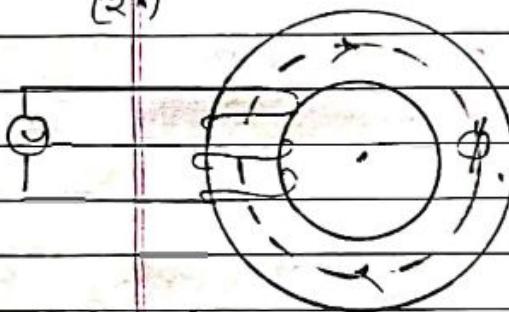


Transformer :- Magnetic circuit

### Magnetic circuit

- (i) It is a closed Path followed by magnetic flux in the magnetic material

(2)

Excitation :-

MMF (magneto motor  
magnetic force)

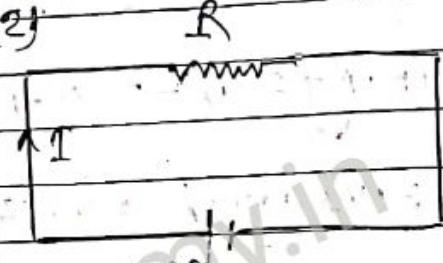
unit :- mmf = NI

Ampere turns (AT)

### Electric circuit

It is the closed path followed by electric current in the electric conductor

(2)

Excitation :-

EMFC (Electric  
motive force)

$$v = IR$$

unit :- volt

Response :- flux

$$\phi = mmf$$

$\delta$  (Resistance)

unit  $\phi$  :- Weber (wb)

Resistance

It opposes the flow of magnetic flux in the magnetic circuit

$$SF \text{ mmf}$$

$$\phi \cdot \text{unit} : AT/\text{wb}$$

Response :- Current

$$I = V/R$$

unit : Ampere

Resistance

It opposes the flow of electric current.  $R = V/I$ ,  
unit : ohm

series combination in magnetic circuit :-

$$\mu_{eq} = S_1 T S_2 T S_3 T \dots T S_n$$

Parallel combination

$$I = \frac{1}{S_1} + \frac{1}{S_2} + \frac{1}{S_3} + \dots + \frac{1}{S_n}$$

Premiance :-

$$P = \frac{1}{S}$$

unit : wb/AT

defn: it is the easyness to flow of magnetic flux in magnetic circuit, or in other words inverse of Reluctance

Reluctivity

$$S = \frac{1}{\mu L}$$

$\frac{1}{\mu L}$  = Reluctivity

$\mu$  = Permeability

Magnetic field intensity.

$$H = \frac{F}{L}$$

length.

unit = AT/m

series combination in electric circuit :-

$$R_{eq} = R_1 + R_2 + R_3 + \dots + R_n$$

Parallel combination :-

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots + \frac{1}{R_n}$$

conductance :-

$$G = \frac{1}{R}$$

unit = S

it is the easyness to flow of electric current in the electric circuit and inverse of Resistance

Resistivity :-

$$R = \rho l / A$$

$$\rho = R A / l$$

$\rightarrow$  Resistivity

Electric field intensity  $E$

$$E = V/L$$

unit = volt/meter

## (M.Q2.) Difference b/w electric circuit and magnetic circuit

### Air Magnetic circuit

### Electric circuit

(1) Flux is assumed to flow in magnetic circuit. It is an imaginary quantity.

(1) Electric current actually flows in the circuit. It is a real quantity.

(2.) There is no insulator available in case of magnetic circuit.

2) Various types of insulator available in case of electric circuit.

(3.) Flux can pass through the air.

(3.) Electric current can not pass through the air.

(4.) MMF is required only to generate magnetic flux in the magnetic circuit. It is not required to maintain magnetic flux.

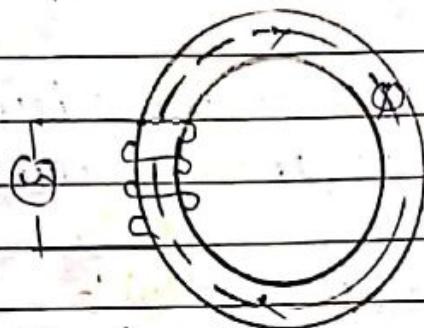
(4.) EMF is required for both generating and maintaining electric current in the electric circuit.

05/02/2019-

## Basic Definitions:-

### (i) Magnetic Circuit:

It is (the closed path followed by magnetic flux in a magnetic material).



### Magnetic flux:-

(i) It is the magnetic lines of forces, acting in a direction, in which magnetic force acts.

$$\phi = N \cdot I \cdot f$$

$S$  (Resistance)

unit  $\phi = \text{Weber (Wb)}$ .

### MMF (magneto motive force):

MMF. It is a force that drives the magnetic flux in a magnetic circuit.

$$\text{mmf} = I \cdot N$$

where  $N = \text{no. of Turns}$

$I = \text{current}$

unit (mmf) = AT i.e. ampere Turns.

$$\text{mmf} = \phi \cdot S$$

$\phi = \text{magnetic flux}$

$S = \text{Resistance}$

$$\text{mmf} = H \cdot L$$

$H \rightarrow \text{field intensity i.e. magnetic field per unit current}$

$L \rightarrow \text{length of magnetic circuit}$

### Permeability :- (H) :-

It is the property of material which measures how much material can conduct magnetic flux.

$$\cdot \mu = \mu_0 \mu_r$$

where,  $\mu_0$  = freespace Permeability

$\mu_r$  = Relative Permeability  
Value of  $\mu_0$ :  $4\pi \times 10^{-7}$

### Magnetic flux density :- (B) :-

It is magnetic flux per unit area.

$$\cdot B = \Phi/A = \text{cwb/m}^2$$

$$\cdot B = \mu H$$

where  $\mu$  = Permeability.

$H$  = magnetic field intensity

### Reluctance :- (S) :-

It is the property of material which opposes the flow of flux in a magnetic circuit.

$$\cdot S = \text{mmf} = A/I$$

$$\Phi = \frac{S}{R}$$

$$\cdot R = \frac{\Phi}{I}$$

$$NAt$$

where  $N$  = Reluctivity

### Magnetic field intensity :- (H)

It is the ratio of magneto motive force (MMF) to the length of magnetic circuit.

$$\cdot H = \text{mmf} = A/I \text{ m-unit}$$

## Permeance ( $P$ ) :-

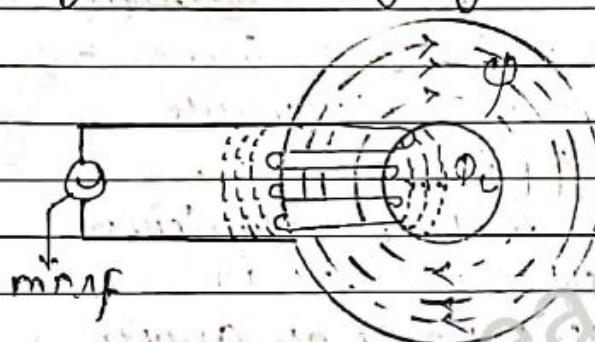
It is the inverse of Reluctance; it can be defined as the easiness provided by the circuit to form the magnetic flux.

$$P = 1/R$$

unit : Vsb.

AT

## leakage flux Arising :-



### Leakage flux ( $\Phi_L$ ) :-

It is the flux which is not linking with the magnetic core and is circulating near the coil.

### useful flux ( $\Phi$ ) :-

It is the flux which is perfectly linking with the magnetic core.

### Total flux ( $\Phi_T$ ) :-

It is the combination of leakage flux and useful flux.

$$\Phi_T = \Phi_L + \Phi$$

The ratio of total flux (flux in the iron path) to magnetic flux to the useful flux is known as leakage factor. 
$$\frac{\text{Total Flux}}{\text{useful flux}}$$

06/02/2019 -

## 1Φ Transformer:-

Faraday's Law of Electromagnetic induction -

(i) whenever magnetic flux linking in a closed circuit changes w.r.t the time an emf is induced e

(ii) the magnitude of induced emf is given by -ve of rate of change of magnetic flux linked with the closed circuit

$$e = -N \frac{d\phi}{dt}$$

N = no. of turns

-ve sign is due to Lenz's law; which states that the direction of induced emf is such that it opposes the cause that produced it.

