

Electric Circuit

The system in which electric current can flow from source to load through one path and after delivering energy at load can return to the other terminal of source through another path is referred as electric circuit.

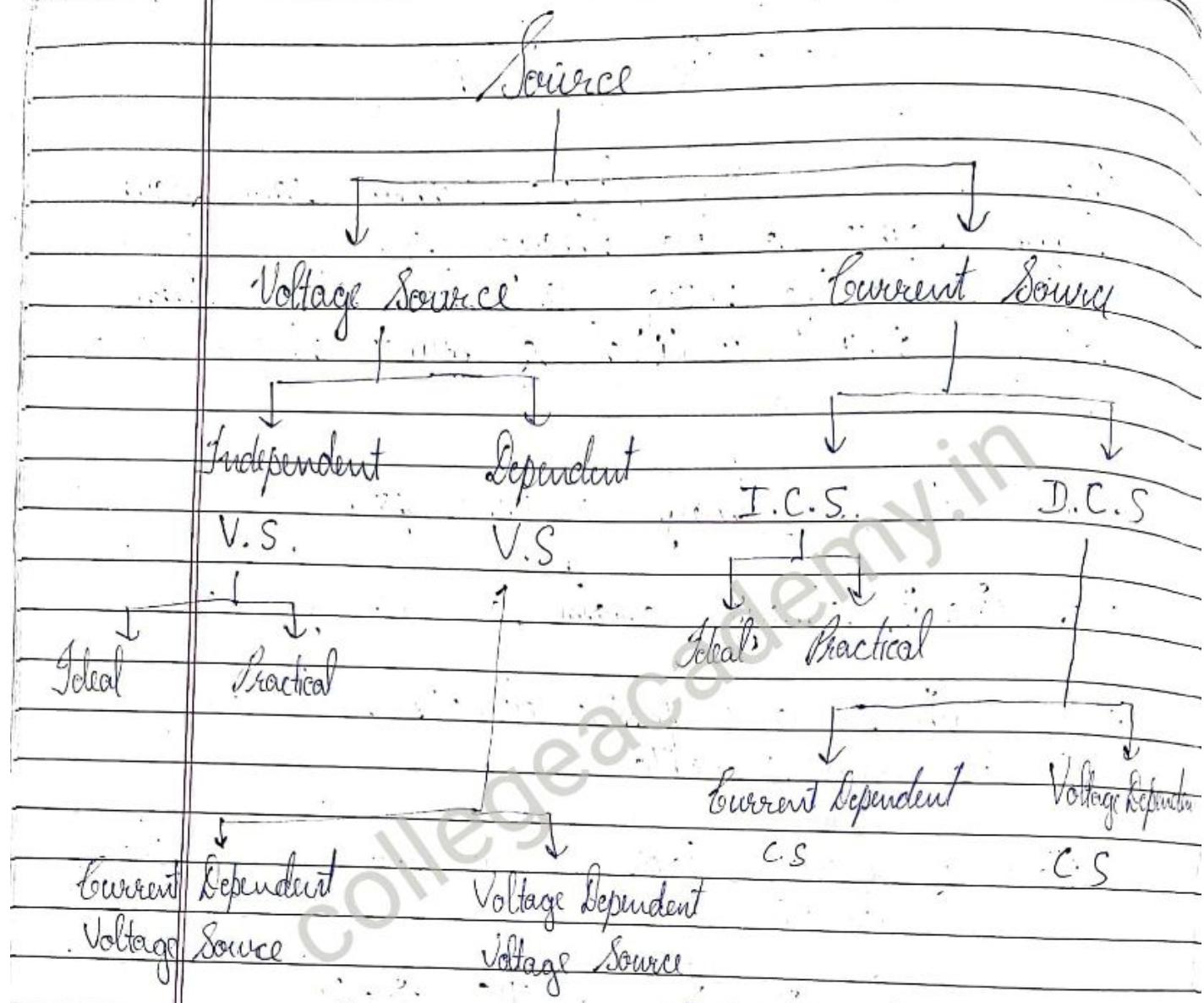
- A circuit is always a closed path.
- A circuit always contain an energy source.
- A circuit contains passive elements such as resistor, inductor and capacitor.
- Flow of current leads to the p.d. across the various elements.

Classification of DC circuit

Active Element

Passive Element

Source - Source is a pair of terminal which provides energy to the electrical circuit.



Independent Voltage Source

In this type of source voltage across its terminal does not depends on the voltage or current across another terminal

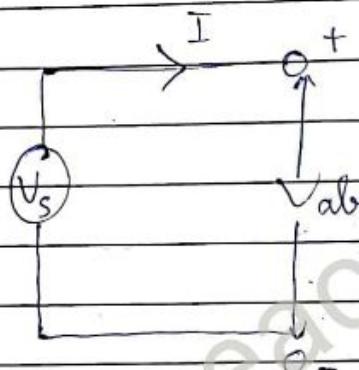
→ Ideal Voltage Source → Voltage across the

ideal voltage source does not depend on current flowing through its terminals, it means it remains unchanged even though current flowing through

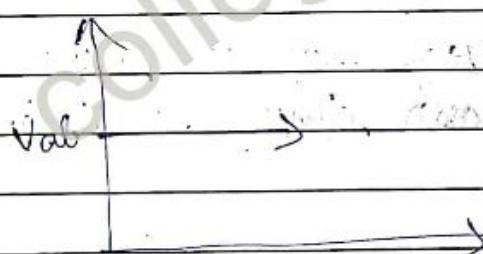
its terminal. Its terminal voltage remain same.

if internal resistance of ideal voltage source is equal to zero.

if terminal voltage is always equal to the source voltage

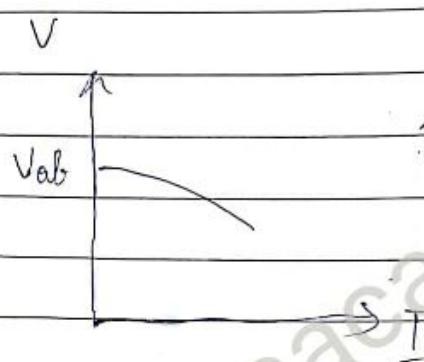
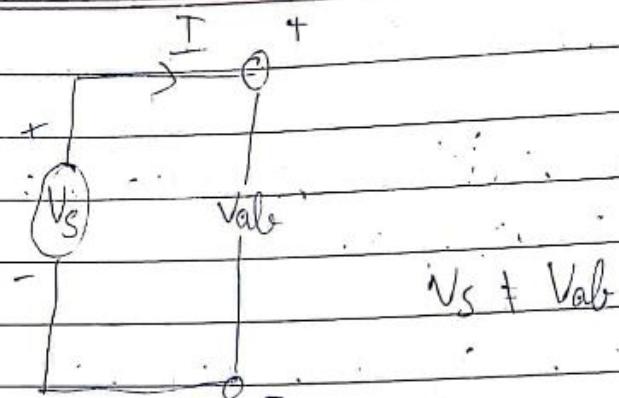


$$V_s = V_{ab}$$



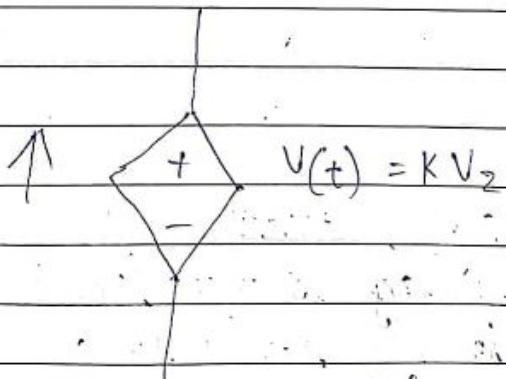
Practical Voltage Source

In practical voltage source terminal voltage is never equal to the source voltage it is difficult to maintain internal resistance of voltage source to zero, that means a internal resistance always appears that may be very small.



Voltage dependent voltage source

In the VDVS voltage source always depends on the voltage across other terminal



Current Dependent Voltage Source

In CDVS source voltage always depends on the current flowing through the other terminal



$$V(t) = k i$$

Independent Current Source

Current flowing through its terminal does not depend on the voltage or current across other terminal.

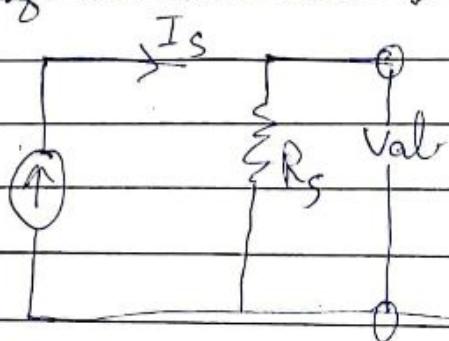
Ideal Current Source.

In ideal current source current flowing through its terminal remains unchanged it does not depend on voltage across its terminal.

Internal resistance of an ideal current source is infinite in parallel.

Practical Current Source

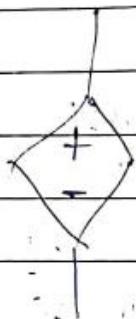
A practical current source is represented by source current with parallel resistance in this type of source, if V_{ab} increases terminal current decreases.



$$I = I_s = \frac{V_{ab}}{R_s}$$

Voltage dependent Current Source

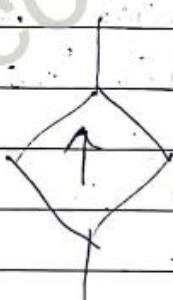
In VDVS current source always depends on voltage across the other terminal



$$V(t) = KV$$

Current dependent Current Source

In CDVS current source always depends on the current across other terminal



$$i(t) = Ki_2$$

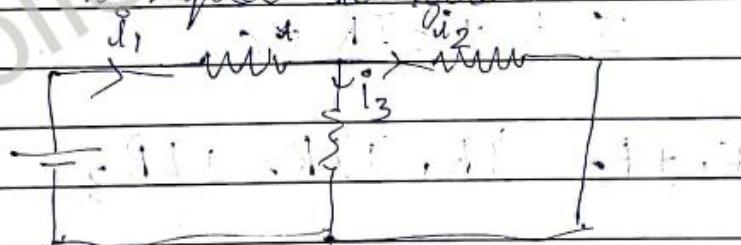
Kirchoff's Law

This law is helpful in determination of equivalent resistance of a complete network and the network current flowing in the various branches of the network.

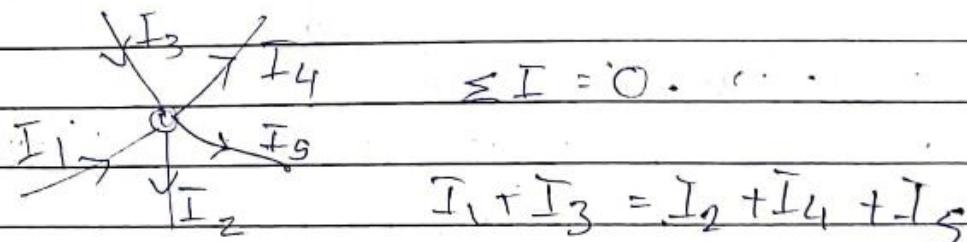
i) KCL \rightarrow Kirchoff's Current Law

KCL states that the summation of current flowing towards the node is equal to the summation of currents flowing away from the node.

That means in any network the algebraic sum of all currents in all branches meeting at a node is equal to zero.

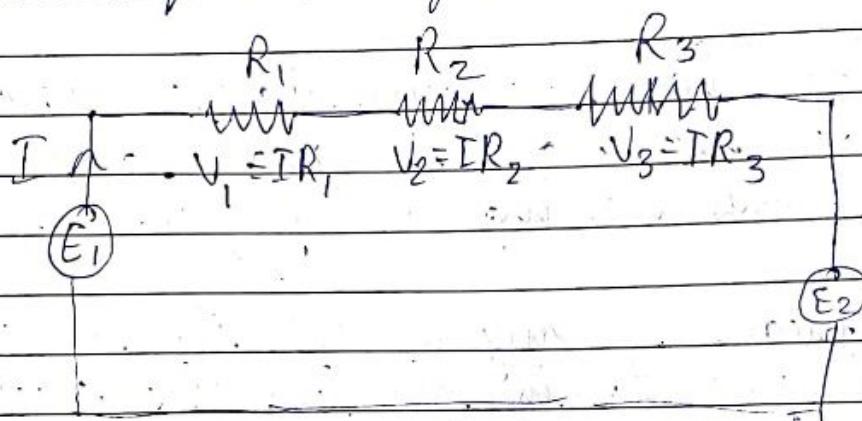


$$i_1 = i_2 + i_3$$



2. Kirchhoff's Voltage Law

KVL : states that the algebraic sum of product of current and resistance of various branches of a closed mesh in a circuit is equal to zero or the summation of voltage source and voltage drops should be equal to zero



$$\sum E + \sum IR = 0$$

$$E_1 + E_2 = IR_1 + IR_2 + IR_3$$

→ Node - node is a point of interconnection between two or more elements

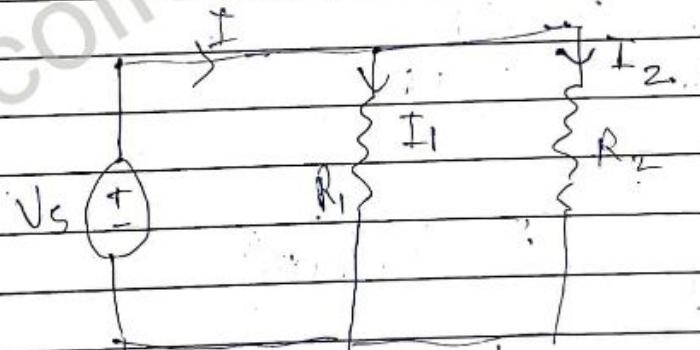
→ Junction - junction is a point of interconnection between three or more elements

Note → Junction can be node but node can never be junction

- Branch - A branch is an elemental connection between two nodes.
- Mesh - Mesh is a closed path of a circuit or network which should not have further closed path.
- Loop - Loops are all possible closed paths of a circuit

Note → A mesh can be a loop but a loop cannot be a mesh.

