

Question #1 of 15

Question ID: 439395

Which of the following is **NOT** one of the assumptions of the Black-Scholes-Merton (BSM) option-pricing model?

- ✓ **A) Any dividends are paid at a continuously compounded rate.**
- ✗ B) Options valued are European style.
- ✗ C) There are no taxes.
- ✗ D) There are no transaction costs.

Explanation

The BSM model assumes there are no cash flows on the underlying asset.

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Question ID: 439401

Consider a 145-day put option at 30 on a stock selling at 27 with an annualized standard deviation of 0.30 when the continuously compounded risk-free rate is 4 percent. The value of the put option is *closest* to: [round d1 and d2 rather than interpolate for N(.)].

$$P_T = [Xe^{-r(T)} \times (1 - N(d_2))] - [S_T \times (1 - N(d_1))]$$

where:

$$d_1 = [\ln(S_t / X) + [r + \sigma^2/2](T)] / \sigma \sqrt{(T-t)}$$

$$d_2 = d_1 - \sigma \sqrt{(T)}$$

Cumulative Standard Normal Probability:

| | 0.06 | 0.07 | 0.08 | 0.09 |
|-----|--------|--------|--------|--------|
| 0.3 | 0.6406 | 0.6443 | 0.6480 | 0.6517 |
| 0.4 | 0.6772 | 0.6808 | 0.6844 | 0.6879 |
| 0.5 | 0.7123 | 0.7157 | 0.7190 | 0.7224 |

- ✗ A) \$3.97.
- ✗ B) \$4.07.
- ✓ C) \$3.64.
- ✗ D) \$3.32.

Explanation

$$T = 145/365 = 0.39726$$

$$d_1 = [\ln(27/30) + [.04 + .3^2/2](.39726)] / (.3\sqrt{.39726})$$

$$\begin{aligned}
 &= (-.10536052 + .0337671) / .18908569 \\
 &= -.07159342 / .18908569 \\
 &= -0.37863 \\
 d_1 &= -0.37863 \approx -0.38 \quad N(d_1) = 1 - 0.6480 = 0.3520
 \end{aligned}$$

$$\begin{aligned}
 d_2 &= -0.37863 - .3\sqrt{.39726} \\
 &= -0.37863 - .18908569 \\
 &= -.56771569 \\
 &= -.56772 \\
 d_2 &= -0.56772 \approx -0.57 \quad N(d_2) = 1 - 0.7157 = 0.2843
 \end{aligned}$$

$$\begin{aligned}
 P_T &= 30e^{-.04(.39726)} (1 - .2843) - 27(1 - .352) \\
 &= (29.527056 \times .7157) - 17.496 \\
 &= 21.1325 - 17.496 \\
 p &= \$3.64
 \end{aligned}$$

Question #3 of 15

Question ID: 439399

Using the Black-Scholes model, compute the value of a European call option using the following inputs:

Underlying stock price: \$100
 Exercise price: \$90
 Risk-free interest rate: 5%
 Volatility: 20%
 Dividend yield: 0%
 Time to expiration: one year

The Black-Scholes call option price is *closest* to:

- ☒ A) \$13.65.
- ☐ B) \$17.99.
- ☒ C) \$16.71.
- ☐ D) \$15.33.

Explanation

This value is obtained using the Black-Scholes model for call option without dividends:

So $d_1 = (\ln(100/90) + (0.05 + 0.20^2/2)) / 0.2\sqrt{1} = 0.8768$ and using the table, $N(0.88) = 0.8106$. $d_2 = 0.8768 - 0.2\sqrt{1} = 0.6768$, so from the table, $N(d_2) = N(0.68) = 0.7517$.

So the call value is $100(0.8106) - 90e^{(-0.05)}(0.7517) = \16.71 .

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Question ID: 439404

Which of the following methods is **NOT** used for estimating volatility inputs for the Black-Scholes model?

- ☐ A) Using exponentially weighted historical data.
- ☒ B) Models of changing volatility.

- X **C)** Using the most current historical data.
- X **D)** Using long term historical data.

Explanation

The volatility is constant in the Black-Scholes model.

Question #5 of 15

Question ID: 439396

Which of the following is **NOT** one of the assumptions of the Black-Scholes-Merton option-pricing model?

- ✓ **A) The yield curve for risk-free assets is fixed over the term of the option.**
- X **B)** There are no taxes and transactions costs are zero for options and arbitrage portfolios.
- X **C)** There are no cash flows over the term of the options.
- X **D)** The volatility is known and remains constant over the term of the option.

Explanation

The yield curve is assumed to be flat so that the risk-free rate of interest is known and *constant* over the term of the option. Having a fixed yield curve does not necessarily imply that the yield curve is flat.

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Question ID: 439408

Dividends on a stock can be incorporated into the valuation model of an option on the stock by:

- X **A) subtracting the future value of the dividend from the current stock price.**
- X **B)** adding the future value of the dividend to the option value.
- X **C)** adding the present value of the dividend to the current stock price.
- ✓ **D)** subtracting the present value of the dividend from the current stock price.

Explanation

The option pricing formulas can be adjusted for dividends by subtracting the present value of the expected dividend(s) from the current asset price.

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Question ID: 439406

Which of the following is **TRUE** for an option's price? An option's price is:

- ✓ **A) an increasing function of the underlying asset's volatility.**
- X **B)** a decreasing function of the underlying asset's volatility.
- X **C)** unaffected by changes in the underlying asset's volatility.
- X **D)** a decreasing function of the underlying asset's volatility when it has a long time remaining until expiration and an increasing function of its volatility if the option is close to expiration.

Explanation

Since an option has limited risk but significant upside potential, its value always increases when the volatility of the underlying asset

increases.

