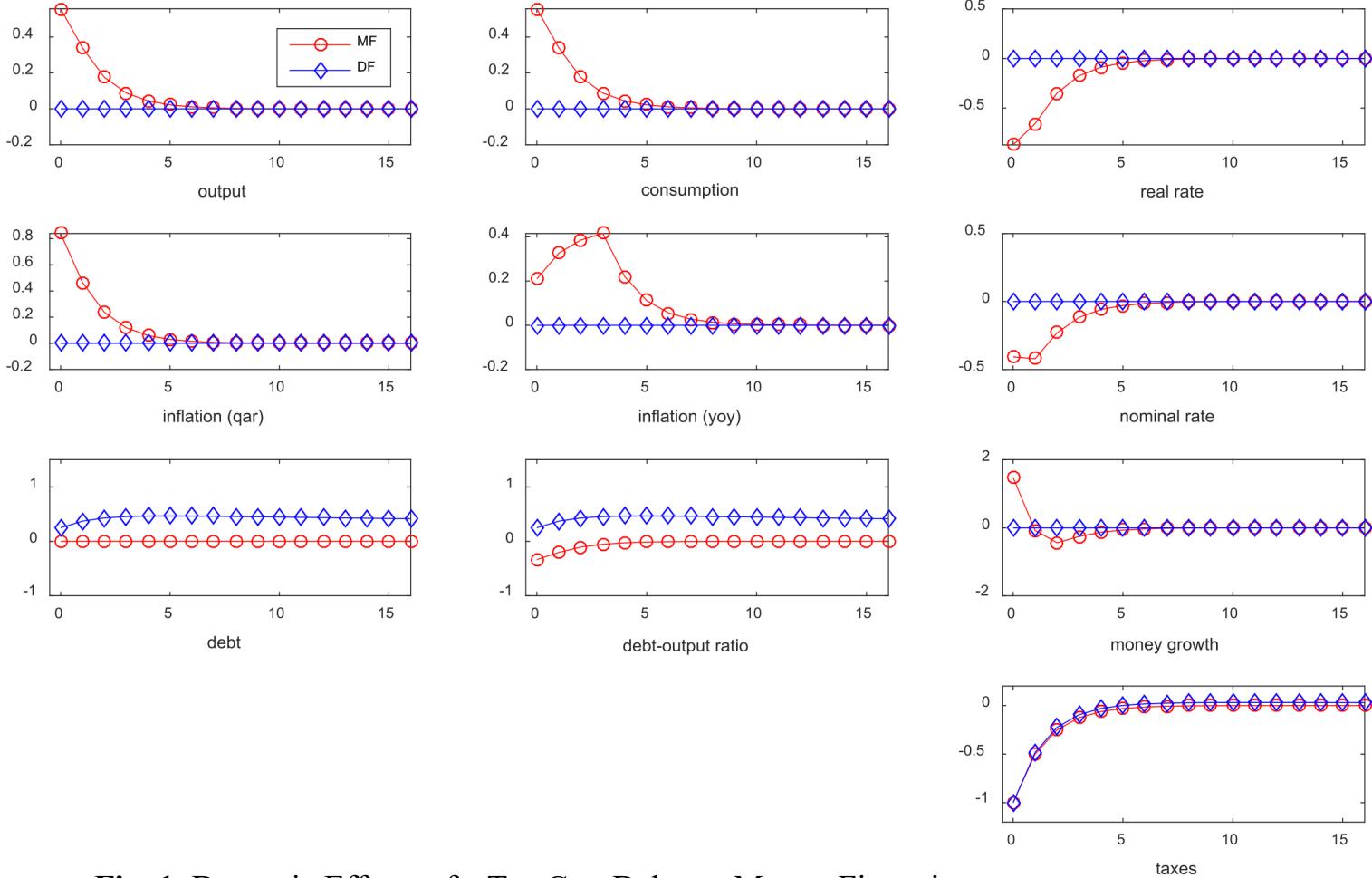


Fig. 1. Dynamic Effects of a Tax Cut: Debt vs. Money Financing

DF: $\pi = 0$

$$\text{tax} \downarrow \Rightarrow D \uparrow$$

MF: $D = 0$

$$\text{tax} \downarrow \Rightarrow \Delta M \uparrow \Rightarrow \begin{cases} c \uparrow \Rightarrow y \uparrow \Rightarrow \tilde{y} \uparrow \Rightarrow \pi \uparrow \\ i \downarrow (\pi \uparrow) \Rightarrow r \downarrow \Rightarrow c \uparrow \end{cases}$$

6.1 Ricardian equivalence

- Why does the Ricardian equivalence property apply to the debt-financed tax cut but not to the money-financed one?