Current Division Rule



$$I_1 = \frac{V_s}{R_1} \quad I_2 = \frac{V_s}{R_2}$$

$$\text{A.T. KCL} = I = I_1 + I_2$$

$$I = \frac{V_s}{R_1} + \frac{V_s}{R_2}$$

$$I = V_s \left(\frac{1}{R_1} + \frac{1}{R_2} \right)$$

Kirchhoff's Voltage Law

$$V_s = I \left[\frac{1}{R_1} + \frac{1}{R_2} \right]$$

$$V_s = \frac{I}{\left[\frac{1}{R_1} + \frac{1}{R_2} \right]}$$

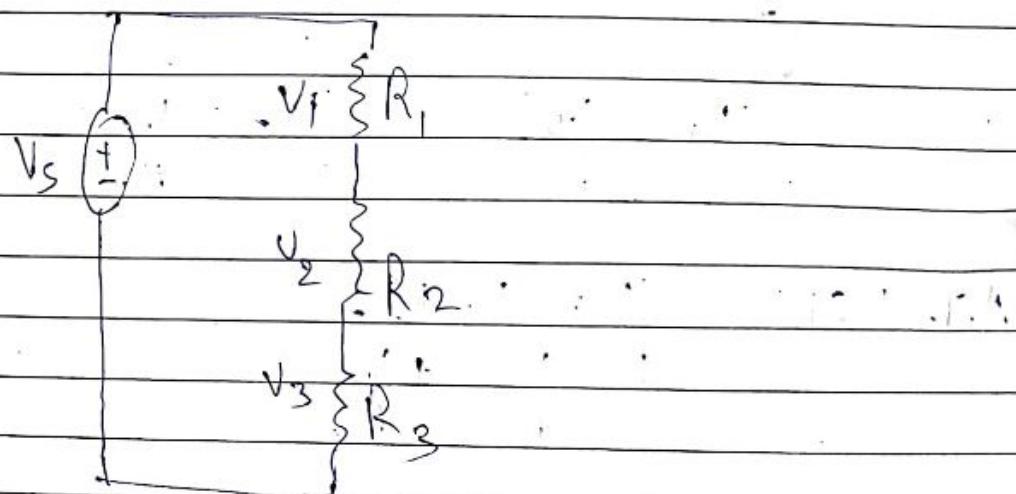
$$V_s = I R_1 R_2$$

$$R_1 + R_2$$

$$I_1 = \frac{V_s}{R_1} = \frac{I R_2}{R_1 + R_2}$$

$$I_2 = V_s = \frac{I R_1}{R_1 + R_2}$$

Voltage Division Rule



$$V_1 = \frac{V_s R_1}{R_1 + R_2 + R_3}$$

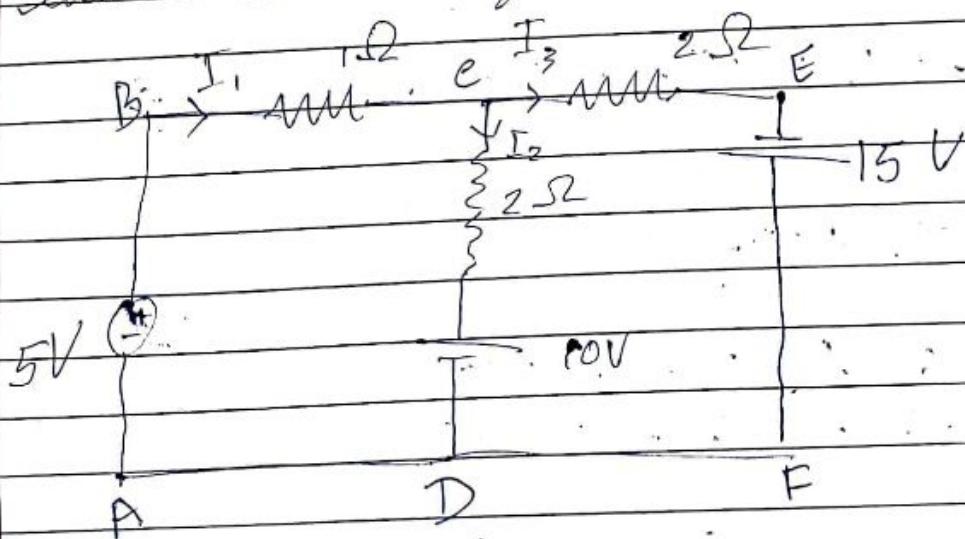
$$V_2 = \frac{V_s R_2}{R_1 + R_2 + R_3}$$

$$V_3 = \frac{V_s R_3}{R_1 + R_2 + R_3}$$

Procedures for KVL:

1. Mark the current in each branch.
2. Apply KVL in each closed path and no. of KVL should be equal to no. of unknown currents.

Q By using KVL find out the current in each branch of circuit.



$$I_1 = I_2 + I_3 \quad \text{---(1)}$$

Apply KVL in loop ABCDA

$$-5 + I_1 + 2I_2 + 10 = 0$$

$$I_1 + 2I_2 = -5 \quad \textcircled{2}$$

Apply KVL in loop DCEFD

$$10 - 2I_2 + 2I_3 - 15 = 0$$

$$-2I_2 + 2I_3 = 25 \quad \textcircled{3}$$

put $I_1 = I_2 + I_3$ in eqn $\textcircled{2}$

$$I_2 + I_3 + 2I_2 = -5 \quad \textcircled{4}$$

$$3I_2 + I_3 = -5$$

$$-2I_2 + 2I_3 = 25 \quad \textcircled{5}$$

$$\cancel{I_2 + 3I_3} =$$

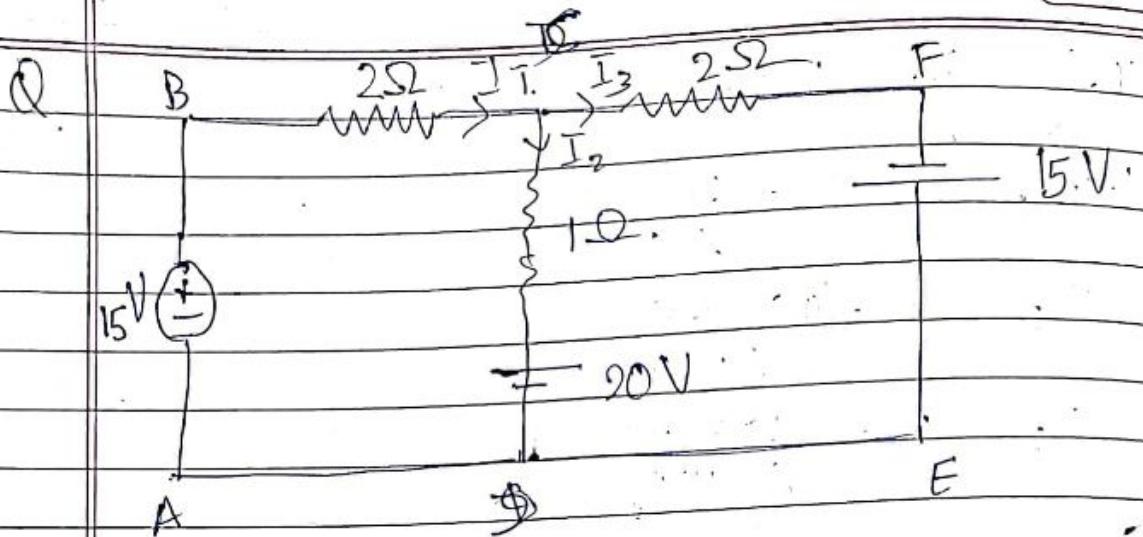
$$6I_2 + 2I_3 = -10$$

$$-6I_2 + 6I_3 = 75$$

$$8I_3 = 65$$

$$I_3 = \frac{65}{8}$$

$$I_2 = -\frac{35}{8}$$



$$I_1 = I_2 + I_3 \quad \text{--- (1)}$$

In loop ABCDA.

$$-15 + 2I_1 + I_2 + 20 = 0$$

$$2I_1 + I_2 = -5$$

$$2I_2 + 2I_3 + I_2 = -5$$

$$3I_2 + 2I_3 = -5 \quad \text{--- (2)}$$

In loop DC FED

$$-20 - I_2 + 2I_3 - 15 = 0$$

$$-I_2 + 2I_3 = 35 \quad \text{--- (3)}$$

$$4I_2 = -40$$

$$I_2 = -10 \quad \cancel{\text{A}}$$

$$I_3 = 10 + 2 I_3 = 35.$$

$$2 I_3 = 25$$

$$I_3 = \frac{25}{2} A$$

$$I_1 = -10 + \frac{25}{2}$$

$$= -10 + \frac{25}{2}$$

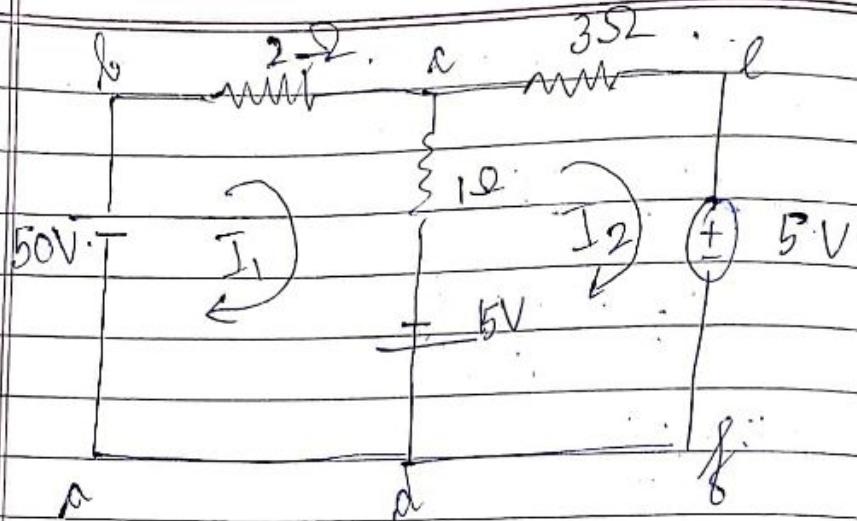
$$= \frac{5}{2} A$$

⇒ The drawback of KVL is that if the no. of branches in the given circuit increases than the no. of unknown current also increases and it becomes difficult to determine different currents.

Mesh Analysis

It eliminates the drawback of simple KVL.

In a mesh analysis loop currents are marked in each loop instead of branch currents therefore no. of unknown currents decreases. Thus simple KVL is applied in each loop to determine loop current.



Apply KVL in loop abcda

$$-50 + 2I_1 + 1(I_1 - I_2) + 15 = 0$$

$$3I_1 - I_2 = 65 \quad \text{--- (1)}$$

Apply KVL in loop dcefd

$$15 + 1(I_2 - I_1) + 3I_2 + 5 = 0$$

$$4I_2 - I_1 = -20$$

$$12I_2 - 3I_1 = -60$$

$$11I_2 = 5$$

$$I_2 = \frac{5}{11}$$

$$3I_1 = 65 + 5$$

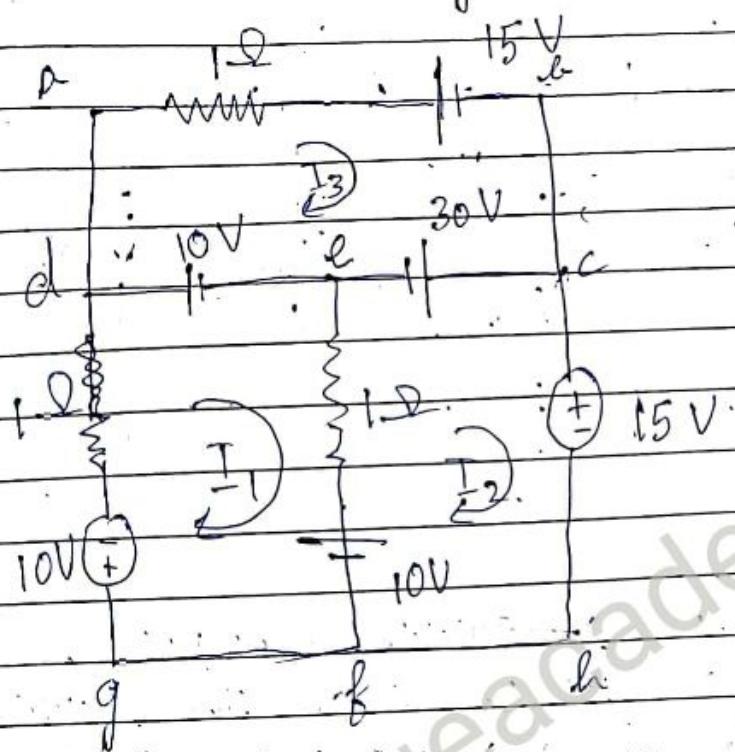
$$\frac{4 \times 5}{11} + 20 = I_1$$

$$I_1 =$$

$$I_1 = \frac{20 + 220}{11}$$

$$I_1 = \frac{240}{11}$$

d) By using mesh analysis find cut loop current in the given circuit.



In loop dgfe.

$$-10 - 10 - 10 = I_1 + I_1 - I_2$$

$$-30 = 2I_1 - I_2$$

~~In loop of side each fe~~

$$30V - 15 + 10 = I_2 - I_1$$

$$25 = I_2 - I_1 \quad \text{In loop a b c d a}$$

$$-15 - 30 + 10 = I_3$$

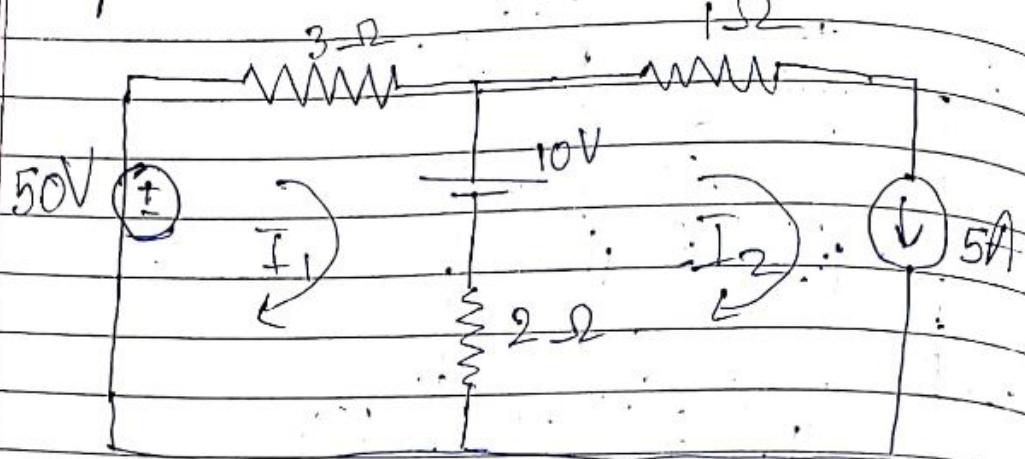
$$I_1 = -5A$$

$$I_2 = 20$$

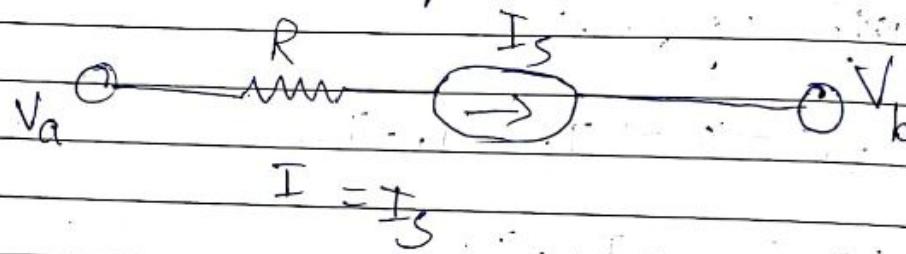
$$I_3 = -35A$$

$\frac{40}{25} = \frac{15}{25}$

Q. By using mesh analysis find out loop current in the given circuit.



Note → When a current source is connected in a branch than the current in the branch is equal to the source current.



Branch current I does not depend on voltages V_a and V_b .