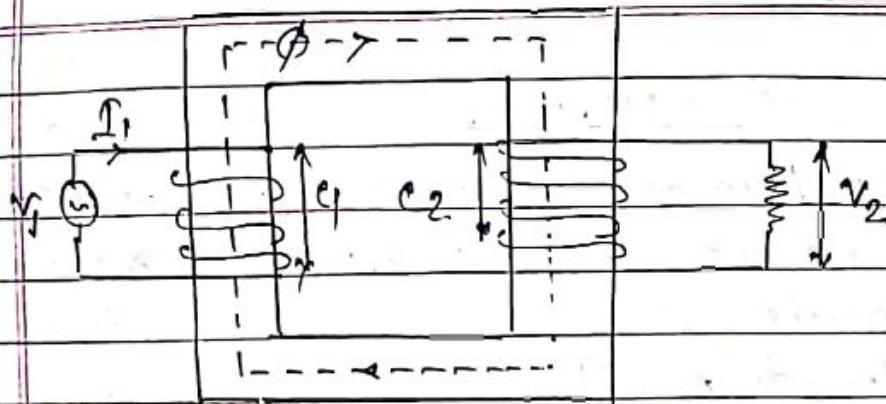
## Transformer :-

It is an ac static device which transforms low voltage, high current to high voltage, low current and vice-versa without changing its frequency.

### Principle :-

The working principle of transformer is based on mutual induction.

The phenomena of generation of induced emf in the secondary coil by changing the current in primary coil known as mutual induction.



$\epsilon_1 \rightarrow$  Self induction.

$\epsilon_2 \rightarrow$  Mutual induction

Operation of transformer is based on Faraday's law of electromagnetic induction.

(i) An alternating voltage  $V_1$  is applied across the primary winding of the transformer which will result in alternating current  $I_1$  flowing through primary winding.

(2.) Flux ( $\Phi$ ) is produced across the primary winding due to primary current  $I_1$ . This flux is also alternating in nature.

(3.) According to Faraday's law of emf, whenever magnetic flux linked with closed circuit is changing w.r.t time an emf is induced. Hence emf  $\epsilon_1$  is induced across primary winding due to self induction.

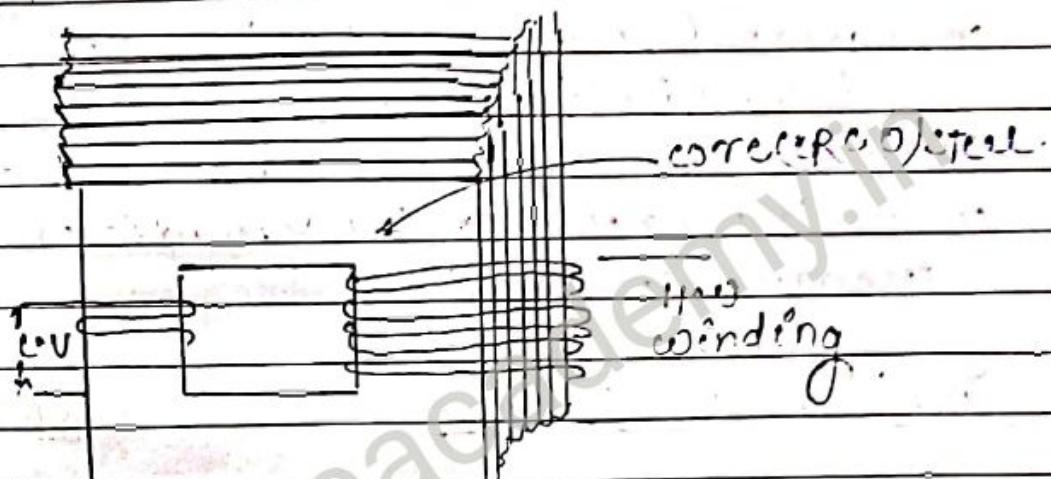
(4.) Since both windings (primary and secondary) are mounted on the same magnetic core, the same flux  $\Phi$  will also link with the secondary winding. Hence emf  $\epsilon_2$  will be induced across secondary winding due to

mutual induction.

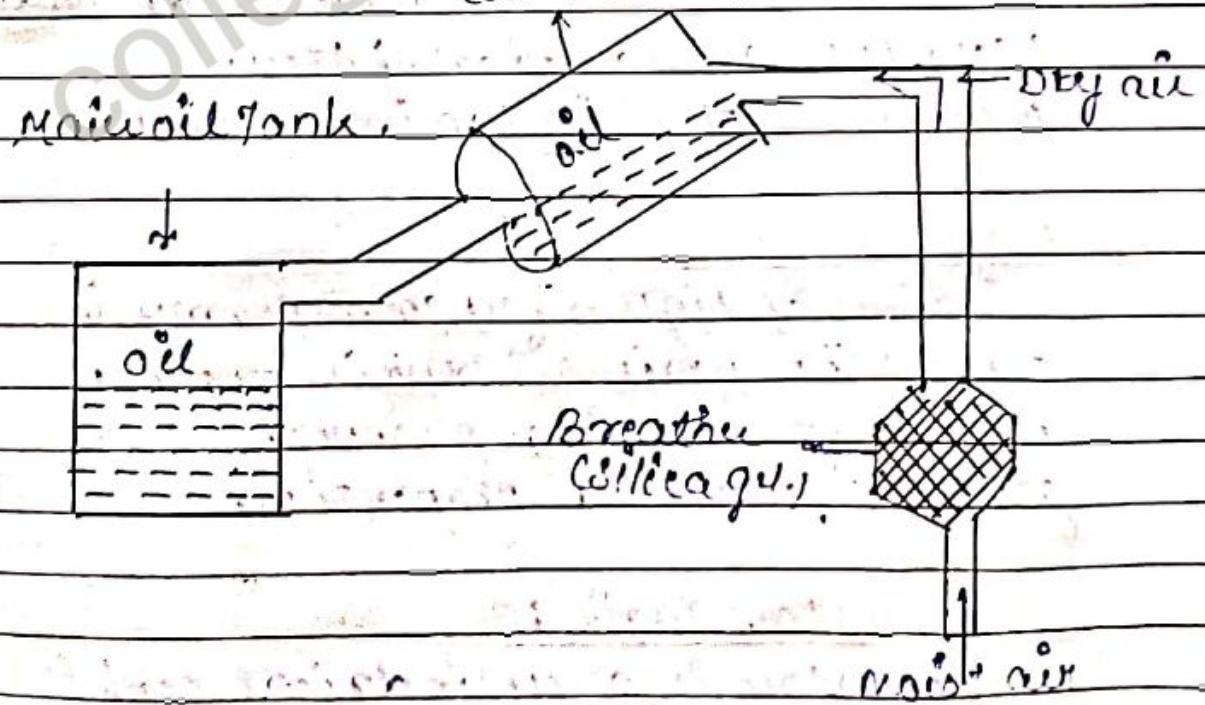
- (5) Current  $I_2$  is produced in the secondary winding due to  $E_2$  which is known as secondary current.

07/02/18

cRACO  $\rightarrow$  (cold rolled grain oriented)



Oil conservator tank.



## Transformer Winding :-

(X-mer)

It forms the electrical circuit for the X-mer generally made up of copper wires, transformer winding is one of two types:-

① High voltage winding

② Low voltage winding

→ These windings have a large no. of turns as compare to low voltage windings.

→ Winding which is connected to the source is known as primary winding and the one which is connected to the load is called secondary winding.

## Transformer core :-

It forms the magnetic circuit for the transformer, it is made up of CRGO (Cold Rolled Grained Oriented Steel).

In the form of thin laminated sheet.

## Main oil tank :-

Windings of high rated transformer is kept in the main oil tank in order to ensure good cooling properties & good insulation properties.

## Conductor tank :-

Conductor is a cylindrical tank attached to the main oil tank and is used to prevent direct contact of moist air with oil in the main oil tank.

During high load operations winding of transformer gets hot & heat up and oil from main oil tank evaporates to the conservator tank.