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Question ID: 439407

Compared to the value of a call option on a stock with no dividends, a call option on an identical stock expected to pay a dividend during the term of the option will have a:

- ✓ **A) lower value in all cases.**
- X B) higher value in all cases.
- X C) lower value only if it is an American style option.
- X D) higher value only if it is an American style option.

Explanation

An expected dividend during the term of an option will decrease the value of a call option.

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Question ID: 439405

The implied volatility of interest rates can be *best* computed using the market price of an:

- X A) interest rate futures contract.
- ✓ B) interest rate call option contract.
- X C) S&P 500 option contract.
- X D) interest rate forward contract.

Explanation

Implied volatility of interest rates can be best computed using interest rate option contracts. Forward or futures contract pricing models do not have interest rate volatility as an input. S&P 500 option contracts have the volatility of the S&P 500 index (and not interest rates) as an input.

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Question ID: 439402

Consider a 120-day call option at 28 on a stock selling at 30 with an annualized standard deviation of 0.20 when the continuously compounded risk-free rate is 7 percent. The value of the call is closest to: [round d1 and d2 rather than interpolate for N(.)]

$$C_T = [S_T \times N(d_1)] - [Xe^{-rT}N(d_2)]$$

where:

$$d_1 = \ln(S_T / X) + [r + \sigma^2/2]T / \sigma \sqrt{T}$$

$$d_2 = d_1 - \sigma \sqrt{T}$$

Figure 1: Cumulative Standard Normal Probability

| | | | | |
|--|------|------|------|------|
| | 0.03 | 0.04 | 0.05 | 0.06 |
|--|------|------|------|------|

| | | | | |
|-----|--------|--------|--------|--------|
| 0.6 | 0.7357 | 0.7389 | 0.7422 | 0.7454 |
| 0.7 | 0.7673 | 0.7704 | 0.7734 | 0.7764 |
| 0.8 | 0.7967 | 0.7995 | 0.8023 | 0.8051 |

✓ **A) \$3.07.**

✗ **B) \$3.02.**

✗ **C) \$3.33.**

✗ **D) \$3.12.**

Explanation

$$T=120/365 = 0.328767$$

$$d_1 = 0.8596 \approx 0.86 \quad N(d_1) = 0.8051$$

$$d_2 = 0.7449 \approx 0.74 \quad N(d_2) = 0.7704$$

$$c = \$3.07$$

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Question ID: 439403

If we use four of the inputs into the Black-Scholes-Merton option-pricing model and solve for the asset price volatility that will make the model price equal to the market price of the option, we have found the:

✗ **A) market volatility.**

✗ **B) option volatility.**

✓ **C) implied volatility.**

✗ **D) historical volatility.**

Explanation

The question describes the process for finding the expected volatility implied by the market price of the option.

Question #12 of 15

Question ID: 439398

Using the Black-Scholes model compute the value of a European put option using the following inputs:

- Underlying stock price: \$90
- Exercise price: \$90
- Risk-free interest rate: 5%
- Volatility: 20%
- Dividend yield: 0%
- Time to expiration: one year

The Black-Scholes put option price is *closest* to:

- X A) \$6.12.
- X B) \$4.11.
- ✓ C) \$5.01.
- X D) \$5.89.

Explanation

It is found as follows:

$$\text{Put Price} = Xe^{-rt} * [1 - N(d_2)] - S * [1 - N(d_1)]$$

Where $d_1 = (\ln(90/90) + (.05 + .04/2)1) / .2\sqrt{1} = .35$ and using the Normal Z table, $1 - N(.35) = 1 - .6368 = .3632$.

$d_2 = .35 - .2\sqrt{1} = .15$, and using the Normal Z table, $1 - N(.15) = 1 - .5596 = .4404$.

So the put value = $90e^{(-.05*1)}(.4404) - 90(.3632) = \5.01

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Question ID: 439400

The current price of a stock is \$55. A put option with a \$50 strike price that expires in 3 months is available. If $N(d_1) = 0.8133$, $N(d_2) = 0.7779$, the underlying stock exhibits an annual standard deviation of 25 percent, and current risk free rates are 3.25 percent, the Black-Scholes value of the put is *closest* to:

- X A) \$5.00.
- ✓ B) \$0.75.
- X C) \$1.50.
- X D) \$1.25.

Explanation

This question is not as straight-forward as it looks because $N(d_1)$ and $N(d_2)$ are given instead of $N(-d_1)$ and $N(-d_2)$ which are needed to solve for the price of a put.

$$N(-d_1) = 1 - 0.8133 = 0.1867; N(-d_2) = 1 - 0.7779 = 0.2221$$

The Black-Scholes formula for pricing a put is $P = Xe^{(-rT)} N(-d_2) - S_0 N(-d_1)$

$$P = (\$50e^{(-0.0325*0.25)} * 0.2221) - (\$55 * 0.1867) = \$0.75$$

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Question ID: 439397

Which of the following is *least likely* one of the assumptions of the Black-Scholes-Merton option pricing model?

- ✓ A) Changes in volatility are known and predictable.
- X B) The risk-free rate of interest is known and does not change over the term of the option.
- X C) The options are European style.
- X D) There are no cash flows on the underlying asset.

Explanation

The BSM model assumes that volatility is known and *constant*. The term predictable would allow for non-constant changes in

volatility.

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Question ID: 439409

The value of a put option will be higher if, all else equal, the:

- ☐ A) underlying asset has less volatility.
- ☐ B) exercise price is lower.
- ☒ C) underlying asset has positive cash flows.
- ☐ D) stock price is higher.

Explanation

Positive cash flows in the form of dividends will lower the price of the stock making it closer to being "in the money" which increases the value of the option as the stock price gets closer to the strike price.