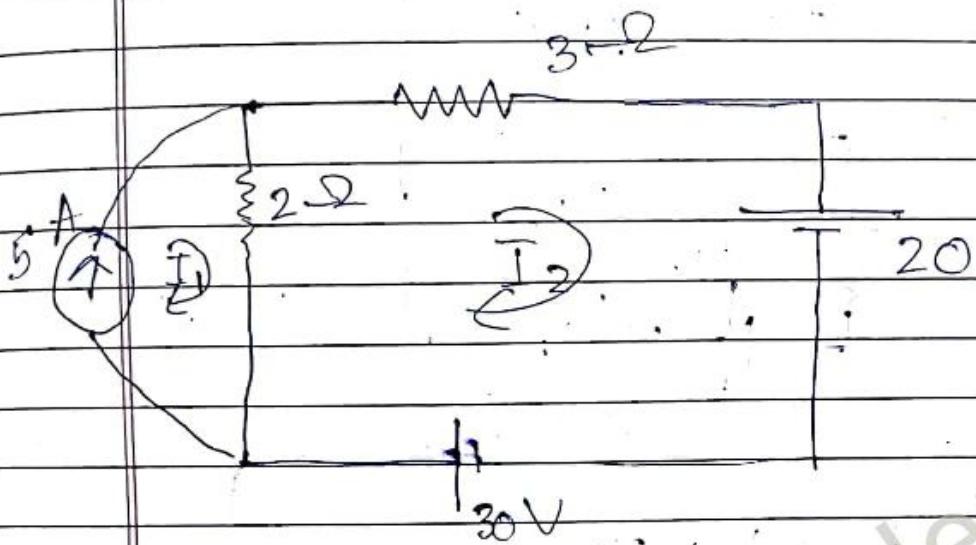
$$-10 + 50 = 3I_1 + 2(I_1 - I_2) = 0$$

$$40 = 3I_1 + 2 \cancel{I_1} - 10$$

$$\frac{50}{5} = I_1$$

$$I_1 = 10 A$$

a) By using mesh analysis, find loop current in the circuit.



$$I_1 = 5 \text{ A}$$

~~$$0 = (I_1 - I_2) \cdot 2$$~~

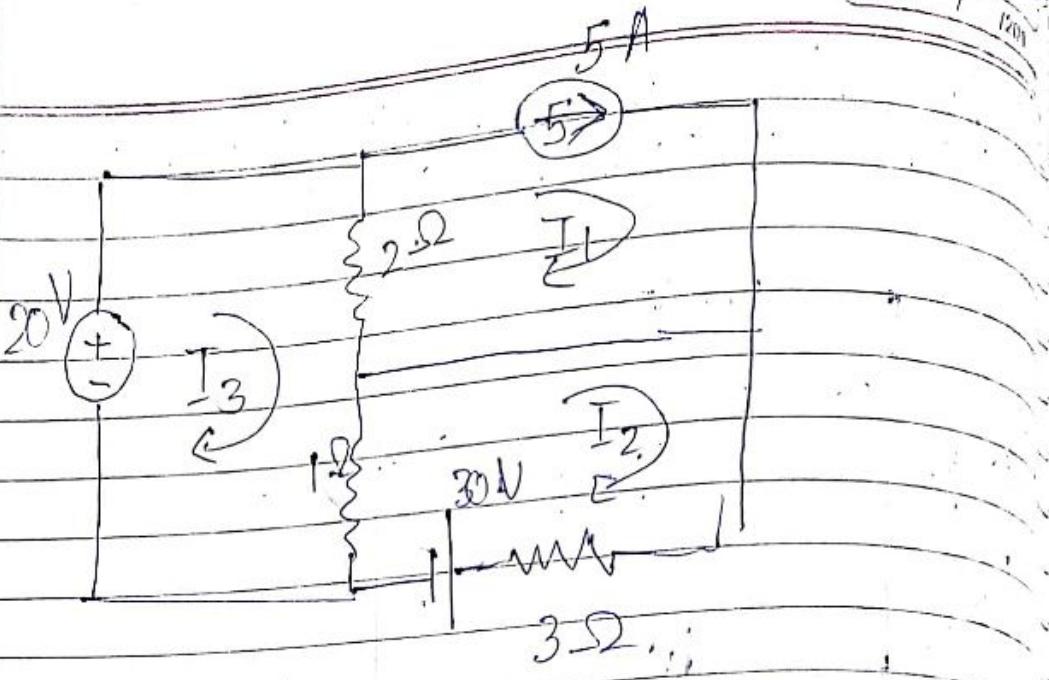
$$-20 + 30 = 2(I_2 - I_1) + 3I_2$$

$$10 = 2(I_2 - 5) + 3I_2$$

$$10 = 5I_2 - 10$$

$$\frac{20}{5} = I_2$$

$$I_2 = 4$$



$$-30 = (I_2 - I_3) + 3I_2$$

$$-30 = 4I_2 - I_3$$

$$-90 = 12I_2 - 3I_3$$

$$20 = 2(I_3 - I_1) + (I_3 - I_2)$$

$$20 = 2I_3 - 10 - I_3 - I_2$$

$$30 = 3I_3 - I_2$$

$$11I_2 = -60$$

$$I_2 = \frac{-60}{11}$$

~~30~~
~~60~~
~~270~~

$$30 = 3I_3 + \frac{60}{11}$$

$$\frac{30 - 60}{11} = 3I_3$$

$$\frac{30 - 60}{3 \times 11} = I_3$$

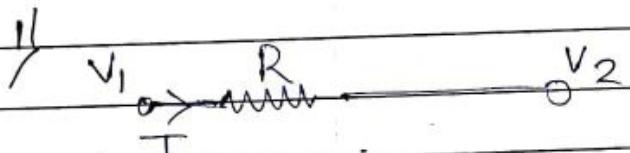
$$I_3 = \frac{270 - 60}{3 \times 11}$$

Procedure for KCL.

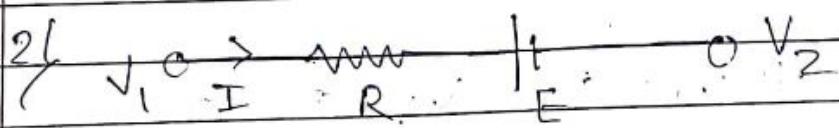
According to KCL summation of all currents at any node is always equal to 0.
 KCL states the conservation of charges.

Procedure for node Analysis

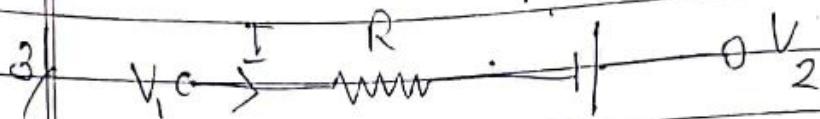
1. Mark the no. of nodes in the given circuit
2. Mark the node voltage
3. Mark one node as ground terminal
4. Apply KCL at $(n-1)$ node
5. Solve the equations for node voltages



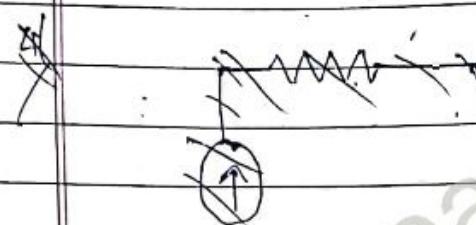
$$I = \frac{V_2 - V_1}{R}$$



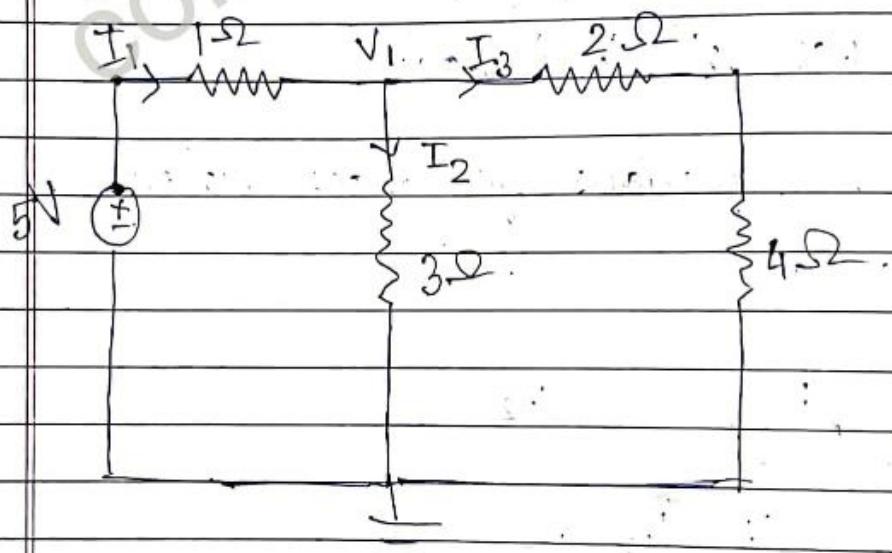
$$I = \frac{V_2 - V_1 - E}{R}$$



$$I = \frac{V_2 - V_1 + E}{R}$$



Q Find the value of T_1 , T_2 , and I_3 in the given by using nodal analysis.



Apply KCL at node V_1

$$\frac{V_1 - 5}{1} + \frac{V_1 - 0}{3} + \frac{V_1 + 0}{6} = 0$$

$$6V_1 - 30 + 2V_1 + V_1 = 0$$

$$9V_1 = 30$$

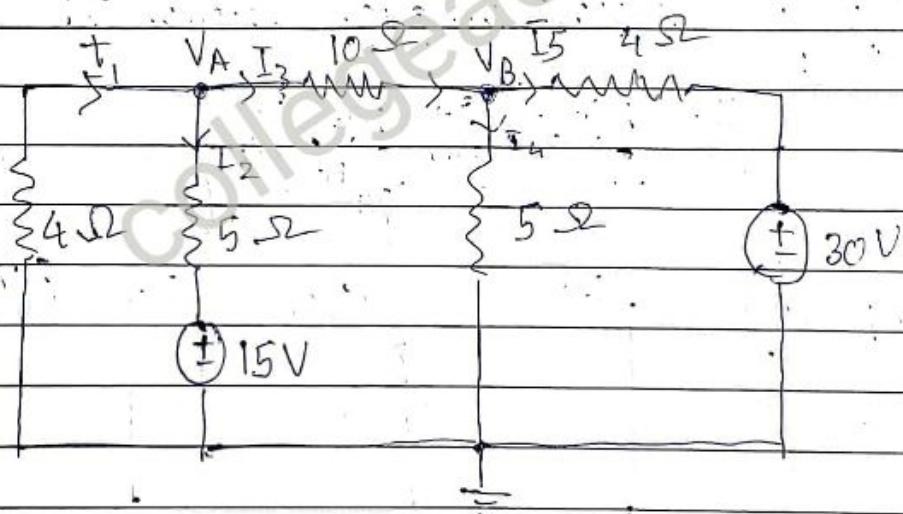
$$\frac{V_1}{9} = \frac{30}{3} = 10 \text{ V}$$

$$I_1 = \frac{10 - 5}{3} = -\frac{5}{3}$$

$$I_2 = \frac{10}{9}$$

$$I_3 = \frac{10}{18}$$

Q Using nodal analysis find out current through $10\ \Omega$ resistance.



Apply KCL at V_A

$$\frac{V_A - 0}{4} + \frac{V_A - 15}{5} + \frac{V_A - V_B}{10} = 0$$

$$5V_A + 4V_A - 60 = -2(V_A - V_B)$$

Apply KCL at V_B

$$\frac{V_B - 30}{4} + \frac{V_B - V_A}{5} + \frac{V_B - 15}{10} = 0$$

$$5V_B - 150 + 4V_B = -2(V_B - V_A)$$

$$9V_A - 60 = 2V_B - 2V_A$$

$$9V_B - 150 = -2V_B + 9V_A$$

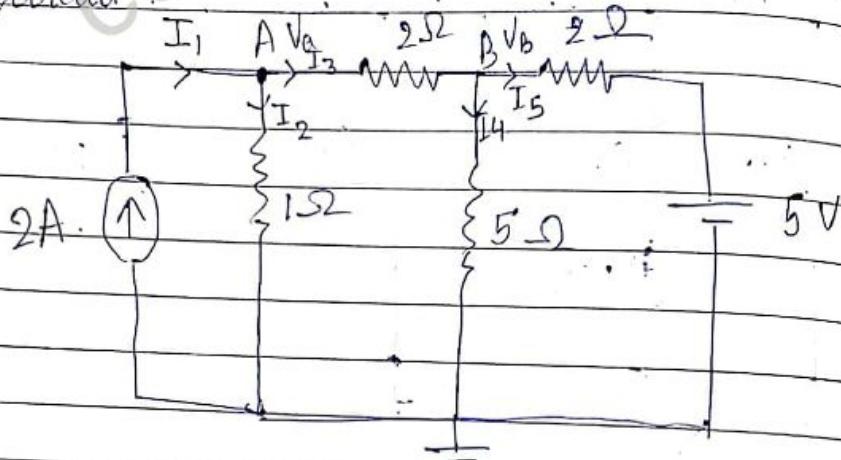
$$11V_A - 2V_B - 60 = 0$$

$$11V_B - 2V_A - 150 = 0$$

$$V_A = 8.205 \quad V_B = 15.128$$

$$I_3 = \frac{V_A - V_B}{10} \\ = 0.7$$

Q) Determine current through branch AB for given circuit.



Applying KCL across V_A .

$$-2 + V_A + V_A - V_B = 0$$

Applying KCL across V_B

$$\frac{V_B}{5} + \frac{V_B - 5}{2} + \frac{V_B - V_A}{2} = 0$$

Superposition Theorem

According to superposition theorem in a linear bilateral network which consist of more than one source, response across any load can be determined by algebraic sum of responses due to each individual independent source.

The response due to each independent source can be determined by replacing the other independent source inactive (a source can be inactive if a voltage source is replaced by short circuit and a current source replaced by open circuit.) dependent sources remains in the circuit that means dependent sources never replaced by open circuit or short circuit.

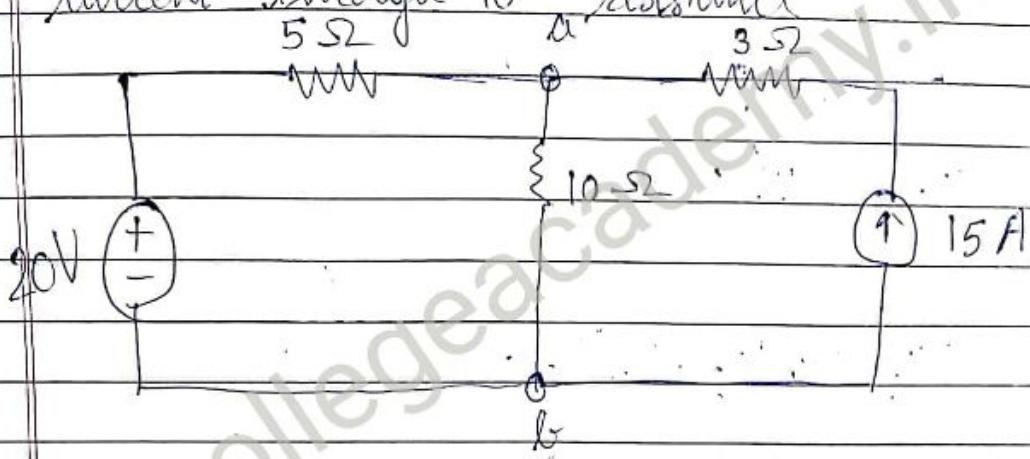
Procedure for superposition theorem

- 1) mark the load terminal
- 2) find out the current through the load due to each independent source while replacing other source inactive
- 3) replace voltage sources with short circuit and current sources with open circuit
- 4) The overall response is the algebraic sum of responses due to each independent source.

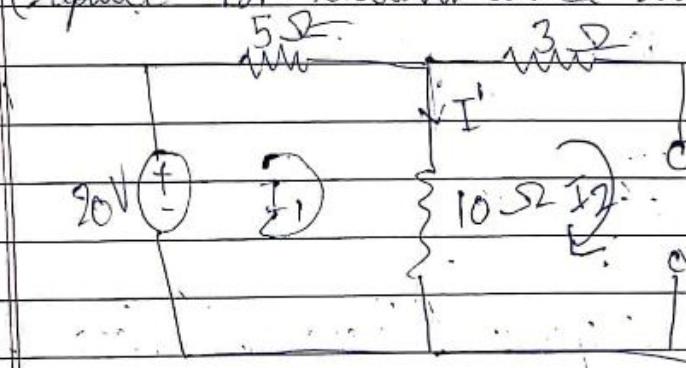
Limitations of Superposition Theorem.

- It is used to determine only voltage or current across the load that means power cannot be determined by this theorem.
- This theorem is only applicable in linear circuit.

Q Using superposition theorem find out the current through 10Ω resistance



Current through 10Ω resistance due to 20V supply
(replace 15A current source with open circuit)



→ Apply KVL in first loop.