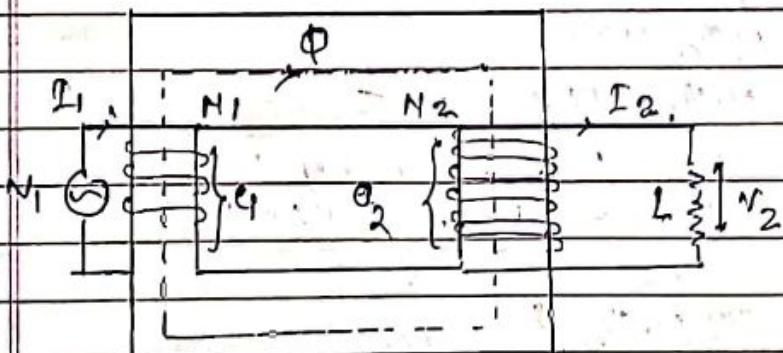
- During low load operation windings of transformer gets cool & then oil from conservator tank refresh back to the main oil tank.

### Breather:-

Breather is attached to conservator tank and it is made up of silica gel. It ensures only dry air goes into the conservator tank during low load operation of transformer.

08/02/19 -

### EMF Equations of Transformer



where  $N_1$  = no. of Turns in primary winding  
 $N_2$  = no. of Turns in secondary winding

$V_1$  = Primary/ source voltage

$V_2$  = Secondary/ load voltage       $e_1$  = induced emf in

$I_1$  = Primary current                  Primary winding

$I_2$  = Secondary current                   $e_2$  = induced emf in

$\Phi$  = Flux                                  Secondary winding

$f$  = frequency

The instantaneous equation of flux is given by

$$\Phi = \Phi_m \sin \omega t \quad (1)$$

The induced emf in the primary winding is given by  $e_1 = -N_1 \frac{d\Phi}{dt}$  (ii)

By putting the value of  $\Phi$  in eqn. (2) :-

$$e_1 = -N_1 \frac{d}{dt} (\Phi_m \sin \omega t)$$

$$e_1 = -N_1 \Phi_m \omega \cos \omega t$$

$$e_1 = -N_1 \Phi_m \omega \sin(\omega t - \pi/2) \quad (iii)$$

$$[\because -\cos \omega t = \sin(\omega t - \pi/2)]$$

By comparing equations (i) & (3) it is clear that emf lags the flux by  $\pi/2$ .

Now comparing equation 3 with instantaneous equation of emf..

$$e = E_{max} \sin \omega t$$

$$E_{max} = N_1 \Phi_m \omega$$

$$E_{max} = N_1 \Phi_m 2\pi f$$

Rms value of emf is given by !

$$E_{rm} = \frac{E_{max}}{\sqrt{2}} = \frac{N_1 \Phi_m 2\pi f}{\sqrt{2}}$$

$$E_{rm} = e_1 = 4.44 N_1 \Phi_m f \quad (4)$$

Similarly,

for secondary winding rms value of emf is given by

$$e_2 = 4.44 N_2 \Phi_m f \quad (5)$$

Transformation Ratio (k) :-

Dividing eq. 5 by 4.44.

$$\frac{e_2}{e_1} = \frac{N_2}{N_1} = k \text{ for practical transformer}$$

conditions for Ideal transformer

- Resistance of Primary & Secondary winding becomes negligible.
- There should be no leakage flux
- There should be no losses in transformer

$$\text{Q/P Power} = \text{O/P Power}$$

$$E_1 I_1 \cos\phi = E_2 I_2 \cos\phi$$

$$\frac{E_2}{E_1} = \frac{I_1}{I_2}$$

, for Ideal Transformer.

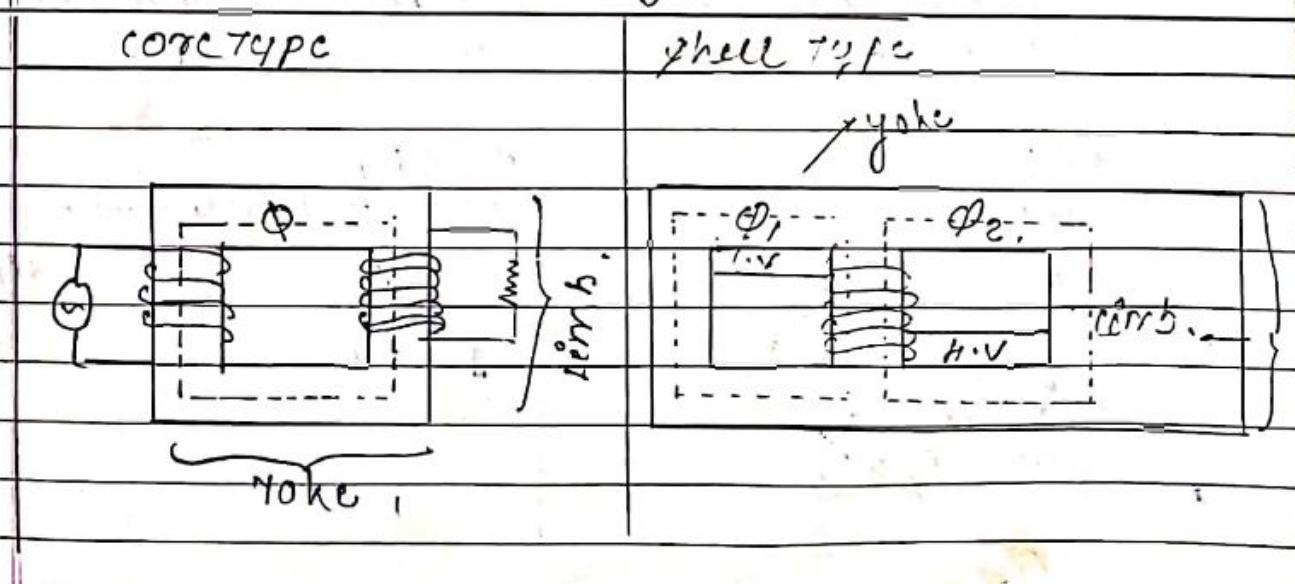
$$\frac{e_2}{e_1} = \frac{N_2}{N_1} = \frac{I_1}{I_2} = k$$

also  $e_1 \approx v_1$  and  $e_2 \approx v_2$ .

$$\frac{e_2}{e_1} = \frac{v_2}{v_1} = \frac{N_2}{N_1} = \frac{I_1}{I_2} = k$$

11/02/19  $\rightarrow$  Classification of Transformer

① Based on position of windings:-



core type

- (1.) In core type transform  
core is surrounded  
by the windings.  
 (2.) • no. of limbs = 02.  
     • no. of yokes = 02

(3.) no. of magnetic  
path = 1

shell type

- In the shell type transform.  
windings is surrounded  
by core.  
 • no. of limbs = 03.  
     • no. of yokes = 02

no. of magnetic  
path = 02

Based on the operation:-

Step-up

Step-down.



It transforms low  
voltage, high current  
to high voltage,  
low current.

- $N_p < N_s$ .

↳ primary winding  
 $N_p \rightarrow$  secondary  
winding

$$\therefore V_p < V_s$$

$$\text{also } I_p > I_s$$

It transforms high  
voltage, low current  
to low voltage high  
current.

- $N_s < N_p$ ,

$N_s \rightarrow$  Primary winding

$N_p \rightarrow$  Secondary winding

$$V_s < V_p$$

$$I_s > I_p$$

③ Based on the location of transformer.

Distribution transformer. Power transformer.

- output rating = 5 KVA

- efficiency i.e.  $\eta = 80\%$

- distribution transformer remains energized for 24 hours.

- it transforms transmission line voltage to the distribution voltage (230V) that the ease of household supply.

it transforms high voltage to

- output rating = 500 KVA

$$\eta = 80\%$$

- it remains energized for high load operation and it is used as power stations.

- it transforms transmission voltage to the transmission voltage.

### Losses in Transformer:-

↓  
Core loss:

winding loss  
(C.R)

→ Eddy current loss.

→ Hysteresis loss

#### Core Losses:-

These losses takes place in the core material (magnetic part of transformer). There are of two types → Eddy current loss and Hysteresis loss.