Recall the household's period budget constraint:

$$P_t C_t + M_t + B_t = B_{t-1}(1 + i_{t-1}) + M_{t-1} + W_t N_t + D_t - P_t T_t \quad (32)$$

Letting $Y_t \equiv (W_t N_t + D_t)/P_t$ denote real income, and defining $\mathcal{A}_t \equiv (B_{t-1}(1 + i_{t-1}) + M_{t-1})/P_t$, the previous constraint can be rewritten as:

$$C_t + \frac{i_t}{1 + i_t} L_t + \frac{1}{\mathcal{R}_t} \mathcal{A}_{t+1} = \mathcal{A}_t + Y_t - T_t \quad (33)$$

Solving (33) forward from period zero onward and using the transversality condition $\lim_{T \rightarrow \infty} \Lambda_{0,T} \mathcal{A}_T = 0$ yields

$$\sum_{t=0}^{\infty} \Lambda_{0,t} \left(C_t + \frac{i_t}{1 + i_t} L_t \right) = \mathcal{A}_0 + \sum_{t=0}^{\infty} \Lambda_{0,t} (Y_t - T_t) \quad (34)$$

where $\Lambda_{0,t} \equiv \mathcal{R}_0^{-1} \mathcal{R}_1^{-1} \dots \mathcal{R}_{t-1}^{-1}$.

6.1 Ricardian equivalence

- The government's *consolidated* budget constraint:

$$G_t + \mathcal{B}_{t-1} \mathcal{R}_{t-1} = T_t + \mathcal{B}_t + \Delta M_t / P_t$$

On the other hand, solving the consolidated government budget constraint (2) forward from period 0 onwards yields:

$$\sum_{t=0}^{\infty} \Lambda_{0,t} G_t + \frac{B_{-1}(1+i_{-1})}{P_0} = \sum_{t=0}^{\infty} \Lambda_{0,t} \left(T_t + \frac{\Delta M_t}{P_t} \right) \quad (35)$$

where the transversality condition $\lim_{T \rightarrow \infty} \Lambda_{0,T} \mathcal{B}_T = 0$ has been imposed, as implied by $\lim_{T \rightarrow \infty} \Lambda_{0,T} \mathcal{A}_T = 0$ combined with the non-negativity constraint on money holdings.

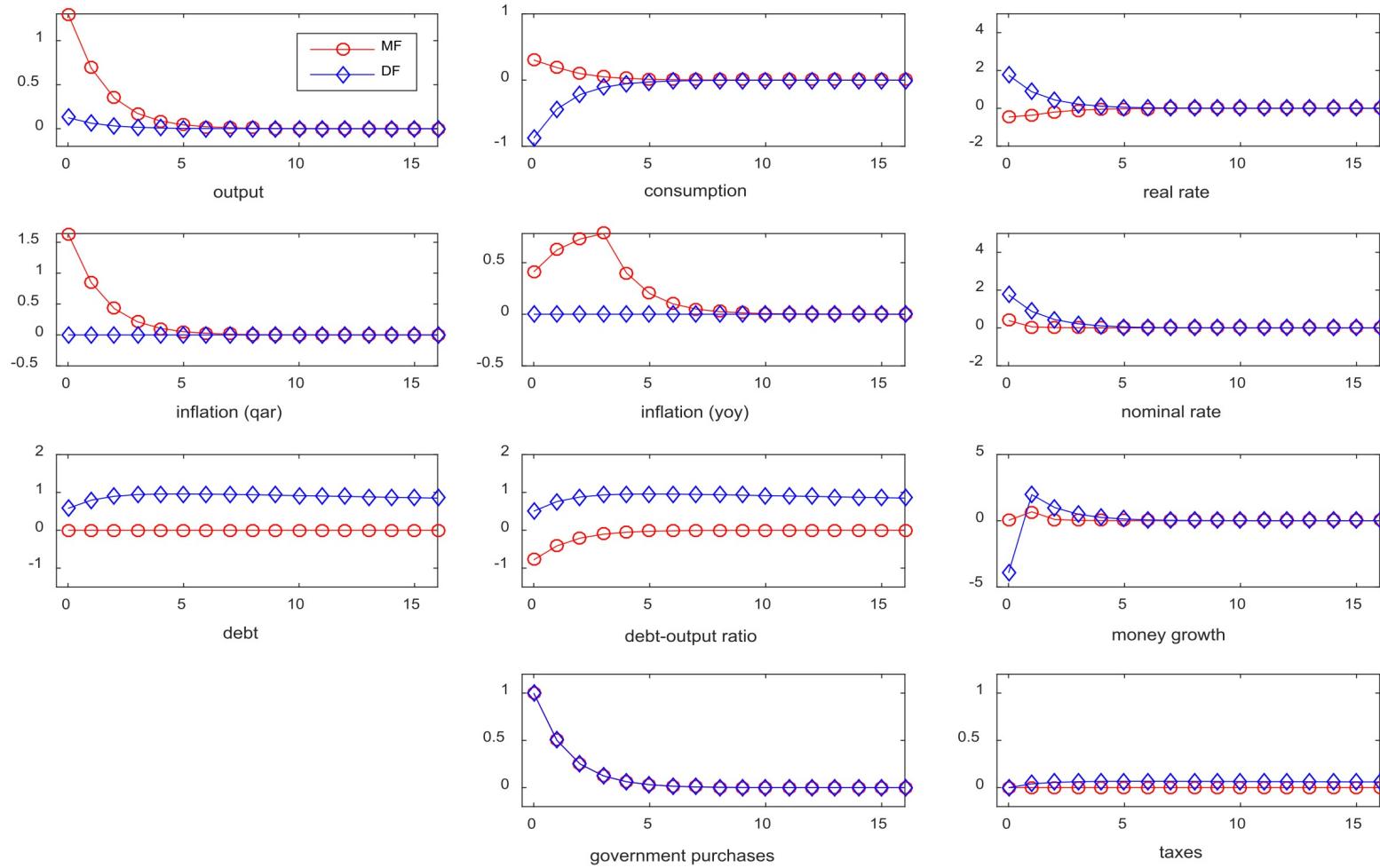
Combining (35) and (34), we obtain:

$$\sum_{t=0}^{\infty} \Lambda_{0,t} \left(C_t + \frac{i_t}{1+i_t} L_t \right) = \frac{M_{-1}}{P_0} + \sum_{t=0}^{\infty} \Lambda_{0,t} \left(Y_t - G_t + \frac{\Delta M_t}{P_t} \right) \quad (36)$$

...

$$\rightarrow C_0 = \frac{1-\beta}{1+\chi} \left(\frac{M_{-1}}{P_0} + \sum_{t=0}^{\infty} \Lambda_{0,t} \left(Y_t - G_t + \frac{\Delta M_t}{P_t} \right) \right)$$

6.2. A money-financed increase in government purchases



DF: $\pi = 0$

$$G \uparrow \Rightarrow \begin{cases} y \uparrow (\text{tiny}), i \uparrow (\pi = 0) \Rightarrow \begin{cases} r \uparrow \Rightarrow c \downarrow \\ \Delta M \downarrow \end{cases} \\ D \uparrow \end{cases}$$

MF: $D = 0$

$$G \uparrow \Rightarrow \begin{cases} y \uparrow \Rightarrow \tilde{y} \uparrow \Rightarrow \pi \uparrow \\ \Delta M \uparrow \Rightarrow \begin{cases} c \uparrow \Rightarrow y \uparrow \Rightarrow \tilde{y} \uparrow \Rightarrow \pi \uparrow \\ i \downarrow \Rightarrow r \downarrow \Rightarrow c \uparrow \end{cases} \end{cases}$$

Fig. 2. Dynamic Effects of an Increase in Government Purchases: Debt vs. Money Financing