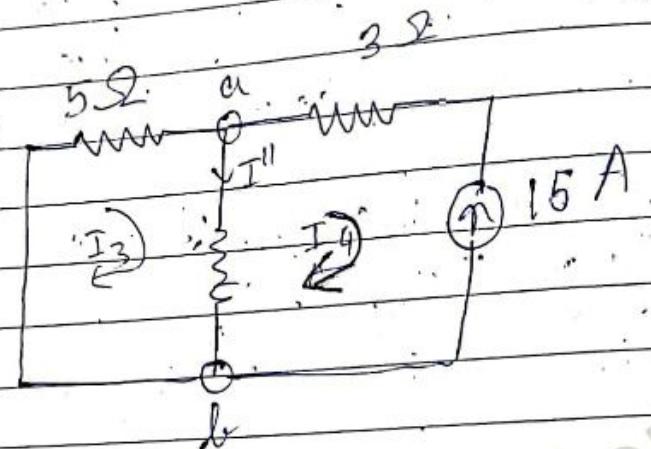
$$-20 + 5I_1 + 10I_1 = 0$$

$$I_1 = \frac{20}{15} = 1.33 \text{ A}$$

$$I' = I_1 - I_2$$

$$I' = 1.33 \text{ A}$$

→ Current through $10\ \Omega$ resistance due to 15A current source (replace 20V supply with short circuit)



$$I_4 = -15\text{ A}$$

$$5I_3 + 10(I_3 - I_4) = 0$$

$$5I_3 + 10(I_3 + 15) = 0$$

$$15I_3 + 150 = 0$$

$$I_3 = -10\text{ A}$$

$$I'' = I_3 - I_4$$

$$= -10 + 15$$

$$= 5\text{ A}$$

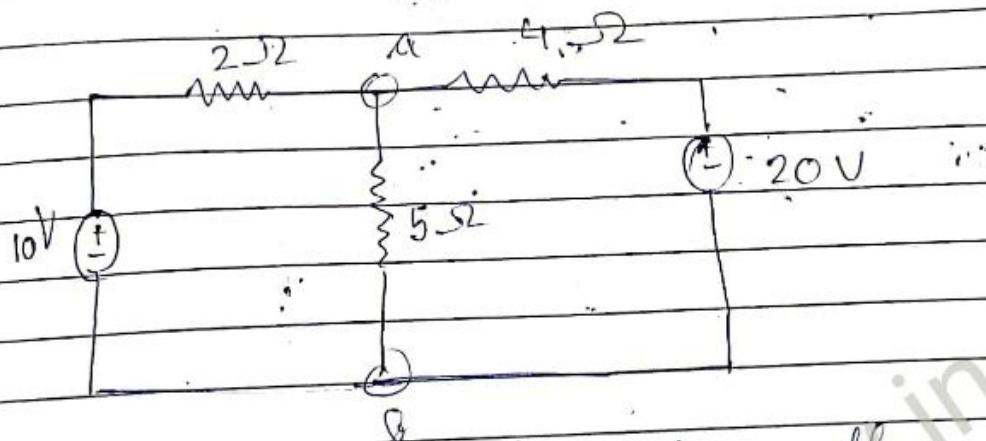
The overall response through the load is

$$I = I' + I''$$

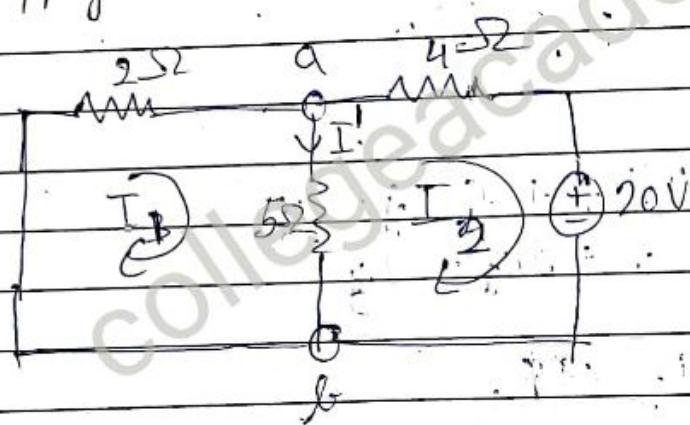
$$= 5 + 1.33$$

$$= 6.33\text{ A}$$

Q Using superposition theorem find out the current across 5Ω resistance.



Current through 5Ω resistance through 20V supply.



$$2I_1 + 5(I_1 - I_2) = 0$$

$$7I_1 - 5I_2 = 0$$

$$4I_2 + 5(I_1 - I_2) = -20$$

$$5I_1 + 9I_2 = -20$$

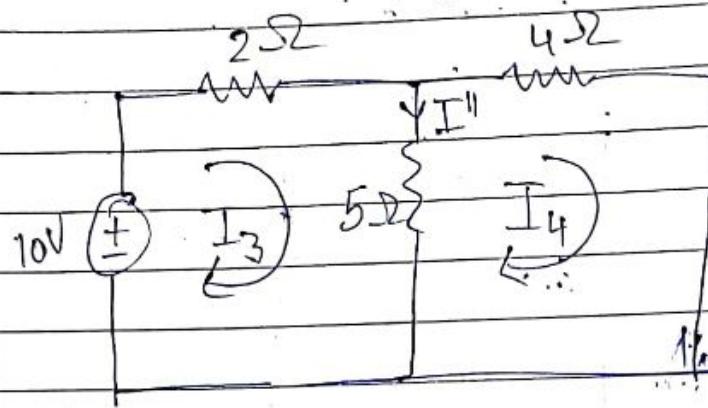
$$I_1 = -5.5 - 2.63 \text{ A}$$

$$I_2 = -7.77 - 3.68 \text{ A}$$

$$I^1 = 1.05 \text{ A}$$

$$I = I^1 + I^{II} = 2.10 \text{ A}$$

Current through 5Ω resistor by 10V supply



$$10V = 2I_3 + 5(I_3 - I_4)$$

$$10V = 7I_3 - 5I_4 \quad \text{--- (3)}$$

$$0 = 4I_4 + 5(I_4 - I_3)$$

$$0 = 4I_4 + 5I_3 - 5I_3$$

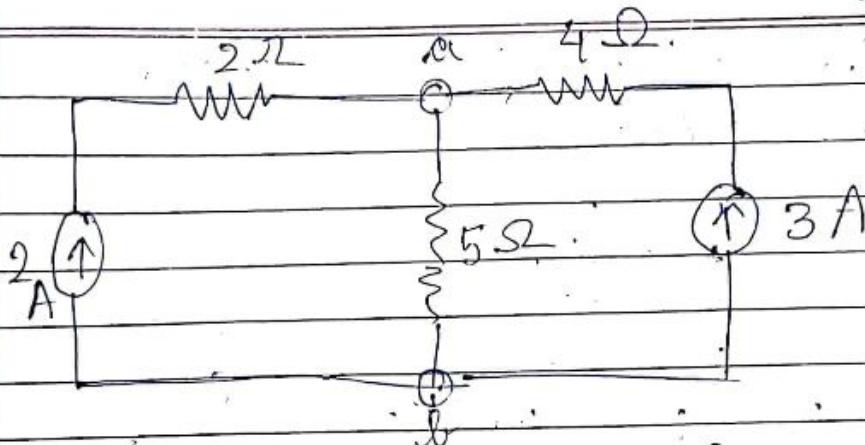
$$0 = -5I_3 + 9I_4$$

~~$I_3 = -0.5 \quad I_3 = 2.3G A$~~

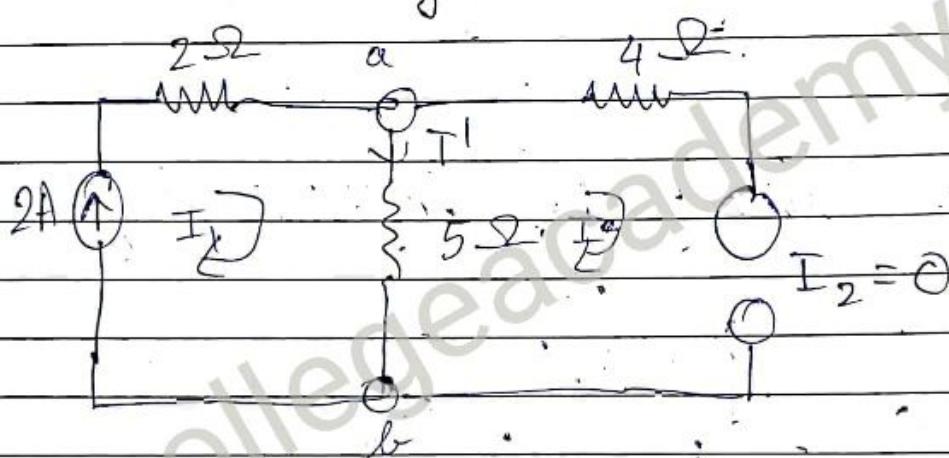
~~$I_4 = -2.77 \quad I_4 = 1.31 A$~~

~~$I'' = 1.05$~~

$$I = I' + I'' = 2.10 A$$



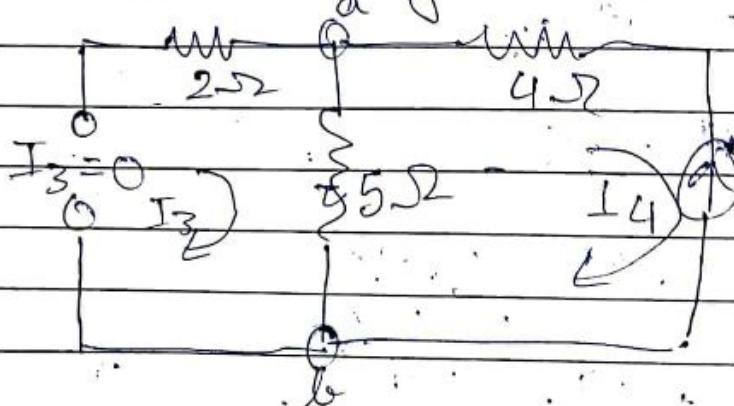
Current through 5Ω resistor through 2Ω .



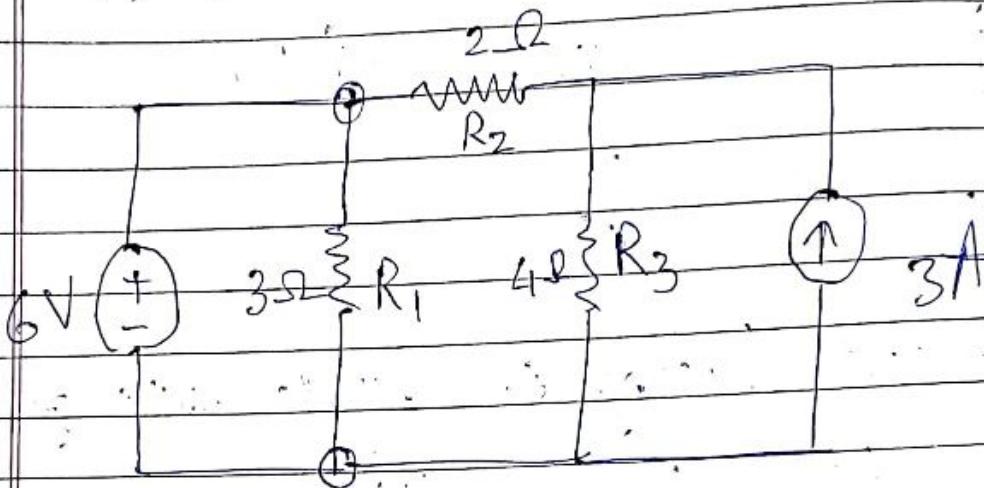
$$I_1 = 2A \quad I_2 = 0$$

$$I^1 = 2$$

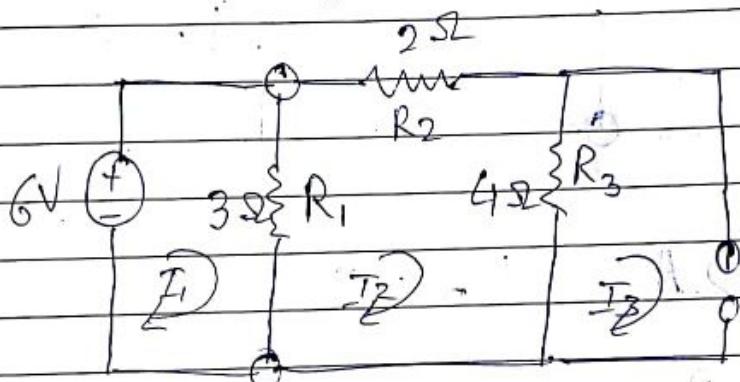
Current through 5Ω by $3A$



Determine current in the resistors
 R_1 , R_2 and R_3



Current through R_1 by 6V supply.



$I_3 = 0$
apply KVL in 1st loop

$$3I_1 - 3I_2 = 6$$

KVL in 2nd loop:

$$3(I_2 - I_1) + 2I_2 + 4(I_2) = 0$$

$$9I_2 - 3I_1 = 0 \quad \text{--- (2)}$$

$$I_1 = 3A$$

$$I_2 = 1A$$

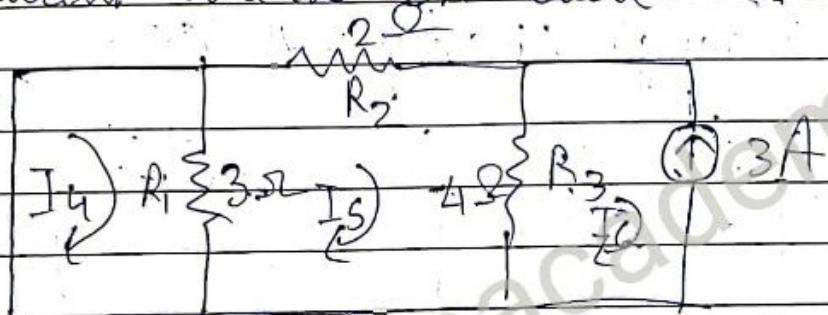
$$I_3 = 0$$

$$I' = I_1 - I_2 = 2A$$

$$I'' = 1A$$

$$I''' = 1A$$

Current due to $3A$ current source :



$$I_6 = -3$$

$$3(I_6 - I_4) + 2I_5 + 4(I_5 + 3) = 0$$

$$I_4 - I_5 = 0$$

$$I_4 = -2A$$

$$I_5 = -2A$$

$$I_6 = -3A$$

$$I'_1 = 0$$

$$I''_1 = -2$$

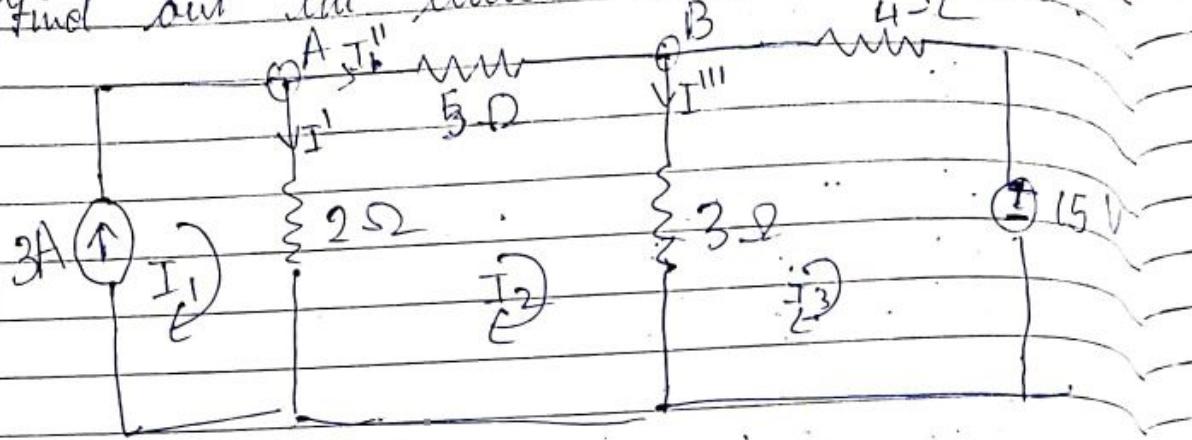
$$I'''_1 = 1$$

overall response across $R_1 \rightarrow I'_1 + I' = 2A$

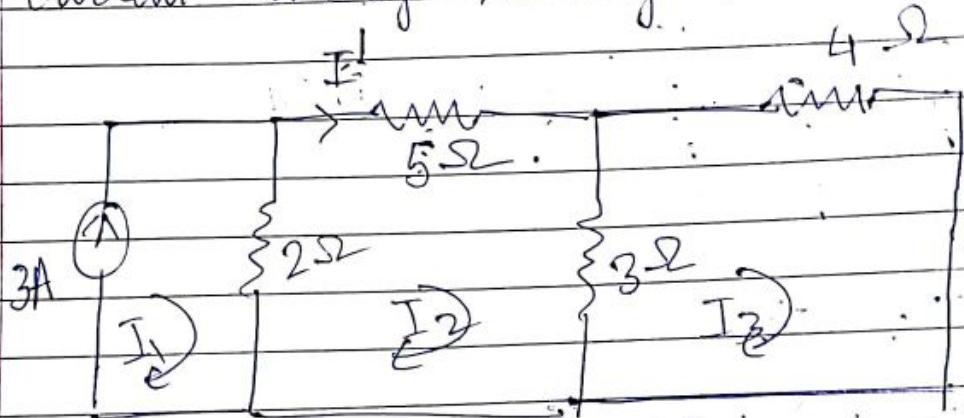
$$R_2 \rightarrow I''_1 + I'' = -1A$$

$$R_3 \rightarrow I'''_1 + I''' = 2A$$

Q) Find out the current across branch AB.