## Eddy current loss -

Q

Because of the alternating field emf is induced in core which causes induced current known as Eddy current. The Eddy current loss in Watts can be given as -

$$W_e = k_e B_m f^2 t^2 v$$

$B_m$  : maximum flux density.

$f$  → frequency

$t$  = thickness of lamination

$v$  = volume of core

$k_e$  = eddy current coefficient

These losses can be minimised by providing laminated core.

## Hysteresis loss -

These losses depends on the quality of core material can be minimised by using good quality material such as. (Silicon steel, nickel iron, CRGO steel)

$$T W_h = k_h B_m^{1.6} f v$$

## Total core losses.

$$P_c = W_e + W_h$$

### Note:-

The core losses are fixed losses. They do not depends on the load.

## Copper Loss (Ohmic Loss) -

These losses takes place in the conducting materials (windings) of the transformer and they are given by  $P_{oh} = I^2 R$  watts.

Ohmic power loss

since, there are two windings in normal transformer  $\therefore P_{oh} = \frac{I_1^2}{2} r_1 + \frac{I_2^2}{2} r_2$

These losses are normally calculated at  $75^\circ\text{C}$ . These are variable losses since they depends on the load current.

## Vary Load loss :-

Occurrence of these losses is due to presence of leakage field. Percentage of these losses is very small as compare to copper loss and core losses. So can be neglected for calculation of efficiency.

## Dielectric Loss -

This loss occurs in insulating material or oil. This loss is also negligible and it is not taken into account for calculation of efficiency.

## Efficiency :-

Since there are no rotational losses (frictional and windage), so the transformer has very high efficiency which is defined as a ratio of output Power to the input Power.

$$\eta = \frac{\text{Output Power in watts}}{\text{Input Power in watts}}$$

OR

No output  
current source

$\Rightarrow$  no  $I_{\text{source}}$

$\Rightarrow$  no core loss

where

$V_o$  = voltage across the load

$I_o$  = current through the load

$P_o$  = core no-load loss

$P_{\text{load}}$  = no-load ohmic losses)

const. = load power factor

$$\text{In percentage } \eta = \frac{V_o I_o \cos \phi}{V_o I_o \sin \phi} \times 100\%$$

regulation

efficiency can be also written in terms of  
of input and losses:

$$\eta = \frac{\text{Input - losses}}{\text{Input}} \times 100\%$$

All Day Efficiency (Daily efficiency) :-

On the primary of distribution transformer  
the voltage across the load is  
continuously changing throughout all day.  
so, the efficiency is normally expressed in  
energy level x time.

$$\eta = \frac{\text{Output in kWh} \times 100}{\text{Input in kWh}}$$

voltage regulation of A-motor

it is defined as a change in magnitude of secondary terminal voltage when load at a given power factor is removed with primary supply voltage is kept constant.  
it is defined as a percentage of p.u of secondary ratio voltage, no load voltage.

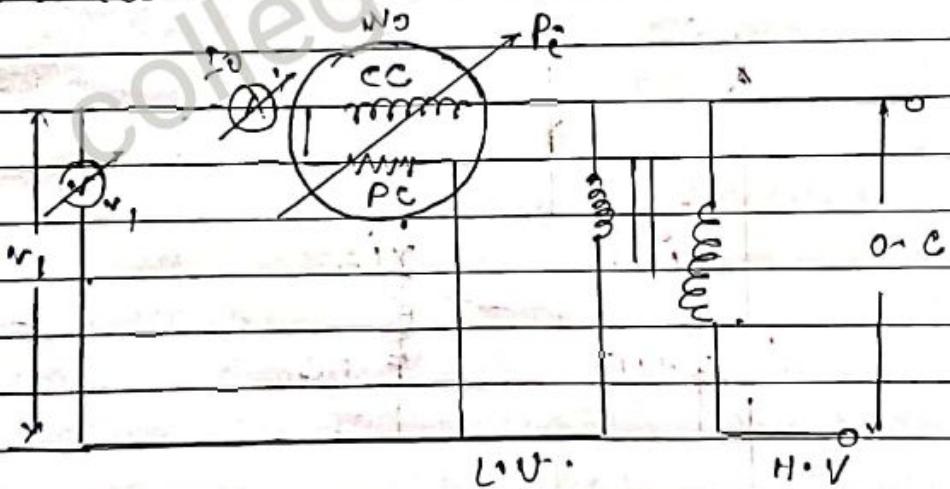
$$\text{Voltage Regulation} = \frac{E_2 - V_2}{V_2} \text{ in P.U}$$

$$\% \text{ V.R} = \frac{E_2 - V_2}{E_2} \times 100 \text{ (in \%)}$$

$E_2$  = secondary voltage (no load voltage)

$V_2$  = secondary terminal voltage at full load.

13/02/2019 - 0  
open circuit test



- open circuit test is performed to determine iron losses (core losses)

- open circuit test determines parameters of parallel branch of equivalent circuit of transformer i.e.  $R_c \cdot X_m$

- high voltage winding is kept open during open circuit test.

- top  $E_2$  carried out at low voltage side that means

all the instruments (voltmeter, ammeter) are connected at low voltage side.

Since there is no load connected at the secondary side hence the value of no load current i.e.  $I_0$  is very small (2-5% of Full rated current)

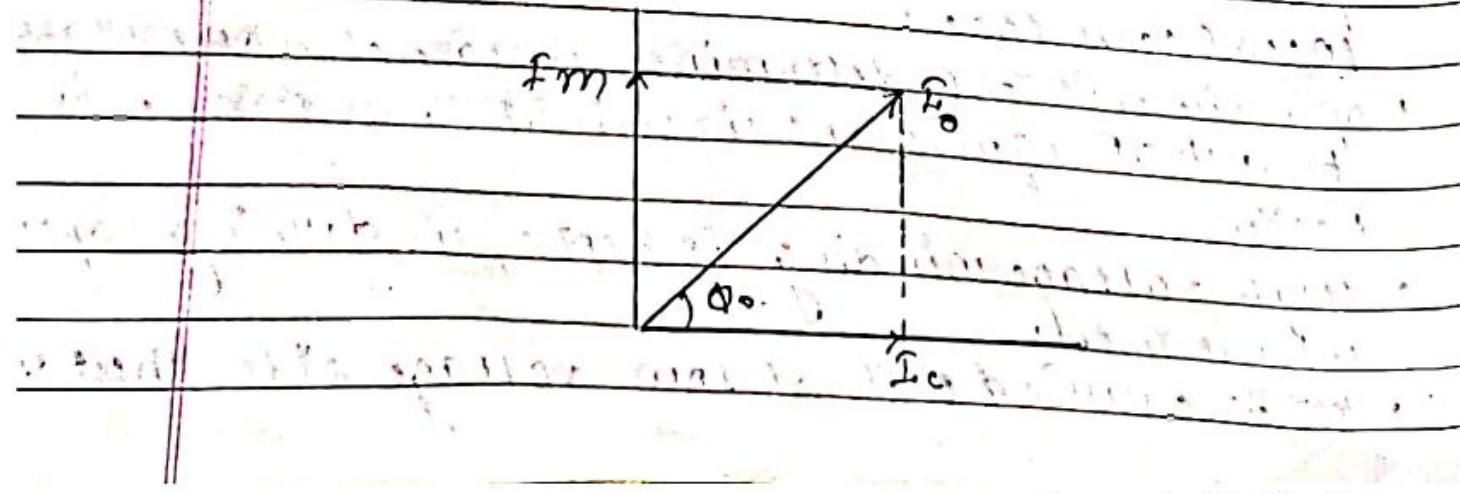
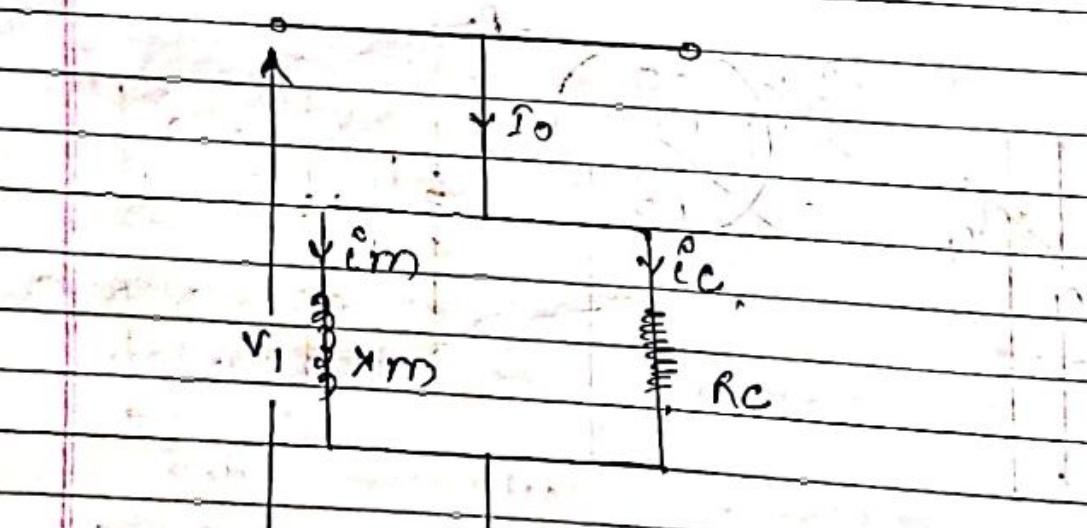
Readings of different instruments are as follows:

Ammeter =  $I_0$  = no. load current

Voltmeter =  $V$  = primary voltage

Wattmeter =  $P_e^e$  = iron loss

iron loss is given by  $I_{00} = V I_0 \cos \phi_0$



$\text{O.C} \rightarrow$  Open Circuit

$\text{S.C} \rightarrow$  Short Circuit

$$T_c = T_0 \cos \phi_b$$

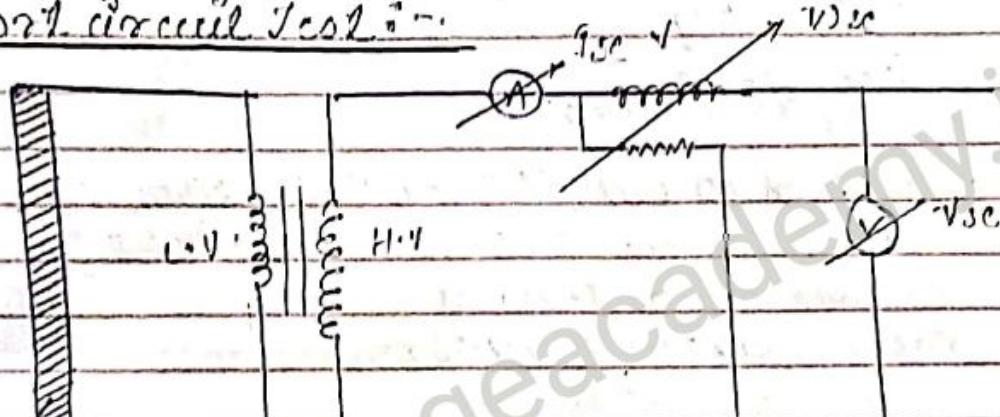
$$T_m = T_0 \sin \phi_b$$

$$R_c = \frac{M_1}{\omega_c}$$

$$X_m = \frac{N_1}{A_m}$$

14/02/2019 - 15/02/19 -

Short circuit Test :-



shorted by copper wire.

- (1) short circuit test determines copper losses ( $P_c$ ).
- (2) short circuit test determines parameters of shunt branch of equivalent circuit of transformer i.e.  $R_1$ ,  $X_1$  and  $R_2$ ,  $X_2$ .
- (3) low voltage side is shorted by thick copper wire during short circuit test. Test is carried out at high voltage side, that means all instruments are connected at high voltage side.

- (4) the Readings of different instruments are as follows.  
ammeter  $I_{sc}$  = short circuit current  
voltmeter  $V_{sc}$  = short circuit voltage  
inattmeter =  $W_{sc} = P_c$  = copper losses.

The core loss is given by :  $W_{sc} = 2^{\circ}\text{sc} \cdot R_{eq}$ .  
 $R_{eq} = \frac{W_{sc}}{I_{sc}}$   $\hookrightarrow$  Required.

(5.) The equivalent impedance is given by

$$V_{sc} = I_{sc} \times Z_{sc}$$

$$Z_{sc} = \frac{V_{sc}}{I_{sc}}$$

(6.) The equivalent leakage reactance is given by

$$Z_{sc} = \sqrt{R_{eq}^2 + X_{sc}^2}$$

$$X_{sc} = \sqrt{Z_{sc}^2 - R_{eq}^2}$$

Numerical: A 10 kVA, 200/400 volt, 50 Hz, 1Ø x-mag using for open circuit test results are as follows

$$O.C.T \quad 120W, 20V, 1.25A$$

$$P_f = 120W = 120W$$

$$V_1 = 20V$$

$$I_0 = 1.25A$$

$$S.C.T \quad 200W, 20V, 25A$$

$$P_c = W_{sc} = 200W$$

$$V_{sc} = 20V$$

$$I_{sc} = 25A$$

① calculate magnetising current/ working current at normal voltage & current.

② Efficiency of transformer when transformer is supplying rated load at 0.8 power factor lagging.

$$V_2 I_2 = 10kVA$$

$$V_2 I_2 = 10000VA$$

$$V_1 = 200V$$

$$V_2 = 400V$$

$$f = 50Hz$$

$$I_0 = P_0 \cos \phi_0$$

$$\cos \phi_0 = \frac{P_0}{V_1 I_0} = \frac{120}{200 \times 1.25} = 0.48$$

$$I_m = I_0 \sin \phi_0 \Rightarrow 1.25 \times \sqrt{1 - (0.48)^2}$$

$$I_m = 1.096 \text{ A}$$

$$I_c = I_0 \cos \phi_0 \\ = 1.25 \times 0.48$$

$$I_C = 0.6 \text{ A}$$

$$R_C = V_1 / I_C = 200 / 0.60 = 333.3 \Omega$$

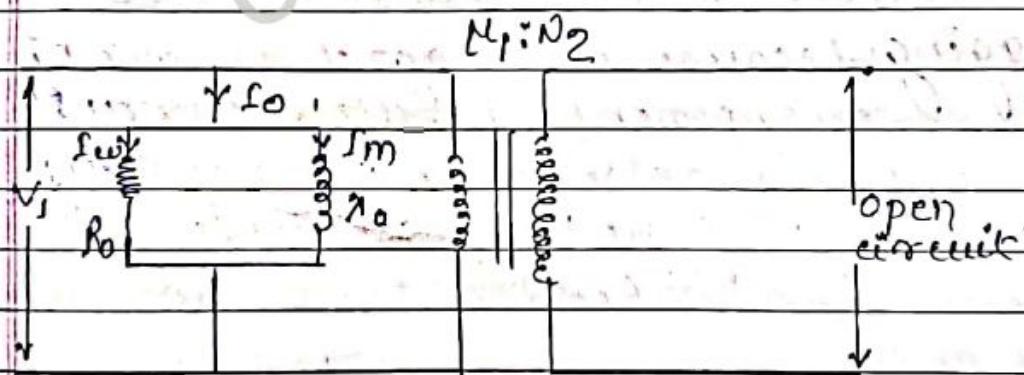
$$X_m = V_1 / I_m = 200 / 1.096 = 182.46 \Omega$$

$$\eta = \frac{V_2^2 \cos \phi \times 100}{V_2^2 \cos \phi + P_e + P_C}$$

$$= \frac{10000 \times 0.8}{(10000 \times 0.8) + 120 + 200} = 96\%$$

21/02/2018 :-

Equivalent circuit of a-mere under no load :-

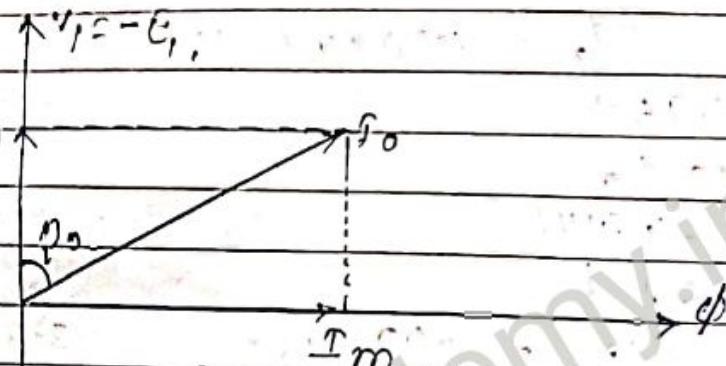


$$R_0 = N_1^2, X_0 = N_1^2 X_w, I_m$$

$R_0$  and  $X_0$  should be in parallel and should be in Primary circuit. This parallel branch carry no load & branch is shunt branch.

