

**Spring 2026: Mathematical Statistics****Recitation 2 Problems**

Feb. 6, 2026

1. [4.74] The number of offspring of an organism is a discrete random variable with mean  $\mu$  and variance  $\sigma^2$ . Each of its offspring reproduces in the same manner. Find the expectation and variance of the number of offspring in the third generation.
2. [5.18] Suppose that a company ships packages that are variable in weight, with an average weight of 15 lb and a standard deviation of 10 lb. Assuming that the packages come from a large number of different customers so that it is reasonable to model their weights as independent random variables, find the probability that 100 packages will have a total weight exceeding 1700 lb.
3. Find the mean and variance of  $X \sim \text{Gamma}(\alpha, \lambda)$  in terms of  $\alpha$  and  $\lambda$ .
  - (a) Find the moment generating function of the gamma distribution.  
[Hint: No need to compute complicated integrals here. Recall that the pdf of the gamma distribution integrates to 1.]
  - (b) Find the mean and variance of  $X$ .
4. Show that if  $X_i$  are independent, identically distributed exponential random variables,  $X_i \sim \text{Exp}(\lambda)$ , then

$$Y_i = \sum_{i=1}^n X_i \sim \text{Gamma}(n, \lambda).$$