

hw_1

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Question 1(a)

```
divide <- function(d,a) {  
  if (a==0) stop("division by zero is undefined.")  
  if (d<0 || a<0) stop("divide() only works for positive 'a' and 'd'.")  
  quotient <- 0  
  while (a<=d){  
    d = d - a  
    quotient = quotient + 1  
  }  
  c(q = quotient, r = d)  
}  
divide(22, 7)
```

```
## q r  
## 3 1
```

```
22 %/% 7
```

```
## [1] 3
```

```
22 %% 7
```

```
## [1] 1
```

```
divide(22, 0)
```

```
## Error in divide(22, 0): division by zero is undefined.
```

```
divide(-22,7)
```

```
## Error in divide(-22, 7): divide() only works for positive 'a' and 'd'.
```

```
divide(21,7)
```

```
## q r  
## 3 0
```

Question 1(b)

```
mod <- function(d,a) {  
  a<- divide(d,a)  
  unname(a[2])  
}  
mod(23, 7)
```

```
## [1] 2
```

```
mod(21,7)
```

```
## [1] 0
```

Question 1(c)

Question 1(d)

```
is.divisor <- function(d,a) {  
  if (a==0){  
    rem <- 1  
  }  
  else rem <- mod(abs(d),abs(a))  
  rem == 0  
}  
is.divisor(6, 3)
```

```
## [1] TRUE
```

```
is.divisor(6, 4)
```

```
## [1] FALSE
```

```
is.divisor(-6, 3)
```

```
## [1] TRUE
```

```
is.divisor(6, 0)
```

```
## [1] FALSE
```

Question 1(e)

```
divisors <- function(d) {
  if (d==0) stop("Input cannot be zero")
  num <- c(-abs(d):abs(d))
  check <- lapply(num, is.divisor, d=d)
  num[unlist(check)]
}
divisors(7)
```

```
## [1] -7 -1 1 7
```

```
divisors(18)
```

```
## [1] -18 -9 -6 -3 -2 -1 1 2 3 6 9 18
```

Question 1(f)

```
gcd_naive <- function(a,b) {
  if ( a!=0 && b!=0){
    div_a <- divisors(a)
    div_b <- divisors(b)
    common <- intersect(div_a, div_b)
    gcd <- max(common)
  }
  else{
    gcd <- max(abs(a),abs(b))
  }
  gcd
}
gcd_naive(64, 28)
```

```
## [1] 4
```

```
gcd_naive(64, -28)
```

```
## [1] 4
```

```
gcd_naive(64,0)
```

```
## [1] 64
```

```
gcd_naive(-64,0)
```

```
## [1] 64
```

```
gcd_naive(0,0)
```

```
## [1] 0
```

Question 1(g)

```
is.prime_naive <- function(p) {  
  div <- divisors(p)  
  length(div) == 4  
}  
is.prime_naive(5)
```

```
## [1] TRUE
```

```
is.prime_naive(20)
```

```
## [1] FALSE
```

```
is.prime_naive(1)
```

```
## [1] FALSE
```

```
is.prime_naive(-3)
```

```
## [1] TRUE
```

Question 1(h)

```
naive_seive <- function(n) {  
  num <- c(1:n)  
  check <- lapply(num, is.prime_naive)  
  num[unlist(check)]  
}  
naive_seive(100)
```

```
## [1] 2 3 5 7 11 13 17 19 23 29 31 37 41 43 47 53 59 61 67 71 73 79 83 89 97
```

Question 1(i)

```
eratosthenes_sieve <- function(n) {  
  
}
```

Question 1(j)

```
is.relprime <- function(a, b) {  
  gcd_naive(a, b) == 1  
}  
is.relprime(9, 16)
```

```
## [1] TRUE
```

```
is.relprime(6, 21)
```

```
## [1] FALSE
```

Question 1(k)

```
gcd_recursive <- function(a, b, quiet=TRUE) {  
  if (quiet == FALSE) {  
    cat("(" , a , " , " , b , ")\n")  
  }  
  if (a==0 && b==0) 0  
  if (a==0 || b==0){  
    max(abs(a),abs(b))  
  }  
  else{  
    c <- abs(min(a,b))  
    d <- abs(max(a,b))  
    d <- mod(d,c)  
    gcd_recursive(c,d, quiet)  
  }  
}  
gcd_recursive( 64, 28, quiet = FALSE)
```

```
## ( 64 , 28 )  
## ( 28 , 8 )  
## ( 8 , 4 )  
## ( 4 , 0 )
```

```
## [1] 4
```

```
gcd_recursive(64,-28)
```

```
## [1] 4
```

```
gcd_recursive( 64, 0)
```

```
## [1] 64
```

```
gcd_recursive(-64, 0)
```

```
## [1] 64
```

```
gcd_recursive( 0, 0)
```

```
## [1] 0
```

Question 1(l)

```
gcd <- function(a, b, quiet = TRUE) {  
}
```

Question 2(a)

```
inv <- function(b, x0 = 10^-(ceiling(log10(abs(b)))), tol = sqrt(.Machine$double.eps),  
               message = FALSE) {  
  if (b==0) stop("zero has no multiplicative inverse")  
  dif <- 1 #initilaizing a difference > tol  
  if (b > 0){ #for positive input b  
    while (dif > tol){  
      y <- x0 #setting the intial x iteration to y  
      x0 <- x0 * (2 - b * x0)  
      dif <- x0 - y #subtracting the newly iteration from the previous iteration  
      if (message) print(x0) #for message=TRUE  
    }  
    x0  
  }  
  else { #for negative input b  
    b <- -b  
    while (dif > tol){  
      y <- x0  
      x0 <- x0 * (2 - b * x0)  
      dif <- x0 - y  
    }  
    -x0  
  }  
}
```

```
inv(1000, message = TRUE)
```

```
## [1] 0.001
```

```
## [1] 0.001
```

```
inv(-1000)
```

```
## [1] -0.001
```

```
inv(0)
```

```
## Error in inv(0): zero has no multiplicative inverse
```

```
divide_real_fast <- function(a, b) {
  if (b==0) stop("division by zero is undefined.")
  a * inv(b)
}
```

```
divide_real_fast(22, 7)
```

```
## [1] 3.142857
```

```
divide_real_fast(2, -4)
```

```
## [1] -0.5
```

```
divide_real_fast(2, 0)
```

```
## Error in divide_real_fast(2, 0): division by zero is undefined.
```

```
divide_fast <- function(a, d){
  divide(a,d)
  c <- zapsmall(divide_real_fast(a,d))
  floor_c <- floor(c)
  t <- c - floor_c
  q <- floor_c
  r <- round(d * t) #computing remainder and rounding
  c(q = q, r = r)
}

a <- 1e8; d <- 2
divide(a, d)
```

```
##      q      r
## 5e+07 0e+00
```

```
divide_fast(a, d)
```

```
##      q      r
## 5e+07 0e+00
```

```
a %/% d
```

```
## [1] 5e+07
```

```
a %% d
```

```
## [1] 0
```