## Phasor Diagram of A-mut under no-load

Condition:-



$V_{E_2}$

$V_{E_1}$

- $\phi_2 = \text{no load phase angle of Transformer}$   
any its ranges,  $70^\circ$  to  $75^\circ$
- $\cos\phi_2 = \text{no load power factor of}$   
transformer any the range is  $0.2$  to  $0.25$   
lagging.

Transformer has poor no load  
Power factor of the order of  $0.2$  to  $0.25$   
lagging because its magnetizing current  
component of no load current  
is very high as compare to the working  
current of no load current.  
( $I_m \gg I_{cu}$ )

## TRANSFORMER on LOAD :-

when the secondary circuit of a transformer  
is complete through an impedance or load.  
The transformer is said to be loaded and  
current flows through the secondary  
winding and load.

(iii) The magnitude and phase of secondary current ( $I_2$ ) will depend on the secondary terminal voltage  $V_2$  coil. It depends upon the characteristic of load i.e.  $I_2$  will be in same phase with  $V_2$ , for non-inductive load, (Resistive).

$I_2$  lags  $V_2$  for inductive load,  $I_2$  leads  $V_2$  for capacitive load

(3.)



When the transformer is on no load, as shown in figure, it draws no load current  $I_0$  from the supply mains. The no load current  $I_0$  sets up an mmf  $N_1 I_0$  which produces flux  $\phi$  in the core.

(4.)

When an impedance is connected across the secondary terminal, current  $I_2$  flows through the secondary winding. Now the secondary current  $I_2$  sets up, its own mmf  $N_2 I_2$  and hence creates a secondary flux  $\phi_2$  which opposes the main flux  $\phi$ , setup by exciting current  $I_0$ . According to Lenz law,

22/02/19 -

(5.) The opposing secondary flux  $\phi_2$  weakens the main flux momentarily, so primary back emf  $E_p$  tends to reduce, so difference of applied voltage  $V$  and back emf  $E_p$  increases. Therefore more current is drawn from the source of supply flowing through the primary winding until the original

value of flux  $\phi$  is obtained. It again causes increase in back EMF  $E_b$  and it adjusts itself such that there is a balance between applied voltage  $V_1$  and back EMF  $E_b$ .

(6) Let the additional primary current be  $I'_p$ . The current  $I'_p$  is in phase opposition with secondary current  $I_s$ , and is called as counter balancing current.

(7) The addition of current  $I'_p$  sets up an mmf  $N_1 I'_p$  producing the flux  $\phi'_p$  in the same direction as that of main flux  $\phi$  and cancel out the flux  $\phi_2$  produced by secondary mmf  $-N_2 I_s$  being equal in magnitude.

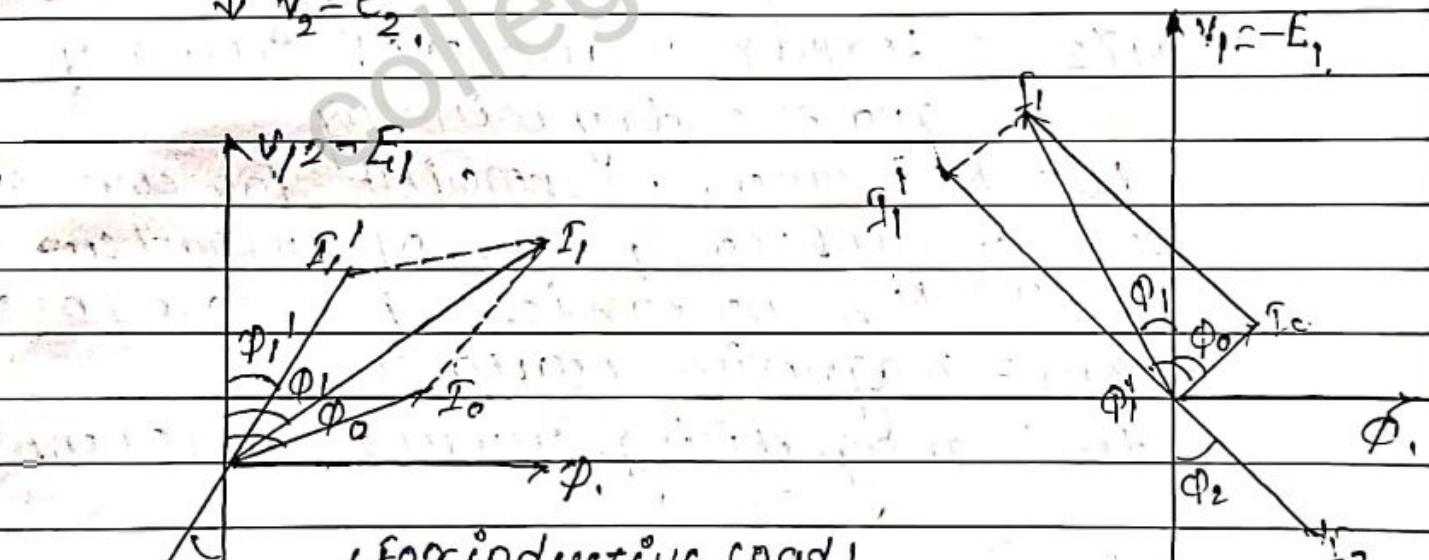
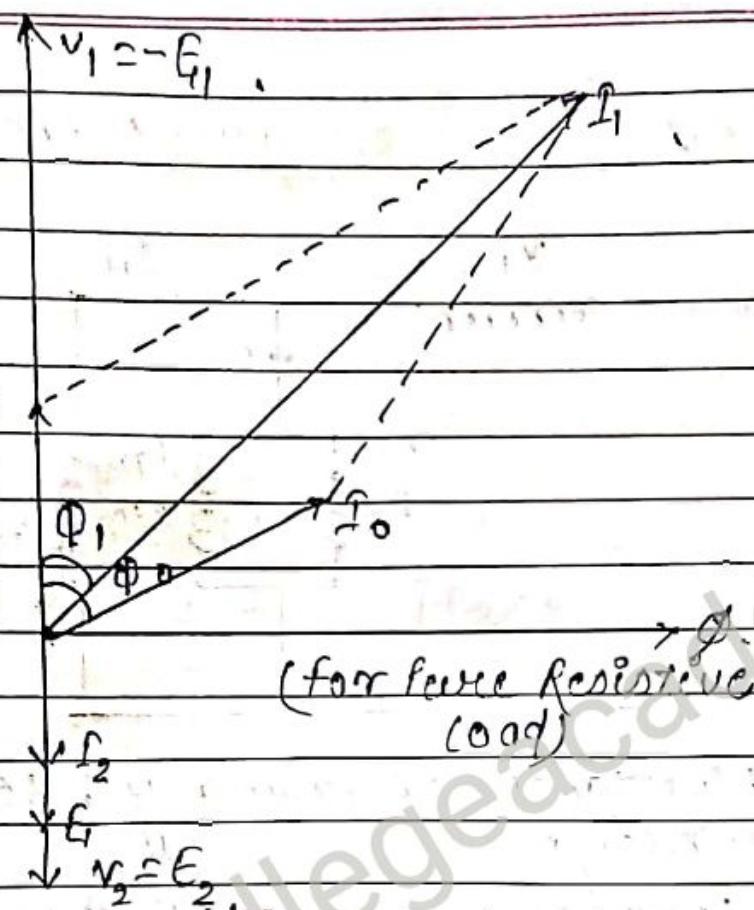
$$N_1 I'_p = N_2 I_s$$

