



Mahakal Institute of Technology, Ujjain

Department of Mathematics

PYQ's Unit -V

Q.N.	Question	Marks	RBT Level	CO
Q1	Verify Gauss Divergence theorem for $F = x^3i + y^3j + z^3k$ taken over the cube bounded by $x=0, x=a, y=0, y=a, z=0, z=a$. dec2023			
Q2	Using Green's theorem, Find the area of the region in the first quadrant bounded by the curve $Y=X, Y=1/X, Y=x/4$. June 2023			
Q3	Find the directional derivative of $f(x,y,z) = e^{2x} \cos yz$ at $(0,0,0)$ in the direction of the tangent to the curve $x = a \sin t, y = a \cos t, z = at$ at $t = \pi/4$. June 2023			
Q4	Show that the vector $(x^2-yz)i + (y^2-zx)j + (z^2-xy)k$ is irrotational. Find its scalar potential. NOV 2022			
Q5	Verify Green's theorem for $\int [3x^2 - 8y^2] dx + [4y-6xy] dy$. Where C is the region bounded by $x=0, y=0$ and $x+y=1$. NOV2022			
Q.6	Verify Gauss Divergence theorem for $F = x^2i + y^2j + z^2k$ over the cube bounded by the planes $x=0, x=a, y=0, y=b, z=0, z=c$. june2022.			
Q.7	Prove that $r^n r$ is solenoidal if $n=-3$. June 2022			
Q.8	Find the angle between the surfaces $x^2+y^2+z^2=9$ and $z=x^2+y^2-3$ at the point $(2,-1,2)$. June 2022			
Q.9	Find $\text{div}(\text{curl } F)$ where $F = x^2yi + xzj + 2yzk$. June 2020, NOV2019			
Q.10	Using Gauss's divergence theorem, Find $\iiint_C F \cdot n \, ds$ where $F = (2x+3z)i - (xz+y)j + (y^2+2z)k$ and S is the surface of sphere with center $(3,-1,2)$ and radius 3. Nov2019			
Q.11	If $F = 3xyi - y^2j$, evaluate $\int_C F \cdot dr$, where C is the arc of the parabola $y=2x^2$ from $(0,0)$ to $(1,2)$.			
Q.12	Evaluate $\iint_S A \cdot n \, ds$, where $A = (x+y^2)i - 2xj + 2yzk$ and S is the surface of plane $2x+y+2z=6$ in the first octant. may2019			

Q13	Solve $\int_0^{1+i} (x - y + ix^2) dz$ along the real axis from $z=0$ to $z=1$ and then along a line parallel to imaginary axis from $z=1$ to $z=1+i$. june 2023		
Q14	Prove that $\Delta^2 f(r) = f''(r) + \frac{2}{r} f'(r)$ june 2023		
Q15	Prove that $\text{curl} (r^n r) = 0$ Dec 2023		
Q16	Write short note on: 1. Stokes theorem. Dec 2023		