6.2. comparsion

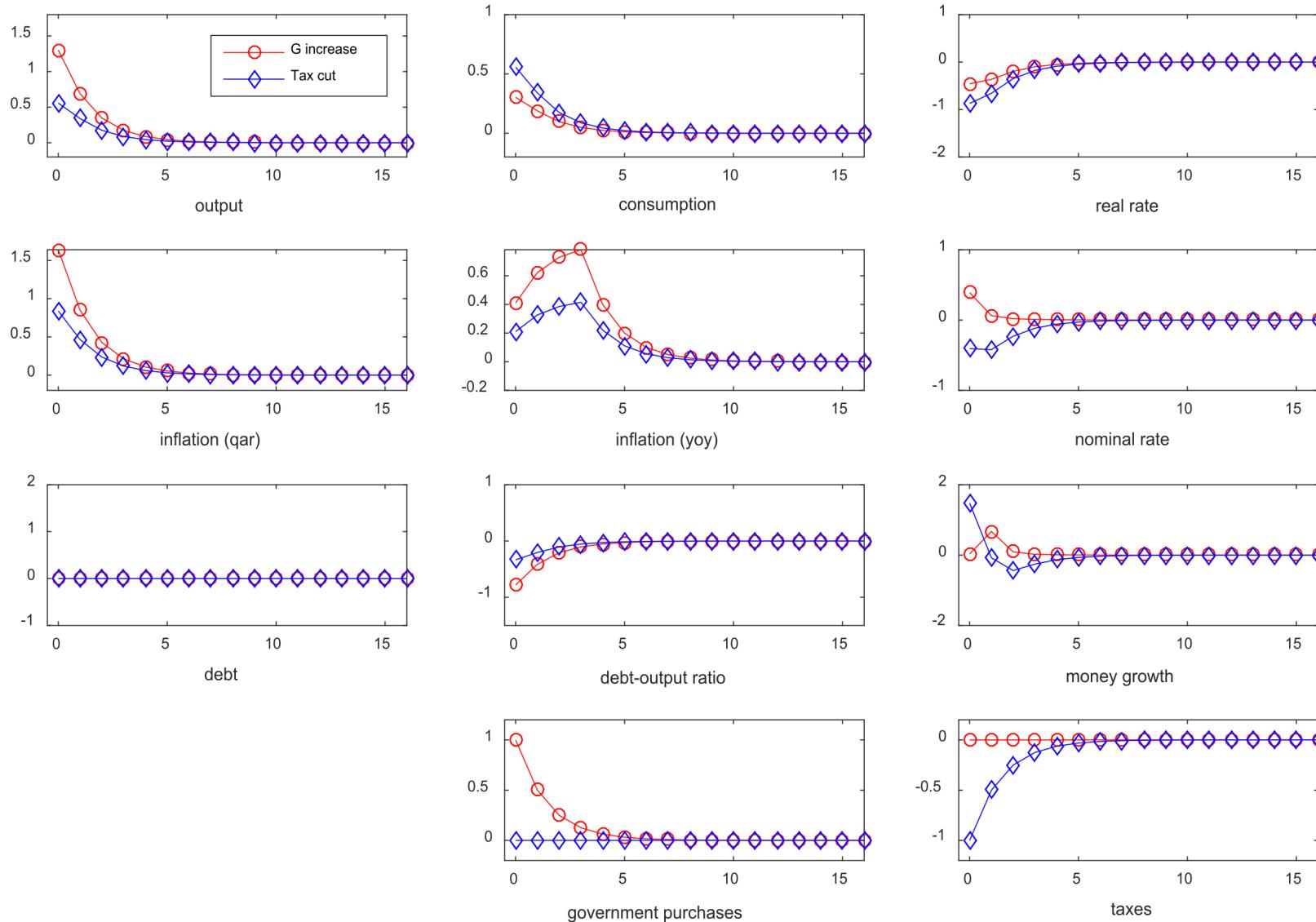


Fig. 3. Dynamic Effects of Money-Financed Fiscal Stimuli: Tax cut vs. Increase in Government Purchases