$$I'_p = N_2 I_s$$

$$N_1$$

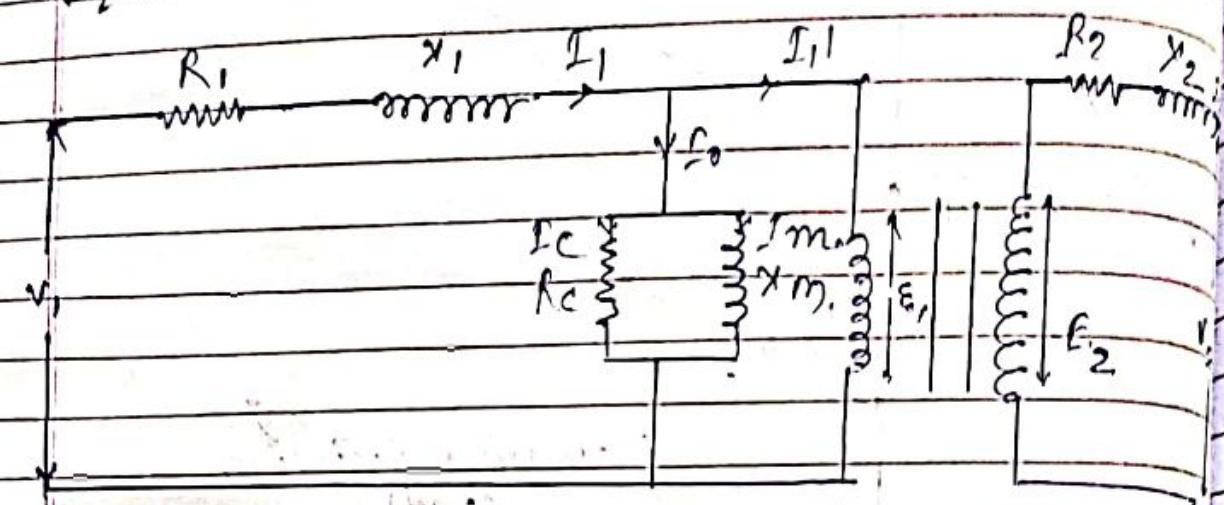
(8) The total Primary current  $I_p$  is therefore phasor sum of counter balancing current  $I'_p$  and no load current  $I_{L0}$ , which will approx. equal to the  $I_p$ , as  $I_{L0}$  is usually very small as compare to  $I'_p$ .

(9) Since the secondary flux  $\phi_2$  produced by secondary mmf  $N_2 I_s$  is neutralized by the flux  $\phi'_p$  produced by mmf  $N_1 I'_p$  set up by counterbalancing primary current  $I'_p$ , the flux in the transformer core terminals almost constant forms no load to full load.



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## Equivalent circuit of Transformer



$R_1 R_2$  = Resistances of primary & secondary winding.

$X_1 X_2$  = Leakage reactance of primary and secondary winding

$R_c$  = Resistance responsible for core losses.

$I_c$  = current component of no load current working responsible for core loss.

$X_m$  = magnetism reactance.

$I_m$  = magnetising current component of  $I_0$ .

$$I_0 = I_m + I_c$$

= no load current.

$I_p$  = balancing current or counter current

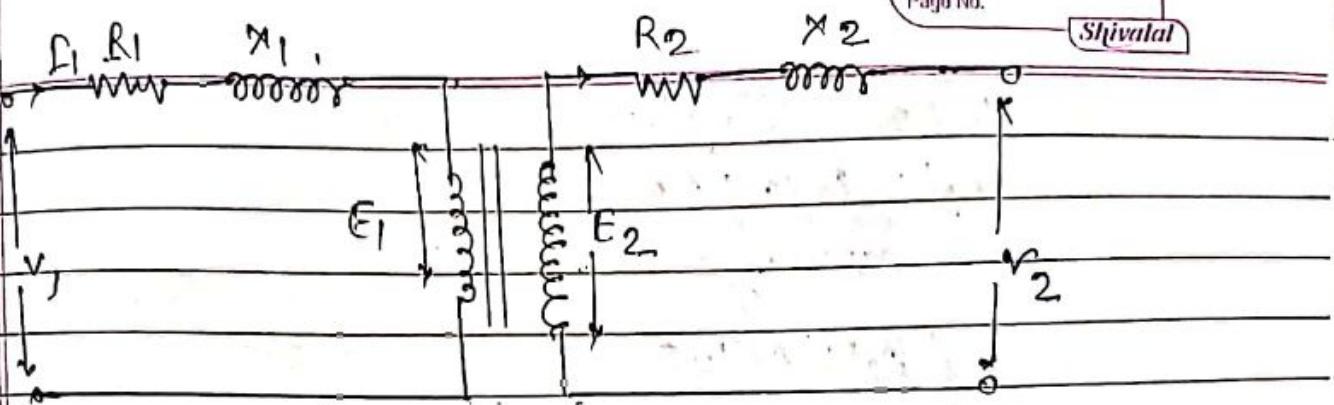
$$I_p = I_0 + I_s$$

= Primary current.

$I_2$  = Secondary current

for simplification of circuit ignore  $I_0$

i.e. parallel branch can be removed from the equivalent circuit.



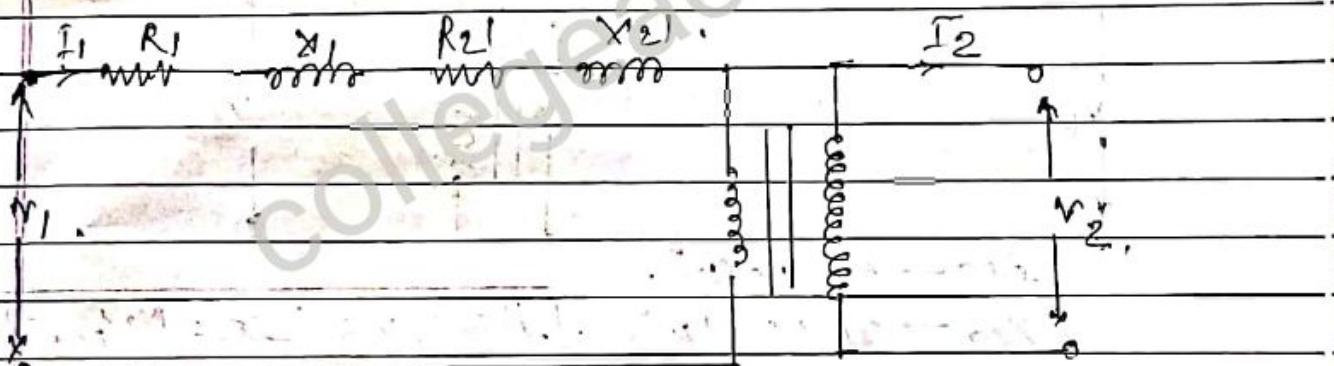
By applying KVL :-

$$V_1 = E_1 + I_1 R_1 + j I_1 X_1$$

$$E_2 = V_2 + I_2 R_2 + j I_2 X_2$$

Equivalent circuit:-

Equivalent circuit referred to Primary side:-



where  $R_2' = \text{secondary resistance } R_2 \text{ referred to primary side..}$

$X_2'$  = secondary leakage reactance  
referred to primary side.