Current through AB by 3A CS.



$$I_1 = 3A$$

$$2(I_2 - I_1) + 5I_2 + 3(I_2 - I_3) = 0$$

$$10I_2 - 6 - 3I_3 = 0$$

$$10I_2 - 3I_3 = 6 \quad \text{--- (1)}$$

$$3(I_3 - I_2) + 4I_3 = 0$$

$$3I_2 + 7I_3 = 0$$

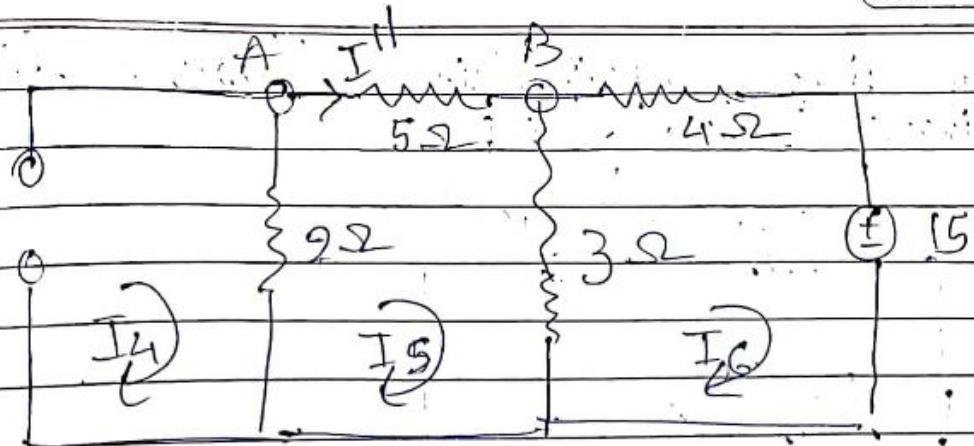
~~$$\frac{I_2}{I_3} = 0.42$$~~

~~$$\frac{I_2}{I_3} = 0.68$$~~

$$I_2 = 0.68 \quad \text{A}$$

$$I_3 = 0.29 \quad \text{A}$$

$$I = 0.68$$



$$I_4 = 0$$

$$2(I_5) + 5I_5 + 3(I_5 - I_6) = 0$$

$$10I_5 - 3I_6 = 0$$

$$3(I_6 - I_5) + 4I_6 = -15$$

$$7I_6 - 3I_5 = -15$$

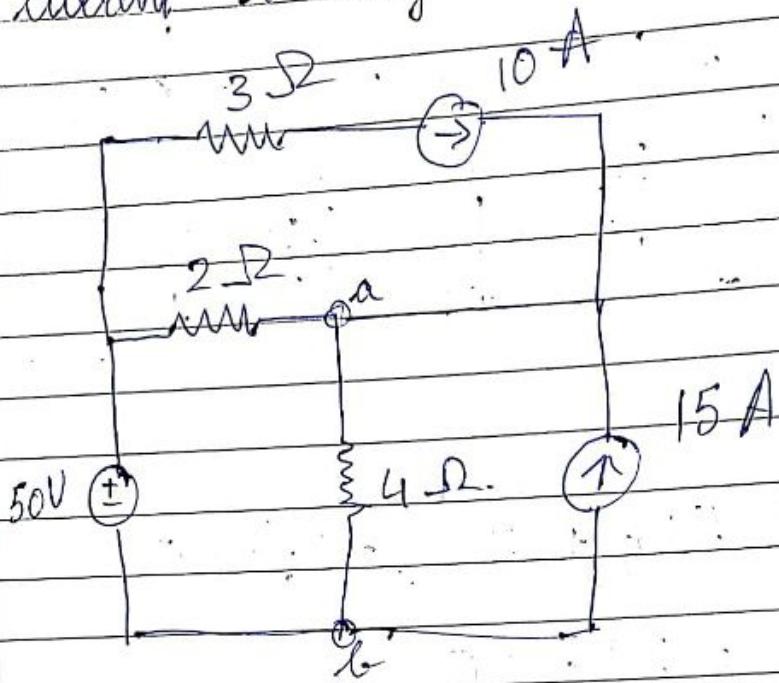
$$I_5 = -0.7$$

$$I_6 = -2.4$$

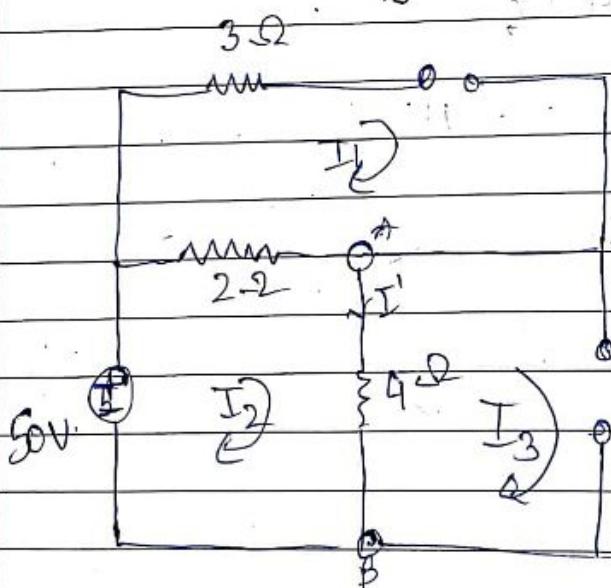
$$I'' = -0.7$$

$$\begin{aligned} I &= I' + I'' \\ &= -0.05 \end{aligned}$$

Q. By using superposition theorem find current through AB



Current through AB by 50 V supply.



$$I_1 = 0 \quad I_3 = 0$$

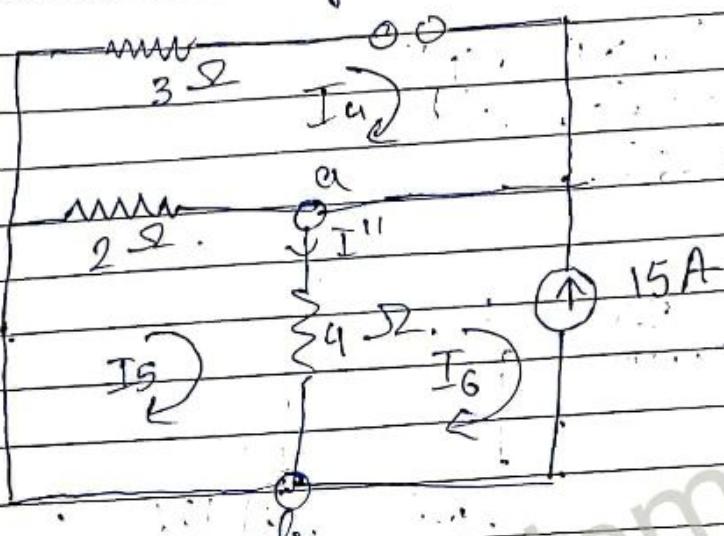
$$50 = 2I_2 + 4I_2$$

$$I_2 = 25\text{A}$$

$$I_2 = \frac{50}{6} \text{A} = 8.33 \text{A}$$

$$I = 8.33 \text{A}$$

Current through 15 A



$$I_6 = -15$$

$$I_4 = 0$$

$$2(I_5 - I_4) + 4(I_5 - I_6) = 0$$

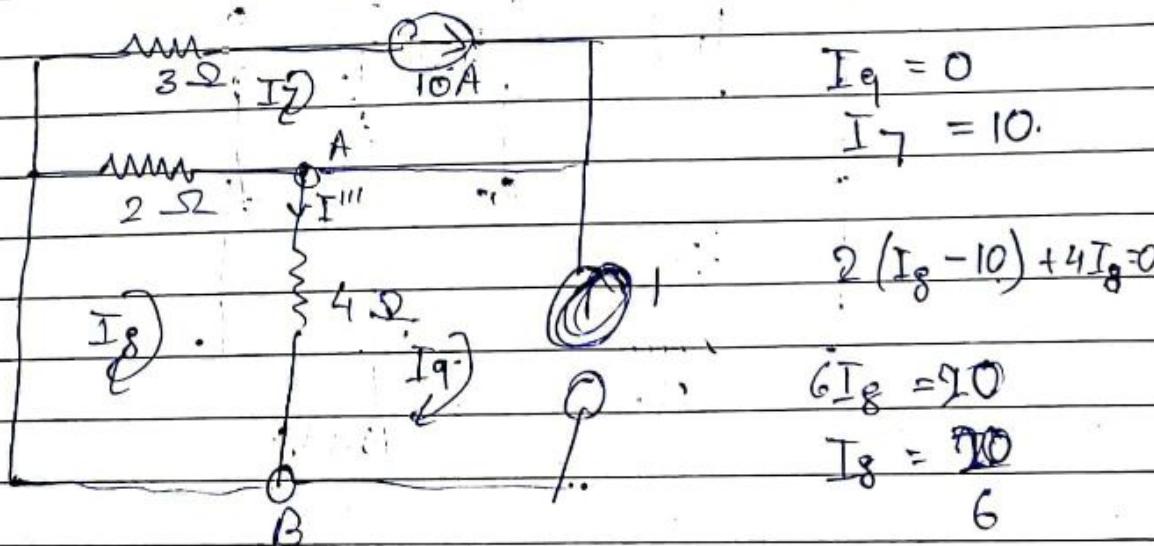
$$2I_5 + 4(I_5 + 15) = 0$$

$$6I_5 + 60 = 0$$

$$I_5 = -10$$

$$I'' = 5 \text{ A}$$

Current due to 10 A current source.



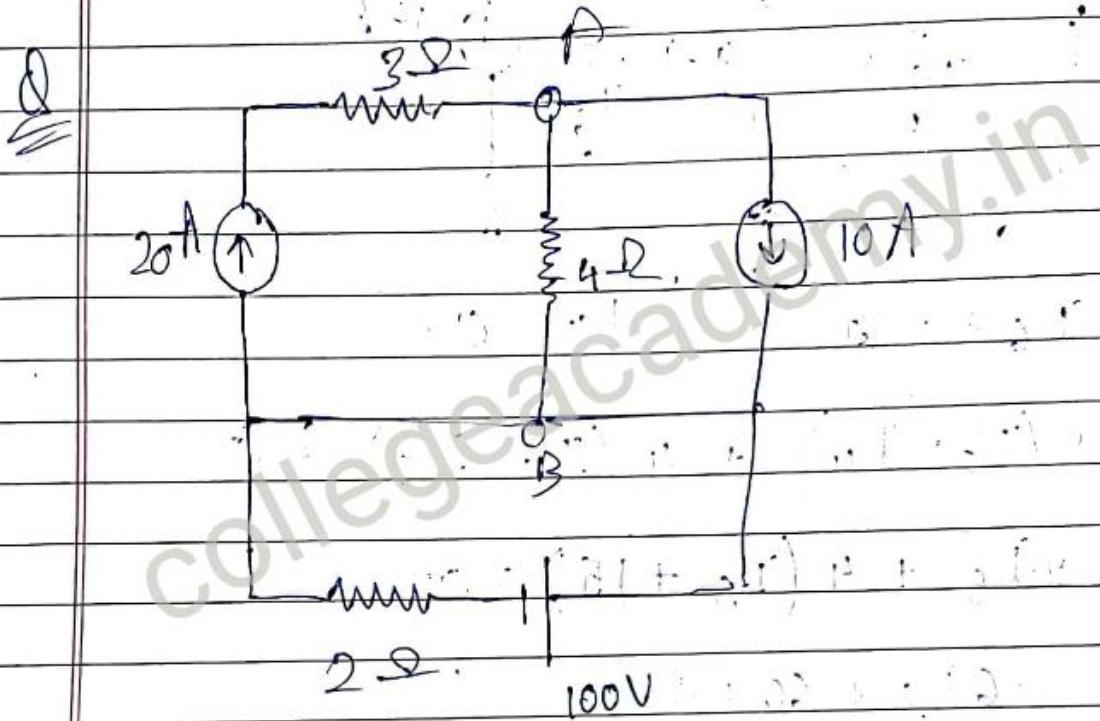
$$I = 14 \cancel{A}$$

$$I''' = 3.33$$

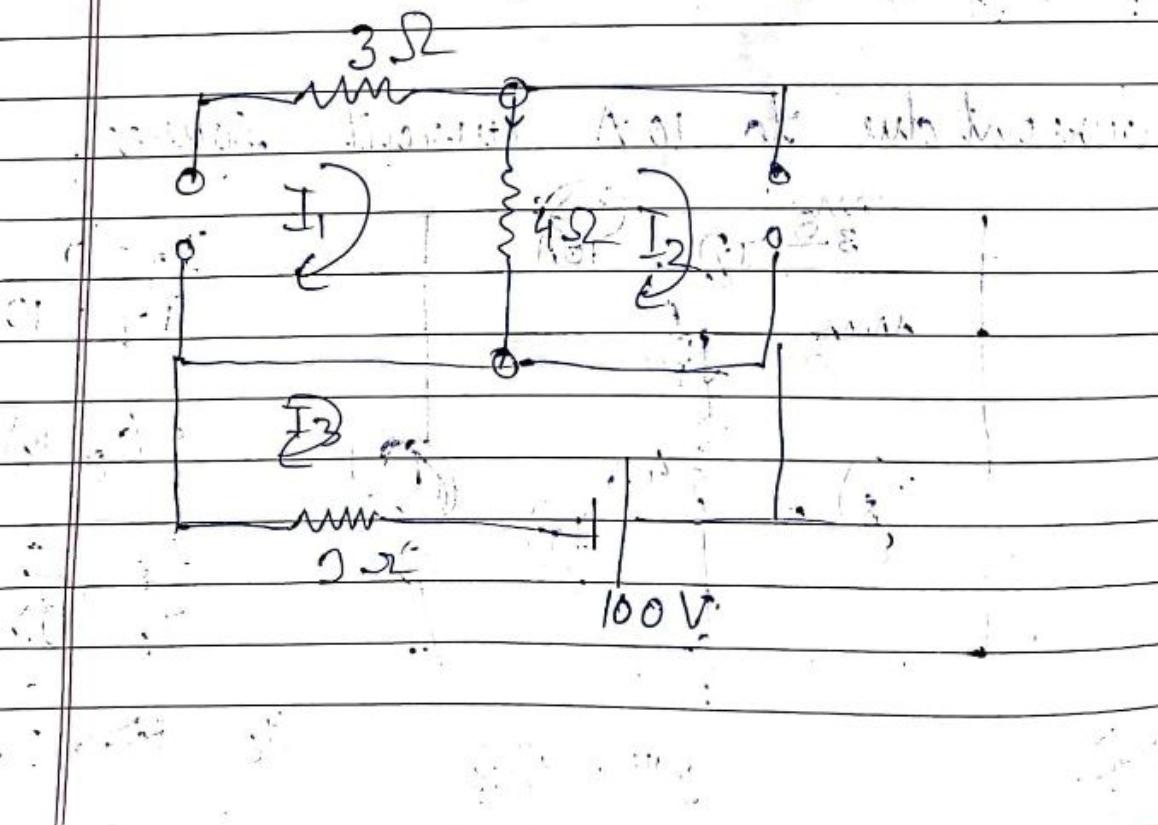
$$I_8 = 3.33$$

Total response

$$\begin{aligned} I &= I' + I'' + I''' \\ &= 8.33 + 5 + 3.83 \\ &= 16.66 \end{aligned}$$