6.3. Sensitivity analysis

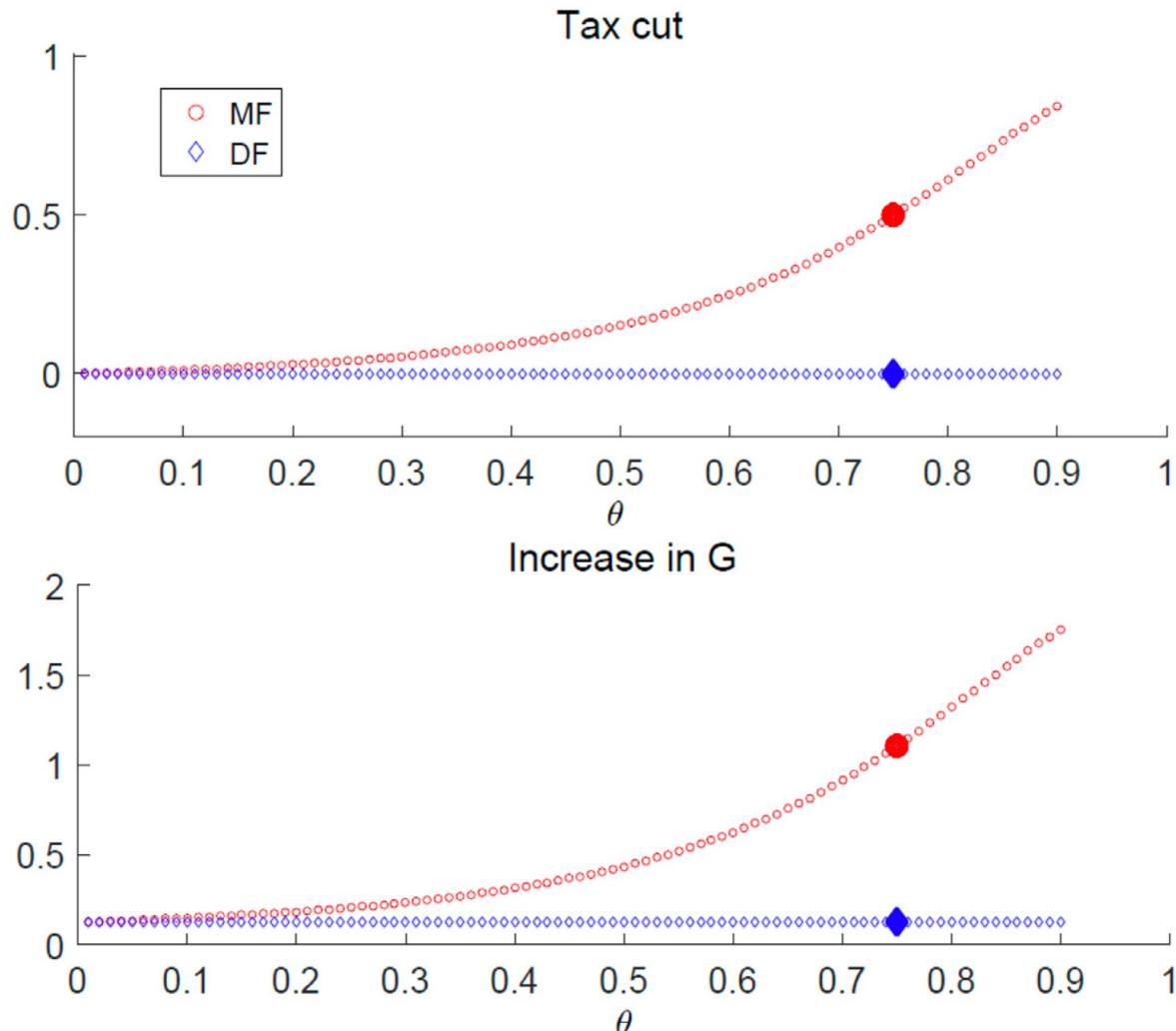


Fig. 4. Fiscal Multipliers: The Role of Price Stickiness

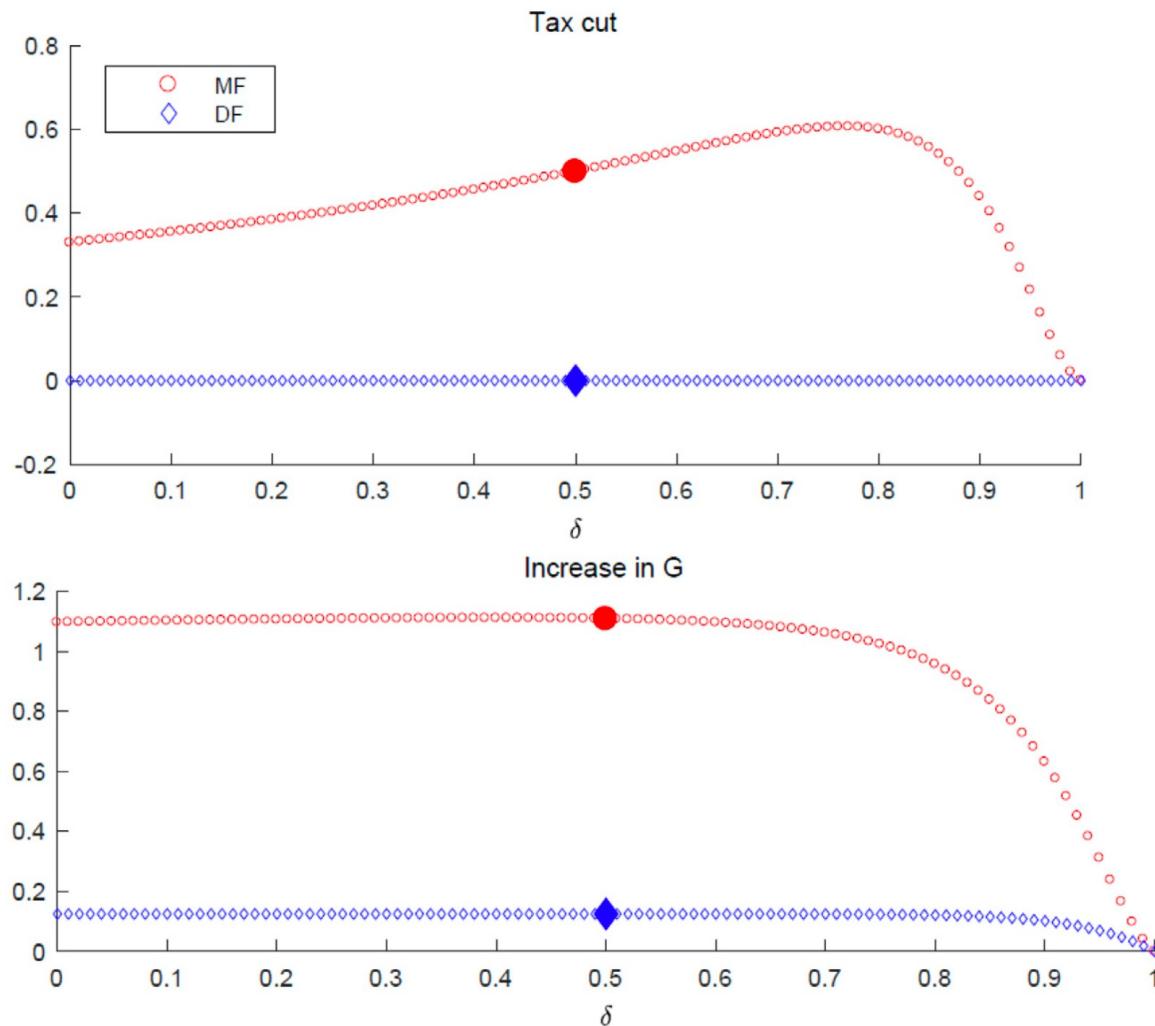
- 在一种完全竞争与灵活价格经济中，货币融资的财政刺激对产出和就业的影响非常小，但是对通胀则有巨大影响，私人消费会下降。另一方面，由于通胀导致的债务实际价值缩水而使得债务比率下降。

- 因此，在这种“古典”经济环境下，货币融资的财政刺激计划并没有什么吸引力。

- 当经济处在不完全竞争、粘性工资和价格环境下，货币融资的财政刺激计划则对经济活动具有强烈的作用，而对通胀的影响则相对温和。

- 这是因为由于更高的通胀预期，使得利率持续降低，从而导致了私人消费的挤入效应。
- 由于更低的利率，债务-GDP比率也会随着时间而下降；
- 如果产出低于其有效水平太多，即使政府支出是一种纯浪费，货币融资的财政刺激也可以提高福利。

6.3. Sensitivity analysis



that money-financed fiscal stimuli are **more effective than** their debt-financed counterparts, and that the output multipliers for a money-financed increase in government purchases **are larger than** that of a money-financed tax cut.

