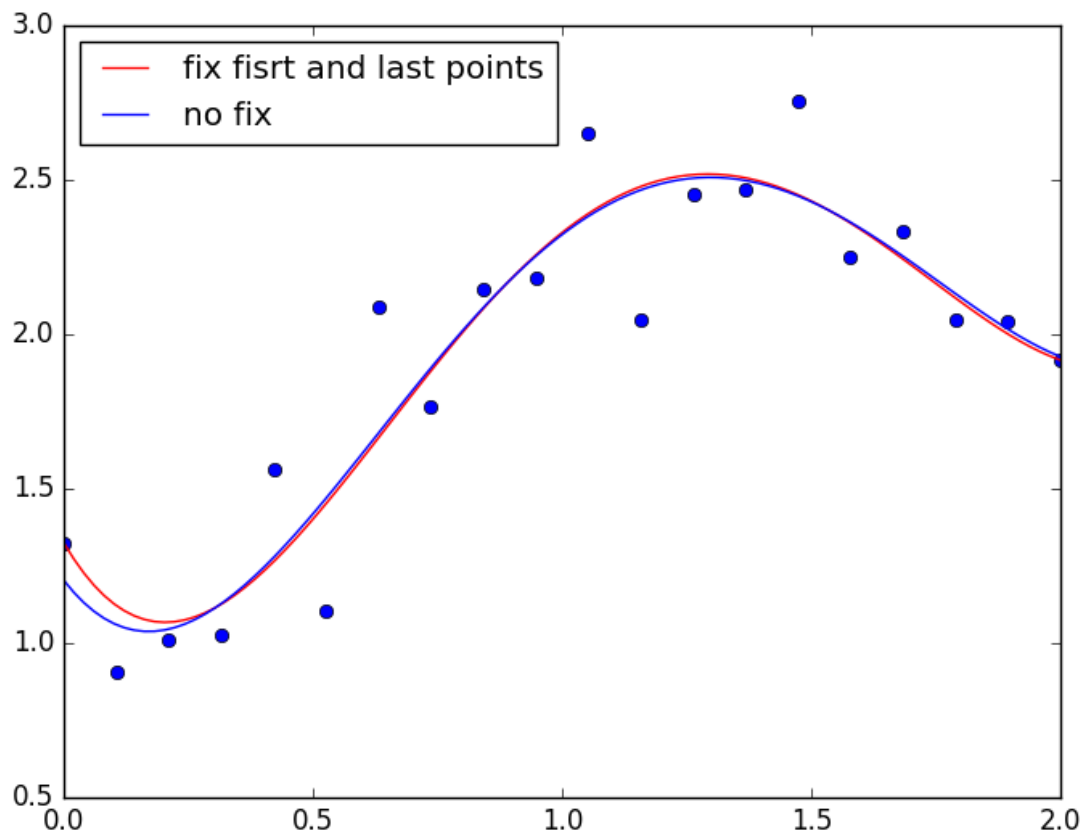


## 1. Frist Method (Least-Squares of different weight):



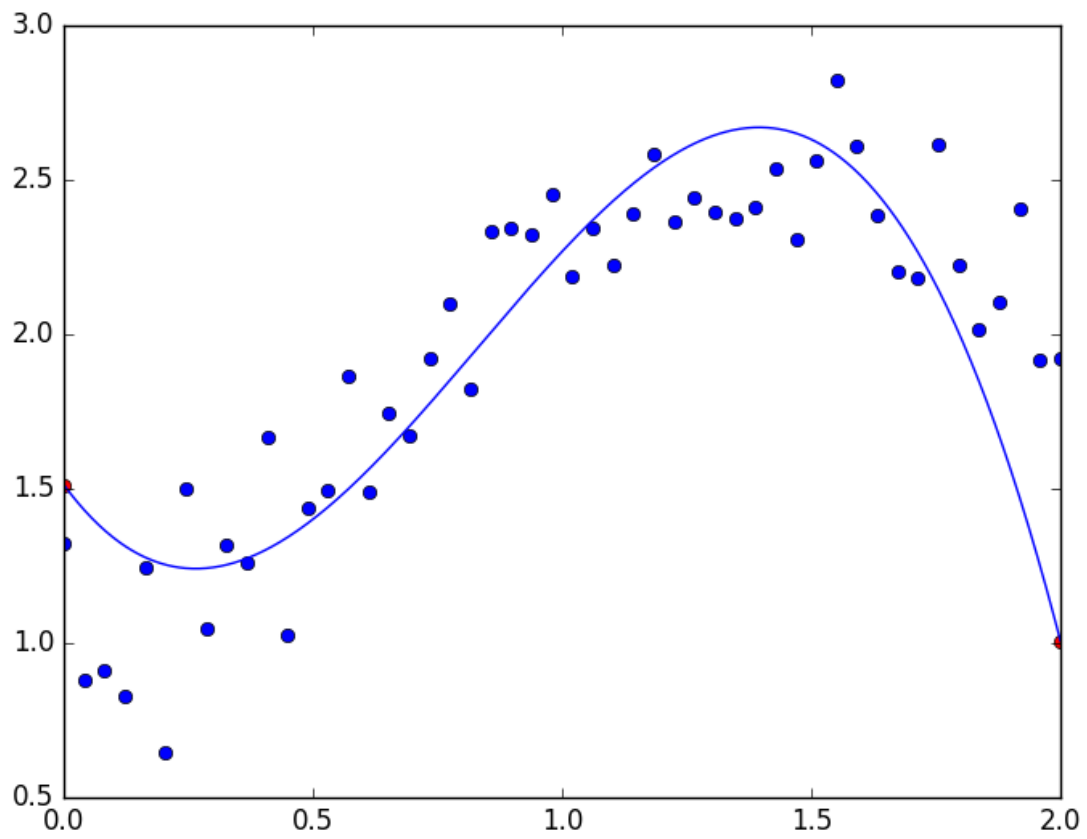
### Gaps between true postions and estimated positions:

```
[-1.70151737e-09  2.13200659e-01  5.82894199e-02  1.01063834e-01  
-3.01783237e-01  3.49270969e-01 -4.24853965e-01  1.16438435e-01  
-6.42954705e-02  7.30313001e-02 -2.61367118e-01  4.33974843e-01  
 6.18798111e-02  3.85966324e-02 -3.04436898e-01  1.08990259e-01  
-9.08017694e-02  7.06520371e-02 -3.98460040e-02  3.21449978e-10]
```

We can give the first and the last point a very little weight to make them infinitely close to the true value, but it's not certainly to be exact. It depends on the tolerance we can have.

## 2. Second Method ( Lagrange Multipliers with equation constraint )

In theory, the equation is strictly solved. However, in computer science, it's rarely true.



**Gaps between true postions and estimated positions(first and last):**

(-1.3322676295501878e-15, 3.7747582837255322e-15)

This method is not until well implemented.