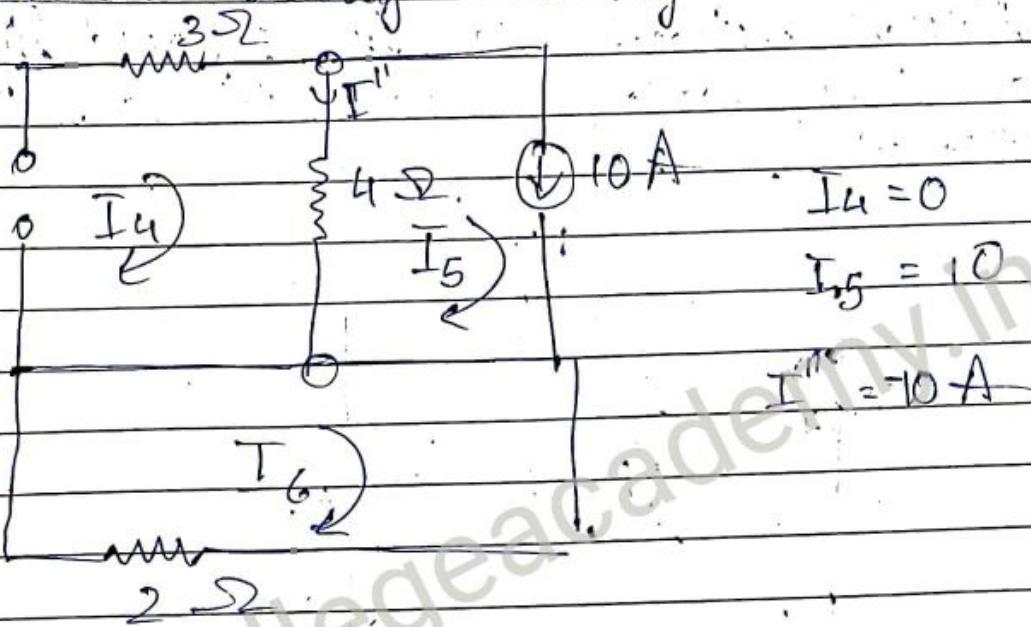
current through A.B by 100 V supply.



$$I_2 = 0$$

$$I' = 0.$$

Current through AB by $10A$ current source

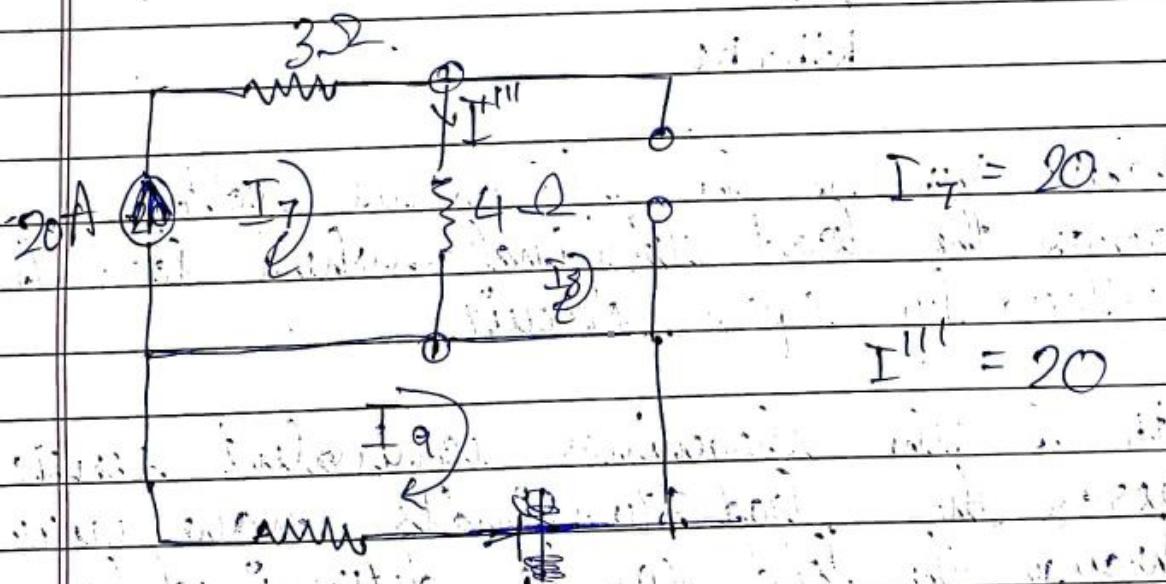


$$I_4 = 0$$

$$I_5 = 10$$

$$I'' = -10A$$

Current through AB by $20A$ e.s



$$I_7 = 20$$

$$I''' = 20$$

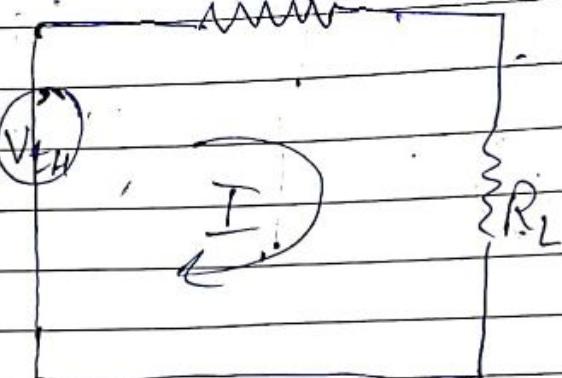
$$\text{Total response} = I' + I'' + I'''$$

$$= 100A$$

Thevenines Theorem

According to Thevenines Theorem... any linear bilateral network can be replaced by a single voltage source with a series resistance.

R_{th}



$$I = \frac{V_{th}}{R_{th} + R_L}$$

where V_{th} is the Thevenines voltage across the load terminal when load is replaced by open circuit.

R_{th} is the Thevenines equivalent resistance across the load terminals, now current through the load can be determined by connecting the load terminal across the Thevenines equivalent resistance.

- Procedure for V_{th}
- 1) Mark the load terminal
 - 2) Replace load terminal with open circuit and mark open circuit voltage with V_{oc}
 - 3) By using KVL or KCL determine (V_{oc} , V_{th})

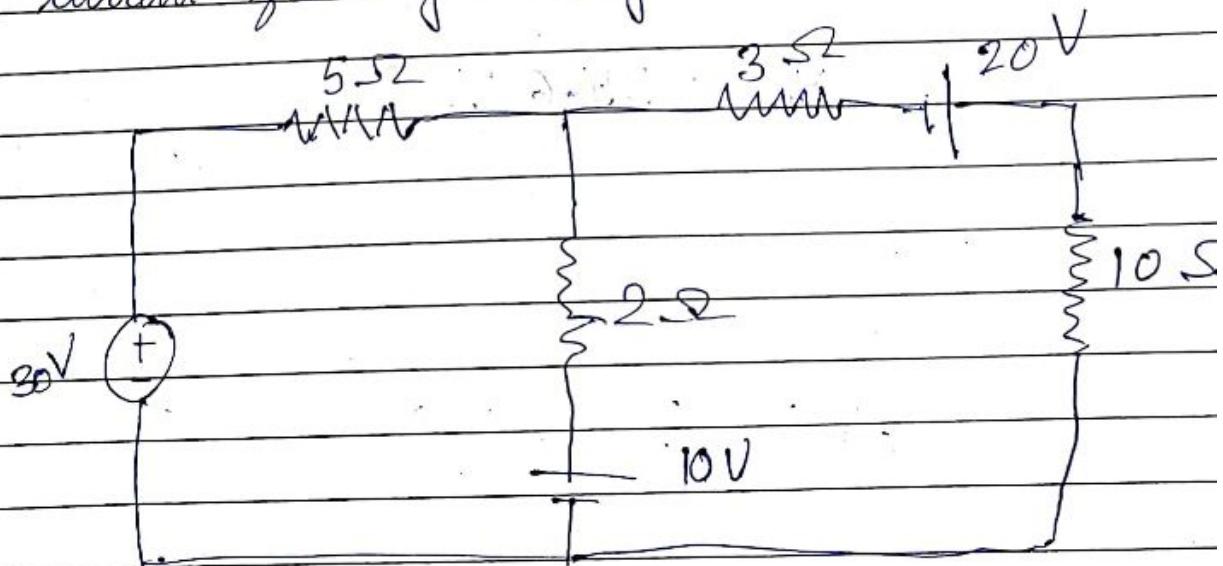
Calculation for R_{th}

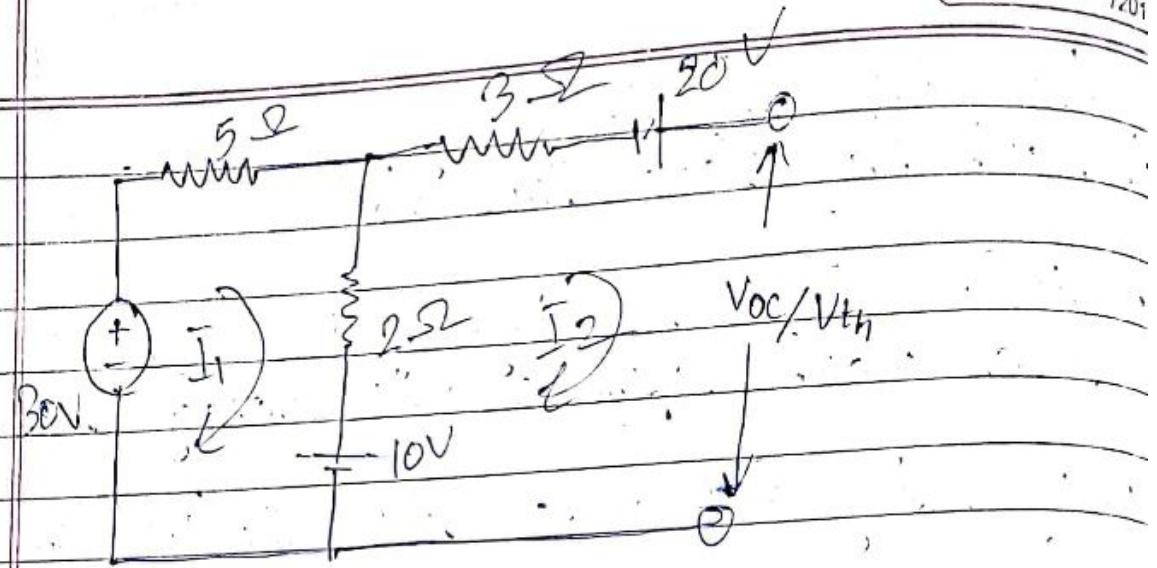
- 1) Replace load terminal with open circuit.

- 2) Replace all independent voltage sources with short circuit and all current sources with open circuit.

- 3) Find out equivalent resistance R_{eq} seen from open circuit terminal.

- Q) By using Thevenin's theorem find out the current flowing through 10Ω resistance





$$I_2 = 0$$

Apply KVL in I loop:

$$-30 + 5I_1 + 2I_1 + 0 = 0$$

$$7I_1 = 20$$

$$I_1 = 2.86 \text{ A}$$

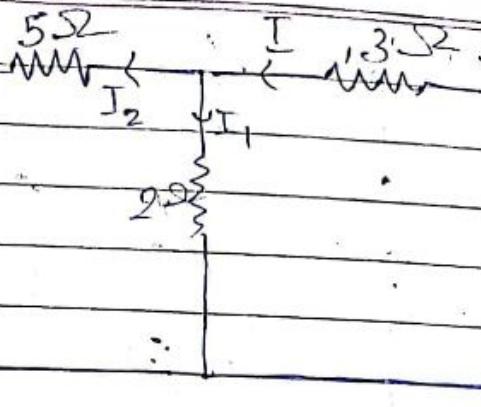
Apply KVL in II Loop

$$-2I_1 - 20 + V_{oc} - 10 = 0$$

$$-5 \cdot 6 - 30 + V_{oc} = 0$$

$$V_{oc} = 35.6 \text{ V}$$

$$\frac{I_1}{5\Omega} = \frac{7}{7\Omega} = 10.69$$



$$R_{th} = 6 \Omega$$

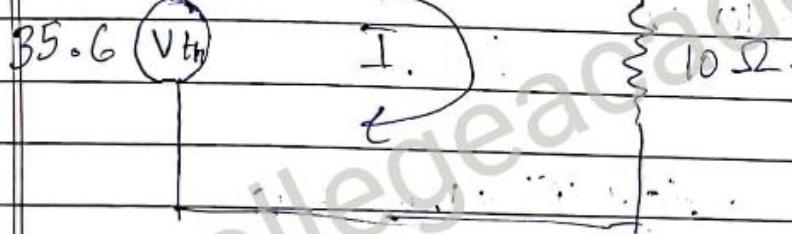
$$\frac{1}{3} + \frac{1}{2} = \frac{1}{R}$$

$$R_{th} = 6 \Omega$$

$$R = \frac{6}{5} + 5$$

$$= \frac{6+25}{5}$$

$$= \frac{31}{5} \Omega$$

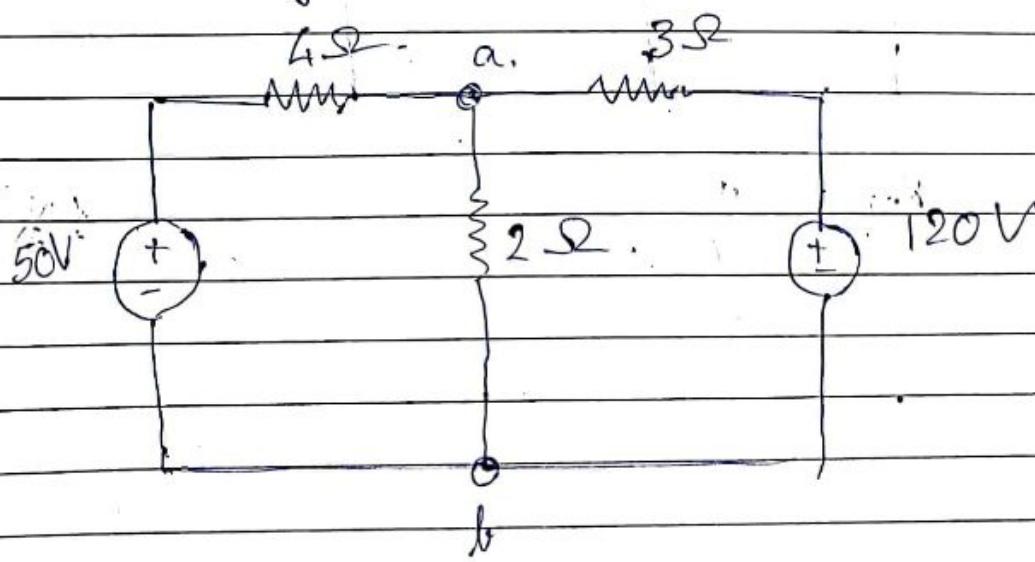


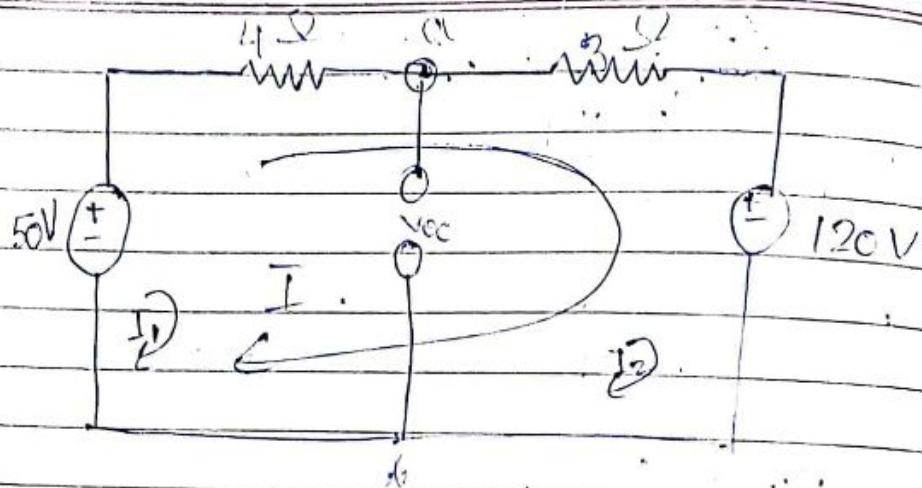
$$I = \frac{V_{th}}{R_{th} + R_L}$$

$$R_{th} + R_L$$

$$I = 0.19 A$$

Q) By using Thévenin's theorem. Find out the current through 2 Ω resistor.