Fig. 5. Fiscal Multipliers: The Role of Shock Persistence

7. The effects of a money-Financed fiscal stimulus in a liquidity trap

- The ZLB constraint can be incorporated formally in the set of equilibrium conditions above by replacing (20) with the complementarity slackness condition:

$$(\hat{i}_t - \log \beta)(\hat{l}_t - \hat{c}_t + \eta \hat{i}_t) = 0$$

for all t , where $\hat{i}_t \geq \log \beta$ is the ZLB constraint and $\hat{l}_t \geq \hat{c}_t - \eta \hat{i}_t$ represents the demand for real balances.

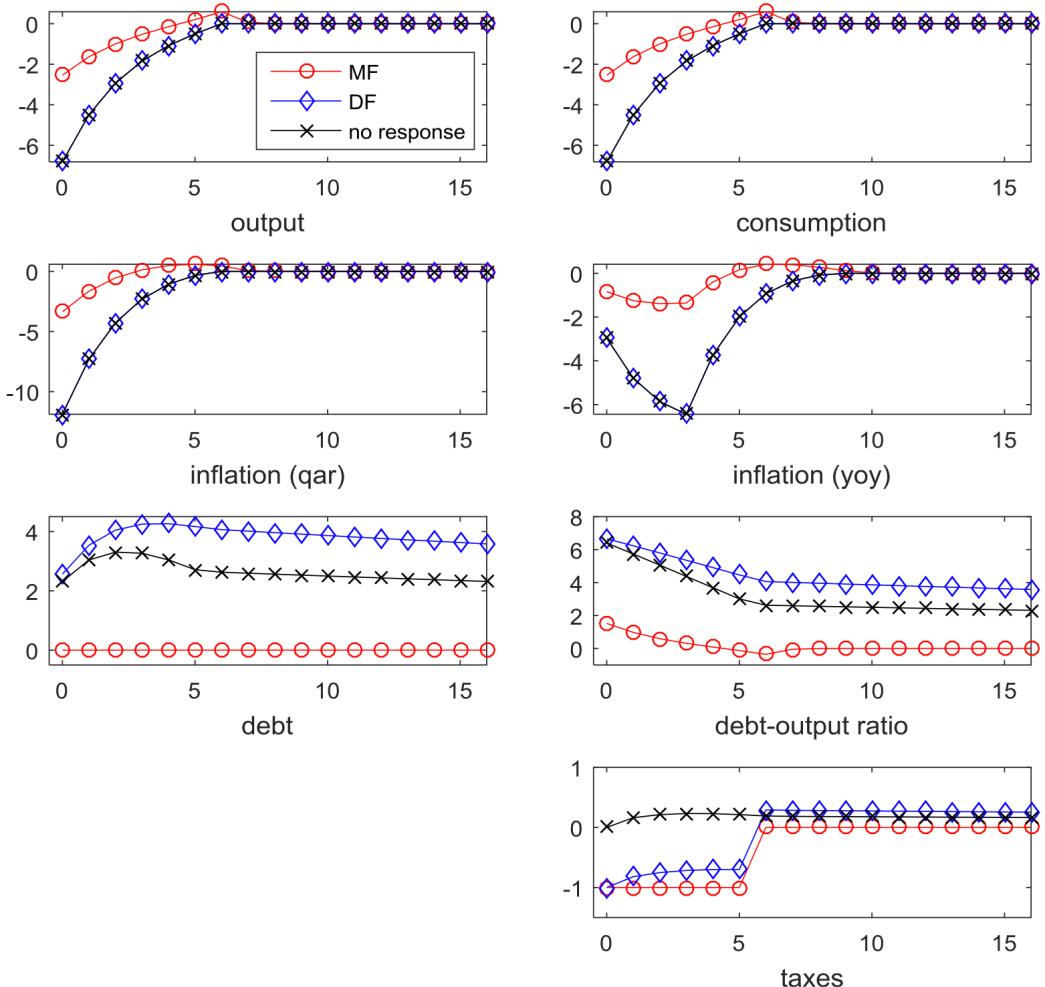
- In the case of debt-financed fiscal stimulus(replace(24))

$$(\hat{i}_t - \log \beta)\pi_t = 0$$

for all t , together with

$$\pi_t = 0$$

7. The effects of a money-Financed fiscal stimulus in a liquidity trap



Z shock:

$$Z \downarrow \Rightarrow \begin{cases} c \downarrow \Rightarrow y \downarrow \\ r^n \downarrow \Rightarrow \tilde{y} \downarrow \Rightarrow \begin{cases} y \downarrow \\ \pi \downarrow (i=0) \Rightarrow r \uparrow \Rightarrow \Delta M \downarrow \end{cases} \end{cases}$$