Condition:-

We can move the resistance and leakage from Secondary side to Primary side, only when they can consume same amt. of power in Primary side as they were consuming in Secondary side.

$$I_2^2 R_2 = I_1^2 R_2'$$

$$R_2' = (I_2/I_1)^2 R_2$$

$$\left( \frac{V_2}{V_1} = \frac{I_1}{I_2} = K \right)$$

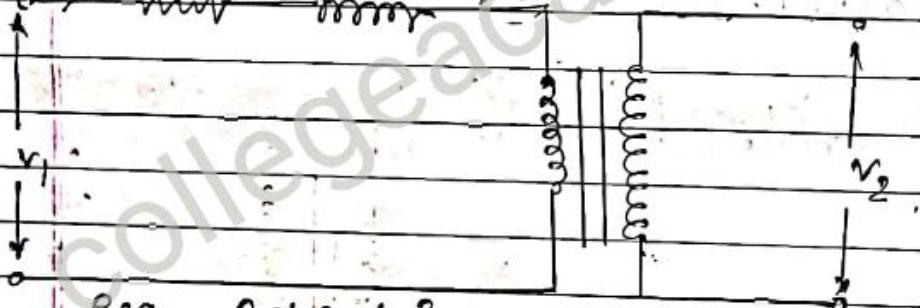
$$(R_2' = R_2/K^2)$$

$$\text{similarity, } I_2^2 X_2 = I_1^2 X_2'$$

$$X_2' = (I_2/I_1)^2 X_2$$

$$\left( \frac{X_2'}{X_2} = \frac{I_2}{I_1} = \frac{K}{1} \right)$$

$$f, R_{eq} = R_1 + R_2' \quad ; \quad X_{eq} = X_1 + X_2'$$



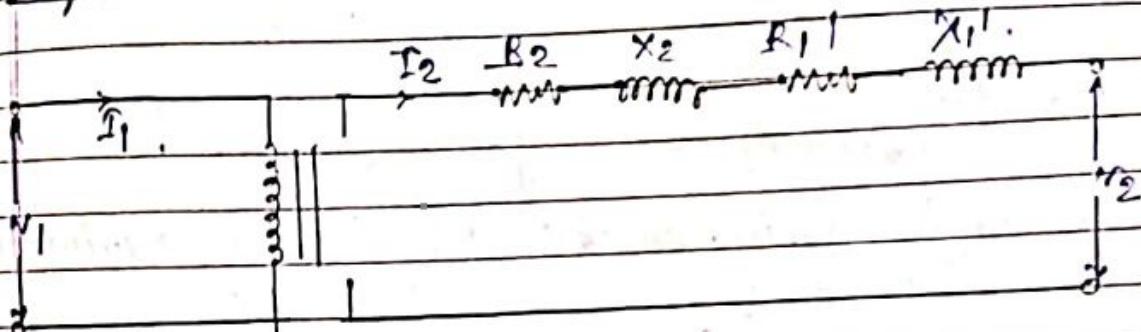
$$R_{eq} \rightarrow R_1 + R_2'/K^2$$

$$X_{eq} \rightarrow X_1 + X_2'/K^2 \quad ; \quad K = \frac{V_2}{V_1} = \frac{E_2}{E_1} = \frac{N_2}{N_1} = \frac{I_1}{I_2}$$

$R_{eq}$  = equivalent Resistance referred to  
 $X_{eq}$  primary side

$X_{eq}$  = equivalent leakage Reactance referred  
to primary side

Equivalent circuit referred to SECONDARY SIDE:



$R_1'$  = Primary resistance referred to Secondary side

$X_1'$  = Primary leakage resistance referred to Secondary side

We can move the resistance and leakage resistance from primary side to the secondary side only when they will consume some amount of power in secondary side as they were consuming in primary.

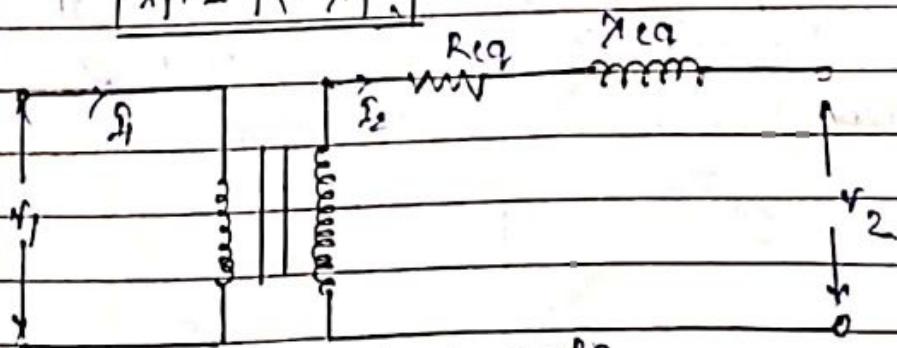
$$I_1^2 R_1 = \frac{V_1^2}{k^2}$$

$$R_1' = \left(\frac{I_1}{I_2}\right)^2 R_1$$

$$\left[\because \frac{V_2}{V_1} = \frac{I_2}{I_1} = k\right]$$

$$R_1' = k^2 R_1$$

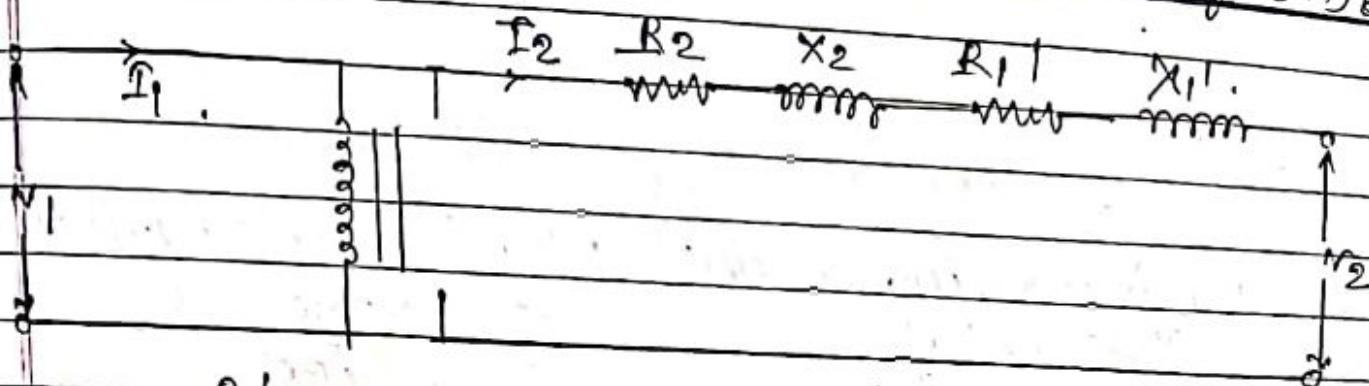
$$X_1' = k^2 X_1$$



$$R_{eq} = R_2 + R_1' = R_2 + k^2 R_1$$

$$X_{eq} = X_2 + X_1' = X_2 + k^2 X_1$$

Equivalent circuit referred to SECONDARY SIDE



$R_1'$  = Primary resistance referred to secondary side.

$X_1'$  = Primary leakage resistance referred to secondary side.

We can move the resistance and leakage reactance from primary side to the secondary side only when they will consume some amt. of power in secondary side as they were consuming in primary.

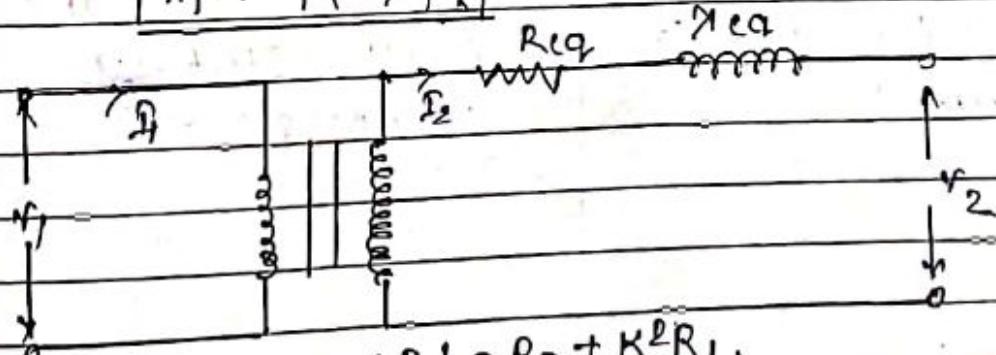
$$I_1^2 R_1 = I_2^2 R_1'$$

$$R_1' = (I_1/I_2)^2 R_1$$

$$[\because V_2/V_1 = I_2/I_1 = K]$$

$$R_1' = K^2 R_1$$

$$X_1' = K^2 X_1$$



$$R_{eq} = R_2 + R_1' = R_2 + K^2 R_1$$

$$X_{eq} = X_2 + X_1' = X_2 + K^2 X_1$$