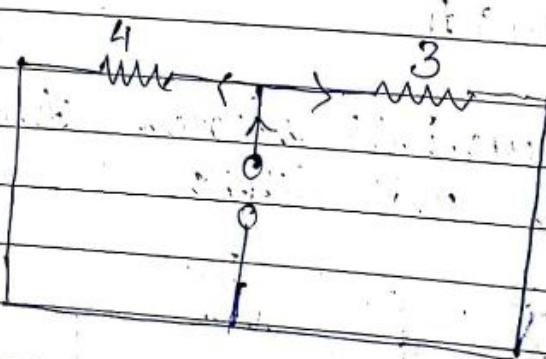
$$50 - 120 = 4I + 3I$$

$$-70 = 7I$$

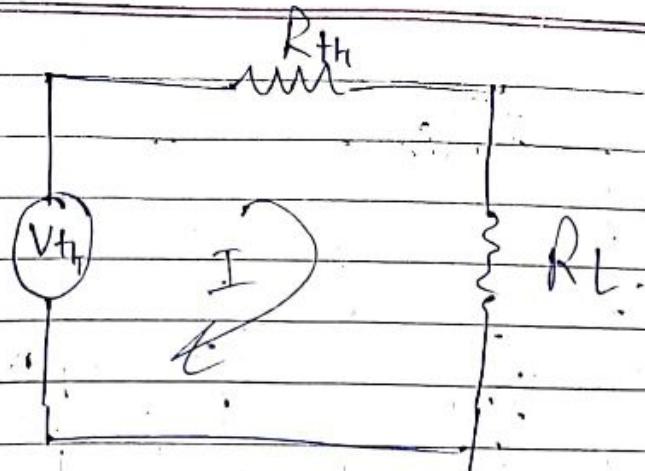
$$I = -10 \text{ A}$$

$$50 + \cancel{4I} - 50 + 4I + VOC = 0$$

$$120 = 3I \quad VOC = 90 \text{ V}$$



$$Req = \frac{12}{7}$$

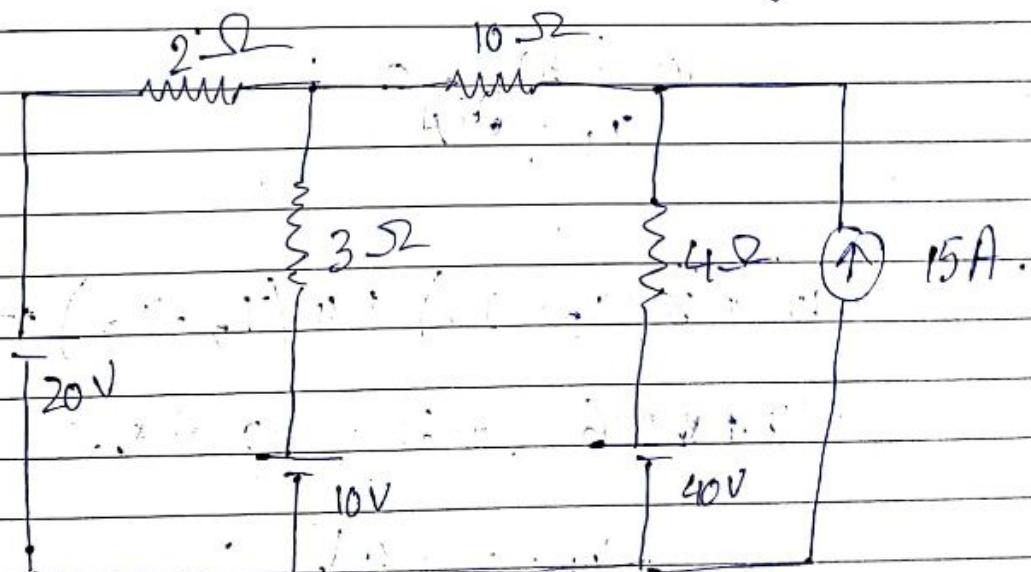


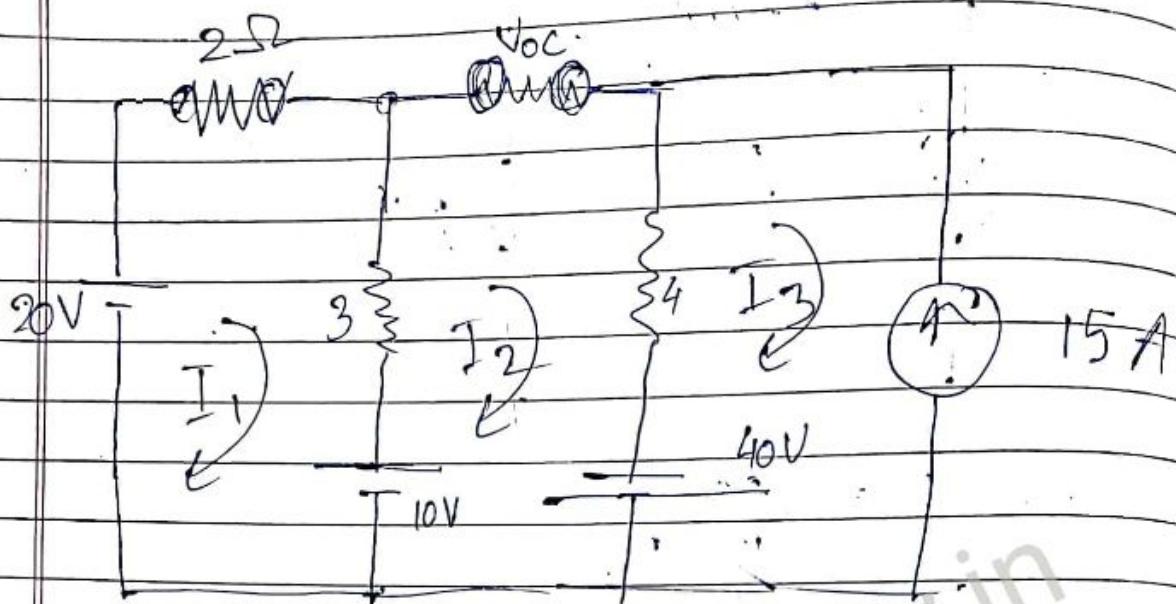
$$I = \frac{90}{\frac{12+2}{7}}$$

$$= \frac{90 \times 7}{26}$$

$$= 24.3 \text{ A}$$

Q By using Thevenin's theorem find out the current across $10\text{-}\Omega$ in given circuit.





$$I_2 = 0$$

$$I_3 = -15 \text{ A}$$

$$20 + 2I_1 + 3I_1 - 10 = 0$$

$$10 + 5I_1 = 0$$

$$I_1 = -2 \text{ A}$$

$$-10 + 3(I_2 - I_1) + 4(I_2 - I_3) \div 40 = 0$$

$$-10 + 3(-6) + 60 - 40 \neq V_{oc} = 0$$

$$V_{oc} = -4 \text{ V}$$

2Ω

Voc. 0

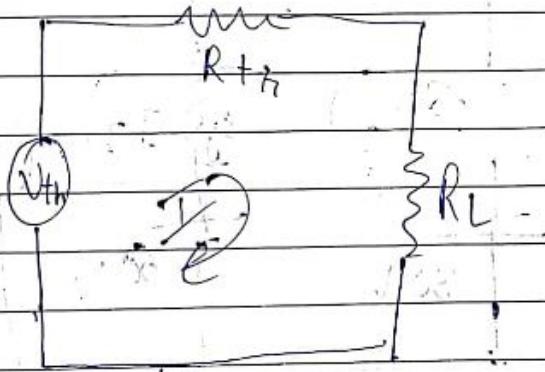
3Ω

4Ω

$$R_{2,3} = \frac{6}{5}$$

$$R_{2,3,4} = \frac{6}{5} + 4$$

$$= \frac{26}{5} = 5.2$$



$$I = -4$$

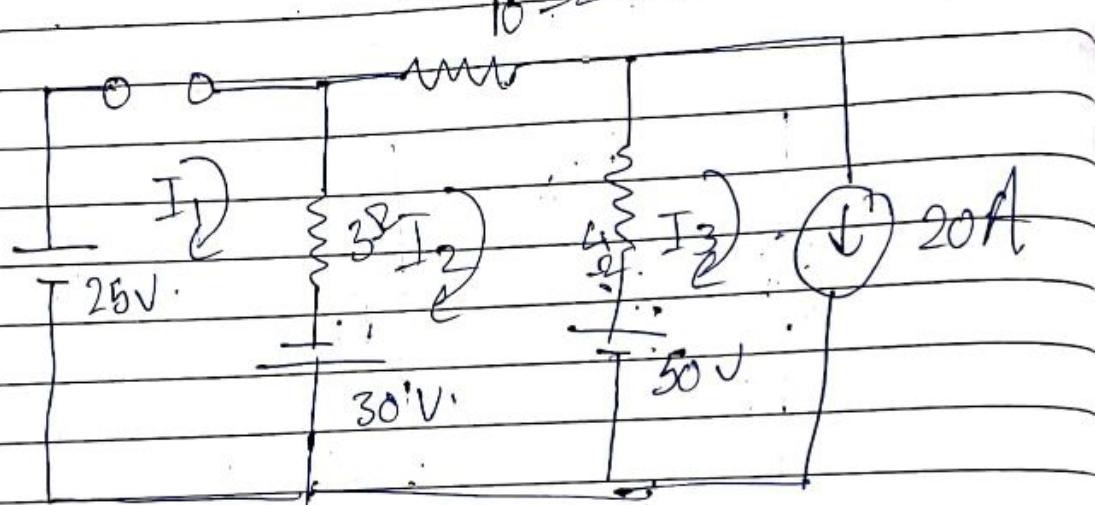
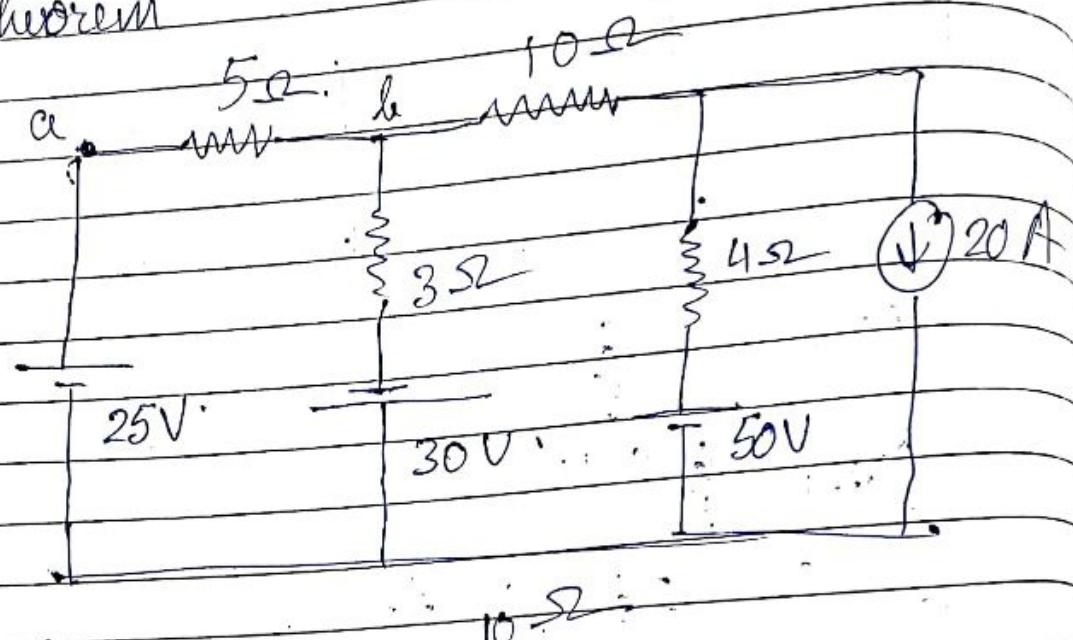
$$5.2 + 10$$

$$= -4$$

$$15.2$$

$$= -0.26 A$$

Q Find out the voltage across 5Ω resistance with the help of Thévenin's theorem



$$I_1 = 0 \quad I_3 = 20A$$

$$-80 - 50 = 3I_2 + 10I_2 + 4(I_2 - 20)$$

$$-80 = 17I_2 - 80$$

$$\frac{-60}{17} = I_2$$

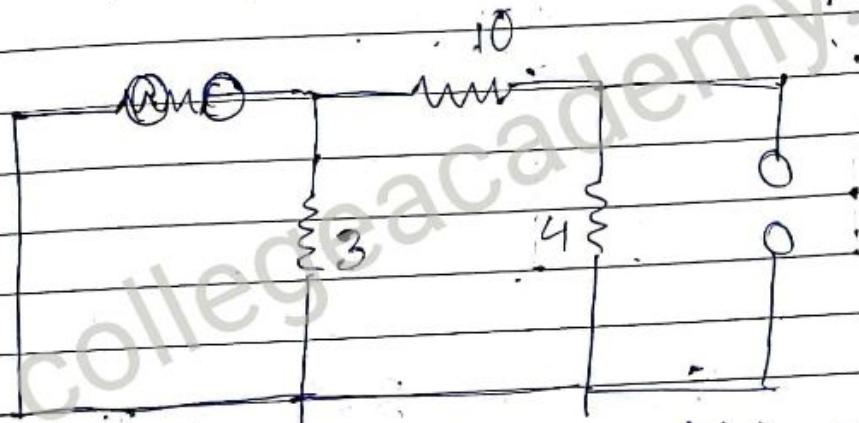
$$-30 - 50 = 3(I_2) + 10 \cdot I_2 + 4(I_2 - 20)$$