DF: $\pi = 0$

$\text{tax } \downarrow \Rightarrow D \uparrow$ 无效

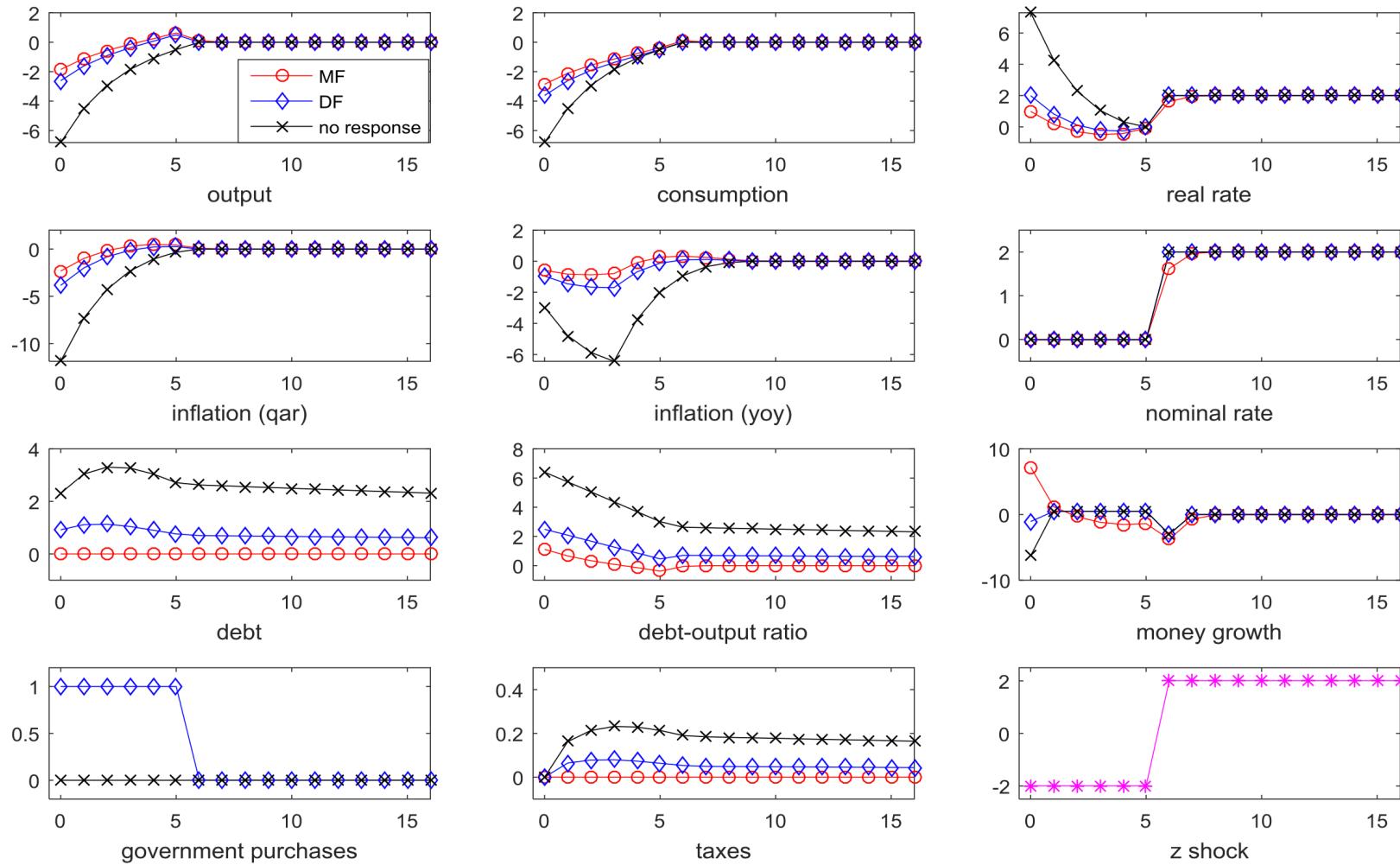
MF: $D = 0$

$\text{tax } \downarrow \Rightarrow \Delta M \uparrow \Rightarrow y \uparrow (i=0) \Rightarrow \tilde{y} \uparrow \Rightarrow \pi \uparrow$
 $\Rightarrow r \downarrow (i=0) \Rightarrow c \uparrow$

有效

Fig. 6. Dynamic Effects of a Tax Cut in a Liquidity Trap

7. The effects of a money-Financed fiscal stimulus in a liquidity trap



Z shock:

$$Z \downarrow \Rightarrow \begin{cases} c \downarrow \Rightarrow y \downarrow \\ r^n \downarrow \Rightarrow \tilde{y} \downarrow \Rightarrow \begin{cases} y \downarrow \\ \pi \downarrow (i=0) \Rightarrow r \uparrow \Rightarrow \Delta M \downarrow \end{cases} \\ \text{tax} \uparrow \end{cases}$$

DF: $\pi = 0$

$$G \uparrow \Rightarrow \begin{cases} y \uparrow \Rightarrow \tilde{y} \uparrow \Rightarrow \pi \uparrow \Rightarrow r \downarrow (i=0) \Rightarrow \Delta M \uparrow \\ D \uparrow \end{cases}$$

MF: $D = 0$

$$G \uparrow \Rightarrow \begin{cases} y \uparrow \Rightarrow \tilde{y} \uparrow \Rightarrow \pi \uparrow \Rightarrow r \downarrow (i=0) \Rightarrow \Delta M \uparrow \\ \Delta M \uparrow \end{cases}$$

Fig. 7. Dynamic Effects of an Increase in Government Purchases in a Liquidity Trap