$$-80 = 17I_2 - 80$$

$$\therefore I_2 = 0$$

$$25 + 30 + V_{oc} = 3(I_1 - I_2) + V_{oc}$$

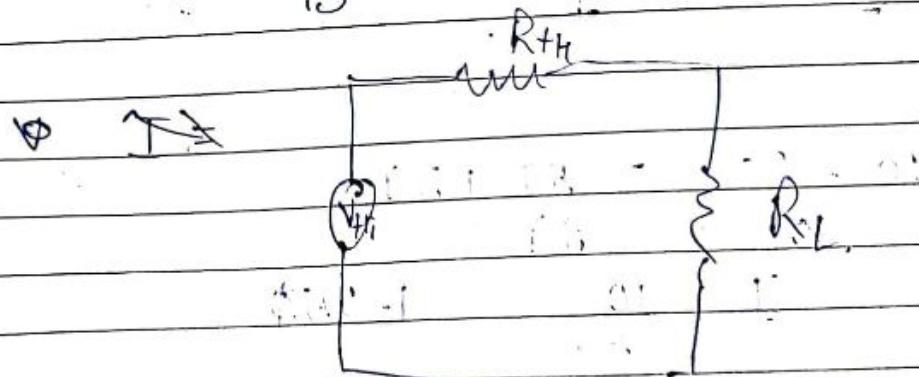
$$V_{oc} = 55$$



$$R_{10,3} = \frac{30}{13}$$

$$R_{eq} = \frac{30 + 4}{13}$$

$$= \frac{82}{13} = 6.30$$



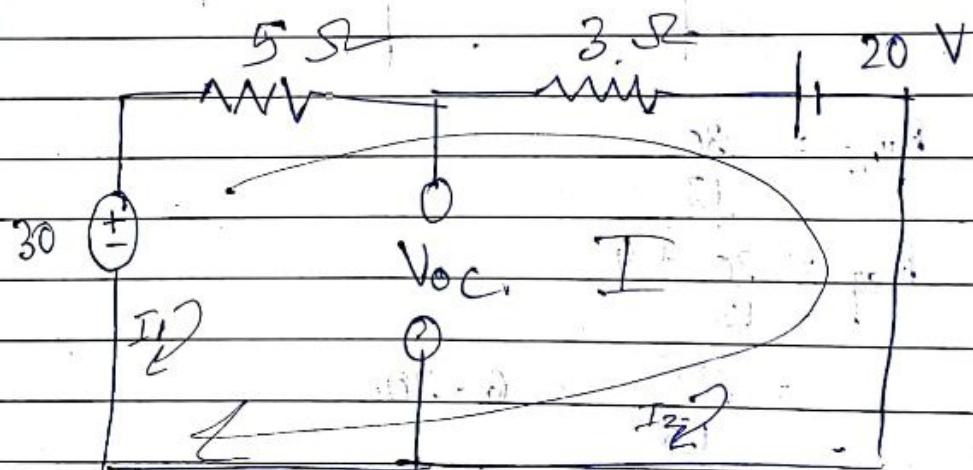
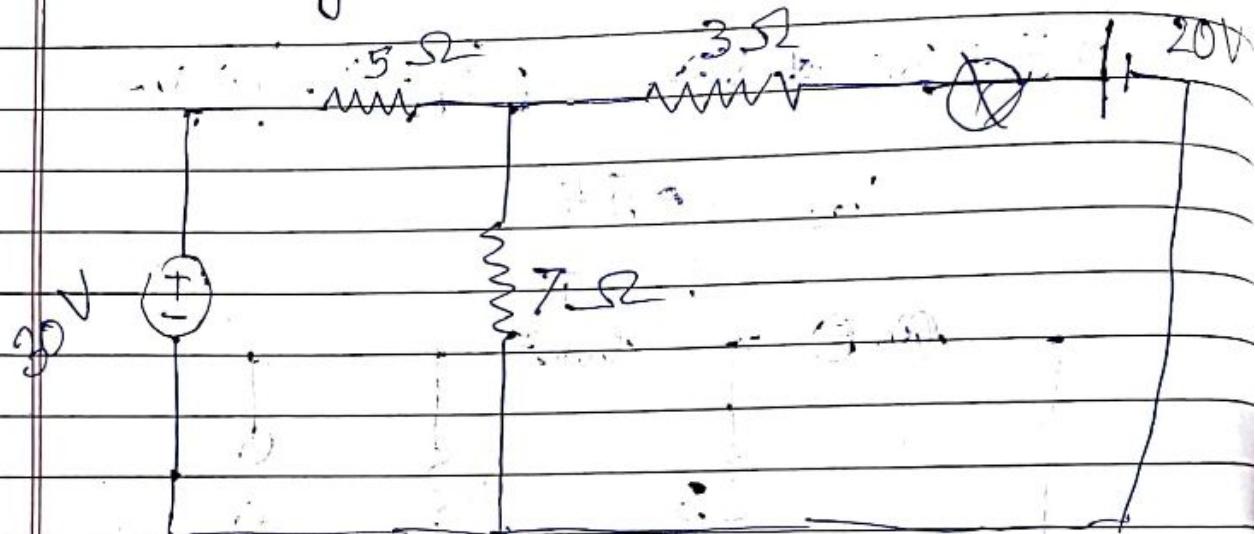
$$I = \frac{55}{5 + 6.3} = 4.867256637 A$$

$$V_L = I \times R_L$$

$$= 4.867 \times 5$$

$$= 24.3 \text{ V}$$

Q Find out voltage across $7\text{-}\Omega$ resistance in the given circuit.



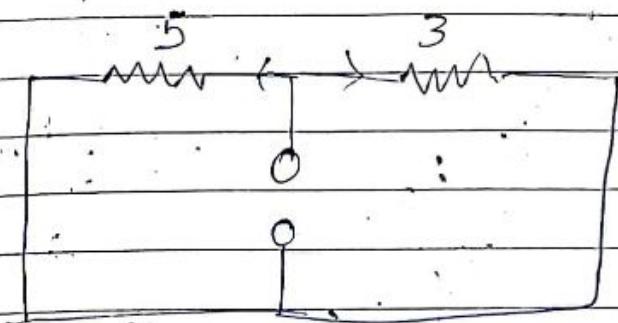
$$30 - 20 = 5I + 3I$$

$$10 = 8I$$

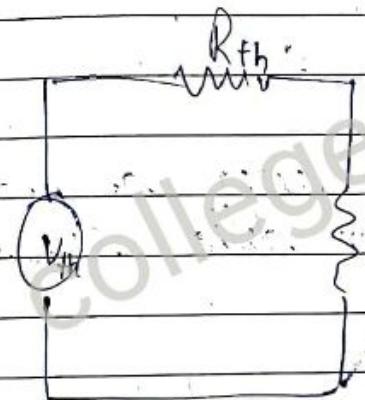
$$I = \frac{10}{8} = 1.25$$

$$30 = 5I_p + \Delta V_o$$

$$24.75 = \Delta V_o$$



$$R_{th} = \frac{15}{8} = 1.875$$



$$I = 23.75$$

$$1.875 + 7$$

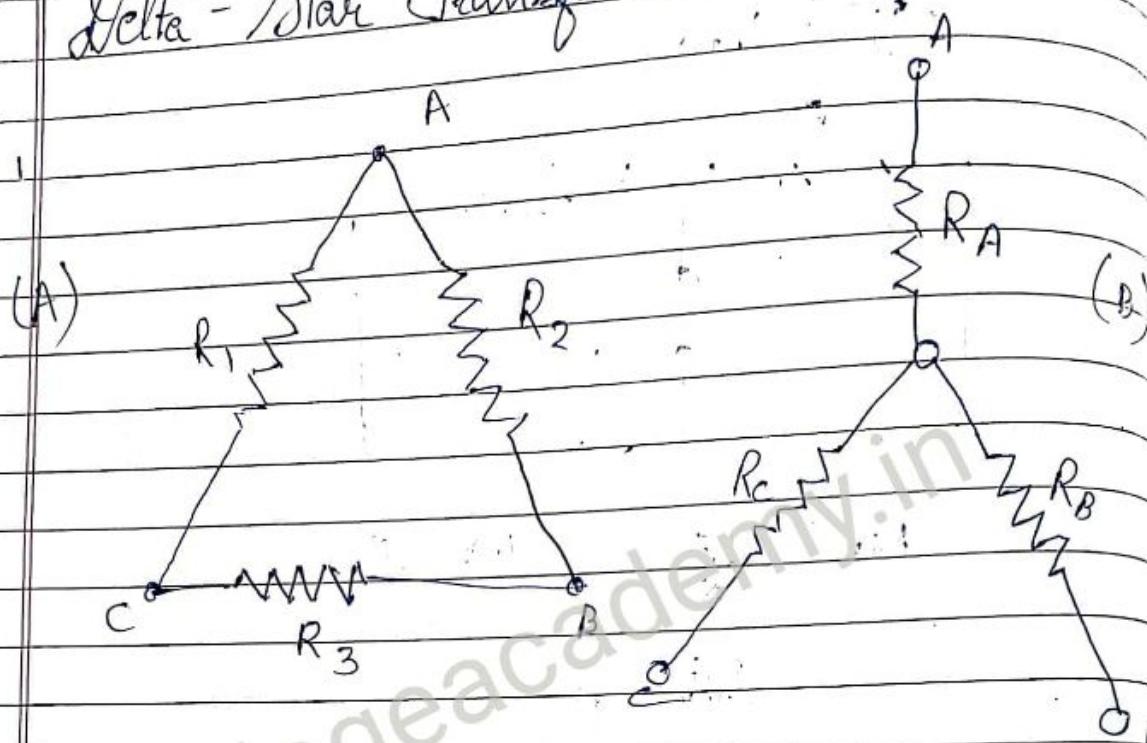
$$\approx 2.676$$

$$V = I \cdot R$$

(B)

$$\approx 18.073$$

Delta - Star Transformation

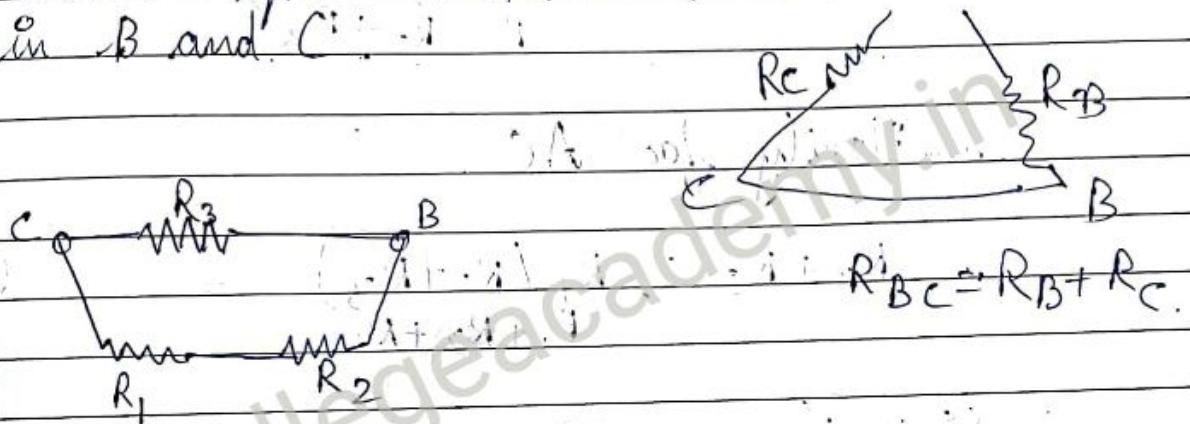


- 1) When 3 resistances connected as shown in fig. (A) are said to be delta connected or mesh connected.
- 2) When 3 resistances are connected as shown in fig (B) are said to star connected or Y connected.
- 3) If the nodes A, B and C at which the two sets of resistances are connected are part of a large network than it is possible to assign values to the two sets of resistances so that they have exactly the same effect on the network.
- 4) Since delta connected resistances are part of a network it is possible to substitute them by the star connected

ones and vice-versa.

5) The replacement of delta by equivalent star system is known as delta star transformation.

The two systems will be equivalent or identical if the resistances measured between any pair of lines is same in both of the systems when the third line is open. Hence resistance will be R_B in B and C.



$$R_{BC} = R_3 \parallel (R_1 + R_2)$$

In Δ system $R_3 \parallel (R_1 + R_2)$

$$R_{BC} = \frac{R_3(R_1 + R_2)}{R_1 + R_2 + R_3}$$

In Y system $R_B + R_C$

$$R_{BC} = R_B + R_C$$

Since the two system are identical resistances measured betⁿ terminal must be equal.

Hence resistances betⁿ terminal B and must be equal for Y as well as Δ system.

$$R_B + R_C = \frac{R_3(R_1 + R_2)}{R_1 + R_2 + R_3} \quad (1)$$

Similarly for AC

$$R_A + R_C = \frac{R_1(R_2 + R_3)}{R_1 + R_2 + R_3} \quad (2)$$

Similarly for AB

$$R_A + R_B = \frac{R_2(R_1 + R_3)}{R_1 + R_2 + R_3} \quad (3)$$

by adding all eqⁿ

$$2(R_A + R_B + R_C) = 2(R_1R_3 + R_1R_2 + R_2R_3) \\ R_1 + R_2 + R_3$$

$$\Rightarrow R_A + R_B + R_C = \frac{R_1R_3 + R_1R_2 + R_2R_3}{R_1 + R_2 + R_3}$$

Now subtracting 1, 2, 3. from 4 ...

$$(4) - (1)$$

$$R_A := \frac{R_1 R_2}{R_1 + R_2 + R_3} \quad (5)$$

$$(4) - (2)$$

$$R_B := \frac{R_1 R_3}{R_1 + R_2 + R_3} \quad (6)$$

$$(4) - (3)$$

$$R_C = \frac{R_2 R_3}{R_1 + R_2 + R_3} \quad (7)$$

Star-Delta Transformation:

The replacement of star system by equivalent delta system is known star delta transformation

Multiplying $5 \times 6 = 6 \times 7 = 7 \times 5$

$$(5) \times (6)$$

$$R_A R_B = \frac{R_1 R_2^2 R_3}{(R_1 + R_2 + R_3)^2} \quad (8)$$

$$(6) \times (7)$$

$$R_B R_C = \frac{R_1 R_2 R_3^2}{(R_1 + R_2 + R_3)^2} \quad (9)$$

$$(7) \times (5)$$

$$R_A R_C = \frac{R_1^2 R_2 R_3}{(R_1 + R_2 + R_3)^2} \quad (10)$$

Addition of A, B & C

$$R_A R_B + R_B R_C + R_C R_A = \frac{R_1 R_2 R_3^2}{(R_1 + R_2 + R_3)^2} + \frac{R_1 R_2^2 R_3}{(R_1 + R_2 + R_3)^2} + \frac{R_1^2 R_2 R_3}{(R_1 + R_2 + R_3)^2}$$

$$R_A R_B + R_B R_C + R_C R_A = \frac{R_1 R_2 R_3 (R_1 + R_2 + R_3)}{(R_1 + R_2 + R_3)^2}$$

$$R_A R_B + R_B R_C + R_C R_A = \frac{R_1 R_2 R_3}{R_1 + R_2 + R_3} \quad \textcircled{8}$$

Now dividing $\textcircled{8}$ by $\textcircled{5}, \textcircled{6}, \textcircled{7}$

$$\textcircled{8} \div \textcircled{5}$$

$$R_3 = \frac{R_B + R_C + R_B R_C}{R_A} \quad \textcircled{9}$$

$$\textcircled{8} \div \textcircled{6}$$

$$R_1 = \frac{R_A + R_C + R_A R_C}{R_B} \quad \textcircled{10}$$

$$\textcircled{8} - \textcircled{7}$$

$$R_2 = \frac{R_A + R_B + R_A R_B}{R_C} \quad \textcircled{11}$$