7.comparison

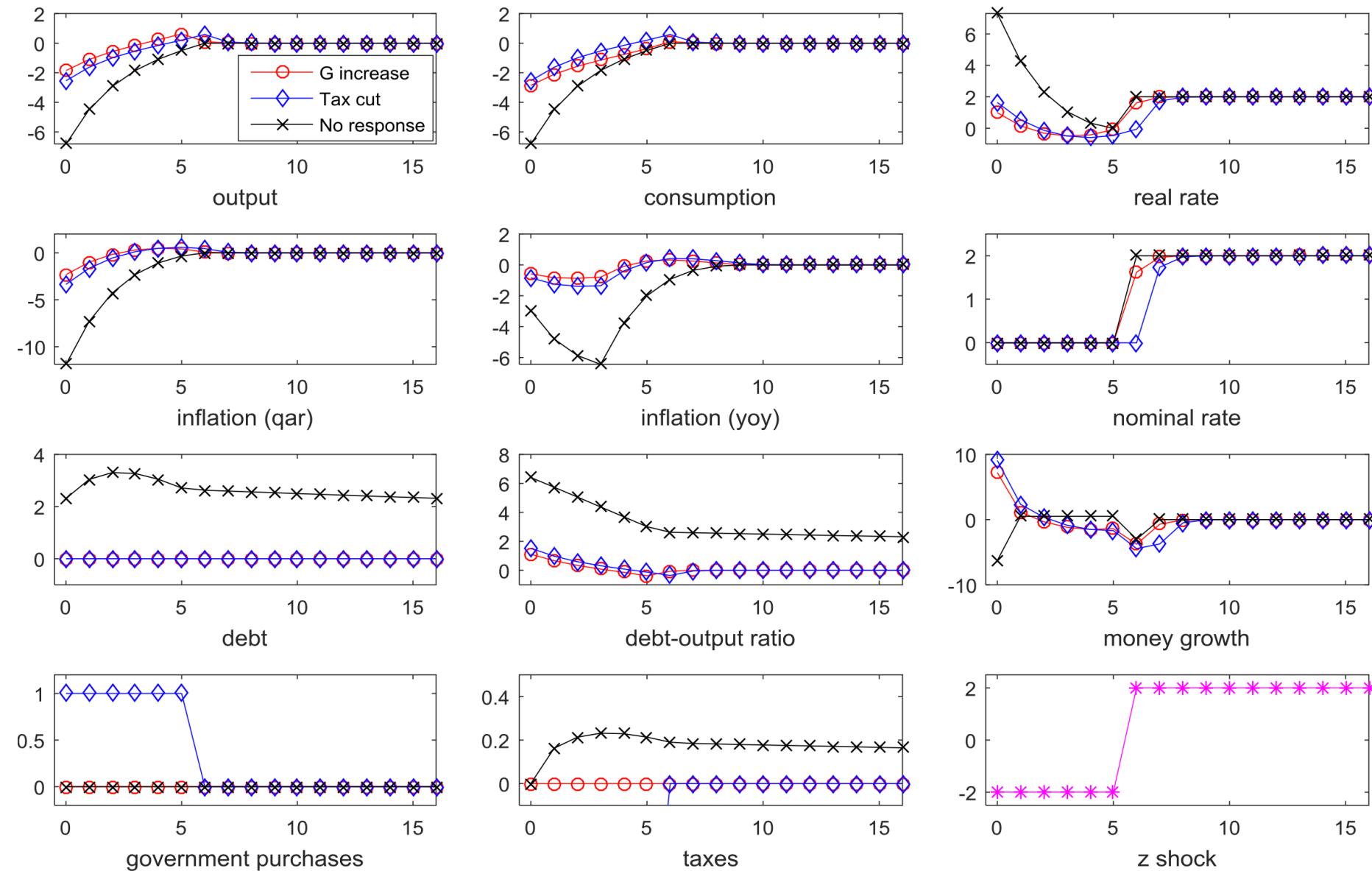


Fig. 8. Dynamic Effects of Money-Financed Fiscal Stimuli in a Liquidity Trap

8. Concluding remarks

- The effects of a **money-financed fiscal stimulus** vs **conventional debt-financed stimulus**.
- A number of results from that analysis are worth stressing.
 - a money-financed fiscal stimulus, in the form of a **tax cut or an increase in government purchases**, provides a way to **boost economic activity effectively**, as long as prices are reasonably sticky.
 - money-financed fiscal stimuli appear to be **more effective** than their debt-financed counterparts.
 - a money-financed increase in government purchases has a **larger output multiplier** than a money-financed tax cut.
 - money-financed tax cuts also appear to be **more effective countercyclical policies** than their debt-financed counterparts when the ZLB is binding
- A number of issues that are beyond the scope of the present paper.
 - the fact that monetary policy is (at least temporarily) driven by the requirements of the fiscal authority may be perceived as an outright violation of the principle of **central bank independence**
 - would likely be a source of an **inflation bias** and bring about changes in individual behavior likely to under-mine their effectiveness (e.g. **indexation or greater price flexibility**).

Thanks!